

POSGRADO EN CIENCIA E INGENIERÍA DE LA COMPUTACIÓN
Universidad Nacional Autónoma de México

APRENDIZAJE AUTOMÁTICO

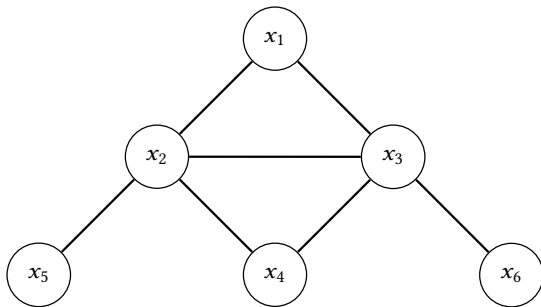
MGP: moralización.

Ayudantes: Bere y Ricardo

Mayo, 2021

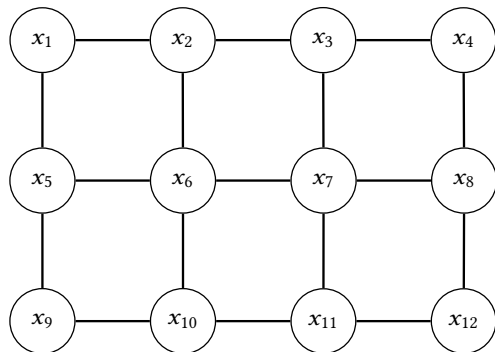
Redes de Markov (RM)

- Gráfica no dirigida que expresa una distribución de probabilidad conjunta.



$$P(x_1, x_2, x_3, x_4, x_5, x_6) = \frac{1}{Z} \psi(x_1, x_2, x_3) \psi(x_2, x_3, x_4) \psi(x_2, x_5) \psi(x_3, x_6)$$

Independencia en redes de Markov



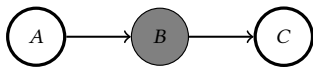
$$x_1 \perp\!\!\!\perp x_3 \mid x_2, x_5$$

$$x_1 \perp\!\!\!\perp x_7 \mid x_3, x_6, x_{10}$$

$$x_9 \perp\!\!\!\perp x_{12} \mid x_2, x_7, x_{10}$$

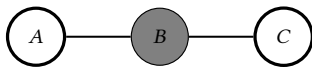
RB a RM: cadena causal

Red bayesiana



$$A \perp\!\!\!\perp C \mid B$$

Red de Markov

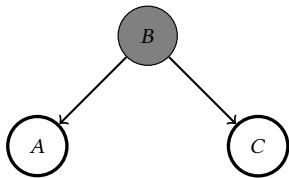


$$A \perp\!\!\!\perp C \mid B$$

RB a RM: causa común

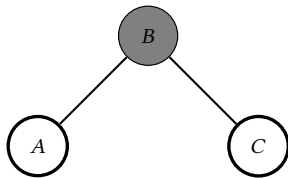
Red bayesiana

Causa común



$$A \perp\!\!\!\perp C \mid B$$

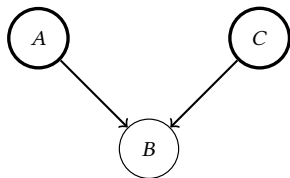
Red de Markov



$$A \perp\!\!\!\perp C \mid B$$

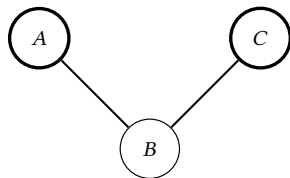
RB a RM: efecto común

Red bayesiana



$$A \perp\!\!\!\perp C \mid$$

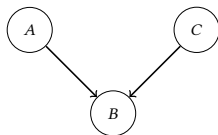
Red de Markov



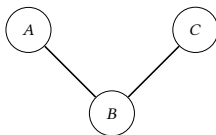
$$A \not\perp\!\!\!\perp C \mid$$

RB a RM: moralización

Red bayesiana

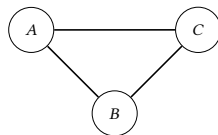


Red de Markov



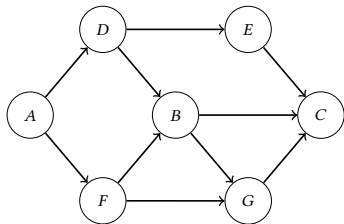
Conversión
incorrecta

Moralización

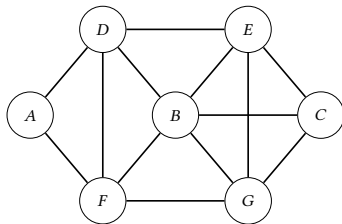


- Si en una RB dos vertices A y B son padres de C entonces estos se conectan.

Ejemplo: RB a RM



Red bayesiana



Red de markov

¿Qué independencias condicionales se pierden?