

# Allometry und Biomass



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# What is Allometry?



Allometry is about measuring and comparing relationships between the dimension (body size) and their relationship to various biological quantities (source: Wikipedia)

$$y = a \cdot x^b \quad \text{Allometry equation}$$

is based on the differential equation

$$\frac{dy}{y} = b \cdot \frac{dx}{x}$$

Otto Snell, Göttingen



Photo Wikipedia

# Allometry for biomass determination



## Application:

Allometries can be used to estimate the biomass (total AGB or biomass components) from easily measurable tree sizes (usually BHD and height).

$$BM = a \cdot DBH^b$$

Classic nonlinear equation

$$\ln(BM) = a_0 + b \cdot \ln(DBH)$$

Ln-transformed linear equation

**Advantage:** can be parameterized with linear regression  
Heteroscedasticity solved

**Disadvantage:** Must be corrected with variance in back-transformation must be corrected

If uniform stands with similar heights of all trees are used, the BHD is usually sufficient as the only parameter.

# More complex multiple regressions



More complex equations use further independent variables

$$\mathbf{BM} = \mathbf{a} \cdot \mathbf{DBH}^b \cdot \mathbf{H}^c$$

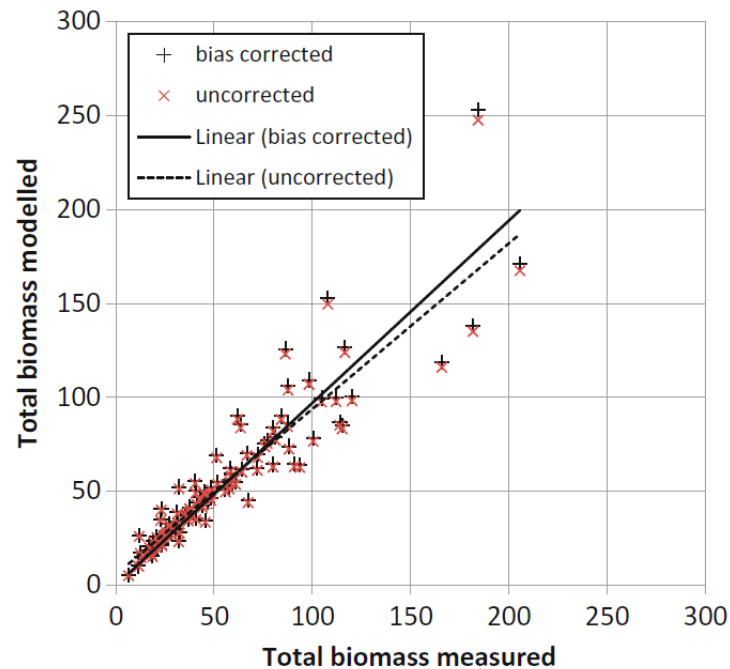
Classic nonlinear equation

$$\ln(\mathbf{BM}) = \mathbf{a}_0 + \mathbf{b} \cdot \ln(\mathbf{DBH}) + \mathbf{c} \cdot \ln(\mathbf{H})$$

Linearised Equation

Advantage: can be parameterized with linear regression  
Disadvantage: Must be bias-corrected with variance in back-transformation

Caution: When using ln-transformed estimates, a bias correction is necessary! back-transformation correction (bias correction) is necessary!



Seifert and Seifert 2014

$$\ln(\text{AGB}_{\text{total}}) = a + b \ln(D^2H) + c \ln(H)$$

$$\text{AGB}_{\text{total}} = e^{(a + b \ln(D^2H) + c \ln(H) + \text{Varianz } 0.5)}$$

## Additivity

If there are several biomass components, the sums of the BM component models should equal the sum of the total biomass

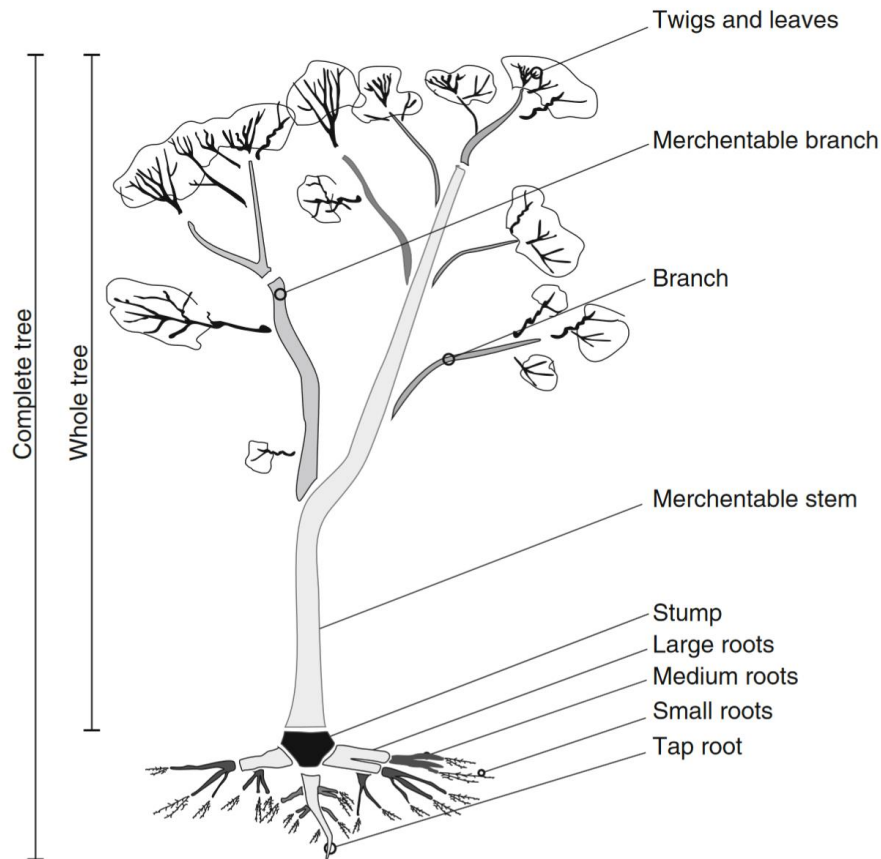
Multivariate regressions:

Dirichlet regression (Schindler et al. 2023)

Seemingly unrelated regression (Vonderach et al 2019)

Proportionality estimation with the Aitchison copmplex (Seifrt & Seifert 2014).

# Biomassekomponenten



Seifert und Seifert (2014)

## Why biomass components?

- Biological statements about Allocation distribution
- Nutrient removals with the timber harvest
- Biomass production for thermal utilization



# How to determine above ground dry mass?



## I. Bulk method

1. Chip felled tree
2. Mix chips and weigh chips fresh
3. Dry sample of chips
4. Determine dry weight / fresh weight proportion
5. Scale up to the tree



Bundler, Foto Block

### Remember

About 10-15 % branch/needle biomass remains in the stand and cannot be harvested without big effort



# I. Bulk method



## Advantage

- Delivers accurate estimations
- Fast and cheap for whole stands (biomass plantations)

## Disadvantage

- not feasible at single tree level (mechanical losses)
- not able to split biomass in fractions within a tree (e.g. needles, bark, stemwood, branches, etc.)

# How to determine above ground dry mass?



## II. Sampling method with full fresh weight record

1. Fell tree
2. Determine fresh weight of tree partitions:  
stem+bark, branch+needles
3. Sample partitions
4. Dry samples
5. Determine dry weight / fresh weight proportion
6. Scale up to the tree



Bundler, Foto Schuck

## II Sampling method full fresh weight record



Fresh stem weight with bark



Fresh branch and needle weight

## II Sampling method full fresh weight record



### **Advantage**

- Delivers accurate estimations
- Allows for differentiation of tree partitions

### **Disadvantage**

- Only feasible for smaller trees
- Bark and wood as well as branches and needles cannot be separated easily



# III. Sampling method with a regression approach

## Step 1: Sampling

1. Fell tree

stem

branch

1. Cut stem discs
2. Measure green volume (with and without bark)
3. Dry discs
4. Determine basic density

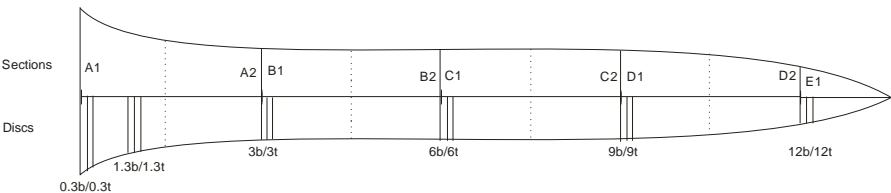
1. Measure branches in height and diameter at the stem
2. Sample branches for fresh weight (wood, bark, needles)
3. Dry branch samples and determine proportion for fresh / dry weight for wood, bark, needles separately



# III. Sampling method with a regression approach

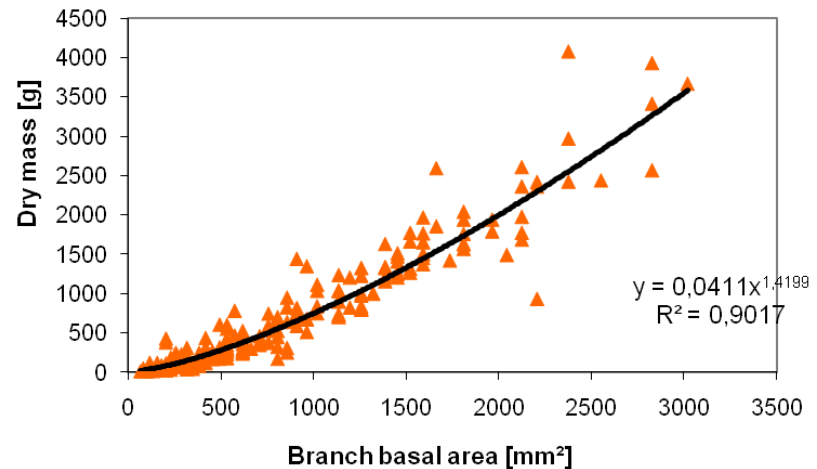


## III. Compartment method based on regression



Biomass=Volume·Basic Density

$$BM = V \cdot R$$



### Step 2: Upscaling

1. Reconstruct stem and bark volume from discs to scale up
2. Model basic density along stem
3. Multiply density with volume

Allometric models  $\ln(BM_{leaf}) = a + b \cdot \ln(bba)$

4. develop allometric models that relate biomass (wood, bark, needles) to branch area or diameter
5. Use model for each branch diameter of the tree to scale up to tree level

# III. Sampling method with a regression approach



## Step 1: Sampling

1. Fell tree

stem

branch

1. Cut stem discs
2. Measure green volume (with and without bark)
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1. Measure branches in height and diameter at the stem
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## Step 2: Upscaling

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5. Use model for each branch diameter of the tree to scale up to tree level

Here we are at tree level



# What is Biomass?



Biomasse von Holz = Volumen · Basic density

Unitzs

kg

m<sup>3</sup>

kg/m<sup>3</sup>

Example:

**Biomasse:**

A tree species has a basic density of 420 kg/m<sup>3</sup> and we want to determine  
How much biomass 2 fm (m<sup>3</sup>) wood of this species have.

$$420 \text{ kg/m}^3 \cdot 2 \text{ m}^3 = 840 \text{ kg}$$

# How much carbon is in a tree?



$$\text{Carbon} = \text{Biomass} \cdot 0.5$$

Units

kg

kg

## Example Calculation:

Biomass:

A tree species has a basic density of 420 kg/m<sup>3</sup>, and we want to determine how much biomass (weight) 2 solid cubic meters (fm) of this tree species contain.

$$420 \text{ kg/m}^3 \cdot 2 \text{ m}^3 = 840 \text{ kg}$$

Carbon Content:

$$840 \text{ kg} \cdot 0.5 = 420 \text{ kg C}$$

# How are the carbon dioxide equivalents calculated (CO<sub>2</sub>e)?



$$\text{CO}_2 = \text{Carbon} \cdot 3.67$$

Einheiten      kg                              kg

## Example

A tree species has a basic density of 420 kg/m<sup>3</sup> and we would like to know the C content  
420 kg/m<sup>3</sup> · 2 m<sup>3</sup> = 840 kg

**Carbont:** 840 kg · 0,5 = 420 kg (C)

**CO<sub>2</sub>** = Kohlenstoff · 3,67 = 420 kg (C) · 3,67 = 1541,4 kg(CO<sub>2</sub>)

# How to calculate C->CO<sub>2</sub>



Reacztion equation:  $C + O_2 \rightarrow CO_2$

1) From 1 Mol(CO<sub>2</sub>) we will lget 1 Mol(C) entsteht

2) Basic equation

$$m = M \cdot n$$

Mass = molare Mass · Anount

The molar Masse of C ist  $M(C) = 12 \text{ g/mol}$

$$n(C) = m(C) / M(C) = 1000 \text{ g} / 12 \text{ g/mol} = 83,333 \text{ mol}$$

Im Periodensystem

12,0 6C	16,0 8O
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3) Molar Mass of a CO<sub>2</sub> Molecule is calculated the following way:

C: 12, O<sub>2</sub>: 16, CO<sub>2</sub> a mucle consists of 1 C and 2 O

equals  $M(CO_2) = 12 + 16 + 16 = 44 \text{ g/mol}$

4) Jetzt Gleichung 2 und 3 zusammenführen und lösen

$$m(\text{Kohlenstoffdioxid}) = n(CO_2) \cdot M(CO_2) = 83,333 \text{ mol} \cdot 44 \text{ g/mol} = 3666,66 \text{ g} = \mathbf{3,67 \text{ kg}}$$

**Ergebnis:** 1 kg Kohlenstoff im Holz entspricht 3,67 kg Kohlendioxi

# Carbon in forests stands



## C in Forest stands

AGB + BGB + NM + litter+ SOC

**AGB** Above Ground biomass

**BGB** below ground biomass

**NM** necromass

**Litter**

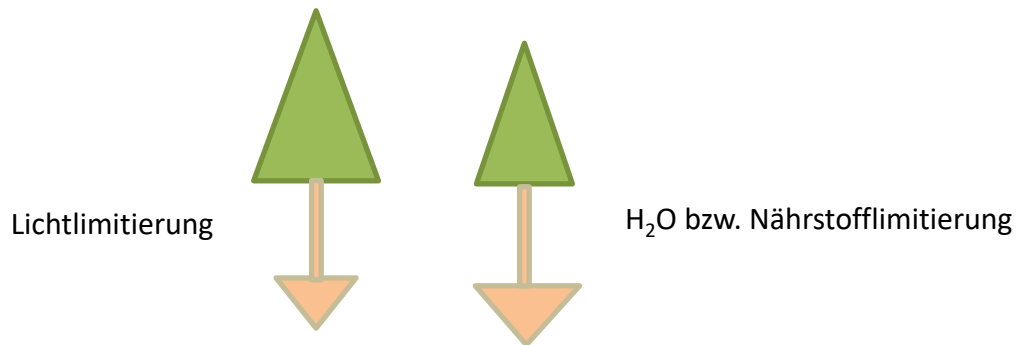
**SOC** Soil organic carbon

# AGB vs BGB



Die Datenlage bei unterirdischer Biomasse ist schlecht

On average 25% of the tree biomass is BGB



Influence of H<sub>2</sub>O und Nutrient on Proportions of AGB and BGB

# Wieviel Holz kommt denn aus dem Wald?



Erntefestmeter = Vorratsfestmeter · 0,8

**Standing Volume (Vfm)** is usually measured with bark included. It refers to coarse wood (>7 cm in diameter). This is used to describe the stock of standing wood in the forest, and the harvest rate is also expressed in terms of Vfm.

**Harvest Volume (Efm)** is used when wood is harvested. Depending on the tree species, it typically involves a deduction of about 10% for bark and 10% for harvesting losses. Species-specific conversion factors are available for this.

"Diameter under bark." means that the bark deduction has already been applied (coarse wood without bark).

Even during the harvesting of branches and limb material, about 15–20% usually remains in the forest as harvesting losses.



# How much wood is used for structural purposes?

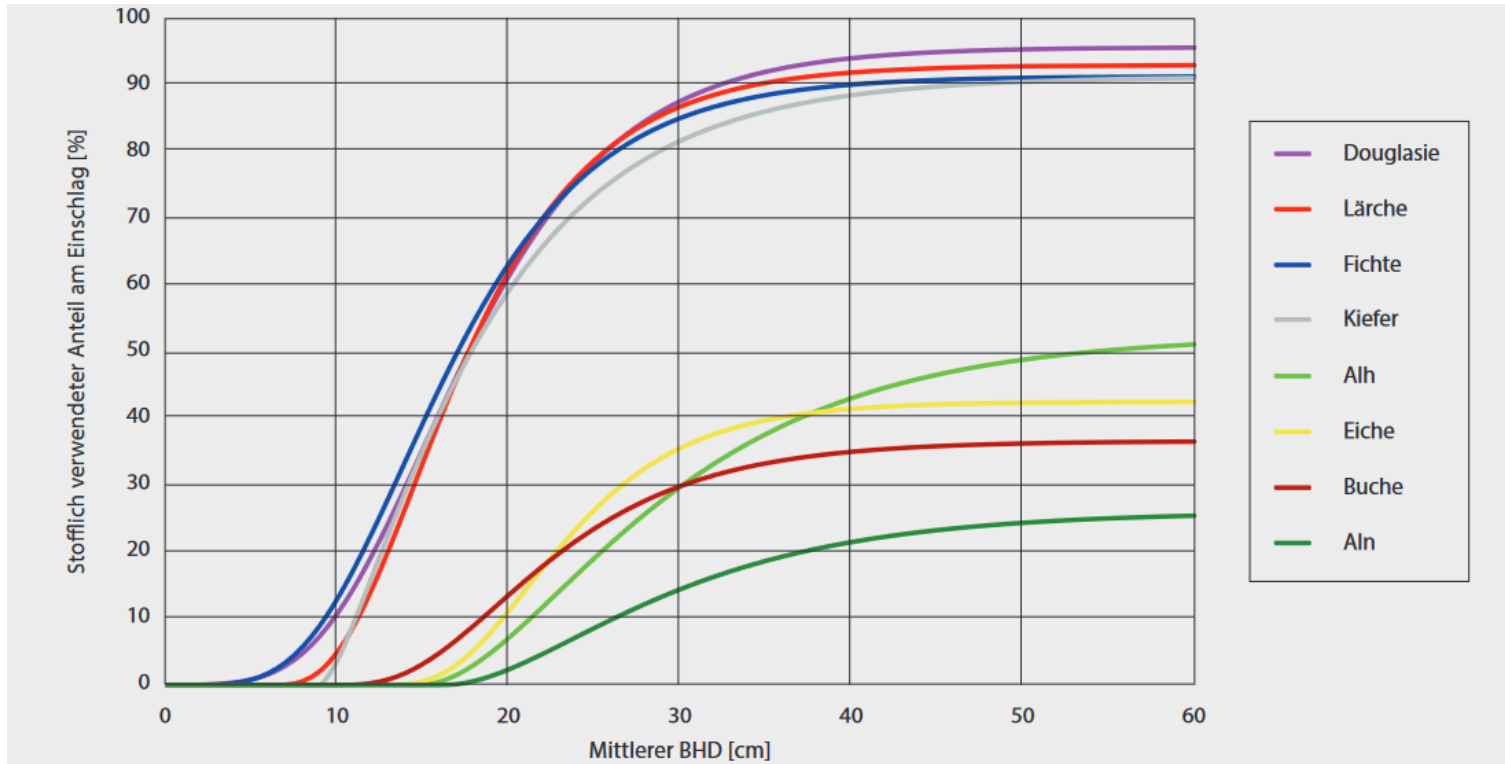


Abbildung 3

Anteil der stofflichen Verwendung in Abhängigkeit des mittleren BHD getrennt nach Baumartengruppen

# How much sawing residues are lost from roundwood in Sawmills?



About 50%

Typically used for energy production for the sawmill or as pellets.