

Importing data

Pre-processing phase

Filtering phase

Building the correlation network

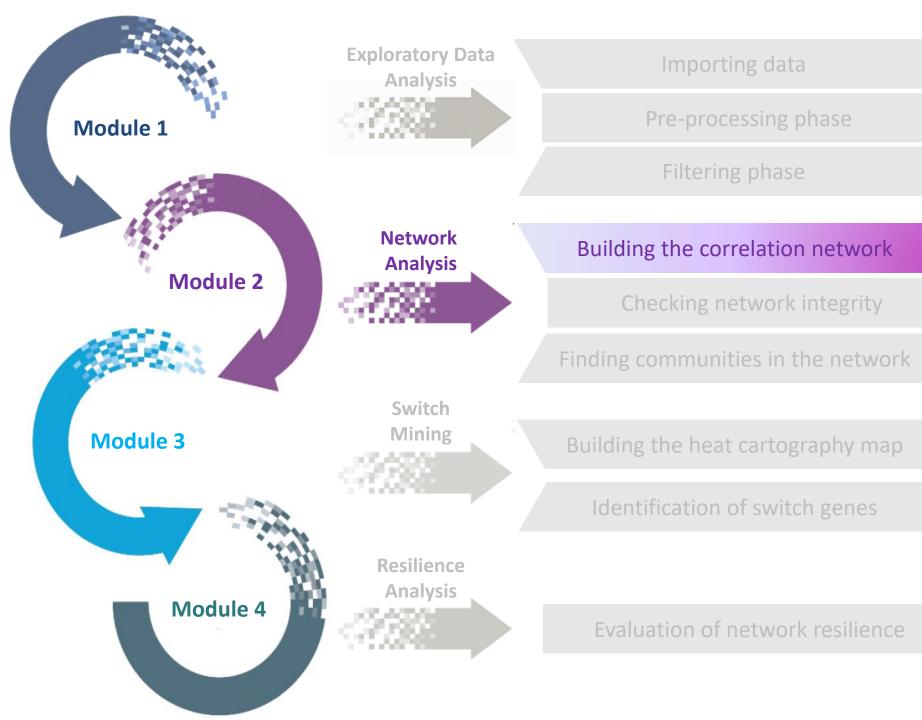
Checking network integrity

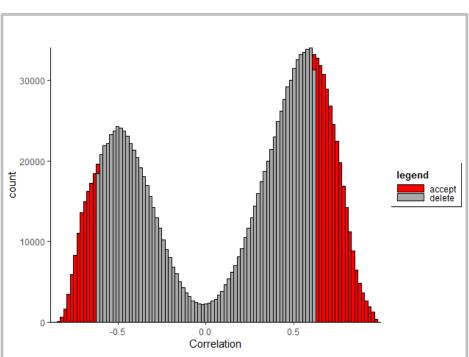
Finding communities in the network

Building the heat cartography map

Identification of switch genes

Evaluation of network resilience





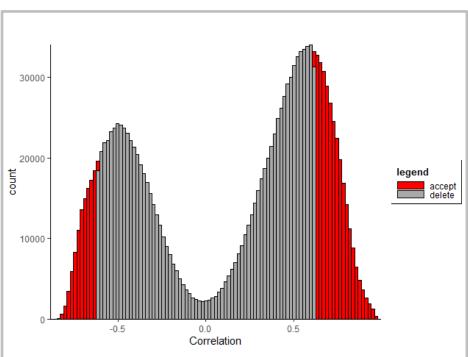
- x-axis represents the Person correlation coefficient between the expression profiles of all pairs of genes
- y-axis represents the frequency
- red bars are the selected highly correlated pairs
- grey bars are the deleted poorly correlated pairs

#### **Correlation between two variables**

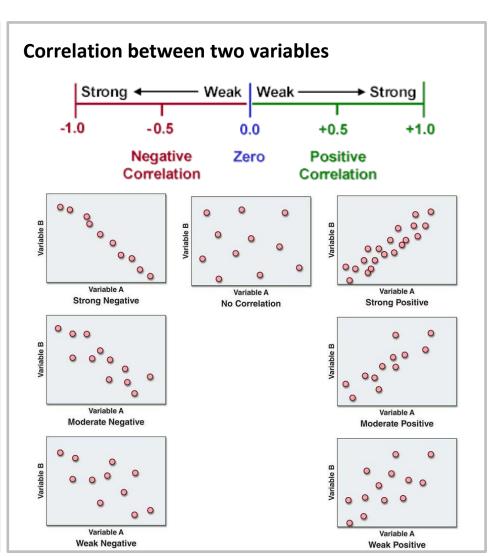
 The existence of a linear relationship between two normally distributed continuous variables (e.g., gene expression values of gene X and gene Y) can be expressed by the Pearson correlation coefficient ρ

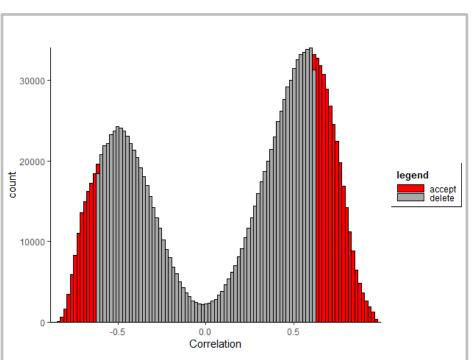
$$\rho_{xy} = \frac{\sum_{i=1}^{col} \left(x_i - x\right) \left(y_i - y\right)}{\sqrt{\sum_{i=1}^{col} \left(x_i - x\right)^2 \sum_{i=1}^{col} \left(y_i - y\right)^2}}$$

 p coefficient varies between -1 and 1 and shows strength (value) and direction (sign) of correlation



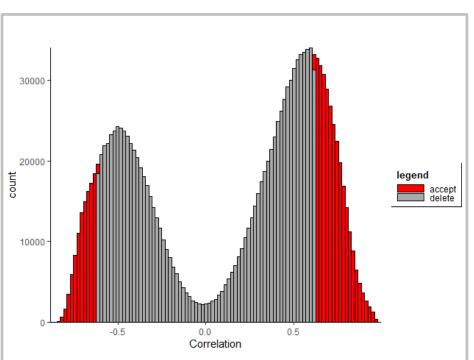
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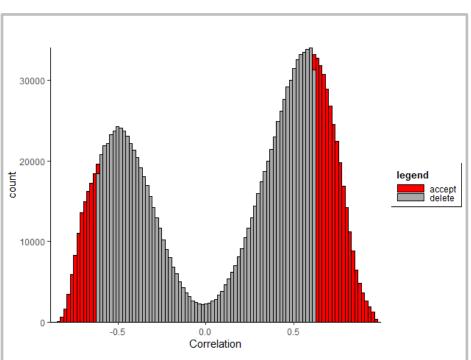
#### **Correlation between two variables**



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#### Correlation between two variables

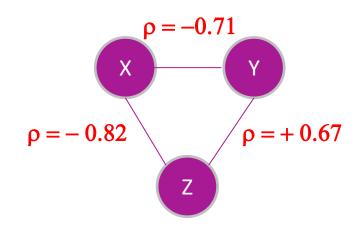
Caveat: the user can choose even other correlation methods (e.g. type = Spearman)

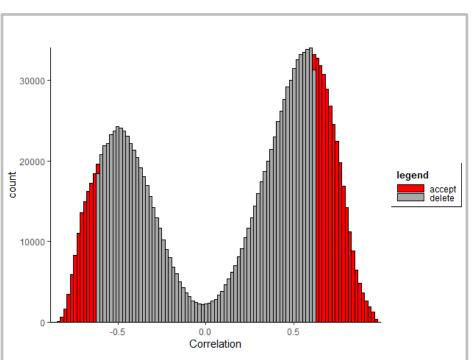


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#### **Correlation network**

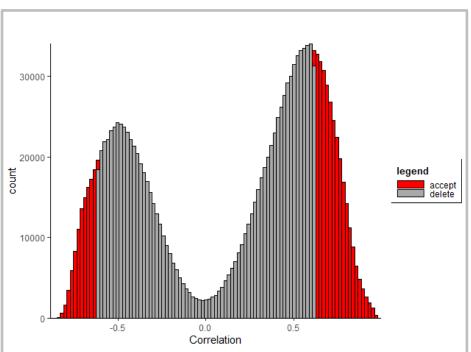
Nodes are genes (including RNAs and miRNAs if available) and a link occurs between two nodes if the absolute value of the Pearson correlation between their expression profiles is greater than the selected threshold (e.g., 80<sup>th</sup> percentile → 0.63)





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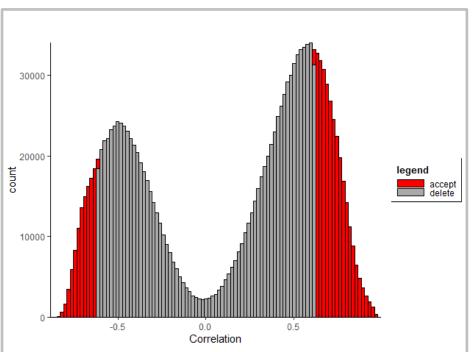
#### **Correlation network**



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### **Histogram of Pearson correlation**

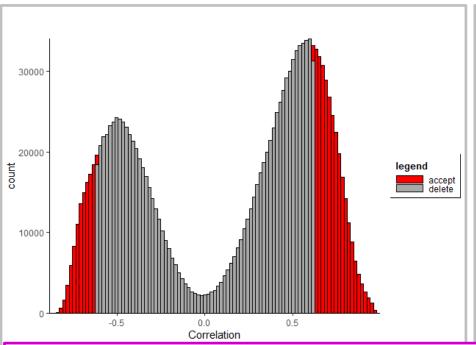
```
getHistogram <- function(x,threshold,title,xlabel){</pre>
  df <- data.frame(variable = x)</pre>
  df$legend <- ifelse( (abs(x) <= threshold), "delete", "accept")</pre>
  w < - (max(x) - min(x)) / 100
 p = ggplot(df, aes(variable, fill = legend)) + geom_histogram
(binwidth = w, colour='black') +
    scale_x_continuous(expand = c(0, 0)) + scale_y_continuous(expand
    scale_fill_manual(values = c("delete" = "darkgrey", "accept" =
    theme(panel.grid.major = element_blank(), panel.grid.minor =
element_blank(),
          panel.background = element_blank(), axis.line = element_li
ne(colour = "black"),
          plot.title = element_text(hjust = 0.5, face = "bold"),
          legend.title = element_text(colour = "black", size=10,
face="bold"),
          legend.key.height = unit(0.2, "cm"),legend.key.width =
unit(1, "cm"),
          legend.box.background = element_rect(colour = "black")) +
    labs(title = title, x = xlabel)
 print(p)
```



- x-axis represents the Person correlation coefficient between the expression profiles of all pairs of genes
- red /! Caveat: Only the highly correlated pairs (red bars) according to the grey selected threshold will be used to build the correlation network
- y-axis represents the frequency
   print(p)

Histogram of Pearson correlation

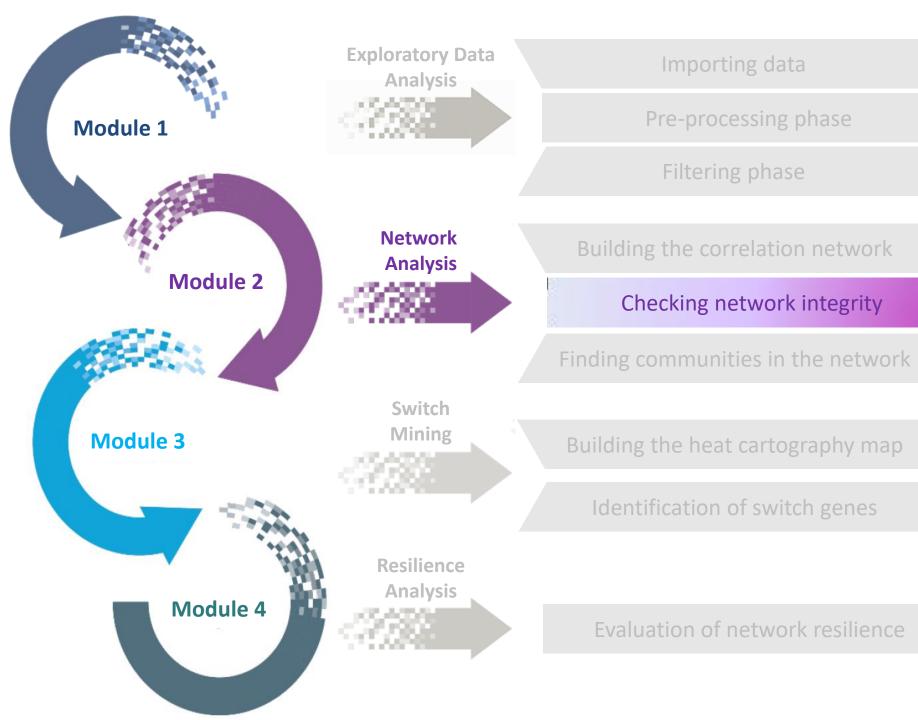
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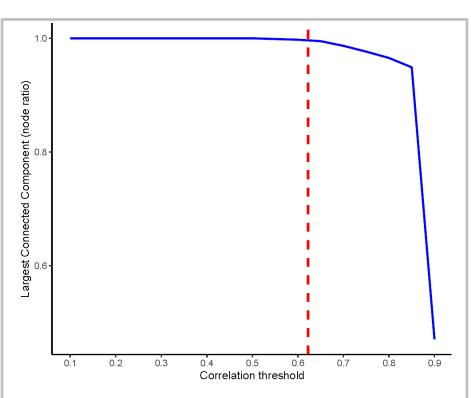


### **Histogram of Pearson correlation**



Correlation threshold should reflect a right balance between the number of edges and the number of connected components of the network: the number of edges should be as small as possible in order to have a manageable network (high threshold) and the number of connected components should be as small as possible in order to preserve the integrity of the network (small threshold).



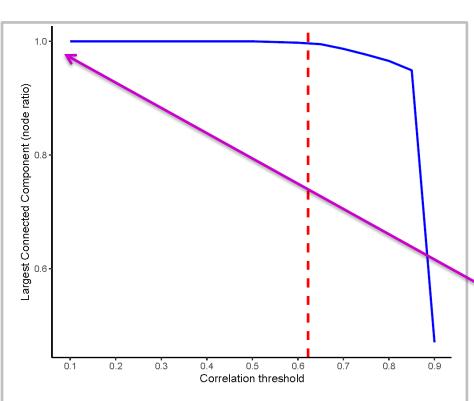


- x-axis represents the Pearson correlation threshold varying in the chosen range
- y-axis represents the fraction of nodes populating the largest connected component
- dashed red line correspond to the selected threshold

### **Network integrity**

- This step evaluates the effect on the network connectivity of varying the Pearson correlation threshold
- It is optional: set "T" on main.R

```
network <- NetworkAnalysis(data, checkNetIntegrity = T,
screePlot = T)</pre>
```

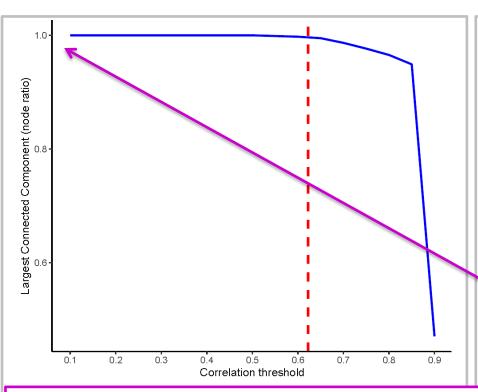


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y=1 means that all nodes fall in the largest component and thus the network is fully connected; otherwise more components exist



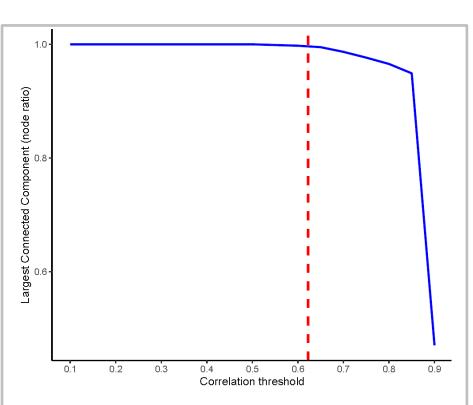
#### **Network integrity**

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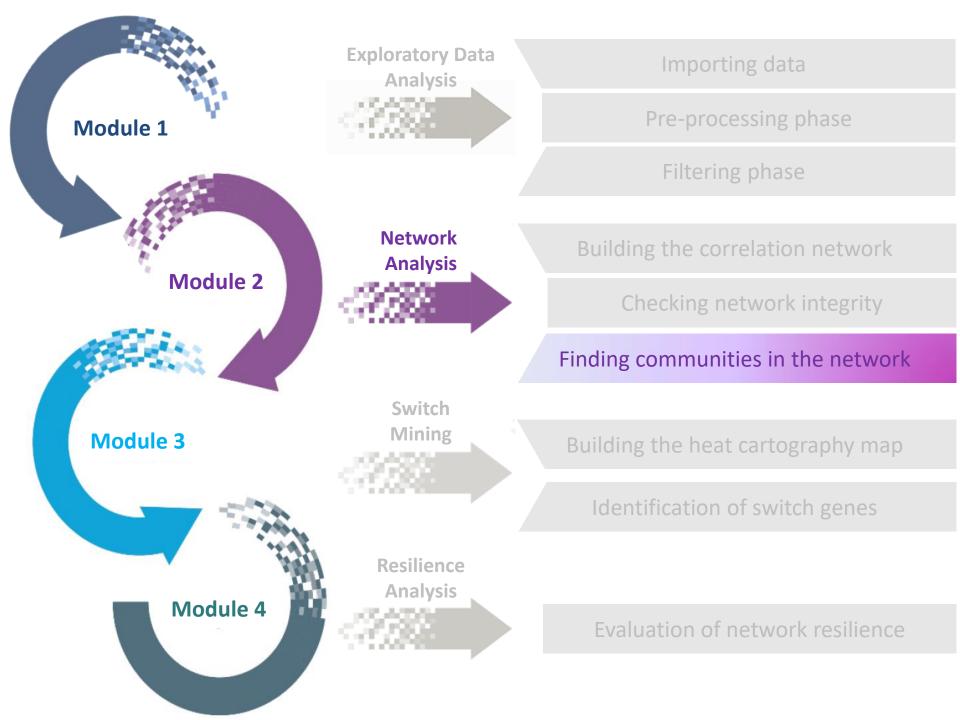
A reasonable choice for the correlation threshold should be the largest one (corresponding to the smallest number of edges) for which the fraction of nodes of the largest connected component is equal to 1. Here, we could have increased the threshold up to 0.7.



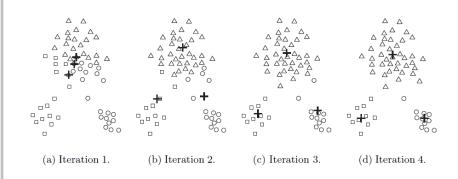
- x-axis represents the Pearson correlation threshold varying in the chosen range
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- dashed red line correspond to the selected threshold

#### **Network integrity plot**

```
getNetworkIntegrityPlot <- function(df,min_rho,max_rho</pre>
,threshold_corr,output_file){
 p <- ggplot(df, aes(x = threshold_corr, y = frac_node_LCC))</pre>
    geom_line(color = "blue", size = 1) + scale_x_continuous
(breaks=seq(min_rho,max_rho,0.1)) +
    theme(panel.grid.major = element_blank(), panel.grid.minor
= element_blank(),
          panel.background = element_blank(), #axis.title =
element_text(face = "bold"),
          axis.line = element_line(colour = "black")) +
    labs(x = "Correlation threshold", y = "Largest Connected")
Component (node ratio)") +
    geom_vline(xintercept = threshold_corr, linetype =
"dashed", color = "red", size = 1)
  print(p)
  savePDF(p,output_file)
```



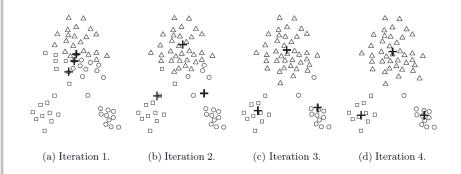
- 1: Select K points as initial centroids.
- 2: repeat
- 3: Form K clusters by assigning each point to its closest centroid.
- 4: Recompute the centroid of each cluster.
- 5: until Centroids do not change.



### K-means algorithm

- This step searches for communities in the correlation network by a k-means algorithm
- k-means is a clustering algorithm whose aim is to partition a set of n objects in N groups (clusters) so that each object belongs to the cluster with the nearest centroid

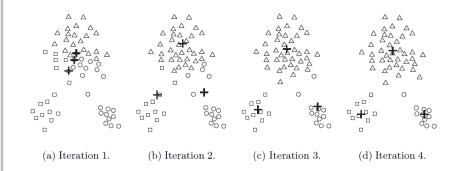
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### K-means algorithm

- It requires to know the number of clusters in advance
- The k-means algorithm performs iterations until the minimum of the Sum of the Squared Error (SSE) function is reached
- SWIMmer repeats the clustering many times (replicates), each with a new set of initial cluster centroid positions, randomly chosen, and selects the clusters configuration corresponding the minimum of SSE among all replicates

- 1: Select K points as initial centroids.
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### K-means algorithm

The Sum of the Squared Error function is

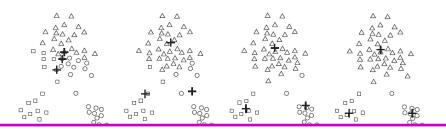
$$SSE = \sum_{i=1}^{K} \sum_{x \in C_i} dist^2(c_i, x)$$

 where dist is the Euclidean distance, K is the number of the clusters, C<sub>i</sub> is the i<sup>th</sup> cluster, x is a node in the i<sup>th</sup> cluster, c<sub>i</sub> is the centroid of the i<sup>th</sup> cluster given by:

$$c_i = \frac{1}{m_i} \sum_{x \in C_i} x_i$$

• where  $m_i$  is the number of nodes in the  $i^{th}$  cluster. There are as many centroids as the number of the clusters.

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### K-means algorithm

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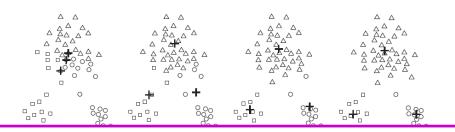


The choice of the Euclidean distance is intended to emphasize the differences between correlated and anti-correlated genes.

$$dist^{2}(A,B) = (x_{1}^{A} - x_{1}^{B})^{2} + (x_{2}^{A} - x_{2}^{B})^{2} + \dots + (x_{N}^{A} - x_{N}^{B})^{2}$$

 $x_1^A = a_{A,1}$  where  $a_{N,N}$  is the weighted adjacency matrix and the weights are the Pearson correlation coefficients

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### K-means algorithm

The Sum of the Squared Error function is

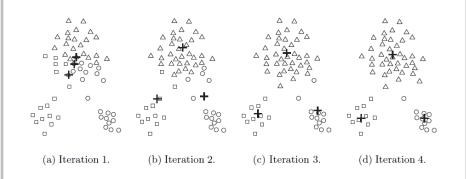
$$SSE = \sum_{i=1}^{K} \sum_{x \in C_i} dist^2(c_i, x)$$

• where *dist* is the Euclidean distance, K is the number of the clusters,  $C_i$  is the  $i^{th}$  cluster, x is a node in the  $i^{th}$  cluster,  $c_i$  is the centroid of the  $i^{th}$  cluster given by:



Thus, two nodes A, B are close in the network (dist=0) if they are highly correlated ( $\rho=1$ ) and they are far apart in the network ( $dist=dist_{max}$ ) if they are highly anti-correlated ( $\rho=-1$ ).

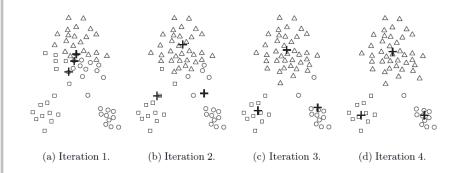
- 1: Select  $\overline{K}$  points as initial centroids.
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#### K-means algorithm

```
parameters
               weighted
          adjacency matrix
getClustering <- function(w_adj_num_clusters,iter_max_num_repeats
,output_file_idx){
 model <- kmeans(w_adj, centers = num_clusters, iter.max = iter_max,</pre>
nstart = num_repeats
                           # the Within-cluster Sum of Square
 WSS <- model$withinss
 TWSS <- model$tot.withinss # the Total Within-cluster Sum of Square
 size <- model$size
 idx <- data.frame(cluster = as.factor(model$cluster))</pre>
 write.table(idx, output_file_idx, sep="\t", row.names = T, col.names =
NA, quote = F)
 res <- list(idx = idx, size = size, WSS = WSS, TWSS = TWSS)
 return(res)
```

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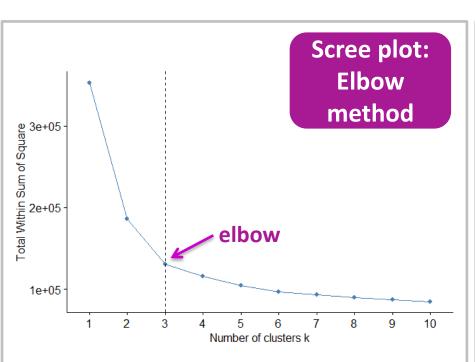
#### K-means parameters

- the number of clusters
- the maximum number of iterations allowed for each replicate of k-means
- the number of replicates for a given number of clusters

**!** Caveat: maximum number of iterations should be large enough to guarantee convergence

**!** Caveat: more replicates get you more confident to be far from a local minimum

# Scree plot



- x-axis refers to the number of clusters
- y-axis refers to the value of the error function corresponding to the best clusters configuration among all replicates for that number of clusters

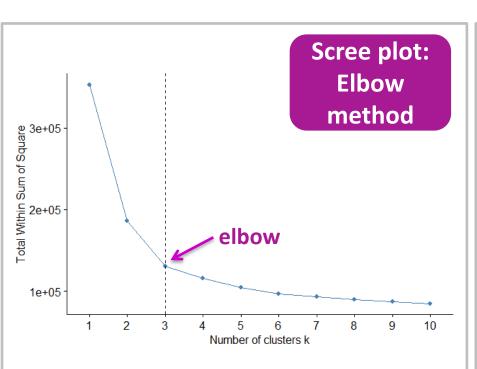
### Scree plot computation

- Scree plot will be produced to suggest the best choice for the number of clusters
- It is optional: set "T" on main.R

```
network <- NetworkAnalysis(data, checkNetIntegrity = T,
screePlot = T)</pre>
```

- It shows the value of the error function (SSE) for each number of clusters
- a good choice for the optimal number of clusters is in correspondence of the elbow

# Scree plot



- x-axis refers to the number of clusters
- y-axis refers to the value of the error function corresponding to the best clusters configuration among all replicates for that number of clusters

#### Scree plot computation

