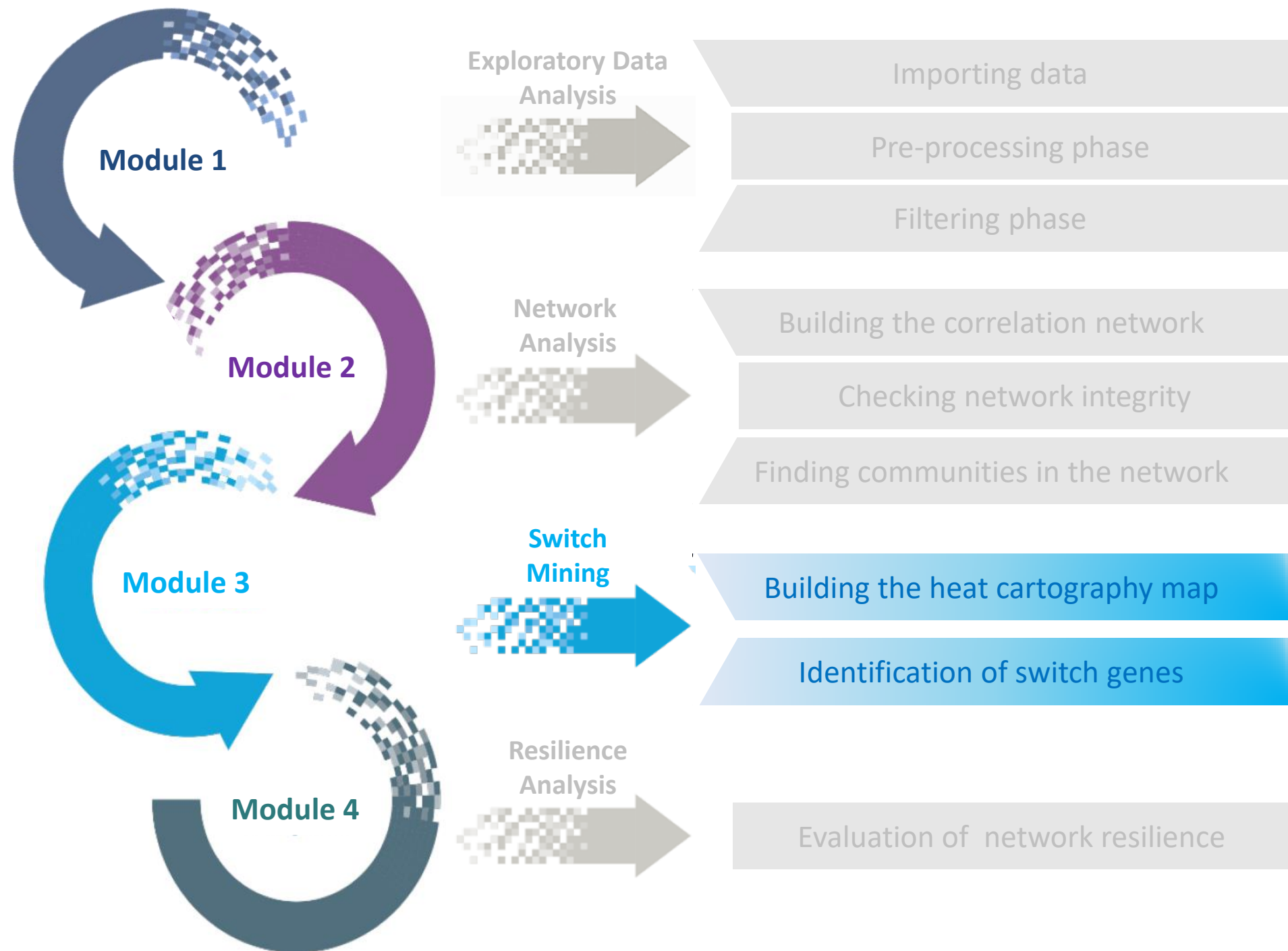
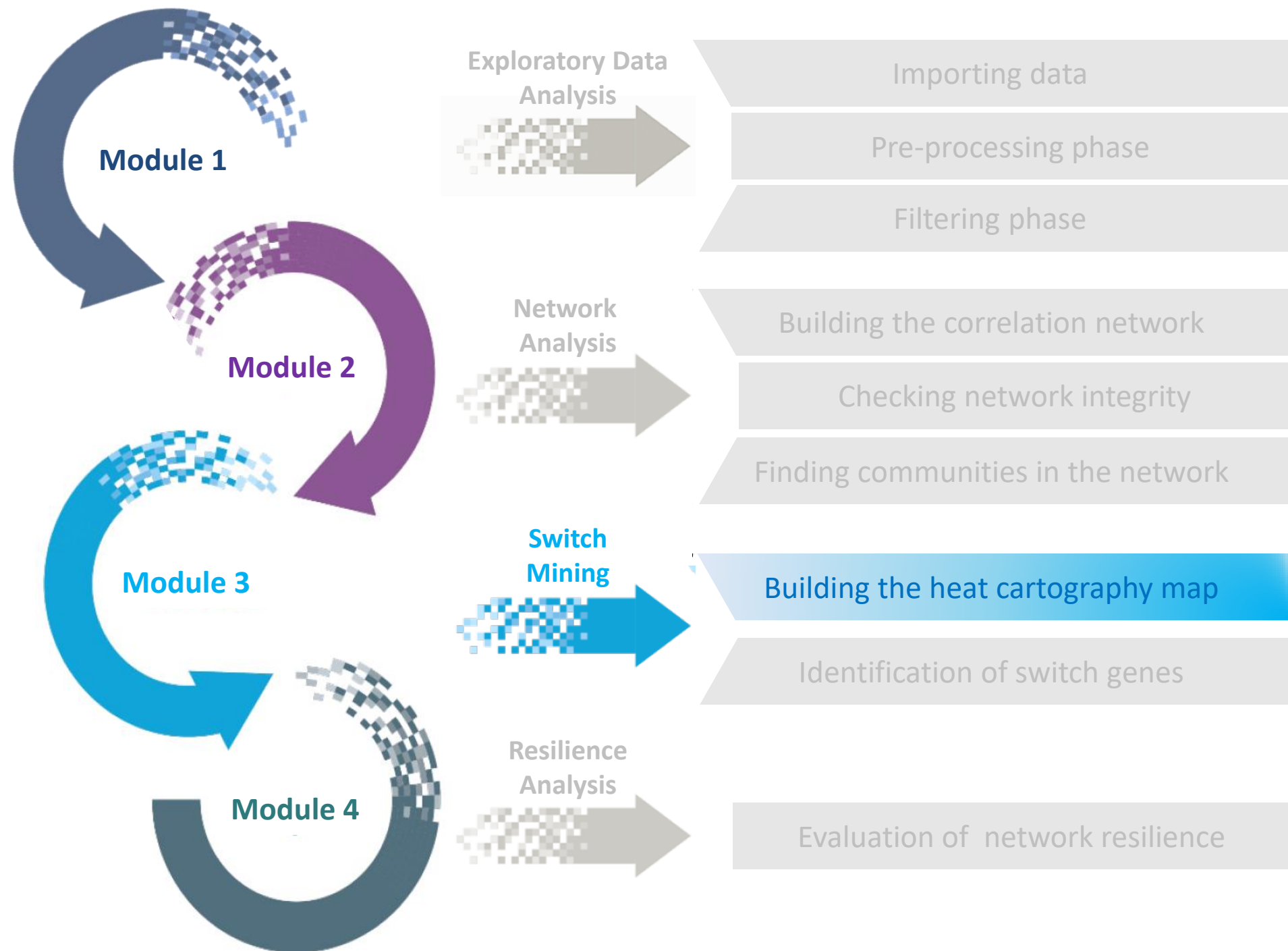




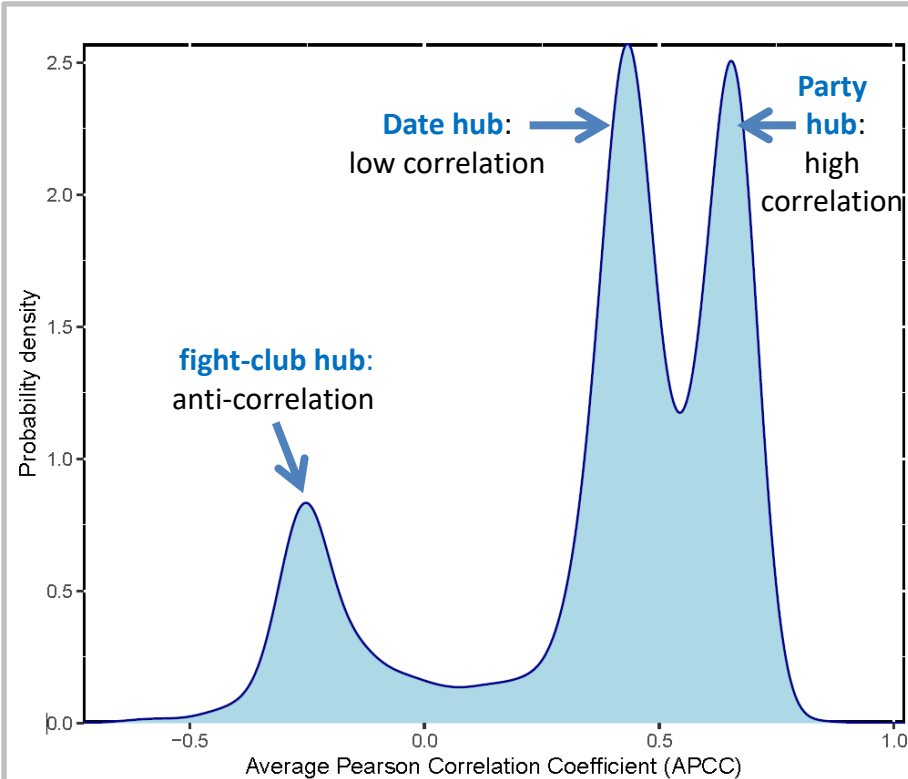
Module 3: Switch Mining







APCC distribution

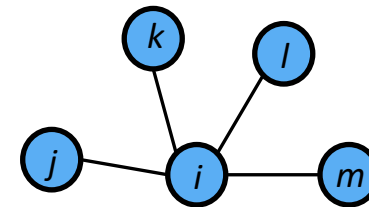


- x-axis refers to APCC values computed between the expression profiles of each hub of correlation network and its nearest neighbors
- y-axis refers to the probability density

Average Pearson Correlation Coefficient (APCC)

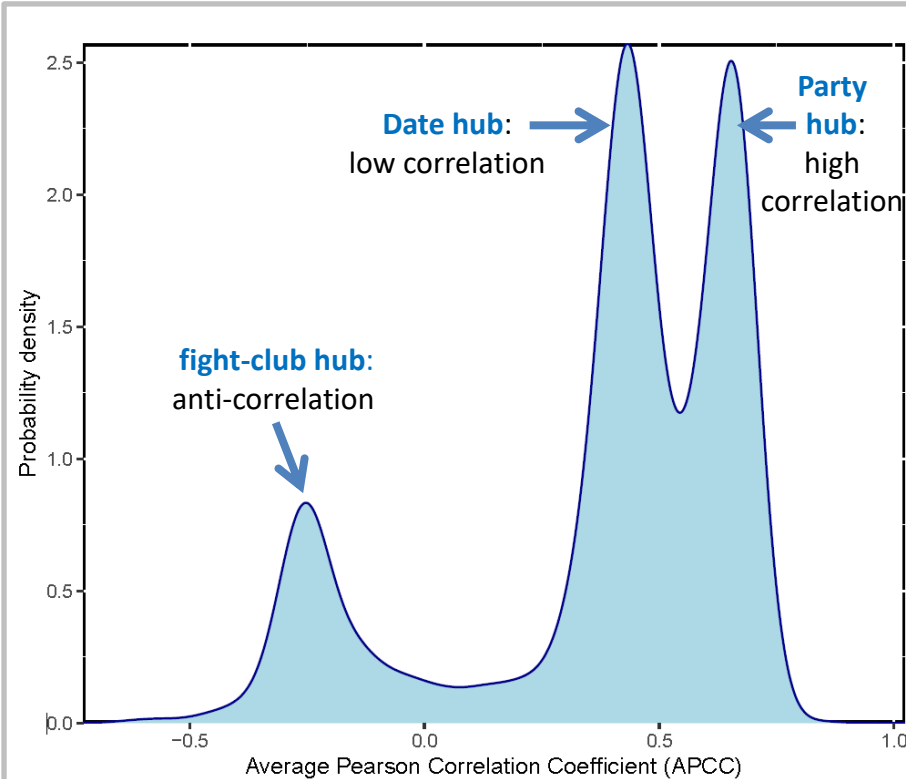
- An APCC value is assigned to each node of correlation network
- APCC measures how the nodes are co-expressed with their nearest neighbors

Example:



$$APCC_i = \frac{\rho(i,j) + \rho(i,k) + \rho(i,l) + \rho(i,m)}{4}$$

APCC distribution

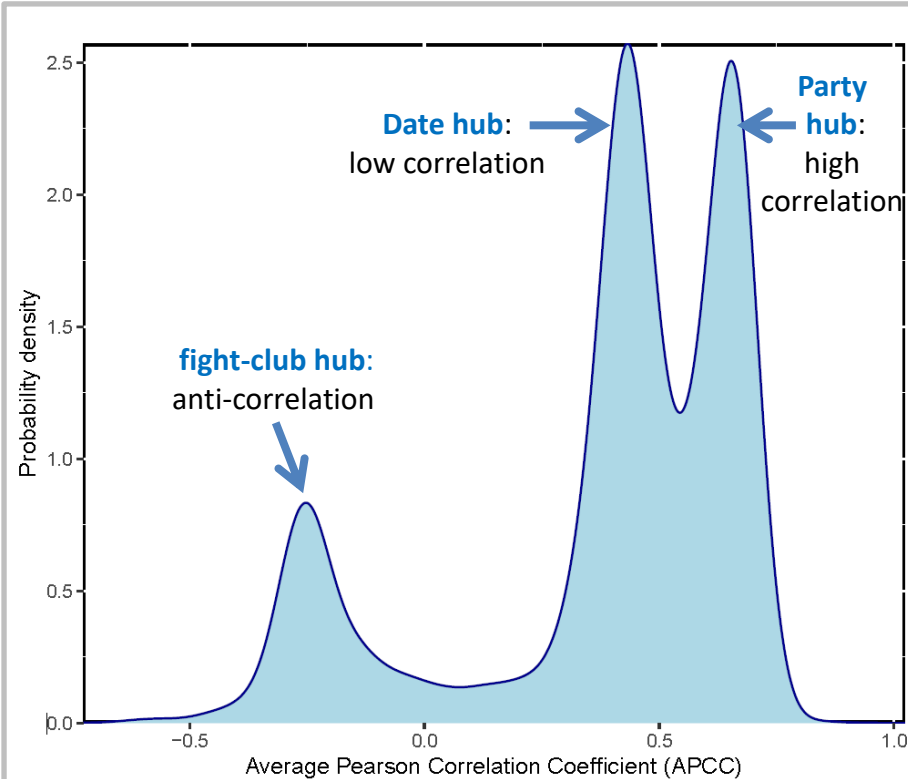


- x-axis refers to APCC values computed between the expression profiles of each hub of correlation network and its nearest neighbors
- y-axis refers to the probability density

Average Pearson Correlation Coefficient (APCC)

```
computeAPCC <- function(w_adj){  
  w_adj[w_adj==0] <- NA  
  APCC <- data.frame(APCC = rowMeans(w_adj, na.rm = T))  
  return(APCC)  
}
```

APCC distribution

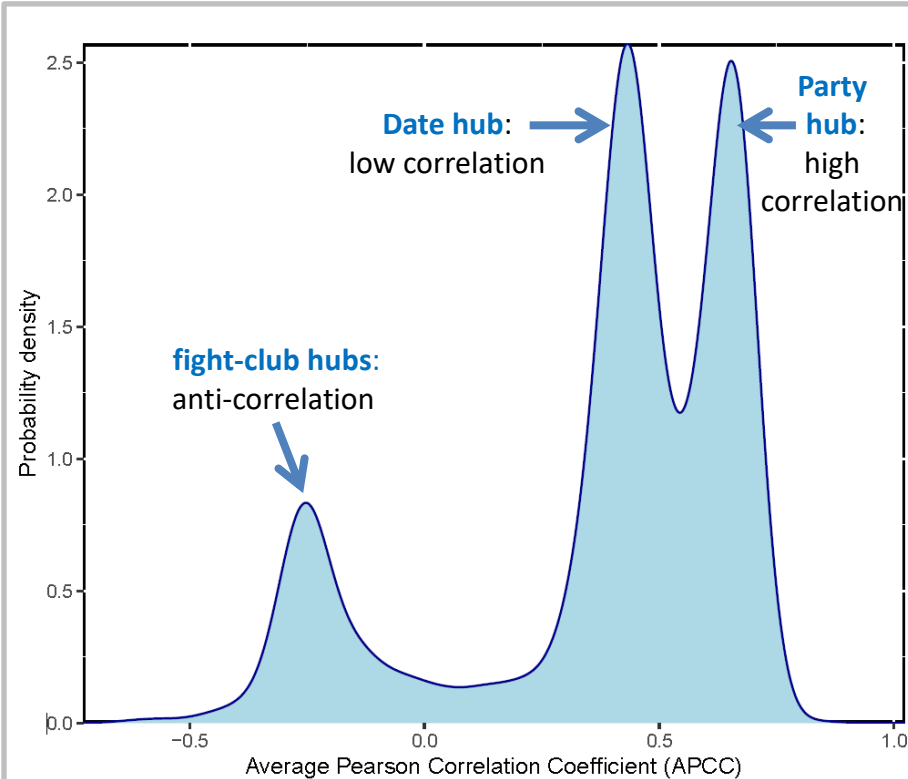


- x-axis refers to APCC values computed between the expression profiles of each hub of correlation network and its nearest neighbors
- y-axis refers to the probability density

APCC distribution

- The curve represents the estimated probability density using a smoothing algorithm with a Gaussian kernel of the APCC values' distribution
- It appears to be trimodal and the three peaks correspond to three different kind of hubs:
 1. **party hubs** which are highly correlated in expression with their interaction partners;
 2. **date hubs** which show moderate correlation in expression with their interaction partners;
 3. **fight-club hubs** which show an average negative correlation in expression with their interaction partners.

APCC distribution



- x-axis refers to APCC values computed between the expression profiles of each hub of correlation network and its nearest neighbors
- y-axis refers to the probability density

APCC distribution

```
getHubClassification <- function(APCC,deg){
  condition1 <- (APCC$APCC > 0) & (APCC$APCC < 0.5) & (deg$deg >= 5)
  condition2 <- (APCC$APCC >= 0.5) & (deg$deg >= 5)
  condition3 <- (APCC$APCC < 0) & (deg$deg >= 5)
  condition4 <- (deg$deg < 5)

  hub_class <- data.frame(hub = ifelse(condition1,"DATE",
                                     ifelse(condition2,"PARTY",
                                     ifelse(condition3,"FIGHT CLUB",
                                     ifelse(condition4,"no hub","not
available")))))
  rownames(hub_class) <- rownames(deg)

  return(hub_class)
}
```

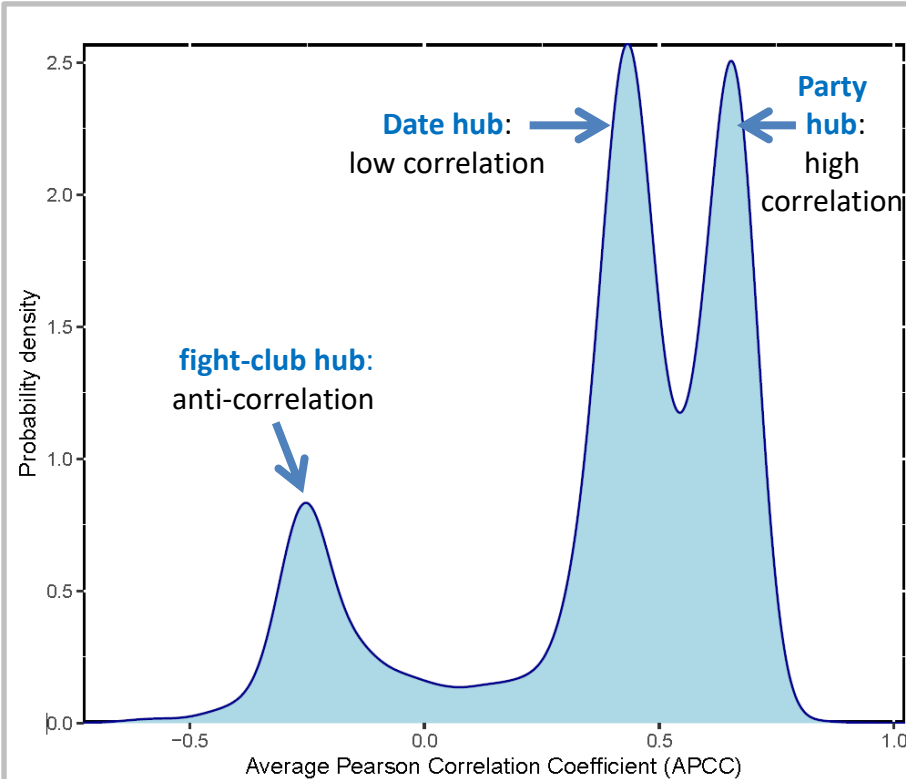


Caveat: hub is defined as a node with a degree greater than 5 [Han et al., Nature 2004]



Caveat: In order to optimally separate date and party hubs, a date/party threshold is arbitrarily set to 0.5 for the APCC [Han et al., Nature 2004].

APCC distribution



- x-axis refers to APCC values computed between the expression profiles of each hub of correlation network and its nearest neighbors
- y-axis refers to the probability density

APCC distribution

```
getAPCCdistribution <- function(attribute,output_file){
  m <- min(attribute$APCC) - 0.1
  M <- max(attribute$APCC) + 0.1

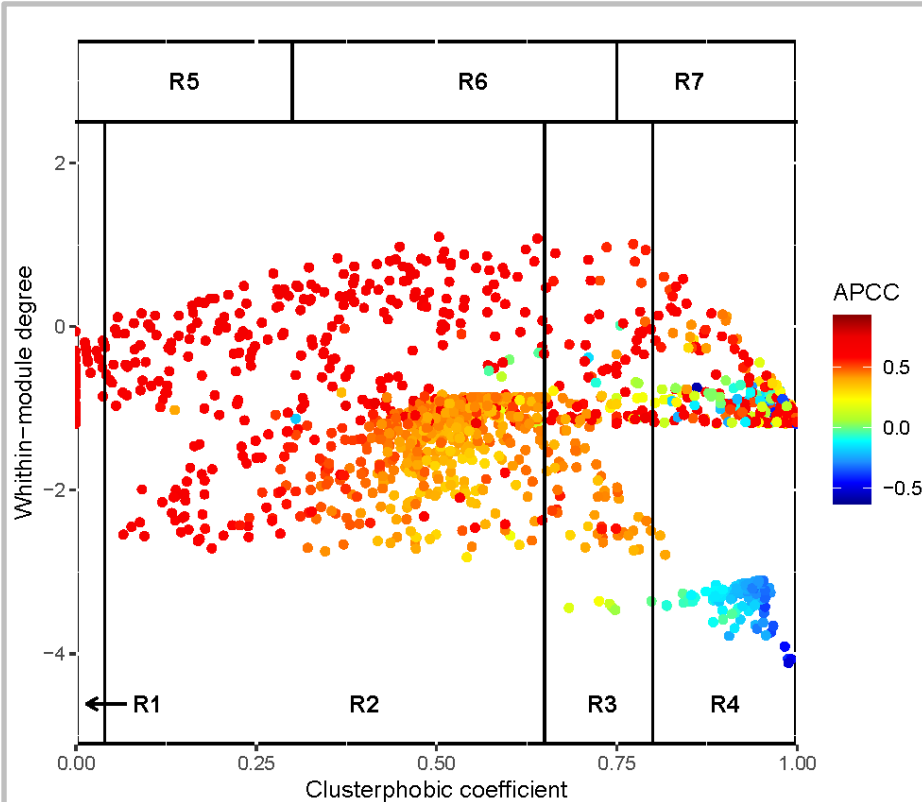
  ind <- which(attribute$Hub_classification == "no hub")
  if(length(ind) > 0) attribute <- attribute[-ind,]

  p <- ggplot(attribute, aes(x=APCC)) + geom_density(color="darkblue",
    fill="lightblue") +
    scale_x_continuous(expand = c(0, 0), limits = c(m,M)) + scale_y_co
    ntinuous(expand = c(0, 0)) +
    theme(panel.background = element_rect(fill = "white", colour =
    "black", size = 1)) +
    labs(x = "Average Pearson Correlation Coefficient (APCC)", y =
    "Probability density")

  print(p)
  savePDF(p,output_file)
}
```

Computes and draws
kernel density estimate

Heat cartography map

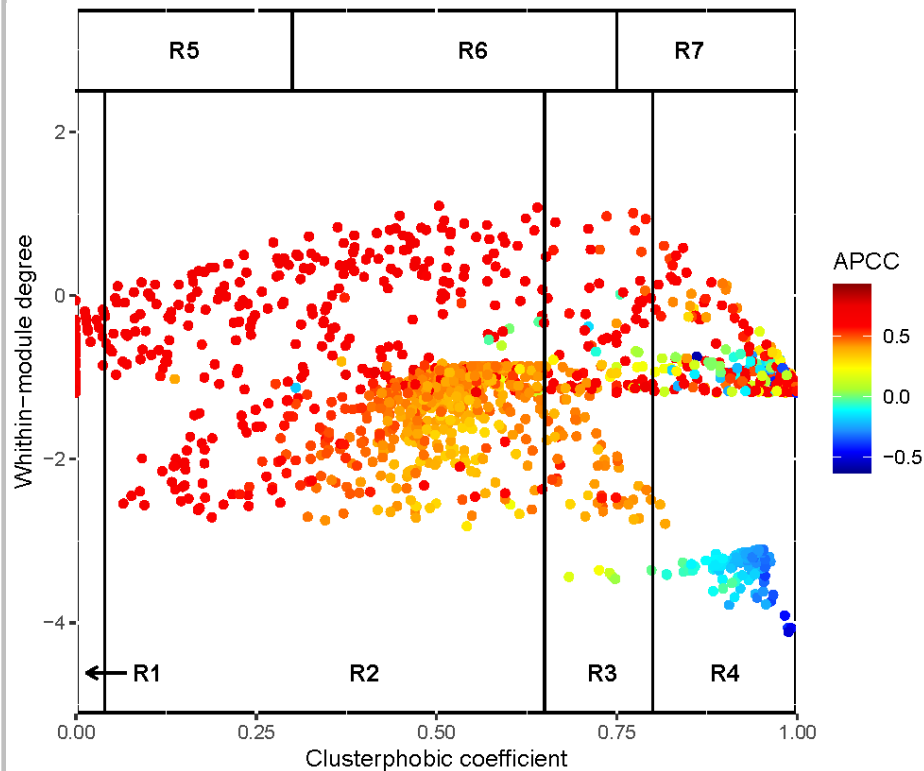


- x-axis refers to K_π (clusterphobic coefficient)
- y-axis refers to z_g (within-module degree)
- Color scale refers to APCC

Heat cartography map

- The cartography is defined by two parameters: z_g (**within-module degree**) and K_π (**clusterphobic coefficient**) that divided the plane into seven regions, each defining a specific node role (R1-R7)
- The **heat cartography map** is computed by coloring each node of the correlation network according to its **APCC value**

Heat cartography map



- x-axis refers to K_π (clusterphobic coefficient)
- y-axis refers to z_g (within-module degree)
- Color scale refers to APCC

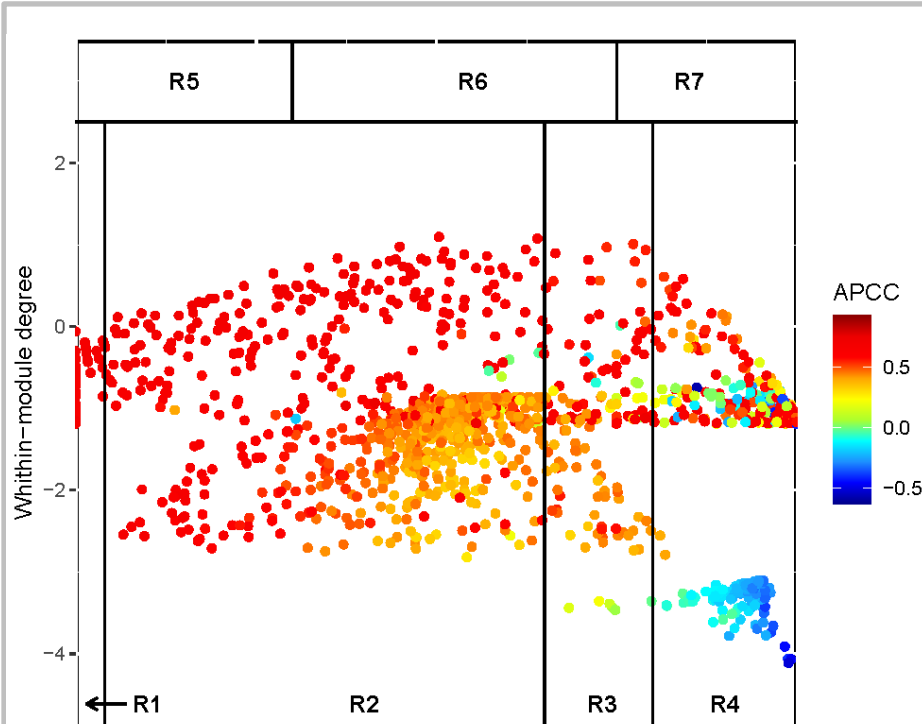
Clusterphobic coefficient (K_π)

- K_π measures the “fear” of being confined in a cluster
- It evaluates the ratio of internal to external connections of a node and thus represents a measure of **global connectivity**
- A high value of K_π denotes nodes having much more external than internal links

$$K_\pi = 1 - \left(\frac{k_i^{in}}{k_i} \right)^2$$

- k_i^{in} is the number of links of node i to nodes in its module C_i
- k_i is the total degree of node i (i.e., the number of links connected to it)

Heat cartography map



Clusterphobic coefficient (K_π)

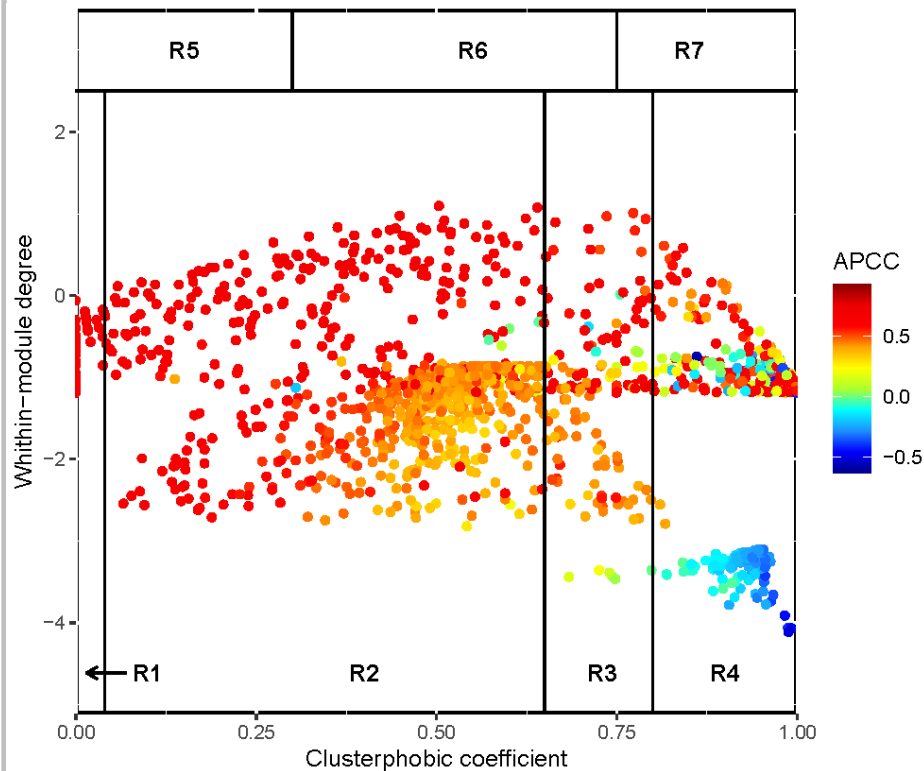
- K_π measures the “fear” of being confined in a cluster
- It evaluates the ratio of internal to external connections of a node and thus represents a measure of **global connectivity**
- A high value of K_π denotes nodes having much more external than internal links

$$K_\pi = 1 - \left(\frac{k_i^{in}}{k_i} \right)^2$$



Note that $K_\pi = 0$ when a node has only links within its module, i.e., it does not communicate with the other modules ($k_i^{in} = k_i$). On the contrary, K_π is close to 1 when the majority of its links are external to its own module.

Heat cartography map



- x-axis refers to K_π (clusterphobic coefficient)
- y-axis refers to z_g (within-module degree)
- Color scale refers to APCC

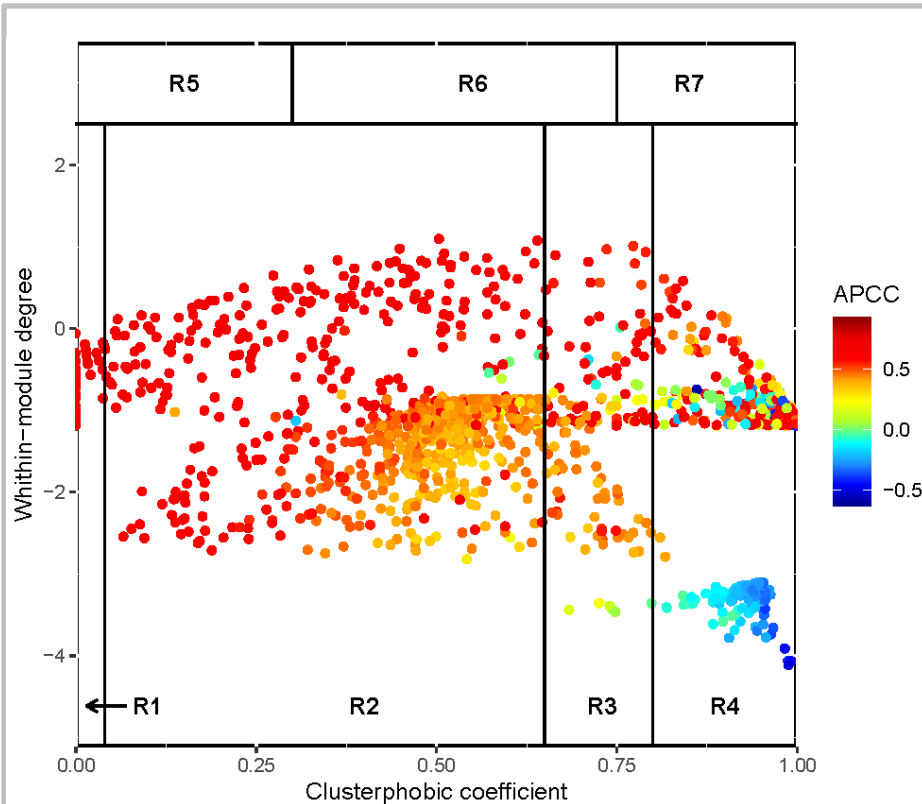
Within-module degree (z_g)

- z_g measures how much a node is a hub in its community and thus represents a measure of **local connectivity**

$$z_g^i = \frac{k_i^{in} - \bar{k}_{C_i}}{\sigma_{C_i}}$$

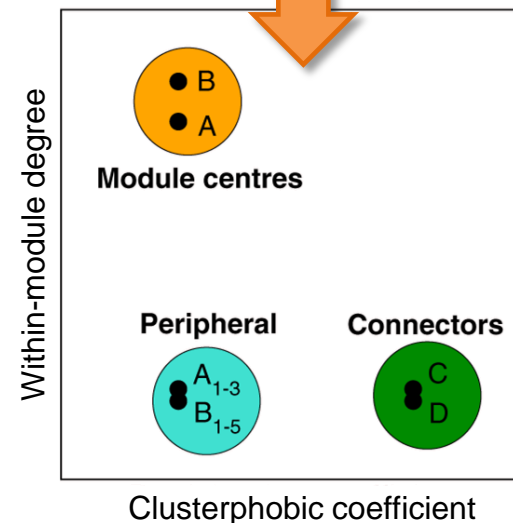
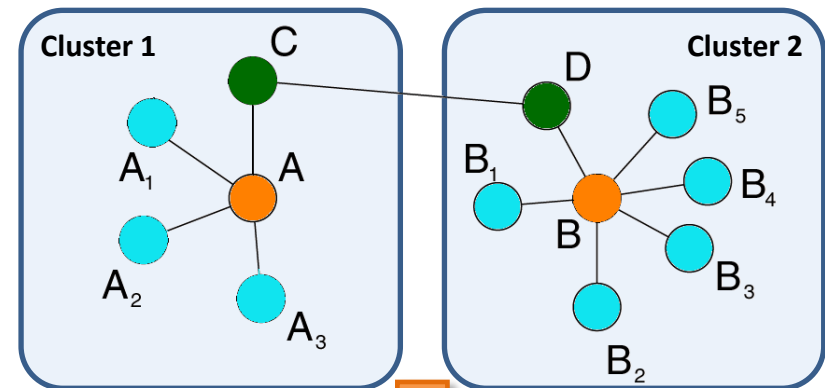
- k_i^{in} is the number of links of node i to nodes in its module C_i
- \bar{k}_{C_i} and σ_{C_i} are the average and standard deviation of the total degree distribution of the nodes in the module C_i

Heat cartography map

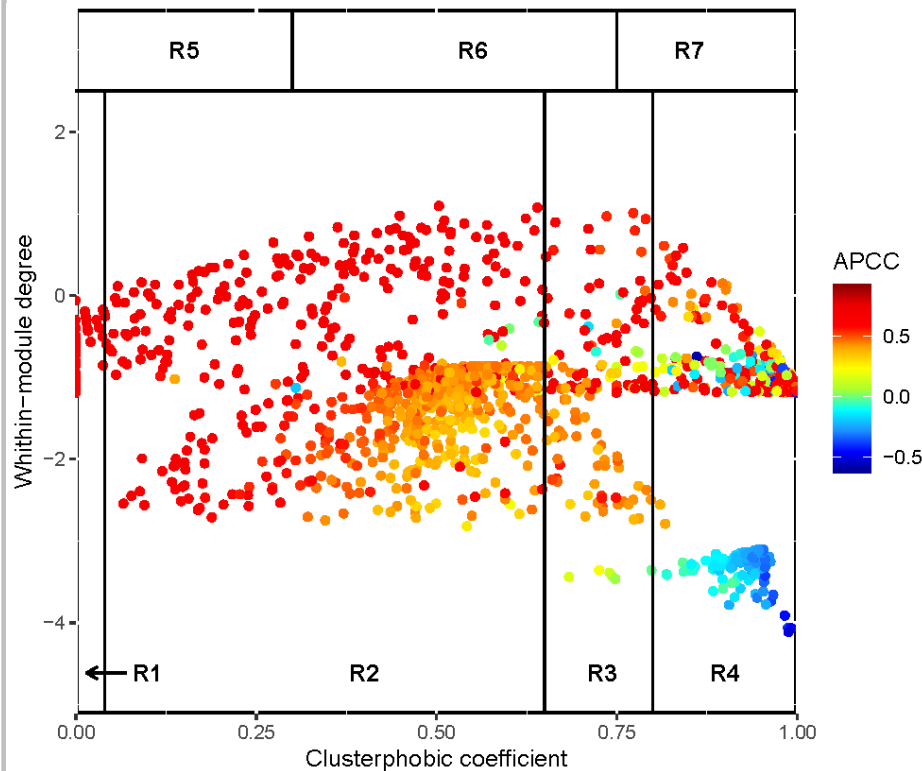


- x-axis refers to K_π (clusterphobic coefficient)
- y-axis refers to z_g (within-module degree)
- Color scale refers to APCC

Roles of nodes in the correlation network



Heat cartography map



- x-axis refers to K_π (clusterphobic coefficient)
- y-axis refers to z_g (within-module degree)
- Color scale refers to APCC

Roles of nodes in the correlation network

z_g and K_π divide the plane into R1-R7 regions, each defining a specific node role:

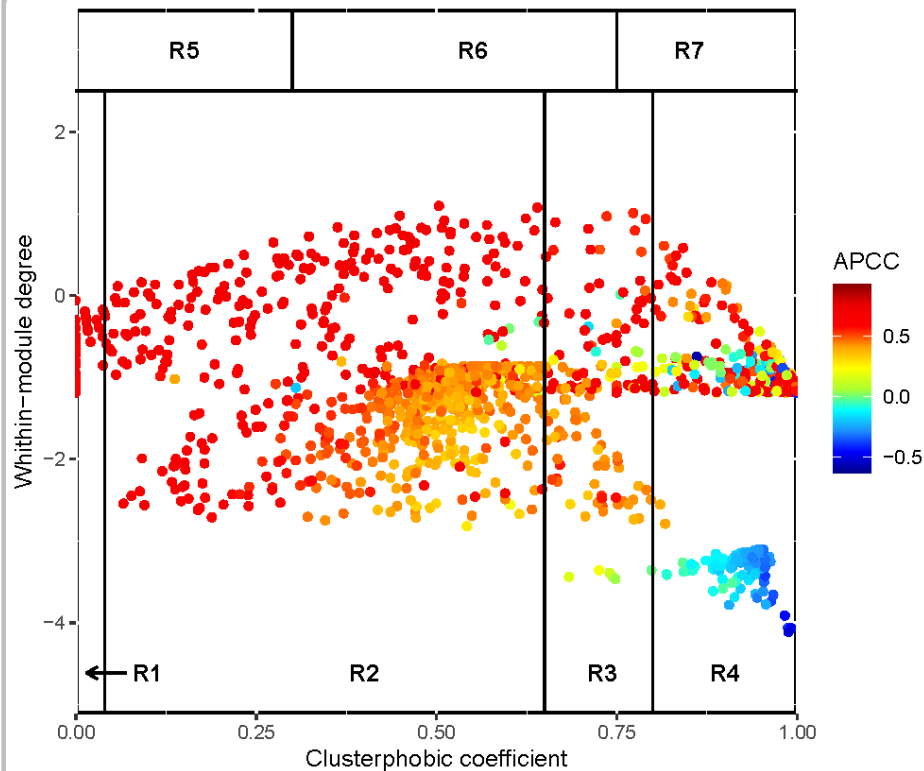
non local hub for $z_g < 2.5$

- | | |
|-------------------------|----------------------------------|
| $K_\pi = 0$ | Ultra-peripheral nodes (role R1) |
| $K_\pi \leq 0.625$ | Peripheral nodes (role R2) |
| $0.62 < K_\pi \leq 0.8$ | Non-hub connectors (role R3) |
| $K_\pi > 0.8$ | Non-hub kinless nodes (role R4) |

local hub for $z_g \geq 2.5$

- | | |
|-------------------|---------------------------|
| $K_\pi = 0.3$ | Provincial hubs (role R5) |
| $K_\pi \leq 0.75$ | Connector hubs (role R6) |
| $K_\pi > 0.75$ | Kinless hubs (role R7) |

Heat cartography map



- x-axis refers to K_π (clusterphobic coefficient)
- y-axis refers to z_g (within-module degree)
- Color scale refers to APCC

Heat cartography map

```
buildCartography <- function(df_stat,idx,res_deg,APCC,hub_class,network,output_file_attribute,
                             output_file_CartographyNetwork,output_file_CartographyNetwork_
R){
  deg <- res_deg$deg
  ideg <- res_deg$ideg

  cluster <- split(idx,idx$cluster)

  cluster_info <- lapply(names(cluster),function(k){
    y <- rownames(cluster[[k]])

    parameter <- computePz(y,deg,ideg)
    P <- parameter$P
    z <- parameter$z

    role <- getNodeRole(y,z,P)

    df <- data.frame(y,role$hub,role$region,role$type,deg[y,],ideg[y,],APCC[y,],hub_class[y
    ],P,z,k)
    colnames(df) <- c("node", "Hub", "Region", "Type", "Total_Degree", "Internal_Degree",
                     "APCC", "Hub_classification", "P", "z", "cluster_ID")

    return(df)
  })

  attribute <- data.frame(rbindlist(cluster_info))

  ind <- which( (attribute$`Total Degree` == 0) | (attribute$`Internal Degree` == 0)
)

  if(length(ind)>0){
    node_to_remove <- attribute$node[ind]

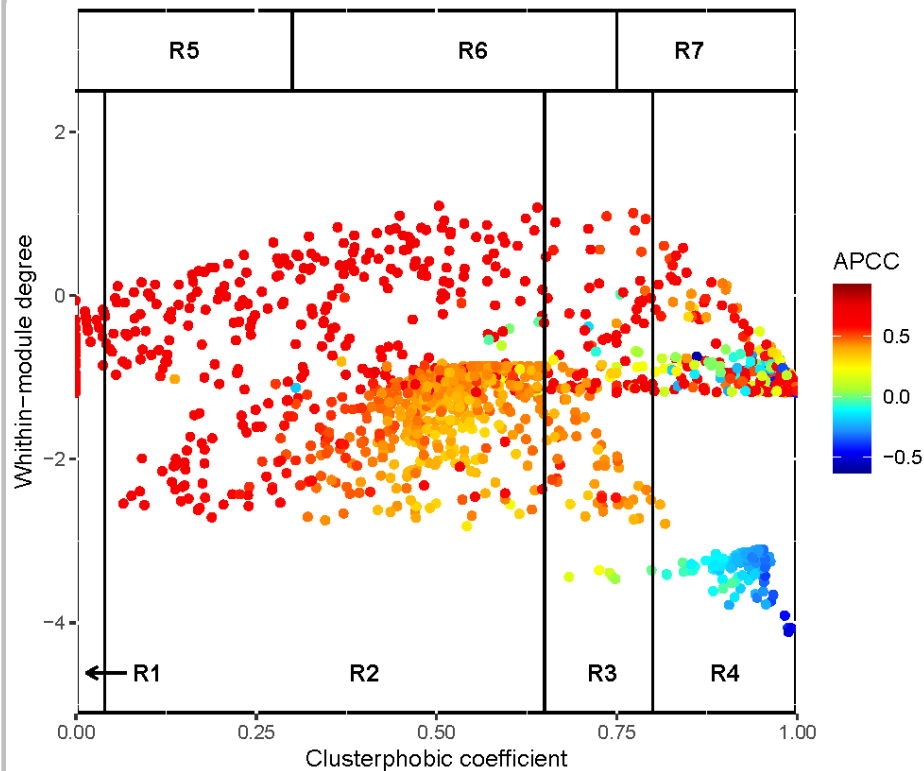
    found <- which( (network$source %in% node_to_remove) | (network$target %in%
node_to_remove) )
    network <- network[-found,]

    attribute <- attribute[-ind,]
  }
}
```

...

[Scroll down](#)

Heat cartography map



- x-axis refers to K_{π} (clusterphobic coefficient)
- y-axis refers to z_g (within-module degree)
- Color scale refers to APCC

Heat cartography map

```
buildCartography <- function(df_stat, idx, res_deg, APCC, hub_class, network, output_file_attribute,
                             output_file_CartographyNetwork, output_file_CartographyNetwork_R){
  deg <- res_deg$deg
  ideg <- res_deg$ideg

  cluster <- split(idx, idx$cluster)

  cluster_info <- lapply(names(cluster), function(k){
    y <- rownames(cluster[[k]])

    parameter <- computePz(y, deg, ideg)
    P <- parameter$P
    z <- parameter$z

    role <- getNodeRole(y, z, P)

    df <- data.frame(y, role$hub, role$ass)
    colnames(df) <- c("node", "hub", "ass", "APCC")

    return(df)
  })

  attribute <- merge(attribute, df_stat, by.x = "node", by.y = 0, all = F)

  write.table(attribute, output_file_attribute, row.names = F, col.names = T, sep =
    "\t", quote = F)
  write.table(network, output_file_CartographyNetwork, row.names = F, col.names = T,
    sep = "\t", quote = F)

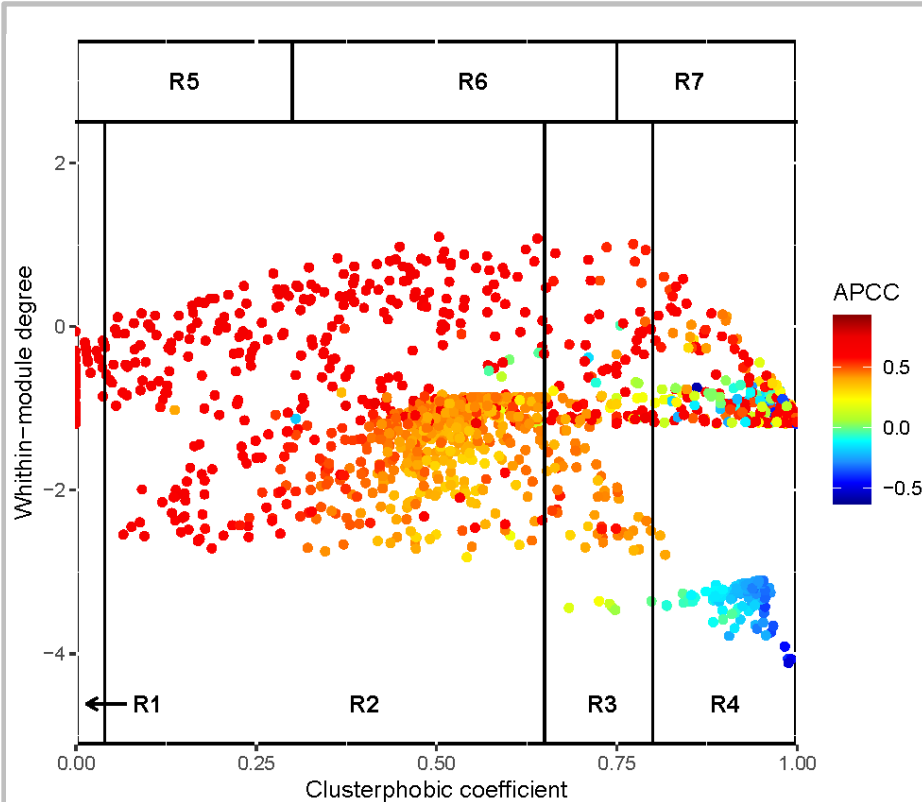
  save(network, file = output_file_CartographyNetwork_R)

  res <- list(attribute = attribute, num_node = nrow(attribute), num_edge = nrow(
    network))

  return(res)
}
```

Add statistical information
from df_stat

Heat cartography map



- x-axis refers to K_{π} (clusterphobic coefficient)
- y-axis refers to z_g (within-module degree)
- Color scale refers to APCC

Heat cartography map

```
getHeatCartography <- function(attribute,output_file){

  df <- attribute[,c("P","z","APCC")]

  m <- min(df$z) - 1
  M <- 3.5
  d <- 0.5

  my_color <- colorRampPalette(colors = c("blue4","blue","dodgerblue1","deepskyblue","cyan",
    "greenyellow","yellow","orange","red","red2","red4"))(100)

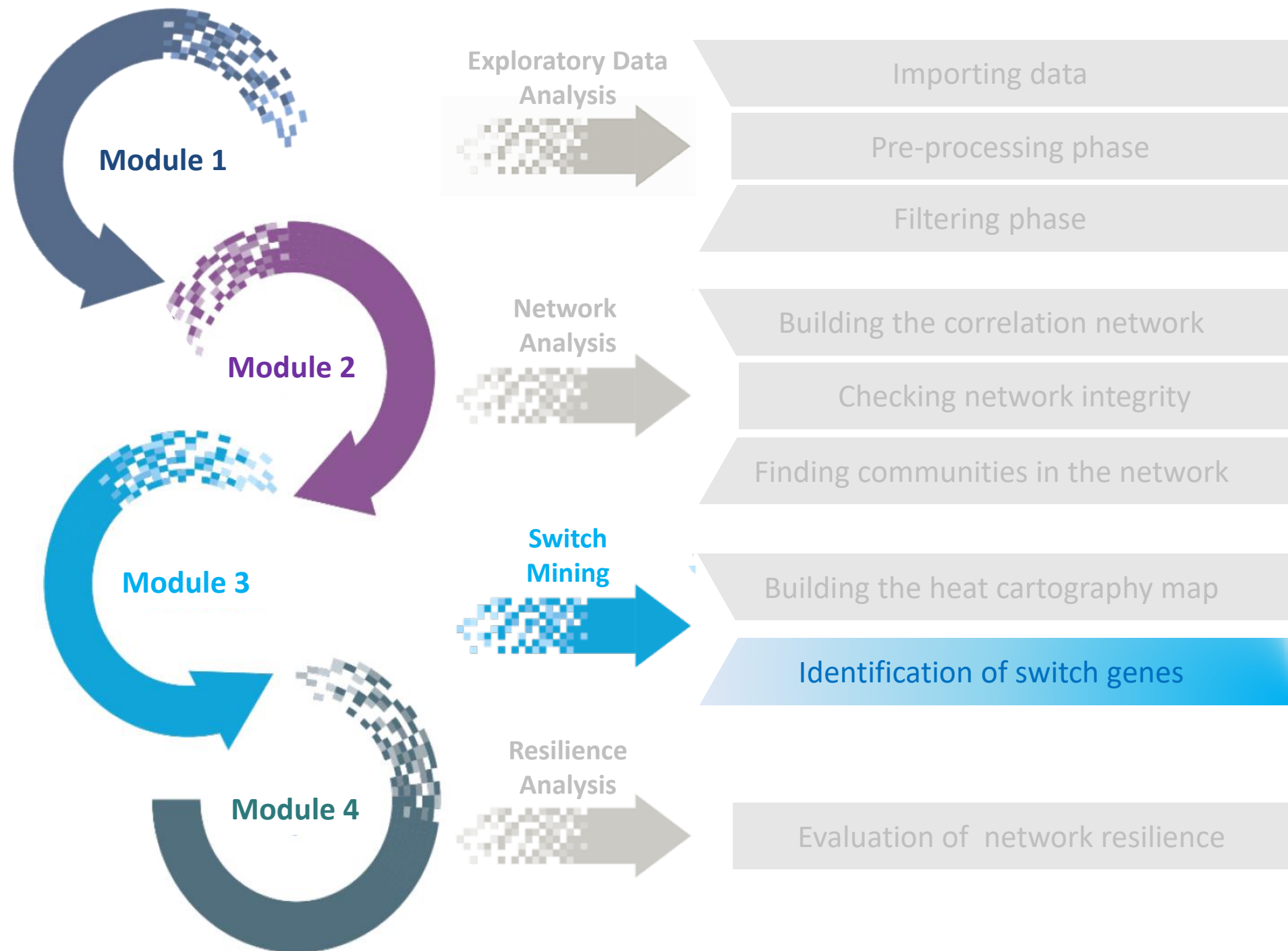
  p <- ggplot(df, aes(x = P, y = z, color = APCC)) + geom_point() +
    scale_x_continuous(expand = c(0, 0)) + scale_y_continuous(expand = c(0, 0)) +
    theme(panel.background = element_rect(fill = "white", colour = "black", size = 1)) +
    labs(x = "Clusterphobic coefficient", y = "Within-module degree") +
    geom_line(data = data.frame(x = c(0, 1), y = 2.5), aes(x = x, y = y),
      linetype = "solid", color = "black") +
    geom_line(data = data.frame(x = 0.04, y = c(m, 2.5)), aes(x = x, y = y),
      linetype = "solid", color = "black") +
    geom_line(data = data.frame(x = 0.65, y = c(m, 2.5)), aes(x = x, y = y),
      linetype = "solid", color = "black") +
    geom_line(data = data.frame(x = 0.8, y = c(m, 2.5)), aes(x = x, y = y),
      linetype = "solid", color = "black") +
    geom_line(data = data.frame(x = 0.3, y = c(2.5, M)), aes(x = x, y = y),
      linetype = "solid", color = "black") +
    geom_line(data = data.frame(x = 0.75, y = c(2.5, M)), aes(x = x, y = y),
      linetype = "solid", color = "black") +
    annotate(geom="text", x = 0.1, y = m+d, label = "R1",
      color = "black", fontface = "bold") +
    annotate(geom="text", x = 0.4, y = m+d, label = "R2",
      color = "black", fontface = "bold") +
    annotate(geom="text", x = 0.73, y = m+d, label = "R3",
      color = "black", fontface = "bold") +
    annotate(geom="text", x = 0.9, y = m+d, label = "R4",
      color = "black", fontface = "bold") +
    annotate(geom="text", x = 0.15, y = M-d, label = "R5",
      color = "black", fontface = "bold") +

    geom_segment(aes(x = 0.07, y = m+d, xend = 0.015, yend = m+d),
      arrow = arrow(length = unit(0.2, "cm")), colour = "black") +
    scale_color_gradientn(colours = my_color, limits=c(-1,1))

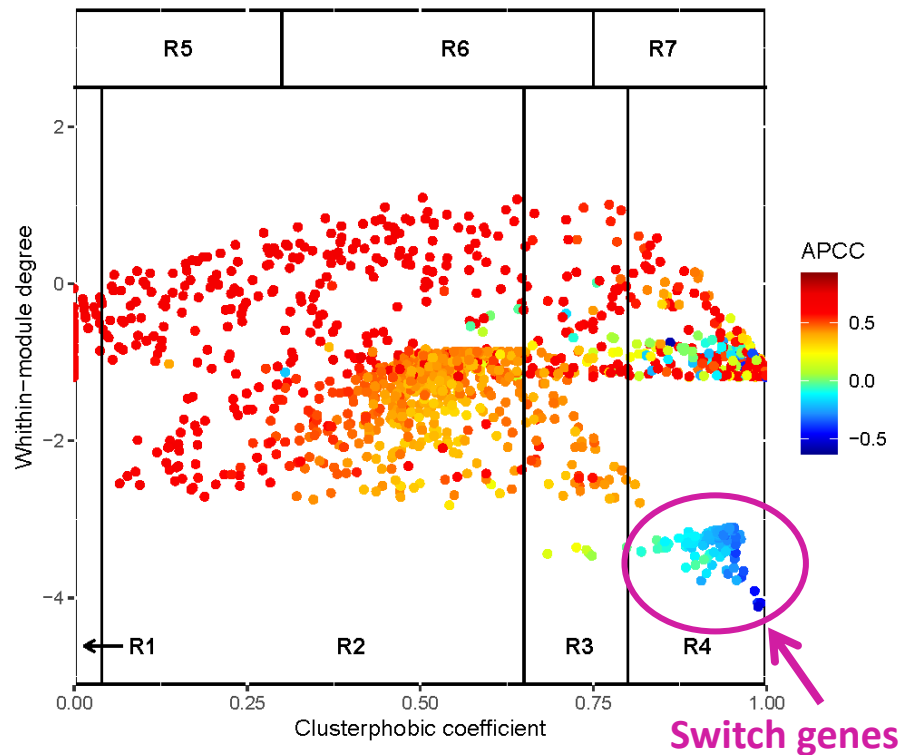
  print(p)

  savePDF(p,output_file)

}
```



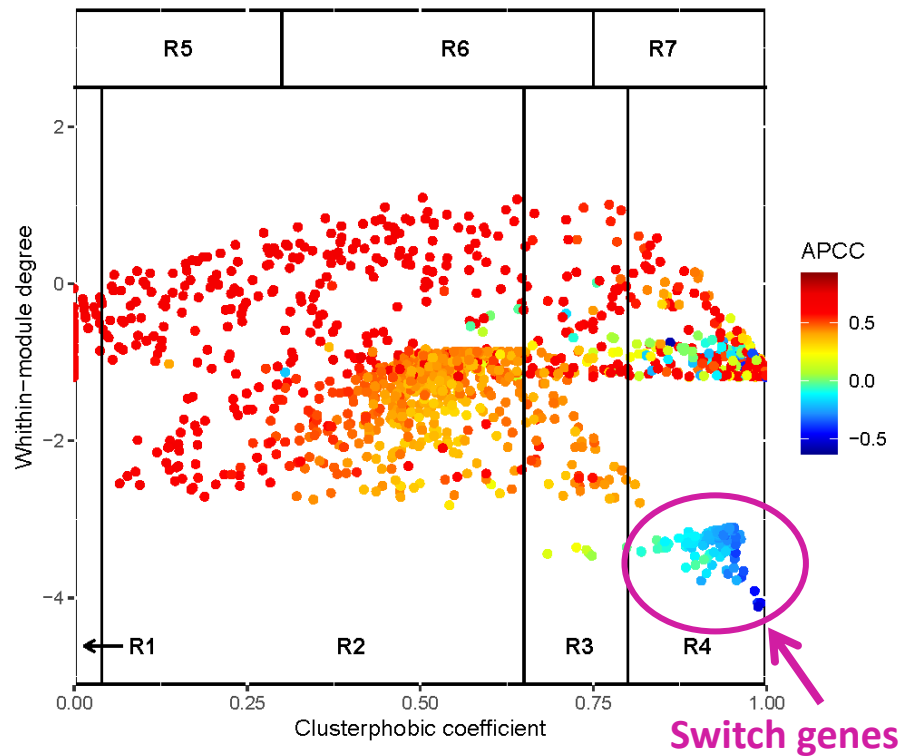
Switch genes



Switch genes

- Looking at the heat cartography map, we called “**switch genes**” the subset of the **fight-club hubs** falling in **R4** (i.e., mainly interacting outside their cluster)
- In particular, they satisfy the following topological and expression features:
 - being not a hub in their own cluster ($z_g < 2.5$)
 - having many links outside their own cluster ($K_\pi > 0.8$)
 - having a negative average weight of their incident links ($APCC < 0$)

Switch genes



Switch genes

```
getSwitch <- function(attribute,output_file){
  #####
  # input parameters
  output_file_attribute_switch <- output_file$filename_attribute_switch
  output_file_switch <- output_file$filename_switch
  #####

  ind <- which(attribute$Region == "R4" &
               attribute$Hub_classification == "FIGHT CLUB")

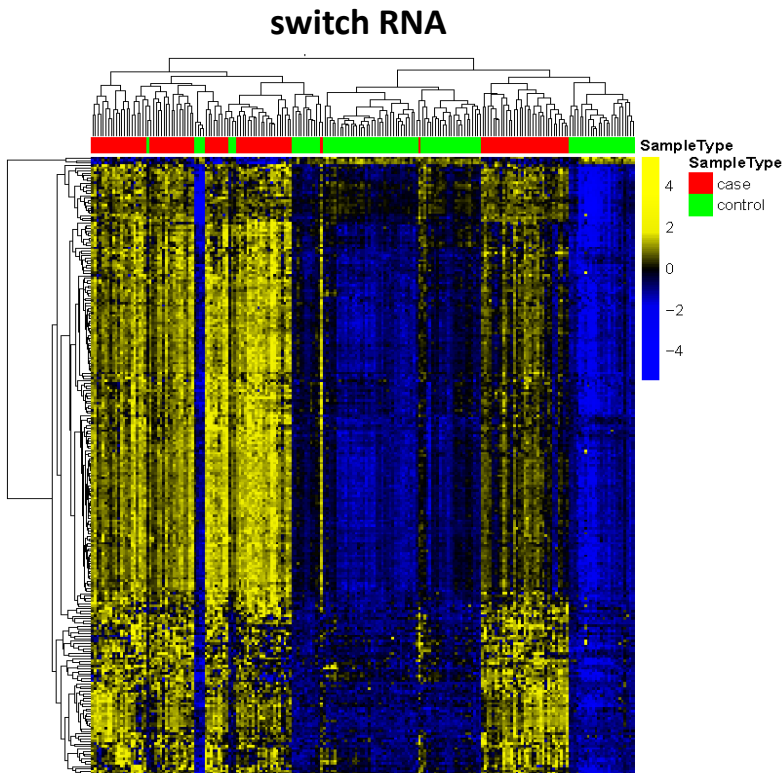
  attribute_switch <- attribute[ind,]

  switch <- attribute_switch$node

  write.table(attribute_switch, output_file_attribute_switch , row.names = F, col.names = T,
              sep = "\t", quote = F)
  write.table(switch, output_file_switch, row.names = F, col.names = F, sep = "\t", quote = F)
  )

  return(attribute_switch)
}
```

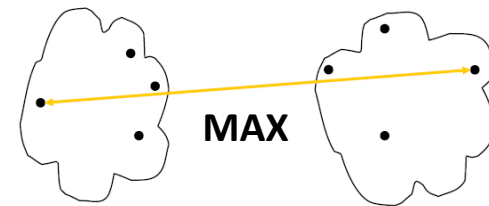
Heatmap of switch genes (RNAs)



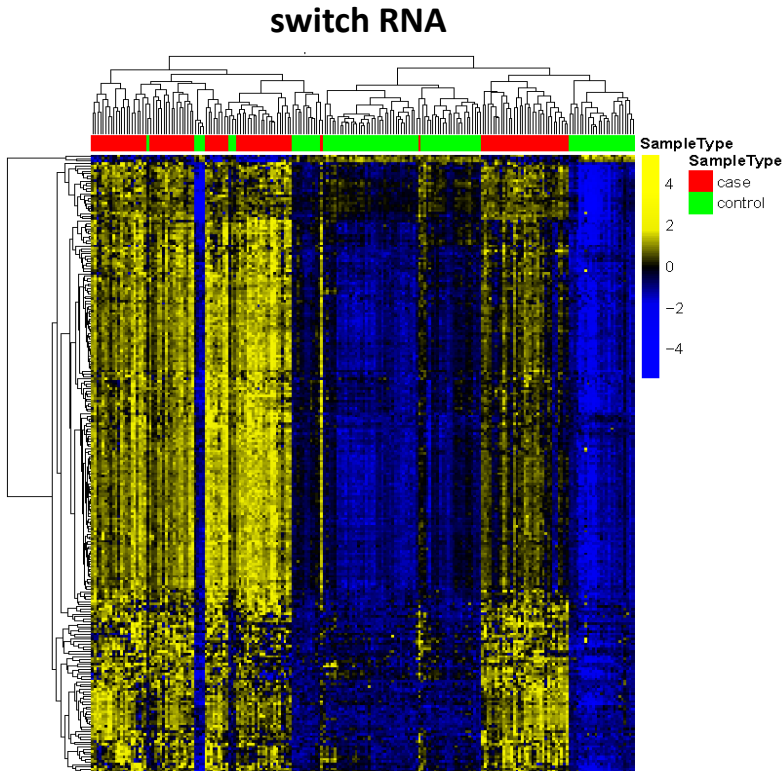
- Row refers to switch RNAs
- Columns refers to samples
- Colors represent different expression levels that increase from blue to yellow

Hierarchical clustering

- Hierarchical clustering of switch genes by using:
 - ❖ **Pearson correlation** as distance metric
 - ❖ linkage **complete** as clustering method (where distance is measured between the farthest pair of observations in two clusters)



Heatmap of switch genes (RNAs)



- Row refers to switch RNAs
- Columns refers to samples
- Colors represent different expression levels that increase from blue to yellow

```
getHeatmap <- function(data.Filtered,output_file,title){

#####
# input parameters

data <- data.Filtered$data
control <- colnames(data.Filtered$data_control)
case <- colnames(data.Filtered$data_case)
#####
samples <- ifelse( (colnames(data) %in% control), "control", "case"
)
annotation <- data.frame(SampleType = samples)
rownames(annotation) <- colnames(data)

annotation_colors <- list(SampleType = c(case = "red", control =
"green"))

colorbar <- colorRampPalette(colors = c("blue","blue1","blue2",
,"black","yellow2","yellow1","yellow"))(100)

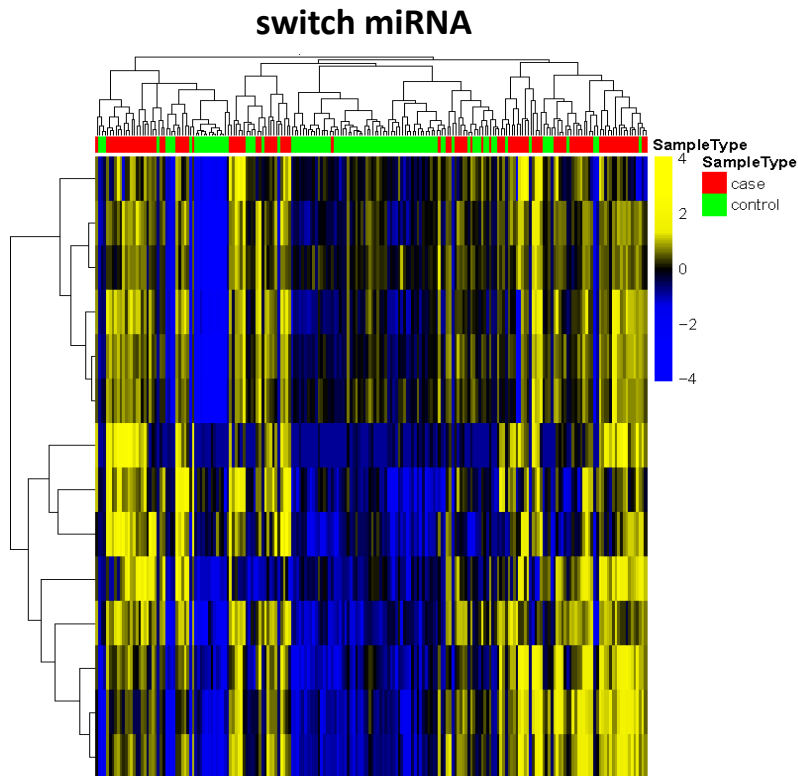
out <- pheatmap(data, scale = "row",
border_color = NA,
clustering_distance_rows = "correlation",
clustering_distance_cols = "correlation",
clustering_method = "complete",
cluster_cols = T,
cluster_rows = T,
annotation_col = annotation,
annotation_colors = annotation_colors,
color = colorbar,
show_rownames = F,
show_colnames = F,
main = title
#width = 10,
#height = 10,
#treeheight_row = 30,
#fontsize = 10,
#cellwidth = 0.3,
#cellheight = 0.3

)

saveHeatmapPDF(out,output_file)

}
```

Heatmap of switch genes (RNAs)



- Row refers to switch miRNAs
- Columns refers to samples
- Colors represent different expression levels that increase from blue to yellow

```
getHeatmap <- function(data.Filtered,output_file,title){

#####
# input parameters

data <- data.Filtered$data
control <- colnames(data.Filtered$data_control)
case <- colnames(data.Filtered$data_case)
#####
samples <- ifelse( (colnames(data) %in% control), "control", "case"
)
annotation <- data.frame(SampleType = samples)
rownames(annotation) <- colnames(data)

annotation_colors <- list(SampleType = c(case = "red", control =
"green"))

colorbar <- colorRampPalette(colors = c("blue","blue1","blue2",
,"black","yellow2","yellow1","yellow"))(100)

out <- pheatmap(data, scale = "row",
border_color = NA,
clustering_distance_rows = "correlation",
clustering_distance_cols = "correlation",
clustering_method = "complete",
cluster_cols = T,
cluster_rows = T,
annotation_col = annotation,
annotation_colors = annotation_colors,
color = colorbar,
show_rownames = F,
show_colnames = F,
main = title
#width = 10,
#height = 10,
#treeheight_row = 30,
#fontsize = 10,
#cellwidth = 0.3,
#cellheight = 0.3

)

saveHeatmapPDF(out,output_file)

}
```



At the end of Module 3, you will
obtain the list of switch genes