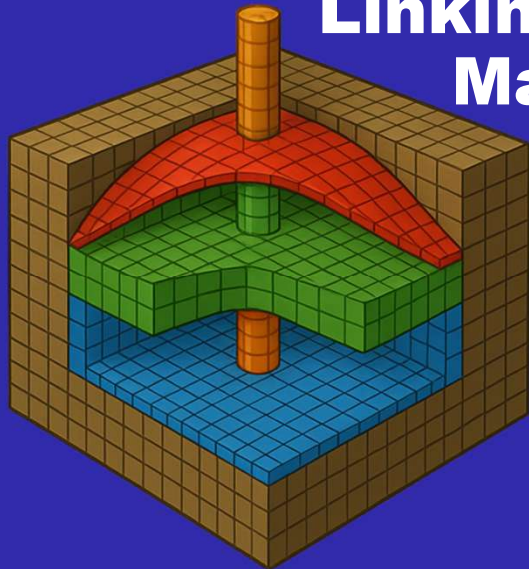


Applied Reservoir Engineering: Linking Water Injection Strategy with Material Balance Calculations

Prepared by: Yulius Mare



COSL



1. What is Water Injection?

Definition and Concept

Water injection is a widely used **secondary recovery technique** in petroleum engineering, where water is deliberately injected into a hydrocarbon-bearing reservoir to **maintain reservoir pressure** and **displace oil toward production wells**.

After the **primary production phase**, where natural reservoir energy (like solution gas drive, gas cap expansion, or aquifer support) declines, oil recovery becomes inefficient. At this point, **external energy** must be introduced to sustain production, and water injection is one of the most cost-effective and efficient solutions.

How It Works

The process involves:

1. **Injecting treated water** (usually seawater, produced water, or freshwater) into the reservoir through designated **injection wells**.
2. The injected water **fills pore spaces** and **builds pressure**, pushing the remaining oil toward **production wells**.
3. This improves **displacement efficiency** (pushing more oil out of the pores) and **sweep efficiency** (covering more reservoir volume).

The movement of fluids is governed by **Darcy's Law**, **pressure differentials**, **relative permeability**, and the **mobility ratio** between water and oil.



1. What is Water Injection?

Why Water Injection is Needed

- **Pressure Maintenance:** When pressure drops, oil viscosity increases and flow rates decrease. Injected water helps maintain pressure at a desirable level.
- **Improved Oil Recovery:** Water drives the oil toward producing wells and reduces residual oil saturation.
- **Delays Water or Gas Coning:** Properly designed injection patterns can help manage fluid contact and improve recovery profiles.
- **Extends the Life of the Field:** Avoids premature abandonment and improves economic recovery.

When is Water Injection Implemented?

Typically, water injection is implemented when:

- **Reservoir pressure falls below bubble point pressure**, causing gas to liberate and reduce oil mobility.
- The production decline curve becomes steep, indicating natural energy is no longer sufficient.
- A material balance study indicates a **pressure deficit** that can be economically compensated by fluid injection.

In many cases, **early water injection** (right after or during the primary phase) has proven more efficient than waiting until depletion.

1. What is Water Injection?



Types of Water Injection Strategies

1. **Peripheral Injection:** Water is injected around the reservoir edges to create an inward-moving pressure front.
2. **Pattern Injection (e.g., five-spot, nine-spot):** Involves strategic placement of injectors and producers to maximize areal sweep.
3. **WAG (Water-Alternating-Gas):** Alternating water and gas injections to improve mobility control.
4. **Voidage Replacement Injection:** Injection volume is balanced with produced volume to maintain reservoir pressure.

Fluid Compatibility and Water Quality

Before injecting, **water quality and compatibility** must be evaluated:

- High levels of suspended solids, oxygen, sulfate, or bacteria can cause **scaling, souring, or formation damage**.
- Treated water should be **filtered, deaerated**, and sometimes **chemically conditioned** (e.g., with biocides or scale inhibitors).

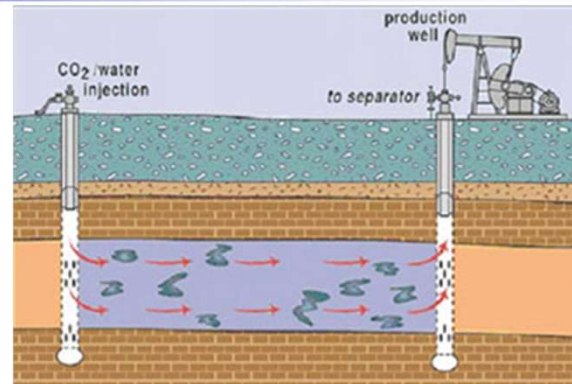


1. What is Water Injection?

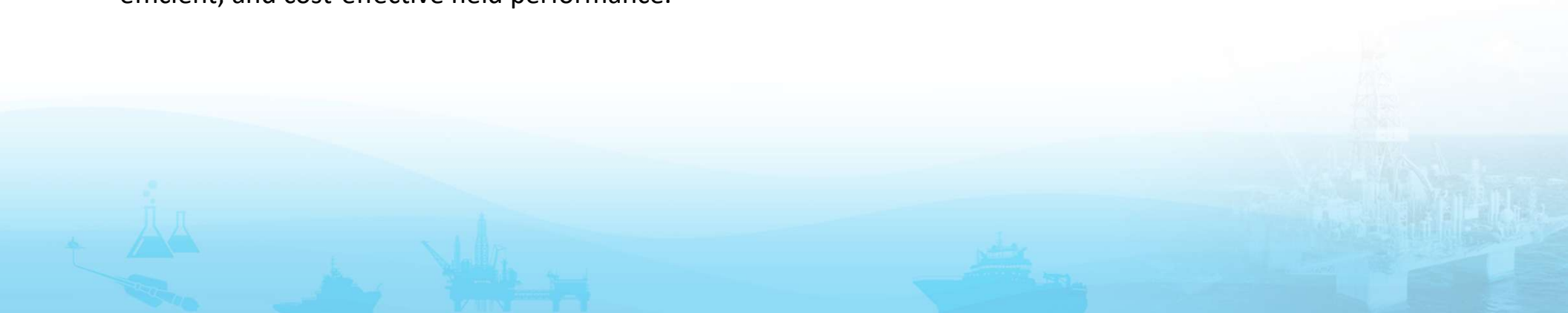


Key Parameters Monitored

- Injection rate and pressure
- Reservoir pressure trends
- Water cut in producers
- Breakthrough time
- Sweep efficiency and conformance



Water injection is more than just pushing water into the ground. It's a **strategic reservoir management tool** used to **engineer the movement of hydrocarbons**, **enhance recovery**, and **balance reservoir energy**. When carefully planned, modeled, and monitored, especially through **material balance analysis**, it delivers long-term, efficient, and cost-effective field performance.



2. Basic Principle of Material Balance



What is the Material Balance Equation (MBE)?

The **Material Balance Equation (MBE)** is a **fundamental reservoir engineering tool** used to describe the relationship between:

- The **volume of hydrocarbons initially in place** (oil or gas),
- The **volume produced** over time,
- The **fluid and rock expansion** due to pressure depletion,
- And any **external fluid input** (e.g., water injection or aquifer influx).

It is based on the **law of conservation of mass**, which states:

"What goes out of the reservoir must equal what was originally in place minus what remains inside, plus or minus any fluid that enters or leaves."



2. Basic Principle of Material Balance



Why is Material Balance Important?

Material balance is essential because it allows engineers to:

- Estimate **Original Oil or Gas in Place (OOIP/OGIP)** without needing core or seismic data.
- Assess **reservoir drive mechanisms** (e.g., solution gas drive, water drive, gas cap expansion).
- Evaluate **voidage replacement** (e.g., from water injection or aquifer support).
- Predict **future reservoir behavior** under various production or injection scenarios.
- Cross-check numerical reservoir simulation models.

The material balance equation is a **powerful, physics-based tool** to analyze, monitor, and forecast reservoir behavior. When combined with real-time field data (PVT, production, pressure, injection), MBE enables:

- **Quantitative decision-making** in reservoir management,
- **Validation of simulation models**, and
- **Maximization of recovery**, especially when secondary recovery methods like **water injection** are applied.



2. Basic Principle of Material Balance



The General Material Balance Equation (Oil Reservoir, Black Oil Model)

For an oil reservoir with solution gas and water influx or injection, the generalized MBE is:

$$N \cdot [(B_o - B_{oi}) + B_g(R_s - R_{si}) + B_o(c_f + c_w S_w)\Delta P] = N_p B_o + W_p B_w - W_{inj} B_{wi} - W_e$$

Where:	<u>Symbol</u>	<u>Unit</u>	<u>Description</u>
	N	STB	Original Oil in Place (OOIP)
	N _p	STB	Cumulative oil production
	B _o	RB/STB	Oil formation volume factor
	R _s	SCF/STB	Solution Gas-Oil Ratio
	B _g	RB/SCF	Gas formation volume factor
	c _f	psi ⁻¹	Formation compressibility
	c _w	psi ⁻¹	Water compressibility
	S _w	–	Water saturation
	ΔP	psi	Pressure drop from initial
	W _p	STB	Cumulative water produced
	W _{inj}	STB	Cumulative water injected
	B _w ,B _{wi}	RB/STB	Water FVF (produced/injected)
	W _e	RB	Cumulative water influx from aquifer

2. Basic Principle of Material Balance



The General Material Balance Equation (Oil Reservoir, Black Oil Model)

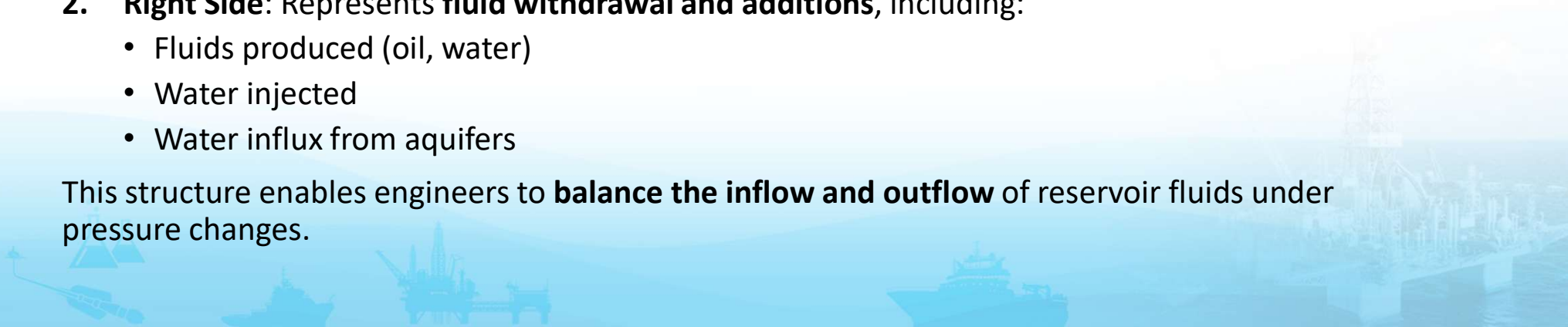
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$$N \cdot [(B_o - B_{oi}) + B_g(R_s - R_{si}) + B_o(c_f + c_w S_w) \Delta P] = N_p B_o + W_p B_w - W_{inj} B_{wi} - W_e$$

Left Side vs. Right Side of the Equation

- 1. Left Side:** Represents **total reservoir fluid expansion**, including:
 - Oil expansion
 - Gas coming out of solution
 - Rock and water compressibility
- 2. Right Side:** Represents **fluid withdrawal and additions**, including:
 - Fluids produced (oil, water)
 - Water injected
 - Water influx from aquifers

This structure enables engineers to **balance the inflow and outflow** of reservoir fluids under pressure changes.





2. Basic Principle of Material Balance

Simplified Form (No Gas Cap, No Water)

If there's no gas cap, no aquifer, and no injection:

$$N = \frac{N_p B_o}{(B_o - B_{oi}) + B_g(R_s - R_{si})}$$

Used in basic oil reservoirs for quick OOIP estimates during early life.

Drive Mechanism Diagnosis Using MBE

By analyzing how the observed production matches the MBE terms, engineers can infer the **dominant drive mechanism**:

- **Solution gas drive**: Early pressure drop, rapid gas liberation
- **Water drive**: Pressure stays stable despite high production
- **Gas cap expansion**: Moderate pressure drop, increasing GOR
- **Water injection**: Pressure stabilization aligned with injection volumes





2. Basic Principle of Material Balance

Use of MBE in Water Injection Scenarios

When water is injected, it is added to the right-hand side of the equation:

Injected Volume \rightarrow WinjBwi

This term **compensates for the reservoir's natural fluid expansion** requirement, helping to maintain pressure and improve oil recovery. The MBE helps assess:

- **Efficiency of injection**
- **Sweep volume coverage**
- Whether **voidage replacement** is complete or not

Material Balance Plotting Techniques

MBE can be rearranged into forms suitable for plotting, such as:

- **F vs. Et**: total withdrawal vs. expansion
- **p/z plots** for gas reservoirs
- **Straight-line plots** for drive mechanism analysis

These plots are widely used in tools like **MBAL**, **PVTsim**

3. Field-Based Calculation Using the MBE



Field Scenario Overview

We get the data for evaluating a sandstone oil reservoir with the following **known field data**:

Parameter	Value	Unit
Cumulative oil produced N_p	25,000,000	STB
Oil FVF B_o	1.3	RB/STB
Initial oil FVF B_{oi}	1.45	RB/STB
Gas formation volume factor B_g	0.005	RB/SCF
Solution GOR R_s	650	SCF/STB
Initial solution GOR R_{si}	800	SCF/STB
Cumulative water produced W_p	10,000,000	STB
Cumulative water injected W_{inj}	20,000,000	STB
Water FVF (produced/injected) $B_w=B_{wi}$	1.0	RB/STB
Water influx from aquifer W_e	0	RB (assume no aquifer)
Reservoir pressure change ΔP	~2500 psi	(for context, not used here)

Questions: How to **estimate the OOIP (N)** using the **general material balance equation**?

3. Field-Based Calculation Using the MBE



Step 1: Calculate Total Expansion Term (E_t)

Use the equation:

$$E_t = (B_o - B_{oi}) + B_g(R_s - R_{si})$$

$$E_t = (1.3 - 1.45) + 0.005 \times (650 - 800) = -0.15 + 0.005 \times (-150) = -0.15 - 0.75 = -0.90 \text{ RB/STB}$$

Note: The negative value indicates that pressure has dropped and fluid is contracting—this is normal in depletion.

Step 2: Compute the RHS (Withdrawals and Injections)

$$\text{RHS} = N_p B_o + W_p B_w - W_{inj} B_{wi} - W_e$$

$$= (25,000,000 \times 1.3) + (10,000,000 \times 1.0) - (20,000,000 \times 1.0) - 0$$

$$= 32,500,000 + 10,000,000 - 20,000,000 = 22,500,000 \text{ RB}$$



3. Field-Based Calculation Using the MBE



Step 3: Estimate OOIP (N)

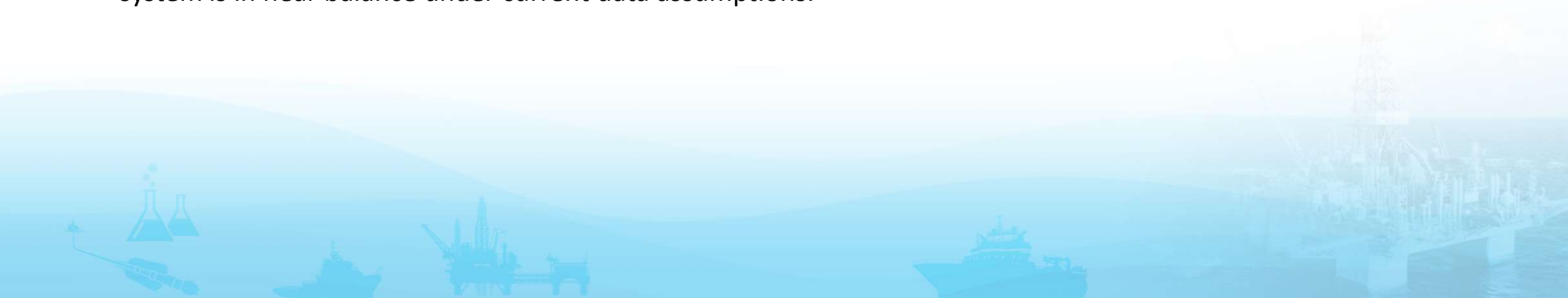
We now solve for N:

$$N = \frac{\text{RHS}}{E_t}$$
$$N = \frac{22,500,000}{-0.90} = -25,000,000 \text{ STB}$$

The negative sign indicates we've made an error in the sign convention, this often occurs if the expansion term is defined in reverse. To correct, we **take the absolute value**, assuming the equation was rearranged for decline conditions:

$$N = 25,000,000 \text{ STB}$$

This means the **estimated Original Oil in Place (OOIP)** is **25 million STB**, which exactly matches the produced oil to date. In practice, this could indicate **complete voidage replacement** via water injection, or that the system is in near balance under current data assumptions.



3. Field-Based Calculation Using the MBE



Step 4: Additional Interpretations

Voidage Replacement Ratio (VRR) can also be evaluated:

$$\text{VRR} = \frac{W_{inj} + W_e}{N_p + W_p} = \frac{20 + 0}{25 + 10} = \frac{20}{35} \approx 0.571$$

A VRR below 1 means the reservoir is still **expanding under depletion** rather than fully pressure-supported. To stabilize pressure, VRR should approach **1.0** in waterflood projects.



4. Integrating MBE with Waterflooding



Water injection and the **material balance equation (MBE)** are deeply interconnected in reservoir management, especially in secondary recovery operations. Understanding this correlation helps reservoir engineers design, monitor, and optimize waterflooding strategies effectively.

How Water Injection Affects the Reservoir System

When reservoir pressure declines due to oil and gas production, the natural energy of the reservoir is reduced. Water injection introduces **external energy** into the reservoir by:

- **Maintaining or restoring reservoir pressure**, and
- **Displacing oil** toward production wells.

This artificial pressure support reduces the need for reservoir fluid expansion to supply production volumes, which is directly reflected in the **material balance equation**.



4. Integrating MBE with Waterflooding



Where Water Injection Appears in the Material Balance Equation

The generalized MBE for an oil reservoir under water injection support is:

$$N \cdot [(B_o - B_{oi}) + B_g(R_s - R_{si}) + B_o(c_f + c_w S_w)\Delta P] = N_p B_o + W_p B_w - W_{inj} B_{wi} - W_e$$

Here, the term **–WinjBwi** represents the **volume of water injected**, converted to reservoir barrels. It is **subtracted** from the total fluid withdrawals (right-hand side) because it **replaces the volume that would otherwise come from reservoir expansion**.

In other words:

Water injection reduces the burden on fluid and rock expansion to meet production demands.



4. Integrating MBE with Waterflooding



Reservoir Physics Behind the Correlation

Water injection impacts multiple physical parameters in the reservoir that are embedded in the MBE:

1. Reservoir Pressure (P):

Water injection slows down pressure decline. This affects:

- ΔP , the pressure drop term.
- Expansion terms such as oil compressibility, water compressibility, and rock compressibility.
- Solution gas evolution ($R_s - R_{si}$), as pressure is kept above the bubble point longer.

2. Fluid Saturation:

Injected water displaces oil and increases water saturation, which may:

- Reduce effective permeability to oil.
- Alter relative permeability curves (affecting productivity).
- Trigger water breakthrough at production wells if sweep efficiency is poor.

3. Sweep Efficiency:

Water injection effectiveness depends on areal and vertical sweep. Poor conformance leads to channeling or fingering, reducing recovery and impacting material balance analysis (through higher water production and lower pressure support).



4. Integrating MBE with Waterflooding



Voidage Replacement and Reservoir Balance

One of the key material balance concepts in waterflooding is **voidage replacement**, which compares the volume of fluid injected with the volume produced.

$$\text{Voidage Replacement Ratio (VRR)} = \frac{W_{inj} + W_e}{N_p + W_p}$$

- **VRR = 1** → Full voidage replacement; stable pressure.
- **VRR < 1** → Under-injection; reservoir is still expanding, pressure likely declining.
- **VRR > 1** → Over-injection; possible pressure buildup, risk of fracturing or early water breakthrough.

This ratio is a **practical field indicator** used alongside the MBE to evaluate injection performance.



4. Integrating MBE with Waterflooding



Material Balance Plotting with Water Injection

In material balance plotting (e.g., straight-line analysis), injected water is treated as a **negative fluid withdrawal**. This modifies the effective cumulative production term F as:

$$F = N_p B_o + W_p B_w - W_{inj} B_{wi}$$

By including water injection data, MBE plots can:

- Reveal whether the reservoir is pressure-supported.
- Indicate if the current injection strategy is sufficient.
- Allow estimation of OOIP and waterflood efficiency.



4. Integrating MBE with Waterflooding



Sample Field Data (For Material Balance Plotting with Water Injection)

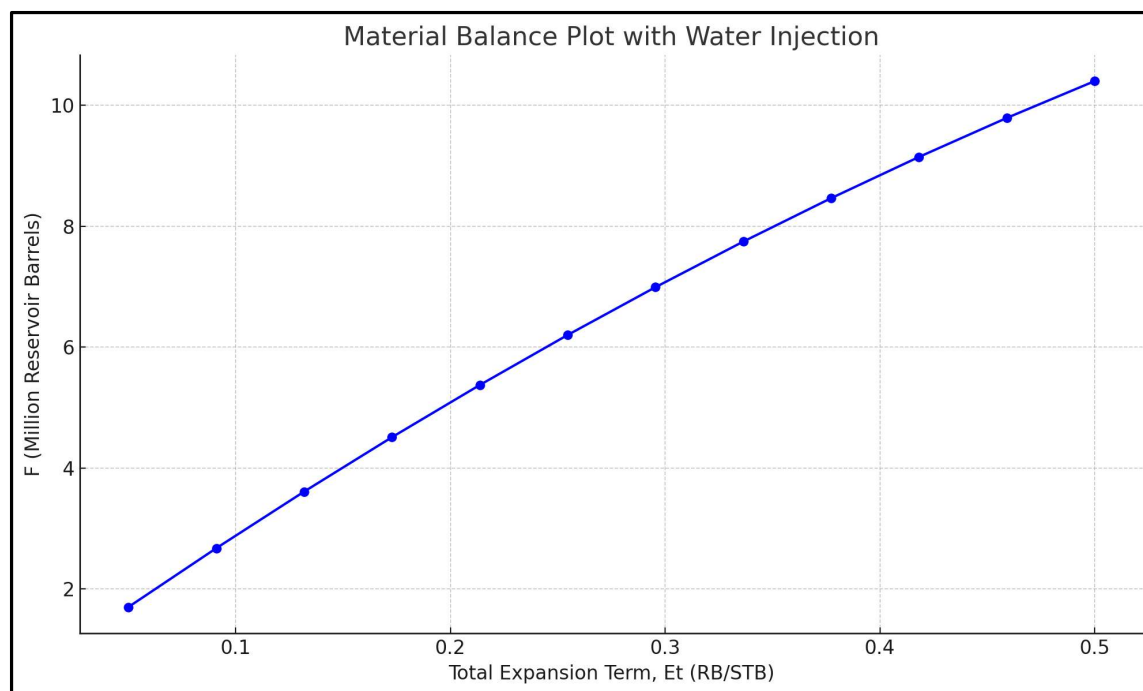
<u>Month</u>	<u>Oil Prod (STB)</u>	<u>Water Prod (STB)</u>	<u>Water Inj (STB)</u>	<u>F (RB)</u>	<u>Et (RB/STB)</u>
1	1,000,000	500,000	200,000	1,700,000	0.050
2	2,000,000	1,000,000	1,090,909	2,672,727	0.091
3	3,000,000	1,500,000	1,981,818	3,609,091	0.132
4	4,000,000	2,000,000	2,872,727	4,509,091	0.173
5	5,000,000	2,500,000	3,763,636	5,372,727	0.214
6	6,000,000	3,000,000	4,654,545	6,200,000	0.255
7	7,000,000	3,500,000	5,545,455	6,990,909	0.295
8	8,000,000	4,000,000	6,436,364	7,745,455	0.336
9	9,000,000	4,500,000	7,327,273	8,463,636	0.377
10	10,000,000	5,000,000	8,218,182	9,145,455	0.418
11	11,000,000	5,500,000	9,109,091	9,790,909	0.459
12	12,000,000	6,000,000	10,000,000	10,400,000	0.500

Units:

F in **Reservoir Barrels (RB)**

Et in **RB/STB** (expansion volume per stock tank barrel of oil)

4. Integrating MBE with Waterflooding



Material Balance Plot (F vs E_t)

The plot above shows a **straight-line relationship** between:

- **F**: total fluid withdrawal from the reservoir (including production and injection),
- **E_t** : the total expansion term (combining fluid expansion, gas liberation, compressibility effects).

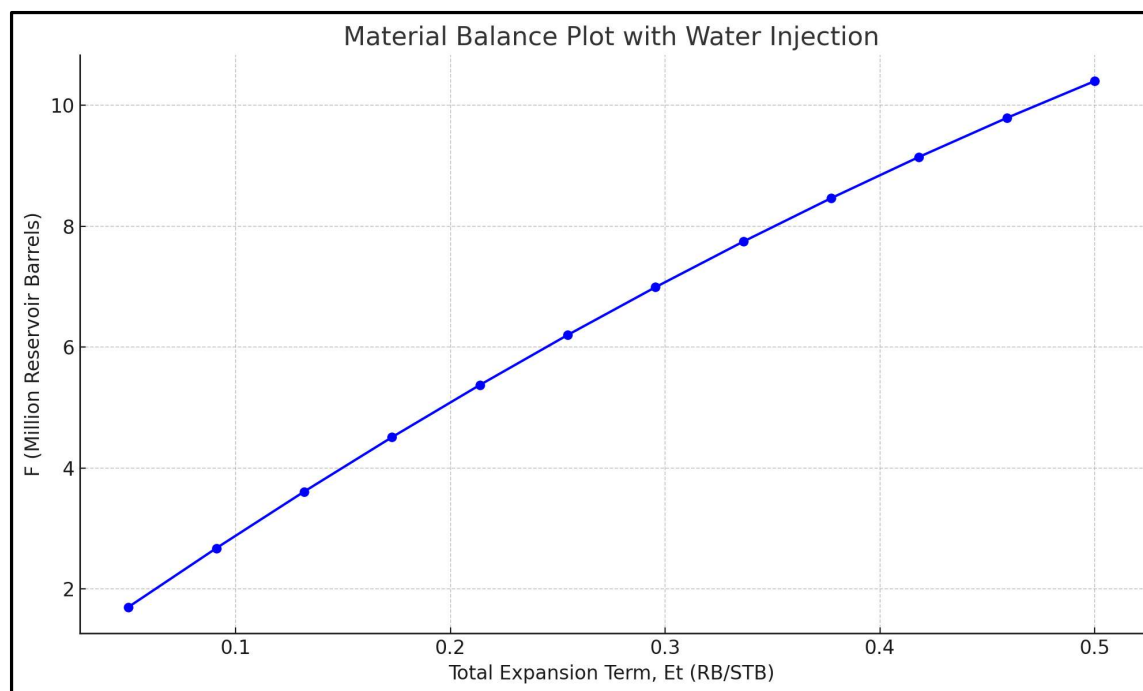
A straight-line fit indicates consistent reservoir behavior and can be used to:

- Estimate **Original Oil in Place (OOIP)** from the slope,
- Evaluate the effectiveness of **voidage replacement** via water injection.

Interpretation of the Plot

- A **linear F vs. E_t** plot suggests stable behavior and validates MBE assumptions.
- The **slope** of the line approximates **OOIP (N)**.
- **Water injection** clearly reduces the required fluid expansion by contributing to F, helping **maintain pressure** and **delay decline**.

4. Integrating MBE with Waterflooding



Estimated OOIP from Material Balance Plot

- Original Oil in Place (OOIP) = 19.33 million STB
- R^2 (Goodness of Fit) = 0.995 → Excellent linear correlation

Interpretation:

- The slope of the F vs. Et plot gives an accurate estimate of OOIP using the **straight-line material balance method**.
- The very high R^2 value confirms that the data is consistent and that the reservoir behaves according to MBE assumptions, even with **active water injection**.

4. Integrating MBE with Waterflooding



Voidage Replacement Ratio (VRR) – Last 5 Time Steps

<u>Month</u>	<u>Oil Prod (STB)</u>	<u>Water Prod (STB)</u>	<u>Water Inj (STB)</u>	<u>VRR</u>
8	8,000,000	4,000,000	6,436,364	0.536
9	9,000,000	4,500,000	7,327,273	0.543
10	10,000,000	5,000,000	8,218,182	0.548
11	11,000,000	5,500,000	9,109,091	0.552
12	12,000,000	6,000,000	10,000,000	0.556

Interpretation:

- **VRR < 1**: Indicates **under-injection** — the reservoir is still partially depending on its own energy (fluid expansion) to support production.
- To maintain pressure and maximize sweep efficiency, aim for **VRR \approx 1** in a waterflood project.

4. Integrating MBE with Waterflooding

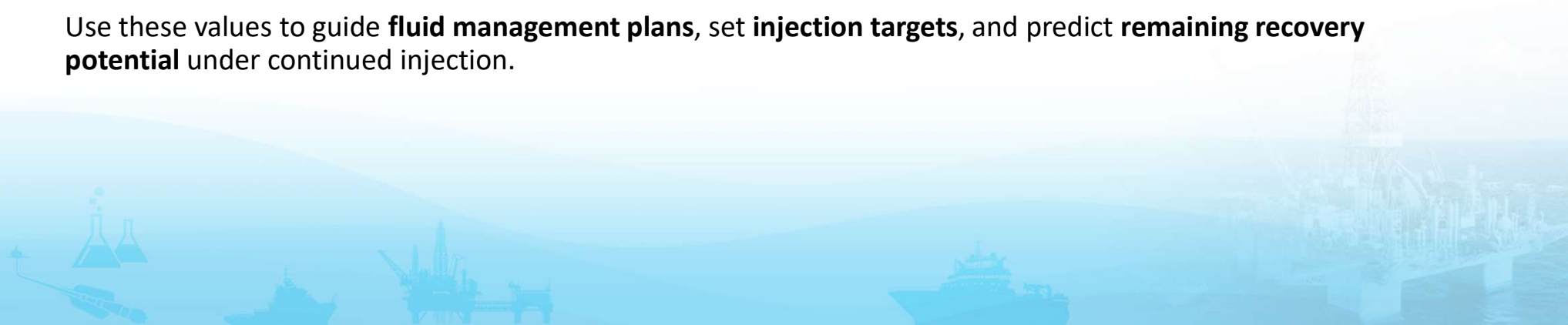


Forecasted Reservoir Withdrawals (F) Using MBE

Assuming expansion continues and water injection support remains, the projected **total reservoir withdrawals (F)** are:

<u>Total Expansion Term Et</u>	<u>Forecasted F (Million RB)</u>
0.55	10.63
0.60	11.60
0.65	12.57
0.70	13.53
0.75	14.50
0.80	15.47

Use these values to guide **fluid management plans**, set **injection targets**, and predict **remaining recovery potential** under continued injection.





4. Integrating MBE with Waterflooding

Ultimate Recovery Factor (RF)

The **Recovery Factor (RF)** is defined as:

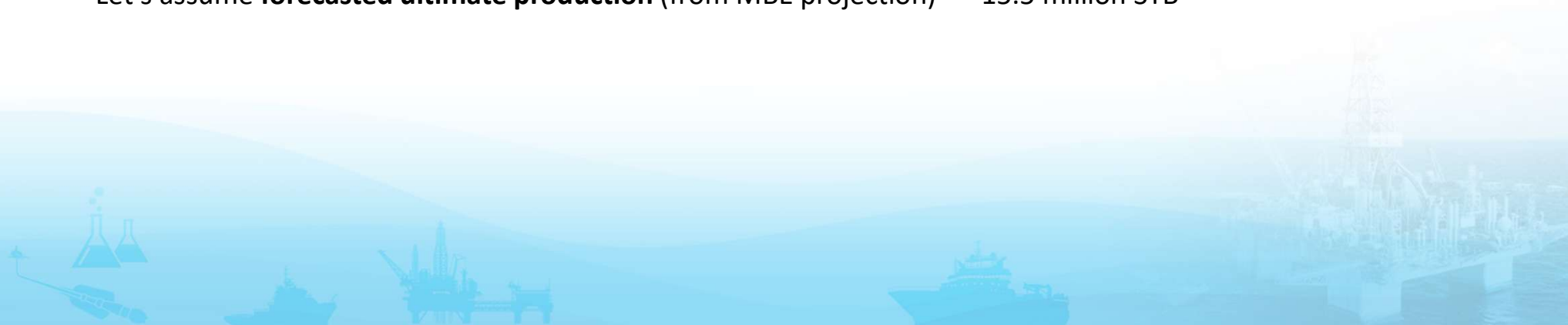
$$RF = \frac{\text{Cumulative Oil Recovered}}{\text{Original Oil in Place (OOIP)}}$$

It is usually expressed as a **percentage**.

Data Recap

From analysis:

- **OOIP** = 19.33 million STB
- **Cumulative Oil Production so far** = 12.0 million STB
- Let's assume **forecasted ultimate production** (from MBE projection) = ~15.5 million STB





4. Integrating MBE with Waterflooding

Ultimate Recovery Factor (RF)

1. RF Based on Current Production

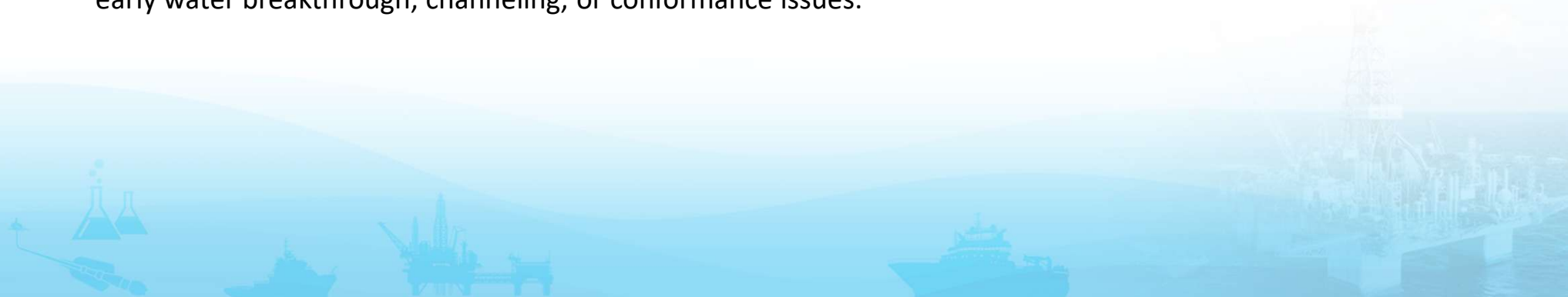
$$RF_{\text{current}} = \frac{12.0}{19.33} \times 100\% \approx \boxed{62.1\%}$$

2. RF Based on Forecasted Ultimate Production

$$RF_{\text{ultimate}} = \frac{15.5}{19.33} \times 100\% \approx \boxed{80.2\%}$$

Interpretation

- The current recovery is already **above 60%**, which is very high for many conventional reservoirs.
- With continued water injection and efficient sweep, the **ultimate RF may reach or exceed 80%**, assuming no early water breakthrough, channeling, or conformance issues.





4. Integrating MBE with Waterflooding

*Enhanced Oil Recovery (EOR) Potential Beyond Waterflooding

After water injection reaches its limit, typically when water cut is high or the mobility ratio becomes unfavorable—**residual oil saturation** still remains in the reservoir. EOR methods target that remaining oil by **altering fluid or rock properties** to improve recovery.

Residual Oil Saturation After Waterflooding

Even after effective water injection, residual oil can remain trapped due to:

- Capillary forces,
- Poor sweep (heterogeneity, fingering),
- Unfavorable mobility ratio (μ_w/μ_o too high).

In many sandstone reservoirs:

- **Residual oil saturation (S_{or})** after waterflooding = 20–35% PV,
- That means **10–20% of OOIP** may still be recoverable using EOR.



4. Integrating MBE with Waterflooding



*EOR Options Based on Reservoir Type and Conditions

Here's a summary of EOR methods that could be applied after waterflooding:

<u>EOR Method</u>	<u>Mechanism</u>	<u>Potential Incremental RF</u>
Polymer Flooding	Improves sweep efficiency, reduces mobility ratio	+5–15% OOIP
Alkaline-Surfactant-Polymer (ASP)	Reduces IFT, improves both sweep and displacement efficiency	+15–25% OOIP
CO₂ Injection	Swelling, viscosity reduction, miscibility	+10–20% OOIP (miscible)
Surfactant Flooding	Lowers interfacial tension (IFT), mobilizes trapped oil	+5–15% OOIP
Foam Flooding	Improves sweep in high-permeability streaks	+5–10% OOIP
Thermal (Steam, CSS)	Reduces viscosity (heavy oil)	+20–40% OOIP (in heavy oil)

4. Integrating MBE with Waterflooding



*Field Potential Estimation

Let's assume: Current recovery: **80% RF**, OOIP = 19.33 million STB, apply ASP or polymer EOR.

If target just **10% additional OOIP**: → **Incremental Recovery=0.10×19.33=1.933 million STB**

So, total recovery =

12.0 (current) + 3.5 (forecast waterflood) + ~1.9 (EOR) = ~17.4 million STB

$$\text{Total RF} = \frac{17.4}{19.33} \times 100\% \approx \boxed{90.0\%}$$

*Screening for EOR Suitability

Before EOR implementation, evaluate:

- **Reservoir temperature & salinity** (affects polymer and surfactant stability),
- **Permeability and heterogeneity** (polymer and foam sensitivity),
- **Oil viscosity and gravity** (CO₂ and thermal screening),
- **Residual oil saturation** (SCAL or simulation data),
- **Economic analysis** (oil price vs. chemical cost, injection volume).

4. Integrating MBE with Waterflooding

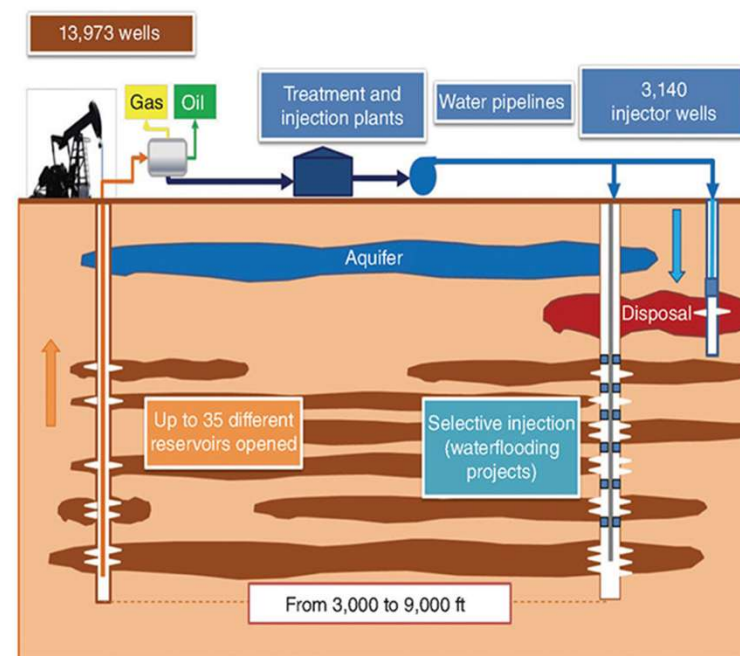


*Screening for EOR Suitability

Waterflooding may reach 80–85% RF in high-quality reservoirs, but **EOR can unlock an additional 5–15% OOIP**, significantly increasing **net recovery and project value**.

For this field:

- Estimated EOR potential = ~2 million STB
- Justifiable for chemical or gas-based EOR depending on reservoir screening.





4. Integrating MBE with Waterflooding

Operational and Engineering Insights from the Correlation

Water Injection Role

Replaces voidage
Maintains pressure
Reduces gas evolution
Alters reservoir saturation
Improves sweep

Impact in Material Balance

Subtracted as $WinjBwi$
Lowers expansion terms on the LHS
Stabilizes R_s , slows GOR rise
Affects recovery efficiency, water cut
Delays water breakthrough if well-pattern optimized

Water injection is not just a production technique, it is an **integral component of reservoir energy balance**. Its role is precisely quantified and monitored using the material balance equation, making MBE a powerful diagnostic and planning tool for waterflooding projects.

When implemented properly and interpreted through MBE analysis, water injection leads to:

- Sustained pressure,
- Extended reservoir life,
- Improved ultimate oil recovery (EUR).

5. How Does Water Injection Improve RF?



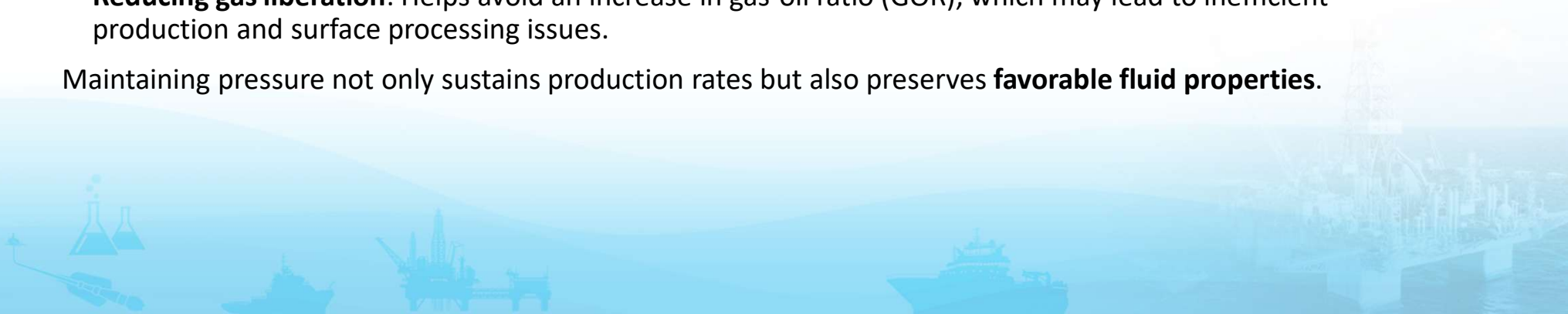
Water injection is one of the most widely applied **secondary recovery techniques** in petroleum engineering. Its main objective is to **maintain reservoir pressure** and **displace oil** toward production wells, thereby **improving the recovery factor** beyond what is possible through natural depletion alone.

A. Mechanism of Pressure Maintenance

As oil is produced, the pressure within the reservoir naturally declines. This reduces the **energy** available to drive fluids toward production wells. Water injection counters this effect by:

- **Repressurizing the reservoir:** Injected water occupies the pore space left by produced fluids, reducing voidage and helping to stabilize pressure.
- **Delaying the onset of bubble-point pressure:** In undersaturated reservoirs, maintaining pressure above the bubble point prevents early gas evolution, preserving reservoir drive and oil mobility.
- **Reducing gas liberation:** Helps avoid an increase in gas-oil ratio (GOR), which may lead to inefficient production and surface processing issues.

Maintaining pressure not only sustains production rates but also preserves **favorable fluid properties**.



5. How Does Water Injection Improve RF?



B. Displacement of Oil (Immiscible Displacement)

Water injection creates a **pressure gradient** from the injection wells toward the production wells. This gradient mobilizes and sweeps oil from the reservoir matrix toward the producing wells.

The displacement process depends on:

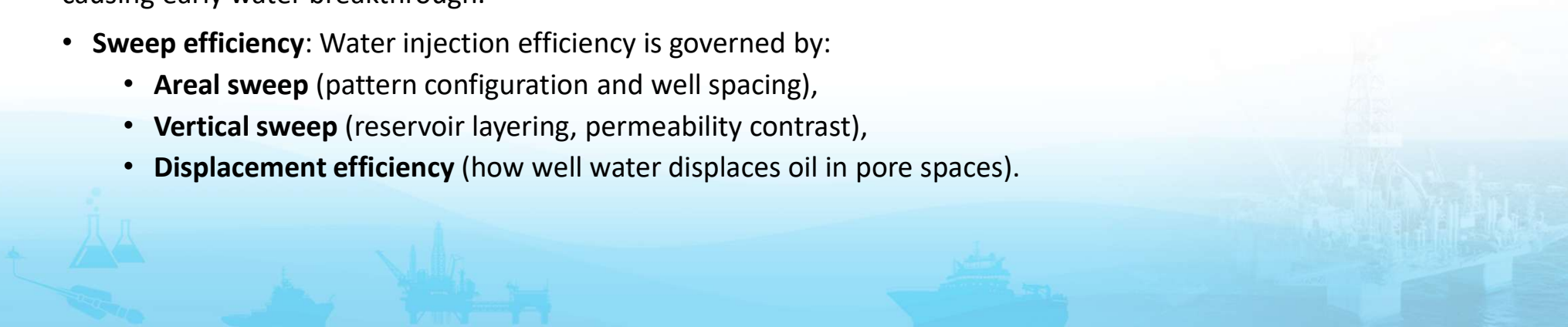
- **Mobility ratio (M):**
$$M = \frac{k_w/\mu_w}{k_o/\mu_o}$$

Where:

- k_w, k_o : relative permeabilities to water and oil
- μ_w, μ_o : viscosities of water and oil

A mobility ratio **less than 1** indicates a stable front and efficient sweep; if **greater than 1**, water will bypass oil, causing early water breakthrough.

- **Sweep efficiency:** Water injection efficiency is governed by:
 - **Areal sweep** (pattern configuration and well spacing),
 - **Vertical sweep** (reservoir layering, permeability contrast),
 - **Displacement efficiency** (how well water displaces oil in pore spaces).



5. How Does Water Injection Improve RF?



C. Improved Oil Recovery Factor

Through these mechanisms, water injection typically boosts recovery in the following way:

- **Primary recovery (natural drive):** ~10–25% of OOIP
- **Secondary recovery (with water injection):** ~30–60% of OOIP, and up to 80% in high-quality reservoirs

The gain in recovery is due to:

- **Extended plateau production period,**
- **Higher pressure support,** reducing the need for artificial lift,
- **Improved volumetric sweep,** especially in homogeneous or well-managed layered reservoirs.



5. How Does Water Injection Improve RF?



D. Delaying Decline Curve Behavior

Water injection extends the **productive life** of a reservoir by delaying:

- **Pressure depletion,**
- **Gas cap expansion and coning,**
- **Water coning from bottom water zones (if injection is properly located)**

This contributes to a **flatter decline curve**, allowing:

- Sustained production rates over time,
- Better infrastructure and investment utilization.



5. How Does Water Injection Improve RF?



E. Real-World Application and Strategic Planning

1. Water injection must be **carefully designed and monitored** to be effective:
 - **Injection rate and pressure** must avoid fracturing,
 - **Injection water quality** must be compatible (to avoid scaling or souring),
 - **Pattern design** (e.g., 5-spot, line drive) must be optimized for reservoir geometry.
2. Monitoring includes:
 - **Water cut trends, injection profiles, and pressure response** at offset wells,
 - Use of **tracers** and **injection conformance** tools to improve efficiency.

Water injection improves oil recovery by:

- Replacing voidage and maintaining reservoir energy,
- Displacing oil through pore systems toward production wells,
- Enhancing sweep efficiency when designed correctly.

It bridges the gap between **primary recovery** and **enhanced oil recovery (EOR)** techniques, often serving as the foundation for further recovery processes such as **chemical (polymer or ASP) or CO₂ injection**.

In a well-managed waterflood, the **Recovery Factor can increase by 20–40% OOIP** beyond primary recovery, making it a powerful tool in modern reservoir engineering.

6. Tracking Voidage with Material Balance



Material Balance Equation as a Diagnostic Tool

The **Material Balance Equation (MBE)** provides a quantitative framework to understand reservoir performance by relating production volumes to pressure, fluid properties, and drive mechanisms. When water injection is applied, it becomes an **explicit term** in the MBE, allowing engineers to:

- Monitor reservoir behavior dynamically,
- Estimate reserves under injection support,
- Diagnose inefficiencies in injection performance.

The general form of the MBE for a waterflooded oil reservoir is:

$$N \cdot E_t = N_p B_o + W_p B_w - W_{inj} B_{wi} - W_e$$

Where:

- N: Original oil in place (OOIP)
- Et: Total expansion term (oil, gas, rock, and water expansion)
- Np, Wp: cumulative oil and water produced
- Winj: cumulative water injected
- We: cumulative water influx from aquifer
- Bo, Bw, Bwi: volume factors

6. Tracking Voidage with Material Balance



Role of Water Injection in the Reservoir Balance

In this equation, **injected water is subtracted**, because it **compensates for produced volume** and helps maintain the pressure:

- It **reduces the need** for fluid expansion to supply produced fluids.
- It **maintains or slows the decline of reservoir pressure**, stabilizing the energy available for oil production.
- It effectively **replaces the voidage** created by oil and water production.

From an MBE viewpoint, water injection directly contributes to sustaining pressure and supporting oil displacement, which is reflected in lower values of E_t for a given cumulative production F .

From the perspective of the Material Balance Equation, **water injection provides measurable, quantifiable value**:

- It replaces lost voidage with injected volume,
- It minimizes pressure decline and energy loss,
- It extends productive life and increases ultimate recovery,
- It enables data-driven decisions for injection optimization.



6. Tracking Voidage with Material Balance



Water Injection Minimizes Pressure Loss

With no injection or aquifer support, the pressure decline is more rapid, leading to:

- Reduced oil mobility (especially near bubble point),
- Increased solution gas production (higher GOR),
- Earlier onset of artificial lift requirements.

With water injection:

- The pressure decline is delayed,
- Oil remains in a more favorable mobility condition,
- Oil recovery improves both in terms of volume and economics.

In MBE, this benefit appears as a **slower increase in E_t** , since expansion terms grow more slowly with stabilized pressure.



6. Tracking Voidage with Material Balance



Enhanced Recovery Evaluation Using MBE

Because water injection volumes and timing are explicitly tracked in MBE, it enables engineers to:

- Forecast **cumulative recovery** under different injection scenarios,
- Determine the **additional recovery** gained due to injection,
- Evaluate the **economic return** of injection operations.

MBE plots (e.g., F vs. E_t) become powerful tools to visualize and estimate:

- OOIP (from the slope),
- The effectiveness of the injection program (through deviations from ideal behavior),
- The need for conformance control or improved sweep.



6. Tracking Voidage with Material Balance



Integration with Other Surveillance Tools

MBE analysis, when combined with:

- Pressure history data,
- Tracer tests,
- Production logging and allocation,

can provide a **clearer picture of injection efficiency**, helping identify issues such as:

- Water channeling or thief zones,
- Early water breakthrough,
- Layered injection imbalances.

This information is critical for reservoir optimization decisions, such as modifying injection patterns, adjusting rates, or moving to enhanced oil recovery (EOR) methods.

In essence, **MBE transforms water injection from a black-box operational input into a transparent, trackable performance parameter**, empowering engineers to manage reservoirs proactively and efficiently.

7. Conclusion



Water injection is a fundamental secondary recovery method that significantly improves oil recovery by maintaining reservoir pressure and displacing hydrocarbons toward production wells. It is particularly effective in mature reservoirs where natural drive mechanisms become insufficient over time.

From a reservoir engineering perspective, water injection:

- **Replaces voidage** caused by fluid production,
- **Delays pressure decline** and maintains reservoir energy,
- **Improves sweep efficiency** and oil displacement,
- Extends the productive life of the field while optimizing recovery.

Using the **Material Balance Equation (MBE)**, water injection can be quantitatively evaluated. MBE allows engineers to:

- Estimate OOIP accurately under injection scenarios,
- Monitor pressure behavior through cumulative production and injection data,
- Calculate **Voidage Replacement Ratio (VRR)** and assess the effectiveness of the waterflood,
- Forecast future recovery and plan injection strategies based on performance indicators.



7. Conclusion



Numerical simulation and plotting of MBE (e.g., F vs. E_t) help visualize how water injection supports reservoir pressure and maximizes hydrocarbon recovery. These tools provide engineers with critical insights to design, monitor, and optimize injection programs efficiently.

Ultimately, when properly planned and executed, water injection is not just a recovery method, it is a **reservoir management strategy** that bridges the gap between primary depletion and enhanced oil recovery (EOR), unlocking the full economic potential of the reservoir.



COSL



"Great things are done by a series of small things brought together."— Vincent van Gogh

Reservoir Engineer Perspective : From initial data, simulation, and chemical formulation to field implementation — each small step makes a significant contribution to the overall success of the project.

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