

1.11 ~~1, 2, 3, 4, 5, 6, 7, 8~~

1.12 ~~1, 2, 3, 4, 5, 6, 7, 8~~

1) ~~2 exp(iπ/2)~~

$$\sqrt{R_0} \exp\left[i\left(\frac{\theta_0}{n} + \frac{2k\pi}{n}\right)\right]$$

a) $\sqrt{2} \exp\left(i\left(\frac{\pi}{4} + \frac{k\pi}{4}\right)\right) \rightarrow \sqrt{2} \exp\left(i\left(\frac{\pi}{4} + 0\right)\right) \& \sqrt{2} \exp\left(i\left(\frac{\pi}{4} + \frac{2\pi}{4}\right)\right)$

$$\sqrt{2} \exp\left(i\left(\frac{\pi}{4} + 0\right)\right) = \sqrt{2} \left(\cos\left(\frac{\pi}{4}\right) + i \sin\left(\frac{\pi}{4}\right) \right) = 1 + i$$

$$\pm (1 + i) \quad k=1 \text{ moves to positive}$$

b) $1 - \sqrt{3}i$

$$\sqrt[4]{4} \exp\left(i\left(\frac{-\pi}{3} + \frac{2k\pi}{n}\right)\right)$$

$$\sqrt{2} \exp\left(i\left(\frac{-\pi}{6} + k\pi\right)\right)$$

$$\sqrt{2} \exp\left(i\left(\frac{-\pi}{6} + 0\right)\right), 2 \exp\left(i\left(\frac{-\pi}{6} + \pi\right)\right)$$

$$\pm \frac{\sqrt{3} - i}{\sqrt{2}}$$

3) $(-8 - 8\sqrt{3}i)^{1/4} = 16^{1/4} \exp\left[i\left(\frac{\pi}{3}\right)\right]$

$$2 \exp\left[i\left(\frac{\pi}{12} + 0\right)\right]$$

$n=0 \quad 2 \cos\left(\frac{\pi}{12}\right) + 2i \sin\left(\frac{\pi}{12}\right) = (1 + \sqrt{3}i)$

$n=1 \quad 2 \cos\left(\frac{\pi}{12} + \frac{2\pi}{4}\right) + 2i \sin\left(\frac{\pi}{12} + \frac{2\pi}{4}\right) = (-\sqrt{3} + i)$

$n=2, n=3 \dots \text{yields } \pm (1 + \sqrt{3}i) \& \pm (\sqrt{3} - i)$

$$z_0 = (1 + i)$$

$$b) \quad z_1 = \sqrt{2} e^{i\left(\frac{\pi}{4} + \frac{\pi}{2}\right)} = (-1 + i)$$

$$z_2 = \sqrt{2} e^{i\left(\frac{\pi}{4} + \frac{\pi}{4}\right)} = (-1 - i)$$

$$z_3 = \sqrt{2} e^{i\left(\frac{\pi}{4} + \frac{6\pi}{4}\right)} = (1 - i)$$

$$(z^2 + 2z + 2)(z^2 - 2z + 2)$$

$$8) \quad az^2 + bz + c = 0$$

$$a\left(z + \frac{b}{2a}\right)^2 + c - \frac{b^2}{4a} = 0$$

$$\cancel{a\left(z + \frac{b}{2a}\right)^2} + \cancel{c} - \frac{b^2}{4a} = \frac{b^2}{4a}$$

$$\cancel{a\left(z + \frac{b}{2a}\right)^2} + \cancel{c} = \frac{b^2}{4a}$$

$$a\left(z + \frac{b}{2a}\right)^2 + c = \frac{b^2}{4a}$$

$$\left(z + \frac{b}{2a}\right)^2 = \frac{b^2}{4a^2} - \frac{c}{a}$$

$$z + \frac{b}{2a} = \frac{b^2}{2a} - \frac{\sqrt{c}}{\sqrt{a}} = \frac{b^2}{2a} - \frac{\sqrt{4ac}}{2a} = \frac{b^2 - 4ac}{2a}$$

$$z = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$4 - 4 - 4i \\ +4i \quad \sqrt{4i}$$

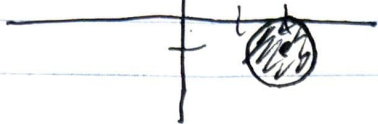
$$b) \quad a=1, \quad b=2 \quad c=1-i$$

$$\frac{-2 \pm \sqrt{4 - 4(1-i)}}{2} = \frac{-2 \pm 2\sqrt{i}}{2}$$

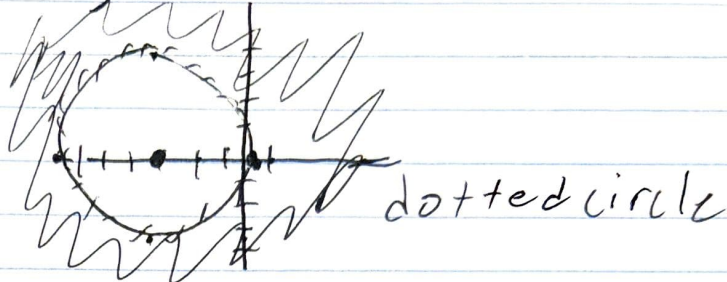
$$\left(-1 + \frac{1}{\sqrt{2}}\right) + \frac{i}{\sqrt{2}} \quad \left(-1 - \frac{1}{\sqrt{2}}\right) - \frac{i}{\sqrt{2}} = -1 + 2\sqrt{i}$$

1.12

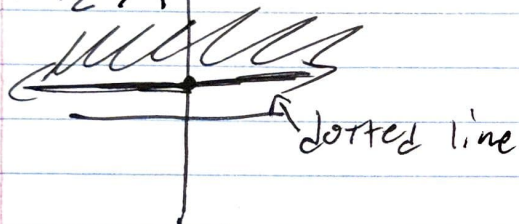
1) a) $|z - 2 + i| \leq 1$



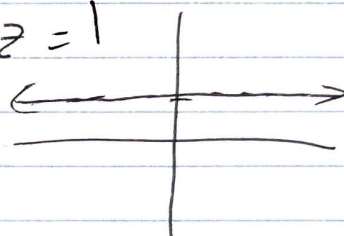
b) $|2z + 3| > 4$



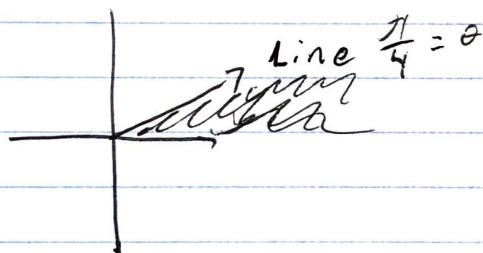
c) $\text{Im } z > 1$



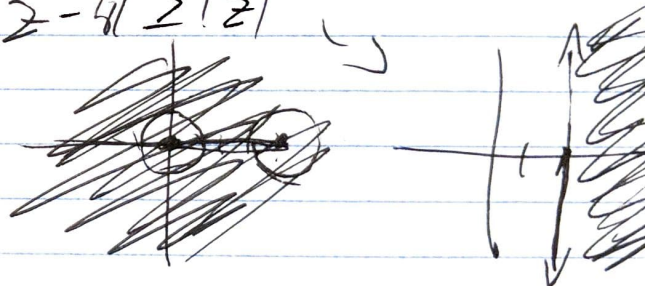
d) $\text{Im } z = 1$



e)



f) $|z - 4| \geq |z|$



b & c are domains

2) e, containing points on 2 sides, but goes to infinity.

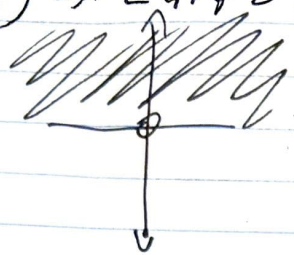
3) a, fully bounded by function

$$(x+yi)^2 = x^2 - y^2 + 2xyi$$

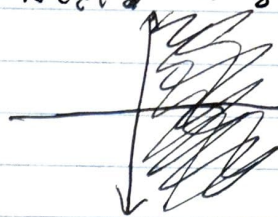
$$x^2 < x^2 + y^2 \quad 0 < y^2$$

$$\sqrt{x^2} < \sqrt{x^2 + y^2}$$

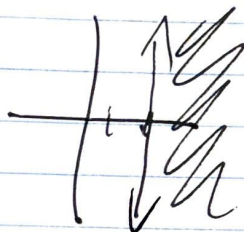
4) a) $-\pi < \arg z < \pi$



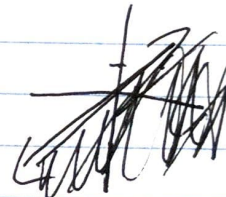
b) $\operatorname{Re} z < |z|$



$$c) \operatorname{Re} \frac{1}{z} \leq \frac{1}{2} = \frac{1}{x} \leq \frac{1}{2} = 2 \leq x$$



d) $\operatorname{Re} z^2 \geq 0$



7) a) none, every other is real / imaginary

b) 0, as $n \rightarrow \infty$, $z_n \rightarrow 0$

c) 0, points accumulate to origin

d) $\pm (1 \pm i)$

