

Tree --- : need to be able to compare elements  
(nodes of type comparable)

2 1 2 3 4 5  
3 7 11 13 17  
index = length/2 - 1 = 5/2 - 1 = 1  
∴ 3 is parent of last node,  
2 - 4 are leaves

## Build Heap

3 11 13 17  
0 1 2 3  
L R

1. Let index = length/2-1. This is the parent of the last node in the tree, i.e. list[index + 1] . . . list[length-1] are leaves
2. Convert the subtree with root of list[index] into a heap.
  - a. Given list[a] is root of tree, list[b] is left child (root \*2 +1), list[c] is right child (root\*2+2), if exists
  - b. Compare list[b] with list[c] to determine larger child, list[largerIndex]
  - c. Compare list[a] with list[largerIndex]. If list[a] < list[largerIndex], then swap, else already a heap
  - d. If swap, repeat step 2 for the subtree of list[largerIndex]
3. Convert the subtree with the root of list[index-1] into a heap, repeat until list[0]

Merge Sort

## Heap Sort

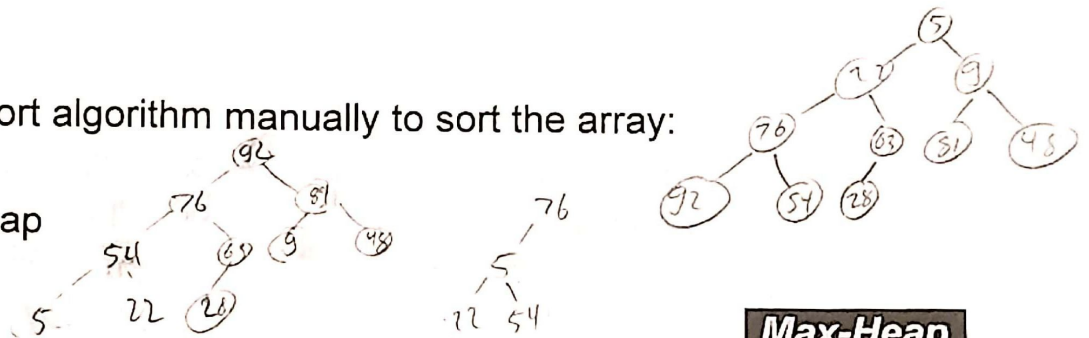
1. Swap the root with the end of the list.
2. Heapify the list up to but not including the root
3. Repeat until there is only one node in the list

bubble  
selection  
insertion  
merge

Simulate the heapsort algorithm manually to sort the array:

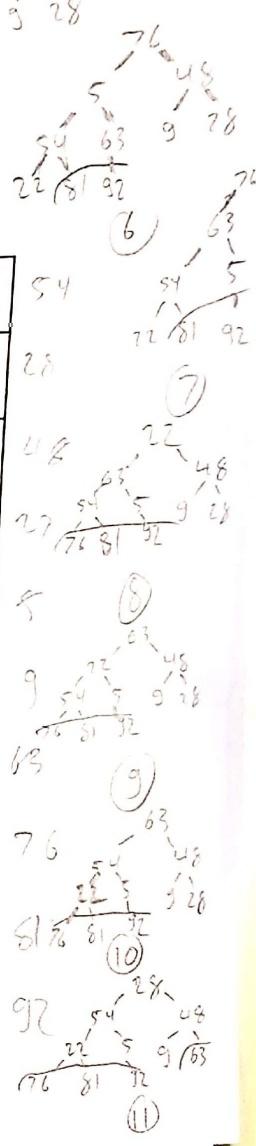
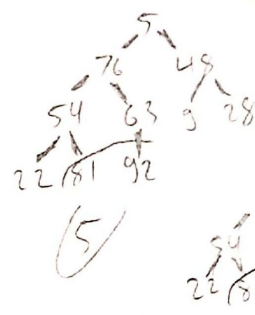
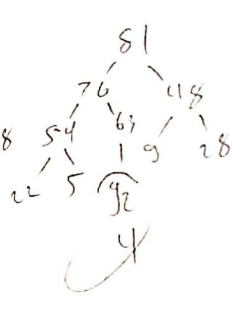
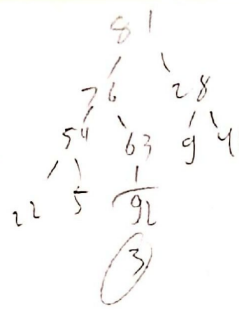
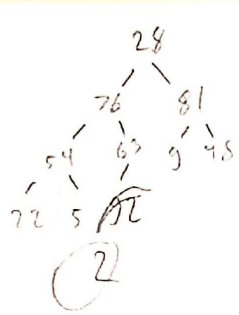
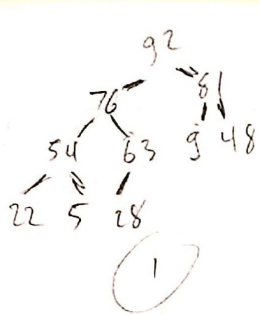
Show all steps

1. Make into a heap
2. Sort



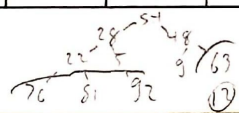
**Max-Heap**

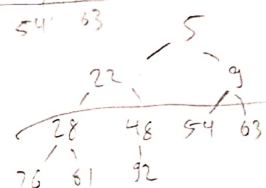
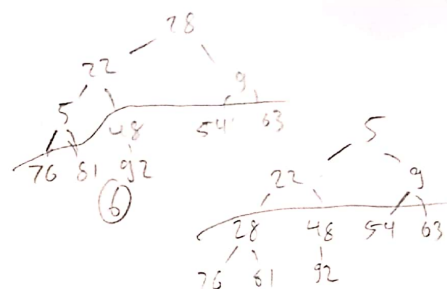
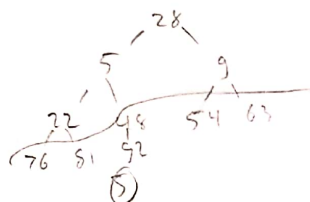
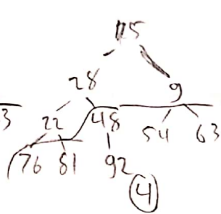
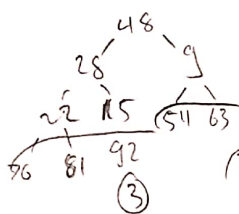
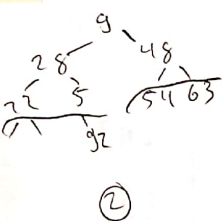
[0]	5					→	92					→	92
[1]	22			→	92		→	5	76			→	76
[2]	9		→	81								→	81
[3]	76	92		→	22	76		→	5	54		→	54
[4]	63											→	63
[5]	81		→	9								→	9
[6]	48											→	48
[7]	92	76			→	22						→	22
[8]	54							→	5				5
[9]	28												28



1 2 3 4 5 6 7 8 9 10 11 12

[0]	92	28	81		5	76		22	63		28	54
[1]	76					5	63		22	54		28
[2]	81		28	48							48	
[3]	54								22		22	
[4]	63					5					5	
[5]	9										9	
[6]	48		28							63	63	
[7]	22						76				76	
[8]	5			81							81	
[9]	28	92									92	





	1	2	3	4	5	6	7	8	9	10	11	
[0]	54	9	48	5	28		5	22	9	5	5	
[1]	28				5	22		5		9	9	
[2]	48		9						22		22	
[3]	22					5	28				28	
[4]	5			48							48	
[5]	9	54									54	
[6]	63										63	
[7]	76										76	
[8]	81										81	
[9]	92										92	

