

d_2, d_2^*, d_2^s calculation

Kujin Tang

1 EX_w, EY_w calculation:

$$EX_w = M(\beta - k + 1)(p_{Xw} + p_{X\bar{w}})$$

$$EY_w = M(\beta - k + 1)(p_{Yw} + p_{Y\bar{w}})$$

$$\widetilde{X}_w = X_w - EX_w$$

$$\widetilde{Y}_w = Y_w - EY_w$$

2 D_2, D_2^*, D_2^s calculation:

$$D_2 = \sum_{w \in A^k} X_w Y_w$$

$$D_2^* = \sum_{w \in A^k} \frac{\widetilde{X}_w \widetilde{Y}_w}{\sqrt{EX_w EY_w}}$$

$$D_2^s = \sum_{w \in A^k} \frac{\widetilde{X}_w \widetilde{Y}_w}{\sqrt{\widetilde{X}_w^2 + \widetilde{Y}_w^2}}$$

3 d_2, d_2^*, d_2^s calculation:

$$d_2 = 1 - \frac{D_2}{\sqrt{\sum_{w \in A^k} X_w^2} \sqrt{\sum_{w \in A^k} Y_w^2}}$$

$$d_2^* = \frac{1}{2} \left(1 - \frac{D_2^*}{\sqrt{\sum_{w \in A^k} \frac{\widetilde{X}_w^2}{EX_w}} \sqrt{\sum_{w \in A^k} \frac{\widetilde{Y}_w^2}{EY_w}}} \right)$$

$$d_2^s = \frac{1}{2} \left(1 - \frac{D_2^s}{\sqrt{\sum_{w \in A^k} \frac{\widetilde{X}_w^2}{\sqrt{\widetilde{X}_w^2 + \widetilde{Y}_w^2}}} \sqrt{\sum_{w \in A^k} \frac{\widetilde{Y}_w^2}{\sqrt{\widetilde{X}_w^2 + \widetilde{Y}_w^2}}} \right)$$