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TECHNICAL REPORT

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ChantLab: Gregorian Chant Analytics

Institute of Formal and Applied Linguistics

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Contents

Introduction

Welcome to the documentation of ChantLab, a tool for computational analysis of Gregorian Chant!

Gregorian chant, a subset of mostly medieval music, is of great interest for many musicologists, as it is a foundational body of music and has had a substantial impact on European culture. One of the most interesting problems regarding Gregorian chant is its evolution across centuries. Discovering related chants, and, conversely, unrelated ones, is a necessary step in the handling of the problem, after expert selection of the set of chants to compare. Computational methods may help with this step, as it requires aligning large amounts of chants. While there exist large databases of digitalized chants, digital musicology lacks the software necessary to perform this step. This thesis presents a software tool that can help in the discovery of related chants using *multiple sequence alignment* (MSA) algorithms, methods borrowed from bioinformatics. It enables researchers to align arbitrary sets of related (and unrelated) chants, thus revealing clusters of related melodies. Additionally, it facilitates the discovery of contrafacta and transpositions. Nevertheless, the tool has some limitations: it is run locally and some of its interactive functionality becomes slow when processing hundreds of data. Further development is planned as part of an ongoing collaboration with digital musicology researchers from the Czech Academy of Sciences and the Faculty of Arts of Charles University.

Figure 1: An example of chants as inscribed in manuscripts.

The tool, available online[1][2], provides the ability to align a a potentially large and diverse set of chants in multiple ways, each of which has slightly different uses. One important implication of the tool is that it makes the discovery contrafacta (chants with the same melody but different lyrics) and transpositions (chants with the same melody but shifted by an interval) across large repertoires easy. A demo server is deployed at `https://chantlab.mua.cas.cz`. Note that while the CantusCorpus v0.2 dataset is made available as part of the installation, the use can – and is expected to – upload their own datasets.

In this document, we provide the user documentation (sec. 2), we describe the dataset and dataset format (sec. 3), the Multiple Sequence Alignment methods used in the background (sec. 4), and finally we provide development documentation (sec. 5). Note that ChantLab is under active development – this document might not always be 100 % up-to-date. In any case, address your communication to `hajic@mua.cas.cz`.

[1]`https://github.com/Genome-of-Melody/chantlab_frontend`

[2]`https://github.com/Genome-of-Melody/chantlab_backend`

1. Installation instructions

ChantLab is designed to work as locally-run web application. Once running, it can be accessed via a web browser by navigating to the corresponding localhost URL (typically `localhost:4200`, see below). A deployed online instance is available at `https://chantlab.mua.cas.cz`. This page is a relatively low-performance demo server; we recommend local setup. The MAFFT alignment algorithm does not require too much computational resources and likely your computer is faster than the demo server.

To set up and run the application locally, follow these instructions. If you just want to use the web demo, you can skip to Chap. 2.

First, get the code from GitHub:

- The front end: `https://github.com/Genome-of-Melody/chantlab_frontend`
- The back end: `https://github.com/Genome-of-Melody/chantlab_backend`

Clone both repositories to your device.

Next, there are dependencies.

Install the MAFFT v7.505 for your platform.[1] If you are using Windows, choose the option for installing it on WSL.[2] In this case, make sure that MAFFT can be accessed by running `wsl mafft <options>` from command line.

Ensure that you have both Python (>=3.9.2) and Node.js installed. If you do not, follow the installation instructions on their respective web pages[3][4]

Set up the Django framework by following the installation instructions.[5]

Do the same for the Angular platform.[6]

Once all these dependencies are installed, navigate to the back end directory. In command line, run `pip install -r requirements.txt`.

Additionally, it is necessary to download the Latin corpus for the correct processing of Latin texts.[7]

Then, in the appropriate Python environment, run the following commands:

```
from cltk.data.fetch import FetchCorpus
corpus_downloader = FetchCorpus(language="lat")
corpus_downloader.import_corpus("lat_models_cltk")
```

To run the back end, type `python manage.py runserver`.

Now, navigate to the front end directory and run `npm install`. This will install the required packages.

To run the front end, type `ng serve`.

The application can be accessed from your browser on the address `localhost:4200`.

[1]`https://mafft.cbrc.jp/alignment/software/`
[2]`https://docs.microsoft.com/en-us/windows/wsl/install-win10`
[3]`https://www.python.org/downloads/`
[4]`https://nodejs.org/en/download/`
[5]`https://www.djangoproject.com/download/`
[6]`https://angular.io/guide/setup-local`
[7]`https://docs.cltk.org/en/latest/data.html`

2. User documentation

ChantLab is a tool for analyzing user-defined data. It comes with some data already provided, however, it does not substitute the function of database webs.

In this chapter, we present an overview of the functionality of the application. The first section sketches out the overall functionality of the application. The following sections describe each feature in more detail.

2.1 Site map

Figure 2.1 shows a sitemap of the application. It shows how the site can be navigated to get to the different functions. The rectangles represent pages with their own URLs, while the ellipses represent the pages' functions.

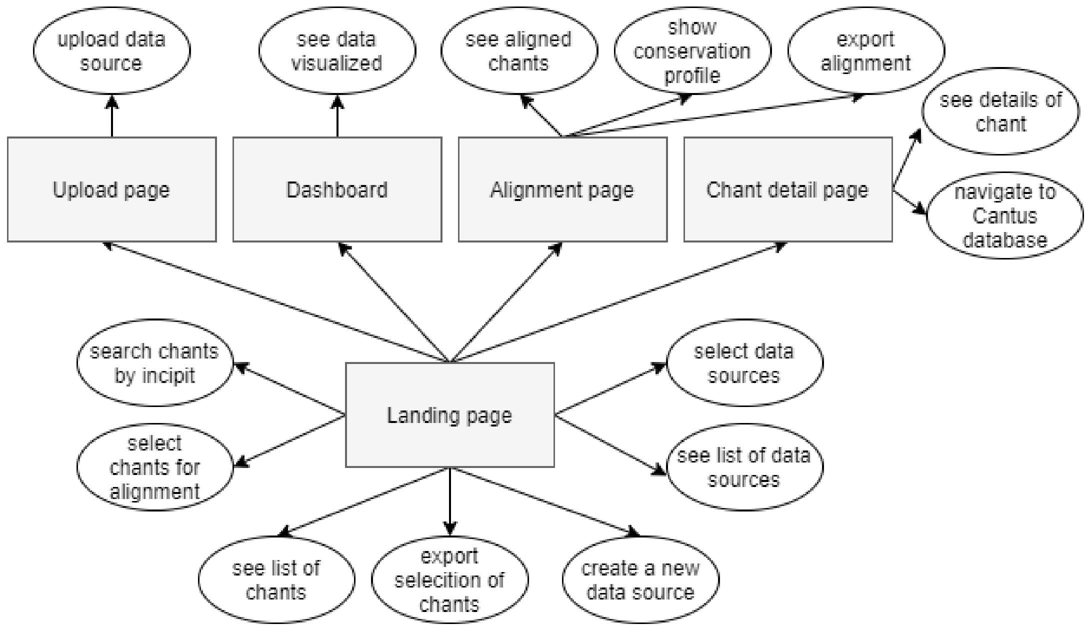


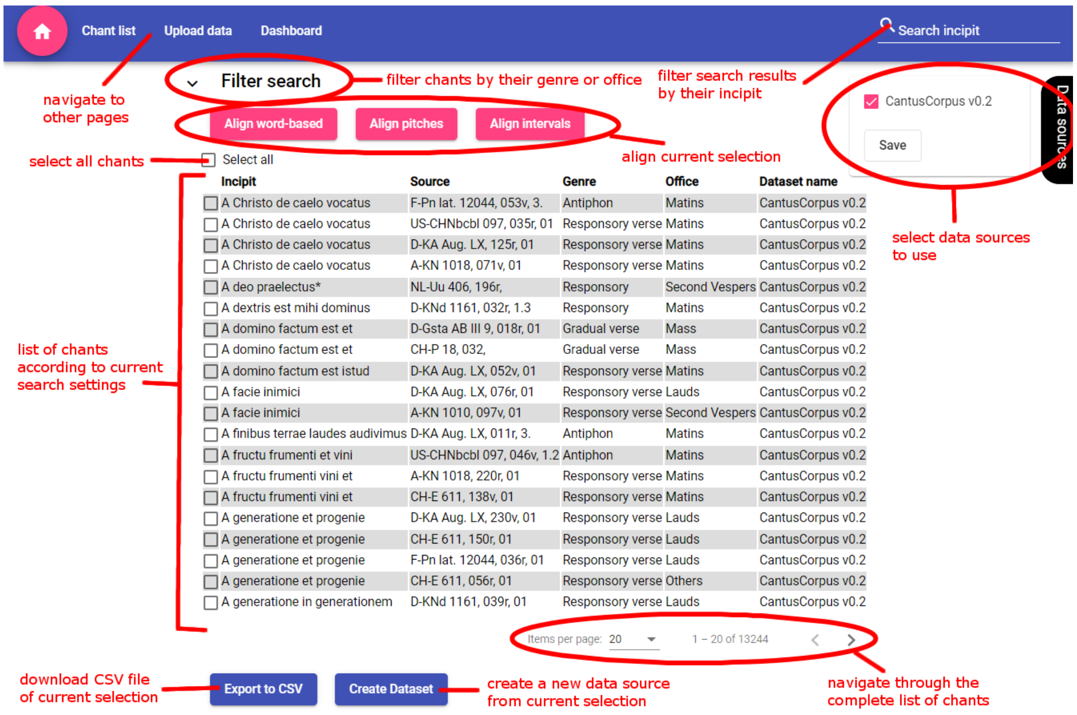
Figure 2.1: Sitemap of the application.

2.2 Landing page

The application contains one or more data sources. A data source is a set of chant data defined by the user. The application comes with one data source, *CantusCorpus v0.2*, already uploaded. The separation of data sources enables users to compare different datasets.

The landing page provides several functions (see Figure 2.2). The top panel, which is always present on the page, allows for quick navigation to other pages and for filtering search by chants' incipit (the first few words of text). It shows a list of chants from the current search settings, as well as a filter panel used for modifying the settings. There is an option to export a selection of chants to a CSV file and to create a new data source from them, as well as several options for their alignment.

The panel on the right side enables data source selection. To change data source (more than one can be selected at once), click the checkbox next to the data source name and click *save*. To hide or unhide the data source panel, click on the black *Data sources* button. The panel is available in the entire application.


Chant list
Upload data
Dashboard
Search incipit
navigate to other pages
Filter search
filter chants by their genre or office
filter search results by their incipit
Align word-based
Align pitches
Align intervals
align current selection
CantusCorpus v0.2
Save
Data sources
select data sources to use
select all chants
Select all
list of chants according to current search settings
Items per page: 20
1 – 20 of 13244
navigate through the complete list of chants
download CSV file of current selection
Export to CSV
Create Dataset
create a new data source from current selection

Incipit	Source	Genre	Office	Dataset name
A Christo de caelo vocatus	F-Pn lat. 12044, 053v, 3.	Antiphon	Matins	CantusCorpus v0.2
A Christo de caelo vocatus	US-CHNbcbl 097, 035r, 01	Responsory verse	Matins	CantusCorpus v0.2
A Christo de caelo vocatus	D-KA Aug. LX, 125r, 01	Responsory verse	Matins	CantusCorpus v0.2
A Christo de caelo vocatus	A-KN 1018, 071v, 01	Responsory verse	Matins	CantusCorpus v0.2
A deo praelectus*	NL-Uu 406, 196r,	Responsory	Second Vespers	CantusCorpus v0.2
A dextris est mihi dominus	D-KNd 1161, 032r, 1.3	Responsory	Matins	CantusCorpus v0.2
A domino factum est et	D-Gsta AB III 9, 018r, 01	Gradual verse	Mass	CantusCorpus v0.2
A domino factum est et	CH-P 18, 032,	Gradual verse	Mass	CantusCorpus v0.2
A domino factum est istud	D-KA Aug. LX, 052v, 01	Responsory verse	Matins	CantusCorpus v0.2
A facie inimici	D-KA Aug. LX, 076r, 01	Responsory verse	Lauds	CantusCorpus v0.2
A facie inimici	A-KN 1010, 097v, 01	Responsory verse	Second Vespers	CantusCorpus v0.2
A finibus terrae laudes audivimus	D-KA Aug. LX, 011r, 3.	Antiphon	Matins	CantusCorpus v0.2
A fructu frumenti et vini	US-CHNbcbl 097, 046v, 1.2	Antiphon	Matins	CantusCorpus v0.2
A fructu frumenti vini et	A-KN 1018, 220r, 01	Responsory verse	Matins	CantusCorpus v0.2
A fructu frumenti vini et	CH-E 611, 138v, 01	Responsory verse	Matins	CantusCorpus v0.2
A generatione et progenie	D-KA Aug. LX, 230v, 01	Responsory verse	Lauds	CantusCorpus v0.2
A generatione et progenie	CH-E 611, 150r, 01	Responsory verse	Lauds	CantusCorpus v0.2
A generatione et progenie	F-Pn lat. 12044, 036r, 01	Responsory verse	Lauds	CantusCorpus v0.2
A generatione et progenie	CH-E 611, 056r, 01	Responsory verse	Others	CantusCorpus v0.2
A generatione in generationem	D-KNd 1161, 039r, 01	Responsory verse	Lauds	CantusCorpus v0.2

Figure 2.2: Landing page and its features.

2.2.1 List of available chants

The landing page displays a list of chants from a specified source, which is by default set to the provided data source *CantusCorpus v0.2*. As we assume that the number of all selected chants can be large, we do not display all of them at once. Instead, the user can choose the number of chants displayed at once and paginate through the list to get to later ones.

Some elements of the list have an incipit ending with an asterisk (∗). This indicates that the specific chant does not have its entire text transcribed, only the part in the incipit.

2.2.2 Incipit search

The landing page provides the possibility to filter chants from the current selection by their incipit (the first few words of the chant). To do so, enter the desired string into the field in the top-right corner marked as *Search incipit* and press Enter (Figure 2.3). A set of chants that contain the query as a substring (not necessarily as a prefix) of their incipit will be displayed (Figure 2.4). Be aware that a misspelled query will not return the correct results.

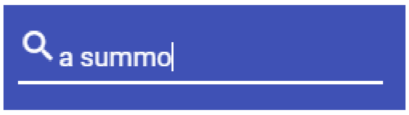
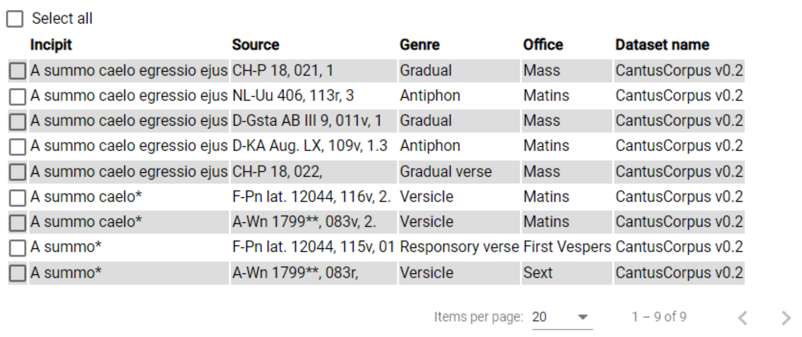


Figure 2.3: Entering search query into the *Search incipit* box.



☐ Select all

	Incipit	Source	Genre	Office	Dataset name
☐	A summo caelo egressio ejus	CH-P 18, 021, 1	Gradual	Mass	CantusCorpus v0.2
☐	A summo caelo egressio ejus	NL-Uu 406, 113r, 3	Antiphon	Matins	CantusCorpus v0.2
☐	A summo caelo egressio ejus	D-Gsta AB III 9, 011v, 1	Gradual	Mass	CantusCorpus v0.2
☐	A summo caelo egressio ejus	D-KA Aug. LX, 109v, 1.3	Antiphon	Matins	CantusCorpus v0.2
☐	A summo caelo egressio ejus	CH-P 18, 022,	Gradual verse	Mass	CantusCorpus v0.2
☐	A summo caelo*	F-Pn lat. 12044, 116v, 2.	Versicle	Matins	CantusCorpus v0.2
☐	A summo caelo*	A-Wn 1799**, 083v, 2.	Versicle	Matins	CantusCorpus v0.2
☐	A summo*	F-Pn lat. 12044, 115v, 01	Responsory verse	First Vespers	CantusCorpus v0.2
☐	A summo*	A-Wn 1799**, 083r,	Versicle	Sext	CantusCorpus v0.2

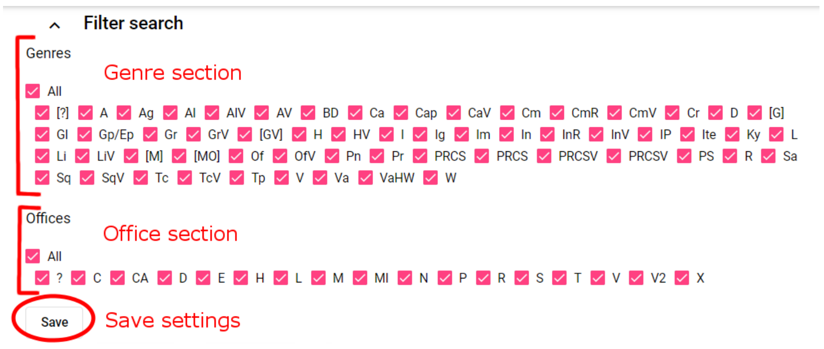
Items per page: 20 1 – 9 of 9

Figure 2.4: The result of the query. Notice that each incipit has the query as a substring.

2.2.3 Search filter

It is possible to filter the search results by their genre and office. The filter panel can be opened by clicking the down arrow next to the *Filter search* heading. By default, all genres and all offices are selected. To select or unselect some of them, click the checkbox next to their abbreviation. To select or unselect all genres or offices, click the checkbox next to *All* in the respective section (Figure 2.5).

The filter panel does not use the full names of the genres and offices, as in some cases, the name can be very long. Instead, it uses their abbreviations as used in Cantus Index. Attachments A and B provide a list of genres, resp. offices and their abbreviations.



Filter search

Genres

✓ All

✓ [?] ✓ A ✓ Ag ✓ Al ✓ AlV ✓ AV ✓ BD ✓ Ca ✓ Cap ✓ CaV ✓ Cm ✓ CmR ✓ CmV ✓ Cr ✓ D ✓ [G]
✓ Gl ✓ Gp/Ep ✓ Gr ✓ GrV ✓ [GV] ✓ H ✓ HV ✓ I ✓ Ig ✓ Im ✓ In ✓ InR ✓ InV ✓ IP ✓ Ite ✓ Ky ✓ L
✓ Li ✓ LiV ✓ [M] ✓ [MO] ✓ Of ✓ OfV ✓ Pn ✓ Pr ✓ PRCS ✓ PRCS ✓ PRCSV ✓ PRCSV ✓ PS ✓ R ✓ Sa
✓ Sq ✓ SqV ✓ Tc ✓ TcV ✓ Tp ✓ V ✓ Va ✓ VaHW ✓ W

Offices

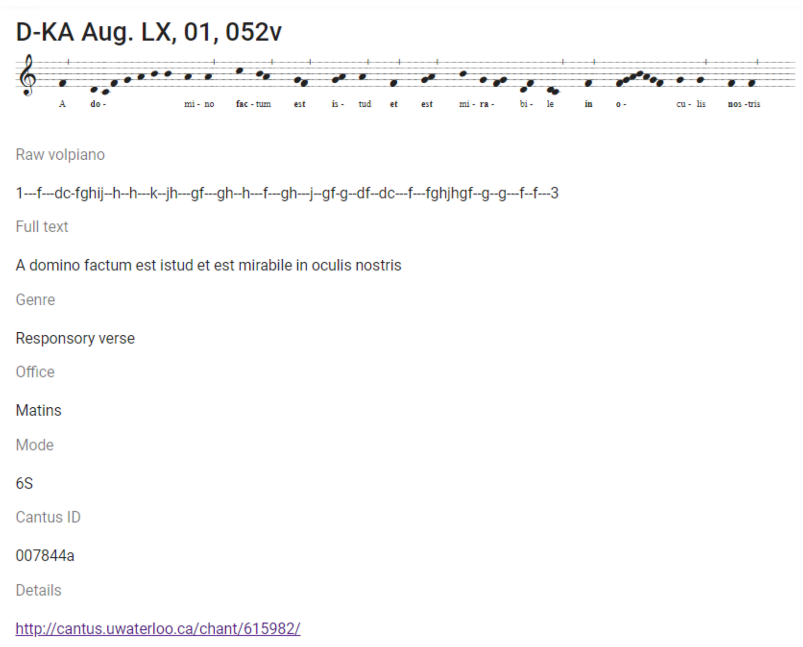
✓ All

✓ ? ✓ C ✓ CA ✓ D ✓ E ✓ H ✓ L ✓ M ✓ MI ✓ N ✓ P ✓ R ✓ S ✓ T ✓ V ✓ V2 ✓ X

Figure 2.5: Search filter panel.

2.2.4 Chant detail

By clicking on a chant's incipit in the search results list, the user is redirected to a page which displays the chant's melody with the text in full, as well as other information of interest. It shows the chant's Cantus ID, by which it can be found in the Cantus Database. It also shows a URL which points to the corresponding entry on the Cantus website (Figure 2.6). These fields are valid for all chants from the default *CantusCorpus v0.2* dataset, but there is no guarantee of their correctness in user-uploaded data.


A do- mi- no fac-tum est is- tud et est mi- ra- bi- le in o- cu- lis nos-tris

D-KA Aug. LX, 01, 052v

Raw volpiano

1---f---dc-fghij--h--h---k--jh---gf---gh--h---f---gh---j--gf-g--df--dc---f---fghjhgf--g--g---f--f---3

Full text

A domino factum est istud et est mirabile in oculis nostris

Genre

Responsory verse

Office

Matins

Mode

6S

Cantus ID

007844a

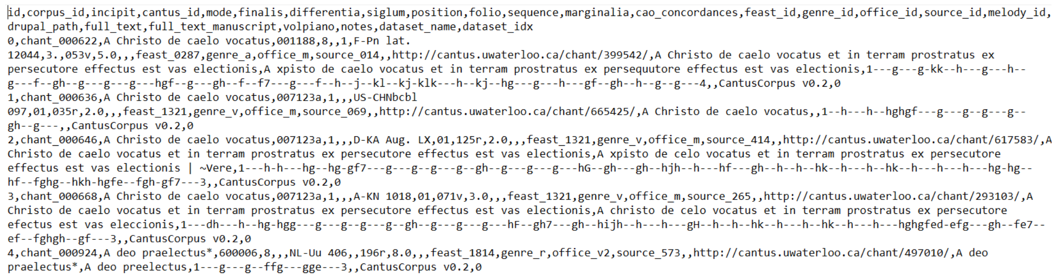
Details

http://cantus.uwaterloo.ca/chant/615982/

Figure 2.6: Page with the detail of the selected chant.

2.2.5 Data export

The user may wish to export the results of their search into a CSV file. In that case, select the desired chants by checking the checkbox next to their incipit (or *Select all*) and click the *Export to CSV* button at the bottom of the page. A file with the name *dataset.csv* will be automatically downloaded (Figure 2.7).



```
id,corpus_id,incipit,cantus_id,mode,finalis,differentia,siglum,position,folio,sequence,marginalia,cao_concordances,feast_id,genre_id,office_id,source_id,melody_id,
drupal_path,full_text,full_text_manuscript,volpiano,notes,dataset_name,dataset_idx
0,chant_000622,A Christo de caelo vocatus,001188,8,,1,F-Pn lat.
12044,3.,053v,5.0,,,feast_0287,genre_a,office_m,source_014,,http://cantus.uwaterloo.ca/chant/399542/,A Christo de caelo vocatus et in terram prostratus ex
persecutore effectus est vas electionis,A xpisto de caelo vocatus et in terram prostratus ex persequutore effectus est vas electionis,1---g---g-kk--h---g---h--
g---f--gh--g---g---g---hgf--g---gh--f--f7---g---f--h--j--kl--kj-klk---h--kj--hg---g---h---gf--gh--h--g--g---4,,CantusCorpus v0.2,0
1,chant_000636,A Christo de caelo vocatus,007123a,1,,,US-CHNbcbl
097,01,035r,2.0,,,feast_1321,genre_v,office_m,source_069,,http://cantus.uwaterloo.ca/chant/665425/,A Christo de caelo vocatus,,1--h---h--hghgf---g---g--g---g--
gh--g---,,CantusCorpus v0.2,0
2,chant_000646,A Christo de caelo vocatus,007123a,1,,,D-KA Aug. LX,01,125r,2.0,,,feast_1321,genre_v,office_m,source_414,,http://cantus.uwaterloo.ca/chant/617583/,A
Christo de caelo vocatus et in terram prostratus ex persecutore effectus est vas electionis,A xpisto de celo vocatus et in terram prostratus ex persecutore
effectus est vas electionis | ~Vere,1---h-h---hg--hg-gf7---g---g--g---g--gh--g---g---g---hG--gh---gh--hjh--h---hf---gh--h--h--hk--h---h--hk--h---h---h---hg-hg--
hf--fghg--hkh-hgfe--fgh-gf7---3,,CantusCorpus v0.2,0
3,chant_000668,A Christo de caelo vocatus,007123a,1,,,A-KN 1018,01,071v,3.0,,,feast_1321,genre_v,office_m,source_265,,http://cantus.uwaterloo.ca/chant/293103/,A
Christo de caelo vocatus et in terram prostratus ex persecutore effectus est vas electionis,A christo de celo vocatus et in terram prostratus ex persecutore
efectus est vas eleccionis,1---dh---h--hg-hgg---g---g--g---g--gh--g---g---g---hF--gh7---gh--hijh--h---h---gH--h--h--hk--h---h--hk--h---h---hghgfed-efg---gh--fe7--
ef--fghgh--gf---3,,CantusCorpus v0.2,0
4,chant_000924,A deo praelectus*,600006,8,,,NL-Uu 406,,196r,8.0,,,feast_1814,genre_r,office_v2,source_573,,http://cantus.uwaterloo.ca/chant/497010/,A deo
praelectus*,A deo preelectus,1---g---g--ffg---gge---3,,CantusCorpus v0.2,0
```

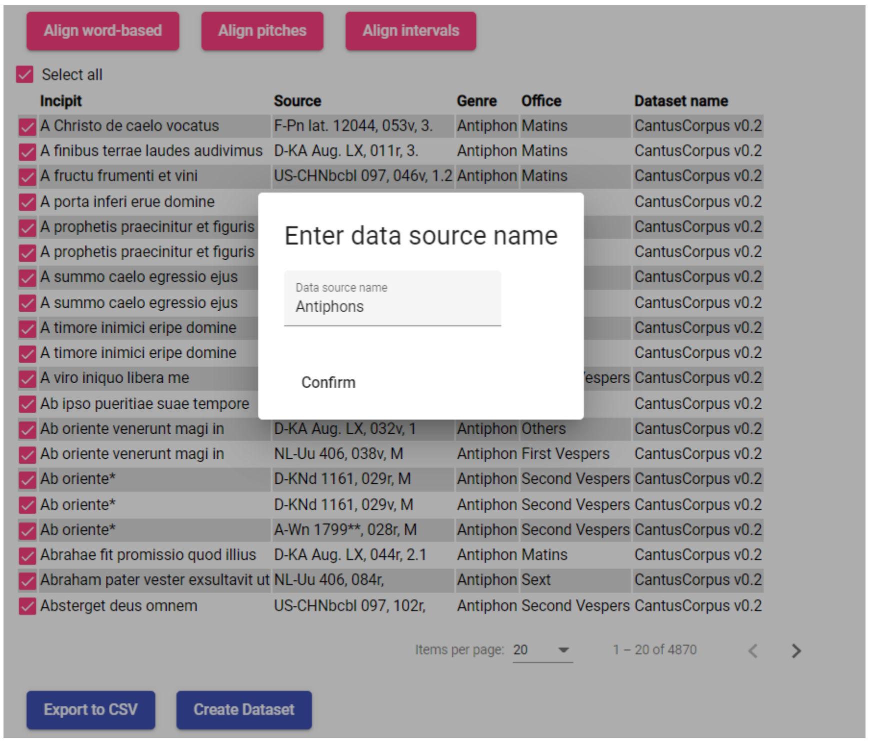
Figure 2.7: First few lines of the exported CSV file.

2.3 Data source creation

The application is not limited to the data present by default. The user can either create a data source from their search results, or upload completely new data.

2.3.1 Create from search

To create a data source from the search results, check the checkboxes next to the desired chants and click the *Create Dataset* button at the bottom of the page. The user will be prompted for the data source name (Figure 2.8). If no name is entered, the name of the data source will be *undefined*. After confirming the name, the data source list will be automatically updated with the newly-created one (Figure 2.9).



Incipit	Source	Genre	Office	Dataset name
A Christo de caelo vocatus	F-Pn lat. 12044, 053v, 3.	Antiphon	Matins	CantusCorpus v0.2
A finibus terrae laudes audivimus	D-KA Aug. LX, 011r, 3.	Antiphon	Matins	CantusCorpus v0.2
A fructu frumenti et vini	US-CHNbcbl 097, 046v, 1.2	Antiphon	Matins	CantusCorpus v0.2
A porta inferi erue domine				CantusCorpus v0.2
A prophetis praecinitur et figuris				CantusCorpus v0.2
A prophetis praecinitur et figuris				CantusCorpus v0.2
A summo caelo egressio ejus				CantusCorpus v0.2
A summo caelo egressio ejus				CantusCorpus v0.2
A timore inimici eripe domine				CantusCorpus v0.2
A timore inimici eripe domine				CantusCorpus v0.2
A viro iniquo libera me			espers	CantusCorpus v0.2
Ab ipso pueritiae suae tempore				CantusCorpus v0.2
Ab oriente venerunt magi in	D-KA Aug. LX, 032v, 1	Antiphon	Others	CantusCorpus v0.2
Ab oriente venerunt magi in	NL-Uu 406, 038v, M	Antiphon	First Vespers	CantusCorpus v0.2
Ab oriente*	D-KNd 1161, 029r, M	Antiphon	Second Vespers	CantusCorpus v0.2
Ab oriente*	D-KNd 1161, 029v, M	Antiphon	Second Vespers	CantusCorpus v0.2
Ab oriente*	A-Wn 1799**, 028r, M	Antiphon	Second Vespers	CantusCorpus v0.2
Abrahae fit promissio quod illius	D-KA Aug. LX, 044r, 2.1	Antiphon	Matins	CantusCorpus v0.2
Abraham pater vester exsultavit ut	NL-Uu 406, 084r,	Antiphon	Sext	CantusCorpus v0.2
Absterget deus omnem	US-CHNbcbl 097, 102r,	Antiphon	Second Vespers	CantusCorpus v0.2

Figure 2.8: Prompt for entering the name of the data source appears after clicking the *Create Dataset* button.

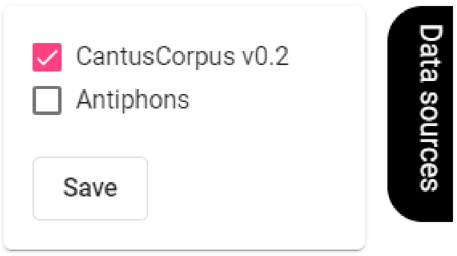


Figure 2.9: The newly created data source automatically appears in the data source list.

2.3.2 User data upload

To upload new data, navigate to the *Upload data* page in the top panel. Select the file to upload and enter the data source name (Figure 2.10). The file should be in CSV format and its contents are specified in Section 3.3. Click *Upload* to upload the file. After the file is processed, the data source list will be automatically updated (Figure 2.11). The exported file created in Section 2.2.5 is suitable for upload.

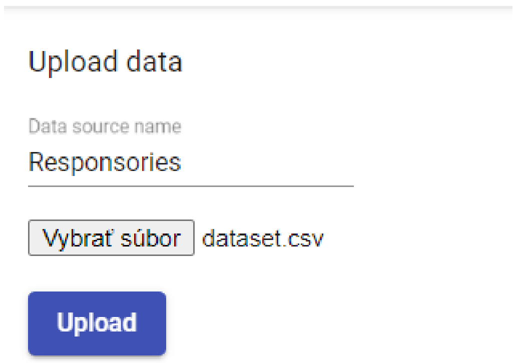


Figure 2.10: The upload form with the file *dataset.csv* selected for upload. The new data source will have the name *Responsories*.

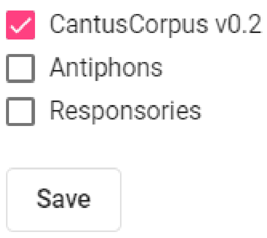


Figure 2.11: The uploaded data source automatically appears in the list.

2.4 Alignment

The alignment tool is the core functionality of the application.

It is possible to select a set of chants and have them be aligned using one of the methods described in Section 4.3. The alignment option is selected by clicking on one of the buttons above the chant list (see Figure 2.2) after selecting the chants to be aligned. After doing so, the user is redirected to a page where the alignment result is shown. In some cases, the alignment make take up to a minute to complete.

The alignment result is shown as a list of melodies (Figure 2.12). The melodies are either arranged in the same order as they were displayed in the chant list (in the case of naive alignment) or in the order of similarity.

To show more information about each melody, the user can click on the chant source button by which each chant is identified. The same information as when navigating to the chant's page is displayed (Figure 2.13). To hide the detail, click on the chant source button again.

If the user wishes to rearrange the displayed melodies, simply click anywhere close to a melody and drag it to another position (Figure 2.14).

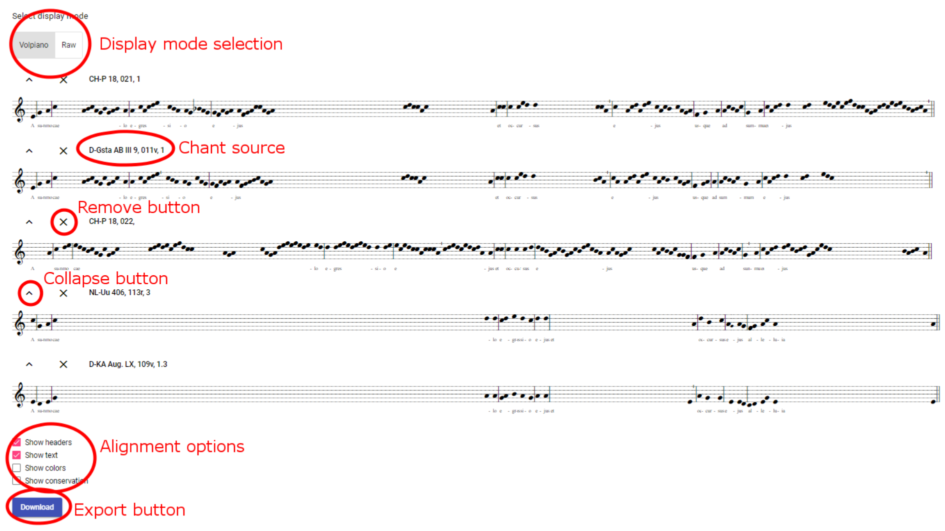
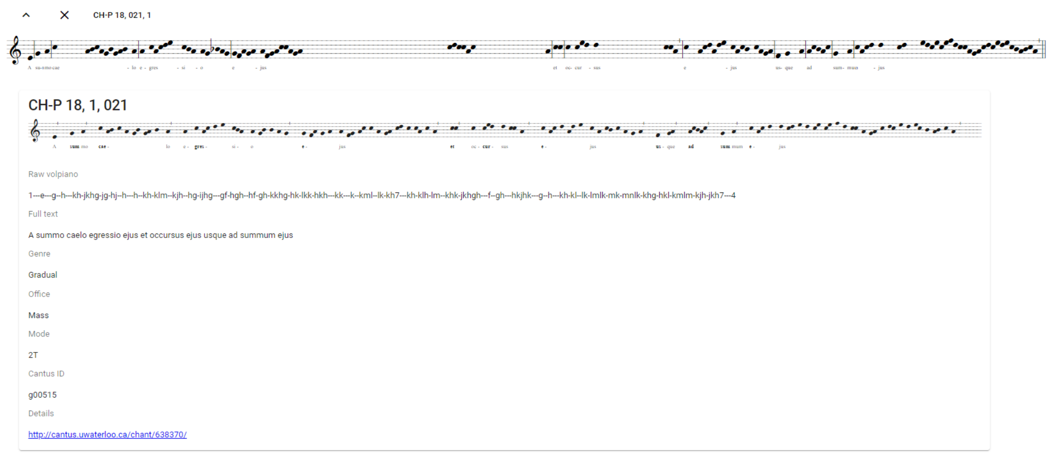


Figure 2.12: Result of the alignment.



CH-P 18, 1, 021

Raw volpiano

1---e---g--h---kh-jkhg-jg-hj--h---h--kh-klm--kjh--hg-ijhg---gf-hgh--hf-gh-kkhg-hk-lkk-hkh---kk---k--kml--lk-kh7---kh-klh-lm--khk-jkhgh---f--gh---hkjhk---g--h---kh-kl--lk-lmlk-mk-mnlk-khg-hkl-kmlm-kjh-jkh7---4

Full text

A summo caelo egressio ejus et occursus ejus usque ad summum ejus

Genre

Gradual

Office

Mass

Mode

2T

Cantus ID

g00515

Details

http://cantus.uwaterloo.ca/chant/638370/

Figure 2.13: Aligned melody with the chant information displayed.

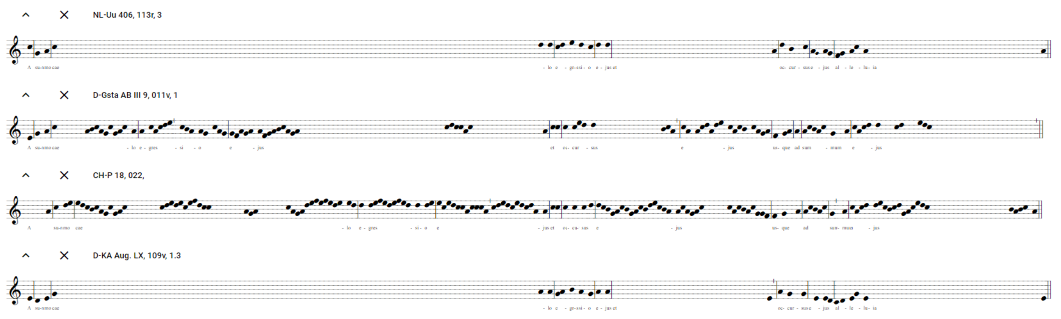


Figure 2.14: Alignment after dragging and dropping the last melody. Compare to Figure 2.12.

2.4.1 Collapsing and deleting alignment

After the alignment is shown, the user can choose to collapse the alignment (i.e. hide the notes) by clicking on the *Collapse* button (Figure 2.15) in each melody's header or to remove it completely by clicking on the *Remove button* (Figure 2.16).

The chant can be uncollapsed by clicking on the same button. However, removing the chant entirely is permanent. To get the removed chant back, the page needs to be reloaded.

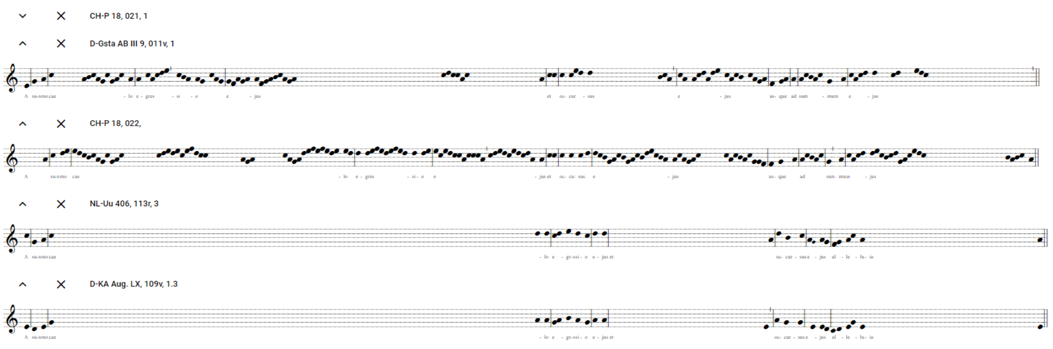


Figure 2.15: The first chant is collapsed.

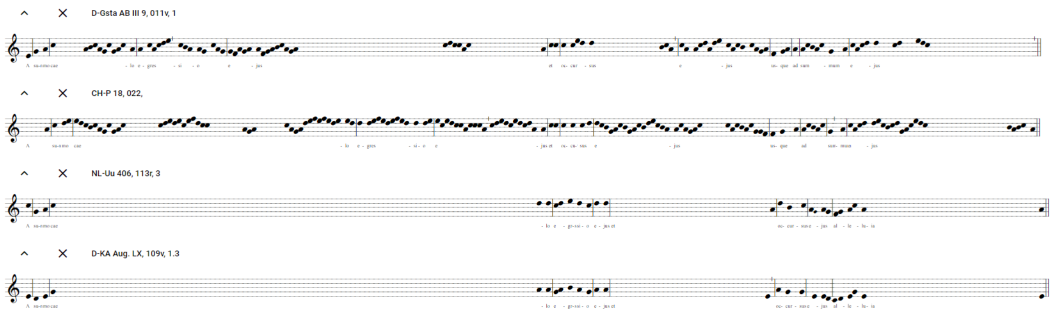


Figure 2.16: The first chant is removed. Compare to Figure 2.12.

2.4.2 Alignment display options

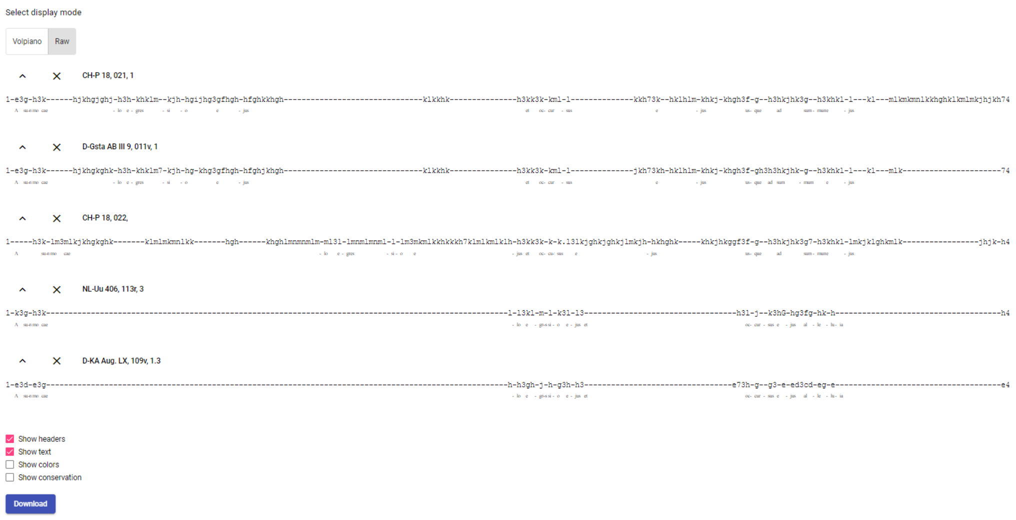
Once the chants have been aligned, there exist several options to better show how they are aligned.

As the Volpiano font does not have characters of equal width, the notes that are actually aligned might not be shown as aligned. To see the actual alignment, the user can change the display mode above the aligned melodies to *Raw*, which shows the melodies as the encoded string in a monopaced font (Figure 2.17).

To see the aligned sequences better, it is possible to remove the headers and the text independently by unclicking the corresponding boxes in the alignment options (Figure 2.18, Figure 2.19).

It is possible to see how similar certain regions are. The first option is to color each note based on its absolute pitch (Figure 2.20). In the case of interval alignment, this option may show different colors even though the intervals are the same.

The other option is to show the conservation profile, i.e. the proportion of the other chants sharing the same note or interval at the given position. This option will show conservation profile corresponding to the intervals in the interval alignment option. Darker colors mean the position is more conserved, while lighter colors mean less conserved (Figure 2.21). Moreover, this option shows the


Select display mode

Volpiano | Raw

CH-P 18, 021, 1

```
1-e3g-h3k------hjkhgjghj-h3h-khklm--kjh-hgijhg3gfhgh-hfghkkhgh-------------------------------klkkhk--------------h3kk3k-kml-l-------------kkh73k--hklhlm-khkj-khgh3f-g--h3hkjhk3g--h3khkl-l---kl---mlkmkmnlkkhghklkmlmkjhjkh74
```

D-Gsta AB III 9, 011v, 1

```
1-e3g-h3k------hjkhgkghk-h3h-khklm7-kjh-hg-khg3gfhgh-hfghjkhgh-------------------------------klkkhk--------------h3kk3k-kml-l-------------jkh73kh-hklhlm-khkj-khgh3f-gh3h3hkjhk-g--h3khkl-l---kl---mlk---------------------74
```

CH-P 18, 022,

```
1-----h3k-lm3mlkjkhgkghk-------klmlmkmnlkk-------hgh------khghlmnmnmlm-ml3l-lmnmlmnml-l-lm3mkmlkkhkkkh7klmlkmlklh-h3kk3k-k-k.l3lkjghkjghkjlmkjh-hkhghk-----khkjhkggf3f-g--h3hkjhk3g7-h3khkl-lmkjklghkmlk----------------jhjk-h4
```

NL-Uu 406, 113r, 3

```
1-k3g-h3k---------------------------------------------------------------------------------------------------------l-l3kl-m-l-k3l-l3---------------------------------h3l-j--k3hG-hg3fg-hk-h-------------------------------------h4
```

D-KA Aug. LX, 109v, 1.3

```
1-e3d-e3g---------------------------------------------------------------------------------------------------------h-h3gh-j-h-g3h-h3--------------------------------e73h-g--g3-e-ed3cd-eg-e-------------------------------------e4
```

[✓ Show headers]
[✓ Show text]
☐ Show colors
☐ Show conservation

Download

Figure 2.17: Aligned melodies shown as the raw string.

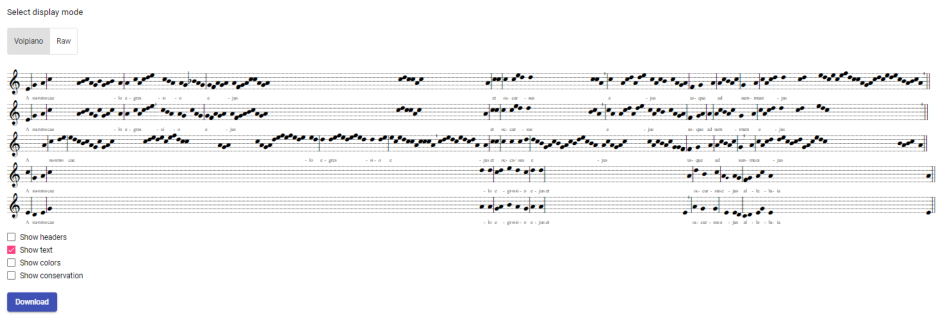
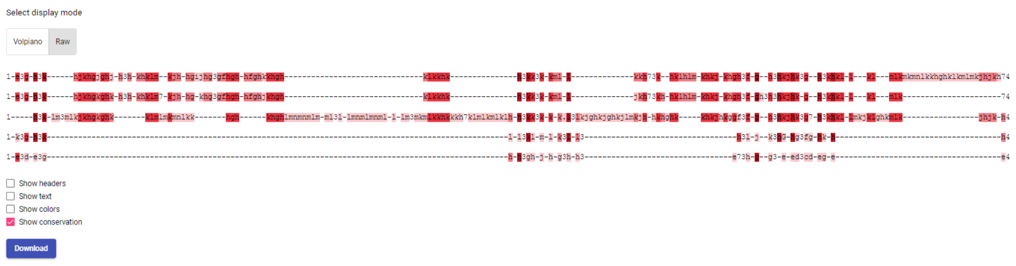


Figure 2.18: The aligned melodies shown without headers.


Select display mode

Volpiano | Raw

```
1-e3g-h3k------hjkhgjghj-h3h-khklm--kjh-hgijhg3gfhgh-hfghkkhgh-------------------------------klkkhk--------------h3kk3k-kml-l-------------kkh73k--hklhlm-khkj-khgh3f-g--h3hkjhk3g--h3khkl-l---kl---mlkmkmnlkkhghklkmlmkjhjkh74
1-e3g-h3k------hjkhgkghk-h3h-khklm7-kjh-hg-khg3gfhgh-hfghjkhgh-------------------------------klkkhk--------------h3kk3k-kml-l-------------jkh73kh-hklhlm-khkj-khgh3f-gh3h3hkjhk-g--h3khkl-l---kl---mlk---------------------74
1-----h3k-lm3mlkjkhgkghk-------klmlmkmnlkk-------hgh------khghlmnmnmlm-ml3l-lmnmlmnml-l-lm3mkmlkkhkkkh7klmlkmlklh-h3kk3k-k-k.l3lkjghkjghkjlmkjh-hkhghk-----khkjhkggf3f-g--h3hkjhk3g7-h3khkl-lmkjklghkmlk----------------jhjk-h4
1-k3g-h3k---------------------------------------------------------------------------------------------------------l-l3kl-m-l-k3l-l3---------------------------------h3l-j--k3hG-hg3fg-hk-h-------------------------------------h4
1-e3d-e3g---------------------------------------------------------------------------------------------------------h-h3gh-j-h-g3h-h3--------------------------------e73h-g--g3-e-ed3cd-eg-e-------------------------------------e4
```

☐ Show headers
☐ Show text
☐ Show colors
[✓ Show conservation]

Download

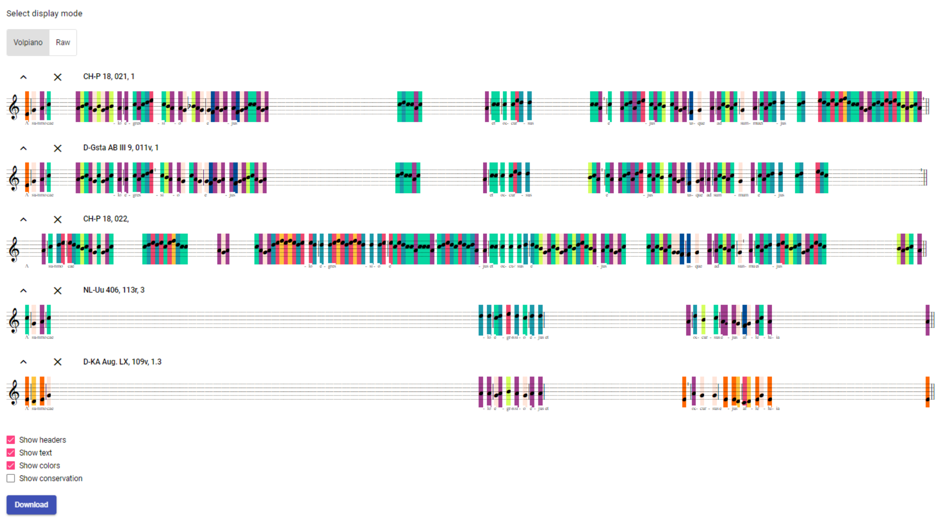
Figure 2.19: The aligned melodies shown in *Raw* mode without headers and text.

overall conservation indicator of the entire set. Using this option, it is possible to see how similar entire regions are.

2.4.3 Alignment export

To export the aligned melodies, click the *Download* button at the bottom of the page. The format of the file will be suitable to pass directly into MAFFT again. Each melody's identifier is the string stored in the *drupal_path* field.

The melodies in the exported file will be either encoded as symbols corresponding to Volpiano characters in the case of naive and pitch alignment, or as symbols corresponding to intervals in the case of interval alignment.


Select display mode

Volpiano | Raw

CH-P 18, 021, 1

D-Gsta AB III 9, 011v, 1

CH-P 18, 022,

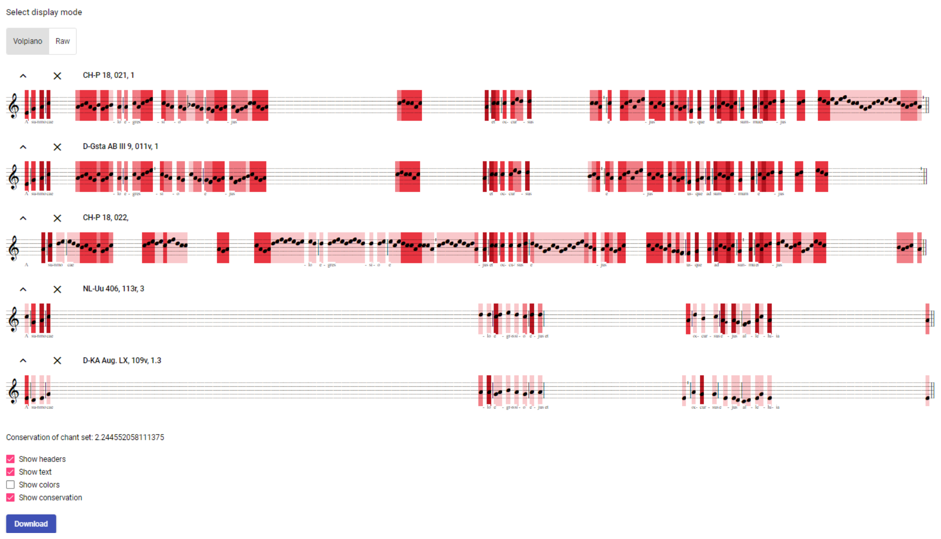
NL-Uu 406, 113r, 3

D-KA Aug. LX, 109v, 1.3

[✓] Show headers
[✓] Show text
[✓] Show colors
[ ] Show conservation

Download

Figure 2.20: Aligned melodies with each note colored a different color.


Select display mode

Volpiano | Raw

CH-P 18, 021, 1

D-Gsta AB III 9, 011v, 1

CH-P 18, 022,

NL-Uu 406, 113r, 3

D-KA Aug. LX, 109v, 1.3

Conservation of chant set: 2.244552058111375

[✓] Show headers
[✓] Show text
[ ] Show colors
[✓] Show conservation

Download

Figure 2.21: Aligned melodies with their conservation profile shown.

Only the unremoved melodies will be present in the file. Their order will be the same as the current order on the page.

2.5 Dashboard

The dashboard provides visualizations of the data. The visualizations are simple, as this feature is not the main priority of the application. Since at the time of development it was not completely clear what data visualizations are useful for chant research, we only provide some most basic ones. Other visualizations will be added as the application is used and it is clarified what researchers need most.

The dashboard is responsive, i.e. changing data sources has an immediate effect on the visualization.

The visualizations currently provided by the dashboard are comparison of melody length and text length for different data sources (Figure 2.22), a histogram of melody length (Figure 2.23) and a histogram of text length (Figure 2.24).

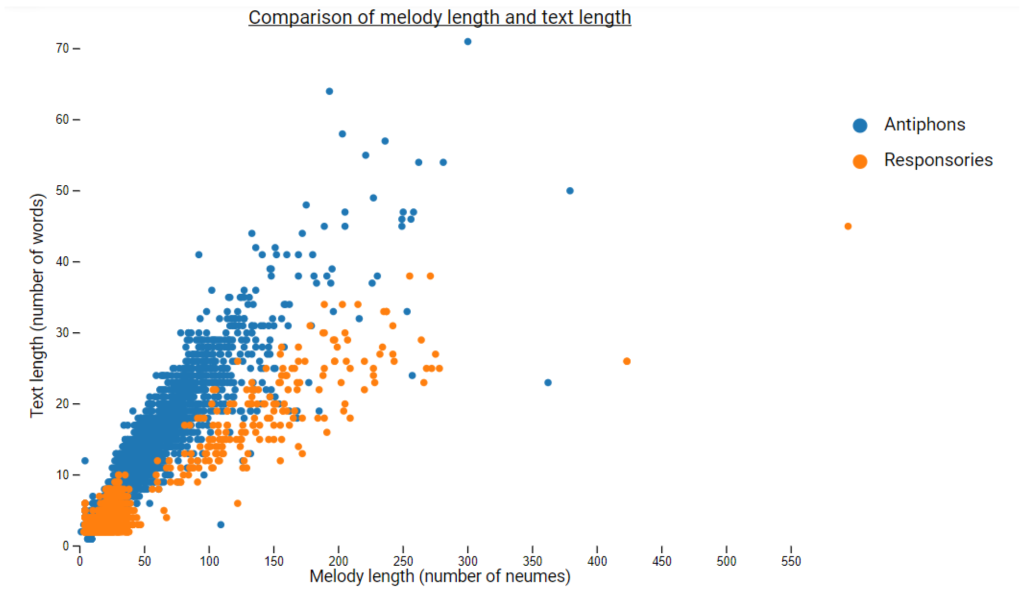


Figure 2.22: Scatter plot of melody and text length for the data sources *Antiphons* and *Responsories*.

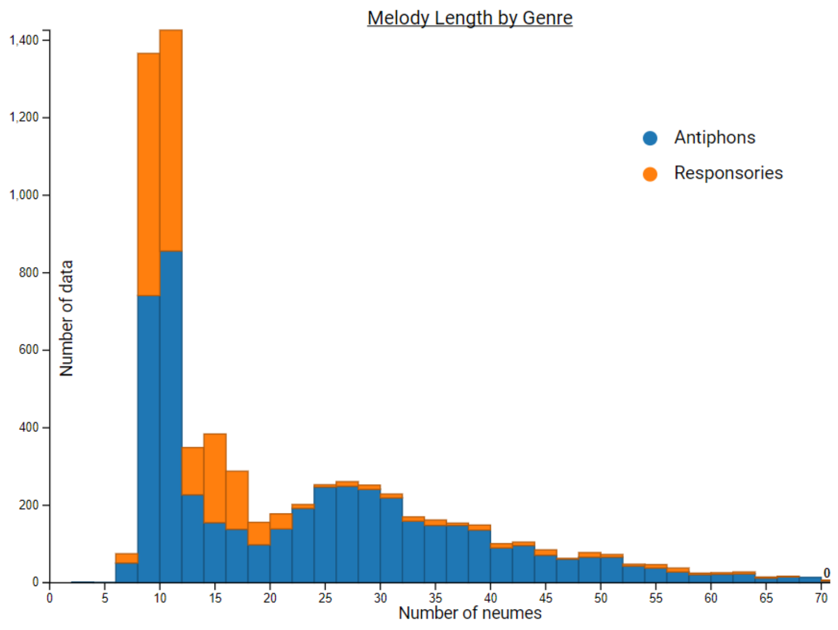


Figure 2.23: Histogram of melody length for the data sources *Antiphons* and *Responsories*.

2.6 Known issues

When displaying alignment results, some melodies may differ in their width on the screen even though they contain the same number of characters. This is caused

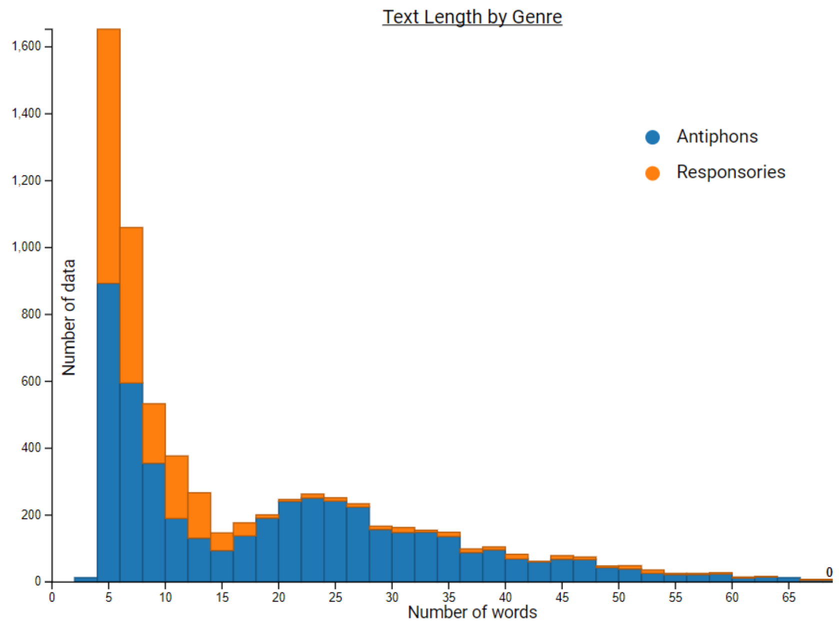


Figure 2.24: Histogram of text length for the data sources *Antiphons* and *Responsories*.

by the font Volpiano which does not have characters of equal width. There is no simple solution to this problem; to overcome it, we provide the option to display the alignment as raw strings (not musical notation) using a monospaced font.

When aligning a larger number of chants (around 30 or more), the rendering becomes relatively slow and the page reacts to user input with a noticeable delay. In the future, we may consider offering a simplified view without the interactive elements so that the delay is reduced to a minimum.

3. Data

Despite the fact that the aim of ChantLab is not to create a database of chants, nor to carry out experiments on data, but rather to create a tool that researchers can use to conduct trials, we provide a source of data that can be used for the purposes. It is the largest set of digitalized chants that musicologists regularly use in their research.

Our main source of data is the Cantus database [Lacoste et al.], one of the databases indexed in the Cantus Index. The database serves as a digital archive of chants, each entry containing information about its source, liturgical occasion, mode, and others. Work on the project started in the late 1980s, and to date, around 500,000 individual chants from approximately 150 manuscripts have been indexed. Each entry is transcribed manually and undergoes a thorough examination before publishing [Lacoste, 2012].

We are using a scraped version of the Cantus database released as CantusCorpus v0.2.[Cornelissen et al., 2020] Unlike the Cantus database which is continuously being updated and is therefore unsuitable for computational study, the corpus is versioned, therefore each version always contains the same data. We are using version 0.2 released in July 2020 which contains 497,071 entries. However, a majority of the data is not suitable for this application, as they do not contain both melodic and textual data in full, therefore we are only using a subset of size around 13,000. The corpus is available for download in CSV format.

Aside from providing a basic dataset to ChantLab, CantusCorpus also defines how user-uploaded data must be formatted (see below: 3.3).

3.1 CSV

CSV is one of the most common formats for tabular data. The abbreviation stands for *comma-separated values*. As the name suggests, the format uses commas to separate columns (although other separators, such as a semicolon, can be used as well to allow for simpler parsing in case that the data frequently contains commas that would otherwise need to be escaped), while the individual rows are separated by a line break. The data is stored as plaintext, which makes it easily readable. Parsing CSV files becomes more complicated when the data contains column and row separators inside fields; in that case quotation marks or esape sign has to be used. There exist many well-designed parsers, one such parser is the Python module simply called *csv*[1]. This application uses the module *pandas*[2] to parse CSV files, which in turn uses the *csv* module.

3.2 Database fields

Table 3.1 represents the data fields in the database.

Data field	Description

[1]https://docs.python.org/3/library/csv.html
[2]https://pandas.pydata.org/

id	automatically generated id in the database
corpus_id	human-readable id identifying the chant in the CantusCorpus
incipit	incipit (the first few words) of chant
cantus_id	id identifying the chant in the Cantus Index
mode	mode of the chant
finalis	the final note of the chant
differentia	the melodic ending of psalms
siglum	manuscript in which the chant is found
position	liturgical role of the chant
folio	page of the manuscript where the chant is found
sequence	order in which the chant is found in the folio
marginalia	clarification about the location of the chant
cao_concordances	references to older literature
feast_id	feast of the year during which the chant was sung
genre_id	genre of the chant, e.g. *antiphon*, *responsory*
office_id	office of the day during which the chant was sung, e.g. *Laudes*, *Vespers*
source_id	id of the manuscript in which the chant is found
melody_id	id of melody by which it can be found in the Cantus Index
drupal_path	URL of the chant on the Cantus database website
full_text	full text in a standardized spelling
full_text_manuscript	full text in the manuscript spelling
volpiano	transcription of the melody in volpiano format
notes	indexing notes
dataset_name	name of the data source to which the chant belongs
dataset_idx	index of the data source to which the chant belongs

Table 3.1: List of database fields

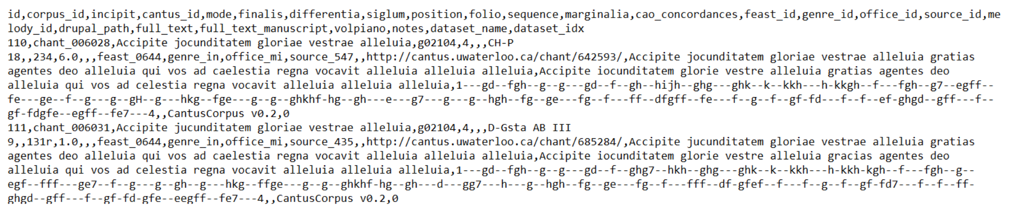
3.3 User-defined data

The application enables user to upload their own dataset. Table 3.2 specifies the fields in the database. Validation of the file is not implemented; it is left up to the user to upload a valid file. The meaning of the individual fields is as described in the previous section unless said otherwise. The value in the column *Required* indicates whether the column must be present in the file. The value *Nullable* indicates whether a data entry can have *null* or an empty value in the column. Figure 3.1 shows a valid CSV file.

Column name	Type	Requi-red	Null-able	Notes
id	number	no	yes	the column will be dropped when processing
corpus_id	string	yes	yes	
incipit	string	yes	no	
cantus_id	string	yes	yes	should be a valid Cantus ID

mode	string	yes	yes	
finalis	string	yes	yes	
differentia	string	yes	yes	
siglum	string	yes	no	
position	string	yes	yes	
folio	string	yes	yes	
sequence	string	yes	yes	
marginalia	string	yes	yes	
cao_concordances	string	yes	yes	
feast_id	string	yes	yes	
genre_id	string	yes	yes	list of genres is in attachment A
office_id	string	yes	yes	list of offices is in attachment B
source_id	string	yes	yes	
melody_id	string	yes	yes	
drupal_path	string	yes	yes	should be a valid URL
full_text	string	yes	no	
full_text_manuscript	string	yes	yes	
volpiano	string	yes	no	has to be in Volpiano format
notes	string	yes	yes	
dataset_name	string	no	yes	the column will be dropped when processing
dataset_idx	number	no	yes	the column will be dropped when processing

Table 3.2: Fields in the user-uploaded CSV



```
id,corpus_id,incipit,cantus_id,mode,finalis,differentia,siglum,position,folio,sequence,marginalia,cao_concordances,feast_id,genre_id,office_id,source_id,me
lody_id,drupal_path,full_text,full_text_manuscript,volpiano,notes,dataset_name,dataset_idx
110,chant_006028,Accipite jocunditatem gloriae vestrae alleluia,g02104,4,,,CH-P
18,,234,6.0,,,feast_0644,genre_in,office_mi,source_547,,http://cantus.uwaterloo.ca/chant/642593/,Accipite jocunditatem gloriae vestrae alleluia gratias
agentes deo alleluia qui vos ad caelestia regna vocavit alleluia alleluia alleluia,Accipite iocunditatem glorie vestre alleluia gratias agentes deo
alleluia qui vos ad celestia regna vocavit alleluia alleluia alleluia,1---gd--fgh--g--g---gd--f--gh--hijh--ghg---ghk--k--kkh---h-kkgh--f---fgh--g7--egff--
fe---ge--f--g---g--gH--g---hkg--fge---g--g--ghkhf-hg--gh---e---g7---g---g--hgh--fg--ge---fg--f---ff--dfgff--fe---f--g--f--gf-fd---f--f--ef-ghgd--gff---f--
gf-fdgfe--egff--fe7---4,,CantusCorpus v0.2,0
111,chant_006031,Accipite jucunditatem gloriae vestrae alleluia,g02104,4,,,D-Gsta AB III
9,,131r,1.0,,,feast_0644,genre_in,office_mi,source_435,,http://cantus.uwaterloo.ca/chant/685284/,Accipite jucunditatem gloriae vestrae alleluia gratias
agentes deo alleluia qui vos ad caelestia regna vocavit alleluia alleluia alleluia,Accipite iocunditatem glorie vestre alleluia gracias agentes deo
alleluia qui vos ad celestia regna vocavit alleluia alleluia alleluia,1---gd--fgh--g--g---gd--f--ghg7--hkh--ghg---ghk--k--kkh---h-kkh-kgh--f---fgh--g--
egf--fff---ge7--f--g---g--gh--g---hkg--ffge---g--g--ghkhf-hg--gh---d---gg7---h---g--hgh--fg--ge---fg--f---fff--df-gfef--f---f--g--f--gf-fd7---f--f--ff-
ghgd--gff---f--gf-fd-gfe--eegff--fe7---4,,CantusCorpus v0.2,0
```

Figure 3.1: Example of a valid CSV file

3.4 Melody encoding

The melodies in the volpiano fields are encoded as strings of alphanumeric characters and dashes. These can be rendered as musical notation using the Volpiano font. Each character represents either a pitch, empty space, or other musical characters, such as a clef.

Volpiano was developed as a research tool optimized for databases and word processors. There are strict rules concerning the transcription, which leads to all Volpiano-encoded melodies having a standardized format. For example, the

Volpiano protocol dictates that each transcription begins with a treble clef followed by three spaces, that words are separated by three spaces and syllables by two, and others. [3] Figure 3.2 shows an example of an encoded melody along with its rendering.

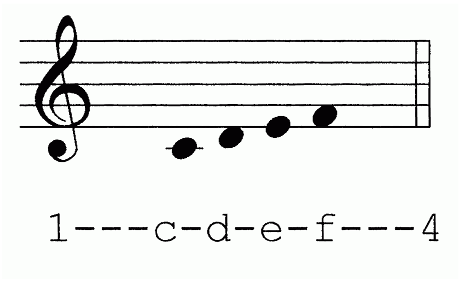


Figure 3.2: Example of volpiano as stored in the database and how it is rendered as musical notation. [Lacoste, 2012, Figure 2]

3.5 Data statistics

As mentioned earlier, not all of the almost 500,000 entries in the CantusCorpus can be aligned. As one of the application's main features is melody alignment, it is necessary that we only use those data points whose *volpiano* field is not empty. Moreover, some visualizations compare text length to melody length, therefore we require the data points to have both. Additionally, text and melody should be able to be aligned, i.e. they contain the same number of words and syllables.

After removing the data that does not adhere to the conditions, we are left with 13,397 usable data points.

In the rest of this section, we outline the basic statistics about the data. We concentrate in particular on the length of the chants' melodies and lyrics, as these characteristics tend to differ among genres. This information is not necessary for the understanding of the thesis. However, it shows the diversity of the chant repertoire and allows us to visualize the amount of information contained in the data.

The dataset contains entries of 37 different genres. 14 of them are associated with more than 100 entries. Figure 3.3 shows their distribution. The following statistics are done on the subset of all data whose entries belong to one of these genres. The list of genres corresponding to each genre ID is in attachment A.

Table 3.3 shows the mean and the standard deviation of text and melody length by genres. Text length is defined as the number of words (strings separated by spaces). Melody length is defined as the number of non-gap characters (`-`) in the Volpiano encoding.

Genre ID	mean text length	standard deviation of text length	mean melody length	standard deviation of melody length

[3] `https://cantus.uwaterloo.ca/sites/default/files/documents/2.%20Volpiano%20Protocols.pdf`

genre_a	9.9	8.0	38.3	38.8
genre_av	7.4	2.9	22.5	13.0
genre_cm	14.6	7.1	82.6	36.0
genre_gr	9.2	4.5	99.1	54.4
genre_grv	10.9	3.7	141.8	44.7
genre_h	5.2	5.5	29.0	22. 4
genre_hv	12.8	5.2	50.7	21.9
genre_i	4.7	3.5	28.0	24.6
genre_in	16.6	7.5	99.4	41.9
genre_of	11.9	9.3	103.3	77.9
genre_r	4.9	5.5	28.9	45.3
genre_tcv	10.7	3.3	102.9	28.2
genre_v	7.0	4.6	36.8	24.8
genre_w	3.3	1.6	11.0	6.2

Table 3.3: Mean text and melody length and standard deviation of chants grouped by genres.

Figure 3.4 shows the comparison of text length to melody length for the individual genres.

Now, we will show the same statistics for chants divided by their offices. First, Figure 3.5 shows the distribution of the offices among the dataset. The list of office names corresponding to each office ID can be found in attachment B.

Table 3.4 shows the mean and the standard deviation of text and melody length of the datasets.

Office ID	mean text length	standard deviation of text length	mean melody length	standard deviation of melody length
office_c	9.8	8.3	38.7	37.5
office_d	5.0	2.6	19.9	20.2
office_e	14.0	8.8	50.0	33.7
office_h	14.2	7.3	65.8	37.4
office_l	8.3	6.4	30.4	25.0
office_m	6.9	10.0	33.8	43.7
office_mi	13.1	10.3	102.8	54.8
office_n	5.4	4.6	19.8	16.9
office_p	4.9	4.5	18.4	20.4
office_r	9.3	6.1	35.44	34.4
office_s	4.9	3.8	17.9	15.5
office_t	5.3	3.8	19.0	15.9
office_v	6.8	7.7	29.0	36.0
office_v2	6.8	7.1	26.4	31.0
office_x	13.1	10.8	61.0	52.3

Table 3.4: Mean text and melody length and standard deviation of chants grouped by office.

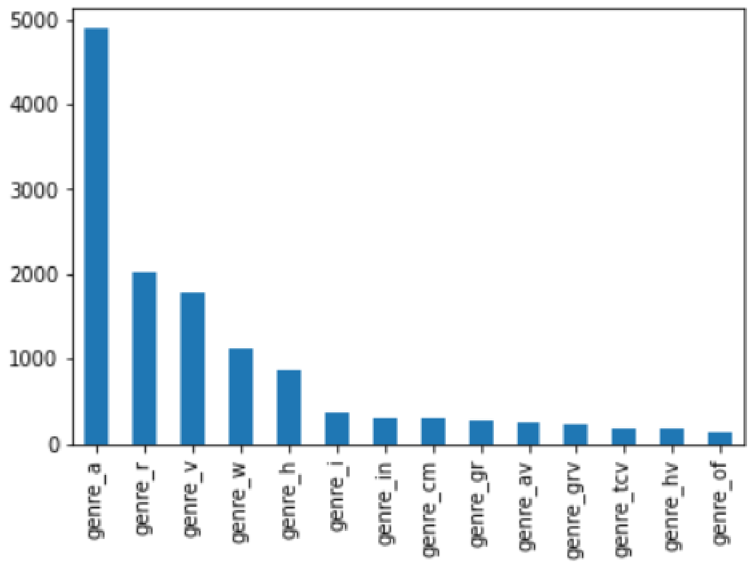


Figure 3.3: Distribution of genres in the dataset.

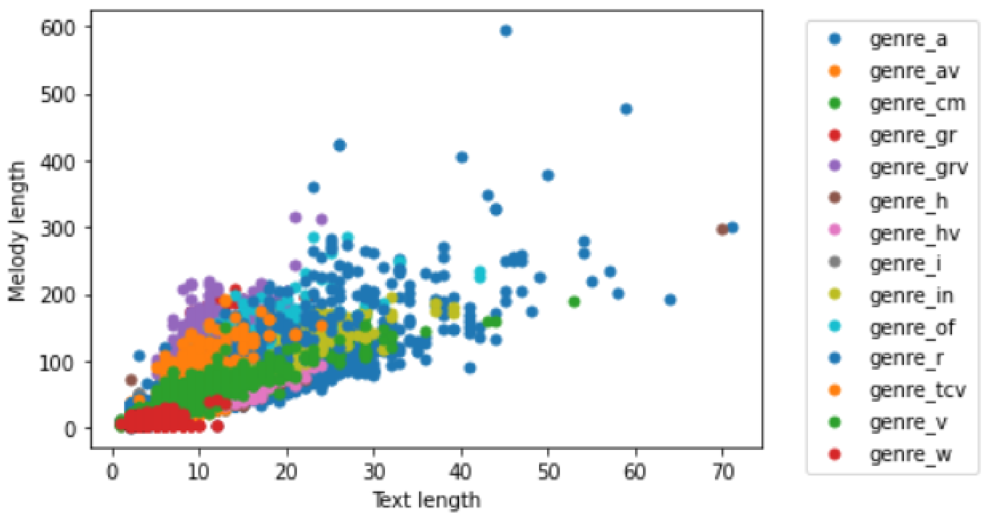


Figure 3.4: Approximate visual comparison of text length and melody length for each genre.

Finally, Figure 3.6 compares lengths text and melody of chants divided by genres.

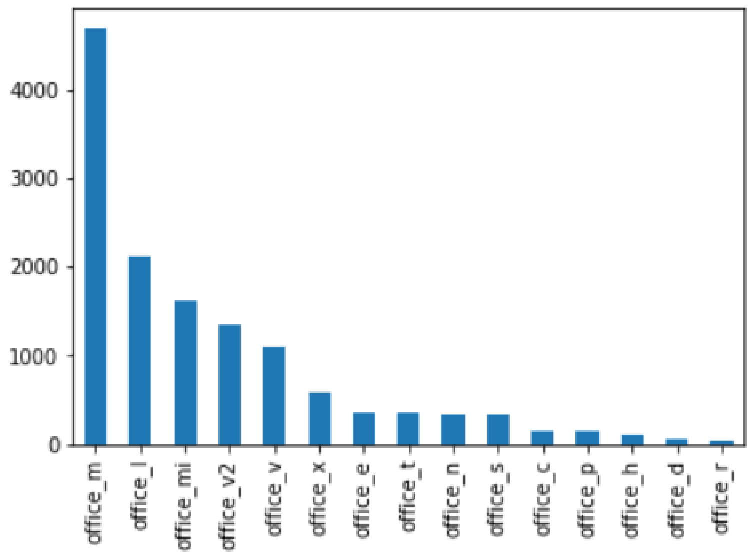


Figure 3.5: Distribution of offices in the dataset.

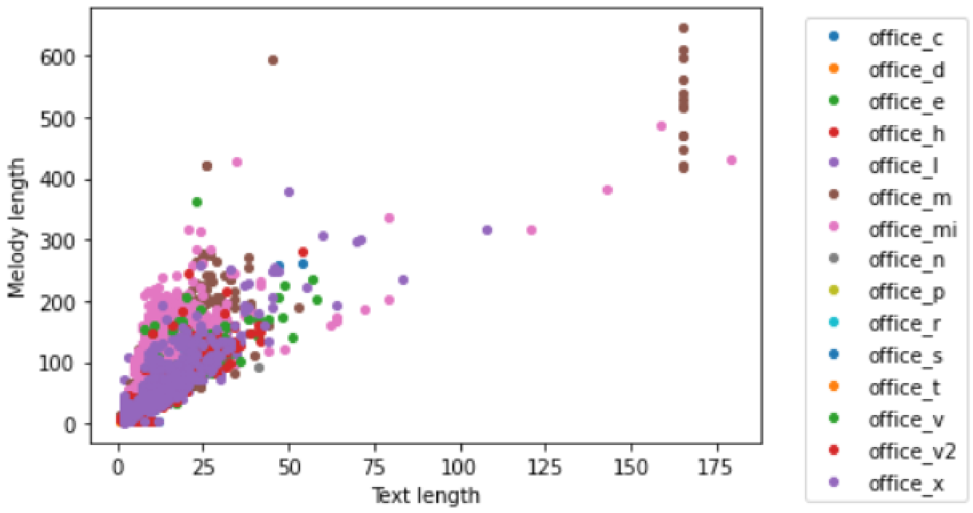


Figure 3.6: Approximate visual comparison of text length and melody length for each office. From this visualization it is already clear that there is a group of chants from the morning prayer that merits further investigation.

4. Multiple sequence alignment

Sequence alignment, in general, is a task whose purpose is to arrange two or more sequences with a common alphabet to identify similar and different regions within them. A set of sequences being *aligned* in this case can be understood as each being extended by spaces in such a way that if they are arranged in a matrix, each sequence occupying one row and each column containing one character, it can be seen what had to happen for one sequence to change into another on a character-by-character basis: insertion (or deletion), character substitution, or nothing if the characters in the given position are identical. A good sequence alignment algorithm is one that does not perform unnecessary insertions (deletions) or substitutions.

The problem of multiple sequence alignment is most studied in bioinformatics. Since DNA was first sequenced in the 1970s, there has been a need to compare various genomes to determine similarity. As organisms mutate and evolve, their DNA or RNA changes. Aligning their genomes reveals similar and different regions, which facilitates the tracking of these mutations and makes it possible to determine the order in which they happened.

However, the applications of sequence alignment are not limited to biology. Every task that makes use of determinig the similarity of some sequences, where the emphasis is put on finding regions where they do not diverge, can make use of the existing methods.

Melody alignment of Gregorian chant can be considered as such. As the tradition spread across Europe, each place changed some of the existing melodies by a little, thereby creating new melodies that can change further as they travel through time and space. This is akin to the mutations in DNA caused by environmental factors. Finding well-conserved regions in many instances of chant provides great insight into which parts of a melody are unlikely to change, and, on the other hand, which ones tend to vary a lot. It can also reveal the ancestors of a melody and the path which it traveled to transform into its final form. This is in line with the focus of philology shifting not to merely reconstructing an earliest layer of a text (with the unspoken assumption that this is the “real” text), but to map the entire tradition of text transmission and evolution, taking the later layers to be as valid within their cultural environment as the older layers.

In this chapter, we will first give the definition of the problem of sequence alignment. We will mention some important considerations, as well as theoretical limitations. Then we will provide an overview of the methods developed for bioinformatics that attempt to solve the problem. Finally, we will show how we applied the existing methods and technologies on Gregorian chant melodies, as encoded using Volpiano in current chant databases.

4.1 The problem of sequence alignment

Assume that we have an alphabet $\mathcal{A}$ and a character σ such that $\sigma \notin \mathcal{A}$. Then let us have a set of sequences $S = \{s_1, s_2, \ldots, s_k\}$ with $s_i \in \mathcal{A}^{l_i}$. The output of a sequence alignment algorithm is the set of aligned sequences $A = \{a_1, a_2, \ldots, a_k\}$, where $a_k \in (\mathcal{A} \cup \{\sigma\})^L$, $L \geq l_i \; \forall i \in \{1, 2, \ldots, k\}$. Each original sequence s_i can be obtained from the aligned sequence a_i by removing all σ.

Given two aligned sequences a_i and a_j and an index $p \leq L$, we define the following operations:

- *Identity*: $(a_i)_k = (a_j)_k$
- *Insertion*: $(a_i)_k = \sigma \wedge (a_j)_k \in \mathcal{A}$
- *Deletion*: $(a_i)_k \in \mathcal{A} \wedge (a_j)_k = \sigma$
- *Substitution*: $(a_i)_k \in \mathcal{A} \wedge (a_j)_k \in \mathcal{A} \wedge (a_i)_k \neq (a_j)_k$

Each of the operations has an associated cost. The cost of substitution can further vary depending on which characters are being substituted. We can then define the overall cost of the alignment A in different ways, e.g. as the sum of costs over all triples (i, j, p) $\forall i, j \in \{1, 2, \ldots, k\}$ $\forall p \leq L$ or as the sum of costs for unordered pairs $\{i, j\}$ and indices p, in which case insertion and deletion are considered the same operation. The goal of a sequence alignment algorithm is to minimize the cost. There are other, more complicated ways of defining the cost function, and the performance of an algorithm is highly dependent on which one it uses.

4.1.1 Pairwise and multiple sequence alignment

Depending on the number of sequences to align, we distinguish between pairwise alignment for pairs of sequences and multiple sequence alignment for more than two. Despite the similarity in their outcomes, the two problems are fundamentally different from a computational perspective.

Pairwise alignment is relatively easy to solve. The Needleman-Wunsch algorithm, which is a dynamic programming algorithm, can find an optimal solution in the asymptotic time of $\mathcal{O}(mn)$, where m and n are the respective lengths of the sequences. This means that it is possible to find an optimal alignment even for longer sequences.

Needleman-Wunsch algorithm can be extended to more than two sequences. However, with each additional sequence, its complexity increases, and it quickly becomes impractical or even practically impossible to align multiple sequences this way. In fact, it has been proven that multiple sequence alignment is an NP-complete problem [Wang and Jiang, 2009]. It is therefore necessary to use various heuristics to generate alignments. Current algorithms do not aim at finding the optimal alignment; instead, they try to produce one that is good enough.

4.1.2 Local and global sequence alignment

There is a distinction to be made between local and global sequence alignment.

The problem description above is the definition of global alignment. Aligning sequences globally means aligning the entire sequences end-to-end. (This does not mean, however, that there cannot be gaps at the beginning or at the end of the generated alignment.) All characters from all sequences must be present in the final alignment. Global alignment is used to compare relatively similar sequences, such as protein homologues or versions of the same chant sung at different points in time.

On the other hand, the goal of local alignment is to find similar regions in divergent sequences, while the rest of the sequences is disregarded. The output of local alignment algorithms contains only a substring of both sequences. Local alignment is suitable for finding conserved patterns.

Both methods are useful in their own way. Local alignment provides a slightly different insight than global alignment, however, they can be combined to extract more information. In fact, the best current multiple sequence alignment algorithms use local alignment for pairs of sequences to generate a better overall global alignment. [Notredame, 2007]

4.2 Sequence alignment methods

The methods used to find sequence alignments depend on how many sequences there are and whether they should be aligned globally or locally. Dynamic programming can used for finding pairwise alignment, both local and global. For many sequences, other methods have been developed. They do not compute the optimal alignment, however, by using appropriate heuristics, their output is good enough.

4.2.1 Pairwise alignment: dynamic programming

Dynamic programming techniques are useful for pairwise alignment. The Needleman-Wunsch algorithm [Needleman and Wunsch, 1970] computes the global alignment of two sequences. A variation of the algorithm, the Smith-Waterman algorithm [Smith and Waterman, 1981], computes the local alignment of two sequences.

Needleman-Wunsch algorithm

This section is based on Needleman and Wunsch [1970].

The idea of the algorithm is to start with two empty sequences and subsequently add characters from either or both of the given sequences so as to obtain an optimal alignment in each step. Namely, suppose that we have two sequence prefixes A and B that have already been aligned optimally and their alignment gives a score of s. Furthermore, suppose that the next characters in the sequences are a and b, respectively. There are three possibilities:

- We append a and b to the respective prefixes. By doing so, we obtain the aligned sequence prefixes Aa and Bb.

```
Aa
Bb
```

- We append a to A and a gap to B. This way, we get the aligned prefixes Aa and B.

```
Aa
B-
```

- We append a gap to A and b to B. Now we have aligned the prefixes A and Bb.

```
A-
Bb
```

Each of the possibilities adds a value to the score s depending on what characters were added. To get the optimal alignment, we choose the one that yields the highest score. We then proceed to the next character, having two optimally aligned prefixes A' and B'. This leads to a recursive algorithm that can be formulated using dynamic programming.

Let us have two input sequences, A and B of lengths m and n with a common alphabet $\mathcal{A}$ and the gap character σ. Let us define the scoring function s as

$$s(a,b) = \begin{cases} 1 & \text{if } a = b \\ -1 & \text{if } a = \sigma \lor b = \sigma \\ -1 & \text{if } a \neq b \end{cases}$$

The algorithm initializes a matrix M of size $(m+1)*(n+1)$. The rows and columns represent the characters of A and B, respectively, except for the first row and the first column, which represent the beginning of a sequence or an empty sequence. That is to say, the row $M_{i,*}$ represents the character A_{i-1} for $i \geq 2$ and analogically, the column $M_{*,j}$ represents the character B_{j-1} for $j \geq 2$.

The algorithm iterates over the rows and columns of the matrix. In each step, it calculates the value of a cell $M_{i,j}$, provided that each of the cells $M_{i-1,j}$, $M_{i,j-1}$ and $M_{i-1,j-1}$ have been filled out, as

$$M_{i,j} = max \begin{cases} M_{i-1,j-1} + s(A_{i-1}, B_{j-1}) \\ M_{i-1,j} + s(A_{i-1}, \sigma) \\ M_{i,j-1} + s(\sigma, B_{j-1}) \end{cases}$$

In other words, the algorithm either aligns the two characters in positions $i-1$ and $j-1$, or it inserts a gap into sequence B, or it inserts a gap into sequence A, and chooses the version which yields the highest score.

The first row and column are apparently special cases, as there is no previous row or column. Therefore, for each cell in the first row or column, there is only one possible choice of score, which is equivalent to inserting a space.

After filling out the entire matrix, the algorithm then finds the optimal alignment by backtracking in the matrix. It starts in the bottom right cell of the matrix, which represents both sequences being aligned. In each iteration, it looks at the cells above, to the left and to the top-left of the current positions and chooses the highest score. If it moves top or left, it means that a gap was inserted. Moving diagonally represents a match or mismatch. By tracing its way back to the top left corner, the algorithm finds the alignment that yielded the highest score.

Let us show the algorithm on an example. Consider two sequences of nucleotide residues:

```
GATTA
GCATG
```

The matrix is initialized without anything filled out.

```
      G  C  A  T  G


G
A
T
T
A
```

We start filling out the matrix in the top left corner. Using the basic scoring scheme (+1 for a match, -1 for everything else), we insert a 0 to the beginning, and, since there is no top cell for the first row and no left cell for the first column, we add -1 to each subsequent cell, representing a gap insertion.

```
      G  C  A  T  G
   0 -1 -2 -3 -4 -5
G -1
A -2
T -3
T -4
A -5
```

The next cell to fill out is the one in the first `G` column and the first `G` row. We have three options:

- Move from the top, represents gap insertion for a score of -1. The final score would be $(-1) + (-1) = -2$.
- Move diagonally, represents match, giving a score of +1. The score in this case would be $0 + 1 = 1$.
- Move from the left, i.e. gap insertion. The score would be -2 as in the first case.

We choose the highest score, which in this case is a diagonal move representing a match. It follows intuition: we are now aligning `G` and `G`, matching them seems logical.

```
      G  C  A  T  G
   0 -1 -2 -3 -4 -5
G -1  1
A -2
T -3
T -4
A -5
```

Now let us look at the cell in the `C` column and the `G` row. Moving from the top yields -3, moving from the left yields 0 and moving diagonally yields -2, as it is a mismatch in this case. The highest of these scores is 0.

```
      G  C  A  T  G
   0 -1 -2 -3 -4 -5
G -1  1  0
A -2
T -3
T -4
A -5
```

We continue filling out the table this way until it is complete.

```
      G  C  A  T  G
   0 -1 -2 -3 -4 -5
G -1  1  0 -1 -2 -3
A -2  0  0  1  0 -1
T -3 -1 -1  0  2  1
T -4 -2 -2 -1  1  1
A -5 -3 -3 -1  0  0
```

As we have now calculated the scores for all prefixes, we can use backtracking to find the optimal alignment for the two sequences. Starting in the bottom right cell, we choose the cell (top, left or top-left) with the highest score. If multiple cells have the same score, we can choose either. The different alignments the cells represent are all optimal. The cell that we choose gives us the optimal alignment of the sequences before the last character was added. Depending on the direction by which we moved, we know whether this last character was a character of the sequence or a gap.

For example, consider the bottom right corner of the matrix.

```
   T  G
T  1  1
A  0  0
```

Starting in the bottom right, we can choose either the top or the top-left cell. Choosing the top-left one, i.e. moving diagonally, means that the last characters in the alignment were `A` and `G` for the respective sequences. We can find the alignment of the prefixes `GATT` and `GCAT` by backtracking from the top-left cell. By contrast, choosing the top cell means inserting a gap in the second sequence, and by backtracking from there we can find the alignment of `GATT` and `GCATG`.

Figure 4.1 shows a path that represents the alignment

```
G A - T T A
G C A T - G
```

$$\begin{tikzcd}[row sep=tiny, column sep=small]
 & & G & C & A & T & G \\
 & 0 & -1 & -2 & -3 & -4 & -5 \\
G & -1 & 1 \arrow[ul] & 0 & -1 & -2 & -3 \\
A & -2 & 0 & 0 \arrow[ul] & 1 \arrow[l] & 0 & -1 \\
T & -3 & -1 & -1 & 0 & 2 \arrow[ul] & 1 \\
T & -4 & -2 & -2 & -1 & 1 \arrow[u] & 1 \\
A & -5 & -3 & 3 & -1 & 0 & 0 \arrow[ul]
\end{tikzcd}$$

Figure 4.1: A path representing an optimal alignment.

Smith-Waterman algorithm

This section is based on Smith and Waterman [1981].

The algorithm is similar to Needleman-Wunsch algorithm. As its purpose is to find an optimal local alignment, it does not penalize long regions of mismatches or gaps. Its purpose is to find regions with the most matches. The only difference from the Needleman-Wunsch algorithm is in how new matrix cells are filled out. Namely, when willing out a new cell, we use the formula

$$M_{i,j} = max \begin{cases} 0 \\ M_{i-1,j-1} + s(A_{i-1}, B_{j-1}) \\ M_{i-1,j} + s(A_{i-1}, \sigma) \\ M_{i,j-1} + s(\sigma, B_{j-1}) \end{cases}$$

In other words, all negative values in what would be the matrix from Needleman-Wunsch algorithm are replaced by 0.

4.2.2 Multiple sequence alignment: progressive methods

As has already been mentioned, it is essentially impossible to use dynamic programming to compute the alignment of more than two sequences. Therefore, other methods have been developed. The most successful ones appear to be the so-called progressive methods. In general, they use some heuristics to estimate a guide tree, which is a phylogenetic tree determining how close the sequences are to each other, and then they compute the actual multiple alignment following the order of this tree.

One of such methods is the Tree-based Consistency Objective Function for alignment Evaluation (T-Coffee) algorithm [Notredame et al., 2000]. Its most important contribution is its extended library generated from both local and global pairwise alignments of all pairs of input sequences. This library enables the algorithm to make fewer mistakes in the initial stages of the guide tree, as these errors propagate throughout the entire tree. Figure 4.2 shows how a word can become misaligned using other progressive approaches.

Another method is MAFFT (the name presumably coming from the acronyms for multiple alignment and fast Fourier transform) [Katoh et al., 2002]. The authors focused on finding alignments that are not only optimal, but also biologically correct. They developed a way of rapid identification of homologous regions between two sequences using FFT, and then used the better pairwise alignments to

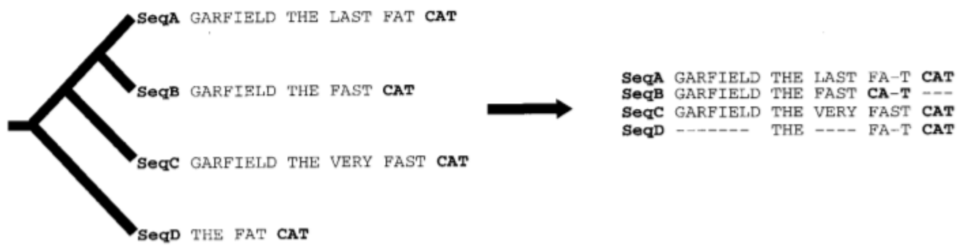

SeqA GARFIELD THE LAST FAT CAT
SeqB GARFIELD THE FAST CAT
SeqC GARFIELD THE VERY FAST CAT
SeqD THE FAT CAT
SeqA GARFIELD THE LAST FA-T CAT
SeqB GARFIELD THE FAST CA-T ---
SeqC GARFIELD THE VERY FAST CAT
SeqD ------- THE ---- FA-T CAT

Figure 4.2: Misalignment of the word CAT using other progressive methods. [Notredame et al., 2000, Figure 2(a)]

create a better multiple alignment.

T-Coffee

This section is based on Notredame et al. [2000].

The T-Coffee algorithm consists of various stages. The first one is to compute pairwise alignments for all pairs of input sequences. Two primary libraries are generated, one for global and one for local alignments. Each can contain more than one alignment for each pair.

As some alignments tend to be more correct than others, weighting is then performed. The authors chose sequence identity of two aligned sequences as the weight of each of the aligned residues in the pair. For example, consider the sequences A `GARFIELD THE LAST FAT CAT` and B `GARFIELD THE FAST CAT`. If they are aligned as

```
GARFIELD THE LAST FAT CAT
GARFIELD THE FAST CAT ---
```

then their sequence identity is 88%, as there are two non-equal characters aligned (i.e. there is no gap penalty). Therefore, the weight of each residue pair $W(A(x), B(y))$, where $A(x)$ denotes the character x from sequence A, and analogically for $B(y)$, is equal to 88. An example of primary library created from pairwise alignments is shown in Figure 4.3.

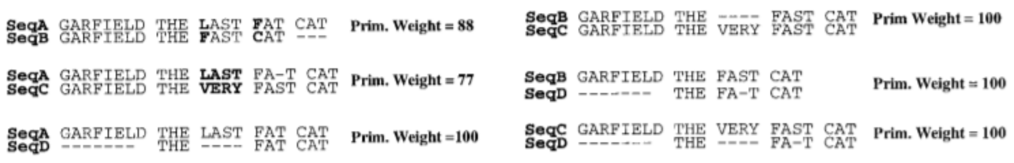

SeqA GARFIELD THE LAST FAT CAT
SeqB GARFIELD THE FAST CAT ---
Prim. Weight = 88
SeqA GARFIELD THE LAST FA-T CAT
SeqC GARFIELD THE VERY FAST CAT
Prim. Weight = 77
SeqA GARFIELD THE LAST FAT CAT
SeqD -------- THE ---- FAT CAT
Prim. Weight =100
SeqB GARFIELD THE ---- FAST CAT
SeqC GARFIELD THE VERY FAST CAT
Prim Weight = 100
SeqB GARFIELD THE FAST CAT
SeqD ------- THE FA-T CAT
Prim. Weight = 100
SeqC GARFIELD THE VERY FAST CAT
SeqD -------- THE ---- FA-T CAT
Prim. Weight = 100

Figure 4.3: Primary library created from 4 sequences. [Notredame et al., 2000, Figure 2(b)]

The two primary libraries are then combined into one by combining all identical residue pairs into one entry and summing their weights, while pairs that are only present once are added with their original weight. Residue pairs that are not present in any alignment have an implicit weight of 0.

Although the information present in the primary library is sufficient to obtain a multiple alignment, it is computationally hard to do so. Instead, the authors chose to generate what they call an extended library using the weights in the primary library.

Library extension is performed by comparing each aligned residue pair with all the others. Consider a residue pair $(A(x), B(y))$ and a sequence C. The initial weight of the pair is then increased by $min(W(A(x), C(z)), W(C(z), B(y)))$, i.e. the minimum weight associated to the alignment of some residue $C(z)$ with both $A(x)$ and $B(y)$. This is done for all residues from all sequences. In practice, most of the weights will be 0, therefore the actual algorithm computes the weights more efficiently. Library extension in effect computes how consistent a residue-pair alignment is. Figure 4.4 shows the computation of extended library.

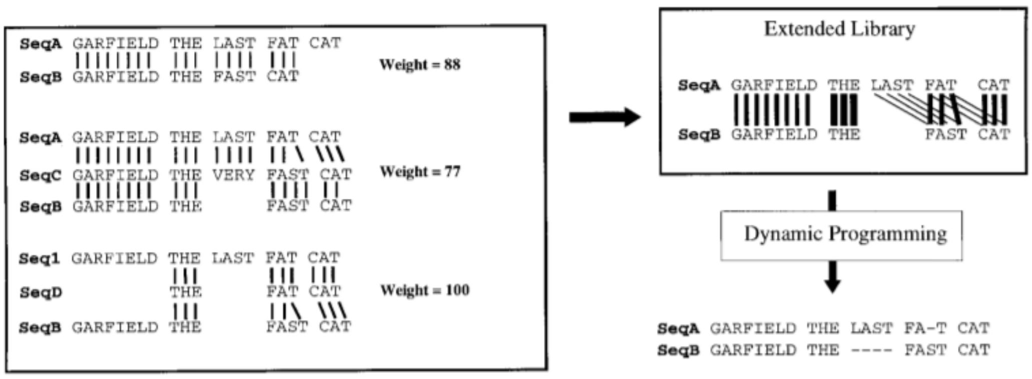

SeqA GARFIELD THE LAST FAT CAT
SeqB GARFIELD THE FAST CAT
Weight = 88
SeqA GARFIELD THE LAST FAT CAT
SeqC GARFIELD THE VERY FAST CAT
SeqB GARFIELD THE FAST CAT
Weight = 77
Seq1 GARFIELD THE LAST FAT CAT
SeqD THE FAT CAT
SeqB GARFIELD THE FAST CAT
Weight = 100
Extended Library
SeqA GARFIELD THE LAST FAT CAT
SeqB GARFIELD THE FAST CAT
Dynamic Programming
SeqA GARFIELD THE LAST FA-T CAT
SeqB GARFIELD THE ---- FAST CAT

Figure 4.4: Extended library weights for two sequences and their alignment recomputed using these weights. [Notredame et al., 2000, Figure 2(c)]

Having obtained the consistency information from the extended library, it is now possible to create the guide tree and the final multiple alignment. Using a distance matrix between all the sequences, the tree is computed as follows. First, we align the closest two sequences using dynamic programming and the weights from the extended library. In each of the following steps, we either add a sequence to an already computed alignment, or we align the next closest sequences. We repeat this step until the alignment of all sequences is complete.

Figure 4.5 shows the layout of the T-Coffee algorithm.

MAFFT

This section is based on Katoh et al. [2002].

The MAFFT method is similar to T-Coffee in that it constructs a library of alignments which it then uses to create the final multiple alignment. The authors developed MAFFT to work in multiple modes, one of which is the progressive method as described above; the other one is the iterative refinement method, which allows for alterations of the multiple alignment obtained from the progressive method.

Pairwise alignment in MAFFT uses the fact that certain amino acids have more similar physico-chemical properties than others. Substitutions tend to preserve the overall structrure of a protein, therefore substitutions of similar amino

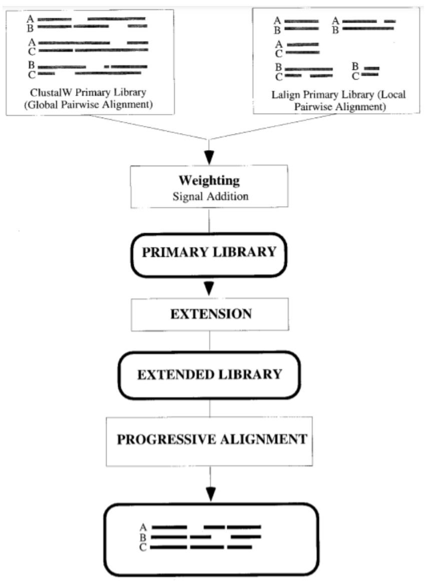

ClustalW Primary Library (Global Pairwise Alignment)
Lalign Primary Library (Local Pairwise Alignment)
Weighting
Signal Addition
PRIMARY LIBRARY
EXTENSION
EXTENDED LIBRARY
PROGRESSIVE ALIGNMENT

Figure 4.5: T-Coffee layout. [Notredame et al., 2000, Figure 1]

acids are more frequent than those of different ones. The two properties the authors use are amino acid volume and polarity.

Let us define the correlation of the volume component between two amino acid sequences with the positional lag of k as

$$c_v(k) = \sum_{1 \leq n \leq N, 1 \leq n+k \leq M} \hat{v}_1(n)\hat{v}_2(n+k)$$

where N and M are the lengths of the sequences and $\hat{v}(a) = [v(a) - \bar{v}]/\sigma_v$ is the normalized volume value with $\bar{v}$ denoting the average volume of all the amino acids and σ_v their standard deviation.

Since the sequences tend to be equal in length, computing $c_v(k)$ using naive methods takes time proportional to N^2. However, applying Fast Fourier transform to the calculation reduces the time to $\mathcal{O}(NlogN)$.

We define the polarity component correlation $c_p(k)$ analogically.

The correlation between two amino acids is then expressed as

$$c(k) = c_v(k) + c_p(k)$$

If we plot the function $c(k)$, there will be some peaks corresponding to the homologous regions of the two sequences, if there are any (Figure 4.6). However, the FFT analysis only gives us the positional lag of the regions, not their positions. To find the exact positions, we use a sliding window (of size 30 in the article), shown in Figure 4.7, and calculate the degree of local homologies for the 20 highest peaks in the $c(k)$ function. If a segment exceeding a given homology threshold is identified, we label it as a homologous region.

After finding homologous segments between two sequences, their alignment is obtained by constructing a homology matrix $S \in R^{n*n}$, where n is the number of homologous segments. The cell S_{ij} is assigned a value depending on whether the i-th homologous segments of the first sequence corresponds to the j-th homologous segment of the second sequence. If so, the cell gets a value corresponding to the

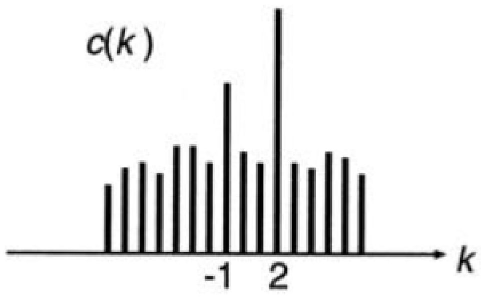


Figure 4.6: Plot of the correlation function $c(k)$. [Katoh et al., 2002, Figure 1A]

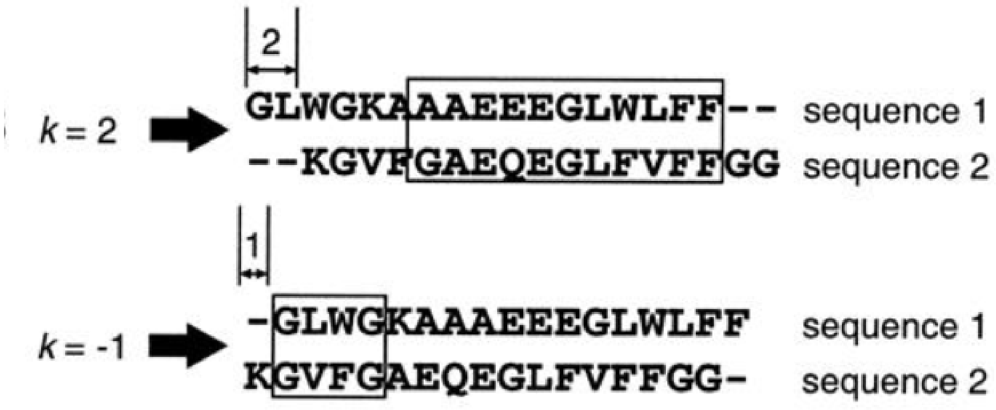


Figure 4.7: Finding homologous regions with different positional lags using a sliding window. [Katoh et al., 2002, Figure 1B]

score of this segment; otherwise it has a value of 0. The optimal arrangment of homologous segments is then obtained using dynamic programming (see Figure 4.8).

Having arranged homologous segments, the algorithm then computes pairwise alignments for each pair of sequences. As in T-Coffee, it uses the alignments to create the primary and extended libraries, which are in turn used to estimate the guide tree and the final alignment. If MAFFT is configured to perform the progressive method, this alignment is the final one. Otherwise, if iterative refinement is allowed, MAFFT uses the weights from the library to adjust the alignment to get a more optimal one. However, iterative refinement is very slow from a relatively low number of sequences, therefore it is not suitable for a large dataset.

4.3 Sequence alignment for chant melodies

As we have discussed before, melodies of Gregorian chant are in many ways similar to biological sequences. The alphabet is different (instead of 20 amino acids in proteins or 4 nucleotide bases in DNA we have around 40 different characters

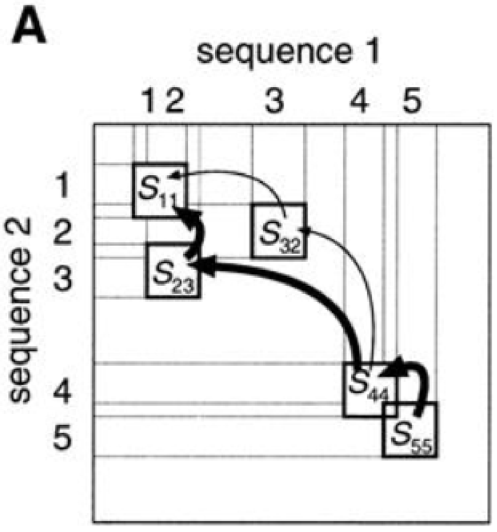


Figure 4.8: Dynamic programming applied to segment arrangement. [Katoh et al., 2002, Figure 2A]

used in melody representation) and the chants are usually shorter in length. The evolution of both biological and melodic sequences is guided by environmental factors such as migration to other places. Some segments tend to undergo a lot of modifications, while other remain relatively unchanged. Studying the alignment of chant melodies can reveal a lot of information about their relationship.

An important aspect to consider is that unlike in bioinformatics, here we are working with two closely related sequences - the melody and the text. They cannot be separated, as they always developed concurrently. Additionally, textual boundaries are important for the segmentation of melodies [Cornelissen et al., 2020]. Here, we do not treat boundary symbols as special characters. However, in the future, it is worth studying whether they should be treated as such.

In the following sections, we describe three approaches to melody alignment used in our application: word-based alignment, alignment on pitches, and alignment on intervals. They all come with their pros and cons. Word-based alignment is a fast method that can provide insight into how the tradition changed over time. It reveals how the length and complexity of otherwise similar chants evolved. Alignment on pitches compares the absolute pitch of chants. It can help identify contrafacta (chants with the same melody but different texts), which was a difficult task until now. However, this approach is unable to identify similar chants differing only by a fixed interval (transposition). Alignment on intervals compares the interval differences between subsequent notes. It is useful for identifying transpositions. However, chants with different notes in a few positions but otherwise identical will be evaluated as dissimilar.

4.3.1 Word-based alignment

The word-based approach serves as a basic tool to show the relationship between the text setting and melody. It is meant primarily for comparing melodies of the same or similar text, such as chants belonging to the same liturgical position. It can reveal how the complexity of chants evolved over time. The algorithm aligns the syllables of all chants in such a way that the syllables in the same position are in one column. Thanks to this, the differences in complexity are clearly visible.

The alignment is computed using Algorithm 1. Its results can be seen in Figure 4.9.

Algorithm 1: Naive approach to alignment

```
input : set of volpiano-encoded melodies $V = \{V_1, \dots, V_k\}$, $V_i$ is
        composed of $w_i$ words $V_i = \{W_{i1}, \dots, W_{iw_i}\}$, $W_{ij}$ is composed of
        $s_{ij}$ syllables $W_{ij} = \{S_{ij1}, \dots, S_{ijs_{ij}}\}$; set of texts $T = \{T_1, \dots, T_k\}$,
        $T_i$ is composed of $w_i$ words $T_i = \{U_{i1}, \dots, U_{iw_i}\}$, $U_{ij}$ is composed
        of $r_{ij}$ syllables $U_{ij} = \{R_{ij1}, \dots, R_{ijr_{ij}}\}$
output: Aligned set of melodies $V^* = \{V_1^*, \dots, V_k^*\}$, $V_i^*$ is composed of $w$
        words $V_i^* = \{W_{i1}^*, \dots, W_{iw}^*\}$, $W_{ij}^*$ is composed of $s_j$ syllables
        $W_{ij}^* = \{S_{ij1}^*, \dots, S_{ijs_j}^*\}$; and their texts $T^* = \{T_1^*, \dots, T_k^*\}$, $T_i^*$ is
        composed of $w$ words $T_i^* = \{U_1^*, \dots, U_{iw}^*\}$, $U_{ij}^*$ is composed of $s_j$
        syllables $U_{ij}^* = \{R_{ij1}^*, \dots, R_{ijs_j}^*\}$

$w \longleftarrow \max_i w_i$;
initialize each $V_i^*$ and $T_i^*$ to be of length $w$;
for $j \in \{1, \dots, w\}$ do
    $s_j \longleftarrow \max_i s_{ij}$;
    set each $W_{ij}^*$ and $U_{ij}^*$ to be of length $s_j$;
end
for $i \in \{1, \dots, k\}$ do
    for $j \in \{1, \dots, w_i\}$ do
        for $m \in \{1, \dots, s_{ij}\}$ do
            $S_{ijm}^* = S_{ijm}$;
            if $s_{ij} < r_{ij}$ then
                if $m = s_{ij}$ then
                    $R_{ijm}^* = concat(R_{ijm}, \dots, R_{ijr_{ij}})$;
                else
                    $R_{ijm}^* = R_{ijm}$;
                end
            else if $s_{ij} > r_{ij}$ then
                if $m > r_{ij}$ then
                    $R_{ijm}^* = ""$;
                else
                    $R_{ijm}^* = R_{ijm}$;
                end
            else
                $R_{ijm}^* = R_{ijm}$;
        end
    end
end
return $V*$, $T*$;
```

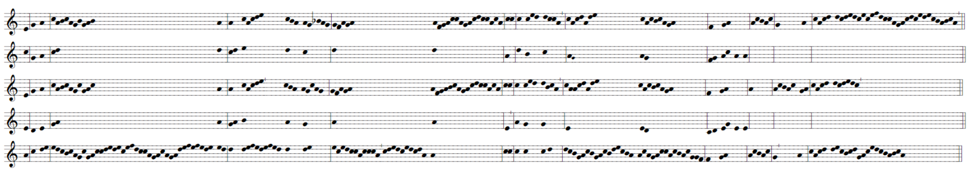


Figure 4.9: Chants of different genres aligned using the naive approach. The vertical lines represent word boundaries.

4.3.2 Melody preprocessing

The alignment software uses the character `-` for marking gaps, it requires that the input sequences do not contain any, or they will be removed. Since melodies encoded as Volpiano use the character to mark ends of words and ends of syllables, we need to perform some preprocessing. Namely, we replace all contiguous sequences `---` with the end-of-word marking symbol `~` and all contiguous sequences `--` with the end-of-syllable marker `|`. All remaining `-`s are removed, if there are any.

4.3.3 Multiple alignment using absolute pitches

For this task, we are using the MAFFT software[1]. MAFFT primarily works for sequences of amino acids and nucleotide bases, but it also has a limited support for non-biological sequences.

After we process the sequences as described in Section 4.3.2, they are passed to MAFFT with the option `--text`, which indicates that the sequences are not biological. Additionally, we also pass the option `--reorder`, which returns the aligned sequences in order of similarity. We made this choice so as to facilitate the identification of related melodies.

After MAFFT performs the alignment, we retrieve the sequences and attempt to combine them with their text. We do this by splitting both the text and the melody into syllables and mapping them onto each other (Algorithm 2). However, this might not be possible. Due to errors in the original encoded melody (i.e. a missing or an extra `-`), we may have altered the structure of the chant in preprocessing. In case of such an event, we remove the affected sequence from consideration and align the remaining sequences again.

The process is described in Algorithm 3. Its results are shown in Figure 4.10.

[1]`https://mafft.cbrc.jp/alignment/software/`

Algorithm 2: Aligning melody and text

```
input  : volpiano-encoded melody $V$, $V$ is composed of $w$ words
         $V = \{W_1, \dots, W_w\}$, $W_i$ is composed of $s_i$ syllables
         $W_i = \{S_{i1}, \dots, S_{is_i}\}$; text $T$, $T$ is composed of $w$ words
         $T = \{U_1, \dots, U_w\}$, $U_i$ is composed of $r_i$ syllables
         $U_i = \{R_{i1}, \dots, R_{ir_i}\}$
output: text $T*$ modified to match the melody; $T*$ is composed of $w$
         words $T^* = \{U_1^*, \dots, U_w^*\}$, $U_i^*$ is composed of $s_i$ syllables
         $U_i^* = \{R_{i1}^*, \dots, R_{is_i}^*\}$

for $i \in \{1, \dots, w\}$ do
    if $s_i < r_i$ then
        $R_{ij}^* = R_{ij} \forall j \in \{1, \dots, s_i - 1\}$;
        $R_{is_i}^* = concat(R_{is_i}, \dots, R_{ir_i})$;
    else if $s_i > r_i$ then
        $R_{ij}^* = R_{ij} \forall j \in \{1, \dots, r_i\}$;
        $R_{ij}^* = "" \forall j \in \{r_i + 1, \dots, s_i\}$;
    else
        $R_{ij}^* = R_{ij} \forall j \in \{1, \dots, s_i\}$;
end
return $T^*$;
```

Once all sequences are successfully aligned without errors in text and melody combination, we can display them to the user. In the application, we use the Volpiano font, so as to maintain consistency. However, the sequences shown are not properly encoded following Volpiano protocols. First of all, we choose different representations of end of a word (here we use a bar line) and end of a syllable (a single space) so that the number of characters in each sequence remains equal and the alignment is visible. Second of all, after the alignment, MAFFT will have inserted -s to represent gaps. In proper Volpiano, these characters represent gaps between words, syllables, and neumes. However, here they just mean empty space.

Algorithm 3: Multiple alignment using absolute pitches

```
input  : a set of volpiano-encoded melodies $V$ with their respective texts $T$
output: aligned melodies $V^*$ and their texts $T^*$
$\hat{V} \longleftarrow V$ preprocessed to a MAFFT-friendly format;
$aligned\_without\_errors \longleftarrow False$;
while not $aligned\_without\_errors$ do
    $aligned\_without\_errors \longleftarrow True$;
    $V^* \longleftarrow$ result after running $\hat{V}$ through MAFFT;
    for $V_i^* \in V^*$ do
        $T_i^* \longleftarrow$ result of algorithm 2 on $V_i^*$ and $T_i$;
        if $T_i^*$ cannot be calculated then
            $\hat{V} \longleftarrow \hat{V} \setminus \{\hat{V}_i\}$;
            $aligned\_without\_errors \longleftarrow False$;
        end
    end
end
return $V^*$ and $T^*$;
```

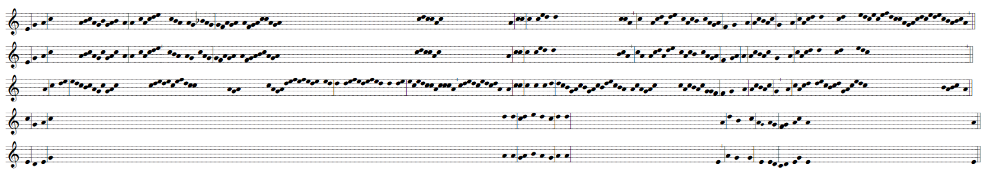


Figure 4.10: Chants aligned using MAFFT on absolute pitches.

4.3.4 Multiple alignment using intervals

The general outline of the algorithm is the same as Algorithm 3. However, as we are not aligning absolute pitches, but rather intervals, we need to compute these intervals.

There are 18 possible pitches, which means 37 possible intervals (17 positive, 17 negative, and one without the change of pitch). We will represent the no-change interval with the character `a`, the positive intervals with the lowercase characters `b-t` and the negative intervals with the uppercase characters `B-T`. The characters `i` and `I` are not used for reasons explained later.

The interval representation is constructed from a Volpiano-encoded melody by replacing the note symbols with the appropriate interval symbol. The i-th note will be replaced with the symbol representing the interval $(i-1, i)$. As the first note has no predecessor, it is left as it is. The non-note symbols also remain unchanged. Algorithm 4 shows how the interval representation is constructed.

Algorithm 4: Converting volpiano-encoded melody into interval representation

```
input  : volpiano-encoded melody $V = v_1 v_2 \dots v_m$, note symbols $N$,
         interval symbols $J$, $J_{ab}$ is the symbol representing the interval
         $(a, b)$
output: interval representation of the input melody $I = i_1 i_2 \dots i_m$
for $k \in \{1, \dots, m\}$ do
    if $v_k \notin N$ then
        $i_k \longleftarrow v_k$;
    else if $v_k \in N \land v_l \notin N \; \forall l < k$ then
        $i_k \longleftarrow v_k$;
        $last\_seen\_note \longleftarrow v_k$;
    else
        $i_k \longleftarrow J_{last\_seen\_note, v_k}$;
        $last\_seen\_note \longleftarrow v_k$;
end
return $I$;
```

We use the interval representations as inputs to MAFFT. That means that what MAFFT returns are the aligned sequences of intervals. To display them to the user properly, we need to decode the sequences. Algorithm 5 shows how to do this.

Algorithm 5: Converting interval representation back to volpiano

```
output: interval representation of a melody $I = i_1 i_2 \dots i_m$, note symbols
        $N$, interval symbols $J$, $J_{ab}$ is the symbol representing the interval
        $(a, b)$
input  : volpiano-encoded equivalent of the input melody $V = v_1 v_2 \dots v_m$
for $k \in \{1, \dots, m\}$ do
    if $i_k \in N \land i_l \notin N \; \forall l < k$ then
        $v_k \longleftarrow i_k$;
        $last\_seen\_note \longleftarrow i_k$;
    else if $i_k \in J \land \exists l : i_l < k \land i_l \in N$ then
        $v_k \longleftarrow a, s.t. \; J_{last\_seen\_note, a} = i_k$;
        $last\_seen\_note \longleftarrow v_k$;
    else
        $v_k \longleftarrow i_k$;
end
return $V$;
```

The reason why `i` and `I` do not represent any interval is that they represent non-note symbols (flat and natural signs). If we used the characters for intervals, it would be problematic to convert an interval representation to Volpiano encoding. As we are looking at whether a character is a note or an interval or neither, if they represented an interval, we would choose the appropriate (interval) branch in Algorithm 5. However, if they had originally represented a non-note symbol, we would mistakenly shift the rest of the melody by an interval.

The complete algorithm to calculate the interval alignment is shown in Algorithm 6, similar to Algorithm 3, and its results are shown in Figure 4.11.

Algorithm 6: Multiple alignment using intervals

```
input  : a set of $n$ volpiano-encoded melodies $V$ with their respective texts $T$
output: aligned melodies $V^*$ and their texts $T^*$
$I_i \longleftarrow V_i$ converted using algorithm 4 $\forall i \in \{1, \ldots, n\}$;
$\hat{I} \longleftarrow I$ preprocessed to a MAFFT-friendly format;
$aligned\_without\_errors \longleftarrow False$;
while not $aligned\_without\_errors$ do
    $aligned\_without\_errors \longleftarrow True$;
    $I^* \longleftarrow$ result after running $\hat{I}$ through MAFFT;
    $V_i^* \longleftarrow I_i^*$ converted using algorithm 5 $\forall i \in \{1, \ldots, n\}$;
    for $V_i^* \in V^*$ do
        $T_i^* \longleftarrow$ result of algorithm 2 on $V_i^*$ and $T_i$;
        if $T_i^*$ cannot be calculated then
            $\hat{I} \longleftarrow \hat{I} \setminus \{\hat{I}_i\}$;
            $aligned\_without\_errors \longleftarrow False$;
        end
    end
end
return $V^*$ and $T^*$;
```

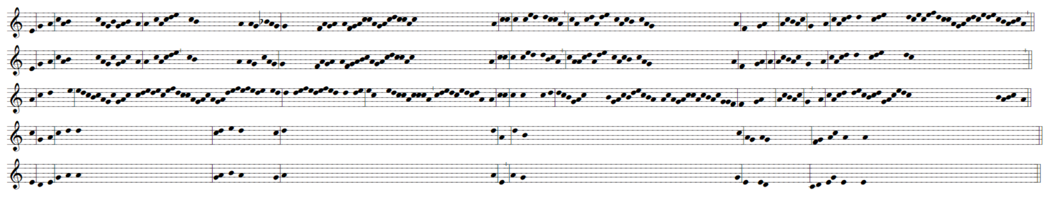


Figure 4.11: Chants aligned using MAFFT on intervals.

4.4 Conservation profile

Having obtained the alignment of chants, we can borrow other bioinformatics concepts to calculate interesting characteristics. One example is *conservation profile*. Given a set of aligned sequences $A = \{A_1, \ldots, A_n\}$, $A_i = a_{i1}a_{i2}\ldots a_{ik}$, we define the conservation value of element A_{ij} as

$$con(A_{ij}) = \frac{\sum_{l=1}^{n} \mathbb{1}[A_{lj} = a_{ij}]}{|A|}$$

In other words, the conservation value gives the proportion of the symbol a_{ij} at position j over all sequences.

Conservation profile is then the vector C whose elements C_j are defined as

$$C_j = \frac{\sum_{i=1}^{n} con(A_{ij})}{|A|}$$

Our application does not visualize conservation profile, but rather the conservation values of all meaningful symbols (i.e. those that represent notes or intervals). It also computes the average conservation value $\frac{\sum_{j=1}^{k} C_j}{k}$.

Conservation profile of aligned sequences depends on what approach we choose. Consider the last two chants shown in Figure 4.11. Each note is different, however, a person well-versed in musical theory immediately notices that they are only shifted by 5 semitones (except for the first note). If we consider only the intervals, they are almost the same melodies. However, if we consider the absolute pitches, they are totally different. Figure 4.12 and Figure 4.13 demonstrate these differences by displaying the chants' conservation profile.

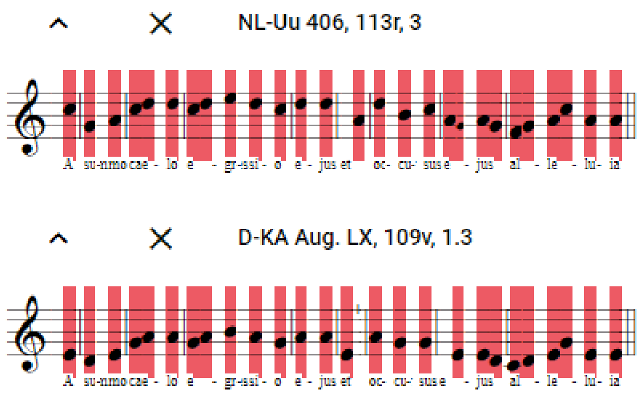

NL-Uu 406, 113r, 3
A su-nmo cae - lo e - gr-asi - o e - jus et oc- cu- sus e - jus al - le - lu- ia
D-KA Aug. LX, 109v, 1.3
A su-nmo cae - lo e - gr-asi - o e - jus et oc- cu- sus e - jus al - le - lu- ia

Figure 4.12: Conservation profile on chants aligned by pitch.

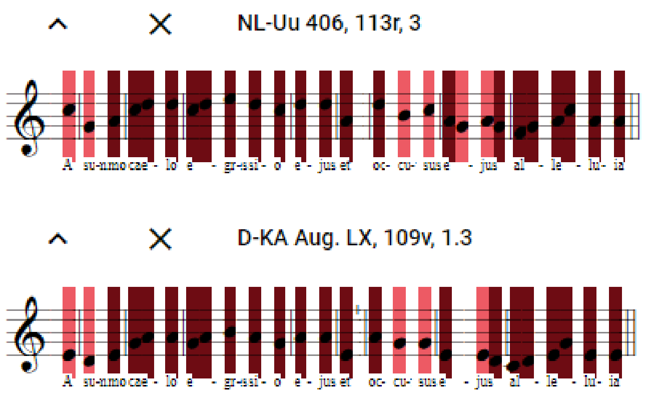

NL-Uu 406, 113r, 3
A su-nmo cae - lo e - gr-asi - o e - jus et oc- cu- sus e - jus al - le - lu- ia
D-KA Aug. LX, 109v, 1.3
A su-nmo cae - lo e - gr-asi - o e - jus et oc- cu- sus e - jus al - le - lu- ia

Figure 4.13: Conservation profile on chants aligned by intervals.

5. Development documentation

The software is a locally-run web application. Setup instructions can be found in attachment ??. It consists of three principal parts that ensure its proper functioning: the database, back end and front end. Their interactions are outlined in Figure 5.1.

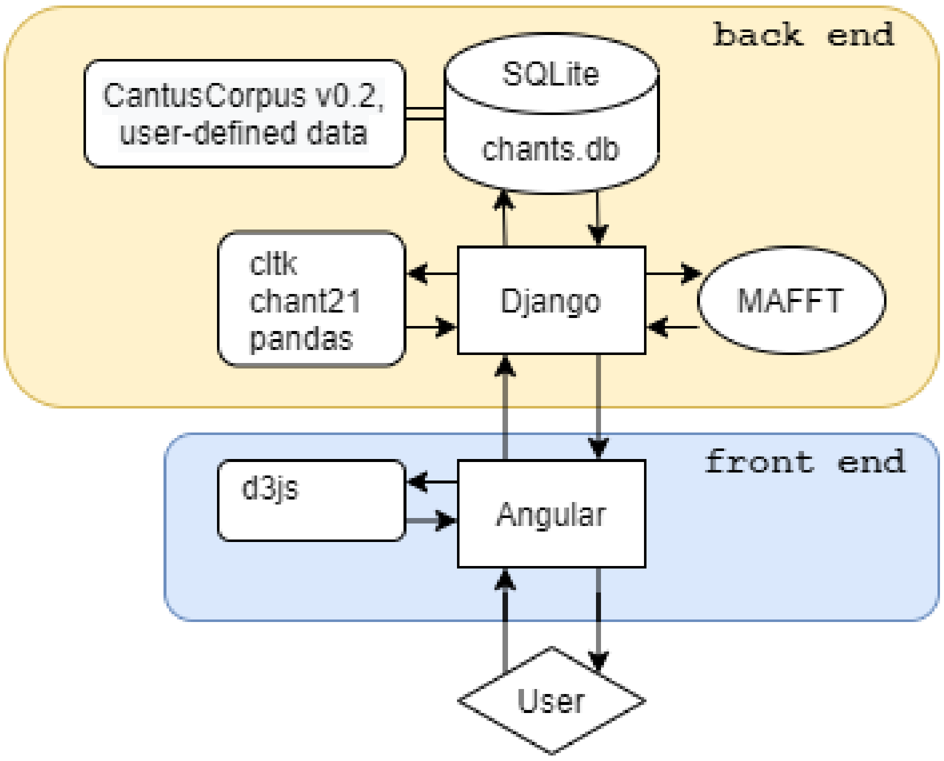


Figure 5.1: A high-level overview of the application's architecture.

The database stores the data used by the application. The data it contains do not impact the functionality of the application. It can be added to or removed from, as long as the added data follows the schema. It is even possible to have multiple databases and use the one that is currently needed.

The back end is the part of the application that takes care of the internal logic. It pulls data from the database and adds new ones. It performs calculations that would be too compute-intensive for the front end. The back end is interacted with via its API: anyone can make an appropriate http request to a specified URL and the back end returns the corresponding response.

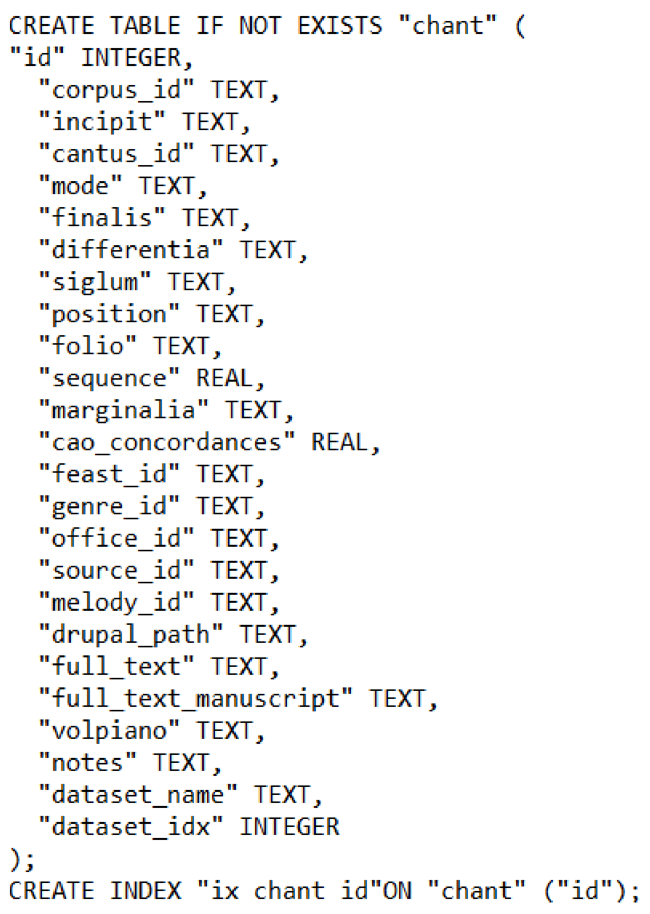
The front end is the user-facing interface. Its main function is to display data returned by the back end. It can also perform some lighter calculations. The user interacts with the front end via a web browser.

In the following sections, we will describe the proper functioning of each part in more detail.

5.1 Data

In this application, we use SQLite[1] as our database technology. It is a lightweight and self-contained database engine, which makes it easy to work with. It is the predefined database for the back end technology and comes with several drawbacks, such as a relatively low performance. However, as our use case is not data-heavy, we have not opted for a different technology since we prefer flexibility over performance.

Our database consists of a single table `chant`. The fields of one entry are described in Section 3.2. Its schema is shown in Figure 5.2.



```
CREATE TABLE IF NOT EXISTS "chant" (
"id" INTEGER,
  "corpus_id" TEXT,
  "incipit" TEXT,
  "cantus_id" TEXT,
  "mode" TEXT,
  "finalis" TEXT,
  "differentia" TEXT,
  "siglum" TEXT,
  "position" TEXT,
  "folio" TEXT,
  "sequence" REAL,
  "marginalia" TEXT,
  "cao_concordances" REAL,
  "feast_id" TEXT,
  "genre_id" TEXT,
  "office_id" TEXT,
  "source_id" TEXT,
  "melody_id" TEXT,
  "drupal_path" TEXT,
  "full_text" TEXT,
  "full_text_manuscript" TEXT,
  "volpiano" TEXT,
  "notes" TEXT,
  "dataset_name" TEXT,
  "dataset_idx" INTEGER
);
CREATE INDEX "ix chant id"ON "chant" ("id");
```

Figure 5.2: Schema of the *chant* table.

The last two fields, `dataset_name` and `dataset_idx` determine to which data source the row belongs. Data source is the main grouping criterion for data in this application. The user may select multiple data sources for comparison. The expected amount of data in each data source is in the order of thousands of entries at most. We chose to store all data in one database, as opposed to e.g. having one database for each data source, as the expected scale of data does not justify working with a more complex scheme.

[1] `https://www.sqlite.org/`

5.2 Back end

The Python programming language is often used in academic contexts. It allows for rapid development and great flexibility. Python applications are easily integrated with other programs, which we need for MAFFT integration. There are also many libraries available for working with data in general (e.g. `pandas`) and for our specific data (`cltk` for working with Latin texts, `chant21` for working with chants). Because of these properties, we decided to use Python for our application's back end.

The back end uses the Django framework.[2] Django is a Python web framework enabling developers to create web applications quickly, having abstracted away the most tedious of web development aspects.

Django programs consist of one or more logical units called *apps*. An *app* is a self-contained program providing some related functionality. Thanks to Django's modularity, an *app* can be plugged in into many projects without the need to always rewrite it. Our application only uses one *app*, `melodies`, which provides REST API to other programs.

The app only contains one app, `melodies`, which provides the API for other applications. The app uses the module `core` providing the essential computations.

To ensure proper integration with the front end, it is necessary to include allow front end's server to interact with the back end. This is done by including front end's URL in the array `CORS_ORIGIN_WHITELIST` in the `settings.py` file. In the event of deployment, the URL would need to be changed appropriately.

5.2.1 REST API

The `melodies` app provides API that offers other programs a way of interacting with it. It is done in the form of web requests to a specific URL. The requests can be either GET or POST requests. GET requests do not contain any additional data; the response returned always depends only on the state of the application. On the contrary, POST requests contain data that the application takes into account when constructing the response.

Table 5.1 summarizes the API provided by the application. The API is described into more detail below.

Endpoint	Method	POST fields	Description
api/chants/	POST	`dataSources`, `incipit`, `genres`, `offices`	Returns a list of chants filtered by their data source, incipit, genre and office
api/chants/<pk>	GET		Returns the chant with the ID `<pk>`
api/chants/sources	GET		Returns a list of all data sources currently present in the database with their name and index

[2]https://www.djangoproject.com/

api/chants/upload/	POST	`file`, `name`	Uploads `file` to the database as a new data source and gives it the specified `name`
api/chants/export/	POST	`idsToExport`	Returns a CSV file containing the chants with the specified IDs
api/chants/create-dataset/	POST	`idsToExport`, `name`	Creates a new data source from the chants with the specified IDs and gives it the specified `name`
api/chants/align/	POST	`idsToAlign`, `mode`	Takes chants with the specified IDs and aligns them according to `mode`

Table 5.1: API of back end.

- **api/chants/** The POST request must contain the fields as specified in Table 5.1. `dataSources` is a list of indices of allowed data sources as stored in the database. `incipit` is a string that must be present as a substring in the *incipit* field in each of the returned entries. `genres` and `offices` are lists of strings, where each string is an identifier of a genre or an office, as seen in Attachment A and Attachment B. Each returned entry must have its genre be an element of `genres` and its office be an element of `offices`. The response is a list of all entries in the database satisfying these constraints.

- **api/chants/<pk>** The application looks for a chant with the ID `pk` in the database. It returns an error if no such entry exists. If it does, it returns a JSON object with the following keys: *db_source*, which is the entry as stored in the database, *json_volpiano*, which is the chant processed in such a way that its melody and text are easy to display in an HTML template, and *stresses*, a list of stressed syllables corresponding to the chant's text, if it can be computed.

- **api/chants/sources** The response is a JSON object with one key, `sources`. Its value is the list of pairs representing the data sources currently present in the database. The first value of each pair is a data source index and the second one is its name.

- **api/chants/upload/** The POST request must contain a CSV file as specified in Section 3.3 in the field `file` and a string `name`. The data in the file will be uploaded directly to the database as a new data source with the given name. Some values may be changed before inserting the data in the database, namely the columns *id*, *dataset_idx*, and *dataset_name*, if the file contains them. The response is a JSON object with the keys *name*, the name of the new data source, and *index*, the index assigned to it.

- **api/chants/export/** The POST request body must contain the field `idsToExport`. It is a list of integers representing the IDs of the chants to be exported. If an ID does not correspond to any chant in the database, the ID will be excluded. The response contains a CSV file with its entries being the corresponding chants, formatted as outlined in Section 3.3.

- **api/chants/create-dataset/** The POST request must contain a list of chant IDs in the field `idsToExport` and a string in the field `name`. The chants that correspond to the IDs will be duplicated in the database, given new IDs and assigned to a new data source with the name as specified in the field `name`. The response is the same JSON object as in the *upload* API, containing the keys *name* and *index*, the name and index of the newly created data source.

- **api/chants/align/** The POST request contains two fields. `idsToAlign` is the list of chant IDs we want to align. `mode` is the mode of alignment we chose. Its values can be *syllables*, which is the word-based alignment, *full*, the alignment on pitches, or *intervals*, the alignment on intervals. If the value is not one of those, the request will return an error. The response is a JSON object with the following keys: *chants* is an object representing the aligned melodies along with their texts, easily renderable by an HTML template. *errors* contains a list of chant IDs of the chants that could not be aligned for various reasons. *successes* contains an object that describes the chants that have been successfully aligned: *sources* are their original sources (i.e. siglum, folio and position), *ids* the IDs as stored in the database, *volpianos* the melodies as given by the alignment algorithm, and *urls* the values in the *drupal_path* field of the database.

5.2.2 Core

`core` is the Python module that contains essential functionality ensuring the proper behavior of the application, e.g. the implementation of alignment, MAFFT integration, and others. Figure 5.3 outlines the classes provided in the submodule and how they interact. The classes' functionality is described below.

- **Exporter.** The class contains one method, `export_to_csv`. It takes as an argument a list of chant IDs contained in the database. It returns a response with a file with the corresponding database entries formatted as CSV. Used by the API call `api/chants/export/`.

- **Uploader.** The class defines one method, `upload_csv`. Its arguments are a *pandas*[3] dataframe, containing data columns as described in Section 3.2, and a dataset name. The method inserts the data into the database, ensuring that no duplication of IDs occurs. Input sanitization is done by the Django framework. Used by the API calls `api/chants/create-dataset/` and `api/chants/upload/`.

- **ChantProcessor.** The class contains functionality for working with Latin texts and with melodies encoded as Volpiano. The class is used by the API call `api/chants/<pk>`. The method `get_syllables_from_text` takes a string of Latin text and returns the text syllabified: the returned value

[3]`https://pandas.pydata.org/`

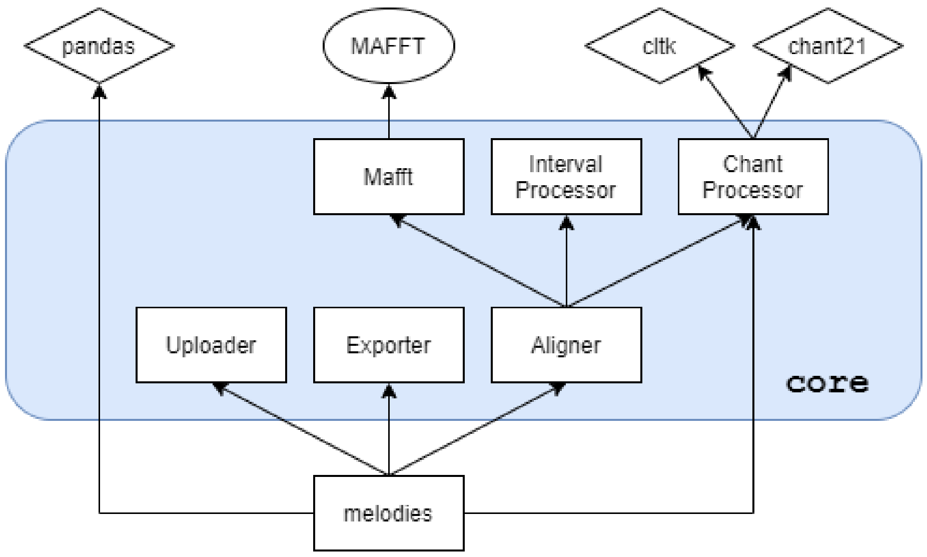


Figure 5.3: Outline of the classes contained in *core* and their interaction. An arrow from A to B indicates that A depends on B. The elements in rectangles are classes, the elements in rhombi are external libraries, MAFFT is an external application.

is a list, each of whose elements represents a word of the text, and each word is a list of strings representing the syllables in that word. To syllabify the text, we use the module `cltk`,[4] which facilitates working with classical languages, including Latin.

Some parts of the application require the encoded melody to contain no `-` characters. Instead, they assume that ends of words are marked with a tilde (`~`) and ends of syllables with a pipe (`|`). The method that converts proper Volpiano-encoded melody to this processed format is the method `insert_separator_chars`. The equivalent of syllabifying text for melodies is `get_syllables_from_volpiano`. It takes a melody encoded as a processed Volpiano string (with `~` and `|` instead of `-`.). It assumes that the melody contains a clef at the first position and a bar line at the last position, which is the proper way of encoding melodies according to the Volpiano protocols.[5] The method returns a list whose elements represent words, and each word is a list of strings representing syllables (equivalent to the syllabifying method for text). Examples of using these functions are shown in Figure 5.4 and Figure 5.5.

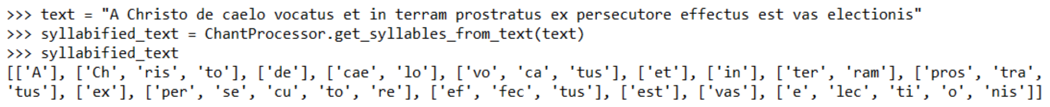
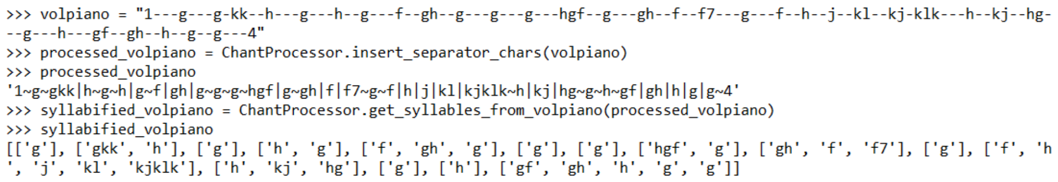

```
>>> text = "A Christo de caelo vocatus et in terram prostratus ex persecutore effectus est vas electionis"
>>> syllabified_text = ChantProcessor.get_syllables_from_text(text)
>>> syllabified_text
[['A'], ['Ch', 'ris', 'to'], ['de'], ['cae', 'lo'], ['vo', 'ca', 'tus'], ['et'], ['in'], ['ter', 'ram'], ['pros', 'tra',
'tus'], ['ex'], ['per', 'se', 'cu', 'to', 're'], ['ef', 'fec', 'tus'], ['est'], ['vas'], ['e', 'lec', 'ti', 'o', 'nis']]
```

Figure 5.4: Example of dividing Latin text into syllables using *ChantProcessor*.

The method `get_stressed_syllables` takes a Latin string as input and returns a list whose elements represent words, where word is a list of 0s and

[4] `http://cltk.org/`

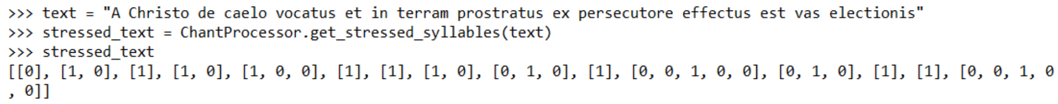
[5] `https://cantus.uwaterloo.ca/sites/default/files/documents/2.%20Volpiano%20Protocols.pdf`



```
>>> volpiano = "1---g---g-kk--h---g---h--g---f--gh--g---g---g---hgf--g---gh--f--f7---g---f--h--j--kl--kj-klk---h--kj--hg-
--g---h---gf--gh--h--g--g---4"
>>> processed_volpiano = ChantProcessor.insert_separator_chars(volpiano)
>>> processed_volpiano
'1~g~gkk|h~g~h|g~f|gh|g~g~g~hgf|g~gh|f|f7~g~f|h|j|kl|kjklk~h|kj|hg~g~h~gf|gh|h|g|g~4'
>>> syllabified_volpiano = ChantProcessor.get_syllables_from_volpiano(processed_volpiano)
>>> syllabified_volpiano
[['g'], ['gkk', 'h'], ['g'], ['h', 'g'], ['f', 'gh', 'g'], ['g'], ['g'], ['hgf', 'g'], ['gh', 'f', 'f7'], ['g'], ['f', 'h
', 'j', 'kl', 'kjklk'], ['h', 'kj', 'hg'], ['g'], ['h'], ['gf', 'gh', 'h', 'g', 'g']]
```

Figure 5.5: Example of dividing a melody encoded as Volpiano into syllables using *ChantProcessor*.

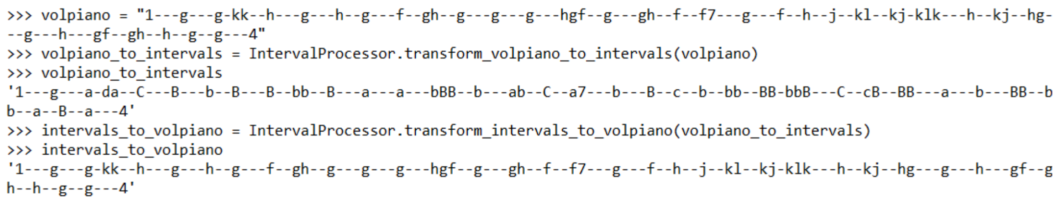
1s, a 0 representing an unstresed syllable and a 1 representing a stressed one. To calculate the stressed syllables, we use the module `cltk`. However, its stress recognition is not completely accurate, therefore this method may also return incorrect results. However, no other functionality depends on the results of the stress calculation. The function is shown in use in Figure 5.6.



```
>>> text = "A Christo de caelo vocatus et in terram prostratus ex persecutore effectus est vas electionis"
>>> stressed_text = ChantProcessor.get_stressed_syllables(text)
>>> stressed_text
[[0], [1, 0], [1], [1, 0], [1, 0, 0], [1], [1], [1, 0], [0, 1, 0], [1], [0, 0, 1, 0, 0], [0, 1, 0], [1], [1], [0, 0, 1, 0
, 0]]
```

Figure 5.6: Example of finding the stressed syllables of a Latin text using *ChantProcessor*.

- **IntervalProcessor.** The class provides tools to work with the interval representation of a melody. It contains two methods, `transform_volpiano_to_intervals` and `transform_intervals_to_volpiano`. `transform_volpiano_to_intervals` takes a string representing a melody (it can be encoded either as dictated by the Volpiano protocol, or processed to have its words separated by `~`s and syllables by `|`s for the purposes of alignment, see Section 4.3.2) and returns the same melody represented as intervals. `transform_intervals_to_volpiano` is its reverse: it takes a string representing a melody encoded by intervals and returns the Volpiano representation. Figure 5.7 shows how these functions are used.



```
>>> volpiano = "1---g---g-kk--h---g---h--g---f--gh--g---g---g---hgf--g---gh--f--f7---g---f--h--j--kl--kj-klk---h--kj--hg-
--g---h---gf--gh--h--g--g---4"
>>> volpiano_to_intervals = IntervalProcessor.transform_volpiano_to_intervals(volpiano)
>>> volpiano_to_intervals
'1---g---a-da--C---B---b--B---B--bb--B---a---a---bBB--b---ab--C--a7---b---B--c--b--bb--BB-bbB---C--cB--BB---a---b---BB--b
b--a--B--a---4'
>>> intervals_to_volpiano = IntervalProcessor.transform_intervals_to_volpiano(volpiano_to_intervals)
>>> intervals_to_volpiano
'1---g---g-kk--h---g---h--g---f--gh--g---g---g---hgf--g---gh--f--f7---g---f--h--j--kl--kj-klk---h--kj--hg---g---h---gf--g
h--h--g--g---4'
```

Figure 5.7: Transforming a Volpiano-encoded melody into an interval representation and back.

- **Mafft.** This class provides the interface for working with the MAFFT software.[6] The software must be installed on the computer that runs the application. On Windows systems, it is assumed that it is installed in a WSL instance.[7] On other systems, it has to be installed natively.

[6]`https://mafft.cbrc.jp/alignment/software/`
[7]`https://docs.microsoft.com/en-us/windows/wsl/`

An instance of the class encapsulates the action of aligning one set of data. It needs to have a specified input file, and, optionally, an output file, which can be set via the methods `set_input` and `set_output`. If the user wishes to run the alignment with other options as specified in MAFFT's documentation, it can be done using the method `add_option`. The method `add_volpiano` can optionally be used if the user does not want to provide their own file (however, its location must still be defined) or wishes to add another sequence to align. MAFFT is only run by calling `run_process`. The result of the alignment is retrieved using the methods `get_aligned_sequences` and `get_sequence_order`, which return the aligned sequences and their headers, respectively, in the order of similarity.

- **Aligner.** The class defines the methods to compute the three types of alignment, as described in Section 4.3: `alignment_syllables`, which performs the word-based alignment; `alignment_pitches`, computing the alignment of pitches; and `alignment_intervals`, which return the alignment of intervals. All of them take as an argument just the list of IDs of the chants to be aligned and return a dictionary easy to work with in HTML templates. `alignment_syllables` does not use the class `Mafft`, the other two do. `alignment_intervals` also uses `IntervalProcessor`. The class is used by the API call `api/chants/align/`.

5.3 Front end

For the front end, our application uses the Angular framework.[8] An Angular application consists of components, which are small, relatively self-contained units exposing some functionality of the application (both appearance and behavior), and services, providing means of sharing and manipulating data, e.g. the interaction with the back end. Both components and services should only contain a small, logically contained set of functionality. This makes the application safe and scalable. Most importantly, the framework keeps track of the data passed to it and updates the appearance dynamically.

This application contains several components and services that interact with each other. Figure 5.8 shows a diagram of the front end architecture.

The following sections describe each service and component in more detail.

5.3.1 Services

- **ChantService.** This service is the service responsible for communication with the back end. It uses back end's API as described in Section 5.2.1 to obtain the desired data. The method `getChant`, taking a single number as an argument, sends a request to the back end to retrieve the chant with the ID equal to the argument. The method `loadData` uses the current values stored int *IncipitService*, *SearchFilterService*, and *DataSourceService* to obtain all chants adhering to the constraints; the method `getList` provides the object where these results are stored. The method `getAlignment` takes a list of chant IDs and an alignment mode and makes a request to the back

[8] https://angular.io/

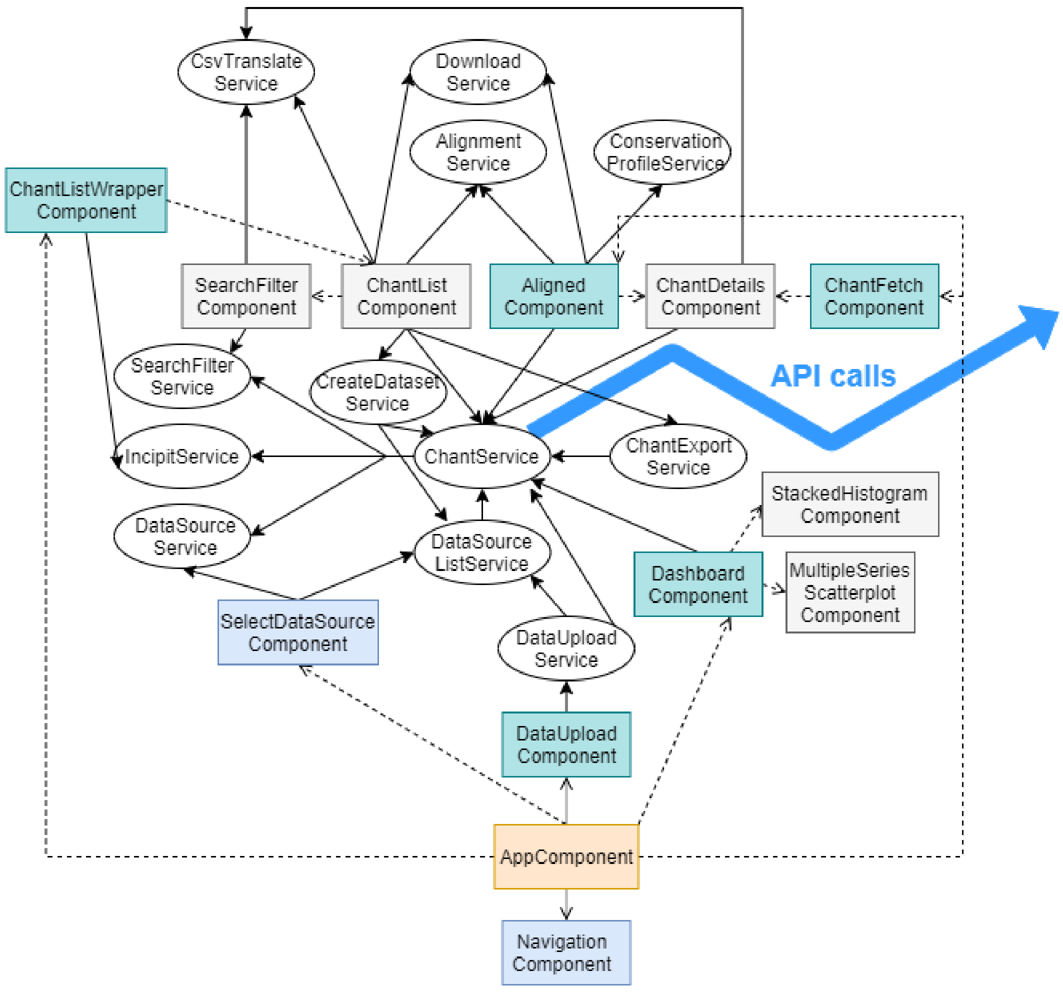


Figure 5.8: The architecture of the front end. Elements in rectangles are components, elements in ellipses are services. *AppComponent* is the component encapsulating the entire application. Blue components are always present on the page. Green components can be navigated to using their own URL. A dashed arrow from component A to component B implies that component A has component B in its HTML template. An arrow from a component or service A to service B means that element A uses service B.

end to calculate the corresponding alignment. `getDataSources` obtains all data sources currently present in the database. `exportChants` takes as an argument a list of chant IDs and the corresponding API call returns a CSV file with their database entries. `createDataset` creates a new data source from the chant IDs and name provided to it. All arguments to these functions are passed as a part of a *FormData*[9] object.

- **IncipitService.** The service stores the value of the incipit search query which is used when pulling data from the database. It provides two methods: `setIncipit` which changes the current value of the search query, and `incipit` which returns a *BehaviorSubject*[10] storing the value.

[9]`https://developer.mozilla.org/en-US/docs/Web/API/FormData`
[10]`https://www.learnrxjs.io/learn-rxjs/subjects/behaviorsubject`

- **SearchFilterService.** The service stores an object containing a list of allowed genres and a list of allowed offices which will be used for filtering when retrieving data from the database. It provides two methods, `setFilterSettings`, which changes the current value, and `getFilterSettings`, returning a *BehaviorSubject* with the value.

- **DataSourceService.** The service stores a list of indices of data sources we are currently using. The stored value persists throughout browser sessions. The service has two methods, `setSourceList`, which changes the value, and `getSourceList`, which returns a *BehaviorSubject* with the list.

- **DataSourceListService.** The service stores a list of the data sources in the database as of the time of the last call to the back end's API. The list is accessed by calling `getAllSources`. The method `refreshSources` retrieves the current list of data sources from back end.

- **CreateDatasetService.** The service contains one method, `createDataset`. It takes as an argument a list of chant IDs and a data source name and ensures that it is sent to back end to be inserted into the database. Additionally, it calls *DataSourceListService*'s `refreshSources` to obtain the most recent list of data sources.

- **DataUploadService.** The service contains one method, `uploadData`. It takes two arguments, a CSV file and a data source name. It passes these to *ChantService* to be inserted into the database and assures that the current data source list is correct by a call to *DataSourceListService*.

- **ChantExportService.** The service provides one method, `exportChants`. Its argument is a list of chant IDs to be exported. The method returns a CSV file with these chants.

- **CsvTranslateService.** The service provides means to obtain a genre's or an office's full description given its identifier as stored in the database. The descriptions are sourced from CSV files provided in CantusCorpus. They can be accessed via the methods `getGenre` and `getOffice`, both taking the identifier of the genre or office as an argument. The service also contains the method `getAllValues`, which takes as an argument either the string *genres* or *offices*, and returns an object containing all values of the given type.

- **DownloadService.** The service contains a single method, `download`. It takes two arguments: `blob`, which is the content of a file to be downloaded, and `filename`, the name of the file. Calling the method triggers the download of the file. The service is used in multiple situations. It ensures the download of CSV files with exported chants, as well as the download of text files with the results of the alignment.

- **AlignmentService.** The service stores the IDs of chants we want aligned and the algorithm using which they should be aligned. Both of these values persist throughout browser sessions. The IDs can be changed or obtained by calling the setter and getter on `idsToAlign`. The algorithm can be set via the method `setMode`, which returns 0 if the provided algorithm is correct and 1 otherwise; and retrieved with the method `getMode`. The allowed algorithm values are *full*, *intervals*, and *syllables.*

- **ConservationProfileService.** The service contains only one method called `calculateConservationProfile`. Given a list of aligned melodies, as computed by the back end, it calculates the conservation value for each position in each melody. It returns it in a form easy to work with in HTML templates.

5.3.2 Components

- **AppComponent.** This component is the one always present on the page, encapsulating other components. It defines the global styles of the entire page. The component displays *SelectDataSourceComponent* and *NavigationComponent*, which means they are always visible on the page. It further displays components depending on the current URL, as indicated by the `router-outlet` tag.

- **NavigationComponent.** The component provides easy navigation to the app's main pages. It also enables the user to enter a query for searching among the chants' incipits via the field in the top right corner. The *home* button in the top left corner leads to the landing page.

- **SelectDataSourceComponent.** The component exposes the interface to change the current selection of data sources. It contains a list of data sources names, each next to a checkbox. The *Save* button saves the current selection of data sources.

- **ChantLlistWrapperComponent.** The component encapsulates *ChantListComponent.* It reads the incipit search query from the current URL and passes it to *IncipitService.*

- **ChantListComponent.** The component displays a list of chants from the current search results. The table contains a chant's incipit, source, genre, office, and its data source. The checkboxes next to the incipits allow for the chants' selection. The component also provides the possibility to filter search results, to export a selection of chants, to align a selection, and to create a new data source.

- **SearchFilterComponent.** The component enables the user to select which genres and offices should be included in search results. It consists of a set of checkboxes that determine whether a specific genre or office is allowed or not. The settings are saved using the *Save* button.

- **AlignedComponent.** The component displays results of alignment. It shows the aligned chants ordered by similarity in rows under each other. It provides the means to hide and unhide text and headers, completely remove or collapse an alignment, rearrange the order, as well as highlight notes and conservation profile. It also provides the possibility to export the results to a file.

- **ChantFetchComponent.** The component encapsulates *ChantDetailsComponent*. It reads chant ID from URL and passes it to *ChantDetailsComponent*.
- **ChantDetailsComponent.** The component displays the relevant information about a selected chant. It displays a melody with its text whose stressed syllables are highlighted if possible.
- **DashboardComponent.** The component displays several visualization of data from the current search selection. It preprocesses the data sent to each of the visualizations.
- **StackedHistogramComponent.** The component contains a histogram of data passed to it. We use the library *d3js*[11] for the plot creation.
- **MultipleSeriesScatterplotComponent.** The component shows a scatter plot of data passed to it. Again, we use the library *d3js*.
- **DataUploadComponent.** The component displays the interface for uploading a file to the database.

5.4 Dependencies

The software depends on several other programs for its correct functionality. For the back end, it is necessary to have Python installed. During development, version 3.9.2 was used; it is not guaranteed that the application will work for lower versions. Additionally, the packages Django (version 3.1.7), pandas (version 1.2.3) chant21 (version 0.4.6) and cltk (version 1.0.5) are required. It is also necessary to have the MAFFT software installed (version 7.470 or higher).

The front end is run on Angular version 11. It uses the library d3 (version 7.6.0) for visualizations.

[11] `https://d3js.org/`

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A. List of genres and their abbreviations

Identifier	Name	Description	Mass or Office
genre_?	[?]	"Unknown, ambiguous, unidentifiable, illegible"	Mass and Office
genre_a	A	Antiphon	Office
genre_ag	Ag	Agnus dei	Mass
genre_al	Al	Alleluia	Mass
genre_alv	AlV	Alleluia verse	Mass
genre_av	AV	Antiphon verse	Office
genre_bd	BD	Benedicamus domino	Mass and Office
genre_ca	Ca	Canticle	Mass and Office
genre_cap	Cap	Capitulum	Office
genre_cav	CaV	Canticle verse	Mass and Office
genre_cm	Cm	Communion	Mass
genre_cmr	CmR	Versus ad repetendum for the communion	Mass
genre_cmv	CmV	Communion verse	Mass
genre_cr	Cr	Credo	Mass
genre_d	D	Dramatic element (used for items of liturgical drama that are not otherwise rubricked)	Mass and Office
genre_g	[G]	Mass chant (a generic code used in the earliest Cantus indices)	Mass
genre_gl	Gl	Gloria	Mass
genre_gpep	Gp/Ep	Gospel/Epistle	Mass
genre_gr	Gr	Gradual	Mass
genre_grv	GrV	Gradual verse	Mass
genre_gv	[GV]	Verse for a Mass chant (a generic code used in the earliest Cantus indices)	Mass
genre_h	H	Hymn	Office
genre_hv	HV	Hymn verse	Office
genre_i	I	Invitatory antiphon	Office
genre_ig	Ig	Ingressa (for the Beneventan liturgy)	Office
genre_im	Im	Improperia	Mass
genre_in	In	Introit	Mass
genre_inr	InR	Versus ad repetendum for the introit	Mass
genre_inv	InV	Introit verse	Mass
genre_ip	IP	Invitatory psalm (when fully written out and notated)	Office
genre_ite	Ite	Ite missa est	Mass
genre_ky	Ky	Kyrie	Mass

genre_l	L	Lesson (when fully written out and notated)	Mass
genre_li	Li	Litany	Office
genre_liv	LiV	Litany verse	Mass and Office
genre_m	[M]	"""Miscellaneous"" (a descriptor used in the earliest versions of Cantus for the Te Deum, Versus in Triduo, prosulae - to be replaced by Va=Varia)"	Mass and Office
genre_mo	[MO]	Mass Ordinary (a generic code used in the earliest Cantus indices)	Mass
genre_of	Of	Offertory	Mass
genre_ofv	OfV	Offertory verse	Mass
genre_pn	Pn	Pater noster	Mass and Office
genre_pr	Pr	Prefatio (when written out and notated)	Mass
genre_prcs	PRCS	Preces (Old Hispanic)	Mass and Office
genre_prcs_1	PRCS		
genre_prcsv	PRCSV	Verse for the Preces (Old Hispanic)	Mass and Office
genre_prcsv_1	PRCSV		
genre_ps	PS	Psalm	Office
genre_r	R	Responsory	Office
genre_sa	Sa	Sanctus	Mass
genre_sq	Sq	Sequence	Mass
genre_sqv	SqV	Sequence verse	Mass
genre_tc	Tc	Tract	Mass
genre_tcv	TcV	Tract verse	Mass
genre_tp	Tp	Tropus	Mass
genre_v	V	Responsory verse	Office
genre_va	Va	Varia	Mass and Office
genre_vahw	VaHW	Varia within Holy Week	Mass and Office
genre_w	W	Versicle	Office

B. List of offices and their abbreviations

Identifier	Name	Description
office_?	?	uncertain
office_c	C	Compline
office_ca	CA	Chapter
office_d	D	Day Hours
office_e	E	Antiphons for the Magnificat or Benedictus (""in evangelio"")
office_h	H	Antiphons based on texts from the Historia
office_l	L	Lauds
office_m	M	Matins
office_mi	MI	Mass
office_n	N	None
office_p	P	Prime
office_r	R	Memorial
office_s	S	Sext
office_t	T	Terce
office_v	V	First Vespers
office_v2	V2	Second Vespers
office_x	X	Supplemental, paraliturgical, rarely-used, or chants that do not fit into the usual categories or that are unclear in their usage