

# Information Filtering

SI650 / EECS549 Information Retrieval

October 8, 2025

Slides adapted from David  
Juergen

# Food for thought: Which Platform has better recommendations?

- Amazon also-purchased
- Spotify songs
- Netflix movies (or Hulu, Apple, Amazon, ...)
- TikTok's For You Page (FYP)
- Twitter trending tweets/topics
- *others?*

# Lecture Plan

- Filtering vs. Retrieval
- Content-based filtering (adaptive filtering)
- Collaborative filtering (recommender systems)
  - How they work
  - Matrix vs network models
  - Latent factor models
  - Even a little deep learning!

# Short vs. Long Term Info Need

- Short-term information need (Ad hoc retrieval)
  - “Temporary need”, e.g., info about used cars
  - Information source is relatively static
  - User “pulls” information
  - Application example: library search, Web search
- Long-term information need (Filtering)
  - “Stable need”, e.g., new data mining algorithms
  - Information source is dynamic
  - System “pushes” information to user
  - Applications: news filter, recommender systems

# Examples of Information Filtering

- News filtering
- Email filtering
- Movie/book recommenders
- Literature recommenders
- And many others ...

# Content-based Filtering vs. Collaborative Filtering

- Basic filtering question: Will user  $U$  like item  $X$ ?
- Two different ways of answering it
  - Look at what  $U$  likes → characterize  $X$  → content-based filtering
  - Look at who likes  $X$  → characterize  $U$  → collaborative filtering
- Can be combined

Collaborative filtering is also called

# “Recommender Systems”

- Content-based filtering is also called
  1. “Adaptive Information Filtering” in TREC
  2. “Selective Dissemination of Information (SDI) in Library & Information Science

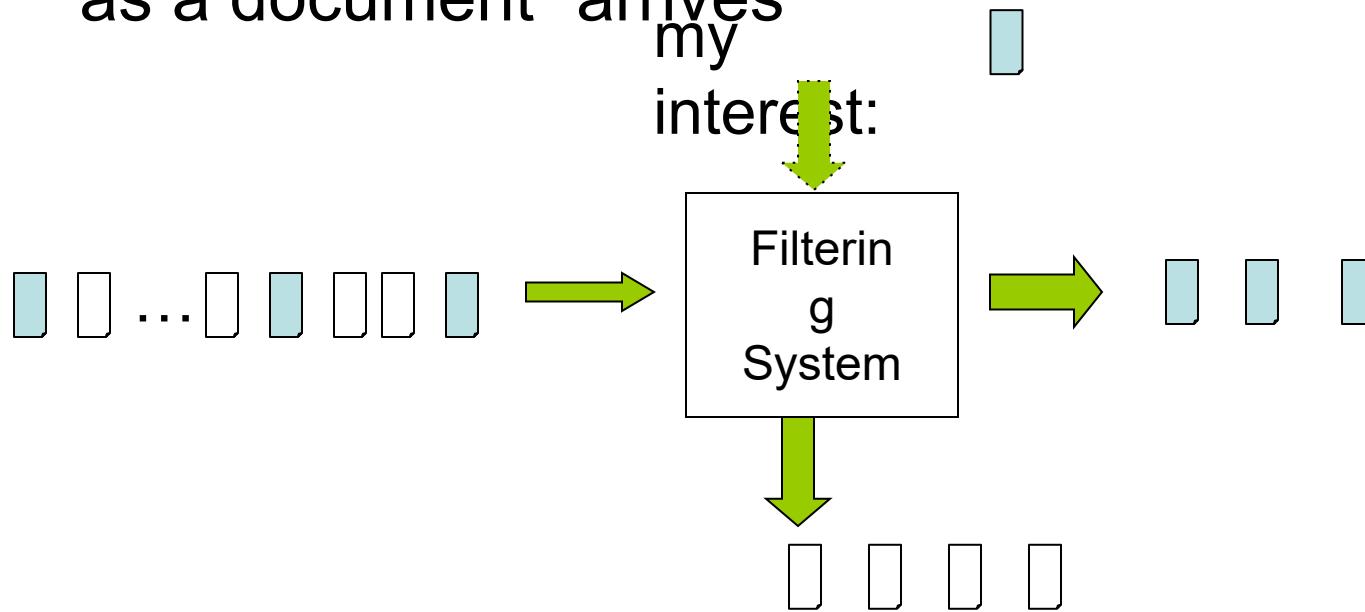
# Why Bother?

- Why do we need recommendation?
- Why should amazon provide recommendation?
- Why does Netflix spend millions to solicit improvement on their recommendation algorithm?
- Why can't we rely on a search engine for all the recommendation?

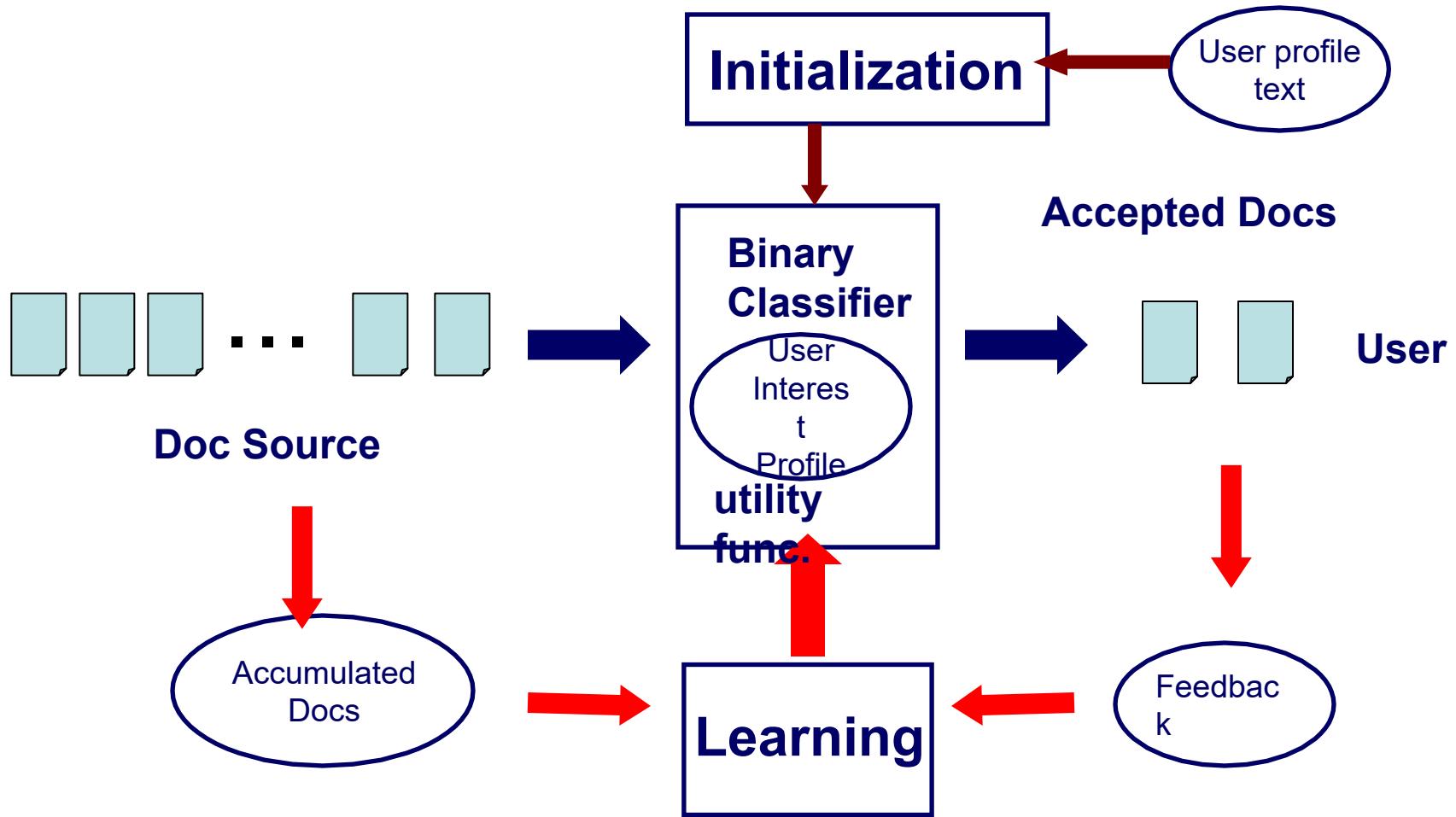
# Part I: Adaptive Filtering

# Adaptive Information Filtering (AIF)

- Stable & long term interest, dynamic information source
- System must make a delivery decision immediately as a document “arrives”



# A Typical AIF System



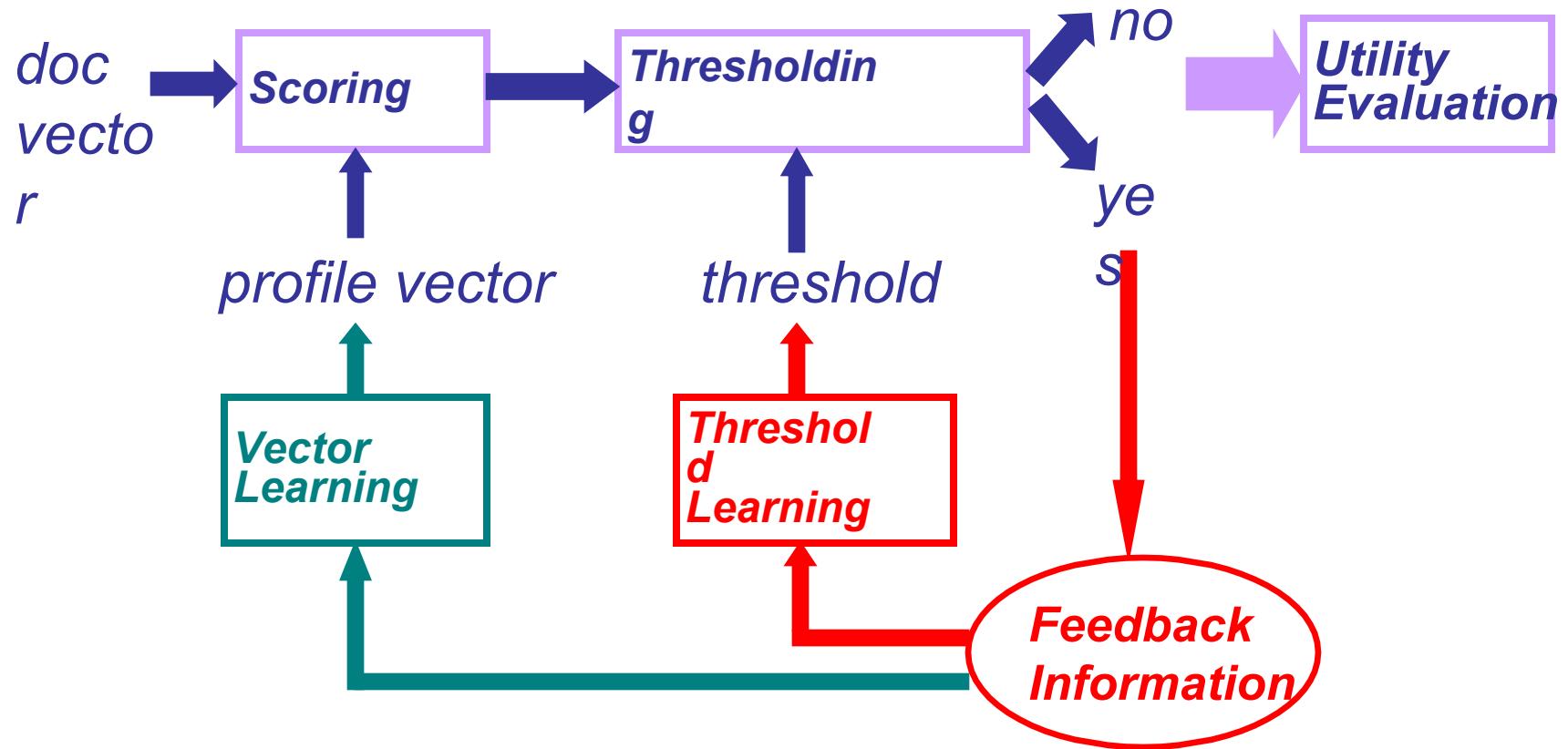
# Three Basic Problems in AIF

- Making filtering decision (Binary classifier)
  - Doc text, profile text → yes/no
- Initialization
  - Initialize the filter based on only the profile text or very few examples
- Learning from
  - Limited relevance judgments (only on “yes” docs)
  - Accumulated documents
- All trying to maximize the utility

# Major Approaches to AIF

- “Extended” retrieval systems
  - “Reuse” retrieval techniques to score documents
  - Use a score threshold for filtering decision
  - Learn to improve scoring with traditional feedback
  - New approaches to threshold setting and learning
- “Modified” categorization systems
  - Adapt to binary, unbalanced categorization
  - New approaches to initialization
  - Train with “censored” training examples

# A General Vector-Space Approach



# Difficulties in Threshold Learning

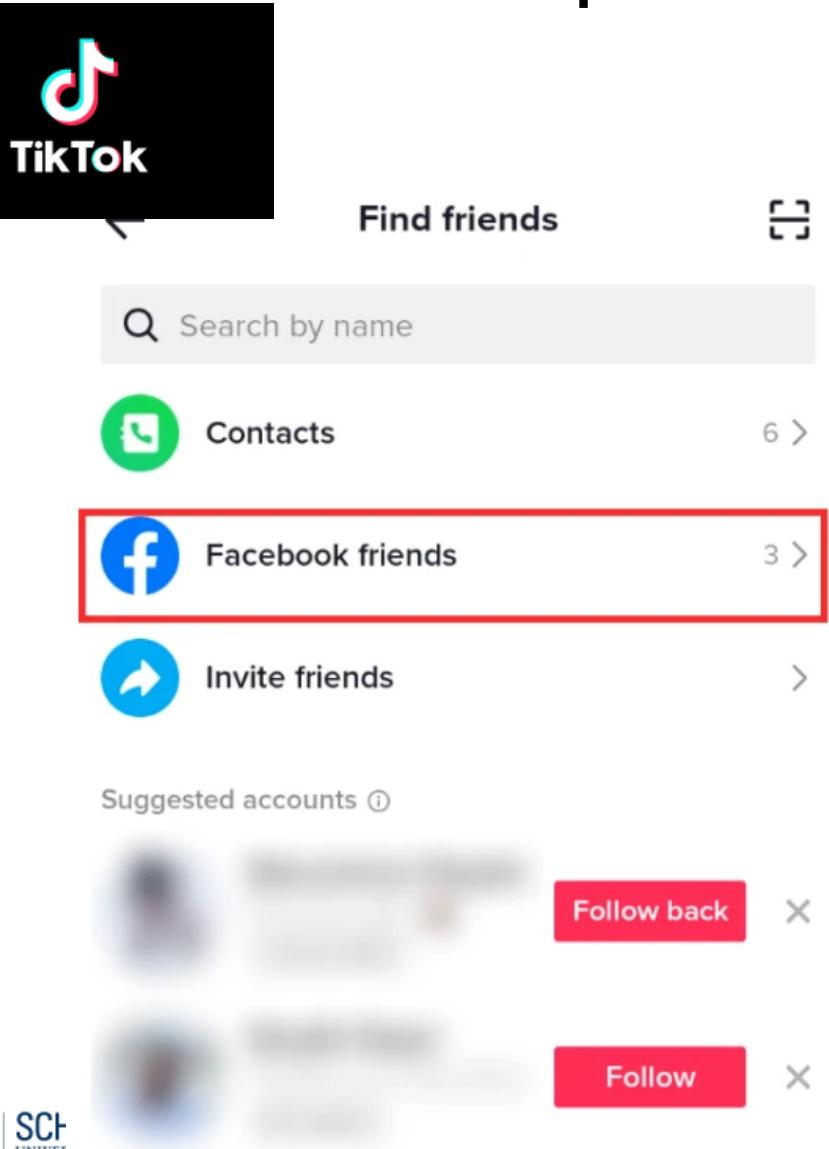
36.5	R
33.4	N
32.1	R
29.9	?
27.3	?
...	
...	

Relevant item  
Not-relevant item

$$\theta=30.0$$

- Censored data
- Little/none labeled data
- Scoring bias due to vector learning
- Exploration vs. Exploitation

# How might platforms identify user preferences?



- Many platforms request information from a user's peers to infer the new user's preferences
- Platforms also *test* on users—explore preferences through specific videos to compare against predictions
- Lots of strategy on identifying user feedback

# Part II: Collaborative Filtering

# What is Collaborative Filtering (CF)?

- Making filtering decisions for an individual user based on the judgments of other users
- Inferring individual's interest/preferences from that of other similar users
- General idea
  - Given a user  $u$ , find similar users  $\{u_1, \dots, u_m\}$
  - Predict  $u$ 's preferences based on the preferences of  $u_1, \dots, u_m$

# CF: Intuitions

- User similarity (*Paul Resnick vs. Rahul Sami*)
  - If Paul liked the paper, Rahul will like the paper
  - If Paul liked the movie, Rahul will like the movie.  
Or will he?
  - Suppose Paul and Rahul viewed similar movies in the past six months ...
- Item similarity
  - Since 90% of those who liked Star Wars also liked Star Trek, and, you liked Star Wars
  - You may also like Star Trek

The content of items “didn’t

# Rating-based vs. Preference-based

- **Rating-based:** User's preferences are encoded using numerical ratings on items
  - Complete ordering
  - Absolute values can be meaningful
  - But, values must be normalized to combine
- **Preference-based:** User's preferences are represented by partial ordering of items  
(Learning to Rank!)
  - Partial ordering
  - Easier to exploit implicit preferences

# Putting Together

Data/Method	User-User CF	Item-Item CF
<b>Using Rating-Based Data</b>	Finds users with similar rating patterns.	Finds items that receive similar ratings from the same users.
<b>Using Preference-Based Data</b>	Finds users who have interacted with a similar set of items.	Finds items that are frequently interacted with by the same users.

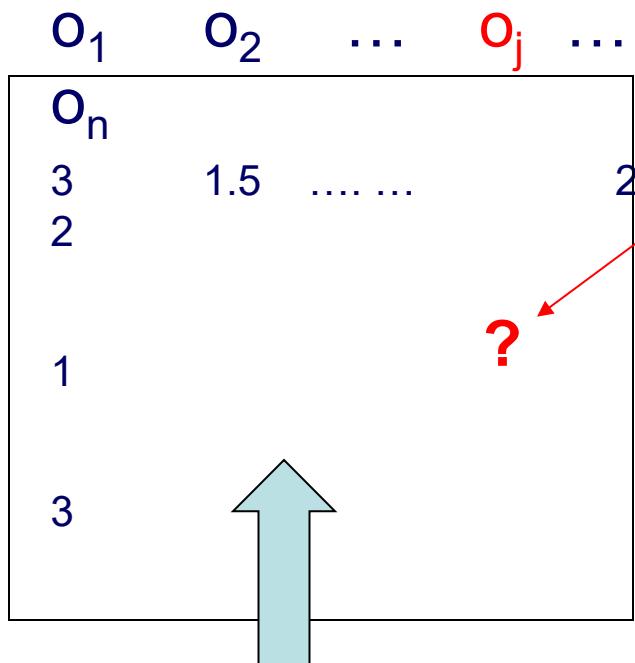
# A Formal Framework for Rating

Objects:  $O$

Users:

$U$

$u_1$   
 $u_2$   
...  
 $u_i$   
...  
 $u_m$



***Unknown function***  
 $f: U \times O \rightarrow R$

$$X_{ij} = f(u_i, o_j) \\ ) = ?$$

**The task**

- Assume known  $f$  values for some  $(u, o)$ 's
- Predict  $f$  values for other  $(u, o)$ 's
- Essentially function approximation, like other learning problems

# Where are the intuitions?

- Similar users have similar preferences
  - If  $u \approx u'$ , then for all o's,  $f(u,o) \approx f(u',o)$
- Similar objects have similar user preferences
  - If  $o \approx o'$ , then for all u's,  $f(u,o) \approx f(u,o')$
- More broadly,
  - If  $u \approx u'$  and  $o \approx o'$ , then  $f(u,o) \approx f(u',o')$
  - “Local smoothness” makes it possible to predict unknown values by interpolation or extrapolation
- What does “local” mean?

# Two Groups of Approaches

- **Memory-based** approaches
  - $f(u, o) = g(u)(o) \approx g(u')(o)$  if  $u \approx u'$   
( $g$  = preference function)
  - Find “neighbors” of  $u$  and combine  $g(u')(o)$ ’s
- **Model-based** approaches (not covered)
  - Assume structures/model: object clusters, user clusters,  $f'$  defined on clusters
  - $f(u, o) = f'(c_u, c_o)$
  - Estimation & Probabilistic inference

# Memory-based Approaches

(Resnick et al. 94)

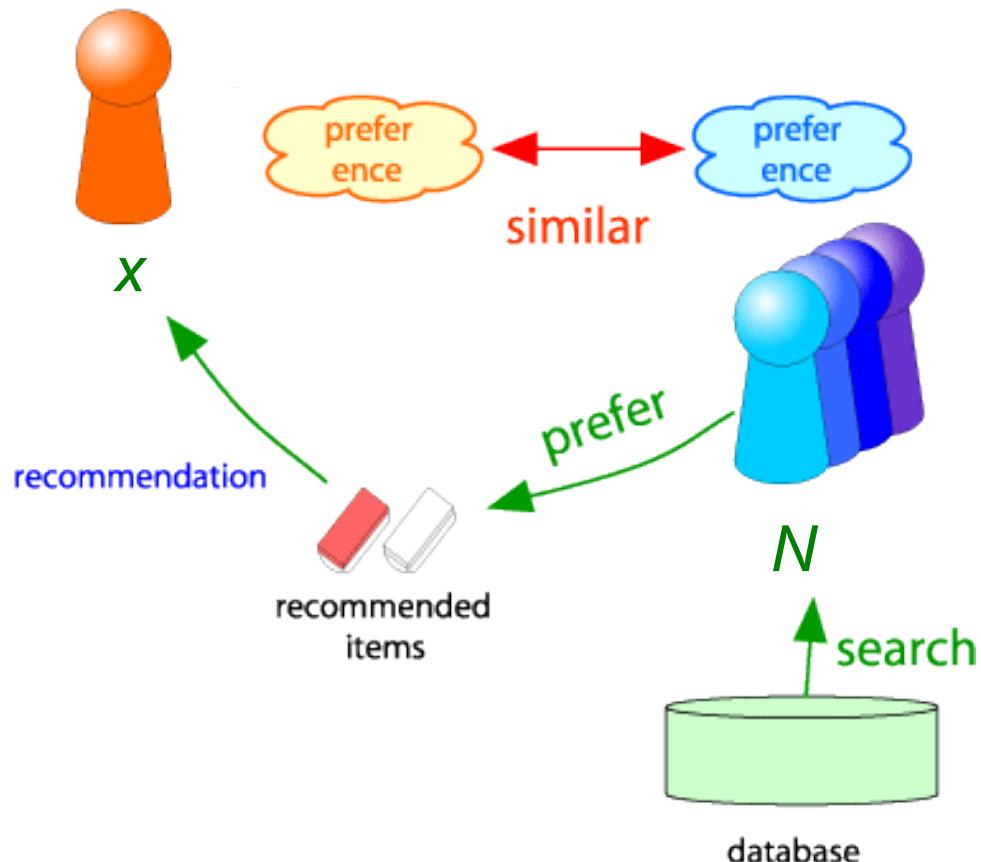
- General ideas:
  - $x_{ij}$ : rating of object j by user i
  - $n_i$ : average rating of all objects by user i
  - Normalized ratings:  $v_{ij} = x_{ij} - n_i$
  - Memory-based prediction

$$v_{dj} = k \sum_{i=1}^m w(a, i) v_{ij} \quad k = 1 / \sum_{i=1}^m w(a, i) \quad \rightarrow \quad x_{aj} = v_{aj} + n_a$$

- Specific approaches differ in  $w(a, i)$  -- the distance/similarity between user a and i

# Collaborative Filtering

- Consider user  $x$
- Find set  $N$  of other users whose ratings are “similar” to  $x$ 's ratings
- Estimate  $x$ 's ratings based on ratings of users in  $N$



# Similarity Metric

	HP1	HP2	HP3	TW	SW1	SW2	SW3
A	4			5	1		
B	5	5	4				
C				2	4	5	
D		3					3

- Intuitively we want:  $\text{sim}(A, B) > \text{sim}(A, C)$
- Jaccard similarity:  $1/5 < 2/4$
- Cosine similarity:  $0.386 > 0.322$ 
  - Considers missing ratings as “negative”
  - Solution: subtract the (row) mean**

	HP1	HP2	HP3	TW	SW1	SW2	SW3
A	2/3			5/3	-7/3		
B	1/3	1/3	-2/3				
C				-5/3	1/3	4/3	
D		0					0

**sim A,B vs.**  
**A,C:**  
 $0.092 > -0.559$   
 Notice cosine sim. is correlation when data is centered at 0

# Finding similar users

- Let  $r_x$  be the vector of user x's ratings
- Jaccard similarity measure
  - Problem: Ignores the values of the rating
- Cosine similarity measure
  - $sim(x, y) = \cos(r_x, r_y) = \frac{r_x \cdot r_y}{\|r_x\| \cdot \|r_y\|}$
  - Problem: Treats missing values as negative
- Pearson correlation coefficient
  - $S_{xy}$  = items rated by both users x and y
  - $sim(x, y) = \frac{\sum_{s \in S_{xy}} (r_{xs} - \bar{r}_x)(r_{ys} - \bar{r}_y)}{\sqrt{\sum_{s \in S_{xy}} (r_{xs} - \bar{r}_x)^2} \sqrt{\sum_{s \in S_{xy}} (r_{ys} - \bar{r}_y)^2}}$

$$r_x = [* , \_, \_, *, * , ***]$$

$$r_y = [* , \_, ** , ** , \_]$$

$r_x, r_y$  as sets:

$$r_x = \{1, 4, 5\}$$

$$r_y = \{1, 3, 4\}$$

$r_x, r_y$  as points:

$$r_x = \{1, 0, 0, 1, 3\}$$

$$r_y = \{1, 0, 2, 2, 0\}$$

$r_x, r_y$  ... avg.  
rating of x, y

# Rating Predictions

- From **similarity metrics** to **recommendations**:
  - Let  $r_x$  be the vector of user  $x$ 's ratings
  - Let  $N$  be the set of  $k$  users most similar to  $x$  who have rated item  $i$
  - Prediction for item  $s$  by user  $x$ 
    - $r_{xi} = \frac{1}{k} \sum_{y \in N} r_{yi}$
    - $r_{xi} = \frac{\sum_{y \in N} s_{xy} \cdot r_{yi}}{\sum_{y \in N} s_{xy}}$
  - Other options?
  - *Many* other tricks possible

# Item-Item Collaborative Filtering

- So far: User-user collaborative filtering
- **Another view:** Item-item
  - For item  $i$ , find other similar items
  - Estimate rating for item  $i$  based on ratings for similar items
  - Can use same similarity metrics and prediction functions as in user-user model

$$r_{xi} = \frac{\sum_{j \in N(i; x)} s_{ij} \cdot r_{xj}}{\sum_{j \in N(i; x)} s_{ij}}$$

$s_{ij}$ ... similarity of items  $i$  and  $j$

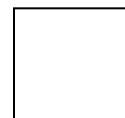
$r_{xj}$ ... rating of user  $u$  on item  $j$

$N(i; x)$ ... set items rated by  $x$  similar to  $i$

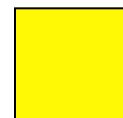
# Item-Item CF ( $|N|=2$ )

users

	12	11	10	9	8	7	6	5	4	3	2	1		
		4			5			5			3		1	1
movies	3	1	2			4			4	5			2	
		5	3	4		3		2	1		4	2	3	
		2			4			5		4	2		4	
	5	2					2	4	3	4			5	
		4			2			3		3		1	6	



- unknown rating



- rating between 1 to 5

# Item-Item CF ( $|N|=2$ )

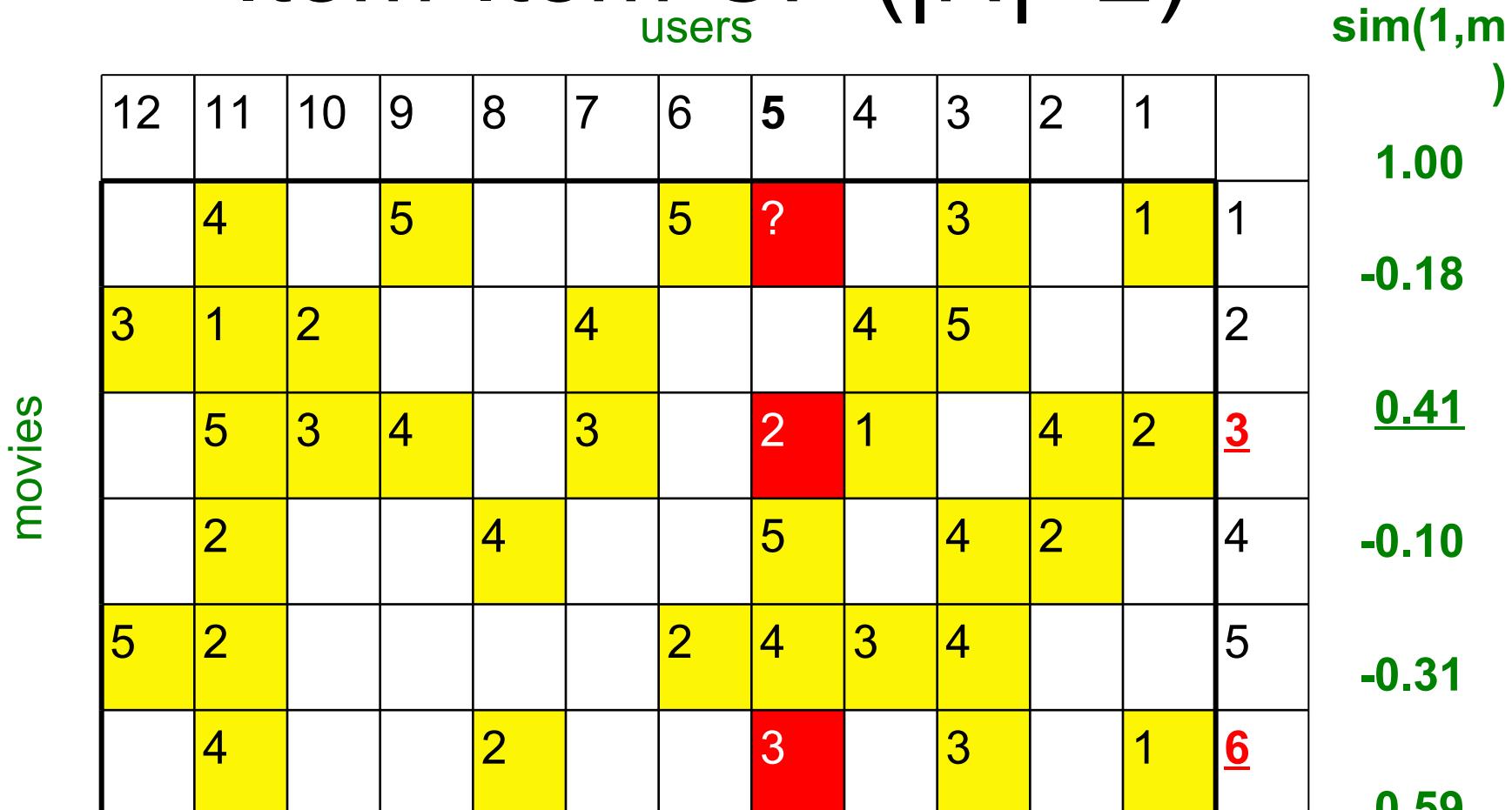
users

	12	11	10	9	8	7	6	5	4	3	2	1	
		4		5			5	?		3		1	1
movies	3	1	2			4			4	5			2
	5	3	4		3			2	1		4	2	3
	2				4			5		4	2		4
	5	2					2	4	3	4			5
	4				2			3		3		1	6



- estimate rating of movie **1** by user **5**

# Item-Item CF ( $|N|=2$ )



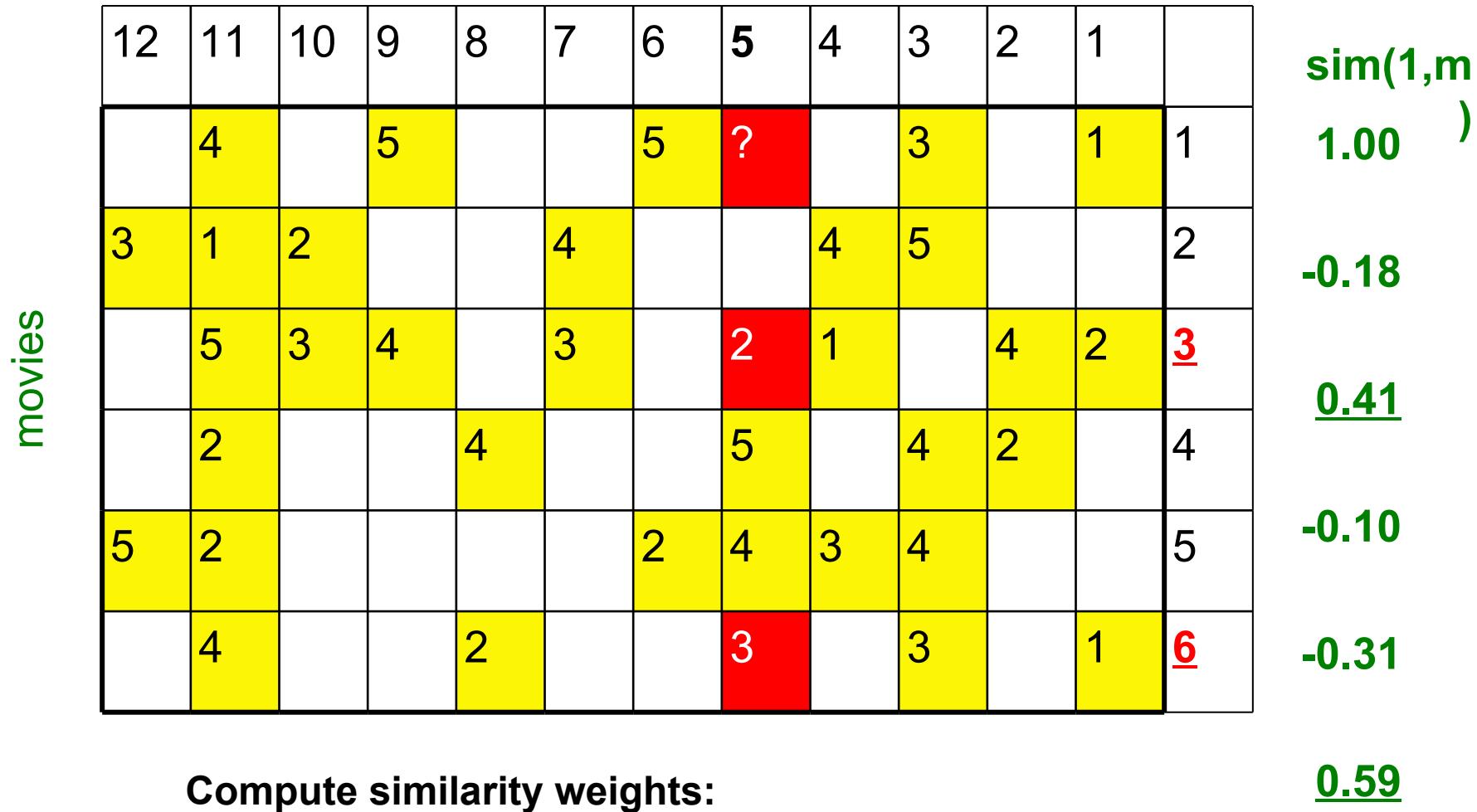
## Neighbor selection:

Identify movies similar to  
movie 1, rated by user 5

Here we use Pearson correlation as similarity:

- 1) Subtract mean rating  $m_i$  from each movie  $i$   
 $m_1 = (1+3+5+5+4)/5 = 3.6$   
 row 1: [-2.6, 0, -0.6, 0, 0, 1.4, 0, 0, 1.4, 0, 0.4, 0]
- 2) Compute cosine similarities between rows

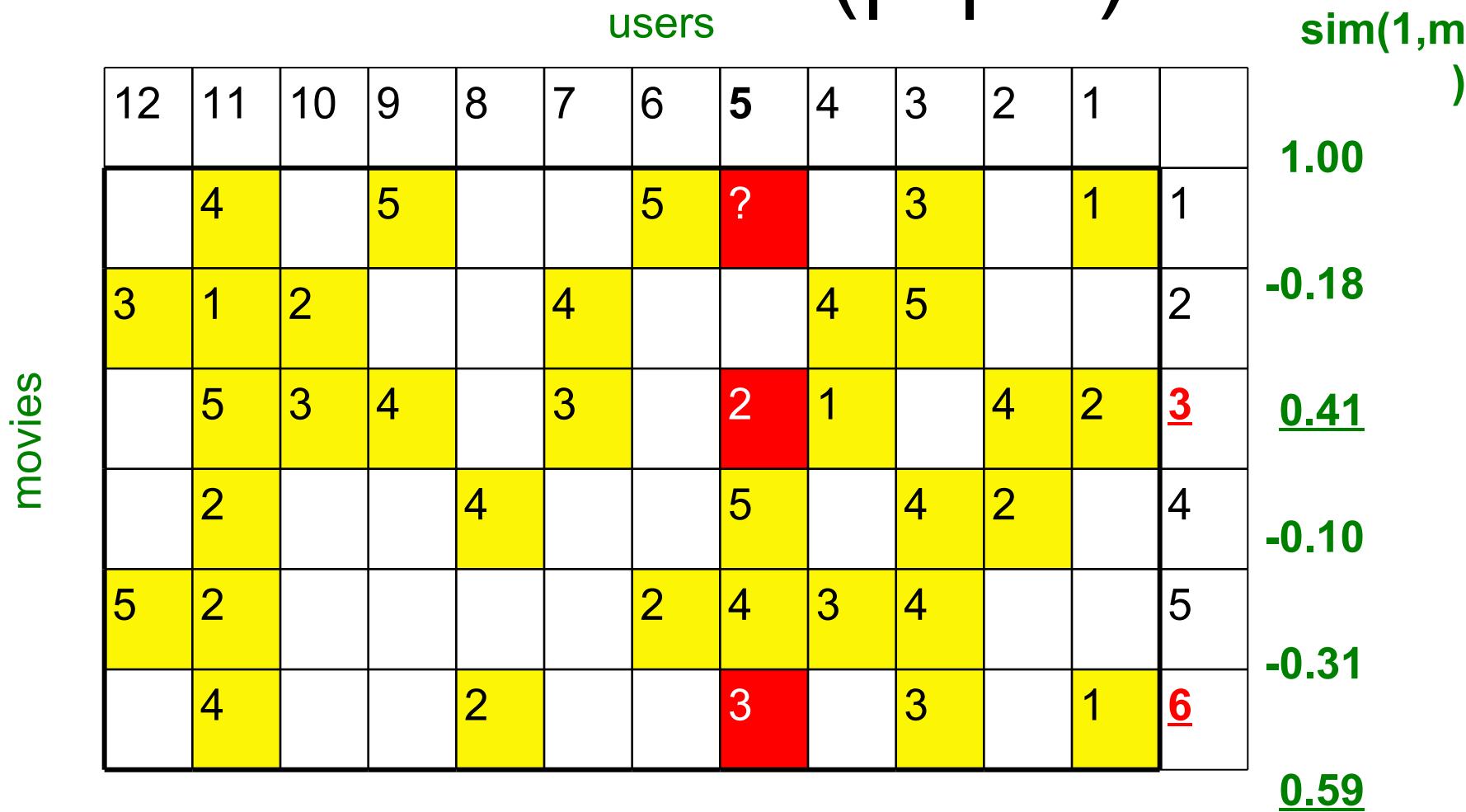
# Item-Item CF ( $|N|=2$ )



Compute similarity weights:

$$s_{1,3}=0.41, s_{1,6}=0.59$$

# Item-Item CF ( $|N|=2$ )



Predict by taking weighted average:

$$r_{1,5} = (0.41 \cdot 2 + 0.59 \cdot 3) / (0.41 + 0.59) = 2.6$$

$$r_{ix} = \frac{\sum_{j \in N(i;x)} s_{ij} \cdot r_{jx}}{\sum s_{ij}}$$

Before:

$$r_{xi} = \frac{\sum_{j \in N(i; x)} s_{ij} r_{xj}}{\sum_{j \in N(i; x)} s_{ij}}$$

# CF: Common Practice

- Define **similarity**  $s_{ij}$  of items  $i$  and  $j$
- Select  $k$  nearest neighbors  $N(i; x)$ 
  - Items most similar to  $i$ , that were rated by  $x$
- Estimate rating  $r_{xi}$  as the weighted average:

$$r_{xi} = b_{xi} + \frac{\sum_{j \in N(i; x)} s_{ij} \cdot (r_{xj} - b_{xj})}{\sum_{j \in N(i; x)} s_{ij}}$$

baseline estimate for  $r_{xi}$

$$b_{xi} = \mu + b_x + b_i$$

- $\mu$  = overall mean movie rating
- $b_x$  = rating deviation of user  $x$   
= (avg. rating of user  $x$ ) –  $\mu$
- $b_i$  = rating deviation of movie  $i$

# Item-Item vs. User-User

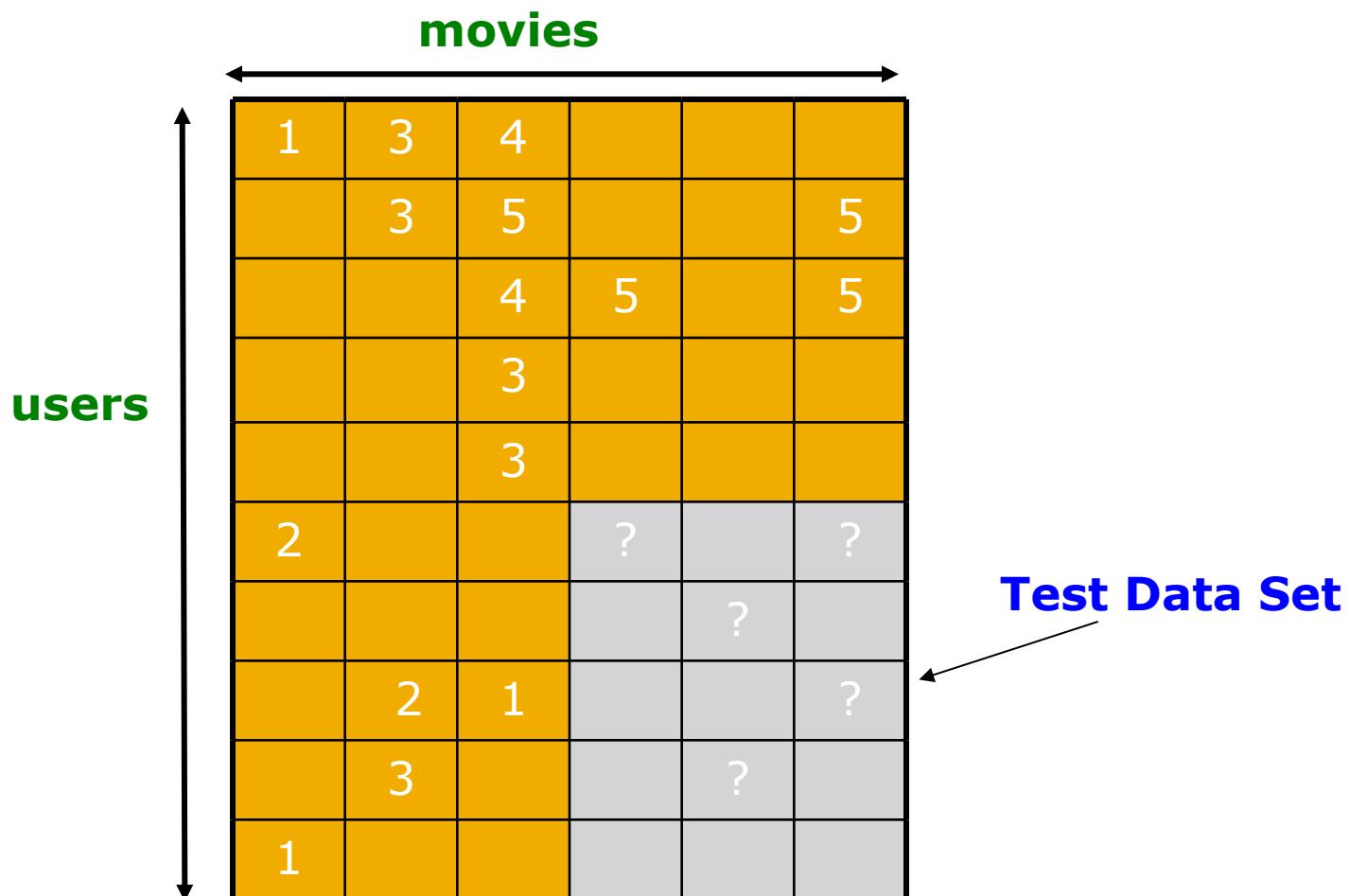
	Marvel	Harry Pot.	Matrix	Pirates
Alice	1		0.8	
Bob		0.5		0.3
Carol	0.9		1	0.8
Rob			1	0.4

- In practice, it has been observed that item-item often works better than user-user. Why?
- Items are simpler, users have multiple tastes

# Evaluation

		movies					
		1	3	4			
			3	5			5
				4	5		5
					3		
					3		
		2			2		2
						5	
			2	1			1
			3			3	
		1					

# Evaluation



# Evaluating Predictions

- **Compare predictions with known ratings**
  - Root-mean-square error (RMSE)
    - where  $r_{xi}$  is predicted and  $r^*_{xi}$  is true rating
  - Prediction@10
    - % of predictions in top 10
  - Rank Correlation
    - Spearman's correlation between system's and user's ranking of items
- **Another approach**: 0/1 model
  - **Coverage**: number of items/users for which the system can make a prediction
  - **Prediction**: Accuracy of ratings
  - **Receiver Operating Character (ROC)**: tradeoff curve between true positives and false negatives

# Pros/Cons of Collaborative Filtering

- + **Works for any kind of item**
  - No feature selection needed
- - **Cold Start:**
  - Need enough users in the system to find a match
- - **Sparsity:**
  - The user/ratings matrix is sparse
  - Hard to find users that have rated the same items
- - **First rater:**
  - Cannot recommend an item that has not been previously rated
  - New items, Esoteric items
- - **Popularity bias:**
  - Cannot recommend items to someone with unique taste
  - Tends to recommend popular items

# Hybrid Methods

- **Implement two or more different recommenders and combine predictions**
  - Perhaps using a linear model
- **Add content-based methods to collaborative filtering**
  - Item profiles for new item problem
  - Demographics to deal with new user problem

# Tip: Add Data

- **Leverage all the data**
  - Don't try to reduce data size in an effort to make fancy algorithms work
  - Simple methods on large data do best
- **Add more data**
  - e.g., add IMDB data on genres
- **More data beats better algorithms**

<http://anand.typepad.com/datawocky/2008/03/more-data-usual.html>

# **Latent Factor Modeling**

**and the Netflix Prize**

# The Netflix Prize

- Training data
  - 100M ratings, 480K users, 17,770 movies
  - 6 years of data: 2000-2005
- Test data
  - Last few ratings of each user (2.8M)
  - Evaluation criterion: Root Mean Squared Error (RMSE)

$$= \frac{1}{|R|} \sqrt{\sum_{(i,x) \in R} (\hat{r}_{ix} - r_{ix})^2}$$

- Competition: 2,700+ teams
- \$1 million prize for 10% improvement over Netflix's method

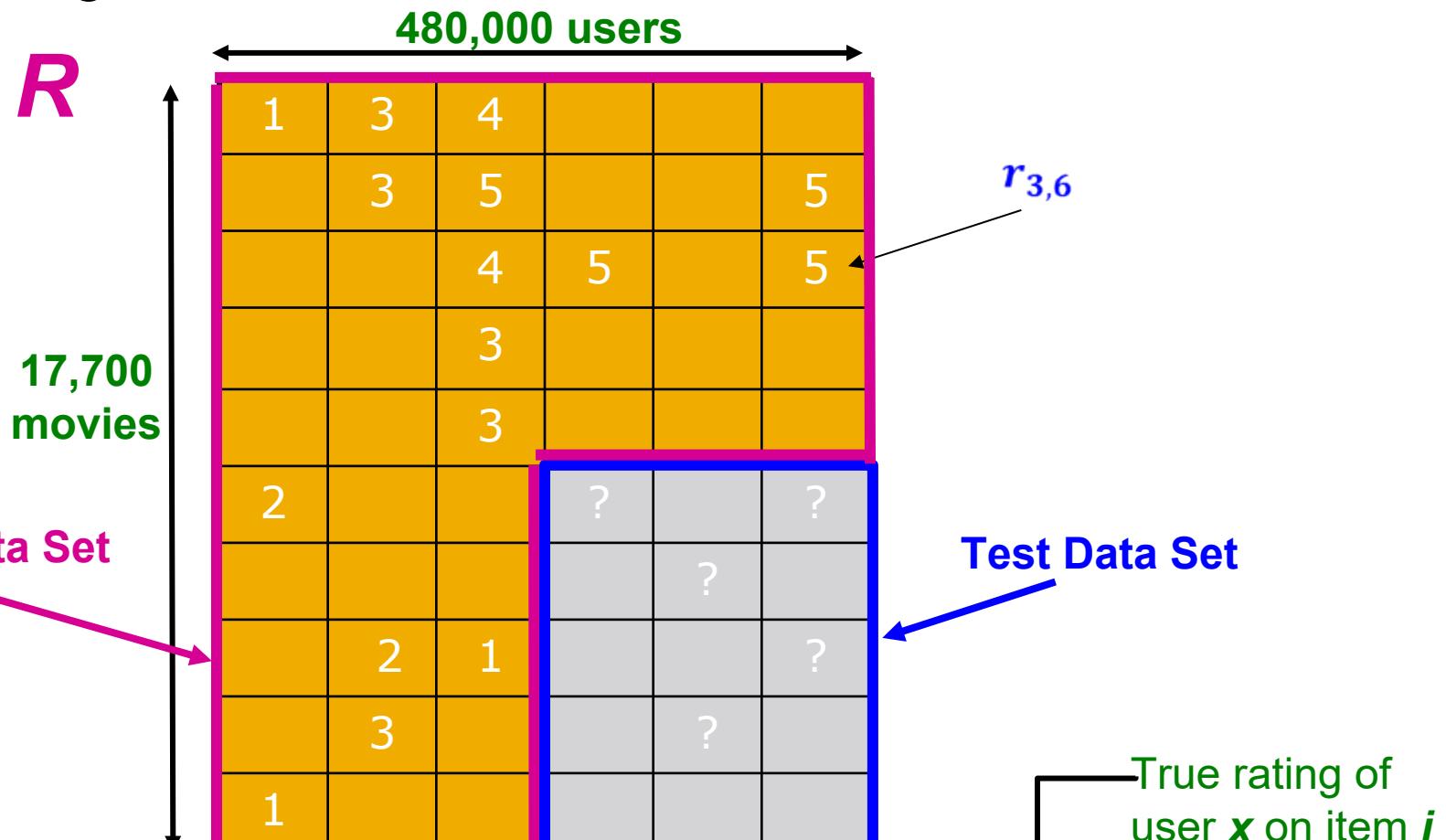
# The Netflix Utility Matrix $R$

**Matrix  $R$**

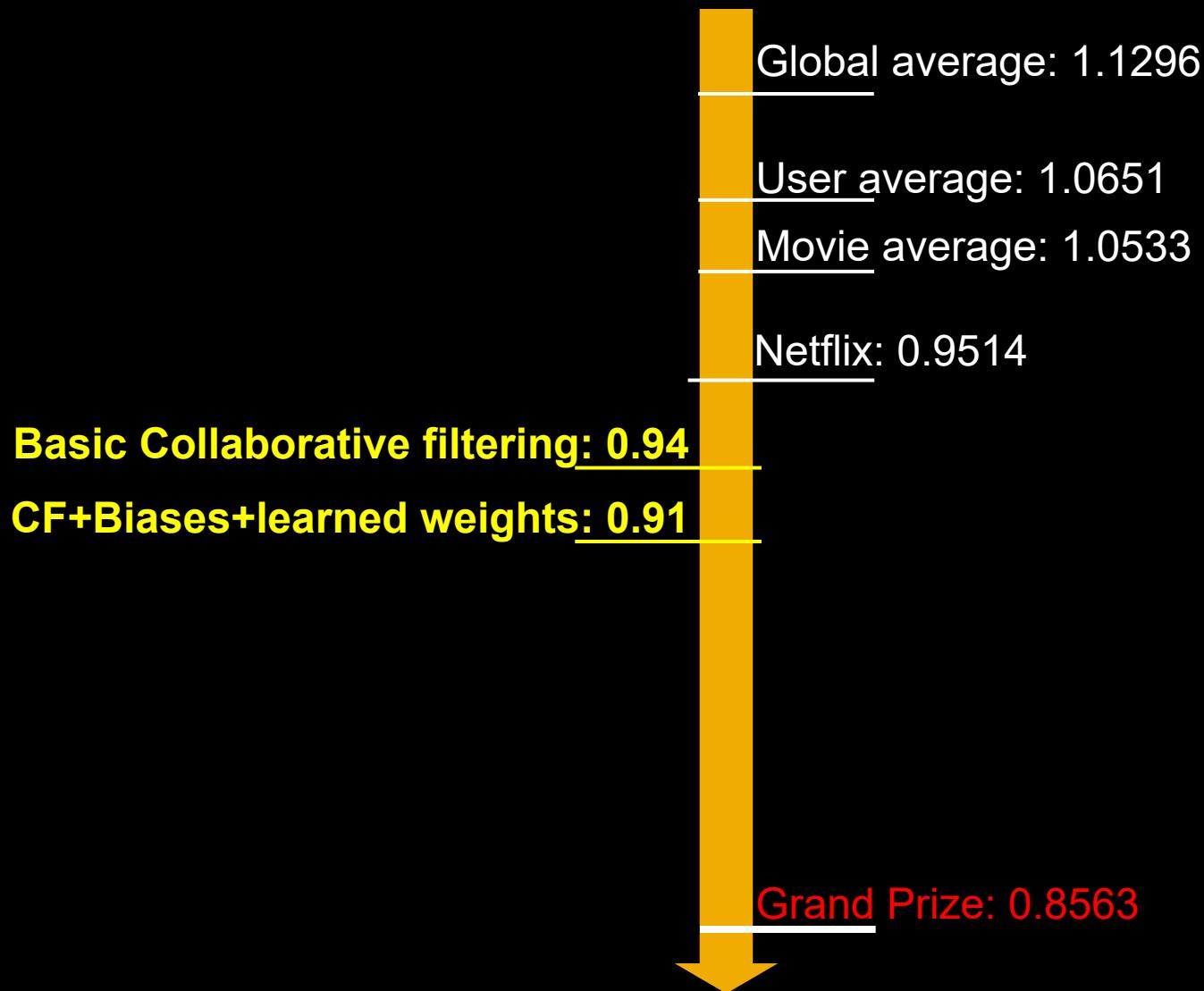
480,000 users					
17,700 movies	1	3	4		
		3	5		5
			4	5	
				3	
				3	
	2			2	2
					5
		2	1		1
			3		3
	1				

# Utility Matrix $R$ : Evaluation

**Matrix  $R$**



$$\text{RMSE} = \frac{1}{|R|} \sqrt{\sum_{(i,x) \in R} (\hat{r}_{xi} - r_{xi})^2}$$

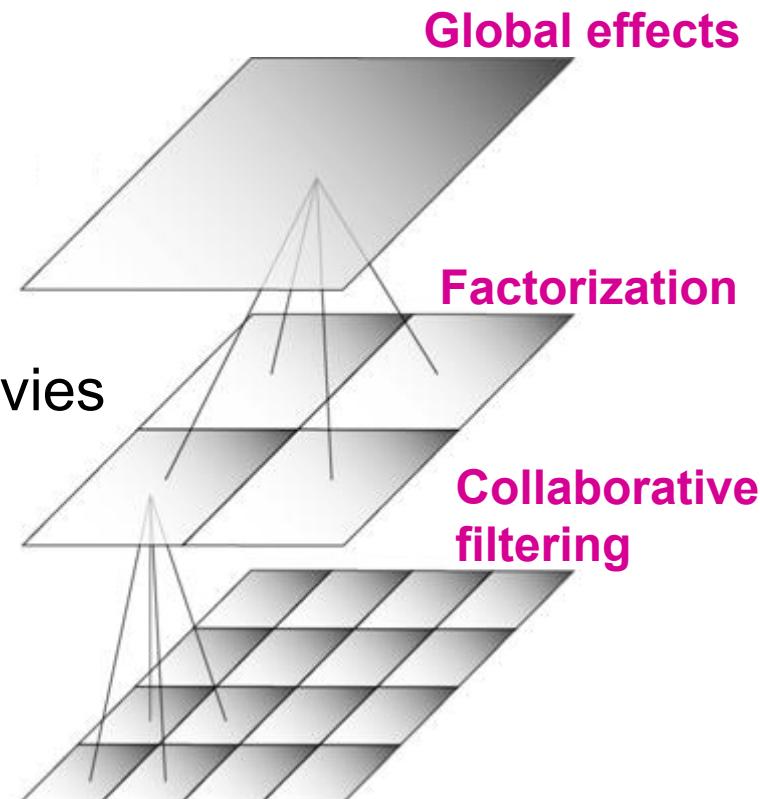


# BellKor Recommender System

- The winner of the Netflix Challenge!
- Multi-scale modeling of the data:

Combine top level, “regional” modeling of the data, with a refined, local view:

- Global:
  - Overall deviations of users/movies
- Factorization:
  - Addressing “regional” effects
- Collaborative filtering:
  - Extract local patterns



# Modeling Local & Global Effects

- In practice we get better estimates if we model *deviations*:

$$\hat{r}_{xi} = b_{xi} + \frac{\sum_{j \in N(i;x)} s_{ij} \cdot (r_{xj} - b_{xj})}{\sum_{j \in N(i;x)} s_{ij}}$$

baseline estimate for  $r_{xi}$

$$b_{xi} = \mu + b_x + b_i$$

$\mu$  = overall mean rating

$b_x$  = rating deviation of user  $x$   
= (avg. rating of user  $x$ ) –  $\mu$

$b_i$  = (avg. rating of movie  $i$ ) –  $\mu$

## Problems/Issues:

- Similarity measures are “arbitrary”
- Pairwise similarities neglect interdependencies among users
- Taking a weighted average can be restricting

**Solution:** Instead of  $s_{ij}$  use  $w_{ij}$  that we estimate directly from data

# Idea: Interpolation Weights $w_{ij}$

- Use a **weighted sum** instead of a **weighted average**

$$\hat{r}_{xi} = b_{xi} + \sum_{j \in N(i;x)} w_{ij} (r_{xj} - b_{xj})$$

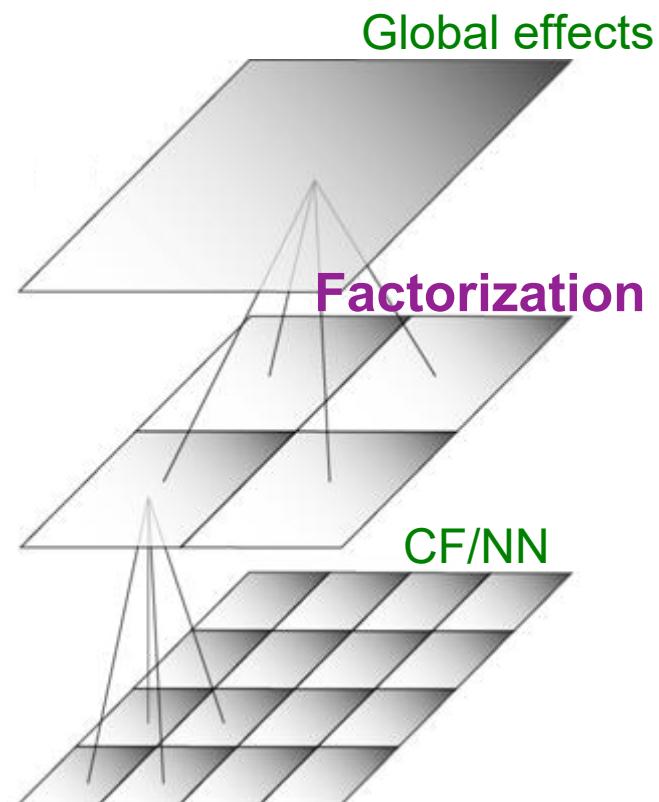
- A few notes:
  - $N(i;x)$  is the set of movies rated by user  $x$  that are similar to movie  $i$
  - $w_{ij}$  is the interpolation weight (some real number)
    - we allow  $\sum_{j \in N(i;x)} w_{i,j} \neq 1$
    - $w_{ij}$  models interactions between pairs of movies (it does not depend on user  $x$ )

# Idea: Interpolation Weights $w_{ij}$

- $\hat{r}_{xi} = b_{xi} + \sum_{j \in N(i,x)} w_{ij} (r_{xj} - b_{xj})$
- How to set  $w_{ij}$ ?
  - Remember, error metric is:  $\frac{1}{|R|} \sqrt{\sum_{(i,x) \in R} (\hat{r}_{xi} - r_{xi})^2}$
  - or equivalently SSE:  $\sum_{(i,x) \in R} (\hat{r}_{xi} - r_{xi})^2$

# Interpolation weights

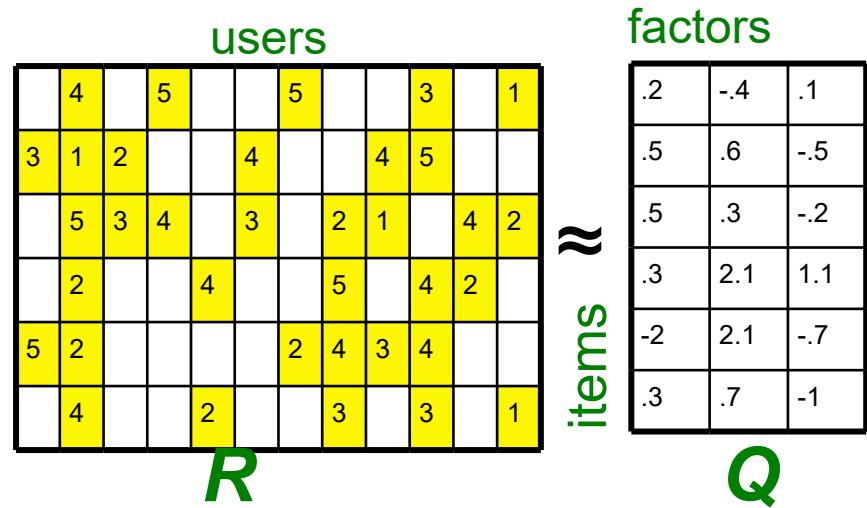
- So far:  $\hat{r}_{xi} = b_{xi} + \sum_{j \in N(i; x)} w_{ij}(r_{xj} - b_{xj})$ 
  - Weights  $w_{ij}$  are derived based on their role
    - no use of an arbitrary similarity measure ( $w_{ij} \neq s_{ij}$ )
  - We are explicitly accounting for interrelationships among the neighboring movies
- Next: **Latent Factor Models**
  - Extract *regional* correlations



# Latent Factor Models

$$\text{SVD: } A = U \Sigma V^T$$

- “SVD” on Netflix data:  $\mathbf{R} \approx \mathbf{Q} \cdot \mathbf{P}^T$



# Ratings as Products of Factors

- How to estimate the missing rating of user  $x$  for item  $i$ ?

		users									
		item 1					item 2				
item 1	item 2	4	5	5	5	3	1	4	5	4	2
		3	1	2	?	4		2	1	4	2
item 1	item 2	5	3	4	3		2	1		4	2
		2		4		5		4	2		
item 1	item 2	5	2			2	4	3	4		
		4		2		3		3		1	

≈

$$\hat{r}_{xi} = \mathbf{q}_i \cdot \mathbf{p}_x$$

$$= \sum_f \mathbf{q}_{if} \cdot \mathbf{p}_{xf}$$

$\mathbf{q}_i$  = row  $i$  of  $\mathbf{Q}$   
 $\mathbf{p}_x$  = column  $x$  of  $\mathbf{P}^T$

		items			factors	
		.2	-.4	.1		
items	factors	.5	.6	-.5		
		.5	.3	-.2		
		.3	2.1	1.1		
		-2	2.1	-.7		
		.3	.7	-1		

$\mathbf{Q}$

users											
-.9	2.4	1.4	.3	-.4	.8	-.5	-2	.5	.3	-.2	1.1
1.3	-.1	1.2	-.7	2.9	1.4	-1	.3	1.4	.5	.7	-.8
.1	-.6	.7	.8	.4	-.3	.9	2.4	1.7	.6	-.4	2.1

$\mathbf{P}^T$

# Ratings as Products of Factors

- How to estimate the missing rating of user  $x$  for item  $i$ ?

		users								
		4	5	5	5	3	1			
items	3	1	2	1.7		4	5			
	5	3	4	3	2	1	4	2		
2			4		5		4	2		
5	2			2	4	3	4			
4			2		3		3			1

≈

$$\hat{r}_{xi} = q_i \cdot p_x$$

$$= \sum_f q_{if} \cdot p_{xf}$$

$q_i$  = row  $i$  of  $Q$

$p_x$  = column  $x$  of  $P^T$

items		
factors		
.2	-.4	.1
.5	.6	-.5
.5	.3	-.2
.3	2.1	1.1
-2	2.1	-.7
.3	.7	-1

• factors

Q

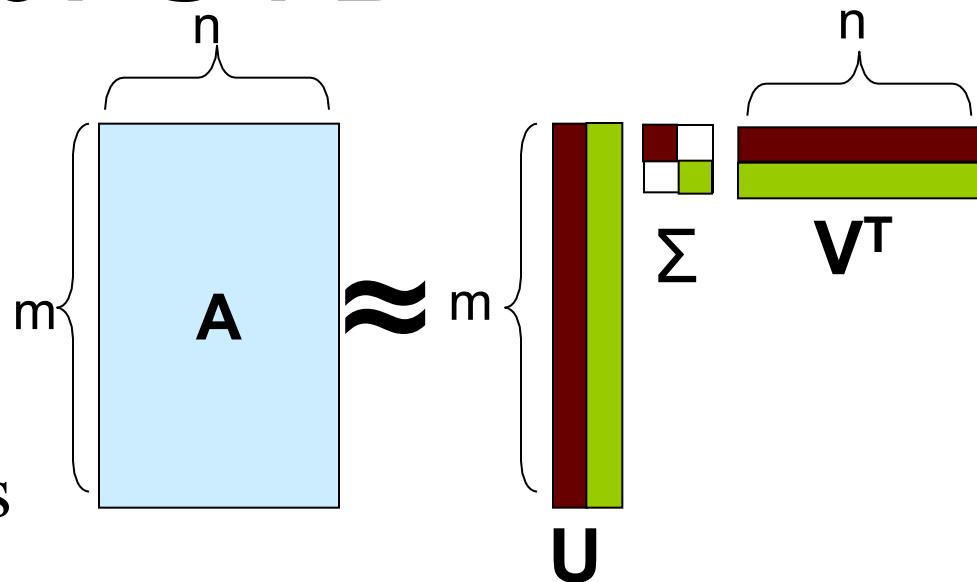
users											
-.9	2.4	1.4	.3	-.4	.8	-.5	-2	.5	.3	-.2	1.1
1.3	-.1	1.2	-.7	2.9	1.4	-1	.3	1.4	.5	.7	-.8
.1	-.6	.7	.8	.4	-.3	.9	2.4	1.7	.6	-.4	2.1

$P^T$

# Recap: SVD

- **Remember SVD:**

- $\mathbf{A}$ : Input data matrix
- $\mathbf{U}$ : Left singular vecs
- $\mathbf{V}^T$ : Right singular vecs
- $\Sigma$ : Singular values



- **So in our case:**

“SVD” on Netflix data:  $R \approx Q \cdot P^T$

$$A = R, \quad Q = U, \quad P^T = \Sigma V^T$$

$$\hat{r}_{xi} = q_i \cdot p_x$$

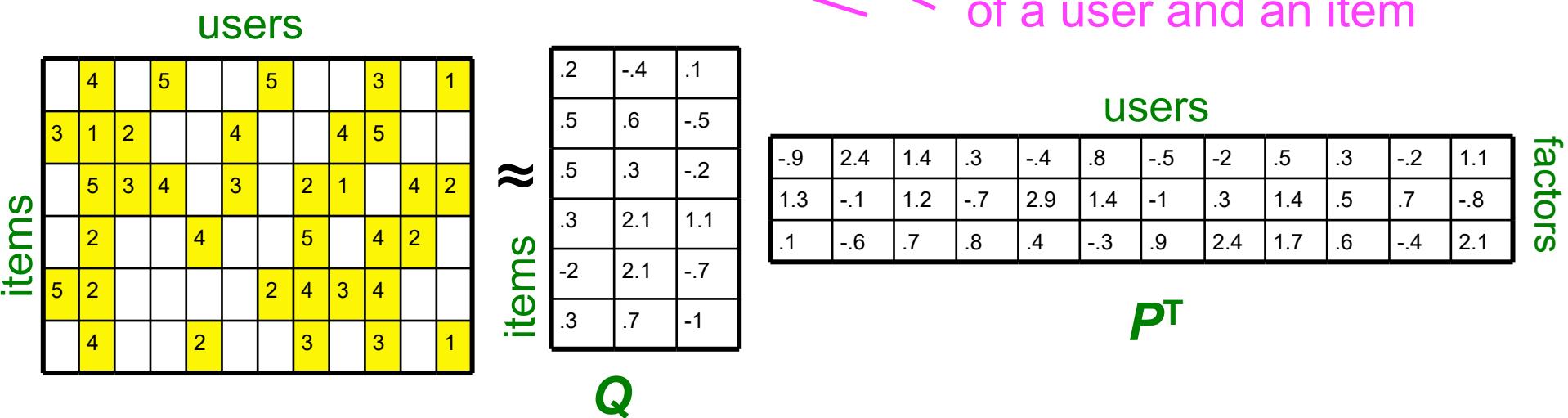
# Finding the Latent Factors

# Latent Factor Models

- Our goal is to find P and Q such that

$$\min_{P,Q} \sum_{(i,x) \in R} (r_{xi} - q_i \cdot p_x)^2$$

vector representations  
of a user and an item



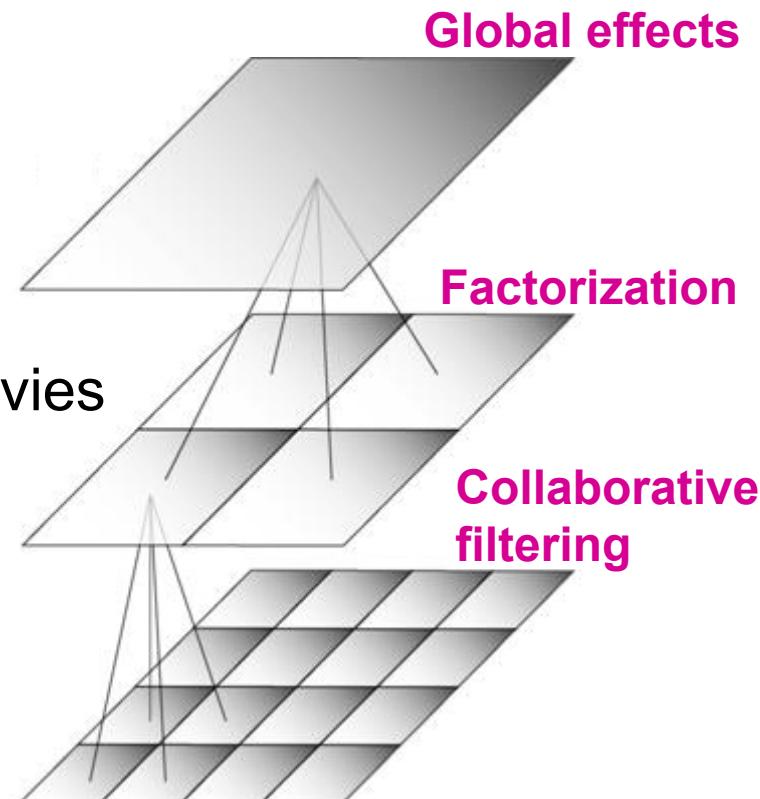
- High level idea: Initialize P and Q using the initial matrix with the zeros and apply SGD.

# BellKor Recommender System

- The winner of the Netflix Challenge!
- Multi-scale modeling of the data:

Combine top level, “regional” modeling of the data, with a refined, local view:

- Global:
  - Overall deviations of users/movies
- Factorization:
  - Addressing “regional” effects
- Collaborative filtering:
  - Extract local patterns



# What you should know

- What are the different types of filtering
- What are the challenges of adaptive filtering
- What are the challenges of collaborative filtering
- How to compare users and items
- Simple methods for implementing collaborative filtering