# Technical university of Liberec

# Faculty of mechatronics, informatics and interdisciplinary studies

# FLOW123D

version 1.6.0

Documentation of file formats and brief user manual.

# Liberec, 2010

**Acknowledgement.** This work was realized under the state subsidy of the Czech Republic within the research and development project "Advanced Remediation Technologies and Processes Center" 1M0554 – Program of Research Centers PP2-D01 supported by Ministry of Education.

### Flow123D

### Introduction

Flow123D is a software for simulation of water flow, solute transport and sorption in a heterogenous porous and fractured medium. In particular it is suited for simulation of underground processes in a granite rock masive. The program is able to describe explicitely processes in 3D medium, 2D fractures, and 1D chanels and exchange between those dimensions. The computational mesh is therefore collection of 3D tetrahedrons, 2D trinagles and 1D line segments.

The water flow model assumes a saturated medium described by Darcy law. For discretization we use mixed hybrid FEM. This version allows only calculation of steady water flow.

The solute transport model can deal with several dissolved substances. It contains non-equilibrium dual porosity model, i.e. exchange between mobile and immobile pores. There is also model for several types of sorption in both the mobile and immobile zone. The imlemented sorption models are linear sorption, Freundlich isotherm and Langmuir isotherm. The solute transport model uses finite volume discretization with upwinding in space and explicit Euler discretization in time. The dual porosity and the sorption are introduced into transport by operator spliting. The dual porosity model use analytic solution and the non-linear adsorption is solved numerically by the Newton method.

The program is implemented in C/C++ using essentially PETSC library for linear algebra. The water flow as well as the transport simulation can be computed in parallel using MPI environment. This version also support output into VTK format, which is widely supported. In particular we recommend Paraview for visualization and postprocessing of the results.

The program is distributed under GNU GPL v. 3 licence and is available on the project web page: http://dev.nti.tul.cz/trac/flow123d

## Usage

On the Linux system the program can be started either directly or through a script run\_flow.sh. When started directly by command

```
> flow123d -s example.ini
```

the program accepts one argument after swith -s which is the name of the principila input file. When you want to start a parallel job you shloud rather use starting script. Basic usage is:

```
> run_flow.sh -np 2 -s example.ini
```

which run simulation on 2 processes using the same INI file as before. For other possible arguments see the beginning of the script.

On the Windows system you can start a squential run by command:

```
> flow123d.exe -s example.ini
```

or a parallel run by command:

```
> mpiexec.exe -np 2 flow123d.exe -s example.ini
```

The principial input file of the program is an INI file which contains names of other necessaryinput files. Those are the file with calculation mesh (\*.msh), the file with specification of neighbourings between dimensions (\*.ngh), the file with material description (\*.mtr) and the file with boundary conditions for the water flow problem (\*.bcd).

In the case of transport simulation one have to specify also the file with transport boundary conditions (\*.tbc) and the file with transport initial condition for individual substances (\*.tic).

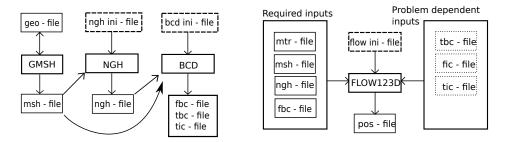


Figure 1: Preparation of input files.

For the preparation of input files we use several utilities (see Figure 1). We usualy begin with a \*.geo file as a description of the domain geomery. This come as an input for the GMSH mesh generator, which produce the mesh file. Then we run program ngh to produce file of neigbourings. Finally we can use program bcd for the preparation of files with boundary and initial conditions. The file with material properties has to be created manualy, preferably by modifying some of the example problems. The programs ngh and bcd are distributed together with flow123d with their own limited documentation.

The output files can be either \*.pos files accepted by the GMSH or one can use VTK format that can be postprocessed by Paraview.

In following sections we briefly describe structure of individual input files.

# Advection-Diffusion equation

Solute transport is governed by advection equation which can be written in the form

$$\frac{\partial c}{\partial t} + \boldsymbol{v} \frac{\partial c}{\partial x} = 0, \tag{1}$$

where c is concentration  $[M^3 \cdot L^{-3}]$ , t is time [T], v is velocity  $[L \cdot T^{-1}]$ , and x is coordinate in cartesian system [L]. Assuming solution which is constant on every element (cell centered finite volume method) and integrating equation (1) we get

$$\int_{e_i} \frac{\partial c}{\partial t} dV + \int_{e_i} \boldsymbol{v} \frac{\partial c}{\partial x} dV = 0.$$

After some rearrangements we obtain on *i*-th element  $(e_i)$ 

$$\frac{\partial c_i}{\partial t} V_i + c \int_{\partial e_i} \mathbf{v} \, \mathbf{dS} = 0, \tag{2}$$

where  $c_i$  is average concentration in  $e_i$  and  $V_i$  its volume, c will be specified later (there are two main possibilities -  $c_i$  or concentration from neighbouring element). Term  $\frac{\partial c}{\partial t}$  we approximate by explicit Euler difference

$$\frac{\partial c}{\partial t} \approx \frac{c_i^{n+1} - c_i^n}{\Delta t}.$$
 (3)

Where  $\Delta t$  is a time step and upper index at  $c_i$  means values in the discrete time steps n+1 and n. We assume that all elements have piecewise smooth element boundary  $\partial e$  with outwards directed normal. Inside the area  $\Omega$  we introduce internal flows. With respect to  $e_i$ , we define internal flow intake  $U_{ij}^-$  (from element  $e_j$ ) and internal flow drain  $U_{ij}^+$  (to element  $e_j$ ) as follows

$$U_{ij}^{-} = \min(\int_{\partial e_i \cap \partial e_j, i \neq j} \boldsymbol{v} \, \mathbf{dS}, 0),$$

$$U_{ij}^{+} = \max(\int_{\partial e_i \cap \partial e_j, i \neq j} \boldsymbol{v} \, \mathbf{dS}, 0).$$
(4)

Those flows realizes solute transport in the area  $\Omega$ . On the  $\partial\Omega$  we define external flows which will be important for transport Dirichlet boundary conditions. In the same way as for internal flows we assume (with respect to element  $e_i$ ) external flow intake  $U_{ij}^{e-}$  (from  $\partial\Omega$ ) and external flow drain  $U_{ij}^{e+}$  (to  $\partial\Omega$ ).

$$U_{ik}^{e-} = \min(\int_{\partial e_i \cap \partial \Omega} \boldsymbol{v} \, \mathbf{dS}, 0),$$

$$U_{ik}^{e+} = \max(\int_{\partial e_i \cap \partial \Omega} \boldsymbol{v} \, \mathbf{dS}, 0).$$
(5)

Direction of the velocity v, which affects sign of the U-terms is significant for the construction solution. For the solution stability it is suitable to use an upwind scheme, which can by written for finite difference on simple 1D geometry in the form

$$v > 0: \frac{\partial c}{\partial x} \approx \frac{c_i^n - c_{i-1}^n}{\Delta x},$$

$$v < 0: \frac{\partial c}{\partial x} \approx \frac{c_{i+1}^n - c_i^n}{\Delta x}.$$
(6)

This scheme can be interpreted as well as in finite volume method - in convection term one can get c value opposite the flow of the quantity v direction. For every  $e_i$  we introduce itemsets  $\mathcal{N}_i, \mathcal{B}_i$  which contains indexes of neighbourging elements, local boundary conditions respectively. Assuming upwind scheme, using (4), (5), and (3) we can write solution of the equation (2) (relation between two consecutive time steps) on  $e_i$  in the form

$$c_i^{n+1} = c_i^n - \frac{\Delta t}{V_i} \left[ \sum_{j \in \mathcal{N}_i} \left[ U_{ij}^+ c_i + U_{ij}^- c_j \right] + \sum_{k \in \mathcal{B}_i} \left[ U_{ik}^{e+} c_i + U_{ik}^{e-} c_{B_{ik}} \right] \right]. \tag{7}$$

Where  $c_{B_{ik}}$  are values of Dirichlet boundary conditions which belong to  $e_i$ . Formula (7) can be rewritten into the matrix notation

$$\mathbf{c}^{n+1} = (\mathbf{I} + \Delta t \mathbf{A}) \cdot \mathbf{c}^n + \Delta t \mathbf{B} \cdot \mathbf{c_B}^n$$
(8)

Where **c** is vector of  $c_i^{n+1}$ , **A** is a square matrix composed from  $\frac{U_{ij}^+}{V_i}$ ,  $\frac{U_{ij}^-}{V_i}$ , and  $\frac{U_{ij}^{e^+}}{V_i}$ . **B** is in general rectangular matrix composed from  $\frac{U_{ij}^{e^-}}{V_i}$  and  $\mathbf{c_B}^n$  is vector of Dirichlet boundary conditions.matrix definition. There is one stability condition for time step which is called Courant-Friedrich-Levy condition. For the problem without sources/sinks it can be written as

$$\Delta t_{max} = \min_{i} \left( \frac{V_i}{\sum_{j} U_{ij}^+ + \sum_{k} U_{ik}^{e^+}} \right) = \min_{i} \left( \frac{V_i}{\sum_{j} |U_{ij}^-| + \sum_{k} |U_{ik}^{e^-}|} \right). \tag{9}$$

This condition has a physical interpretation, which can be understood as conservation law - volume that intakes/drains to/from element  $e_i$  can not be higher then element volume  $V_i$ . From algebraical point of view this condition can be seen as a condition which bounds norm of the evolution operator as follows

$$\|\mathbf{I} + \Delta t \mathbf{A} \quad \Delta t \mathbf{B}\| \le 1. \tag{10}$$

# Generalization

This approach can be used as well as for more general element connections – for compatible/non-compatible element interconnection, if we know the flow integral values  $(U_{ij}^+ \text{ or } U_{ij}^-)$ . The most

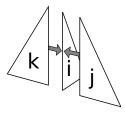


Figure 2: Edge with 3 elements

general case of connection is relation among n elements like in figure (2). For this case we define edge element indexset  $\mathcal{G}_l$  that contains all the indexes of elements which sides make l-th edge  $(g_l)$ , so that  $\mathcal{G}_l = \{i, j, k\}$ . For  $\mathcal{G}_l$  we introduce its subsets  $\mathcal{G}_{ij}$ ,  $\mathcal{G}_{ji}$ ,  $\mathcal{G}_{ki}$ ,  $\mathcal{G}_{kj}$ , and  $\mathcal{G}_{jk}$ , where  $\mathcal{G}_{ij} = \mathcal{G}_{ik} = \mathcal{G}_l \setminus i = \{j, k\}$ ,  $\mathcal{G}_{ji} = \mathcal{G}_{jk} = \mathcal{G}_l \setminus j = \{i, k\}$ , and  $\mathcal{G}_{ki} = \mathcal{G}_{kj} = \mathcal{G}_l \setminus k = \{i, j\}$ .

It can be written in the same way for any edge g with more than 3 elements, it is hold  $|\mathcal{G}_q| - 1 = |\mathcal{G}_{ab}|$ ;  $\forall a, b \in \mathcal{G}_q$ . For l-th edge  $(g_l)$  we can define total edge flow  $U_{q_l}$  eg. as

$$U_{g_{l}} = \sum_{m \in \mathcal{G}_{ji}} \left[ U_{mj}^{+} + \frac{U_{jm}^{+}}{|\mathcal{G}_{ji}|} \right] = \sum_{m \in \mathcal{G}_{jk}} \left[ U_{mj}^{+} + \frac{U_{jm}^{+}}{|\mathcal{G}_{jk}|} \right]$$

$$= \sum_{m \in \mathcal{G}_{ij}} \left[ U_{mi}^{+} + \frac{U_{im}^{+}}{|\mathcal{G}_{ij}|} \right] = \sum_{m \in \mathcal{G}_{ik}} \left[ U_{mi}^{+} + \frac{U_{im}^{+}}{|\mathcal{G}_{ik}|} \right]$$

$$= \sum_{m \in \mathcal{G}_{ki}} \left[ U_{mk}^{+} + \frac{U_{km}^{+}}{|\mathcal{G}_{ki}|} \right] = \sum_{m \in \mathcal{G}_{kj}} \left[ U_{mk}^{+} + \frac{U_{km}^{+}}{|\mathcal{G}_{kj}|} \right], \qquad (11)$$

 $U_{g_l}$  with respect to any  $e_m$ ;  $m \in \mathcal{G}_l$  has to have the same value because continuity equation, for assumed incompresible flow, has to be fulfilled in every edge. Edges with more than two elements and two and more nonzero intakes to edge realize an ideal mixing (to an average concentration) with weights which will be specified later. This fact modifies equation (7) on the general mesh into the form

$$c_{i}^{n+1} = c_{i}^{n} - \frac{\Delta t}{V_{i}} \left[ \sum_{j \in \mathcal{N}_{i}} \left[ U_{ij}^{+} c_{i} + \frac{U_{ij}^{-}}{\sum_{k \in \mathcal{G}_{ij}} \left[ U_{ki}^{+} + \frac{U_{ik}^{+}}{|\mathcal{G}_{ij}|} \right]} \sum_{k \in \mathcal{G}_{ij}} U_{ki}^{+} c_{k} \right] + \sum_{k \in \mathcal{B}_{i}} \left[ U_{ik}^{e+} c_{i} + U_{ik}^{e-} c_{B_{ik}} \right] \right].$$
 (12)

The edges with total edge flow  $U_{g_l} = 0$  can occur breakdown in the equation (12) via term  $\sum_{k \in \mathcal{G}_{ij}} \left[ U_{ki}^+ + \frac{U_{ik}^+}{|\mathcal{G}_{ij}|} \right] = 0.$  This fact implies as well as numerator  $U_{ij}^- = 0$ . In order to avoid dividing by zero we have to assume computation only for nonzero flows. Concentrations  $c_k$ ,  $k \in \mathcal{G}_{ij}$  that may intakes into element  $e_i$  are weighted with weights

$$\alpha_k = \frac{U_{ki}^+}{\sum_{k \in \mathcal{G}_{ij}} \left[ U_{ki}^+ + \frac{U_{ik}^+}{|\mathcal{G}_{ij}|} \right]},\tag{13}$$

so that the ideal mixing in this edge leads to the average concentration

$$c_{av} = \frac{\sum_{k \in \mathcal{G}_{ij}} U_{ki}^{+} c_{k}}{\sum_{k \in \mathcal{G}_{ij}} \left[ U_{ki}^{+} + \frac{U_{ik}^{+}}{|\mathcal{G}_{ij}|} \right]}.$$
 (14)

Matrix notation is the same as in (8). Finally ...

# Flow123D ini file format

Section: [Global]

KEY	TYPE	DEFAULT	DESCRIPTION
Problem_type	int	NULL	Type of solved problem. Currently supported: $1 = \text{steady saturated flow}$
Description	string	undefined	Short description of solved problem - any text.
Stop_time	double	1.0	Time interval of the whole problem.[time units]
Save_step	double	1.0	The output with transport is written every Save_step. [time units]

Section: [Input]

[ I]			
KEY	TYPE	DEFAULT	DESCRIPTION
Mesh	string	NULL	Name of file containing definition of the mesh for the problem.
Material	string	NULL	Name of file with hydraulical properties of the elements.
Boundary	$\operatorname{string}$	NULL	Name of file with boundary condition data.
Neighbouring	string	NULL	Name of file describing topology of the mesh.
Sources	string	NULL	Name of file with definition of fluid sources. This is optional file, if this key is not defined, calculation goes on without sources.

Section: [Transport]

Section: [Hanspert]			
KEY	TYPE	DEFAULT	DESCRIPTION
Transport_on	YES/NO	NO	If set "YES" program compute transport too.
Sorption	YES/NO	NO	If set "YES" program include sorption too.
Dual_porosity	YES/NO	NO	If set "YES" program include dual porosity too.
Reactions	YES/NO	NO	If set "YES" program include reactions too.
Concentration	string	NULL	Name of file with initial concentration.
Transport_BCD	$\operatorname{string}$	NULL	Name of file with boundary condition for transport.
Transport_out	string	NULL	Name of transport output file.
Transport_out_im	string	NULL	Name of transport immobile output file.
Transport_out_sorp	string	NULL	Name of transport sorbed output file.
Transport_out_im_sorp	$\operatorname{string}$	NULL	Name of transport sorbed immobile output file.
N_substances	int	-1	Number of substances.
Substances	string	undefined	Names of the substances separated by commas.
Substances_density_scales	list of doubles	1.0	Scales of substances for the density flow calculation.

Section: [Constants]

KEY	TYPE	DEFAULT	DESCRIPTION
g	double	1.0	Gravity acceleration.
rho	double	1.0	Density of fluid.

Section: [Run]

KEY	TYPE	DEFAULT	DESCRIPTION
Screen_verbosity	int	8	Amount of messages printed on the screen. (0 = no messages,, 7 = all messages)
Pause_after_run	YES/NO	NO	If set to "YES", the program waits for a key press before it finishes.

Section: [Solver]

KEY	TYPE	DEFAULT	DESCRIPTION
Use_last_solution	YES/NO	NO	If set to "YES", uses last known solution for chosen solver.
Solver_name	string	petsc	Type of linear solver. Supported solvers are: petsc, petsc_matis (experimental)
Solver_params	string	NULL	PETSc options to override default choice of iterative solver and preconditioner (use with care). In particular to use UMFPACK sequantial direct solver set:  Solve_params = "-ksp preonly -pc_type lu -pc_factor_mat_solver_package umfpack"  To use parallel direct solver MUMPS use:  Solve_params = "-ksp preonly -pc_type lu -pc_factor_mat_solver_package mumps -mat_mumps_icntl_14 5"
Keep_solver_files	YES/NO	NO	If set to "YES", files for solver are not deleted after the run of the solver.
Manual_solver_run	YES/NO	NO	If set to "YES", programm stops after writing input files for solver and lets user to run it.
Use_control_file	YES/NO	NO	If set to "YES", programm do not create control file for solver, it uses given file.
Control_file	string	NULL	Name of control file for situation, when $Use\_control\_file\ \bar{Y}ES.$
NSchurs	int	2	Number of Schur complements to use. Valid values are 0,1,2. The last one should be the fastest.
${ t Solver\_accuracy}$	double	1e-6	When to stop solver run - value of residum of matrix. Useful values from 1e-4 to 1e-10. Bigger number = faster run, less accuracy.
max_it	int	200	Maximum number of iteration of linear solver.

Section: [Output]

KEY	TYPE	DEFAULT	DESCRIPTION
Write_output_file	YES/NO	NO	If set to "YES", writes output file.
wiite_output_iiie	1 E5/110	NO	in set to TES, writes output me.
Output_file	$\mathbf{string}$	NULL	Name of the output file (type 1).
Output_file_2	$\mathbf{string}$	NULL	Name of the output file (type 2).
Output_digits	int	6	Number of digits used for floating point numbers in output file.
Output_file_type	int	1	Type of output file 1 - GMSH like format 2 - Flow data file 3 - both files (two separate names)
POS_view_params	double[8]	0 0 0 1 1 1 0 0	<ul><li>[x y z] angle of rotation "RotationX"</li><li>[x y z] scaling "ScaleX"</li><li>[x y] screen position shift "TranslationX"</li></ul>
Pos_format	string	ASCII	Output file format. One can use: ASCII, BIN, or VTK_SERIAL_ASCII

Description: Options controling output file of the programm

Section: [Semchem\_module]

KEY	TYPE	DEFAULT	DESCRIPTION
Compute_reactions	Yes/No	"No"	NO = transport without chemical reactions YES = transport influenced by chemical reactions
Output_precission	int	1	Number of decimal places written to output file created by Semchem_module.
Number_of_further_species	int	0	Concentrations of these species are not computed, because they are ment to be unexphaustible.
Temperature	double	0.0	Temperature, one of state variables of the system.
Temperature_Gf	double	0.0	Temperature at which Free Gibbs Energy is specified.
Param_Afi	double	0.0	Parameter of the Debuy-Hückel equation for activity coeficients computation.
Param_b	double	0.0	Parameter of the Debuy-Hückel equation for activity coeficients computation.
Epsilon	double	0.0	Epsilon specifies relative norm of residuum estimate to stop numerical algorithms used by Semchem_module.
Time_steps	int	1	Number of transport step subdivisions for Semchem_module.
Slow_kinetics_substeps	int	0	Number of substeps performed by Runge-Kutta method used for slow kinetics simulation.
Error_norm_type	$\operatorname{string}$	"Absolute"	Through wich kind of norm the error is measured.
Scalling	boolean	"No"	Type of the problem preconditioning for better convergence of numerical method.

Section: [Aqueous\_species]

KEY	TYPE	DEFAULT	DESCRIPTION
El_charge	int	0	Electric charge of an Aqueous_specie particleunder consideration.
dGf	double	0.0	Free Gibbs Energy valid for TemperatureGf.
dHf	double	0.0	Enthalpy
Molar_mass	double	0.0	Molar mass of Aqueous_species.

 ${\bf Section:} \ [{\bf Further\_species}]$ 

KEY	TYPE	DEFAULT	DESCRIPTION
Specie_name	string	)) ))	Name belonging to Further_specie under consideration.
dGf	double	0.0	Free Gibbs Energy valid for TemperatureGf.
dHf	double	0.0	Enthalpy
Molar_mass	double	0.0	Molar mass of Further_species.
Activity	double	0.0	Activity of Further_species.

 $\underline{\text{Section: } [\textbf{Reaction\_i}]}$ 

KEY	TYPE	DEFAULT	DESCRIPTION
Reaction_type	string	"unknown"	Type of considered reaction (Equilibrium, Kinetics, Slow_kinetics).
Stoichiometry	int	0	Stoichiometric coeficients of species taking part in <i>i</i> -th reaction.
Kinetic_constant	double	0.0	Kinetic constant for determination of reaction rate.
Order_of_reaction	int	0	Order of kinetic reaction for participating species.
Equilibrium_constant	double	0.0	Equilibrium constant defining i-th reaction.

Section: [Decay\_module]

KEY	TYPE	DEFAULT	DESCRIPTION
Compute_decay	Yes/No	"No"	Enables to switch on simulation of radioactive decay.
Nr_of_decay_chain	int	0	How many steps is defined decay chain consisting of?

Section: [Decay\_i]

KEY	TYPE	DEFAULT	DESCRIPTION
Reaction_type	enumerate	"decay"	In this time just decay type is possible.
Nr_of_isotopes	int	0	How many isotopes does the section work with.
${\tt Substance\_ids}$	$rac{ ext{array of}}{ ext{int}}$	NULL	Sequence of ids describing the order of isotopes in decay chain.
Half_lives	array of double	NULL	Contain half-lives belonging to isotopes defined by ids.
Bifurcation_on	Yes/No	"No"	Make it possible to switch of bifurcation in current [Decay_i].
Bifurcation	array of double	NULL	Gives a percentage, which is the first isotope in current [Decay_i] decaying to products.

# Mesh file format version 2.0

The mesh file format comes from the GMSH system. Following text is copied from the GMSH documentation.

======= BEGIN OF INSERTED TEXT =========

Version 2.0 of the .MSH file format is Gmsh's new native mesh file format. It is very similar to the old one (Version 1.0), but is more general: it contains information about itself and allows to associate an arbitrary number of integer tags with each element.

The .MSH file format, version 2.0, is divided in three sections, defining the file format (\$MeshFormat-\$EndMeshFormat), the nodes (\$Nodes-\$EndNodes) and the elements (\$Elements-\$EndElements) in the mesh:

### \$MeshFormat

2.0 file-type data-size

### \$EndMeshFormat

### \$Nodes

number-of-nodes

node-number x-coord y-coord z-coord

. . .

### \$EndNodes

### \$Elements

number-of-elements

elm-number elm-type number-of-tags <tags> node-number-list

. . .

### \$EndElements

where:

file-type is an integer equal to 0 in the ASCII file format.

data-size is an integer equal to the size of the floating point numbers used in the file (usually, data-size = sizeof(double)).

number-of-nodes is the number of nodes in the mesh.

node-number is the number (index) of the n-th node in the mesh. Note that the node-numbers do not have to be given in a consecutive (or even an ordered) way.

x-coord y-coord z-coord are the floating point values giving the X, Y and Z coordinates of the n-th node.

number-of-elements is the number of elements in the mesh.

*elm-number* is the number (index) of the *n*-th element in the mesh. Note that the *elm-number*s do not have to be given in a consecutive (or even an ordered) way.

elm-type defines the geometrical type of the n-th element:

- 1 Line (2 nodes)
- 2 Triangle (3 nodes)
- 3 Quadrangle (4 nodes)
- 4 Tetrahedron (4 nodes)
- 5 Hexahedron (8 nodes)
- 6 Prism (6 nodes)
- 7 Pyramid (5 nodes)
- 8 Second order line (3 nodes)
- 9 Second order triangle (6 nodes)
- 11 Second order tetrahedron (10 nodes)
- 15 Point (1 node)

number-of-tags gives the number of tags for the *n*-th element. By default, Gmsh generates meshes with two tags and reads files with an arbitrary number of tags: see below.

tag is an integer tag associated with the *n*-th element. By default, the first tag is the number of the physical entity to which the element belongs; the second is the number of the elementary geometrical entity to which the element belongs; the third is the number of a mesh partition to which the element belongs.

node-number-list is the list of the node numbers of the n-th element (separated by white space, without commas). The ordering of the nodes is given in Gmsh node ordering; for second order elements, the first order nodes are given first, followed by the nodes associated with the edges, followed by the nodes associated with the faces (if any). The ordering of these additional nodes follows the ordering of the edges/faces given in Gmsh node ordering.

==========	END	OF	INSERTED	TEXT	
------------	-----	----	----------	------	--

More information about GMSH can be found at its homepage: http://www.geuz.org/gmsh/

# Comments concerning 1-2-3-FLOW:

- Every inconsistency of the file stops the calculation. These are:
  - Existence of nodes with the same *node-number*.
  - Existence of elements with the same *elm-number*.
  - Reference to non-existing node.
  - Reference to non-existing material (see below).
  - Difference between *number-of-nodes* and actual number of lines in nodes' section.
  - Difference between *number-of-elements* and actual number of lines in elements' section.
- By default 1-2-3-FLOW uses meshes with number-of-tags = 2.

tag1 is number of region in which the element lies.

tag2 is number of material (reference to .MTR file) in the element.

- $\bullet$  Currently, line (type=1), triangle (type=2) and tetrahedron (type=4) are the only supported types of elements. Existence of an element of different type stops the calculation.
- $\bullet$  Wherever possible, we use the file extension .MSH. It is not required, but highly recomended.

# Material properties file format, version 1.0

The file is divided in two sections, header and data. The extension .MTR is highly recomended for files of this type.

```
$MaterialFormat
1.0 file-type data-size
$EndMaterialFormat
$Materials
number-of-materials
material-number material-type < material-type-specific-data > [text]
$EndMaterials
$Storativity
material-number < storativity-coefficient> [text]
$EndStorativity
$Geometry
material-number geometry-type < geometry-type-specific-coefficient> [text]
$EndGeometry
$Sorption
material-number substance-id sorption-type <sorption-type-specific-data> [text]
$EndSorption
$SorptionFraction
material-number < sorption-fraction-coefficient> [text]
$EndSorptionFraction
$DualPorosity
material-number < mobile-porosity-coefficient> < immobile-porosity-coefficient>
<nonequillibrium-coefficient-substance(0)>\ldots<nonequilibrium-coefficient-substance(n-1)>
/text/
$EndDualPorosity
$Reactions
reaction-type < reaction-type-specific-coefficient> [text]
$EndReactions
where:
file-type int — is equal 0 for the ASCII file format.
data-size int — the size of the floating point numbers used in the file. Usually data-size =
     sizeof(double).
number-of-materials int — Number of materials defined in the file.
material-number int — is the number (index) of the n-th material. These numbers do not
     have to be given in a consecutive (or even an ordered) way. Each number has to be
```

- given only onece, multiple definition are treated as inconsistency of the file and cause stopping the calculation (exception \$Sorption section).
- material-type int is type of the material, see table.
- < material-type-specific-data > format of this list depends on the material type.
- <storativity-coefficient> double coefficient of storativity
- geometry-type int type of complement dimension parameter (only for 1D and 2D material), for 1D element is supported type 1 cross-section area, for 2D element is supported type 2 thickness.
- <geometry-type-specific-coefficient> double cross-section for 1D element or thickness for
  2D element.
- substance-id int refers to number of transported substance, numbering starts on  $\theta$ .
- sorption-type int type 1 linear sorption isotherm, type 2 Freundlich sorption isotherm, type 3 Langmuir sorption isotherm.
- <sorption-type-specific-data > format of this list depends on the sorption type, see table.
  Note: Section \$Sorption is needed for calculation only if Sorption is turned on in the ini file.
- <sorption-fraction-coefficient> double ratio of the "mobile" solid surface in the contact with "mobile" water to the total solid surface (this parameter (section) is needed for calculation only if Dual\_porosity and Sorption is together turned on in the ini file).
- <mobile-porosity-coefficient> double ratio of the mobile pore volume to the total volume
   (this parameter is needed only if Transport\_on is turned on in the ini file).
- <immobile-porosity-coefficient> double ratio of the immobile pore volume to the total pore volume (this parameter is needed only if Dual\_porosity is turned on in the ini file).
- <nonequilibrium-coefficient-substance(i)> double nonequilibrium coefficient for substance  $i, \forall i \in \langle 0, n-1 \rangle$  where n is number of transported substances (this parameter is needed only if  $Dual\_porosity$  is turned on in the ini file).
- reaction-type int type 0 zero order reaction
- < reaction-type-specific-data > format of this list depends on the reaction type, see table.

material-type	material-type-specific-data	Description
11	k	$\mathbf{K} = (k)$
-11	a	$\mathbf{A} = \mathbf{K}^{-1} = (a)$
21	k	$\mathbf{K} = \left(\begin{array}{cc} k & 0 \\ 0 & k \end{array}\right)$
22	$k_x$ $k_y$	$\mathbf{K} = \begin{pmatrix} k_x & 0 \\ 0 & k_y \end{pmatrix}$
23	$k_x  k_y  k_{xy}$	$\mathbf{K} = \left(\begin{array}{cc} k_x & k_{xy} \\ k_{xy} & k_y \end{array}\right)$
-21	a	$\mathbf{A} = \mathbf{K}^{-1} = \left(\begin{array}{cc} a & 0 \\ 0 & a \end{array}\right)$
-22	$a_x - a_y$	$\mathbf{A} = \mathbf{K}^{-1} = \left(\begin{array}{cc} a_x & 0\\ 0 & a_y \end{array}\right)$
-23	$a_x  a_y  a_{xy}$	$\mathbf{A} = \mathbf{K}^{-1} = \begin{pmatrix} a_x & a_{xy} \\ a_{xy} & a_y \end{pmatrix}$
31	k	$\mathbf{K} = \left(\begin{array}{ccc} k & 0 & 0 \\ 0 & k & 0 \\ 0 & 0 & k \end{array}\right)$
33	$\begin{vmatrix} a_x & a_y & a_{xy} \end{vmatrix}$ $k &                                   $	$\mathbf{K} = \left(\begin{array}{ccc} k_x & 0 & 0 \\ 0 & k_y & 0 \\ 0 & 0 & k_z \end{array}\right)$
36	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\mathbf{K} = \begin{pmatrix} k_x & k_{xy} & k_{xz} \\ k_{xy} & k_y & k_{yz} \\ k_{xz} & k_{yz} & k_z \end{pmatrix}$
-31	a	$\mathbf{A} = \mathbf{K}^{-1} = \left( \begin{array}{ccc} 0 & a & 0 \\ 0 & 0 & a \end{array} \right)$
-33	$a_x  a_y  a_z$	$\mathbf{A} = \mathbf{K}^{-1} = \begin{pmatrix} a_x & 0 & 0 \\ 0 & a_y & 0 \\ 0 & 0 & a_z \end{pmatrix}$
-36	$\begin{bmatrix} a_x & a_y & a_z & a_{xy} & a_{xz} & a_{yz} \end{bmatrix}$	$\mathbf{A} = \mathbf{K}^{-1} = \begin{pmatrix} a_x & a_{xy} & a_{xz} \\ a_{xy} & a_y & a_{yz} \\ a_{xz} & a_{yz} & a_z \end{pmatrix}$

Note: all variables ( k,  $k_x$ ,  $k_y$ ,  $k_z$ ,  $k_{xy}$ ,  $k_{xz}$ ,  $k_{yz}$ , a,  $a_x$ ,  $a_y$ ,  $a_z$ ,  $a_{xy}$ ,  $a_{xz}$ ,  $a_{yz}$ ) are of the double type.

sorption-type	$sorption\-type\-specific\-data$	Description
1	$k_D[1]$	$s = k_D c$
2	$k_F[(L^{-3} \cdot M^1)^{(1-\alpha)}]  \alpha[1]$	$s = k_F c^{\alpha}$
3	$K_L[L^3 \cdot M^{-1}]$ $s^{max}[L^{-3} \cdot M^1]$	$s = \frac{K_L s^{max} c}{1 + K_L c}$

Note: all variables (  $k_D$ ,  $k_F$ ,  $\alpha$ ,  $K_L$ ,  $s^{max}$  ) are of the double type.

$reaction\-type$	reaction-type-specific-data	Description
0	$substance{-id[1]} \qquad k[M\cdot L^{-3}\cdot T^{-1}]$	$\frac{\partial c_m^{[substance-id]}}{\partial t} = k$

Where  $c_m^{[substance-id]}$  is mobile concentration of substance with id substance-id and  $\Delta t$  is the internal transport time step defined by CFL condition.

text char[] — is a text description of the material, up to 256 chars. This parameter is

optional.

# Comments concerning 1-2-3-FLOW:

ullet If number-of-materials differs from actual number of material lines in the file, it stops the calculation.

# Boundary conditions file format, version 1.0

The file is divided in two sections, header and data.

### \$BoundaryFormat

1.0 file-type data-size

\$EndBoundaryFormat

### \$BoundaryConditions

number-of-conditions

condition-number type <type-specific-data> where <where-data> number-of-tags <tags> [text]

. . .

### \$EndBoundaryConditions

where

file-type int — is equal 0 for the ASCII file format.

data-size int — the size of the floating point numbers used in the file. Usually data-size = sizeof(double).

number-of-conditions int — Number of boundary conditions defined in the file.

condition-number int — is the number (index) of the n-th boundary condition. These numbers do not have to be given in a consecutive (or even an ordered) way. Each number has to be given only onece, multiple definition are treated as inconsistency of the file and cause stopping the calculation.

type int — is type of the boundary condition. See below for definitions of the types.

<type-specific-data> — format of this list depends on the type. See below for specification of the type-specific-data for particular types of the boundary conditions.

where int — defines the way, how the place for the contidion is prescribed. See below for details.

<where-data> — format of this list depends on where and actually defines the place for the condition. See below for details.

number-of-tags int — number of integer tags of the boundary condition. It can be zero.

< tags > number-of-tags\*int — list of tags of the boundary condition. Values are separated by spaces or tabs. By default we set number-of-tags=1, where tag1 defines group of boundary conditions, "type of water" in our jargon. This can be used to calculate total fluxes through the boundary group.

[text] char[] — arbitrary text, description of the fracture, notes, etc., up to 256 chars. This is an optional parameter.

# Types of boundary conditions and their data

type = 1 — Boundary condition of the Dirichlet's type

type = 2 — Boundary condition of the Neumann's type

type = 3 — Boundary condition of the Newton's type

type	$type ext{-}specific ext{-}data$	Description
1	scalar	Prescribed value of pressure (in meters [m])
2	flux	Prescribed value of flux through the boundary
3	scalar sigma	Scalar value and the $\sigma$ coefficient

scalar, flux and sigma are of the double type.

# Ways of defining the place for the boundary condition

where = 1 — Condition on a node

where = 2 — Condition on a (generalized) side

where = 3 — Condition on side for element with only one external side.

where	<pre><where-data></where-data></pre>	Description	
1	node-id	Node id number, according to .MSH file	
2	elm-id sid-id	Elm. id number, local number of side	
3	elm-id	Elm. id number	

The variables node-id, elm-id, sid-id are of the int type.

# Comments concerning 1-2-3-FLOW:

- We assume homegemous Neumman's condition as the default one. Therefore we do not need to prescribe conditions on the whole boundary.
- If the condition is given on the inner edge, it is treated as an error and stops calculation.
- Any inconsistence in the file stops calculation. (Bad number of conditions, multiple definition of condition, reference to non-existing node, etc.)
- At least one of the conditions has to be of the Dirichlet's or Newton's type. This is well-known fact from the theory of the PDE's.
- Local numbers of sides for where = 2 must be lower than the number of sides of the particular element and greater then or equal to zero.
- The element specified for where = 3 must have only one external side, otherwise the program stops.

# Neighbouring file format, version 1.0

The file is divided in two sections, header and data. The extension .NGH is highly recomended for files of this type.

```
$NeighbourFormat
1.0 file-type data-size
$EndNeighbourFormat
$Neighbours
number-of-neighbours
neighbour-number type <type-specific-data>
...
$EndNeighbours
```

φεπαινετέπ

where

file-type int — is equal 0 for the ASCII file format.

data-size int — the size of the floating point numbers used in the file. Usually data-size = sizeof(double).

number-of-neighbours int — Number of neighbouring defined in the file.

neighbour-number int — is the number (index) of the n-th neighbouring. These numbers do not have to be given in a consecutive (or even an ordered) way. Each number has to be given only onece, multiple definition are treated as inconsistency of the file and cause stopping the calculation.

type int — is type of the neighbouring.

<type-specific-data> — format of this list depends on the type.

# Types of neighbouring and their specific data

type = 10 — "Edge with common nodes", i.e. sides of elements with common nodes. (Possible many elements)

type = 11 — "Edge with specified sides", i.e. sides of the edge are explicitly defined. (Possible many elements)

type = 20 — "Compatible", i.e. volume of an element with a side of another element. (Only two elements)

type = 30 — "Non-compatible" i.e. volume of an element with volume of another element. (Only two elements)

type	type-specific-data	Description
10	$n_{-}elm\ eid1\ eid2\dots$	number of elements and their ids
11	$n\_sid\ eid1\ sid1\ eid2\ sid2\ \dots$	number of sides, their elements and local ids
20	eid1 eid2 sid2 coef	Elm 1 has to have lower dimension
30	eid1 eid2 coef	Elm 1 has to have lower dimension

*coef* is of the double type, other variables are ints.

# Comments concerning 1-2-3-FLOW:

- Every inconsistency or error in the .NGH file causes stopping the calculation. These are especially:
  - Multiple usage of the same neighbour-number.
  - Difference between number-of-neighbours and actual number of data lines.
  - Reference to nonexisting element.
  - Nonsence number of side.
- $\bullet$  The variables sid? must be nonegative and lower than the number of sides of the particular element.

# Sources file format, version 1.0

The file is divided in two sections, header and data. The extension .SRC is highly recomended for files of this type.

# \$SourceFormat 1.0 file-type data-size \$EndSourceFormat \$Sources number-of-sources eid density

### \$EndSources

where

file-type int — is equal 0 for the ASCII file format.

data-size int — the size of the floating point numbers used in the file. Usually data-size = sizeof(double).

number-of-sources int — Number of sources defined in the file.

eid int — is id-number of the element, where the source lies.

density double — is the density of the source, in volume of fluid per time unit. Possitive values are sources, negative are sinks.

### Comments concerning 1-2-3-FLOW:

- Every inconsistency or error in the .SRC file causes stopping the calculation. These are especially:
  - Multiple usage of the same *source-number*.
  - Difference between *number-of-sources* and actual number of data lines.
  - Reference to nonexisting element.

# ASCII post-processing file format version 1.2

File format of this file comes from the GMSH system. Following text is copied from the GMSH documentation.

======= BEGIN OF INSERTED TEXT =========

The ASCII post-processing file is divided in several sections: one format section, enclosed between \$PostFormat-\$EndPostFormat tags, and one or more post-processing views, enclosed between \$View-\$EndView tags:

```
$PostFormat
1.2 file-type data-size
$EndPostFormat
$View
view-name nb-time-steps
nb-scalar-points nb-vector-points nb-tensor-points
nb-scalar-lines nb-vector-lines nb-tensor-lines
nb-scalar-triangles nb-vector-triangles nb-tensor-triangles
nb-scalar-quadrangles nb-vector-quadrangles nb-tensor-quadrangles
nb-scalar-tetrahedra nb-vector-tetrahedra nb-tensor-tetrahedra
nb-scalar-hexahedra nb-vector-hexahedra nb-tensor-hexahedra
nb-scalar-prisms nb-vector-prisms nb-tensor-prisms
nb-scalar-pyramids nb-vector-pyramids nb-tensor-pyramids
nb-text2d nb-text2d-chars nb-text3d nb-text3d-chars
< time-step-values>
< scalar-point-values>
< vector-point-values>
<tensor-point-values>
< scalar-line-values>
< vector-line-values >
<tensor-line-values>
<scalar-triangle-values>
< vector-triangle-values>
<tensor-triangle-values>
<scalar-quadrangle-values>
< vector-quadrangle-values>
< tensor-quadrangle-values>
< scalar-tetrahedron-values>
< vector-tetrahedron-values>
<tensor-tetrahedron-values>
<scalar-hexahedron-values>
< vector-hexahedron-values>
<tensor-hexahedron-values>
<scalar-prism-values>
< vector-prism-values>
<tensor-prism-values>
```

< scalar-pyramid-values>

```
<vector-pyramid-values><tensor-pyramid-values><text2d><text2d-chars><text3d><text3d-chars><$EndView
```

where:

file-type is an integer equal to 0 in the ASCII file format.

data-size is an integer equal to the size of the floating point numbers used in the file (usually, data-size = sizeof(double)).

view-name is a string containing the name of the view (max. 256 characters).

*nb-time-steps* is an integer giving the number of time steps in the view.

*nb-scalar-points*, *nb-vector-points*, . . . are integers giving the number of scalar points, vector points, . . . in the view.

nb-text2d, nb-text3d are integers giving the number of 2D and 3D text strings in the view.

nb-text2d-chars, nb-text3d-chars are integers giving the total number of characters in the 2D and 3D strings.

time-step-values is a list of nb-time-steps double precision numbers giving the value of the time (or any other variable) for which an evolution was saved.

scalar-point-value, vector-point-value, ... are lists of double precision numbers giving the node coordinates and the values associated with the nodes of the nb-scalar-points scalar points, nb-vector-points vector points,..., for each of the time-step-values.

For example, vector-triangle-value is defined as:

```
coord1-node1 \ coord1-node2 \ coord1-node3 coord2-node1 \ coord2-node2 \ coord3-node3 coord3-node1 \ coord3-node2 \ coord3-node3 comp1-node1-time1 \ comp2-node1-time1 \ comp3-node1-time1 comp1-node2-time1 \ comp2-node3-time1 \ comp3-node3-time1 comp1-node1-time2 \ comp2-node1-time2 \ comp3-node1-time2 comp1-node2-time2 \ comp2-node2-time2 \ comp3-node2-time2 comp1-node3-time2 \ comp3-node3-time2 comp3-node3-time2
```

text2d is a list of 4 double precision numbers:

```
coord1 coord2 style index
```

where *coord1* and *coord2* give the coordinates of the leftmost element of the 2D string in screen coordinates, *index* gives the starting index of the string in *text2d-chars* and *style* is currently unused.

text2d-chars is a list of nb-text2d-chars characters. Substrings are separated with the '^' character (which is a forbidden character in regular strings).

text3d is a list of 5 double precision numbers

coord1 coord2 coord3 style index

where *coord1*, *coord2* and *coord3* give the coordinates of the leftmost element of the 3D string in model (real world) coordinates, *index* gives the starting index of the string in *text3d-chars* and *style* is currently unused.

text3d-chars is a list of nb-text3d-chars chars. Substrings are separated with the '^' character.

======= END OF INSERTED TEXT ========

More information about GMSH can be found at its homepage: http://www.geuz.org/gmsh/

### Comments concerning FFLOW20:

- FFLOW20 generates .POS file with four views: Elements' pressure, edges' pressure, interelement fluxes and complex view. First three views shows "raw data", results obtained by the solver without any interpolations, smoothing etc. The fourth view contains data processed in this way.
  - **Elements' pressure:** Contains only scalar-triangle-values. Triangles are the same as the elements of the original mesh. We prescribe constant value of the pressure on the element, as it was calculated by the solver as the unknown p. Therefore, the three values on every triangle are the same.
  - **Edge pressure:** Contains only *scalar-line-values*. The lines are the same as the edges of the elements of the original mesh. We prescribe constant value of the pressure on the edge, as it was calculated by the solver as the unknown  $\lambda$ . Therefore, the two values on every edge are the same.
  - Interelement flux: Contains vector-point-values and scalar-triangle-values. The scalar-triangle-values carry no information, all values are set to 0, these are in the file only to define a shape of the elements. The points for the vector-point-values are midpoints of the sides of the elements. The vectors are calculated as un, where u is value of the flux calculated by the solver and n is normalized vector of outer normal of the element's side.
  - Complex view: Contains scalar-triangle-values and vector-point-values. The scalar-triangle-values shows the shape of the pressure field. The triangles are the the same as the elements of the original mesh. Values of pressure in nodes are interpolated from ps and  $\lambda s$ . The vector-point-values shows the velocity of the flow in the centres of the elements.