

# CMPS 130

## Homework 2

## Textbook Exercises

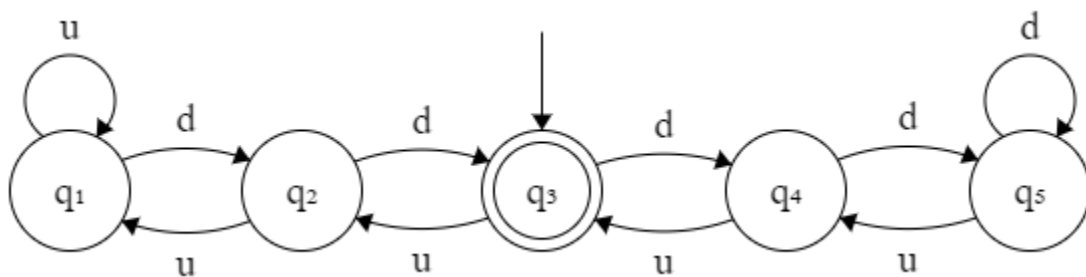
1.1

	$M_1$	$M_2$
a.	$q_1$	$q_1$
b.	$\{q_2\}$	$\{q_1, q_4\}$
c.	$q_1, q_2, q_3, q_1, q_1$	$q_1, q_1, q_1, q_2, q_4$
d.	No	Yes
e.	No	Yes

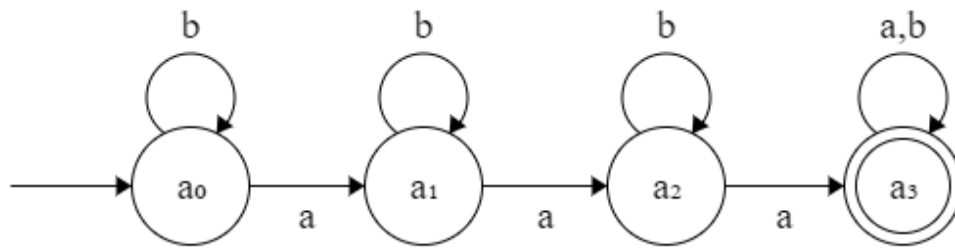
1.2

	$M_1 = (Q, \Sigma, \delta, s, F)$	$M_2 = (Q, \Sigma, \delta, s, F)$																											
$Q$	$\{q_1, q_2, q_3\}$	$\{q_1, q_2, q_3, q_4\}$																											
$\Sigma$	$\{a, b\}$	$\{a, b\}$																											
$\delta$	<table border="1"> <tr> <th></th><th>a</th><th>b</th></tr> <tr> <th><math>q_1</math></th><td><math>q_2</math></td><td><math>q_1</math></td></tr> <tr> <th><math>q_2</math></th><td><math>q_3</math></td><td><math>q_3</math></td></tr> <tr> <th><math>q_3</math></th><td><math>q_2</math></td><td><math>q_1</math></td></tr> </table>		a	b	$q_1$	$q_2$	$q_1$	$q_2$	$q_3$	$q_3$	$q_3$	$q_2$	$q_1$	<table border="1"> <tr> <th></th><th>a</th><th>b</th></tr> <tr> <th><math>q_1</math></th><td><math>q_1</math></td><td><math>q_2</math></td></tr> <tr> <th><math>q_2</math></th><td><math>q_3</math></td><td><math>q_4</math></td></tr> <tr> <th><math>q_3</math></th><td><math>q_2</math></td><td><math>q_1</math></td></tr> <tr> <th><math>q_4</math></th><td><math>q_3</math></td><td><math>q_4</math></td></tr> </table>		a	b	$q_1$	$q_1$	$q_2$	$q_2$	$q_3$	$q_4$	$q_3$	$q_2$	$q_1$	$q_4$	$q_3$	$q_4$
	a	b																											
$q_1$	$q_2$	$q_1$																											
$q_2$	$q_3$	$q_3$																											
$q_3$	$q_2$	$q_1$																											
	a	b																											
$q_1$	$q_1$	$q_2$																											
$q_2$	$q_3$	$q_4$																											
$q_3$	$q_2$	$q_1$																											
$q_4$	$q_3$	$q_4$																											
$s$	$q_1$	$q_1$																											
$F$	$\{q_2\}$	$\{q_1, q_4\}$																											

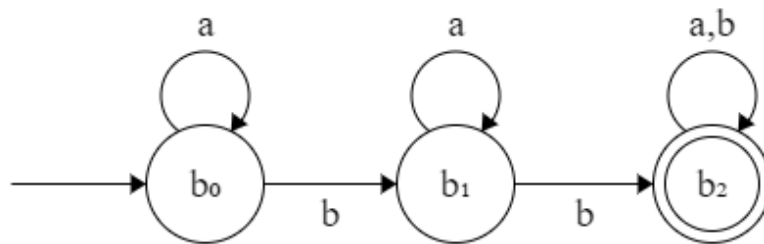
1.3



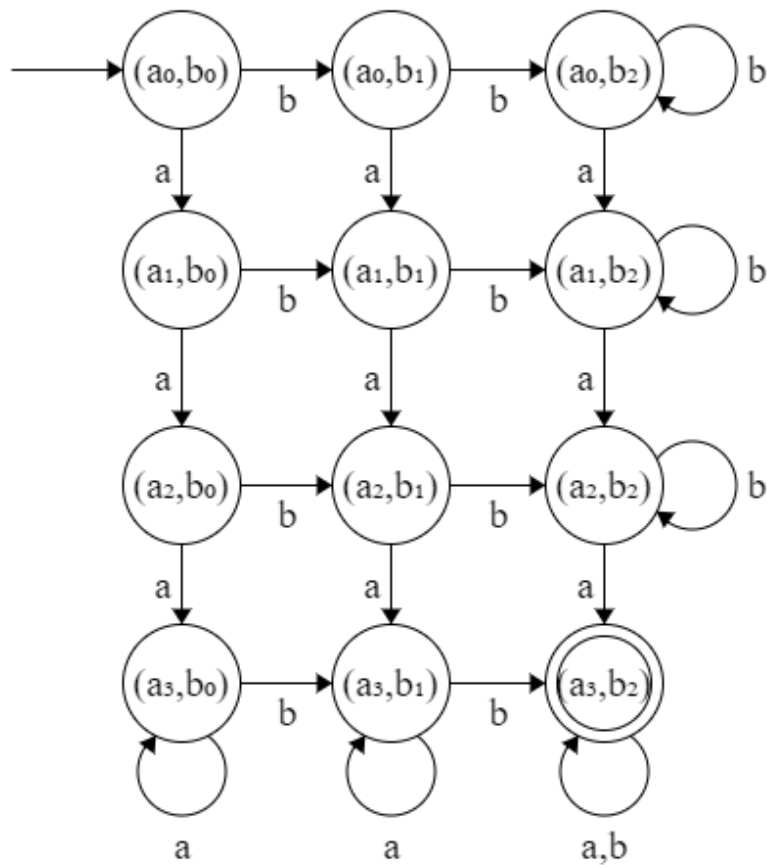
1.4 a.  $\{w \mid w \text{ has at least 3 a's}\}$



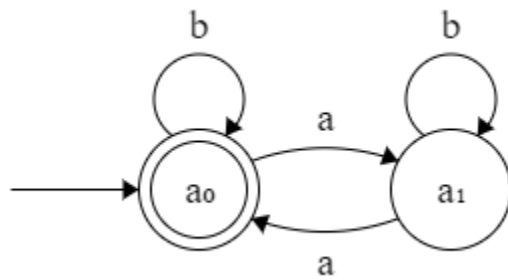
$\{w \mid w \text{ has at least 2 b's}\}$



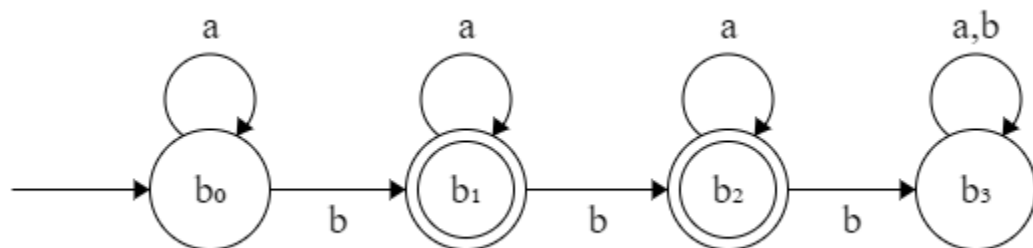
$\{w \mid w \text{ has at least 3 a's and 2 b's}\}$



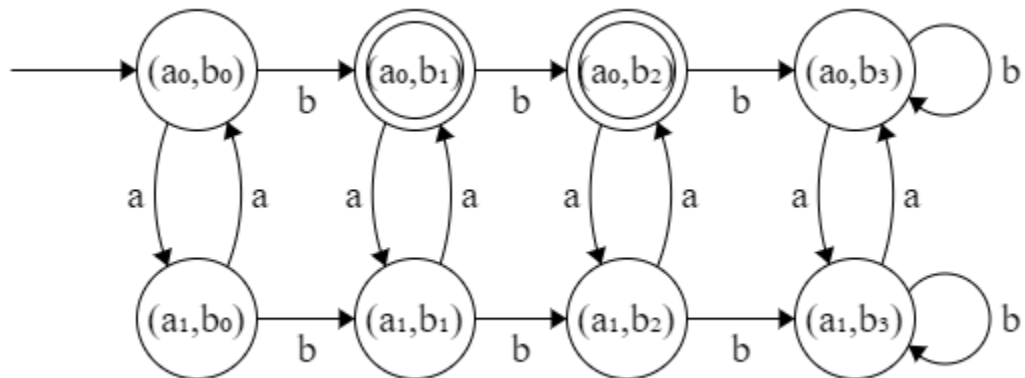
1.4c.  $\{w \mid w \text{ has an even number of } a\text{'s}\}$



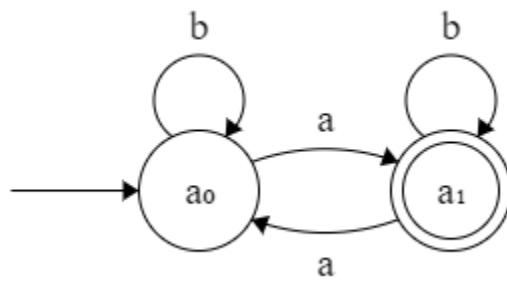
$\{w \mid w \text{ has 1 or 2 } b\text{'s}\}$



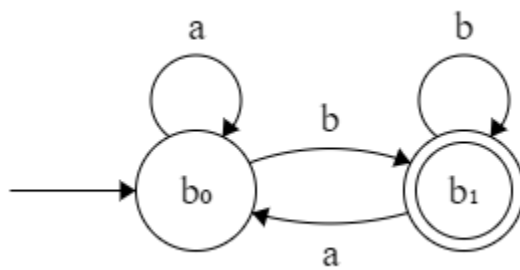
$\{w \mid w \text{ has an even number of } a\text{'s and 1 or 2 } b\text{'s}\}$



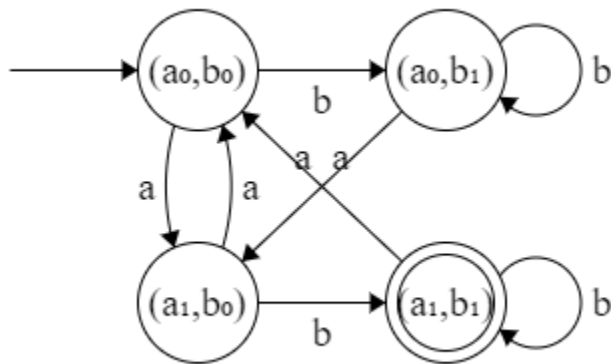
1.4f.  $\{w \mid w \text{ has an odd number of } a\text{'s}\}$



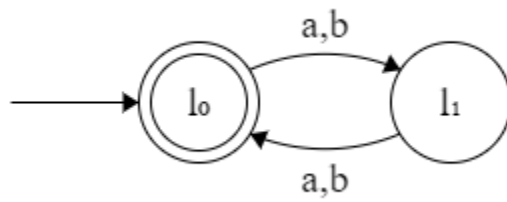
$\{w \mid w \text{ ends with a } b\}$



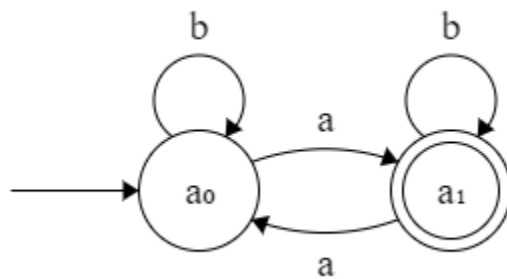
$\{w \mid w \text{ has an odd number of } a\text{'s and ends with a } b\}$



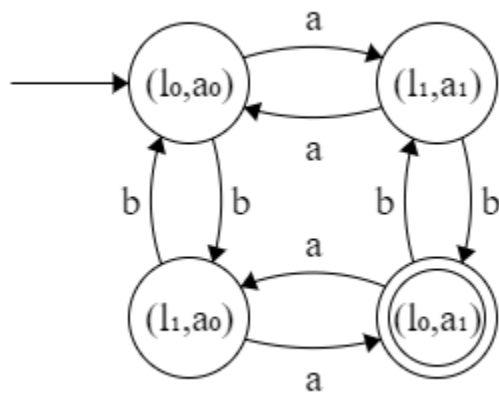
1.4 g.  $\{w \mid w \text{ has an even length}\}$



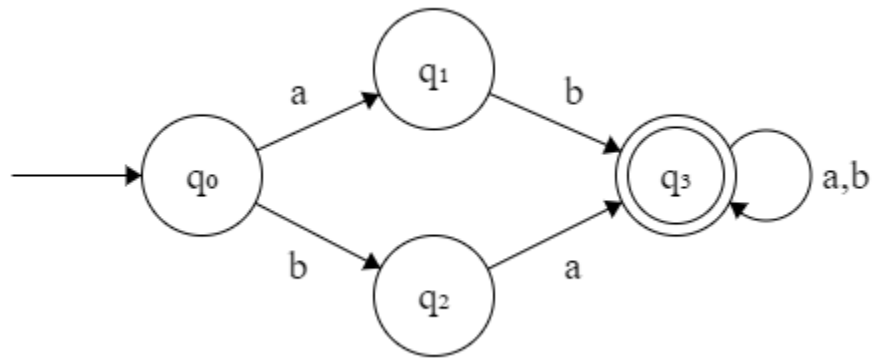
$\{w \mid w \text{ has an odd number of a's}\}$



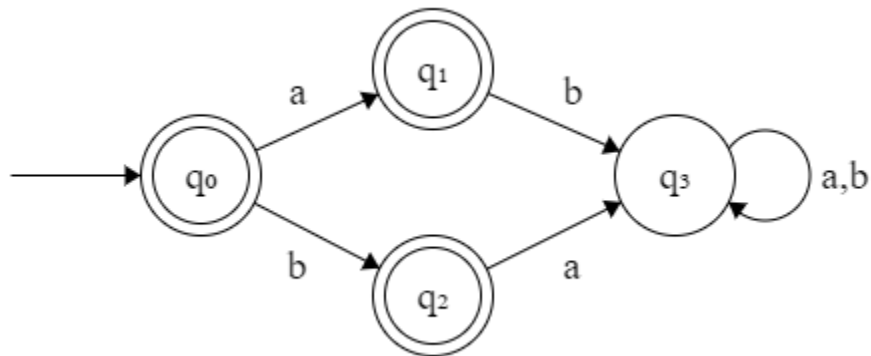
$\{w \mid w \text{ has an even length and an odd number of a's}\}$



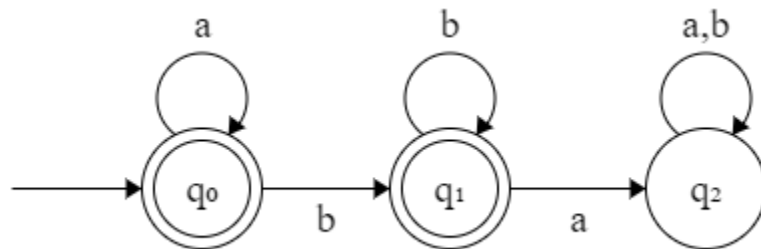
1.5 c.  $\{w \mid w \text{ contains the substrings } ab \text{ or } ba\}$



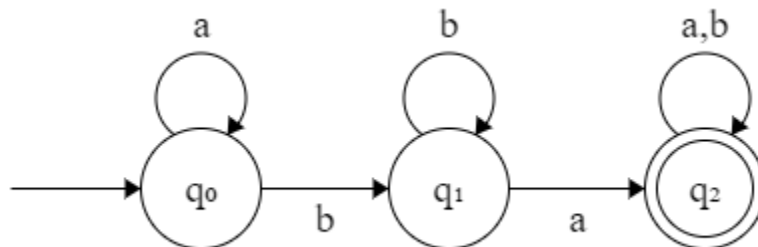
$\{w \mid w \text{ contains neither the substrings } ab \text{ nor } ba\}$



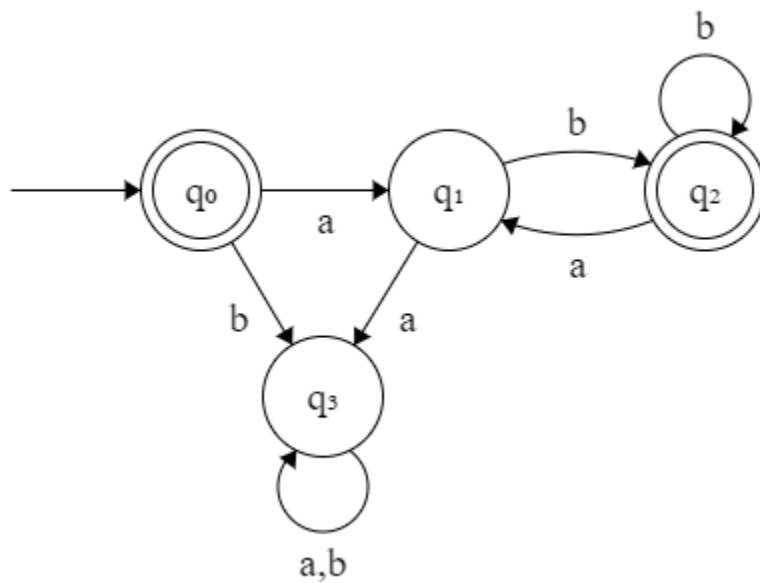
1.5 d.  $\{w \mid w \text{ is any string in } a^*b^*\}$



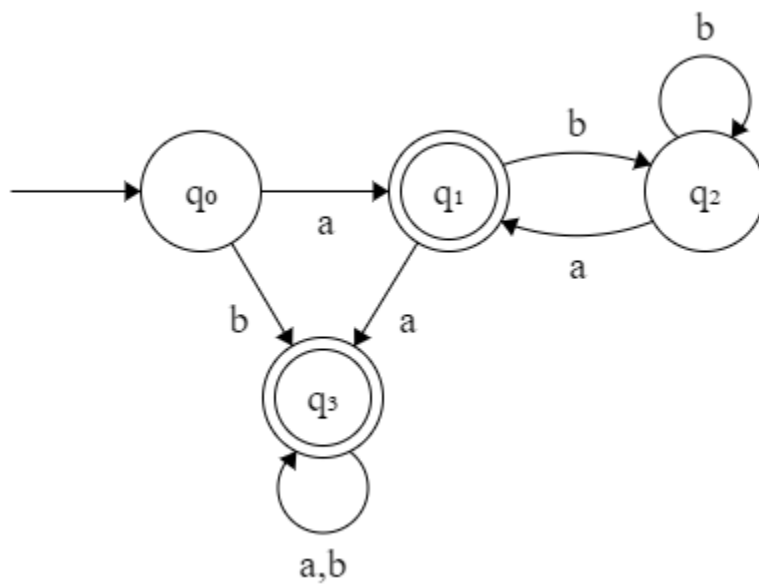
$\{w \mid w \text{ is any string not in } a^*b^*\}$



1.5 e.  $\{w \mid w \text{ is any string in } (ab^+)^*\}$

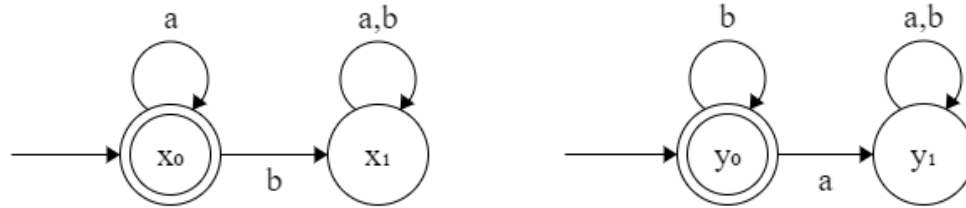


$\{w \mid w \text{ is any string not in } (ab^+)^*\}$

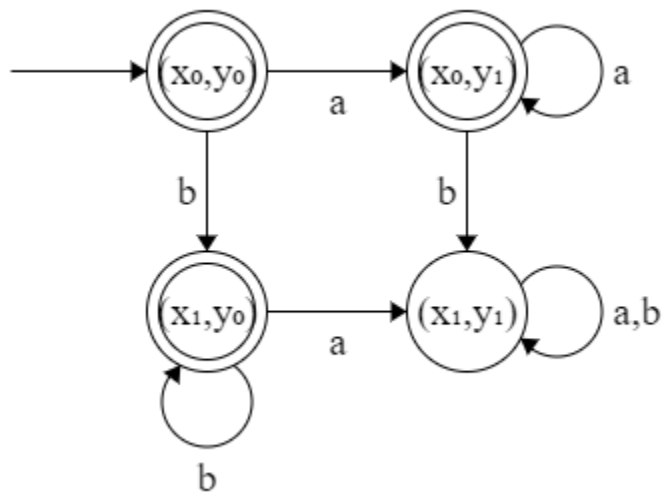




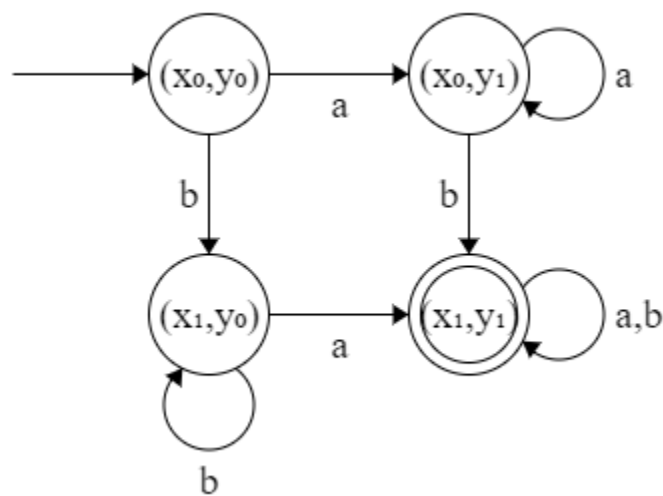
1.5f.  $\{w \mid w \text{ is any string in } a^*\}$        $\{w \mid w \text{ is any string in } b^*\}$



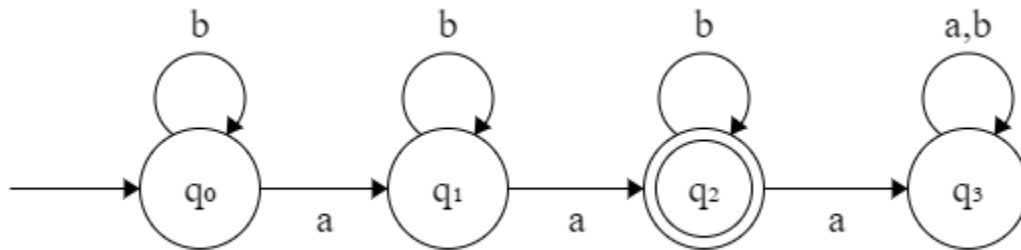
$\{w \mid w \text{ is any string in } a^* \cup b^*\}$



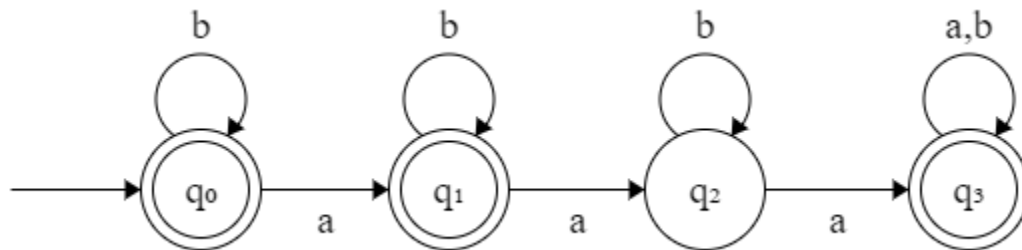
$\{w \mid w \text{ is any string not in } a^* \cup b^*\}$



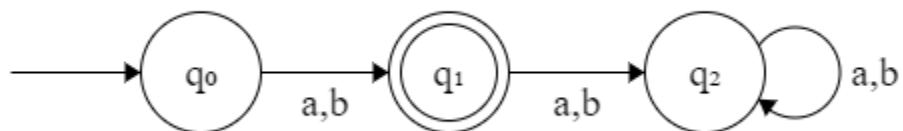
1.5g.  $\{w \mid w \text{ is any string that contains exactly two } a\text{'s}\}$



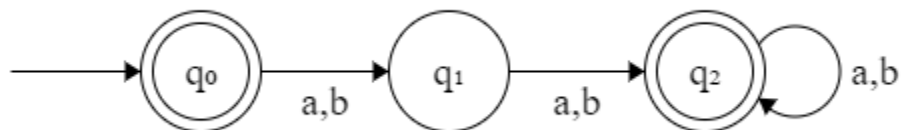
$\{w \mid w \text{ is any string that doesn't contain exactly two } a\text{'s}\}$



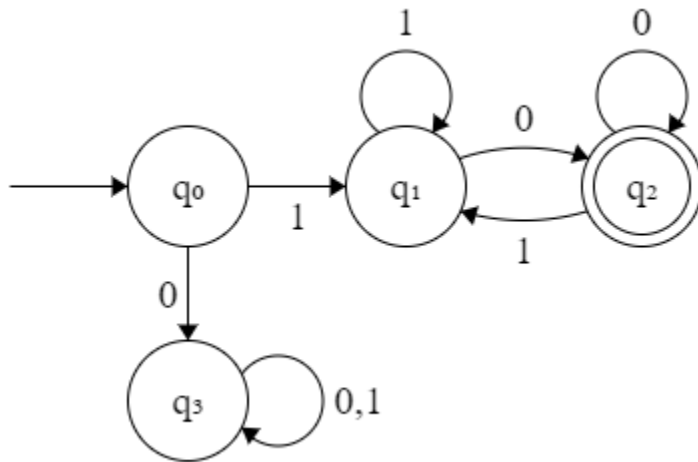
1.5h.  $\{w \mid w \text{ is } a \text{ or } b\}$



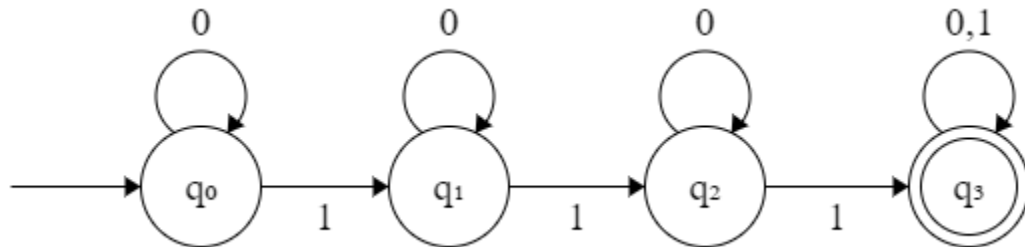
$\{w \mid w \text{ is any string except } a \text{ and } b\}$



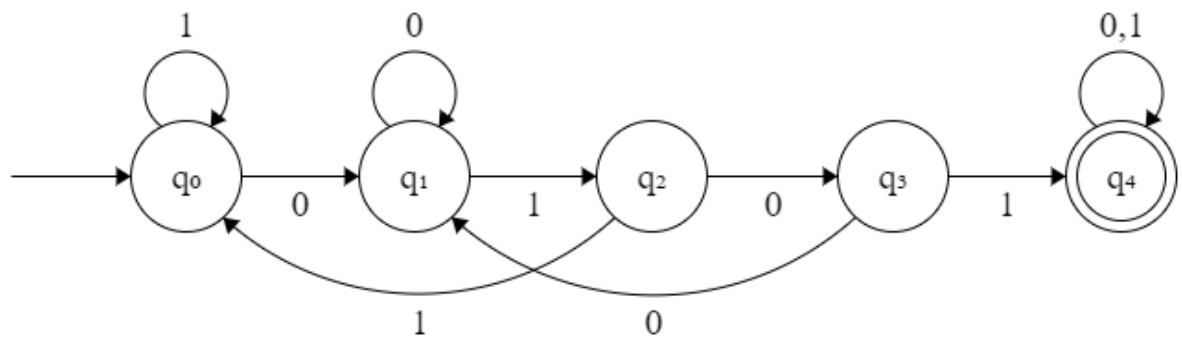
1.6a.  $\{w \mid w \text{ begins with a 1 and ends with a 0}\}$



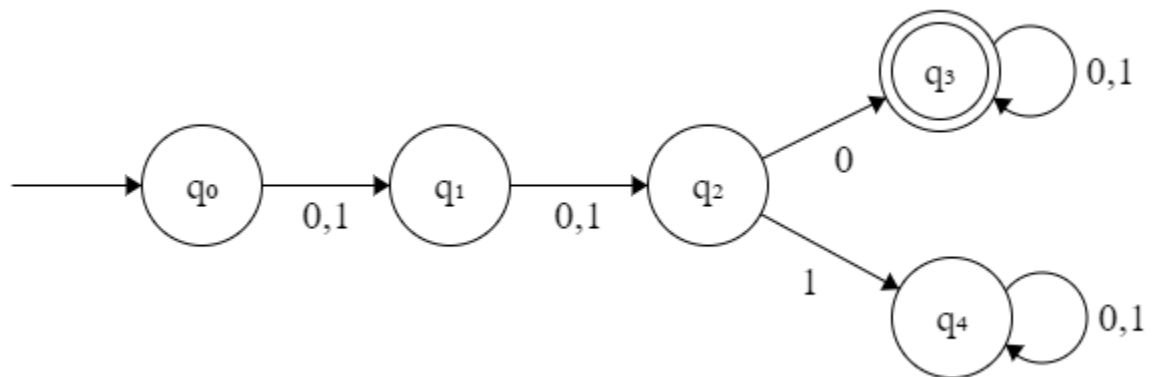
1.6b.  $\{w \mid w \text{ contains at least three 1s}\}$



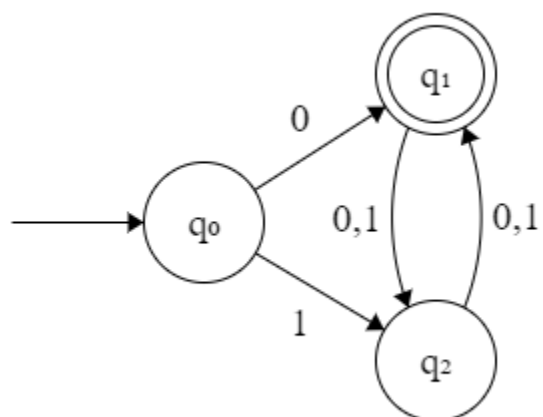
1.6c.  $\{w \mid w \text{ contains the substring 0101}\}$



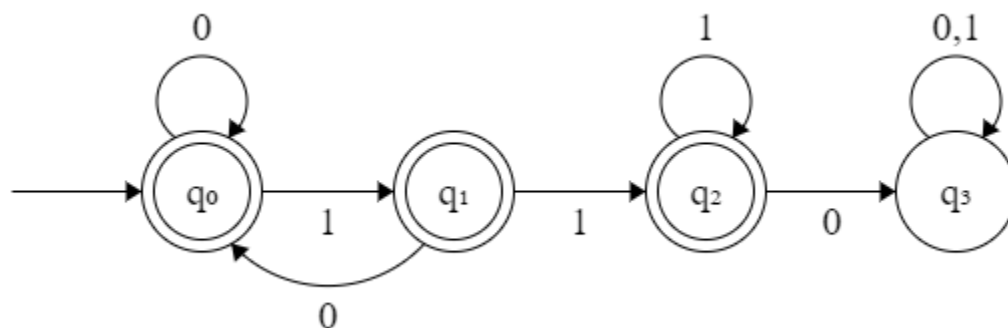
1.6d.  $\{w \mid w \text{ has length at least 3 and its third symbol is a 0}\}$



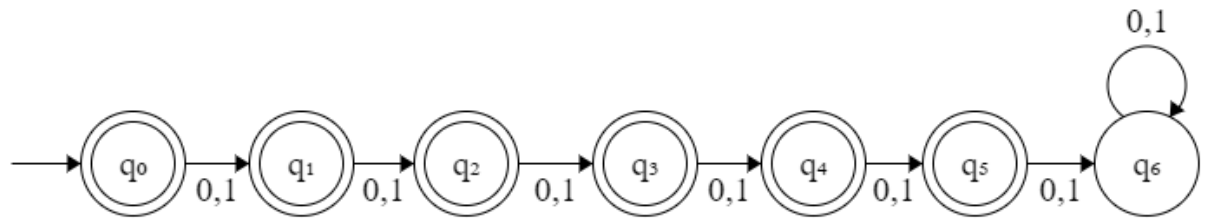
1.6e.  $\{w \mid w \text{ starts with 0 and has odd length, or starts with 1 and has even length}\}$



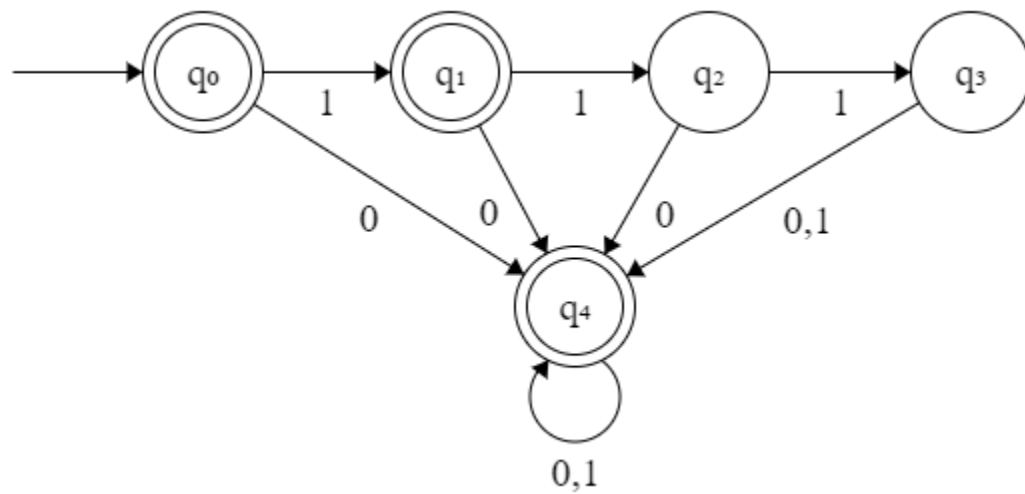
1.6f.  $\{w \mid w \text{ doesn't contain the substring 110}\}$



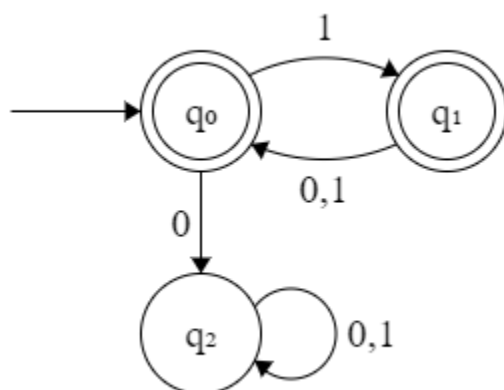
1.6g.  $\{w \mid \text{the length of } w \text{ is at most } 5\}$



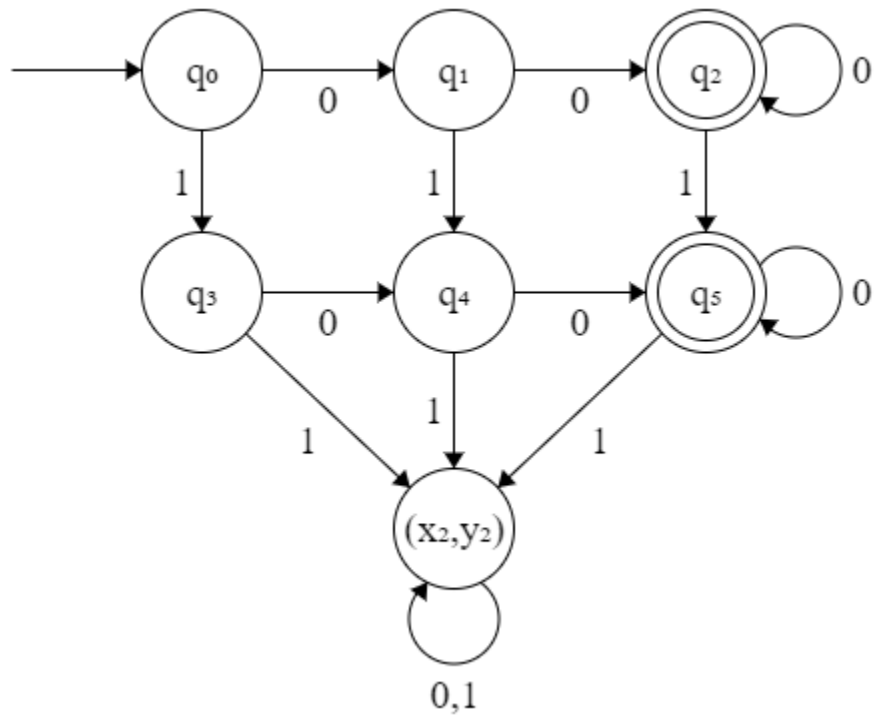
1.6h.  $\{w \mid w \text{ is any string except } 11 \text{ and } 111\}$



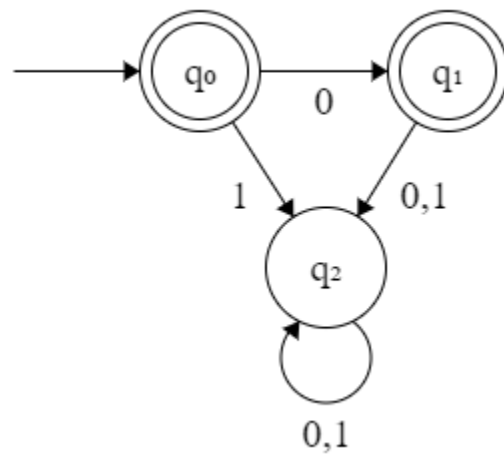
1.6i.  $\{w \mid \text{every odd position of } w \text{ is a } 1\}$



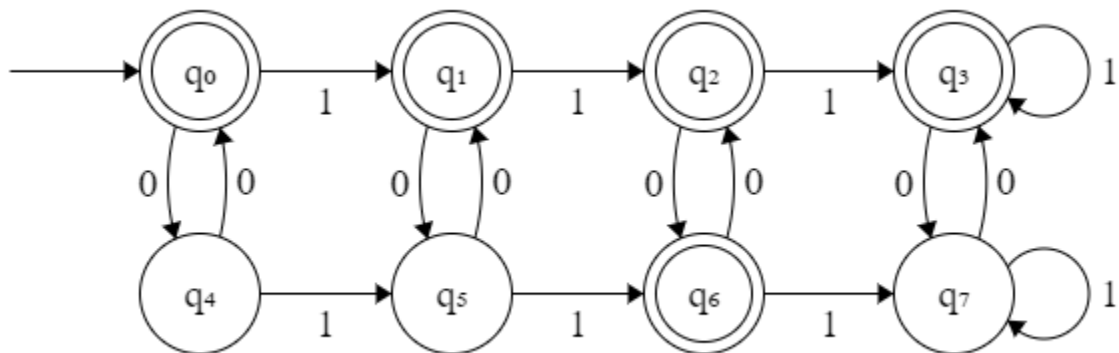
1.6j.  $\{w \mid w \text{ contains at least two 0s and at most one 1}\}$



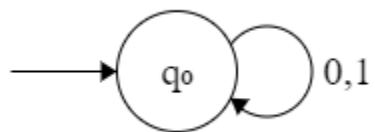
1.6k.  $\{\epsilon, 0\}$



1.6l.  $\{w \mid w \text{ contains an even number of 0s, or contains exactly two 1s}\}$



1.6m. The empty set



1.6n. All strings except the empty string

