

STATS FORMULAS

$$\text{Variance: } s^2 = \frac{1}{n-1} \sum_{i=1}^n (y_i - \bar{y})^2$$

$$\text{STD: } s = \sqrt{s^2}$$

$$\text{Permutation: } P_r^n = \frac{n!}{(n-r)!}$$

$$\text{Combination: } C_r^n = \frac{n!}{r!(n-r)!}$$

$$\text{Probability of Intersection of Two Events: } P(A \cap B) = P(A)P(B|A), P(B)P(A|B)$$

$$\text{Chance of A and B occurring relative to S: } P(A|B) = \frac{P(A \cap B)}{P(B)}$$

If A and B are independent:

$$P(A|B) = P(A)$$

$$P(B|A) = P(B)$$

$$P(A \cap B) = P(A)P(B)$$

Dependent: $P(A) * P(B|A)$

General Addition Rule: A or B occurring relative to S

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

A and B are mutually exclusive, $P(A \cap B) = 0$: $P(A \cup B) = P(A) + P(B)$

$$\text{Total Probability: } P(A) = \sum_{i=1}^n P(A|B_i)P(B_i)$$

$$\text{Bayes' Theorem with } P(A) > 0 \text{ and } P(B) > 0: P(B|A) = \frac{P(A|B)P(B)}{P(A)}$$

$$\text{If } 0 < P(B) < 1: P(B|A) = \frac{P(A|B)P(B)}{P(A|B)P(B) + P(A|B')P(B')}$$

$$\text{Probability Mass Function: } p(y) = P(Y = y)$$

$$\text{Expected: } E(Y) = 1/p$$

$$\text{Variance: } \frac{1-p}{p^2}$$

$$\text{Binomial Distribution: } p(y) = \binom{n}{y} p^y q^{n-y}$$

$$\text{Geometric Distribution: } p(y) = P(Y = y) = q^{y-1}p$$

$$\text{Success occurs on or before } n\text{th trial: } P(X \leq n) = 1 - (1 - p)^n$$

$$\text{Success occurs before the } n\text{th trial: } P(X < n) = 1 - (1 - p)^{n-1}$$

$$\text{Success occurs on or after } n\text{th trial: } P(X \geq n) = (1 - p)^{n-1}$$

$$\text{Success occurs after the } n\text{th trial: } P(X > n) = (1 - p)^n$$

Hypergeometric Probability Distribution: $p(y) = \frac{\binom{r}{y} \binom{N-r}{n-y}}{\binom{N}{n}}$

Poisson Probability Distribution: $p(y) = \frac{\lambda^y}{y!} e^{-\lambda}$

Expected value of continuous random variable Y: $E(Y) = \int_{-\infty}^{\infty} y f(y) dy$

Variance of continuous random variable = $E(Y^2) - E(Y)^2$

Uniform Probability Distribution: $f(y) = \begin{cases} \frac{1}{\theta_2 - \theta_1}, & \theta_1 \leq y \leq \theta_2, \\ 0, & \text{elsewhere.} \end{cases}$

Normal Probability Distribution: $f(y) = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(y-\mu)^2}{2\sigma^2}}, -\infty < y < \infty$

Gamma Probability Distribution: $f(y) = \begin{cases} \frac{y^{\alpha-1} e^{-\frac{y}{\beta}}}{\beta^{\alpha} \Gamma(\alpha)} \\ 0, & \text{elsewhere} \end{cases}$

Exponential distribution with parameter $\beta > 0$: $\begin{cases} \frac{1}{\beta} e^{-\frac{y}{\beta}}, & 0 \leq y < \infty, \\ 0, & \text{elsewhere} \end{cases}$

Beta Probability Distribution: $f(y) = \begin{cases} \frac{y^{\alpha-1} (1-y)^{\beta-1}}{B(\alpha, \beta)}, & 0 \leq y \leq 1, \\ 0, & \text{elsewhere} \end{cases}$

Testing if Y_1 and Y_2 are jointly continuous random variables:

$$\int_{y_2}^{y_1} f(t_1, t_2) dt_2 dt_1$$

Conditional discrete probability function: $p(y_1|y_2) = \frac{p(y_1, y_2)}{p_2(y_2)}$

Showing that Y_1 and Y_2 are independent given a density function $f(y_1, y_2)$:

$$f_1(y_1) = \int_{-\infty}^{\infty} f(y_1, y_2) dy_2$$

$$f_2(y_2) = \int_{-\infty}^{\infty} f(y_1, y_2) dy_1$$

$$f(y_1, y_2) = f_1(y_1)f_2(y_2)$$