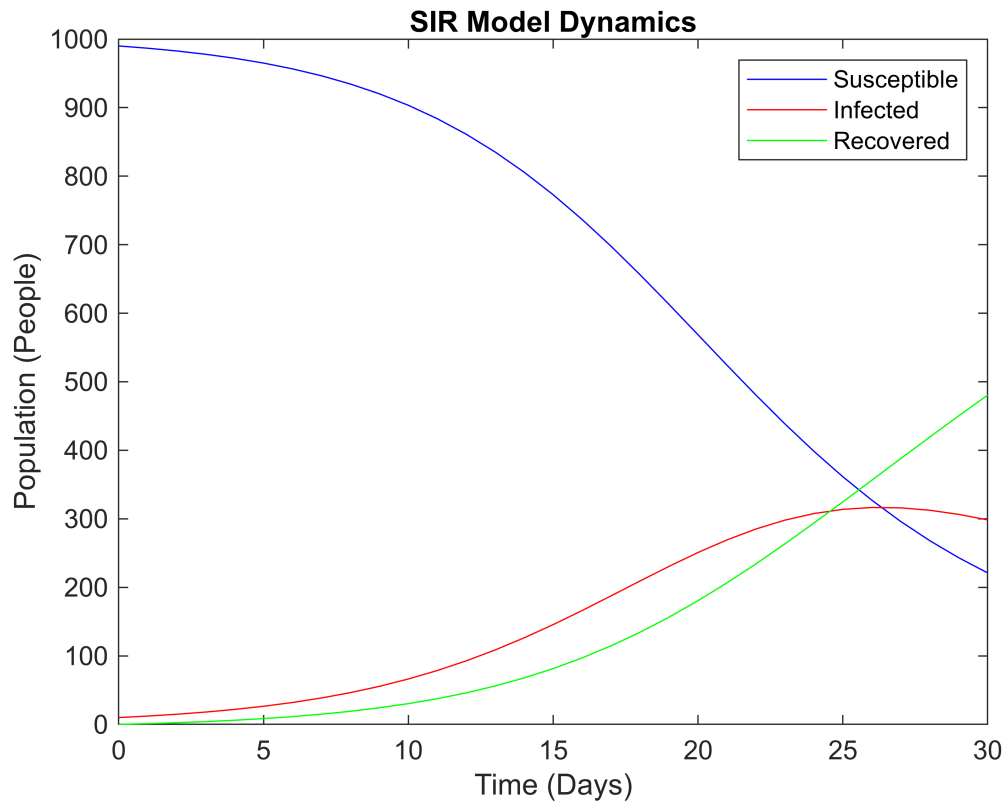


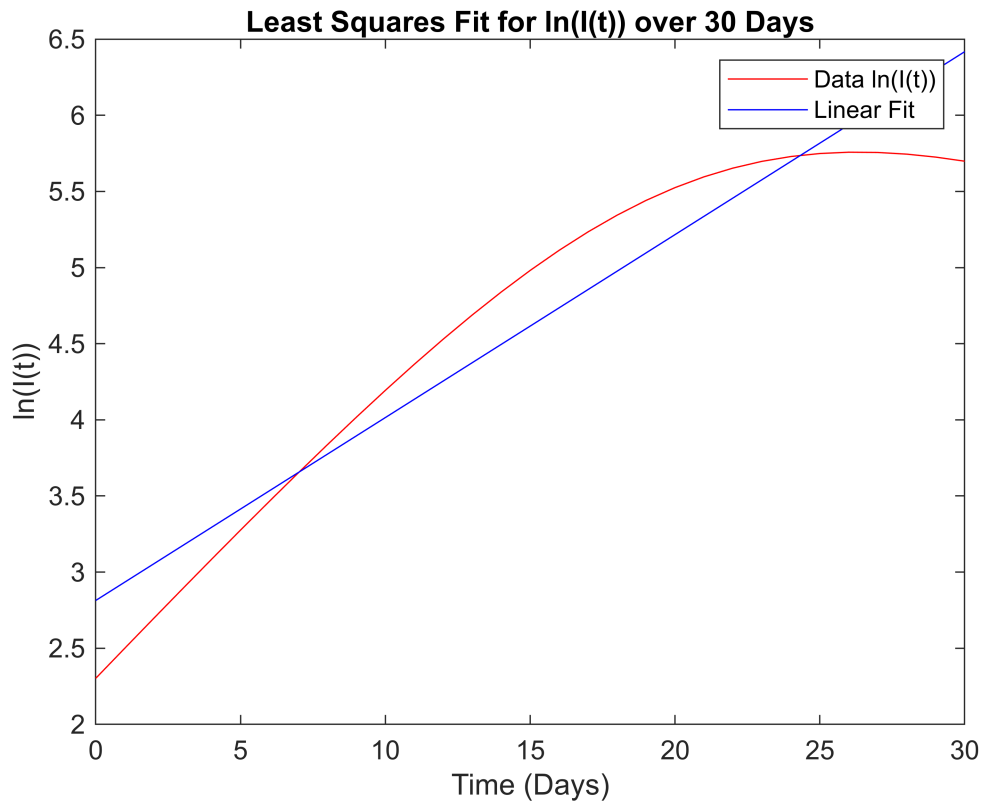
```

% Group Project Part 3: Least-Squares Regression.
% Initial Conditions and Necessary Equations for Step 1.
S(1) = 990;           % Initial susceptible population.
I(1) = 10;            % Initial infected population.
R(1) = 0;             % Initial recovered population.
N = 1000;             % Total population.
B = 0.3;              % Transmission rate.
Y = 0.1;              % Recovery rate.
h = 1;                % Time step.
t = 0:h:30;           % Simulation duration.
dS = @(S,I)(-B*S*I/N); % Given ODE for S(t).
dI = @(S,I)((B*S*I/N)-(Y*I)); % Given ODE for I(t).
dR = @(I)(Y*I);       % Given ODE for R(t).
% Loop that determines the values of S(t), I(t), and R(t) using the given
% initial values and the fourth-order Runge-Kutta Method for each day.
for x = 1:(length(t)-1)
    K1S = dS(S(x),I(x));
    K1I = dI(S(x),I(x));
    K1R = dR(I(x));
    K2S = dS(S(x)+(h/2),I(x)+(K1I*h/2));
    K2I = dI(S(x)+(h/2),I(x)+(K1I*h/2));
    K2R = dR(I(x)+(K1I*h/2));
    K3S = dS(S(x)+(h/2),I(x)+(K2I*h/2));
    K3I = dI(S(x)+(h/2),I(x)+(K2I*h/2));
    K3R = dR(I(x)+(K2I*h/2));
    K4S = dS(S(x)+h,I(x)+(K3I*h));
    K4I = dI(S(x)+h,I(x)+(K3I*h));
    K4R = dR(I(x)+(K3I*h));
    S(x+1) = S(x)+((K1S+(2*K2S)+(2*K3S)+K4S)*h/6);
    I(x+1) = I(x)+((K1I+(2*K2I)+(2*K3I)+K4I)*h/6);
    R(x+1) = R(x)+((K1R+(2*K2R)+(2*K3R)+K4R)*h/6);
end
% Plots the values of S(t), I(t), and R(t) determined in the loop above.
figure(1)
plot(t,S,'b',t,I,'r',t,R,'g')
xlabel('Time (Days)')
ylabel('Population (People)')
title('SIR Model Dynamics')
legend('Susceptible','Infected','Recovered')

```



```
% Initial Conditions and Necessary Equations for Step 2.
n = length(t);
u = sum(t);
w = sum(t.^2);
lnI = log(I);
y = sum(lnI);
z = sum(t.*lnI);
k = ((n*z)-(u*y))/((n*w)-(u^2));
lnI0 = (y-(k*u))/n;
I0 = exp(lnI0);
B1 = ((k+Y)*N)/S(1);
% Plots the analytical solution, I(t) = I(0)e^kt, over 30 days.
figure(2)
plot(t,lnI,'r',t,lnI0+(k*t),'b')
xlabel('Time (Days)')
ylabel('ln(I(t))')
title('Least Squares Fit for ln(I(t)) over 30 Days')
legend('Data ln(I(t))','Linear Fit')
```



```
% Displays the estimated values for I(0), k, and beta over 30 days.
disp("Requested information for Step 2.")
```

Requested information for Step 2.

```
disp("Estimated I(0) over 30 Days: " + I0)
```

Estimated I(0) over 30 Days: 16.6724

```
disp("Estimated k over 30 Days: " + k)
```

Estimated k over 30 Days: 0.12012

```
disp("Estimated beta over 30 Days: " + B1)
```

Estimated beta over 30 Days: 0.22235

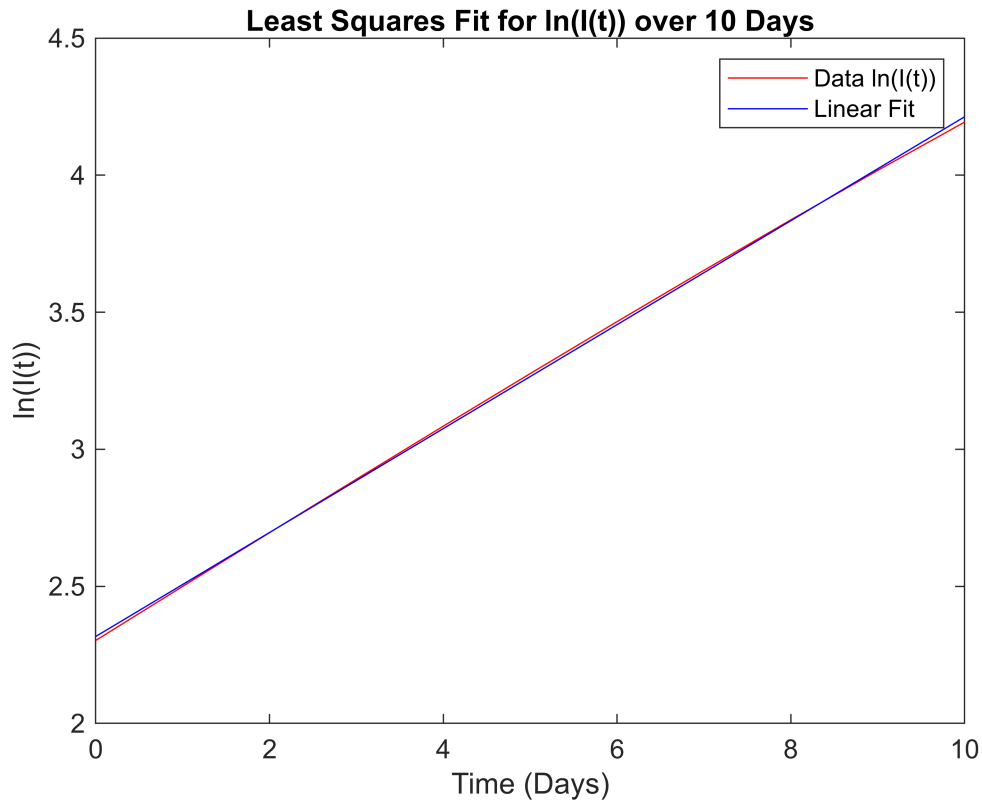
```
% Initial Conditions and Necessary Equations for Step 3.
```

```
d = t(1:11);
m = length(d);
b = sum(d);
c = sum(d.^2);
J = I(1:11);
lnJ = log(J);
e = sum(lnJ);
f = sum(d.*lnJ);
l = ((m*f)-(b*e))/((m*c)-(b^2));
lnJ0 = (e-(l*b))/m;
```

```

J0 = exp(lnJ0);
B2 = ((1+Y)*N)/S(1);
% Plots the analytical solution,  $I(t) = I(0)e^{kt}$ , over 10 days.
figure(3)
plot(d,lnJ,'r',d,lnJ0+(1*d),'b')
xlabel('Time (Days)')
ylabel('ln(I(t))')
title('Least Squares Fit for ln(I(t)) over 10 Days')
legend('Data ln(I(t))','Linear Fit')

```



```

% Displays the estimated values of  $I(0)$ ,  $k$ , and  $\beta$  over 10 days.
disp("Requested information for Step 3.")

```

Requested information for Step 3.

```
disp("Estimated  $I(0)$  over 10 Days: " + J0)
```

Estimated $I(0)$ over 10 Days: 10.1468

```
disp("Estimated  $k$  over 10 Days: " + l)
```

Estimated k over 10 Days: 0.1896

```
disp("Estimated  $\beta$  over 10 Days: " + B2)
```

Estimated β over 10 Days: 0.29252

As can be seen from the graphs of $\ln I(t)$ and the estimated values of $I(0)$, k , and β , reducing the number of days to 10 results in a significant increase in the accuracy of said values. By using fewer sets of data, the model becomes more linear, meaning a line can be fit to the data much more accurately compared to using more data points. Hence the values of $I(t)$, k , and β being much more accurate with 10 days of data instead of the full 30 days of data.