

26.03.2020 Prim's Algorithm

(a) Pseudocode

procedure prim ( $G, w$ )

Input: A connected undirected graph  $G$  with edge weights  $w_e$ .  $\rightarrow = (V, E)$

Output: A minimum spanning tree defined by the array prev.

for all  $u \in V$ :

cost( $u$ ) =  $\infty$

prev( $u$ ) = nil

Pick any initial node  $u_0$ .

cost( $u_0$ ) = 0.

$H = \text{makequeue}(V)$  (priority queue, using cost-values as keys).

while  $H$  is not empty:

$v = \text{deletemin}(H)$

for each  $\{v, z\} \in E$ :

if cost( $z$ ) >  $w(v, z)$ :

cost( $z$ ) =  $w(v, z)$

prev( $z$ ) =  $v$

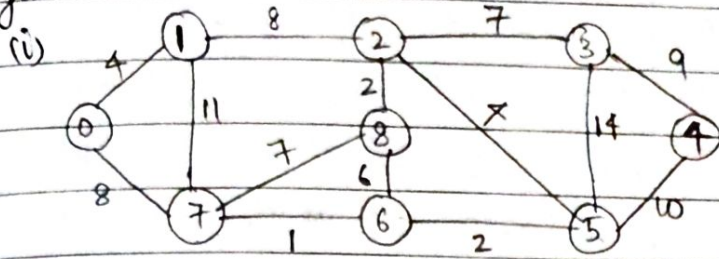
decreasekey( $H, z$ )

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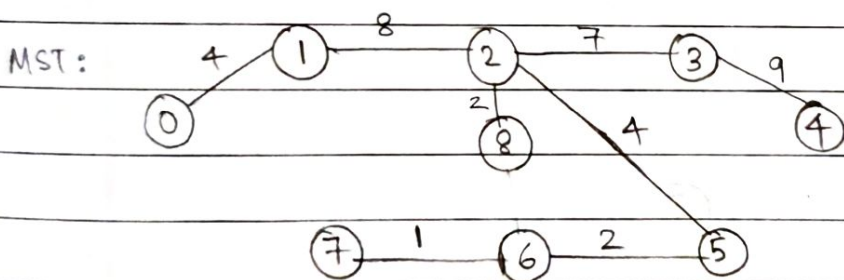


(ii) using the algorithm, find the min. cost spanning tree for the graphs given below:



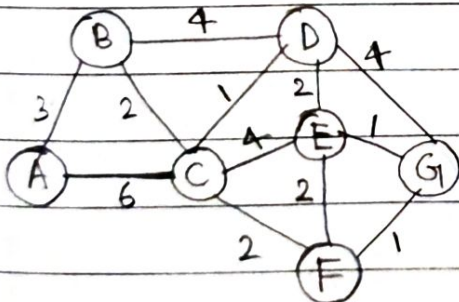
start from vertex 0.  
table has cost/prev values.

Set S	0	1	2	3	4	5	6	7	8
{}	0/nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil
0		4/0	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	8/0	$\infty$ /nil
0, 1			8/1	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	11/1	$\infty$ /nil
0, 1, 2				7/2	$\infty$ /nil	4/2	$\infty$ /nil	$\infty$ /nil	2/2
0, 1, 2, 8				7/2	$\infty$ /nil	4/2	6/8	7/8	-
0, 1, 2, 8, 5				7/2	10/5	-	2/5	7/8	-
0, 1, 2, 8, 5, 6				7/2	10/5	-	-	1/6	-
0, 1, 2, 8, 5, 6, 7				7/2	10/5	-	-	-	-
0, 1, 2, 8, 5, 6, 7, 3				-	9/3	-	-	-	-
0, 1, 2, 8, 5, 6, 7, 3, 4									



$$\begin{aligned} \text{min. cost} &= 4 + 8 + 2 + 4 + 9 + 2 + 1 \\ &= \underline{\underline{32}} \end{aligned}$$

(iii)



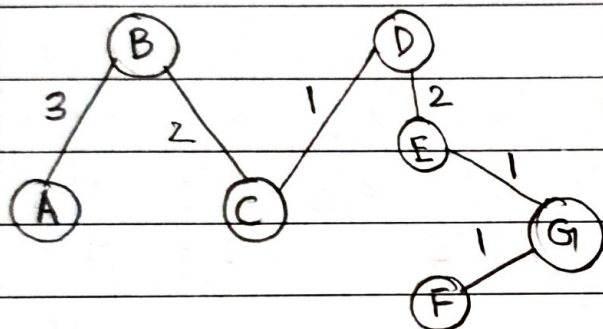
start from vertex A.





	Sets	A	B	C	D	E	F	G
	{}	0/nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil
	A		3/A	6/A	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil
	A, B		-	2/B	4/D	$\infty$ /nil	$\infty$ /nil	$\infty$ /nil
	A, B, C				1/C	4/C	2/C	$\infty$ /nil
	A, B, C, D					2/D	2/C	4/D
	A, B, C, D, E						2/C	1/E
	A, B, C, D, E, G						1/G	
	A, B, C, D, E, G, F							

MST:



Min. cost:  $3+2+1+2+1+1$

$= 10$