# pyTopoComplexity: A Python package for topographic complexity analysis

18 August 2024

## Summary

pyTopoComplexity is a Python package that provides a computationally efficient and customizable implementation of three methods for quantifying topographic complexity. These methods include two-dimensional continuous wavelet transform (2D-CWT) analysis, fractal dimension estimation, and rugosity index calculation across various spatial scales. This package addresses the scarcity of open-source software for these sophisticated methods, which are crucial in modern terrain analysis, and facilitates data comparison and reproducibility. In the software diffusion processes. By combining these features, pyTopoComplexity advances the toolset available to researchers for measuring and simulating

respository, we also include a Jupyter Notebook file that integrates components from the Python-based surface-process modeling platform Landlab (Hobley et al. 2017). This allows researchers to simulate the smoothing of topography over time through terrestrial nonlinear hillslope the time-dependent persistence of topographic complexity signatures against environmental forces on terrain surfaces.

Newman, and Francioni 2019; Pardo-Igúzquiza and Dowd 2022a), evaluating the depositional age of event sedimentation and subsequent erosion processes (Hetz et al. 2016; Johnstone et al. 2018; Booth et al. 2017; LaHusen et al. 2020; Herzig et al. 2023), and identifying habitats to assess ecological diversity on land and seafloor (Frost et al. 2005; Hetz et al. 2016; Wilson et al. 2007). In recent years, several advanced methods for quantifying topographic complexity have been developed, including two-dimensional continuous wavelet transform (2D-CWT) analysis (Booth, Roering, and Perron 2009; Berti, Corsini, and Daehne 2013), fractal dimension estimation (Taud and Parrot 2005; Robbins 2018; Pardo-Igúzquiza and Dowd 2020), and rugosity index calculation (Jenness 2004; Du Preez 2015). These methods are considered more effective for terrain analysis tasks compared to conventional morphological metrics such as variations in local slope and relief.

Despite their importance, comprehensive publicly available tools that incorporate these advanced methods for studying topographic complexity are lacking. Common open-source geospatial analysis software, such as QGIS (QGIS Development Team 2023), GRASS GIS (GRASS Development Team 2023), and WhiteboxTools (J. B. Lindsay 2016), only implement basic conventional methods, limiting the reproducibility and comparability of these newer approaches. Although some specialized programs for calculating the rugosity index exist (Walbridge et al. 2018; Benham 2022), they have been limited to marine bathymetric studies and involve various mathematical choices and designs. To address this gap, we have developed an open-source Python toolkit called pyTopoComplexity, which provides computationally efficient and easily customizable implementations of three modules for performing and visualizing the results of 2D-CWT, fractal dimension, and rugosity calculations (Table 1). This toolkit can detect the grid spacing and unit of the projected coordinate system (acceptable in meters, U.S. survey feet, and international feet) from the input raster DTM file (GeoTIFF format) and automatically conduct unit conversions in necessary calculation steps to ensure data consistency and reproducibility. Results at nodes affected by edge effects due to no-data values outside the input raster will be

removed by default. Users can define the suitable spatial scale to match their research purposes and choose computational approaches (e.g., chunk processing, faster mathematical approximations) to optimize performance (see details in the Methods and features overview section). Table 1 : Modules contained in the **pyTopoComplexity** package. **Modules Method Descriptions** References Classes **CWTMexHat** pycwtmexhat.py Quantifies the wavelet-based Booth, Roering, and Perron (2009); curvature of the land surface using Booth et al. (2017) two-dimensional continuous

analysis on the land surface using Pardo-Igúzquiza and Dowd (2020) variogram procedures RugosityIndex pyrugostiy.py Calculates the rugosity index of Jenness (2004); Du Preez (2015) the land surface Each module of the **pyTopoComplexity** is provided with a corresponding example Jupyter Notebook file for usage instructions, using the Light Detection and Ranging (LiDAR) DTM data of a deep-seated landslide that occurred in 2014 in the Oso area of the North Fork Stillaguamish River valley, Washington State, USA (Washington Geological Survey 2023). In the software repository, we also include an additional Jupyter Notebook file **nonlineardiff\_Landlab.ipynb**, which allows researchers to simulate the smoothing of topography over time via terrestrial nonlinear hillslope diffusion processes (Roering, Kirchner, and Dietrich 1999). This is achieved by employing the TaylorNonLinearDiffuser module from the terrainBento Python package (Barnhart et al. 2019) and running the simulation in the **Landlab** environment (Hobley et al. 2017).

Methods and features overview Two-dimensional continuous wavelet transform analysis The pycwtmexhat.py module in pyTopoComplexity implements the 2D-CWT method for terrain analysis, providing detailed information on how

amplitude is distributed across spatial frequencies at each position in the data by transforming spatial data into position-frequency space. This method is particularly effective for depicting the Laplacian of topography (Torrence and Compo 1998; Lashermes, Foufoula-Georgiou, and Dietrich 2007), revealing concave and convex regions of topography at various scales (Malamud and Turcotte 2001; Struble et al. 2021), identifying deep-seated landslides (Booth, Roering, and Perron 2009; Berti, Corsini, and Daehne 2013), and estimating the depositional ages of landslide deposits (Booth et al. 2017; LaHusen et al. 2020; Underwood 2022; Herzig et al. 2023).

The 2D-CWT is computed by convolving the elevation data z with a wavelet family  $\psi$ , using a wavelet scale parameter s at every location (x, y):

# $C(s, x, y) = \Delta^2 \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} z(x, y) \psi(x, y) \, dx \, dy$

## , where the resultant wavelet coefficient C(s, x, y) provides a measure of how well the wavelet $\psi$ matches the data z at each grid (Torrence and

sensitive to fine-scale features of z. In this implementation, we use the 2D Mexican Hat wavelet (i.e., Ricker wavelet) function to define  $\psi$ :  $\psi = -\frac{1}{\pi (s\Delta)^4} (1 - \frac{x^2 + y^2}{2s^2}) e^{(-\frac{x^2 + y^2}{2s^2})} \qquad \lambda = \frac{2\pi s}{\sqrt{5/2}} \Delta$ The Mexican hat wavelet is proportional to the second derivative of a Gaussian envelope, with its Fourier wavelength ( $\lambda$ ) dependent on the grid spacing ( $\Delta$ ) of the input DTM raster. The wavelet function  $\psi$  is scaled according to the wavelet scale parameter s and the grid spacing  $\Delta$ , ensuring that the resultant wavelet coefficient C signifies concave and convex landforms corresponding to the wavelet scale s. Users can define the value of  $\lambda$  in meters as the targeted spatial scale for landform roughness analysis, and the **pycwtmexhat.py** module will automatically

We note that the C and  $\psi$  equations presented here are the mathmetical approaches adapted in later publications (LaHusen et al. 2020;

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X-axis grids

(grid size ≈ 3.0 [US survey foot])

Mexican Hat 15 m 2D-CWT surface roughness [m<sup>-1</sup>]

Mexican Hat 60m 2D-CWT

X-axis grids

Mexican Hat 30 m 2D-CWT surface roughness [m<sup>-1</sup>]

Mexican Hat 75m 2D-CWT

MIN: 0.0004135138005949557 MAX: 0.1360670030117035 R2 MIN : 0.0002040372637566179 R2 MAX: 0.9999973773956299

Horizontal Variogram (Middle Row)

Vertical Variogram (Middle Column)

1.5 Log(Lag Distance)

Diagonal Variogram

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Fitted Line

Fitted Line

Estimated Fractal Dimension: 2.088997230032921

Data •

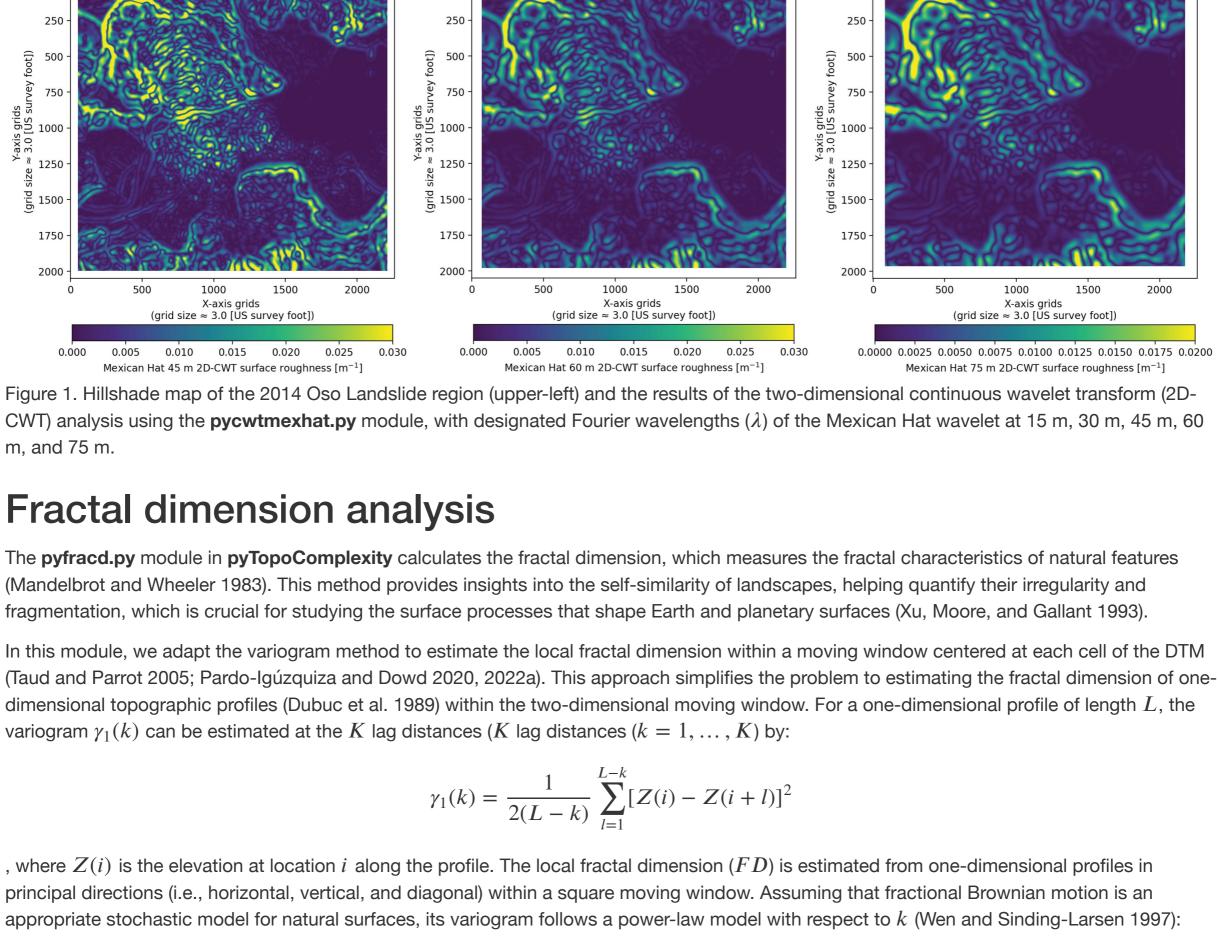
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addition to calculating the fractal dimension, the **pyfracd.py** module also computes reliability parameters such as standard error and the coefficient of determination (
$$R^2$$
) to assess the robustness of the analysis (Figure 2).

Ososlid2014 f 3ftgrid.tif Fractal Dimension (~15.54m x ~15.54m window)

, and its exponent  $\beta$  is related to the local fractal dimension (FD) by:

(grid size ≈ 3.0 [US survey foot])

Standard Error of Fractal Dimension

hillslope diffusion process

Taylor series expansion (Ganti, Passalacqua, and Foufoula-Georgiou 2012):

changes in surface elevation z over time t:

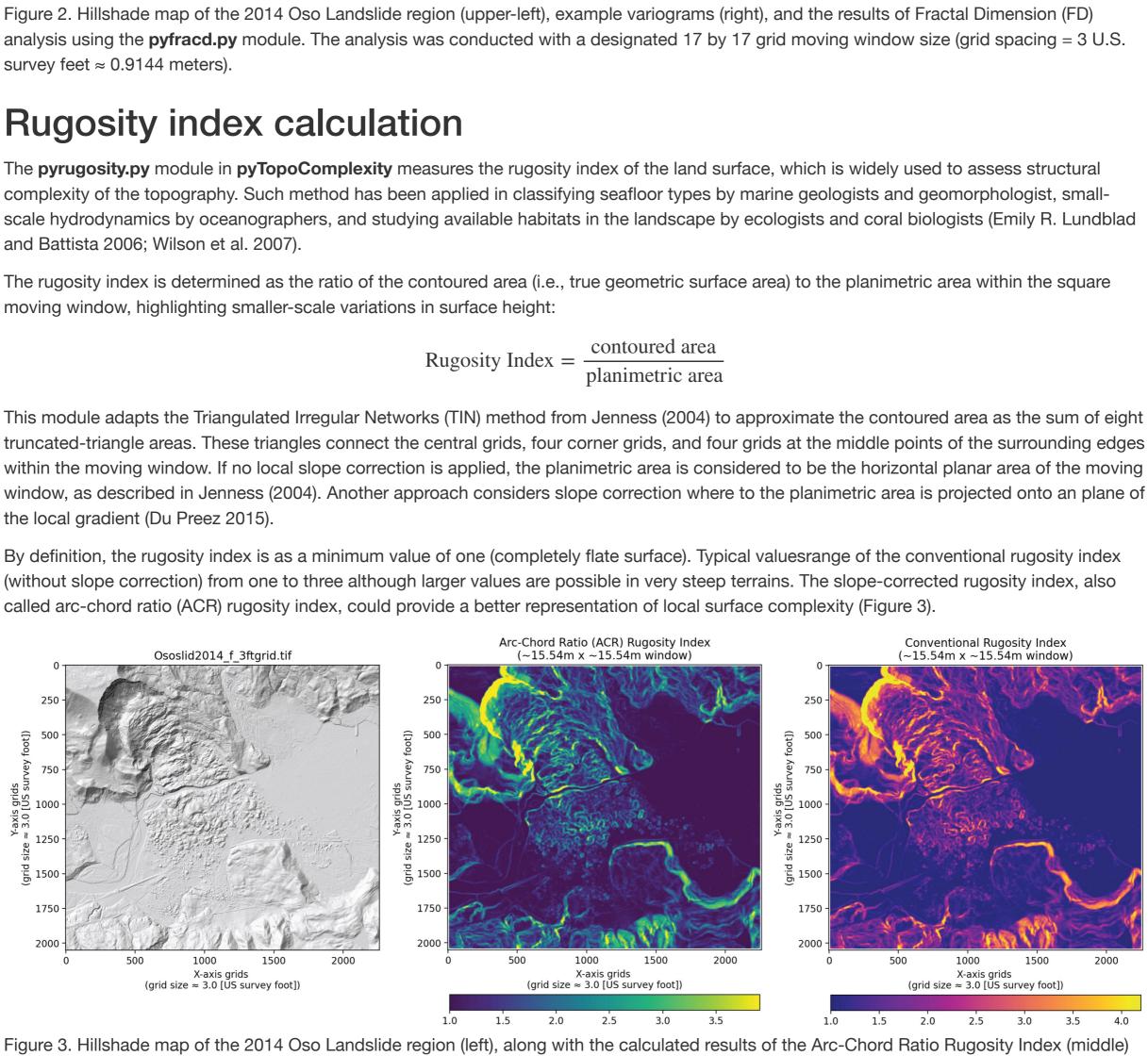
one-dimensional profiles  $(FD)_1^*$ :

250

Y-axis grids ≥ ≈ 3.0 [US survey foot]) 1000 1000 1000

1250

g 1500 1750 1750 0.0 Log(Lag Distance) 2000 2000 -500 1500 2000 X-axis grids X-axis grids Estimated Fractal Dimension: 2.064460226744064



Ososlid2014\_f\_3ftgrid Ososlid2014\_f\_3ftgrid Time: 2000 years (K = 0.0029 m²/yr) Ososlid2014\_f\_3ftgrid Time: 0 years (K = 0.0029 m²/yr) Time: 1000 years ( $K = 0.0029 \text{ m}^2/\text{yr}$ ) 1.080 1.080 1.080 Yaxis grids ≈ 3.0 [US survey foot]) Yaxis grids = 3.0 [US survey foot])

parameter values provided in Booth et al. (2017), in an attempt to reproduce the simulation results presented in that study (Figure 4).

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## Dr. Eulogio Pardo-Igúzquiza, who generously shared his Fortran code for fractal dimension analysis used in his work Pardo-Igúzquiza and Dowd (2022b), which significantly inspired the development of the **pyfracd.py** module. References

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diffusion model used in the pyrugosity module, in attempt to reproduce the simulation results in Booth et al. (2017).

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Figure 4. Hillshade map of the 2014 Oso Lanslide region and surface smoothing evolution over 15,000 years predicted by a nonlinear hillslope

X-axis grids (grid size ≈ 3.0 [US survey foot])

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Acknowledgements

X-axis grids (grid size ≈ 3.0 [US survey foot])

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- - Statement of need Topographic complexity, often referred to as topographic roughness or surface roughness, provides critical insights into surface processes and the interactions among the geosphere, biosphere, and hydrosphere. With the increasing availability, utility, and popularity of digital terrain model (DTM) data, quantifying topographic complexity has become an essential measure in terrain analysis across various research fields. This necessity spans applications such as terrain classification and mapping at various spatial scales (Weiss 2001; Robbins 2018; John B. Lindsay,

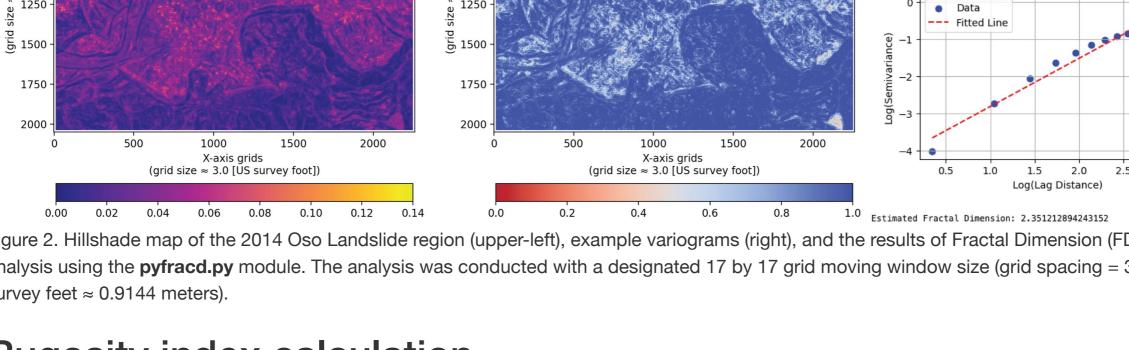
# By bridging the gap between different advanced terrain analytical approaches and incorporating functionality for landscape evolution modeling, pyTopoComplexity serves as a valuable resource for topographic complexity research and has the potential to foster new insights and interdisciplinary collaborations in the fields of geology, geomorphology, geography, ecology, and oceanography.

units and order of magnitude (e.g.,  $10^{-3}$  to  $10^{-4}$  [m<sup>-2</sup>] in Booth et al. (2017) and prior studies;  $10^{-2}$  to  $10^{-3}$  [m<sup>-1</sup>] in LaHusen et al. (2020) thereafter). Despite this discrepency, the C values yielded from these two approaches are linearly scaled and interconvertible, and they both reflect identical spatiotemporal patterns of topographic complexity (i.e., surface roughness). Ososlid2014\_f\_3ftgrid.tif Mexican Hat 15m 2D-CWT Mexican Hat 30m 2D-CWT 250 250

Underwood 2022; Herzig et al. 2023) and ongoing works (Booth and Pétursson 2023; Lai et al. 2023; Ozioko, Booth, and Duvall 2023) of landslide

(2017) (original MATLAB codes available from Booth's personal website). These differences in methatical approach can result C values in different

mapping and age dating studies, with minor differences from the earlier similar research in Booth, Roering, and Perron (2009) and Booth et al.



The **nonlineardiff\_Landlab.ipynb** notebook in the **pyTopoComplexity** package offers a sophisticated tool for simulating landscape evolution

1999). This tool runs the simulation in the **Landlab** environment (version >= 2.7) (Hobley et al. 2017) with the TaylorNonLinearDiffuser module

 $\frac{\partial z}{\partial t} = -\nabla \cdot \mathbf{q}_s$ 

, where  $\mathbf{q}_s$  represents the sediment flux at the surface. The sediment flux is further defined by a nonlinear flux law that is approximated using a

 $\mathbf{q}_{s} = K\mathbf{S} \left[ 1 + \sum_{i=1}^{N} \left( \frac{S}{S_{c}} \right)^{2i} \right]$ 

Here,  $S = -\nabla z$  represents the downslope topographic gradient, and S is its magnitude. The parameter K is a diffusion-like transport coefficient

with dimensions of length squared per time. The simulation also incorporates the critical slope gradient ( $S_c$ ) to ensure numerical stability and

This notebook provides a comprehensive workflow that guides users through setting up, importing raster files, and running simulations. Since Landlab primarily handles DTM data in ESRI ASCII format, this notebook includes utility functions for converting raster files between GeoTIFF

and ESRI ASCII formats. Users are required to specify the values for  $S_c$ , K, the length of each time step in years, and the final time to stop the

simulation. The example included in the notebook uses LiDAR DTM data from the 2014 Oso Landslide (Washington Geological Survey 2023), with

prevent the numerical instability when  $S = S_c$ . N denotes the number of terms in the Taylor expansion, while i specifies the number of

additional terms included. If N=0, the expression simplifies to linear diffusion (Culling 1963). The default is set to N=2 that gives the

behavior described in Ganti, Passalacqua, and Foufoula-Georgiou (2012) as an approximation of the nonlinear diffusion.

from the terrainBento Python package (Barnhart et al. 2019). The main simulation iteratively applies the nonlinear diffusion model to predict

through nonlinear diffusion processes due to near-surface soil disturbances and downslope sediment creep (Roering, Kirchner, and Dietrich

## Y-axis grids (grid size ≈ 3.0 [US survey fo 1.075 1.07 1.311 1.313 1.314 1.315 1.316 1.311 1.313 1.314 1.315 1.313 1.314 1.316 1.316 X-axis grids (grid size ≈ 3.0 [US survey foot]) X-axis grids (grid size ≈ 3.0 [US survey foot]) X-axis grids (grid size ≈ 3.0 [US survey foot]) 1e6 Ososlid2014\_f\_3ftgrid Ososlid2014\_f\_3ftgrid Ososlid2014\_f\_3ftgrid Time: 5000 years ( $K = 0.0029 \text{ m}^2/\text{yr}$ ) Time: 12000 years (K = 0.0029 m<sup>2</sup>/yr) Time: 15000 years ( $K = 0.0029 \text{ m}^2/\text{yr}$ ) 1.080 Yaxis grids (grid size ≈ 3.0 [US survey foot]) 1.00 Yaxis grids = 3.0 [US survey foot]) ≈ 3.0 [US survey foot])

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- - wavelet transform (2D-CWT) with a Mexican Hat wavelet Conducts fractal dimension FracD Wen and Sinding-Larsen (1997); pyfracd.py

  - Compo 1998). When s is large,  $\psi$  is spread out, capturing long-wavelength features of z; when s is small,  $\psi$  becomes more localized, making it

compute the wavelet scale s based on the grid spacing ( $\Delta$ ) of the input raster file (Figure 1).

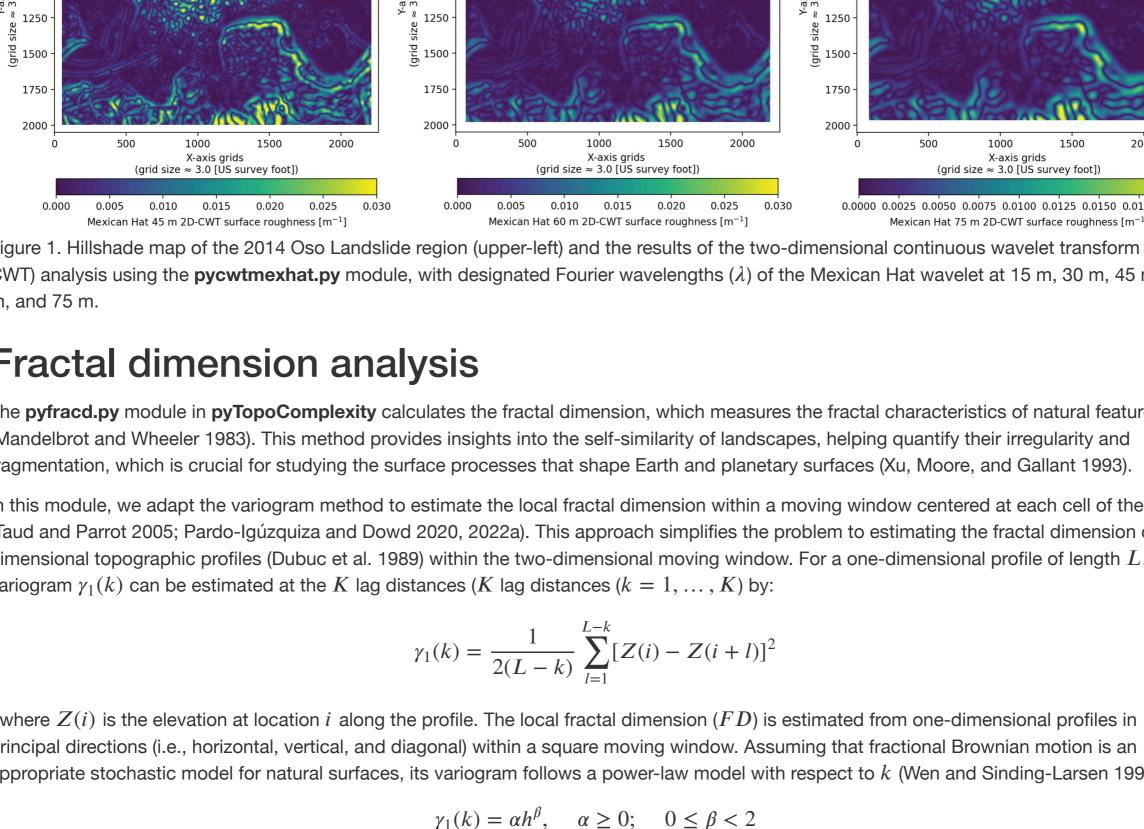
X-axis grids

(grid size ≈ 3.0 [US survey foot])

Mexican Hat 45m 2D-CWT

## Y-axis grids $e \approx 3.0 \text{ [US survey foot]})$ 0521 0000 0251 0000 Y-axis grids ≈ 3.0 [US survey foot]) 000 120 000 000 500 · 750 ·

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 $FD = TD + 1 - \frac{\beta}{2}$ 

, where TD is the topological dimension in the Euclidean space of the fractional Brownian motion. For one-dimensional fractional Brownian

motion, TD = 1; thus, the fractal dimension of the two-dimensional surface  $(FD)_2^*$  can be estimated as the average fractal dimension of the

 $(FD)_2^* = 1 + (FD)_1^*$ 

Users can specify the size (number of grids along each edge) of the moving window to study fractal characteristics at desired spatial scales. In

250

500

(grid size ≈ 3.0 [US survey foot])

2.8