## Technical university of Liberec

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# FLOW123D - draft, scheme of new inputs

version 1.7.0

Documentation of file formats and brief user manual.

## Liberec, 2011

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# Chapter 1

## Quick start

Flow123D is a software for simulation of water flow and reactionary solute transport in a heterogeneous porous and fractured medium. In particular it is suited for simulation of underground processes in a granite rock massive. The program is able to describe explicitly processes in 3D medium, 2D fractures, and 1D chanels and exchange between domains of different dimension. The computational mesh is therefore collection of 3D tetrahedrons, 2D triangles and 1D line segments.

The water flow model assumes a saturated medium described by Darcy law. For discretization, we use lumped mixed-hybrid finite element method. We support both steady and unsteady water flow.

The solute transport model can deal with several dissolved substances. It contains non-equilibrium dual porosity model, i.e. exchange between mobile and immobile pores. There is also model for several types of adsorption in both the mobile and immobile zone. The implemented adsorption models are linear adsorption, Freundlich isotherm and Langmuir isotherm. The solute transport model uses finite volume discretization with up-winding in space and explicit Euler discretization in time. The dual porosity and the adsorption are introduced into transport by operator splitting. The dual porosity model use analytic solution and the non-linear adsorption is solved numerically by the Newton method.

Reaction between transported substances can be modeled either by a SEMCHEM module, which is slow, but can describe all sorts of reactions. On the other hand, for reactions of the first order, i.e. linear reactions or decays, we provide our own solver which is much faster. Reactions are coupled with transport by the operator splitting method,

The program provides output of the pressure, the velocity and the concentration fields in two file formats. You can use file format of GMSH mesh generator and post-processor or you can use output into widely supported VTK format. In particular we recommend Paraview software for visualization and post-processing of VTK data.

The program is implemented in C/C++ using essentially PETSC library for linear algebra. The water flow as well as the transport simulation and reactions can be computed in parallel using MPI environment.

The program is distributed under GNU GPL v. 3 license and is available on the project web page: http://dev.nti.tul.cz/trac/flow123d

## 1.1 Basic usage

#### 1.1.1 How to run the simulation.

On the Linux system the program can be started either directly or through a script flow123d.sh. When started directly, e.g. by the command

#### > flow123d -s example.ini

the program requires one argument after switch -s which is the name of the principal input file. Full list of possible command line arguments is as follows.

format using particular macros.

#### --help

Parameters interpreted by Flow123d.Remaining parameters are passed to PETSC.

#### -s, --solve file

Set principal CON input file. All relative paths in the CON file are relative against current directory.

#### -i, --input\_dir directory

The place holder \${INPUT} used in the path of an input file will be replaced by given directory.

#### -o, --output\_dir directory

All paths for output files will be relative to this *directory*.

#### -1, --log file\_name

Set base name of log files.

#### --no\_log

Turn off logging.

#### --no\_profiler

Turn off profiler output.

#### --full\_doc

Prints full structure of the main input file.

#### --JSON\_template

Prints description of the main input file as a valid CON file template.

All other parameters will be passed to the PETSC library. An advanced user can influence lot of parameters of linear solver. In order to get list of supported options use parameter -help together with some valid input. Options for various PETSC modules are displayed when the module is used for the first time.

Alternatively, you can use script flow123d.sh to start parallel jobs or limit resources used by the program. This script accepts the same parameters as the program itself and further following additional parameters:

-h

Usage overview.

-t timeout

Upper estimate for real running time of the calculation. Kill calculation after *timeout* seconds. Can also be used by PBS to choose appropriate job queue.

-np number of processes

Specify number of parallel processes for calculation.

-m memory limit

Limits total available memory to memory limit bytes.

-n priority

Change (lower) priority for the calculation. See nice command.

-r out file

Stdout and stderr will be redirected to out file.

On the Windows system we use Cygwin libraries in other to emulate Linux API. Therefore you have to keep the Cygwin libraries within the same directry as the program executable. The Windows package that can be downloaded from project web page contains both the Cygwin libraries and the mpiexec command for starting parallel jobs on the Windows workstations.

Then you can start the sequential run by the command:

> flow123d.exe -s example.ini

or the parallel run by the command:

> mpiexec.exe -np 2 flow123d.exe -s example.ini

The program accepts the same parameters as the Linux version, but there is no script similar to flow123d.sh for the Windows system.

#### 1.1.2 Tutorial problem

#### CON file format

The main input file use slightly extended JSON file format which together with some particular constructs forms a CON (C++ object notation) file format. Main extensions of the JSON are unquoted key names (as long as they do not contain whitespaces), possibility to use = instead of : and C++ comments, i.e. // for the one line and /\* \*/ for the multi-line comment. In CON file format, we prefere to call JSON objects as "records" and we introduce also "abstract records" that mimics C++ abstract classes, the arrays of an CON file have only alements of the same type (possibly using abstract record types for polymorphism). The usual keys are in lower case and without spaces (using underscores instead), there are few special upper case keys that are interpreted by the reader: REF key for references, TYPE key for specifing actual type of an abstract record. For detailed description see Section 3.1.2.

#### Geometry

In the following, we shall provide commented input for the tutorial problem (tests/03\_transport\_small\_We consider simple 2D problem with a branching 1D fracture (see Figure 1.1 for the geometry). To prepare the mesh file we use the GMSH software. First, we construct the geometry file. In our case the geometry consists of:

- one physical 2D domain corresponding to the whole square
- three 1D physical domains of the fracture
- four 1D boundary physical domains of the 2d domain
- three 0D boundary physical domains of the 1d domain

In this simple example, we can in fact combine physical domains in every group, however we use this more complex setting for demonstration purposes. Using GMSH graphical interface we can prepare the GEO file where physical domains are referenced by numbers, then we use any text editor and replace numbers with string labels in such a way that the labels of boundary physical domains start with the dot character. These are the domains where we would not do any calculations but use them for setting boundary conditions. Finally, we get the GEO file like this:

```
cl1 = 0.16;
                                               Line Loop(30) = \{20, -19, 24, 25\};
   Point(1) = \{0, 1, 0, cl1\};
2
                                               Plane Surface(30) = \{30\};
                                            21
   Point(2) = \{1, 1, 0, cl1\};
                                               Line Loop(32) = \{23, 19, 21, 28, -22\};
                                            22
   Point(3) = \{1, 0, 0, cl1\};
                                               Plane Surface(32) = \{32\};
                                            23
                                               Line Loop(34) = \{26, 27, -21, -20\};
   Point(4) = \{0, 0, 0, cl1\};
   Point(6) = \{0.25, -0, 0, cl1\};
                                               Plane Surface(34) = \{34\};
                                            25
   Point(7) = \{0, 0.25, 0, cl1\};
                                               Physical Point(".1d_top") = {9};
                                            26
   Point(8) = \{0.5, 0.5, -0, cl1\};
                                               Physical Point(".1d_left") = {7};
8
                                            27
   Point(9) = \{0.75, 1, 0, cl1\};
                                               Physical Point(".1d_bottom") = {6};
                                            28
   Line(19) = \{9, 8\};
                                               Physical Line("1d_upper") = {19};
10
                                            29
                                               Physical Line("1d_lower") = {21};
   Line(20) = \{7, 8\};
11
                                            30
   Line(21) = \{8, 6\};
                                               Physical Line("1d_left_branch") = {20};
12
                                            31
   Line(22) = \{2, 3\};
                                               Physical Line(".2d_top") = {23, 24};
13
                                            32
   Line(23) = \{2, 9\};
                                               Physical Line(".2d_right") = {22};
14
                                            33
   Line(24) = \{9, 1\};
                                               Physical Line(".2d_bottom") = {27, 28};
15
                                            34
   Line(25) = \{1, 7\};
                                               Physical Line(".2d_left") = \{25, 26\};
                                            35
16
   Line(26) = \{7, 4\};
                                               Physical Surface("2d") = {30, 32, 34};
                                            36
17
   Line(27) = \{4, 6\};
18
   Line(28) = \{6, 3\};
```

Notice the labeled physical domains on lines 26-36. Then we just set the discretization step cl1 and use GMSH to create the mesh file. The mesh file contains as the 'bulk' elements where we perform calculations as the 'boundary' elements (on boundary physical domains) where we only set boundary conditions.

Having the computational mesh, we can create the main input file with description of our problem.

```
{
     problem = {
2
       TYPE = "SequentialCoupling",
3
       description = "Transport 1D-2D, (convection, dual porosity, sorption)",
4
5
         mesh_file = "./input/mesh_with_boundary.msh",
6
         sets = [
7
              { name="1d_domain",
                region_labels = [ "1d_upper", "1d_lower", "1d_left_branch" ]
              }
10
           ]
11
       },
12
```

The file starts with particular problem type, currently the type "SequantialCoupling" is suported, and textual problem description. Next, we specify the computational mesh, here it consists of the name of the mesh file and declaration of one region set composed of all 1D regions i.e. representing the whole fracture. Other keys of the mesh record allows lebeling regions given only by numbers, defining new regions in terms of element numbers (e.g to have leakage on single element), defining boundary regions, and set operations with region sets, see Section ?? for details.

#### Flow setting

Next, we setup the flow problem. We shall consider a flow driven only by the pressure gradient (no gravity), setting the Dirichlet boundary condition on the whole boundary with the pressure head equal to x+y. The conductivity will be 1 on the 2D domain and 10 on the 1D domain. The fracture width will be  $\delta_1 = 1$  (quite unnatural) as well as the transition parameter  $\sigma_2 = 1$  which describes a "conductivity" between dimensions. These are currently the default values.

```
primary_equation = {
13
          TYPE = "Steady_MH",
14
15
          bulk_data = [
16
             { r_set = "1d_domain", conductivity = 10 },
17
             \{ \text{ region = "2d"}, 
                                       conductivity = 1 }
18
          ],
19
20
          bc_data = [
21
             { r_set = "BOUNDARY",
22
               bc_type = "dirichlet",
23
               bc_pressure = { TYPE="FieldFormula", value = "x+y" }
24
             }
25
          ],
26
27
```

```
output = {
28
            output_stream = { REF = "/system/output_streams/0" },
29
            pressure_p0 = "flow_output_stream",
30
            pressure_p1 = "flow_output_stream",
31
            velocity_p0 = "flow_output_stream"
32
          },
33
34
          solver = { TYPE = "Petsc", accuracy = 1e-07 }
35
       }, // primary equation
36
```

On line 11, we specify particular implementation (numerical method) of the flow solver, in this case the Mixed-Hybird solver for unsteady probelems. On lines 16 – 19, we set mathematical fields that lives on the computational domain (i.e. the bulk domain), we set only the conductivity field since other bulk fields has appropriate default values. On lines 21 – 26, we set fields for boundary conditions. We use implicitely defined set "BOUNDARY" that contains all boundary regions and set there dirichlet boundary condition in terms of the pressure head. In this case, the field is not of the implicit type "FieldConstant", so we must specify the type of the field "FieldFormula". Se Section ?? for other boundary fields. On lines 28 – 33, we specify which output fields should be written into which output stream (that means particular output file, with given format). Currently, we support only one output stream per equation, so this allows at least switching individual output fields on or off. Notice the reference used on line 29 pointing to the definition of the output streams at the end of the file. Finally, we specify type of the linear solver and its tolerance.

#### Transport setting

We also consider subsequent transport problem with the porosity  $\theta = 0.25$  and zero initial concentration. The boundary condition is equal to 1 and is automatically applied only on the inflow part of the boundary. There is also some adsorption and dual porosity model in this particular test case, but we do not discuss this topic here for the sake of simplicity, see Section ?? for the description.

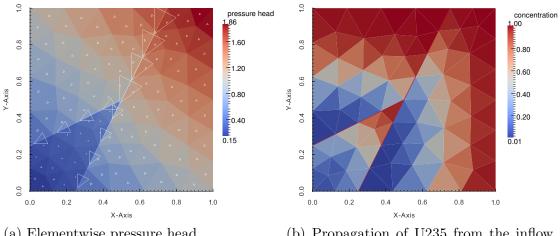
```
secondary_equation = {
37
          TYPE = "TransportOperatorSplitting",
38
39
          dual_porosity = true,
          sorption_enable = true,
41
          substances = [ "age", "U235" ],
42
43
          bulk_data = [
44
            \{ r_{set} = "ALL", 
45
               init\_conc = 0,
46
               por_m = 0.25,
               por_imm = 0.25,
48
               alpha = [0.01, 0.01],
49
               phi = 0.5,
50
               sorp_type = [1, 2],
51
```

```
sorp\_coef0 = [0.02, 0.02],
52
               sorp\_coef1 = [0, 0.5]
53
            }
54
          ],
55
56
          bc_data = [
            { r_set = "BOUNDARY",
58
               bc\_conc = 1.0
59
            }
60
          ],
61
62
          output = {
63
            output_stream = { REF = "/system/output_streams/1" },
            save\_step = 0.01,
65
            mobile_p0 = "transport_output_stream"
66
          },
67
68
          time = { end_time = 1.0 }
69
        } // secondary_equation
70
      }, // problem
71
```

For the transport problem we use implementation called "TransportOperatorSplitting" which is explicit finite volume solver of the convection equation (without diffusion), the operator splitting is used for the equilibrium adsorption as well as for the dual porosity model. Both these are switched on as we can see on lines 40, 41. On the next line, we set names of transported substances, here it is the age of the water and the uranium 235. On lines 44-55, we set the bulk fields in particular the porosity 'por\_m' and the initial concentrations ( one for every substance ). However, on line 46, we see only single value since an automatic conversion is applied to turn the scalar zero into the zero vector (of size 2). On line 53, we can see vector that set different adsorption coefficients for the two substances. Then, on lines 57-61, we set the boundary fields namely the concentration on the inflow part of the boundary. We need not to specify type of the condition since currently this is the only one available. In the output record we have to specify the save step (line 65) for the output fields. And finally, we have to set the time setting, here only the end time of the simulation since the step size is determined from the CFL condition, however you can set smaller time step if you want.

#### Output streams and results

```
system = {
72
        output_streams = [
73
          {
74
            file = "test3.pvd",
75
            format = { TYPE = "vtk", variant = "ascii" },
76
            name = "flow_output_stream"
          },
78
          {
79
            file = "test3-transport.pvd",
80
```



- (a) Elementwise pressure head and velocity field (triangles).
- (b) Propagation of U235 from the inflow part of the boundary.

Figure 1.1: Results of the tutorial problem.

The end of the input file contains declaration of two output streams, on for the flow problem and one for the transport problem. Currently, we support output into VTK format and GMSH data format. On Figure 1.1 you can see the results, the pressure and the velocity field on the left and the concentration of U235 at time t=0.9 on the right. Even if the pressure gradient is the same on the 2D domain as on the fracture, the velocity field is ten times faster on the fracture. Since porosity is same, the substance is transported faster by the fracture and then appears in the bottom left 2D domain before the main wave propagating solely through the 2D domain.

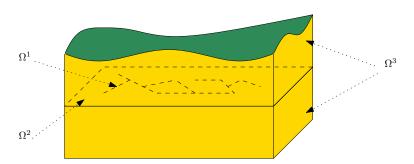
The output files can be either \*.msh files accepted by the GMSH or one can use VTK format that can be post-processed by Paraview.

In the following chapter, we briefly describe structure of individual input files in particular the main INI file. In the last chapter, we describe mathematical models and numerical methods used in the Flow123d.

# Chapter 2

# Mathematical models of physical reality

Flow123d provides models for Dary flow in porous media as well as for the transport and reactions of soluted substances. In this section, we describe mathematical formulations of these models together with physical meaning and units of all involved quantities. Common and unique feature of all models is support of domains with mixed dimension. Let  $\Omega_3 \subset \mathbf{R}^3$  be an open set representing continuum approximation of porous and fractured medium. Similarly, we consider open set  $\Omega_2 \subset \mathbf{R}^2$  representing 2D fractures and open set  $\Omega_1 \subset \mathbf{R}^3$  of 1D channels or preferential paths (see Fig ??). We assume that  $\Omega_2$  and  $\Omega_1$  are polygonal. For every dimension d = 1, 2, 3, we introduce a triangulation  $\mathcal{T}_d$  of the open set  $\Omega_d$  that consists of finite elements  $T_d^i$ ,  $i = 1, \ldots, N_E^d$ . The elements are simplexes that is tetrahedrons, triangles and lines.



Present numerical methods requires meshes satisfying the compatibility conditions

$$T_{d-1}^i \cap T_d \subset \mathcal{F}_d, \quad \text{where } \mathcal{F}_d = \bigcup_k \partial T_d^k$$
 (2.1)

and

$$T_{d-1}^i \cap \mathcal{F}_d$$
 is either  $T_{d-1}^i$  or  $\emptyset$  (2.2)

for every  $i \in \{1, \dots, N_E^{d-1}\}$ ,  $j \in \{1, \dots, N_E^d\}$ , and d = 2, 3. That is the (d-1)-dimensional elements are either between d-dimensional elements and match their sides or they poke out of  $\Omega_d$ .

## 2.1 Darcy flow model

We consider simplest model for the velocity of the steady or unsteady flow in porous and fractured medium given by Darcy low:

$$\mathbf{w} = -\mathbb{K}\nabla H$$
 on  $\Omega_d$ , for  $d = 1, 2, 3$ . (2.3)

We drop the dimension index of quantities in equations if it is same as the dimension of the set where the equation holds. In (2.3),  $\mathbf{w}_d$  [ms<sup>-1</sup>] is the superficial velocity,  $\mathbb{K}_d$  is the conductivity tensor, and  $H_d$  [m] is the piezometric head. The velocity is related to the flux  $\mathbf{q}_d$  with units [m<sup>4-d</sup>s<sup>-1</sup>] through

$$\boldsymbol{q}_d = \delta_d \boldsymbol{w}_d.$$

where  $\delta_d$  [m<sup>3-d</sup>] is a cross section coefficient, in particular  $\delta_3 = 1$ ,  $\delta_2$  [m] is the thickness of a fracture, and  $\delta_1$  [m<sup>2</sup>] is the cross-section of a channel. The flux  $q_d$  is the volume of the liquid (water) that pass through a unit square (d = 3), unit line (d = 2), or through a point (d = 1) per one second. The conductivity tensor is given by the product  $\mathbb{K}_d = k_d \mathbb{A}_d$ , where  $k_d > 0$  is the hydraulic conductivity [ms<sup>-1</sup>] and  $A_d$  is 3x3 dimensionless anisotropy tensor which has to be symmetric and positive definite. The piezometric-head  $H_d$  has units [m] and is related to the pressure head  $h_d$  by  $H_d = h_d + z$  assuming that the gravity force acts in negative direction of the z-axes. Combining these relations we get Darcy low in the form:

$$\mathbf{q} = -\delta k \mathbb{A} \nabla (h+z)$$
 on  $\Omega_d$ , for  $d=1,2,3$ . (2.4)

Next, we employ continuity equation for saturated porous medium:

$$\partial_t(Sh) + \operatorname{div} \mathbf{q} = F$$
 on  $\Omega_d$ , for  $d = 1, 2, 3,$  (2.5)

where  $S_d$  is the storativity and  $F_d$  is a source term. In our setting the principal unknowns of the system (2.4, 2.5) are the pressure head  $h_d$  and the flux  $q_d$ .

The storativity  $S_d > 0$  or the volumetric specific storage  $[m^{-1}]$  can be expressed as

$$S_d = \gamma_w (\beta_r + \nu \beta_w), \tag{2.6}$$

where  $\gamma_w$  [kgm<sup>-2</sup>s<sup>-2</sup>] is the specific weight of water,  $\nu$  is the porosity [-],  $\beta_r$  is compressibility of the bulk material of the pores (rock) and  $\beta_w$  is compressibility of the water both with units [kg<sup>-1</sup>ms<sup>-2</sup>]. For steady problems we set  $S_d = 0$  for all dimensions d = 1, 2, 3. The source term  $F_d$  [m<sup>3-d</sup>s<sup>-1</sup>] on the right hand side of (2.5) consists of the volume density of prescribed sources  $f_d$  [s<sup>-1</sup>] and flux from higher dimension. Exact formula is slightly different for every dimension and will be discussed presently.

On  $\Omega_3$  we simply have  $F_3 = f_3$  [s<sup>-1</sup>].

On the set  $\Omega_2 \cap \Omega_3$  the fracture is surrounded by one 3D surface from every side (or just one surface since we allow also 2D models on the boundary). On  $\partial \Omega_3 \cap \Omega_2$  we prescribe boundary condition of Robin type

$$q_3 \cdot n^+ = q_{32}^+ = \sigma_3^+ (h_3^+ - h_2),$$
  
 $q_3 \cdot n^- = q_{32}^- = \sigma_3^- (h_3^- - h_2),$ 

where  $\mathbf{q}_3 \cdot \mathbf{n}^{+/-}$  [ms<sup>-1</sup>] is the outflow from  $\Omega_3$ ,  $h_3^{+/-}$  is a trace of the pressure head on  $\Omega_3$ ,  $h_2$  is the pressure head on  $\Omega_2$ , and  $\sigma_3^{+/-} = \sigma_{32}$  [s<sup>-1</sup>] is the transition coefficient that will be discussed later. On the other hand, the sum of the interchange fluxes  $\mathbf{q}_{32}^{+/-}$  forms a volume source on  $\Omega_2$ . Therefore  $F_2$  [ms<sup>-1</sup>] on the right hand side of (2.5) is given by

$$F_2 = \delta_2 f_2 + (q_{32}^+ + q_{32}^-). \tag{2.7}$$

The communication between  $\Omega_2$  and  $\Omega_1$  is similar. However, in the 3D ambient space, an 1D channel can join multiple 2D fractures  $1, \ldots, n$ . Therefore, we have n independent outflows from  $\Omega_2$ :

$$q_2 \cdot n^i = q_{21}^i = \sigma_2^i (h_2^i - h_1),$$

where  $\sigma_2^i = \delta_2^i \sigma_{21}$  [ms<sup>-1</sup>] is the transition coefficient integrated over the width of the fracture *i*. Sum of the fluxes forms part of  $F_1$  [m<sup>2</sup>s<sup>-1</sup>]

$$F_1 = \delta_1 f_1 + \sum_i q_{21}^i. (2.8)$$

The transition coefficients  $\sigma_d$  [m<sup>3-d</sup>s<sup>-1</sup>] are independent parameters in our setting however in practice they should be related to the conductivity in direction (or plane) perpendicular to the fracture (channel). According to [4] one can use

$$\sigma_3 = rac{2\mathbb{K}_2:oldsymbol{n}_2\otimesoldsymbol{n}_2}{\delta_2}, \sigma_2^i = rac{2\delta_2\mathbb{K}_1:oldsymbol{n}_1^i\otimesoldsymbol{n}_1^i}{\delta_1}$$

where  $n_2$  is normal to the fracture (sign doesn't matter) and  $n_1^i$  is normal to the channel that is tangential to the fracture i.

In order to obtain unique solution we have to prescribe boundary conditions. Currently we support three basic types of boundary condition. Consider disjoint decomposition of the boundary

$$\partial\Omega_d=\Gamma_d^D\cap\Gamma_d^N\cap\Gamma_d^R$$

into Dirichlet, Neumann, and Robin parts. We prescribe

$$h_d = h_d^D \qquad \text{on } \Gamma_d^D, \tag{2.9}$$

$$\boldsymbol{q}_d \cdot \boldsymbol{n} = q_d^N \qquad \qquad \text{on } \Gamma_d^N, \tag{2.10}$$

$$\mathbf{q}_d \cdot \mathbf{n} = \sigma_d^R (h_d - h_d^R) \qquad \text{on } \Gamma_d^R. \tag{2.11}$$

where  $h_d^D$ ,  $h_d^R$  is the prescribed pressure head [m], which alternatively can be prescribed through the piezometric head  $H_d^D$ ,  $H_d^R$  respectively.  $q_d^N$  is the prescribed surface density of the boundary outflow [m<sup>4-d</sup>s<sup>-1</sup>], and  $\sigma_d^R$  is the transition coefficient [m<sup>3-d</sup>s<sup>-1</sup>]. The problem is well posed only if there is Dirichlet or Robin boundary condition on every component of the set  $\Omega_1 \cup \Omega_2 \cup \Omega_3$  and  $\sigma_d > 0$  for d = 2, 3.

For unsteady problems one has to specify initial condition in terms of initial pressure head  $h_d^0$  or initial piezometric head  $H_d^0$ .

## 2.2 Transport of substances

Flow123d can simulate transport of substances dissolved in water. The transport mechanism is governed by the *advection*, and the *hydrodynamic dispersion*. Moreover the substances can move between ground and fractures.

In the domain  $\Omega_d$  of dimension  $d \in \{1, 2, 3\}$ , we consider a system of mass balance equations in the following form:

$$\delta_d \partial_t (\vartheta c^i) + \operatorname{div}(\boldsymbol{q}_d c^i) - \operatorname{div}(\vartheta \delta_d \mathbb{D}^i \nabla c^i) = F_S + F_C(c^i) + F_R(c^1, \dots, c^s). \tag{2.12}$$

The principal unknown is the concentration  $c^i$  [kgm<sup>-3</sup>] of a substance  $i \in \{1, ..., s\}$ , which means weight of the substance in unit volume of the water. Other quantities are:

- $\vartheta$  [] is the porosity, i.e. fraction of space occupied by water and the total volume.
- The hydrodynamic dispersivity tensor  $\mathbb{D}^i$  [m<sup>2</sup>s<sup>-1</sup>] has the form

$$\mathbb{D}^i = D_m^i au \mathbb{I} + |oldsymbol{v}| \left( lpha_T^i \mathbb{I} + (lpha_L^i - lpha_T^i) rac{oldsymbol{v} imes oldsymbol{v}}{|oldsymbol{v}|^2} 
ight),$$

which represents (isotropic) molecular diffusion, and mechanical dispersion in longitudal and transversal direction to the flow. Here  $D_m^i$  [m<sup>2</sup>s<sup>-1</sup>] is the molecular diffusion coefficient of the *i*-th substance (usual magnitude in clear water is  $10^{-9}$ ),  $\tau = \vartheta^{1/3}$  is the tortuosity (by [5]),  $\alpha_L^i$  [m] and  $\alpha_T^i$  [m] is the longitudal dispersivity and the transversal dispersivity, respectively. Finally,  $\boldsymbol{v}$  [ms<sup>-1</sup>] is the microscopic water velocity, related to the Darcy flux  $\boldsymbol{q}_d$  by the relation  $\boldsymbol{q}_d = \vartheta \delta_d \boldsymbol{v}$ . The value of  $D_m^i$  for specific substances can be found in literature (see e.g. [1]). For instructions on how to determine  $\alpha_L^i$ ,  $\alpha_T^i$  we refer to [2, 3].

- $F_S$  [kgm<sup>-d</sup>s<sup>-1</sup>] is the density of concentration sources.
- $F_C(c^i)$  [kgm<sup>-d</sup>s<sup>-1</sup>] is the density of concentration sources due to exchange between regions with different dimensions, see (2.15) below.
- The reaction term  $F_R(...)$  [kgm<sup>-d</sup>s<sup>-1</sup>] is currently neglected.

Initial and boundary conditions. At time t = 0 the concentration is determined by the initial condition

$$c^i(0, \boldsymbol{x}) = c_0^i(\boldsymbol{x}).$$

The physical boundary  $\partial \Omega_d$  is decomposed into two parts:

$$\Gamma_D(t) = \{ \boldsymbol{x} \in \partial \Omega_d \, | \, \boldsymbol{q}(t, \boldsymbol{x}) \cdot \boldsymbol{n}(\boldsymbol{x}) < 0 \},$$
  
$$\Gamma_N(t) = \{ \boldsymbol{x} \in \partial \Omega_d \, | \, \boldsymbol{q}(t, \boldsymbol{x}) \cdot \boldsymbol{n}(\boldsymbol{x}) \ge 0 \},$$

where n stands for the unit outward normal vector to  $\partial\Omega_d$ . On the inflow part  $\Gamma_D$ , the user must provide Dirichlet boundary condition for concentrations:

$$c^{i}(t, \boldsymbol{x}) = c_{D}^{i}(t, \boldsymbol{x}) \text{ on } \Gamma_{D}(t),$$

while on  $\Gamma_N$  we impose homogeneous Neumann boundary condition:

$$-\vartheta \delta_d \mathbb{D}^i(t, \boldsymbol{x}) \nabla c^i(t, \boldsymbol{x}) \cdot \boldsymbol{n}(\boldsymbol{x}) = 0 \text{ on } \Gamma_N(t).$$

Communication between dimensions. Transport of substances is considered also on interfaces of physical domains with adjacent dimensions (i.e. 3D-2D and 2D-1D, but not 3D-1D). Denoting  $c_{d+1}$ ,  $c_d$  the concentration of a given substance in  $\Omega_{d+1}$  and  $\Omega_d$ , respectively, the comunication on the interface between  $\Omega_{d+1}$  and  $\Omega_d$  is described by:

$$q^{c} = \delta_{d+1}\sigma^{c}(\vartheta_{d+1}c_{d+1} - \vartheta_{d}c_{d}) + \begin{cases} q^{w}c_{d+1} & \text{if } q^{w} \ge 0, \\ q^{w}c_{d} & \text{if } q^{w} < 0, \end{cases}$$
 (2.13)

where

- $q^c$  [kgm<sup>-d</sup>s<sup>-1</sup>] is the density of concentration flux from  $\Omega_{d+1}$  to  $\Omega_d$ ,
- $\sigma^c$  [ms<sup>-1</sup>] is a transition parameter. Its nonzero value causes mass exchange between dimensions whenever the concentrations differ. It is recommended to set either  $\sigma^c = 0$  (exchange due to water flux only) or, similarly as in (2.1),

$$\sigma^cpprox rac{\delta_{d+1}}{\delta_d}\mathbb{D}:m{n}\otimesm{n}.$$

•  $q^w$  [m<sup>3-d</sup>s<sup>-1</sup>] is the water flux from  $\Omega_{d+1}$  to  $\Omega_d$ , i.e.  $q^w = \boldsymbol{q}_{d+1} \cdot \boldsymbol{n}_{d+1}$ .

Equation (2.13) is incorporated as the total flux boundary condition for the problem on  $\Omega_{d+1}$  and a source term in  $\Omega_d$ :

$$-\vartheta \delta_{d+1} \mathbb{D} \nabla c_{d+1} \cdot \boldsymbol{n} + q^w c_{d+1} = q^c, \tag{2.14}$$

$$F_C^d = q^c. (2.15)$$

## Chapter 3

## File formats

## 3.1 Input files

In this section we shall describe whole structure of the program input, namely the structure of the root input file. File formats of other files used for input of the mesh or large field data (e.g. the GMSH file format) are described in separate sections. The program input consists of the root input file given as the parameter on the command line and possibly several other files with large input data. The root input file is in so called CON file format that is a slight extension of the JSON file format.

In this section we shall describe format of the input files. At first, we specify syntax of an extension to the JSON file format. Then we set rules for input of more specific data constructs. We continue by description of general scheme for input of boundary conditions and material time-space variable data. And finally, we describe setting of particular equations and their solvers.

The aim of this draft is twofold. First, we want to outline the way how to translate current input file format (in version 1.6.5) into the new one without extending the existing functionality. Second, we want to propose a new way how to input general boundary and material data. Desired features are:

- input simple data in simple way
- possibility to express very complex input data
- possibility to generate data automatically, and input very large input sets
- input interface that provides uniform access to the data in program independent of the input format

#### [ ... something else?]

As this is a draft version there are lot of remarks, suggestions and questions in square brackets. Some keys are marked OBSOLETE, which means that we want to replace them by something else.

#### 3.1.1 CON file format

The root input file is in the Humanized JSON file format. That is the JSON file format with few syntax extensions and several semantic rules particular to Flow123d. The syntax extensions are

- 1. You can use one line comments using hash #.
- 2. The quoting of the keys is optional if they do not contain spaces (holds for all Flow keys).
- 3. You can use equality sign = instead of colon : for separation of keys and values in JSON objects.
- 4. You can use any whitespace to separate tokens in JSON object or JSON array.

The aim of these extensions is to simplify writing input files manually. However these extensions can be easily filtered out and converted to the generic JSON format. (This way it can be also implemented in Flow123d.)

For those who are not familiar with the JSON file format, we give the brief description right here. The full description can be found at http://www.json.org/. However, we use term record in the place of the JSON object in order to distinguish JSON object, which is merely a data structure written in the text, and the C++ object, i.e. instance of some class.

#### 3.1.2 Humanized JSON

The JSON format consists of four kind of basic entities: null token, true and false tokens, number, string. Number is either integer or float point number possibly in the exponential form and string is any sequence of characters quoted in "" (backslash \ is used as escape character and Unicode is supported, see full specification for details).

In the following, we mean by white space characters: space, tab, and new line. In particular the newline character (outside of comment or quoting) is just the white space character without any special meaning.

The basic entities can be combined in composed entities, in a *record* or in an *array*. The *record* is set of assignments enclosed in the curly brackets

```
{
    #basic syntax
    "some_number":124,
    "some_string":"Hallo",
    "some_subrecord":{},
    "some_array":[],

#extended syntax
    non_quoted_key_extension=123,
    separation_by_whitespace="a" sbw_1="b"
    sbw_2="c"
}
```

One assignment is a pair of the *key* and the *value*. *Key* is *string* or token matching regexp

[a-zA-Z\_] [a-zA-Z\_0-9]\*. Value is basic or composed entity. The key and the value are separated by the colon (generic syntax) or equality sign (extended syntax). Pairs are separated by a comma (generic syntax) or sequence of white space characters (extended syntax). The values stored in the record are accessed through the keys like in an associative array. Records are usually used for initialization of corresponding classes.

The second composed entity is the *array* which is sequence of (basic or composed) entities separated by comma (generic syntax) or whitespace sequence (extended syntax) and enclosed in the square brackets. The values stored in the array are accessed through the order. The Flow reader offers either initialization of a container from JSON array or a sequential access. The latter one is the only possible access for the included arrays, which we discuss later.

On any place out of the quoted string you can use hash mark # to start a one line comment. Everything up to the new line will be ignored and replaced by single white space.

[What about multiple line strings? (Should be allowed)]

#### 3.1.3 CONSpecial keys

Apart from small extensions of JSON syntax, we impose further general rules on the interpretation of the input files by Flow123d reader. First, the capital only keywords have a special meaning for Flow JSON reader. On the other hand, we use only small caps for keys interpreted through the reader. The special keywords are:

#### TYPE:

```
TYPE= <enum>
```

The **<enum>** is particular semantic construct described later on. When appears in the record, it specifies which particular class to instantiate. This only has meaning if the record initializes an abstract class. In consistency with the source code, we shall call such records *polymorphic*.

In fact we consider that every record is of some *type* at least implicitly. The *type* of the record is specification of the keys that are interpreted by the program Flow123d. At some places the program assumes a record of specific *type* so you need not to specify TYPE key in those records.

#### INCLUDE\_RECORD:

This is a simple inclusion of another file as a content of a record:

```
{
    INCLUDE_RECORD = "<file name>"
}
```

#### INCLUDE\_ARRAY:

```
array=
{
          INCLUDE_ARRAY = "<file name>"
          FORMAT = "<format string>"
}
```

The reader will substitute the include record by a sequentially accessible array. The file has fixed number of space separated data fields on every line. Every line becomes one element in the array of type record. Every line forms a record with key names given by the <format string> and corresponding data taken form the line.

The key difference compared to regular JSON arrays is that included arrays can be accessed only sequentially within the program and thus we minimize reader memory overhead for large input data. The idea is to translate raw data into structured format and use uniform access to the data.

Basic syntax for format string could be an array of strings — formats of individual columns. Every format string is an address of key that is given the column. Onother possibility is to give an arbitrary JSON file, where all values are numbers of columns where to take the value.

```
[... better specify format string]
```

[Possible extensions: - have sections in the file for setting time dependent data - have number of lines at the beginning - have variable format - allow vectors in the 'line records']

#### REFERENCE:

```
time_governor={
   REF=<address>
}
```

This will set key time\_governor to the same value as the entity specified by the address. The address is an array of strings for keys and integers for indices. The address can be absolute or relative identification of an entity. The relative address is relative to the entity in which the reference record is contained. One can use string ".." to move to parent entity and string "//" to move to the root record of current file. Indices in address starts from 0.

For example assume the file

```
outer_record={
          output_file="x_out"
          inner_record={
                output_file={REF=["..","output_file"]} # value "x_out"
        }
          x={REF="/array/2/x"} # value "3"
        f_name={REF=["//","mesh","file_name"]} # value "xyz"
}
```

Concept of addres should be better explained and used consistently in reader interface.

#### 3.1.4 Semantic rules

#### Implicit creation of composed entities

Consider that there is a type of record in which all keys have default values (possibly except one). Then the specification of the record type can contain a default key. Then user can use the value of the default key instead of the whole record. All other keys apart from the default key will be initialized by default values. This allows to express simple tasks by simple inputs but still make complex inputs possible. In order to make this working, developers should provide default values everywhere it is possible.

Similar functionality holds for arrays. If the user sets a non-array value where an array is expected the reader provides an array with a unique element holding the given value. See examples in the next section for application of these two rules.

#### Enum construct

Enum values can be integers or strings from particular set. Strings should be preferred for manual creating of input files, while the integer constants are suitable for automatic data preparation.

The input reader provides a way how to define names of members of an enum class and then initialize this enum class from input file. [Need better description]

#### String types

For purpose of this documentation we distinguish several string types with particular purpose and treatment. Those are:

input filename This has to be valid absolute or relative path to an existing file. The string can contain variable \${INPUT} which will be replaced by path given at command line through parameter -i.

[In order to allow input of time dependent data in individual files, we should have also variable \${TIME\\_LEVEL} From user point of view this is not property of general input filename string, however in implementation this should be done in the same way as \${INPUT}. ]

[? Shall we allow both Windows and UNIX slashes?]
[Developers should provide default names to all files. ]

output filename This has to be relative path. The path will be prefixed by the path given at command line through the parameter -o. In some cases the path will be also postfixed by extension of particular file format.

formula Expression that will be parsed and evaluated runtime. Documentation of particular key should provide variables which can appear in the expression, however in general it can be function of the space coordinates  $x,\ y,\ z$  and possibly also function of time t. For full specification of expression syntax see documentation of FParser library: http://warp.povusers.org/FunctionParser/fparser.html# literals

text string Just text without particular meaning.

#### Record types

A record type like particular definition of a class (e.g. in C++). One record type serves usually for initialization of one particular class. From this point of view one record type is set of keys that corresponding class can read.

For purpose of this manual the record type is given by specification of record's keys, their types, default values and meanings. In the next two sections, we describe all record types that forms input capabilities of Flow123d. Description of a record type has form of table. Table heading consists of the name of the record type. Then for every key we present name, type of the value, default value and text description of key meaning. Type of the value can be record type, array of record types, double, integer, enum or string type. Default value specification can be:

**none** No default value given, but input is mandatory. You get an error if you don't set this key.

**null** null value. No particular default value, but you need not to set the key. Usually means feature turned off.

**explicit value** For keys of type: string, double, integer, or enum, the default value is explicit value of this type.

type defaults For keys of some record type we let that record to set its default values.

[? polymorphic record types]

## 3.2 Record types for input of data fields

In this section we describe record types used to describe general time-space scalar, vector, or tensor fields and records for prescription of boundary conditions. Since one possibility how to prescribe input data fields is by discrete function spaces on computational mesh, we begin with mesh setting.

## 3.2.1 Mesh type

The mesh record and should provide a mesh consisting of points, lines, triangles and tetrahedrons in 3D space and further definition of boundary segments and element connectivity.

record type: Mesh

file = < input filename>

DEFAULT: mesh.msh

The file with computational mesh in the ASCII GMSH format.

http://geuz.org/gmsh/doc/texinfo/gmsh.html#MSH-ASCII-file-format

boundary\_segments = < array of boundary segments > DEFAULT: null optional

The set of 0,1, or 2 dimensional boundary faces of the mesh should be partitioned into boundary segments in order to prescribe unique boundary condition on every boundary face. The segments numbers are assigned to boundary faces by iterating through the array. Initially every boundary face has segment number 0. Every record in the array use "auxiliary" physical domains, elements or direct face specification to specify some set of boundary faces. The new segment number is assigned to each face in the set, possibly overwriting previous value.

Physical domains or its parts that appears in the boundary segment definitions are removed form the computational mesh, however, the element numbers of removed elements are stored in the corresponding boundary face and can be used to define face-wise approximations of functions with support on the boundary.

neighbouring = <input file name>

DEFAULT: neigbours.flw

This should be removed as soon as we integrate ngh functionality into flow.

record type: Boundary segment

index = < integer >

DEFAULT: index in outer array

The index of boundary segment can be used later to prescribe particular type of boundary condition on it. Indices must be greater or equal to 1 and should form more or less continuous sequence. The zero boundary segment is reserved for remaining part of the boundary. By default we assign indices to boundary segments according to the order in their array in mesh, i.e. index (counted form 0) plus 1.

physical\_domains = <array of integers>

DEFAULT: null optional

Numbers of physical domains which form the boundary segment. All elements of these physical domains will be removed from actual computational mesh.

elements = < array of integers>

DEFAULT: null optional

The array contains element numbers which should be removed from computational mesh and added to boundary segment.

 $sides = \langle array \ of \ integer \ pairs \rangle$ 

DEFAULT: null optional

The array contains numbers of elements which outer faces will be added to the boundary segment or pairs [element, side\_on\_element] identifying individual faces

### 3.2.2 Time-space field type

A general time and space dependent, scalar, vector, or tensor valued function is given by array of *steady field data*, i.e. time slices. The time slice contains array of *space functions* for individual materials. Then, the *space function* can by either analytical (given by formula) or numerical, given by type of discrete space and array of *elemental functions*. *Elemental function* is just array of values for every degree of freedom on one element.

The function described by this type is tensor values in general and dimensions of this tensor should be specified outside of the function data. For example in description of Transport record type you should specify that function for initial condition is vector valued with vector size equal to number of substances. It is like template for Timespace field type parametrized by shape of the value tensor given by number of lines N and columnes N.

#### record type: Steady field data

 $time = \langle double \rangle$ 

Start time for the spatial filed data.

 $time_interpolation = \langle enum \rangle$  DEFAULT: constant

time interpolation enum cases:

constant=0 Keeps constant data until next time cut.

linear=1 Linear interpolation between current time cut and the next one.

DEFAULT: -Inf

materials = < array of Steady spatial functions> DEFAULT: null optional

record type: Space function

material = <integer> DEFAULT: 0

Material filter. The function has nonzero value only on elements with given material number. Function with filter 0 takes place for all materials where no function is set.

analytic = < multi-array of function formulas > DEFAULT: null optional

The shape of the multi-array is given by rank of the value of the function. Since formula parser can deal only with scalar functions, we have to specify individual members of resulting tensor. Formulas can contain variables x, y, z, and t. The formula is used until the next time slice and is evaluated for every solved time step (can depend on equation).

Instead of constant formulas one can use double values. Usage of formulas or doubles need not to be uniform over the tensor.

numeric\_type = < enum>
DEFAULT: None

FE space enum cases:

None=0 Use analytic function.

P0=1 Zero order polynomial on element.

Currently we support only P0 base functions for data.

```
numeric = < array of element functions>
```

DEFAULT: empty array

Usually, this element-wise array should by included from an external file through INCLUDE\_ARRAY construct.

#### record type: Element function

```
element_id = <integer>
```

DEFAULT: null optional

Element ID in the mesh. By default the element is identified by the index in the array of element function.

```
values = < multi-array of doubles>
```

DEFAULT: null mandatory

Values for degrees of freedom of the base functions on the element. Currently we support only P0 functions which are given by value in the barycenter of the element. In general the value can be tensor, i.e. array of arrays of doubles. However, in accordance to simplification rules, you can use only array of doubles for vector functions or mere double for scalar functions.

[ tensor/vector valued element function should be given also as simple array of DOF values. But we have to provide ordering of tensor products of FE spaces]

[ As follows from next examples, there is no way how to simply set simply tensors. We can introduce automatic conversion form scalar to vector (constant vector) and vector to tensor (diagonal tensor). ]

[ we should also allow 'in place' array includes to simplify material tables etc.]

[How to allow parallel input of field data?]

[Should be there explicit mesh reference in the field specification?]

Examples:

```
constant_scalar_function = 1.0
# is same as
constant_scalar_function = {
  time = -Inf,
  time_interpolation= constant,
  materials = [
    {
      rank=0
      numeric_type=None
      analytic=1.0
                          # the only key withou default value
    }
  ]
}
conductivity_tensor =
  [\{ material = 1, \}]
```

```
rank = 2,
   analytic = [[1.0, 0.0, 0.0], [0.0, 1.0, 0.0], [0.0, 0.0, 1.0]]
},
{ material = 2,
   rank = 2,
   analytic = [[10.0, 0.0, 0.0], [0.0, 10.0, 0.0], [0.0, 0.0, 10.0]]
}
```

## 3.2.3 Boundary conditions

Input of boundary conditions is similar to the Time-space fields. For description of one time slice we have type *steady boundary data*. This contains array of *boundary conditions* for individual boundary segments. *Boundary condition* is given by type and parameters that are analytic or numeric functions. However, numeric functions are considered only on boundary elements.

#### record type: steady boundary data

 $time = \langle double \rangle$  DEFAULT: 0.0

Time when the BC should be applied.

bc = < array of boundary conditions> DEFAULT: empty

#### record type: boundary condition

boundary\_segment =  $\langle integer \rangle$  DEFAULT: 0

Boundary segment where the boundary condition will be applied.

bc\_type = < enum> DEFAULT: dirichlet

Currently there are just three types of boundary condition common to all equations, but some equations can implement some specific boundary conditions. Common boundary condition types are **BC types** enum cases:

dirichlet=0

neumann=1

newton=2 (also known as Robin boundary condition)

value = < space function> DEFAULT: type defaults

Prescribed value for Dirichlet boundary condition and Newton boundary condition, the normal flux for the Neumann boundary condition. Key material of space function is irrelevant.

mean\_value = < scalar or vector constant> DEFAULT: 0

Prescribes flux for Neumann boundary condition by total flux over the boundary segment. If both *value* and *mean\_value* keys are set, we use only *value* key. [How this interact with fracture opening?]

newton\_coef = < scalar space function> DEFAULT: type defaults

Coefficient that appears in the Newton boundary condition. Key material of space function is irrelevant.

E.g. denoting u the unknown scalar or vector field and  $\partial_n u$  density of the normal flux of this field, the meaning of keys value and newton\_coef is following:  $\mathbf{v} \nabla v$ 

u := value for Dirichlet boundary  $A\nabla u \cdot \boldsymbol{n} := value$  for Neumann boundary  $A\nabla u \cdot \boldsymbol{n} := newton_coef(u - value)$  for Newton boundary

Specific interpretation of the boundary conditions should be described in particular equations.

[How to allow both analytic and numerical functions here?]

[In order to allow changing BC type in time, the structure has to be: time array of BC segments array of BC type with data alternatively we can have just one array of BC patches, where one patch has: time, BC segment, BC type, BC data patches with non monotone time will be scratched]

[need vector valued Dirichlet (and Neuman, and Newton) for Transport boundary conditions]

[More examples...]

## 3.3 Other record types recognized by Flow123d

## 3.3.1 Record types not related to equations

record type: Root record

system = <system type>
DEFAULT: type defaults

Record with application setting.

problem = problem type>
DEFAULT: null mandatory

Record with numerical problem to solve.

material = <input filename> DEFAULT: material.flw

Old material file still used for initialization of data fields in equations. This should be replaced by material database type. Then certain input data fields in equations can be constructed from material informations. Main obstacle are various adsorption algorithms depending on material number.

Only these keys are recognized directly at main level, however you can put here your own keys and then reference to them. For example mesh is part of problem type record, but you can put it on the main level and use reference inside problem.

[Should we put problem record to the main level?]

[Should we provide "material database"? Possibility to specify properties of individual materials and use them to construct field data for equations.]

Description. lkajs eflakd flakds fropi pwnfvpweiurv evm qoiefmv lksdm vqoierrv lakfdsvkjweroivlksdmvaoirrf vm a v ve lkvqekfv jf ais i qkd ffo qk dfjhaopdif u wqwddff if j khr if

```
pause\_after\_run = < bool >
```

DEFAULT: no

Wait for press of Enter after run. Good for Windows users, but dangerous for batch computations. Should be rather an command-line option.

```
verbosity = < bool >
```

DEFAULT: no

Turns on/off more verbose mode.

```
output_streams = <output stream>
```

DEFAULT: null optional

One or more output data streams. There are two predefined output streams:

vtk ascii stream:

```
{
   name="dafault_vtk_ascii"
   file="flow_output"
   type="vtk_ascii"
}

GMSH ascii stream:
{
   name="dafault_gmsh_ascii"
   file="flow_output"
   type="gmsh_ascii"
}
```

Possibly here could be variables for check-pointing, debugging, timers etc.

#### record type: Output stream

```
name = \langle string \rangle
```

DEFAULT: null mandatory

Name of the output stream. This is used to set output stream for individual output data.

```
file = < output filename string>
```

DEFAULT: stream name

File name of the output file for the stream. The file name should be without extension, the correct extension will be appended according to the format type.

```
format = \langle enum \rangle
```

DEFAULT: vtk\_ascii

output format enum cases:

```
vtk_ascii=0
```

gmsh\_ascii=1

```
precision = < integer>
```

DEFAULT: 8

Number of valid decadic digits to output floating point data into the ascii file formats.

copy\_file = <output filename string>

DEFAULT: null optional

Optionally one can set copy file to output data into to different file formats.

 $copy\_format = \langle enum \rangle$ 

DEFAULT: null optional

copy\_precision = <integer>

DEFAULT: 8

#### 3.3.2 Equation related record types

Up to now there is only one problem type: TYPE=sequential\\_coupling, but in near future we should introduce full coupling e.g. for density driven flow.

The sequential coupling problem has following keys:

#### record type: Sequential coupling implements Problem type

 $description = \langle string \rangle$ 

DEFAULT: null optional

Short text description of solved problem. Now it is only reported on the screen, but could be written into output files or used somewhere else.

 $mesh = < mesh \ type >$ 

DEFAULT: type defaults

The computational mesh common for both coupled equations.

time\_governor = < time governor type>

DEFAULT: type defaults

Common time governor setting. [Future: allow different setting for each equation]

 $primary_equation = < darcy flow type>$ 

DEFAULT: type defaults

Independent equation.

 $secondary_equation = \langle transport \ type \rangle$ 

DEFAULT: null optional

Equation with some data dependent on the primary equation.

#### record type: Time governor

 $init\_time = < double >$ 

DEFAULT: 0.0

Time when an equation starts its simulation.

 $time\_step = < double>$ 

DEFAULT: 1.0

Initial time step.

 $end\_time = < double >$ 

DEFAULT: 1.0

End time for an equation.

This record type should initialize TimeGovernor class, but there are still questions about steady TimeGovernor and if we allow user setting for other parameters.

There are three subtypes steady saturated MH, unsteady saturated MH, unsteady saturated LMH The common keys are:

record type: **Darcy flow**(abstract type)

 $TYPE = \langle enum \rangle$ 

DEFAULT:

There are three implementations of Darcy flow. Most keys are common but unsteady solvers accept some extra keys. **darcy flow type** enum cases:

steady\_MH=0

unsteady\_LMH=1

unsteady\_MH=2

sources = < time-space field>

DEFAULT: 0

Density of water sources. Scalar valued field (1x1 tensor).

sources\_file = <input file name>

DEFAULT: null optional

File with sources in old format. (OBSOLETE)

source\_formula = <space function>

DEFAULT: 0

Space function that prescribes water source.

coef\_tensor = <tensor steady field>

DEFAULT: 1.0

Conductivity 3x3 tensor. [Should be always 3x3 and then restricted on 2d and 1d fractures.]

boundary\_condition = <array of steady boundary data> DEFAULT: null mandatory New scheme for setting boundary conditions.

boundary\_file = <input file name>

DEFAULT: null mandatory

File with boundary conditions in old format. (OBSOLETE)

 $solver = \langle solver \ type \rangle$ 

DEFAULT: type defaults

n\_schurs = < integer>

DEFAULT: 2

Number of Schur complements to make. Valid values are 0,1,2.

 ${\tt output} = <\! darcy \ flow \ output \ type >$ 

DEFAULT: typ defaults

This is just sub record to separate output setting.

 $initial = \langle steady \ data \ type \rangle$ 

DEFAULT: null mandatory

Initial condition. Scalar valued field (1x1 tensor). (for unsteady only)

initial\_file = <input file name>

DEFAULT: null mandatory

File with initial condition in old format. (OBSOLETE)

 $storativity = \langle steady \ data \ type \rangle$ 

DEFAULT: null mandatory

Storativity coefficient. Scalar valued field (1x1 tensor). (for unsteady only)

record type: Darcy flow output

 $save\_step = < double>$ 

DEFAULT: null optional

Time step between outputs.

output\_times = < array of doubles> DEFAULT: null optional

Force output in prescribed times. Can be combined with regular otuptu given

by save\_step.

velocity\_p0 = <output stream name>
DEFAULT: default\_vtk\_ascii

pressure\_p0 = < output stream name> DEFAULT: default\_vtk\_ascii

pressure\_p1 = < output stream name> DEFAULT: default\_vtk\_ascii

### 3.3.3 Solver type

record type: **Solver type** (abstract)

 $TYPE = \langle enum \rangle$  DEFAULT: petsc

solver types enum cases:

petsc=0 Use any PETSc solver for MPIAIJ matrices.

bddc=1 Use BDDC solver (need not to work with every equation).

 $accuracy = \langle double \rangle$  DEFAULT: solvers defaults

Absolute residual tolerance.

 $max_it = \langle integer \rangle$  DEFAULT: 1000

Maximum number of outer iterations.

parameters = < string> DEFAULT: null optional

String with options for PETSc solvers.

export\_to\_matlab = < bool> DEFAULT: no

Save every solved system in matlab format. Useful for debugging and numerical

experiments.

## 3.3.4 Transport type

record type: Transport type

 $TYPE = \langle enum \rangle$  DEFAULT:

Two types are sofar possible. The second type is for advection-diffusion equation which needs implicit solver. **transport type** enum cases:

TransportOperatorSplitting=0

AdvectionDiffusion\_DG=1

 $sorption = \langle bool \rangle$  DEFAULT: no

 $dual\_porosity = \langle bool \rangle$  DEFAULT: no

transport\_reactions = <bool> DEFAULT: no

What kind of reactions is this? Age of water?

sigma = < double >

DEFAULT: 0

Coefficient of diffusive transfer through fractures.

 $alpha_1 = < double >$ 

DEFAULT: 0

Longitudal dispersivity.

 $alpha_t = < double >$ 

DEFAULT: 0

Transversal dispersivity.

 $d_m = \langle double \rangle$ 

DEFAULT: 1e-6

Molecular diffusivity.

 $dg_penalty = < double>$ 

DEFAULT: 0

Penalty parameter influencing the discontinuity of the solution.

 ${\tt reactions} = <\!\! {\it reaction type}\!\!>$ 

DEFAULT: null optional

Currently only Semchem is supported. [Interface to Phreaq ...]

 $decays = \langle array \ of \ decays \rangle$ 

DEFAULT: null optional

 $substances = \langle array \ of \ strings \rangle$ 

DEFAULT: null mandatory

Names for transported substances. Number of substances is given implicitly by size of the array.

 $initial = \langle steady \ data \ type \rangle$ 

DEFAULT: null mandatory

Vector valued initial condition for mobile phase of all species.

initial\_others = <steady data type>

DEFAULT: null optional

Tensor valued initial condition for immobile, mobile-sorbed, immobile-sorbed phases and all species. (3 x n\_substances). [alternatively have separate key for each phase]

initial\_file = <input file name>

DEFAULT: null mandatory

File with initial condition in old format. (OBSOLETE)

boundary\_condition = <array of steady boundary data> DEFAULT: null mandatory New scheme for setting boundary conditions.

boundary\_file = <input file name>

DEFAULT: null mandatory

File with boundary condition in old format. (OBSOLETE) For time dependent boundary conditions, the filename is postfixed with number of time level.

 $bc\_times = \langle array \ of \ doubles \rangle$ 

DEFAULT: null optional

Times for changing boundary conditions. If you set this variable, you have to prepare a separate file with boundary conditions for every time in the list. Filenames for individual time level are formed from BC filename by appending underscore and three digits of time level number, e.g. transport\_bcd\_000, transport\_bcd\_001, etc. (OBSOLETE)

output = <transport output>

DEFAULT: type defaults

### record type: Transport output

record type. Transport output				
$ exttt{save\_step} = < double>$	DEFAULT: null optional			
Time step between outputs.				
${\tt output\_times} = <\!\!\mathit{array} \ \mathit{of} \ \mathit{doubles}\!\!>$	DEFAULT: null optional			
Force output in prescribed times. Can be by save_step.	combined with regular otuptu given			
$mobile\_p0 = < output \ stream \ name >$	DEFAULT: default_vtk_ascii			
${\tt immobile\_p0} = <\! output \ stream \ name \!\!>$	DEFAULT: default_vtk_ascii			
${\tt mobile\_sorbed\_p0} = <\! output \ stream \ name \!\! >$	DEFAULT: $default_vtk_ascii$			
${\tt immobile\_sorbed\_p0} = <\! \mathit{output\ stream\ name} \!>$	DEFAULT: default_vtk_ascii			
${\tt mobile\_p1} = <\! output \ stream \ name \!\! >$	DEFAULT: default_vtk_ascii			
${\tt immobile\_p1} = <\! output \ stream \ name \!\!>$	DEFAULT: default_vtk_ascii			
${\tt mobile\_sorbed\_p1} = <\! output \ stream \ name \!\!>$	DEFAULT: default_vtk_ascii			

 $\verb|immobile_sorbed_p1| = < output \ stream \ name > \qquad \mathsf{DEFAULT:} \ default\_vtk\_ascii$ 

#### record type: Decay chain

 $substance_ids = \langle array \ of \ integers \rangle$ 

**DEFAULT:** empty

Sequence of N ids of transported substances defining isotopes contained in the decay chain under consideration.

nr\_of\_children = < array of integers>

DEFAULT: either empty or filled up with ones

Number of children of each vertex (belonging to one of isotopes) in a simple graph describing considered decay chain. (NOT USED, YET.)

indices\_of\_children = < array of integers>

DEFAULT: either emmpty or filled up with substan-

Containes identifiers of children of vertex. Children are assigned to vertices through the use of numbers listed in nr\_of\_children. (NOT USED, YET.)

 $half\_lives = \langle array \ of \ doubles \rangle$ 

DEFAULT: empty

This array containes N-1 half-lives belonging to isotopes contained in the array substance ids. If there are no bifurcation key specified, the decay chain is linear  $1 \to 2 \to 3$ . If there is the bifurcation key, the decay chain is branched  $1 \to 2, 1 \to 3$ . (Temporary solution.)

 $bifurcation = \langle array \ of \ double \rangle$ 

DEFAULT: null optional

It should have as many items as the array indices\_of\_children (N-1). It defines relative part of parental contribution in the case of division of decay chain into more branches. (NOT USED, YET.)

Contains N-1 probabilities for individual branches of the bifurcation decay. (Temporary solution.) They should sum to one.

#### record type: First order reactions

 $substance_ids = \langle array\_of\_integers \rangle$ 

**DEFAULT:** empty

Sequence of K ids describing a set of consequtive kinetic reactions of the first order. It is meant to enable simulation of  $A \to B \to C \to \dots \to Z$  set of reactions easily. (NOT USED, YET.)

 $kinetic\_constants = \langle array \ or \ doubles \rangle$ 

DEFAULT: filled up with 0.0s

Sequence of K-1 doubles defining kinetic constants of partial reactions from the set defined in substance\_ids. (NOT USED, YET.)

nr\_of\_children = <array of integer>

DEFAULT: filled up with 1.0s

Number of children of each vertex (belonging to one of species) in a simple graph describing considered first order reactions. (NOT USED, YET.)

indices\_of\_children = < array of integers>

DEFAULT: either emmpty or filled up with substan-

Containes identifiers of children of vertex. Children are assigned to vertices throuh the use of numbers listed in nr\_of\_children. (NOT USED, YET.)

bifurcation = <array of double>

DEFAULT: null optional

It should have as many items as the array indices\_of\_children (K-1). It defines relative part of parental contribution in the case of division of first order reactions describing graph into more branches. (NOT USED, YET.)

 $kinetic_konstant = < double >$ 

DEFAULT: 0.0

Defines kinetic konstant which describes a simple reaction of the type  $A \to B$ .

substance\_ids = <array of integers>

DEFAULT: empty

Contains 2 identifiers of subsatraces (species) which are taking part in considered reaction.

#### record type: Simple reactions

 $decay\_chains = \langle array \ of \ Decay \ chains \rangle$ 

**DEFAULT:** empty

Sequence of records describing decay chains under consideration. (NOT USED, YET.)

first\_order\_reactions = < array of first order reactions> DEFAULT: empty

Sequence of records describing first order reactions under consideration. (NOT USED, YET.)

 $pade_nominator_degree = < integer>$ 

DEFAULT: 2

This number defines the degree of matrix polynomial appearing in nominator of Pade approximant of a matrix exponential.

pade\_denominator\_degree = <integer>

DEFAULT: 2

This number defines the degree of matrix polynomial appearing in denominator of Pade approximant of a matrix exponential.

## 3.4 Other input files

#### 3.4.1 Mesh file format version 2.0

The only supported format for the computational mesh is MSH ASCII format produced by the GMSH software. You can find its documentation on:

http://geuz.org/gmsh/doc/texinfo/gmsh.html#MSH-ASCII-file-format

Comments concerning Flow123d:

- Every inconsistency of the file stops the calculation. These are:
  - Existence of nodes with the same *node-number*.
  - Existence of elements with the same *elm-number*.
  - Reference to non-existing node.
  - Reference to non-existing material (see below).
  - Difference between *number-of-nodes* and actual number of lines in nodes' section.
  - Difference between *number-of-elements* and actual number of lines in elements' section.
- By default Flow123d assumes meshes with number-of-tags = 3.

tag1 is number of material (reference to .MTR file) in the element.

tag2 is number of geometry region in which the element lies.

tag3 is partition number (CURRENTLY NOT USED).

In accordance with specification of GMSH mesh format.

- Currently, line (type = 1), triangle (type = 2) and tetrahedron (type = 4) are the only supported types of elements. Existence of an element of different type stops the calculation.
- Wherever possible, we use the file extension .MSH. It is not required, but highly recomended.
- This file format can be used also for storing simple dicrete scalar or vector fields. We support output into this format (see Section 3.5)

#### 3.4.2 Neighbouring file format, version 1.0

The file is divided in two sections, header and data. The extension .NGH is highly recomended for files of this type.

```
$NeighbourFormat
1.0 file-type data-size
$EndNeighbourFormat
$Neighbours
number-of-neighbours
neighbour-number type < type-specific-data>
...
$EndNeighbours
```

where

file-type int — is equal 0 for the ASCII file format.

data-size int — the size of the floating point numbers used in the file. Usually data-size = sizeof(double).

number-of-neighbours int — Number of neighbouring defined in the file.

neighbour-number int — is the number (index) of the n-th neighbouring. These numbers do not have to be given in a consecutive (or even an ordered) way. Each number has to be given only onece, multiple definition are treated as inconsistency of the file and cause stopping the calculation.

type int — is type of the neighbouring.

<type-specific-data> — format of this list depends on the type.

## Types of neighbouring and their specific data

- type = 10 "Edge with common nodes", i.e. sides of elements with common nodes. (Possible many elements)
- type = 11 "Edge with specified sides", i.e. sides of the edge are explicitly defined. (Possible many elements)
- type = 20 "Compatible", i.e. volume of an element with a side of another element. (Only two elements)
- type = 30 "Non-compatible" i.e. volume of an element with volume of another element. (Only two elements)

type	type-specific-data	Description
10	$nelm\ eid1\ eid2\dots$	number of elements and their ids
11	$n\_sid\ eid1\ sid1\ eid2\ sid2\dots$	number of sides, their elements and local ids
20	eid1 eid2 sid2 coef	Elm 1 has to have lower dimension
30	eid1 eid2 coef	Elm 1 has to have lower dimension

coef is of the double type, other variables are ints.

## Comments concerning Flow123d:

- Every inconsistency or error in the .NGH file causes stopping the calculation. These are especially:
  - Multiple usage of the same *neighbour-number*.
  - Difference between number-of-neighbours and actual number of data lines.
  - Reference to nonexisting element.
  - Nonsence number of side.
- The variables *sid?* must be nonegative and lower than the number of sides of the particular element.

# 3.4.3 Material properties file format, version 1.0

The file is divided in two sections, header and data. The extension .MTR is highly recomended for files of this type.

```
$MaterialFormat
1.0 file-type data-size
$EndMaterialFormat
$Materials
number-of-materials
material-number material-type <material-type-specific-data> [text]
...
$EndMaterials
```

```
$Storativity
material-number < storativity-coefficient> [text]
$EndStorativity
$Geometry
material-number quemetry-type < quemetry-type-specific-coefficient > [text]
$EndGeometry
$Sorption
material-number substance-id sorption-type <sorption-type-specific-data> [text]
$EndSorption
$SorptionFraction
material-number < sorption-fraction-coefficient> [text]
$EndSorptionFraction
$DualPorosity
material-number < mobile-porosity-coefficient> < immobile-porosity-coefficient>
< nonequillibrium-coefficient-substance(0) >
\dots < nonequilibrium-coefficient-substance(n-1) > [text]
$EndDualPorosity
$Reactions
reaction-type < reaction-type-specific-coefficient> [text]
$EndReactions
where:
file-type int — is equal 0 for the ASCII file format.
data-size int — the size of the floating point numbers used in the file. Usually data-size
     = sizeof(double).
number-of-materials int — Number of materials defined in the file.
material-number int — is the number (index) of the n-th material. These numbers do
     not have to be given in a consecutive (or even an ordered) way. Each number has
     to be given only onece, multiple definition are treated as inconsistency of the file
     and cause stopping the calculation (exception $Sorption section).
material-type int — is type of the material, see table.
<material-type-specific-data > — format of this list depends on the material - type.
<storativity-coefficient> double — coefficient of storativity
geometry-type int — type of complement dimension parameter (only for 1D and 2D
     material), for 1D element is supported type 1 - cross-section area, for 2D element
     is supported type 2 - thickness.
```

- <geometry-type-specific-coefficient> double cross-section for 1D element or thickness for 2D element.
- substance-id int refers to number of transported substance, numbering starts on  $\theta$ .
- sorption-type int type 1 linear sorption isotherm, type 2 Freundlich sorption isotherm, type 3 Langmuir sorption isotherm.
- <sorption-type-specific-data > format of this list depends on the sorption type, see table.
  - Note: Section \$Sorption is needed for calculation only if *Sorption* is turned on in the *ini* file.
- <sorption-fraction-coefficient> double ratio of the "mobile" solid surface in the contact with "mobile" water to the total solid surface (this parameter (section) is needed for calculation only if Dual\_porosity and Sorption is together turned on in the ini file).
- <mobile-porosity-coefficient> double ratio of the mobile pore volume to the total volume (this parameter is needed only if Transport\_on is turned on in the ini file).
- <immobile-porosity-coefficient> double ratio of the immobile pore volume to the total pore volume (this parameter is needed only if Dual\_porosity is turned on in the ini file).
- <nonequilibrium-coefficient-substance(i)> double nonequilibrium coefficient for substance i,  $\forall i \in \langle 0, n-1 \rangle$  where n is number of transported substances (this parameter is needed only if Dual-porosity is turned on in the ini file).
- reaction-type int type 0 zero order reaction
- < reaction-type-specific-data > format of this list depends on the reaction type, see table.

material-type	material-type-specific-data	Description
11	k	$\mathbf{K} = (k)$
-11	a	$\mathbf{A} = \mathbf{K}^{-1} = (a)$
21	k	$\mathbf{K} = \left(\begin{array}{cc} k & 0 \\ 0 & k \end{array}\right)$
22	$k_x$ $k_y$	$\mathbf{K} = \begin{pmatrix} k_x & 0 \\ 0 & k_y \end{pmatrix}$
23	$k_x$ $k_y$ $k_{xy}$	$\mathbf{K} = \left(\begin{array}{cc} k_x & k_{xy} \\ k_{xy} & k_y \end{array}\right)$
-21	a	$\mathbf{A} = \mathbf{K}^{-1} = \left(\begin{array}{cc} a & 0 \\ 0 & a \end{array}\right)$
-22	$a_x - a_y$	$\mathbf{A} = \mathbf{K}^{-1} = \left(\begin{array}{cc} a_x & 0\\ 0 & a_y \end{array}\right)$
-23	$a_x  a_y  a_{xy}$	$\mathbf{A} = \mathbf{K}^{-1} = \begin{pmatrix} a_x & a_{xy} \\ a_{xy} & a_y \end{pmatrix}$
31	k	$\mathbf{K} = \left(\begin{array}{ccc} k & 0 & 0 \\ 0 & k & 0 \\ 0 & 0 & k \end{array}\right)$
33	$\begin{vmatrix} a_x & a_y & a_{xy} \end{vmatrix}$ $k &                                   $	$\mathbf{K} = \left(\begin{array}{ccc} k_x & 0 & 0 \\ 0 & k_y & 0 \\ 0 & 0 & k_z \end{array}\right)$
36	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\mathbf{K} = \begin{pmatrix} k_x & k_{xy} & k_{xz} \\ k_{xy} & k_y & k_{yz} \\ k_{xz} & k_{yz} & k_z \end{pmatrix}$
-31	a	$\mathbf{A} = \mathbf{K}^{-1} = \left( \begin{array}{ccc} 0 & a & 0 \\ 0 & 0 & a \end{array} \right)$
-33	$a_x  a_y  a_z$	$\mathbf{A} = \mathbf{K}^{-1} = \begin{pmatrix} a_x & 0 & 0 \\ 0 & a_y & 0 \\ 0 & 0 & a_z \end{pmatrix}$
-36	$\begin{bmatrix} a_x & a_y & a_z & a_{xy} & a_{xz} & a_{yz} \end{bmatrix}$	$\mathbf{A} = \mathbf{K}^{-1} = \begin{pmatrix} a_x & a_{xy} & a_{xz} \\ a_{xy} & a_y & a_{yz} \\ a_{xz} & a_{yz} & a_z \end{pmatrix}$

Note: all variables ( k,  $k_x$ ,  $k_y$ ,  $k_z$ ,  $k_{xy}$ ,  $k_{xz}$ ,  $k_{yz}$ , a,  $a_x$ ,  $a_y$ ,  $a_z$ ,  $a_{xy}$ ,  $a_{xz}$ ,  $a_{yz}$ ) are of the double type.

sorption-type	$sorption\-type\-specific\-data$	Description
1	$k_D[1]$	$s = k_D c$
2	$k_F[(L^{-3} \cdot M^1)^{(1-\alpha)}]  \alpha[1]$	$s = k_F c^{\alpha}$
3	$K_L[L^3 \cdot M^{-1}]$ $s^{max}[L^{-3} \cdot M^1]$	$s = \frac{K_L s^{max} c}{1 + K_L c}$

Note: all variables (  $k_D$ ,  $k_F$ ,  $\alpha$ ,  $K_L$ ,  $s^{max}$  ) are of the double type.

reaction-type	reaction-type-specific-data		Description
0	substance- $id[1]$	$k[M \cdot L^{-3} \cdot T^{-1}]$	$\frac{\partial c_m^{[substance-id]}}{\partial t} = k$

Where  $c_m^{[substance-id]}$  is mobile concentration of substance with id substance-id and  $\Delta t$  is the internal transport time step defined by CFL condition.

text char[] — is a text description of the material, up to 256 chars. This parameter is

optional.

## Comments concerning Flow123d:

• If *number-of-materials* differs from actual number of material lines in the file, it stops the calculation.

## 3.4.4 Boundary conditions file format, version 1.0

The file is divided in two sections, header and data.

```
$BoundaryFormat
1.0 file-type data-size
$EndBoundaryFormat
$BoundaryConditions
number-of-conditions
condition-number type <type-specific-data> where <where-data> number-of-tags
<tags> [text]
...
$EndBoundaryConditions
```

where

file-type int — is equal 0 for the ASCII file format.

data-size int — the size of the floating point numbers used in the file. Usually data-size = sizeof(double).

number-of-conditions int — Number of boundary conditions defined in the file.

condition-number int — is the number (index) of the n-th boundary condition. These numbers do not have to be given in a consecutive (or even an ordered) way. Each number has to be given only onece, multiple definition are treated as inconsistency of the file and cause stopping the calculation.

type int — is type of the boundary condition. See below for definitions of the types.

- <type-specific-data> format of this list depends on the type. See below for specification of the type-specific-data for particular types of the boundary conditions.
- where int defines the way, how the place for the contidion is prescribed. See below for details.
- <where-data> format of this list depends on where and actually defines the place for the condition. See below for details.

number-of-tags int — number of integer tags of the boundary condition. It can be zero.

< tags > number-of-tags\*int — list of tags of the boundary condition. Values are separated by spaces or tabs. By default we set number-of-tags=1, where tag1 defines group of boundary conditions, "type of water" in our jargon. This can be used to calculate total fluxes through the boundary group.

[text] char[] — arbitrary text, description of the fracture, notes, etc., up to 256 chars. This is an optional parameter.

## Types of boundary conditions and their data

type = 1 — Boundary condition of the Dirichlet's type

type = 2 — Boundary condition of the Neumann's type

type = 3 — Boundary condition of the Newton's type

type	type-specific-data	Description
1	scalar	Prescribed value of pressure (in meters [m])
2	flux	Prescribed value of flux through the boundary
3	scalar sigma	Scalar value and the $\sigma$ coefficient

scalar, flux and sigma are of the double type.

## Ways of defining the place for the boundary condition

where = 1 — Condition on a node

where = 2 — Condition on a (generalized) side

where = 3 — Condition on side for element with only one external side.

where	<pre><where-data></where-data></pre>	Description
1	$node ext{-}id$	Node id number, according to .MSH file
2	elm-id sid-id	Elm. id number, local number of side
3	elm-id	Elm. id number

The variables node-id, elm-id, sid-id are of the int type.

## Comments concerning Flow123d:

- We assume homegemous Neumman's condition as the default one. Therefore we do not need to prescribe conditions on the whole boundary.
- If the condition is given on the inner edge, it is treated as an error and stops calculation.
- Any inconsistence in the file stops calculation. (Bad number of conditions, multiple definition of condition, reference to non-existing node, etc.)

- At least one of the conditions has to be of the Dirichlet's or Newton's type. This is well-known fact from the theory of the PDE's.
- Local numbers of sides for where = 2 must be lower than the number of sides of the particular element and greater then or equal to zero.
- The element specified for where = 3 must have only one external side, otherwise the program stops.

## 3.4.5 Transport boundary conditions file format, version 1.0

The file is divided in two sections, header and data.

```
$Transport_BCDFormat
1.0 file-type data-size
$EndTransport_BCDFormat
$Transport_BCD
number-of-conditions
transport-condition-number boundary-condition-number value1 value2 ...
$EndTransport_BCD
```

where

file-type int - is equal 0 for the ASCII file format.

data-size int - the size of the floating point numbers used in the file. Usually data-size = sizeof(double)

number-of-conditions int - Number of conditions defined in the file.

transport-condition-number int - is the number (index) of the n-th transport condition. These numbers do not have to be given in a consecutive (or even an ordered) way. Each number has to be given only once, multiple definition are treated as inconsistency of the file and cause stopping the calculation.

boundary-condition-number int - id number of the boundary-condition where transport boundary condition is prescribed.

valueN double - prescribed boundary concentration of substance N (should be from interval [0,1]).

Comments concerning FLOW123d: Number of transport boundary conditions has to be same as number of boundary conditions. Program stops computation in the other case.

## 3.4.6 Element data file format, version 1.0

Several input data fields are given as constant scalars on every element. In particular this is used for water sources, initial condition of pressure, initial condition for concentrations and substance sources in transport. Common file format of these files is:

#### \$FieldName

number-of-lines eid value1 value2 ...

\$EndFieldName

where

\$FieldName — Unique name of the input field. Since all field data are enclosed by \$FieldName and \$EndFieldName one can even have different fields in one common file.

number-of-sources int — Number of data lines that has to match number of elements in the mesh.

eid int — is id-number of the element (in the input mesh file).

value N double — list of field values. Number of values is specific for each particular type of input.

Description of individual input fields.

water sources FieldName=Sources, there is only one value per line — the density of water source on the element.

pressure initial condition FieldName=PressureHead, there is only one value per line — the initial pressure value on the element.

substance sources FieldName=TransportSources, number of values is 3 times number of substances. The density of one substance source is given by formula:

$$f = d + \sigma(c - c_N)$$

where f is total source, the first term is fixed Neuman-like source density d. The second term is Newton-like source density, where  $\sigma$  is transmisitvity, c is actual concentration, and  $c_N$  is prescribed concentration. For every substance there is triplet of three parameters: d,  $\sigma$ ,  $c_N$ . The order of substances is same as in the main INI file.

concentration initial conditions FieldName=Concentrations, number of values equal to number of transported substances, the order of substances is same as in the main INI file.

# Comments concerning Flow123d:

- Every inconsistency or error in the .SRC file causes stopping the calculation. These are especially:
  - Difference between *number-of-lines* and actual number of data lines.
  - Reference to nonexisting element.

# 3.5 Output files

Flow123d support output of scalar and vaector data fields into two formats. First one can use native fromat of program GMSH (usualy with extension msh) which contains computational mesh and then various datafields for squence of time levels. For second we support output into XML version of VTK files. These files can be viewed and postprocessed by several vizualization softwares. However, our primal goal is to support data transfer into Paraview vizualization software. See key Pos\_format.

## 3.5.1 Output data fields of water flow module

Water flow module provides output of four data fields.

- **pressure on elements** Pressure head in length units [L] piecewise constant on every element. This field is directly produced by the MH method and thus contains no postprocessing error.
- pressure in nodes Same pressure head field, but interpolated into P1 continuous scalar field. Namely you lost discontinuities on fractures.
- **velocity on elements** Vector field of water flux volume unit per time unit  $[L^3/T]$ . For every element we evaluate discrete flux field in barycenter.
- piezometric head on elements Piezometric head in length units [L] piecewise constant on every element. This is just pressure on element plus z-coordinate of the barycenter. This field is produced only on demand (see key output\_piezo\_head).

# 3.5.2 Output data fields of transport

Transport module provides output only for concentrations (in mobile phase) as a field piecewise constant over elements. There is one field for every substance and names of those fields contain names of substances given by key Substances. The physical unit is mass unit over volume unit  $[M/L^3]$ .

# 3.5.3 Auxiliary output files

### **Profiling information**

On every run we collect some bacis profilling informations. After all computations these data are written into the file profiler%y%m%d\_%H.%M.%S.out where %y, %m, %d, %H, %M, %S are two digit numbers representing year, month, day, hour, minute, and second of the program start time.

#### Water flux information

File contains water flow balance, total inflow and outflow over boundary segments. Further there is total water income due to sources (if they are present).

### Raw water flow data file

You can force Flow123d to write raw data about results of MH method. The file format is:

# Chapter 4

# Main input file reference

abstract type: Problem	
Descendants:	
The root record of description of particular the problem to solve.	
SequentialCoupling	
record: SequentialCoupling implements abstract type: Problem	
Record with data for a general sequential coupling.	
$\mathtt{TYPE} = <\!selection:\ Problem\_TYPE\_selection\!\!>$	
Default: SequentialCoupling	
Sub-record selection.	
$ ext{description} = <\!String\;(generic)\!>$	
Default: <optional></optional>	
Short description of the solved problem. Is displayed in the main log, and poss in other text output files.	ibly
mesh = < record: Mesh>	
Default: <obligatory></obligatory>	
Computational mesh common to all equations.	
time = < record: TimeGovernor >	
Default: <optional></optional>	
Simulation time frame and time step.	
$primary_equation = < abstract\ type:\ {\it DarcyFlowMH}>$	
Default: <obligatory></obligatory>	
Primary equation, have all data given.	
${\tt secondary\_equation} = < abstract \ type: \ {\it Transport}>$	

Default: < optional> The equation that depends (the velocity field) on the result of the primary equarecord: Mesh Record with mesh related data. mesh\_file = < input file name> Default: < oblique tory> Input file with mesh description. regions = < Array of record: Region> Default: < optional> List of additional region definitions not contained in the mesh. sets = < Array of record: RegionSet> Default: < optional> List of region set definitions. There are three region sets implicitly defined: ALL (all regions of the mesh), BOUNDARY (all boundary regions), and BULK (all bulk regions) record: **Region** Definition of region of elements.  $name = \langle String (generic) \rangle$ Default: < obligatory> Label (name) of the region. Has to be unique in one mesh.  $id = \langle Integer /0, \rangle$ Default: < oblique tory> The ID of the region to which you assign label. element\_list = <Array of Integer [0, ]> Default: < optional> Specification of the region by the list of elements. This is not recomended record: RegionSet Definition of one region set.

$$name = \langle String (generic) \rangle$$

Default: < obligatory>

Unique name of the region set.

 $region_ids = \langle Array \ of \ Integer \ [0,] \rangle$ 

Default: < optional> List of region ID numbers that has to be added to the region set. region\_labels = < Array of String (generic)> Default: <optional> List of labels of the regions that has to be added to the region set. union =  $\langle Array | 2, 2 \rangle$  of String (generic)> Default: < optional> Defines region set as a union of given pair of sets. Overrides previous keys.  $intersection = \langle Array [2, 2] \ of \ String \ (generic) >$ Default: < optional> Defines region set as an intersection of given pair of sets. Overrides previous  $difference = \langle Array [2, 2] \text{ of String (generic)} \rangle$ Default: < optional> Defines region set as a difference of given pair of sets. Overrides previous keys. record: TimeGovernor Setting of the simulation time. (can be specific to one equation)  $start_time = < Double >$ Default: 0.0 Start time of the simulation.  ${\tt end\_time} = <\!Double>$ Default: < obligatory> End time of the simulation.  $init_dt = < Double /0, >$ Default: < optional> Initial guess for the time step. The time step is fixed if hard time step limits are not set.  $min_dt = \langle Double | 0, \rangle$ Default: "Machine precision or 'init\_dt' if specified" Hard lower limit for the time step.  $\max_{dt} = \langle Double /0, \rangle$ Default: "Whole time of the simulation or 'init\_dt' if specified" Hard upper limit for the time step.

abstract type: DarcyFlowMH

Solver setting.

### Petsc

### Bddc

record: Petsc implements abstract type: Solver	
Solver setting.	
$\mathtt{TYPE} = \langle selection: Solver\_TYPE\_selection \rangle$	
Default: Petsc	
Sub-record selection.	
a_tol = < Double [0, ]>	
Default: 1.0e-9	
Absolute residual tolerance.	
r_tol = < Double [0, 1]>	
Default: 1.0e-7	
Relative residual tolerance (to initial error).	
$\mathtt{max\_it} = < Integer [0, ]>$	
Default: 10000	
Maximum number of outer iterations of the linear solver.	
$options = \langle String (generic) \rangle$	
Default:	
Options passed to the petsc instead of default setting.	
record: <b>Bddc</b> implements abstract type: Solver	
Solver setting.	
$\mathtt{TYPE} = <\!selection:\ Solver\_TYPE\_selection\!\!>$	
Default: Bddc	
Sub-record selection.	
a_tol = < Double [0, ]>	
Default: 1.0e-9	
Absolute residual tolerance.	
r_tol = < Double [0, 1]>	
Default: 1.0e-7	
Relative residual tolerance (to initial error).	
$\mathtt{max\_it} = \langle Integer\ [0,\ ] \rangle$	
Default: 10000	
Maximum number of outer iterations of the linear solver.	

record: DarcyMHOutput	
Parameters of MH output.	
$save\_step = < Double [0, ]>$	
Default: 1.0	
Regular step between MH outputs.	
<pre>output_stream = &lt; record: OutputStrem&gt;</pre>	
Default: <obligatory></obligatory>	
Parameters of output stream.	
$velocity_p0 = < String (generic) >$	
Default: < optional>	
Output stream for P0 approximation of the velocity field.	
$pressure_p0 = < String (generic) >$	
Default: < optional>	
Output stream for P0 approximation of the pressure field.	
$pressure_p1 = \langle String \ (generic) \rangle$	
Default: < optional>	
Output stream for P1 approximation of the pressure field.	
$piezo\_head\_p0 = < String (generic) >$	
Default: <optional></optional>	
Output stream for P0 approximation of the piezometric head field.	
${\tt balance\_output} = < output \ file \ name >$	
Default: water_balance.txt	
Output file for water balance table.	
$raw\_flow\_output = < output file \ name >$	
Default: <optional></optional>	
Output file with raw data form MH module.	
record: OutputStrem	
Parameters of output.	
$\mathtt{name} = \langle String \; (generic) \rangle$	
Default: <obligatory></obligatory>	[
The name of this stream. Used to reference the output stream.	
<pre>file = <output file="" name=""></output></pre>	
Default: < obligatory>	[]

File path to the output stream. format = <abstract type: OutputFormat> Default: < optional> Format of output stream and possible parameters. abstract type: OutputFormat Descendants: Format of output stream and possible parameters. vtk gmsh record: vtk implements abstract type: OutputFormat Parameters of vtk output format. TYPE = < selection: OutputFormat\_TYPE\_selection> Default: vtk Sub-record selection. variant = < selection: VTK variant (ascii or binary)> Default: ascii Variant of output stream file format.  $parallel = \langle Bool \rangle$ Default: false Parallel or serial version of file format. compression = < selection: Type of compression of VTK file format> Default: none Compression used in output stream file format. selection type: VTK variant (ascii or binary) Possible values: ascii: ASCII variant of VTK file format

binary: Binary variant of VTK file format (not supported yet)

### selection type: Type of compression of VTK file format

Possible values:

none: Data in VTK file format are not compressed

zlib: Data in VTK file format are compressed using zlib (not supported yet)

### record: gmsh implements abstract type: OutputFormat

Parameters of gmsh output format.

 $\mathtt{TYPE} = < selection: \ OutputFormat\_TYPE\_selection >$ 

Default: gmsh

Sub-record selection.

### selection type: MH\_MortarMethod

Possible values:

None: Mortar space: P0 on elements of lower dimension.

P0: Mortar space: P0 on elements of lower dimension.

P1: Mortar space: P1 on intersections, using non-conforming pressures.

### record: DarcyFlowMH\_Steady\_BoundaryData

Record to set BOUNDARY fields of the equation 'DarcyFlowMH\_Steady'. The fields are set only on the domain specified by one of the keys: 'region', 'rid', 'r\_set' and after the time given by the key 'time'. The field setting can be over-ridden by any DarcyFlowMH\_Steady\_BoundaryData record that comes later in the boundary data array.

r\_set = <String (generic)>

Default: <optional>

Name of region set where to set fields.

 $region = \langle String (generic) \rangle$ 

Default: <optional>

Label of the region where to set fields.

 $rid = \langle Integer /0, \rangle$ 

Default: <optional>

ID of the region where to set fields.

 $time = \langle Double /0, \rangle$ 

Default: 0.0

Apply field setting in this record after this time. These times has to form an increasing sequence.

 $bc\_type = \langle abstract\ type:\ Field:R3 \rightarrow Enum \rangle$ 

Default: <optional>

Boundary condition type, possible values:

 $bc\_pressure = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: <optional>

Dirichlet BC condition value for pressure.

 $bc_flux = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: <optional>

Flux in Neumman or Robin boundary condition.

 $bc\_robin\_sigma = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: <optional>

Conductivity coefficient in Robin boundary condition.

 $bc\_piezo\_head = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: <optional>

Boundary condition for pressure as piezometric head.

flow\_old\_bcd\_file = <input file name>

Default: <optional>

## abstract type: Field:R3 $\rightarrow$ Enum default descendant: FieldConstant

Descendants:

Abstract record for all time-space functions.

FieldConstant

FieldFormula

FieldPython

FieldElementwise

record: FieldConstant implements abstract type: Field:R3  $\rightarrow$  Enum constructible from key: value

 $R3 \rightarrow Enum$  Field constant in space.

 $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Enum\_TYPE\_selection>$ 

Default: FieldConstant []

Sub-record selection.

value = < selection: EqData\_bc\_Type>

Default: <obliqatory>

Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix.

selection type: **EqData\_bc\_Type** 

Possible values:

dirichlet:		
neumann:		
robin:		
total_flux:		
record: FieldFormula implements abstract type: Field:R3 $\rightarrow$ Enum		
$R3 \rightarrow Enum$ Field given by runtime interpreted formula.		
$\texttt{TYPE} = <\!selection: \ Field:R3 \rightarrow Enum\_TYPE\_selection\!\!>$		
Default: FieldFormula		
Sub-record selection.		
$ ext{value} = \langle String \ (generic) \rangle$		
Default: <obligatory></obligatory>		
String, array of strings, or matrix of strings with formulas for in of scalar, vector, or tensor value respectively. For vector values, yone string to enter homogeneous vector. For square NxN-matrix use: * array of strings of size N to enter diagonal matrix * arrayize $(N+1)*N/2$ to enter symmetric matrix (upper triangle, row one string to enter (spatially variable) multiple of the unit matrix contain variables x,y,z,t and usual operators and functions.	you can use just values, you can cay of strings of by row) * just	
record: FieldPython implements abstract type: Field:R3 $\rightarrow$ Enum		
$R3 \rightarrow Enum$ Field given by a Python script.		
$\texttt{TYPE} = <\!\! selection \colon \mathit{Field} : R3 \to \mathit{Enum\_TYPE\_selection} \!\!>$		
Default: FieldPython		
Sub-record selection.		
$script\_string = < String (generic) >$		
Default: "Obligatory if 'script_file' is not given."		
Python script given as in place string		
$script\_file = < input file name >$		
Default: "Obligatory if 'script_striong' is not given."		
Python script given as external file		
$function = \langle String \ (generic) \rangle$		
Default: <obligatory></obligatory>		
Function in the given script that returns tuple containing conreturn type. For NxM tensor values: tensor(row,col) = tuple(M		

none: Homogeneous Neoumann BC.

### record: FieldElementwise implements abstract type: Field:R3 $\rightarrow$ Enum

 $R3 \rightarrow Enum$  Field constant in space.

 $\mathtt{TYPE} = \langle selection: \ Field: R3 \rightarrow Enum\_TYPE\_selection \rangle$ 

Default: FieldElementwise []

Sub-record selection.

gmsh\_file = <input file name>

Default: <obligatory>

Input file with ASCII GMSH file format.

 $field_name = \langle String (generic) \rangle$ 

Default: < obligatory>

The values of the Field are read from the \$ElementData section with field name given by this key.

abstract type: Field:R3  $\rightarrow$  Real default descendant: FieldConstant

Descendants:

Abstract record for all time-space functions.

FieldConstant

FieldPython

FieldFormula

FieldElementwise

FieldInterpolatedP0

record: FieldConstant implements abstract type: Field:R3  $\rightarrow$  Real constructible from key: value

 $R3 \rightarrow Real$  Field constant in space.

 $\mathtt{TYPE} = \langle selection : Field : R3 \rightarrow Real\_TYPE\_selection \rangle$ 

Default: FieldConstant

Sub-record selection.

value = < Double >

Default: < oblique tory>

Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix.

record: FieldPython implements abstract type: Field:R3  $\rightarrow$  Real

 $R3 \rightarrow Real$  Field given by a Python script.  $\mathtt{TYPE} = \langle selection : Field : R3 \rightarrow Real\_TYPE\_selection \rangle$ Default: FieldPython Sub-record selection. script\_string = <String (generic)> Default: "Obligatory if 'script\_file' is not given." Python script given as in place string script\_file = <input file name> Default: "Obligatory if 'script\_striong' is not given." Python script given as external file function =  $\langle String (generic) \rangle$ Default: < obligatory> Function in the given script that returns tuple containing components of the return type. For NxM tensor values: tensor(row,col) = tuple(M\*row + col). record: FieldFormula implements abstract type: Field:R3  $\rightarrow$  Real  $R3 \rightarrow Real$  Field given by runtime interpreted formula.  $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Real\_TYPE\_selection>$ Default: FieldFormula Sub-record selection.  $value = \langle String (generic) \rangle$ Default: < oblique tory> String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions. record: FieldElementwise implements abstract type: Field:R3  $\rightarrow$  Real  $R3 \rightarrow Real$  Field constant in space.  $\mathtt{TYPE} = \langle selection \colon \mathit{Field} : R3 \to \mathit{Real\_TYPE\_selection} \rangle$ Default: FieldElementwise Sub-record selection. gmsh\_file = <input file name>

Default: < obligatory>

Input file with ASCII GMSH file format.

 $field_name = \langle String (generic) \rangle$ 

Default: < obligatory>

The values of the Field are read from the \$ElementData section with field name given by this key.

### record: FieldInterpolatedP0 implements abstract type: Field:R3 $\rightarrow$ Real

Field given by P0 data on another mesh. Currently defined only on boundary.

 $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Real\_TYPE\_selection>$ 

Default: FieldInterpolatedP0

Sub-record selection.

 $mesh = \langle input \ file \ name \rangle$ 

Default: < oblique tory>

File with the mesh from which we interpolate. (currently only GMSH supported)

raw\_data = <input file name>

Default: <obligatory>

File with raw output from flow calculation. Currently we can interpolate only pressure.

### abstract type: $Field:R3 \rightarrow Real$ default descendant: FieldConstant

Descendants:

Abstract record for all time-space functions.

FieldConstant

FieldFormula

FieldPython

FieldElementwise

record: FieldConstant implements abstract type: Field:R3  $\rightarrow$  Real constructible from key: value

 $R3 \rightarrow Real$  Field constant in space.

 $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Real\_TYPE\_selection>$ 

Default: FieldConstant

Sub-record selection.

value = < Double >

Default: < obligatory>

Value of the constant field. For vector values, you can use scalar value to enter

constant vector. For square NxN-matrix values, you can use: \*vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix.

# record: FieldFormula implements abstract type: Field:R3 $\rightarrow$ Real $R3 \rightarrow Real$ Field given by runtime interpreted formula. $\mathtt{TYPE} = \langle selection \colon \mathit{Field} : R3 \to \mathit{Real\_TYPE\_selection} \rangle$ Default: FieldFormula Sub-record selection. $value = \langle String (qeneric) \rangle$ Default: < oblique tory> String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions. record: FieldPython implements abstract type: Field:R3 $\rightarrow$ Real $R3 \rightarrow Real$ Field given by a Python script. $\mathtt{TYPE} = \langle selection : Field : R3 \rightarrow Real\_TYPE\_selection \rangle$ Default: FieldPython Sub-record selection. script\_string = <String (generic)> Default: "Obligatory if 'script\_file' is not given." Python script given as in place string script\_file = <input file name>

Python script given as external file

 $function = \langle String (generic) \rangle$ 

Default: < obligatory>

Function in the given script that returns tuple containing components of the return type. For NxM tensor values: tensor(row,col) = tuple(M\*row + col).

record: FieldElementwise implements abstract type: Field:R3  $\rightarrow$  Real

Default: "Obligatory if 'script\_striong' is not given."

 $R3 \rightarrow Real Field constant in space.$ 

 $\mathtt{TYPE} = \langle selection : Field : R3 \rightarrow Real\_TYPE\_selection \rangle$ Default: FieldElementwise Sub-record selection. gmsh\_file = <input file name> Default: <obligatory> Input file with ASCII GMSH file format. field\_name = < String (generic)> Default: < oblique or y> The values of the Field are read from the \$ElementData section with field name given by this key. record: DarcyFlowMH\_Steady\_BulkData Record to set BULK fields of the equation 'DarcyFlowMH\_Steady'. The fields are set only on the domain specified by one of the keys: 'region', 'rid', 'r\_set' and after the time given by the key 'time'. The field setting can be overridden by any DarcyFlowMH\_Steady\_BulkData record that comes later in the bulk data array. r\_set = < String (generic)> Default: < optional> Name of region set where to set fields.  $region = \langle String (generic) \rangle$ Default: < optional> Label of the region where to set fields.  $rid = \langle Integer /0, \rangle$ Default: < optional> ID of the region where to set fields.  $time = \langle Double /0, \rangle$ Default: 0.0 П Apply field setting in this record after this time. These times has to form an increasing sequence. anisotropy =  $\langle abstract\ type:\ Field:R3 \rightarrow Real[3,3] \rangle$ Default: < optional> Anisothropic conductivity tensor.  $cross\_section = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: < optional> 

conductivity =  $\langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Complement dimension parameter (cross section for 1D, thickness for 2D).

```
Default: < optional>
       Isothropic conductivity scalar.
sigma = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
       Default: < optional>
                                                                                                  Transition coefficient between dimensions.
water_source_density = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
       Default: < optional>
                                                                                                  Water source density.
init\_pressure = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
        Default: < optional>
                                                                                                  Initial condition as pressure
storativity = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
       Default: < optional>
                                                                                                  Storativity.
init\_piezo\_head = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
       Default: < optional>
                                                                                                  Initial condition for pressure as piezometric head.
abstract type: Field:R3 \rightarrow Real[3,3] default descendant: FieldConstant
Descendants:
        Abstract record for all time-space functions.
FieldConstant
FieldPython
FieldFormula
FieldElementwise
FieldInterpolatedP0
record: FieldConstant implements abstract type: Field:\mathbb{R}^3 \to \mathbb{R} and \mathbb{R}^3 constructible
from key: value
       R3 \rightarrow Real[3,3] Field constant in space.
\mathtt{TYPE} = \langle selection: \ Field: R3 \rightarrow Real/3, 3/\_TYPE\_selection \rangle
        Default: FieldConstant
                                                                                                  Sub-record selection.
value = <Array [1, ] of Array [1, ] of Double >
       Default: < obligatory>
```

Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix.

# record: FieldPython implements abstract type: Field:R3 $\rightarrow$ Real[3,3] $R3 \rightarrow Real[3,3]$ Field given by a Python script. $\mathtt{TYPE} = \langle selection: \ Field: R3 \rightarrow Real/3, 3/\_TYPE\_selection \rangle$ Default: FieldPython Sub-record selection. script\_string = <String (generic)> Default: "Obligatory if 'script\_file' is not given." Python script given as in place string script\_file = <input file name> Default: "Obligatory if 'script\_striong' is not given." Python script given as external file $function = \langle String (generic) \rangle$ Default: < obligatory> Function in the given script that returns tuple containing components of the return type. For NxM tensor values: tensor(row,col) = tuple(M\*row + col). record: FieldFormula implements abstract type: Field:R3 $\rightarrow$ Real[3,3] $R3 \rightarrow Real[3,3]$ Field given by runtime interpreted formula. $\mathtt{TYPE} = \langle selection: \ Field: R3 \rightarrow Real / 3, 3 / TYPE\_selection \rangle$ Default: FieldFormula Sub-record selection. value = <Array [1, ] of Array [1, ] of String (generic)> Default: < oblique tory>

String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions.

record: FieldElementwise implements abstract type: Field:R3  $\rightarrow$  Real[3,3]

 $R3 \rightarrow Real[3,3]$  Field constant in space.  $\mathtt{TYPE} = \langle selection: \ Field: R3 \rightarrow Real/3, 3/\_TYPE\_selection \rangle$ Default: FieldElementwise Sub-record selection. gmsh\_file = <input file name> Default: < obligatory> Input file with ASCII GMSH file format. field\_name = < String (generic)> Default: < oblique or y> The values of the Field are read from the \$ElementData section with field name given by this key.

record: FieldInterpolatedP0 implements abstract type: Field:R3  $\rightarrow$  Real[3,3]

Field given by P0 data on another mesh. Currently defined only on boundary.

 $\mathtt{TYPE} = \langle selection: Field:R3 \rightarrow Real[3,3]\_TYPE\_selection \rangle$ 

Default: FieldInterpolatedP0

Sub-record selection.

 $mesh = \langle input \ file \ name \rangle$ 

Default: < obligatory>

File with the mesh from which we interpolate. (currently only GMSH supported)

raw\_data = <input file name>

Default: < oblique tory>

File with raw output from flow calculation. Currently we can interpolate only pressure.

abstract type: Field:R3  $\rightarrow$  Real default descendant: FieldConstant

Descendants:

Abstract record for all time-space functions.

FieldConstant

FieldFormula

FieldPython

FieldElementwise

record: FieldConstant implements abstract type: Field:R3  $\rightarrow$  Real constructible from key: value

 $R3 \rightarrow Real$  Field constant in space.

 $\mathtt{TYPE} = \langle selection : Field : R3 \rightarrow Real\_TYPE\_selection \rangle$ Default: FieldConstant Sub-record selection. value = < Double >Default: < obligatory> Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix. record: FieldFormula implements abstract type: Field:R3  $\rightarrow$  Real  $R3 \rightarrow Real$  Field given by runtime interpreted formula.  $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Real\_TYPE\_selection>$ Default: FieldFormula Sub-record selection.  $value = \langle String (generic) \rangle$ Default: < oblique tory> String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions. record: FieldPython implements abstract type: Field:R3  $\rightarrow$  Real  $R3 \rightarrow Real Field given by a Python script.$  $\mathtt{TYPE} = \langle selection: Field:R3 \rightarrow Real\_TYPE\_selection \rangle$ Default: FieldPython Sub-record selection. script\_string = <String (generic)> Default: "Obligatory if 'script\_file' is not given." Python script given as in place string script\_file = <input file name> Default: "Obligatory if 'script\_striong' is not given." 

Python script given as external file

 $function = \langle String (generic) \rangle$ 

Function in the given script that returns tuple containing components of the return type. For NxM tensor values: tensor(row,col) = tuple(M\*row + col). record: FieldElementwise implements abstract type: Field:R3  $\rightarrow$  Real  $R3 \rightarrow Real Field constant in space.$  $\mathtt{TYPE} = \langle selection: \ Field:R3 \rightarrow Real\_TYPE\_selection \rangle$ Default: FieldElementwise Sub-record selection. gmsh\_file = <input file name> Default: < obligatory> Input file with ASCII GMSH file format. field\_name = < String (generic)> Default: < oblique or y> The values of the Field are read from the \$ElementData section with field name given by this key. record: Unsteady\_MH implements abstract type: DarcyFlowMH Mixed-Hybrid solver for unsteady saturated Darcy flow. TYPE = < selection: DarcyFlowMH\_TYPE\_selection> Default: Unsteady\_MH Sub-record selection.  $n_schurs = \langle Integer [0, 2] \rangle$ Default: 2 Number of Schur complements to perform when solving MH sytem. solver = <abstract type: Solver> Default: < oblique tory> Linear solver for MH problem. output = < record: DarcyMHOutput> Default: < obligatory> Parameters of output form MH module. mortar\_method = < selection: MH\_MortarMethod> Default: None Method for coupling Darcy flow between dimensions.  $mortar\_sigma = < Double [0, ]>$ 

Default: <obligatory>

Default: 1.0 Conductivity between dimensions. time = < record: TimeGovernor> Default: < oblique tory> Time governor setting for the unsteady Darcy flow model. bc\_data = < Array of record: DarcyFlowMH\_Steady\_BoundaryData> Default: < obligatory> bulk\_data = < Array of record: DarcyFlowMH\_Steady\_BulkData> Default: < oblique tory> record: DarcyFlowMH\_Steady\_BoundaryData Record to set BOUNDARY fields of the equation 'DarcyFlowMH\_Steady'. The fields are set only on the domain specified by one of the keys: 'region', 'rid', 'r\_set' and after the time given by the key 'time'. The field setting can be overridden by any DarcyFlowMH\_Steady\_BoundaryData record that comes later in the boundary data array. r\_set = < String (generic)> Default: < optional> Name of region set where to set fields.  $region = \langle String (generic) \rangle$ Default: < optional> Label of the region where to set fields.  $rid = \langle Integer [0, ] \rangle$ Default: < optional> ID of the region where to set fields.  $time = \langle Double /0, \rangle$ Default: 0.0 П Apply field setting in this record after this time. These times has to form an increasing sequence.  $bc\_type = \langle abstract\ type:\ Field:R3 \rightarrow Enum \rangle$ Default: < optional> Boundary condition type, possible values:  $bc\_pressure = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: < optional> П Dirichlet BC condition value for pressure.

 $bc_flux = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: < optional> Flux in Neumman or Robin boundary condition.  $bc\_robin\_sigma = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: < optional> Conductivity coefficient in Robin boundary condition.  $bc\_piezo\_head = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: < optional> Boundary condition for piezometric head. flow\_old\_bcd\_file = <input file name> Default: < optional> abstract type: Field:R3  $\rightarrow$  Enum default descendant: FieldConstant Descendants: Abstract record for all time-space functions. FieldConstant FieldFormula FieldPython FieldElementwise record: FieldConstant implements abstract type: Field:R3 → Enum constructible from key: value  $R3 \rightarrow Enum$  Field constant in space.  $\mathtt{TYPE} = \langle selection: Field:R3 \rightarrow Enum\_TYPE\_selection \rangle$ Default: FieldConstant Sub-record selection. value = < selection: EqData\_bc\_Type> Default: < oblique tory> Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix.

record: FieldFormula implements abstract type: Field:R3  $\rightarrow$  Enum

 $R3 \rightarrow Enum$  Field given by runtime interpreted formula.

 $\mathtt{TYPE} = \langle selection: \ Field:R3 \rightarrow Enum\_TYPE\_selection \rangle$ 

Default: FieldFormula  Sub-record selection.

value = < String (generic)>

Default: <obligatory>

String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions.

### record: FieldPython implements abstract type: Field:R3 $\rightarrow$ Enum

 $R3 \rightarrow Enum$  Field given by a Python script.

 $\texttt{TYPE} = <\! selection \colon \mathit{Field} : R3 \to \mathit{Enum\_TYPE\_selection} \!\!>$ 

Default: FieldPython []

Sub-record selection.

script\_string = <String (generic)>

Default: "Obligatory if 'script\_file' is not given."

Python script given as in place string

script\_file = <input file name>

Default: "Obligatory if 'script\_striong' is not given."

Python script given as external file

function = < String (generic)>

Default: <obligatory>

Function in the given script that returns tuple containing components of the return type. For NxM tensor values: tensor(row,col) = tuple(M\*row + col).

### record: FieldElementwise implements abstract type: Field:R3 $\rightarrow$ Enum

 $R3 \rightarrow Enum$  Field constant in space.

 $\mathtt{TYPE} = \langle selection: Field:R3 \rightarrow Enum\_TYPE\_selection \rangle$ 

Default: FieldElementwise

Sub-record selection.

gmsh\_file = <input file name>

Default: <obligatory>

Input file with ASCII GMSH file format.

field\_name = <String (generic)>

Default: <obligatory>

The values of the Field are read from the \$ElementData section with field name given by this key.

abstract type: Field:R3  $\rightarrow$  Real default descendant: FieldConstant

Descendants:

Abstract record for all time-space functions.

FieldConstant

FieldFormula

FieldPython

FieldElementwise

record: FieldConstant implements abstract type: Field:R3  $\rightarrow$  Real constructible from key: value

 $R3 \rightarrow Real$  Field constant in space.

 $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Real\_TYPE\_selection>$ 

Default: FieldConstant []

Sub-record selection.

value = < Double >

Default: <obligatory>

Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix.

record: FieldFormula implements abstract type: Field:R3  $\rightarrow$  Real

 $R3 \rightarrow Real$  Field given by runtime interpreted formula.

 $\mathtt{TYPE} = \langle selection \colon \mathit{Field} : R3 \to \mathit{Real\_TYPE\_selection} \rangle$ 

Default: FieldFormula

Sub-record selection.

 $value = \langle String (generic) \rangle$ 

Default: < obligatory>

String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions.

# record: FieldPython implements abstract type: Field:R3 $\rightarrow$ Real

 $R3 \rightarrow Real$  Field given by a Python script.

 $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Real\_TYPE\_selection>$ 

Default: FieldPython

Sub-record selection.

script\_string = <String (generic)>

Default: "Obligatory if 'script\_file' is not given."

Python script given as in place string

script\_file = <input file name>

Default: "Obligatory if 'script\_striong' is not given."

Python script given as external file

 $function = \langle String (generic) \rangle$ 

Default: < obligatory>

Function in the given script that returns tuple containing components of the return type. For NxM tensor values: tensor(row,col) = tuple(M\*row + col).

### record: FieldElementwise implements abstract type: Field:R3 $\rightarrow$ Real

 $R3 \rightarrow Real$  Field constant in space.

 $\mathtt{TYPE} = \langle selection: Field:R3 \rightarrow Real\_TYPE\_selection \rangle$ 

Default: FieldElementwise

Sub-record selection.

gmsh\_file = <input file name>

Default: < obligatory>

Input file with ASCII GMSH file format.

field\_name = < String (generic)>

Default: <obliqatory>

The values of the Field are read from the \$ElementData section with field name given by this key.

### record: DarcyFlowMH\_Steady\_BulkData

Record to set BULK fields of the equation 'DarcyFlowMH\_Steady'. The fields are set only on the domain specified by one of the keys: 'region', 'rid', 'r\_set' and after the time given by the key 'time'. The field setting can be overridden by any DarcyFlowMH\_Steady\_BulkData record that comes later in the bulk data array.

 $r_set = \langle String (generic) \rangle$ 

```
Default: < optional>
        Name of region set where to set fields.
region = < String (qeneric)>
       Default: <optional>
                                                                                                  Label of the region where to set fields.
rid = \langle Integer | 0, \rangle
       Default: < optional>
                                                                                                  ID of the region where to set fields.
time = < Double /0, >
       Default: 0.0
        Apply field setting in this record after this time. These times has to form an
       increasing sequence.
anisotropy = \langle abstract\ type:\ Field:R3 \rightarrow Real[3,3] \rangle
       Default: < optional>
                                                                                                  Anisothropic conductivity tensor.
cross\_section = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
        Default: < optional>
                                                                                                  Complement dimension parameter (cross section for 1D, thickness for 2D).
conductivity = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
        Default: < optional>
                                                                                                  Isothropic conductivity scalar.
sigma = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
        Default: < optional>
                                                                                                  Transition coefficient between dimensions.
water_source_density = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
        Default: < optional>
                                                                                                  Water source density.
init\_pressure = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
        Default: < optional>
                                                                                                  Initial condition as pressure
storativity = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
                                                                                                  Default: < optional>
        Storativity.
init\_piezo\_head = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
                                                                                                  Default: < optional>
```

abstract type: Field:R3  $\rightarrow$  Real default descendant: FieldConstant

Descendants:

Abstract record for all time-space functions.

FieldConstant

FieldFormula

FieldPython

FieldElementwise

record: FieldConstant implements abstract type: Field:R3  $\rightarrow$  Real constructible from key: value

 $R3 \rightarrow Real$  Field constant in space.

 $\mathtt{TYPE} = \langle selection: Field:R3 \rightarrow Real\_TYPE\_selection \rangle$ 

Default: FieldConstant []

Sub-record selection.

 $ext{value} = < Double >$ 

Default: <obligatory>

Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix.

### record: FieldFormula implements abstract type: Field:R3 $\rightarrow$ Real

 $R3 \rightarrow Real$  Field given by runtime interpreted formula.

 $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Real\_TYPE\_selection>$ 

Default: FieldFormula []

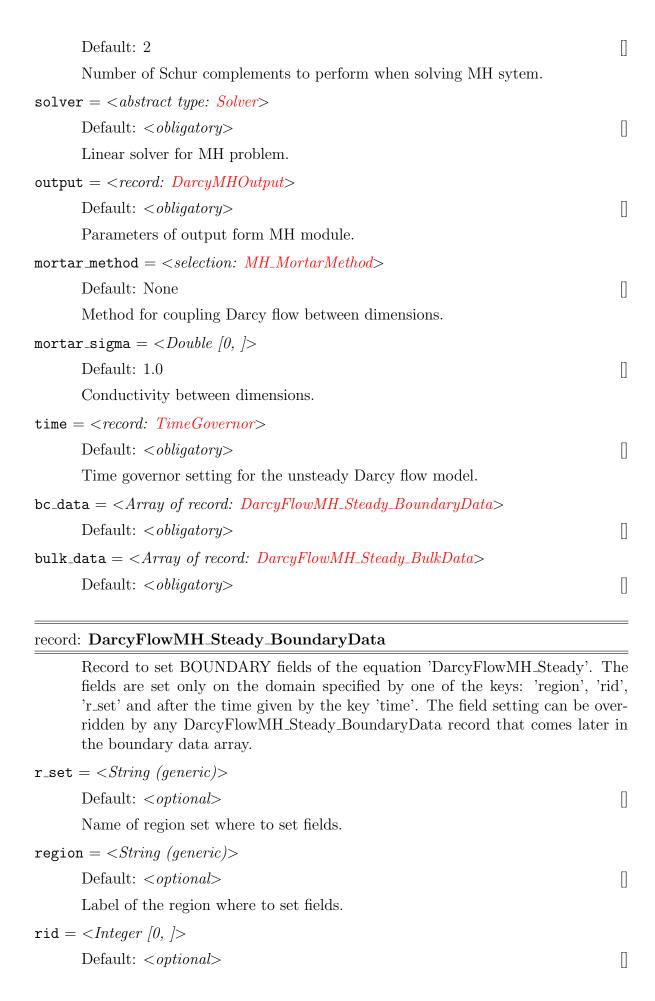
Sub-record selection.

 $value = \langle String (qeneric) \rangle$ 

Default: <obliqatory>

String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions.

record: FieldPython implements abstract type: Field:R3 $\rightarrow$ Real		
$R3 \rightarrow Real Field given by a Python script.$		
$\texttt{TYPE} = \langle selection \colon \mathit{Field} : R3 \to \mathit{Real\_TYPE\_selection} \rangle$		
Default: FieldPython		
Sub-record selection.		
$script\_string = < String (generic) >$		
Default: "Obligatory if 'script_file' is not given."	[]	
Python script given as in place string		
<pre>script_file = <input file="" name=""/></pre>		
Default: "Obligatory if 'script_striong' is not given."	[]	
Python script given as external file		
<pre>function = <string (generic)=""></string></pre>		
Default: <obligatory></obligatory>		
Function in the given script that returns tuple containing comported return type. For NxM tensor values: tensor(row,col) = tuple( M*rov		
record: FieldElementwise implements abstract type: Field:R3 $\rightarrow$ Real		
$R3 \rightarrow Real Field constant in space.$		
$\texttt{TYPE} = \langle selection \colon \mathit{Field} : R3 \to \mathit{Real\_TYPE\_selection} \rangle$		
Default: FieldElementwise		
Sub-record selection.		
<pre>gmsh_file = <input file="" name=""/></pre>		
Default: <obligatory></obligatory>		
Input file with ASCII GMSH file format.		
${\tt field\_name} = <\!\!String\;(generic)\!\!>$		
Default: <obligatory></obligatory>		
The values of the Field are read from the \$ElementData section with given by this key.	h field name	
record: Unsteady_LMH implements abstract type: DarcyFlowMH		
Lumped Mixed-Hybrid solver for unsteady saturated Darcy flow.		
$\mathtt{TYPE} = < selection: \ DarcyFlowMH\_TYPE\_selection>$		
Default: Unsteady_LMH	[]	
Sub-record selection.		
${\tt n\_schurs} = <\! Integer \ [0,\ 2]\!\!>$		



ID of the region where to set fields.  $\mbox{time} = <\!Double~[0,~]\!> \\ \mbox{Default:}~0.0$ 

Apply field setting in this record after this time. These times has to form an increasing sequence.

 $\texttt{bc\_type} = < abstract \ type: \ Field:R3 \rightarrow Enum>$ 

Default: <optional>

Boundary condition type, possible values:

 $bc\_pressure = \langle abstract \ type: \ Field:R3 \rightarrow Real \rangle$ 

Default: <optional>

Dirichlet BC condition value for pressure.

 $bc_flux = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: <optional>

Flux in Neumman or Robin boundary condition.

 $bc\_robin\_sigma = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: < optional>

Conductivity coefficient in Robin boundary condition.

 $bc\_piezo\_head = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: <optional>

Boundary condition for piezometric head.

 ${\tt flow\_old\_bcd\_file} = <\! input \, file \, \, name \!\! > \!\!$ 

Default: <optional>

abstract type: Field:R3  $\rightarrow$  Enum default descendant: FieldConstant

Descendants:

Abstract record for all time-space functions.

FieldConstant

FieldFormula

FieldPython

FieldElementwise

record: FieldConstant implements abstract type: Field:R3  $\rightarrow$  Enum constructible from key: value

 $R3 \rightarrow Enum$  Field constant in space.

 $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Enum\_TYPE\_selection>$ 

Default: FieldConstant []

Sub-record selection.

value = < selection: EqData\_bc\_Type>

Default: < obligatory>

Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix.

### record: FieldFormula implements abstract type: Field:R3 $\rightarrow$ Enum

 $R3 \rightarrow Enum$  Field given by runtime interpreted formula.

 $\texttt{TYPE} = <\! selection \colon \mathit{Field} : R3 \to \mathit{Enum\_TYPE\_selection} \!\!>$ 

Default: FieldFormula

Sub-record selection.

value = < String (generic)>

Default: <obligatory>

String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions.

### record: FieldPython implements abstract type: Field:R3 $\rightarrow$ Enum

 $R3 \rightarrow Enum$  Field given by a Python script.

 $\texttt{TYPE} = <\!\! selection \colon \mathit{Field} : R3 \to \mathit{Enum\_TYPE\_selection} \!\!>$ 

Default: FieldPython []

Sub-record selection.

script\_string = <String (generic)>

Default: "Obligatory if 'script\_file' is not given."

Python script given as in place string

script\_file = <input file name>

Default: "Obligatory if 'script\_striong' is not given."

Python script given as external file

 $function = \langle String (generic) \rangle$ 

Default: <obligatory>

Function in the given script that returns tuple containing components of the return type. For NxM tensor values: tensor(row,col) = tuple(M\*row + col).

record: FieldElementwise implements abstract type: Field:R3  $\rightarrow$  Enum

 $R3 \rightarrow Enum$  Field constant in space.

 $\mathtt{TYPE} = \langle selection: \ Field:R3 \rightarrow Enum\_TYPE\_selection \rangle$ 

Default: FieldElementwise

Sub-record selection.

gmsh\_file = <input file name>

Default: <obligatory>

Input file with ASCII GMSH file format.

 $field_name = \langle String (generic) \rangle$ 

Default: <obligatory>

The values of the Field are read from the \$ElementData section with field name given by this key.

abstract type: Field:R3  $\rightarrow$  Real default descendant: FieldConstant

Descendants:

Abstract record for all time-space functions.

FieldConstant

FieldFormula

FieldPython

FieldElementwise

record: FieldConstant implements abstract type: Field:R3  $\rightarrow$  Real constructible from key: value

 $R3 \rightarrow Real$  Field constant in space.

 $\mathtt{TYPE} = \langle selection : Field : R3 \rightarrow Real\_TYPE\_selection \rangle$ 

Default: FieldConstant

Sub-record selection.

value = < Double >

Default: <obliqatory>

Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix.

record: FieldFormula implements abstract type: Field:R3  $\rightarrow$  Real

 $R3 \rightarrow Real$  Field given by runtime interpreted formula.

 $\mathtt{TYPE} = \langle selection : Field : R3 \rightarrow Real\_TYPE\_selection \rangle$ Default: FieldFormula Sub-record selection. value = < String (generic)> Default: < obligatory> String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions. record: FieldPython implements abstract type: Field:R3  $\rightarrow$  Real  $R3 \rightarrow Real Field given by a Python script.$  $\mathtt{TYPE} = \langle selection : Field : R3 \rightarrow Real\_TYPE\_selection \rangle$ Default: FieldPython Sub-record selection. script\_string = <String (generic)> Default: "Obligatory if 'script\_file' is not given." Python script given as in place string script\_file = <input file name> Default: "Obligatory if 'script\_striong' is not given." Python script given as external file  $function = \langle String (generic) \rangle$ Default: < obligatory> Function in the given script that returns tuple containing components of the return type. For NxM tensor values: tensor(row,col) = tuple(M\*row + col). record: FieldElementwise implements abstract type: Field:R3  $\rightarrow$  Real  $R3 \rightarrow Real Field constant in space.$  $\mathtt{TYPE} = \langle selection: Field:R3 \rightarrow Real\_TYPE\_selection \rangle$ Default: FieldElementwise Sub-record selection. gmsh\_file = <input file name> Default: < oblique tory> 

Input file with ASCII GMSH file format.

field\_name = < String (generic)> Default: < oblique tory> The values of the Field are read from the \$ElementData section with field name given by this key. record: DarcyFlowMH\_Steady\_BulkData Record to set BULK fields of the equation 'DarcyFlowMH\_Steady'. The fields are set only on the domain specified by one of the keys: 'region', 'rid', 'r\_set' and after the time given by the key 'time'. The field setting can be overridden by any DarcyFlowMH\_Steady\_BulkData record that comes later in the bulk data array. r\_set = < String (generic)> Default: < optional> Name of region set where to set fields.  $region = \langle String (generic) \rangle$ Default: < optional> Label of the region where to set fields.  $rid = \langle Integer [0,] \rangle$ Default: < optional> ID of the region where to set fields.  $time = \langle Double /0, \rangle$ Default: 0.0 Apply field setting in this record after this time. These times has to form an increasing sequence. anisotropy =  $\langle abstract\ type:\ Field:R3 \rightarrow Real[3,3] \rangle$ Default: < optional> Anisothropic conductivity tensor.  $cross\_section = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: < optional> Complement dimension parameter (cross section for 1D, thickness for 2D). conductivity =  $\langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: < optional> Isothropic conductivity scalar.  $sigma = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: < optional> Transition coefficient between dimensions.

water\_source\_density =  $\langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: < optional > []

Water source density.

init\_pressure =  $< abstract \ type: \ Field:R3 \rightarrow Real >$ Default: < optional > []

Initial condition as pressure

storativity =  $< abstract \ type: \ Field:R3 \rightarrow Real >$ Default: < optional > []

Storativity.

 $\verb|init_piezo_head| = < abstract type: Field: R3 \rightarrow Real >$ 

Default: <optional>

Initial piezometric head.

abstract type: Field:R3  $\rightarrow$  Real default descendant: FieldConstant

Descendants:

Abstract record for all time-space functions.

FieldConstant

FieldFormula

FieldPython

FieldElementwise

record: FieldConstant implements abstract type: Field:R3  $\rightarrow$  Real constructible from key: value

 $R3 \rightarrow Real$  Field constant in space.

 $\mathtt{TYPE} = \langle selection \colon \mathit{Field} : R3 \to \mathit{Real\_TYPE\_selection} \rangle$ 

Default: FieldConstant []

Sub-record selection.

value = < Double >

Default: <obliqatory>

Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix.

record: FieldFormula implements abstract type: Field:R3  $\rightarrow$  Real

 $\mathrm{R3} \to \mathrm{Real}$  Field given by runtime interpreted formula.

 $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Real\_TYPE\_selection>$ 

Default: FieldFormula Sub-record selection. value = < String (generic)> Default: < oblique or y> String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions. record: FieldPython implements abstract type: Field:R3  $\rightarrow$  Real  $R3 \rightarrow Real Field given by a Python script.$  $\mathtt{TYPE} = \langle selection: \ Field:R3 \rightarrow Real\_TYPE\_selection \rangle$ Default: FieldPython Sub-record selection. script\_string = <String (generic)> Default: "Obligatory if 'script\_file' is not given." Python script given as in place string script\_file = <input file name> Default: "Obligatory if 'script\_striong' is not given." Python script given as external file  $function = \langle String (generic) \rangle$ Default: < obligatory> Function in the given script that returns tuple containing components of the return type. For NxM tensor values: tensor(row,col) = tuple(M\*row + col). record: FieldElementwise implements abstract type: Field:R3  $\rightarrow$  Real  $R3 \rightarrow Real$  Field constant in space.  $\mathtt{TYPE} = < selection: \ Field:R3 \rightarrow Real\_TYPE\_selection>$ Default: FieldElementwise Sub-record selection. gmsh\_file = <input file name> Default: < oblique tory> Input file with ASCII GMSH file format.

 $field_name = \langle String (generic) \rangle$ 

The values of the Field are read from the \$ElementData section with field name given by this key. abstract type: **Transport** Descendants: Secondary equation for transport of substances. TransportOperatorSplitting AdvectionDiffusion\_DG record: TransportOperatorSplitting implements abstract type: Transport Explicit FVM transport (no diffusion) coupled with reaction and sorption model (ODE per element) via. operator splitting.  $\mathtt{TYPE} = \langle selection: Transport\_TYPE\_selection \rangle$ Default: TransportOperatorSplitting Sub-record selection. time = < record: TimeGovernor> Default: < oblique tory> Time governor setting for the transport model. substances = <Array of String (generic)> Default: < obligatory> Names of transported substances.  $sorption_enable = < Bool>$ Default: false Model of sorption.  $dual_porosity = \langle Bool \rangle$ Default: false Dual porosity model. sources\_file = <input file name> Default: < optional> File with data for the source term in the transport equation. output = < record: TransportOutput> Default: < obligatory> Parameters of output stream. reactions = <abstract type: Reactions> Default: < optional> 

Default: < obligatory>

Initialization of per element reactions.

bc\_data = < Array of record: TransportOperatorSplitting\_BoundaryData> Default: < oblique tory> bulk\_data = < Array of record: TransportOperatorSplitting\_BulkData> Default: < obliqatory> record: TransportOutput Output setting for transport equations. output\_stream = < record: OutputStrem> Default: < oblique tory> Parameters of output stream.  $save\_step = < Double [0, ]>$ Default: < obligatory> Interval between outputs.  $output\_times = <Array of Double [0,]>$ Default: < optional> Explicit array of output times (can be combined with 'save\_step'.  $conc\_mobile\_p0 = < String (generic) >$ Default: < optional> Name of output stream for P0 approximation of the concentration in mobile conc\_immobile\_p0 = <String (generic)> Default: < optional> Name of output stream for P0 approximation of the concentration in immobile phase. conc\_mobile\_sorbed\_p0 = < String (generic)> Default: < optional> Name of output stream for P0 approximation of the surface concentration of sorbed mobile phase. conc\_immobile\_sorbed\_p0 = <String (generic)> Default: < optional> Name of output stream for P0 approximation of the surface concentration of sorbed immobile phase.

abstract type: **Reactions** 

Descendants:

Equation for reading information about simple chemical reactions.

# LinearReactions

# PadeApproximant

# Isotope

record: LinearReactions implements abstract type: Reactions	
Information for a decision about the way to simulate radioactive decay.	
${\tt TYPE} = <\! selection: \ Reactions\_TYPE\_selection >$	
Default: LinearReactions	
Sub-record selection.	
$decays = \langle Array \ of \ record: \ \underline{Substep} \rangle$	
Default: < obligatory>	
Description of particular decay chain substeps.	
$\mathtt{matrix\_exp\_on} = <\!Bool\!>$	
Default: false	
Enables to use Pade approximant of matrix exponential.	
record: Substep	
Equation for reading information about radioactive decays.	
$parent = \langle String \ (generic) \rangle$	
Default: <obligatory></obligatory>	[
Identifier of an isotope.	
${\tt half\_life} = <\!Double>$	
Default: < optional>	[
Half life of the parent substance.	
$ ext{kinetic} = <\!Double>$	
Default: < optional>	[
Kinetic constants describing first order reactions.	
$products = \langle Array \ of \ String \ (generic) \rangle$	
Default: < obligatory>	[
Identifies isotopes which decays parental atom to.	
${\tt branch\_ratios} = <\!\!Array \ of \ Double>$	
Default: 1.0	[
Decay chain branching percentage.	

# record: PadeApproximant implements abstract type: Reactions Abstract record with an information about pade approximant parameters. $\mathtt{TYPE} = \langle selection: Reactions\_TYPE\_selection \rangle$ Default: PadeApproximant Sub-record selection. decays = < Array of record: Substep> Default: < oblique tory> Description of particular decay chain substeps. $nom_pol_deg = < Integer >$ Default: 2 Polynomial degree of the nominator of Pade approximant. $den_pol_deg = \langle Integer \rangle$ Default: 2 Polynomial degree of the nominator of Pade approximant record: Substep Equation for reading information about radioactive decays. parent = < String (generic)> Default: < obligatory> Identifier of an isotope. $half\_life = < Double >$ Default: < optional> Half life of the parent substance. kinetic = < Double >Default: < optional> Kinetic constants describing first order reactions. products = <Array of String (generic)> Default: < obligatory> Identifies isotopes which decays parental atom to. branch\_ratios = <Array of Double > Default: 1.0 Decay chain branching percentage. record: Isotope implements abstract type: Reactions

Definition of information about a single isotope.

 $TYPE = \langle selection: Reactions\_TYPE\_selection \rangle$ Default: Isotope Sub-record selection. identifier = < Integer >Default: <obligatory> Identifier of the isotope.  $half_life = < Double >$ Default: < oblique or y> Half life parameter. record: TransportOperatorSplitting\_BoundaryData Record to set BOUNDARY fields of the equation 'TransportOperatorSplitting'. The fields are set only on the domain specified by one of the keys: 'region', 'rid', 'r\_set' and after the time given by the key 'time'. The field setting can be overridden by any TransportOperatorSplitting\_BoundaryData record that comes later in the boundary data array. r\_set = < String (generic)> Default: < optional> Name of region set where to set fields.  $region = \langle String (generic) \rangle$ Default: < optional> Label of the region where to set fields.  $rid = \langle Integer [0,] \rangle$ Default: < optional> ID of the region where to set fields. time = < Double /0, >Default: 0.0 Apply field setting in this record after this time. These times has to form an increasing sequence.  $bc\_conc = \langle abstract \ type: Field:R3 \rightarrow Real[n] \rangle$ Default: < optional> Boundary conditions for concentrations. old\_boundary\_file = <input file name> Default: < optional> Input file with boundary conditions (obsolete).

 $bc\_times = < Array \ of \ Double >$ 

Default: < optional> Times for changing the boundary conditions (obsolete). abstract type:  $Field:R3 \rightarrow Real[n]$  default descendant: FieldConstantDescendants: Abstract record for all time-space functions. FieldConstant FieldPython FieldFormula FieldElementwise FieldInterpolatedP0 record: FieldConstant implements abstract type: Field:R3  $\rightarrow$  Real[n] constructible from key: value  $R3 \to Real[n]$  Field constant in space.  $\mathtt{TYPE} = \langle selection: \ Field: R3 \rightarrow Real[n]\_TYPE\_selection \rangle$ Default: FieldConstant Sub-record selection.  $value = \langle Array | 1, | of Double \rangle$ Default: < obligatory> Value of the constant field. For vector values, you can use scalar value to enter constant vector. For square NxN-matrix values, you can use: \* vector of size N to enter diagonal matrix \* vector of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* scalar to enter multiple of the unit matrix. record: FieldPython implements abstract type: Field:R3  $\rightarrow$  Real[n]  $R3 \rightarrow Real[n]$  Field given by a Python script.  $\mathtt{TYPE} = \langle selection: \ Field: R3 \rightarrow Real[n]\_TYPE\_selection \rangle$ Default: FieldPython Sub-record selection. script\_string = <String (generic)> Default: "Obligatory if 'script\_file' is not given." Python script given as in place string script\_file = <input file name> Default: "Obligatory if 'script\_striong' is not given." 

Python script given as external file

 $function = \langle String (generic) \rangle$ Default: < oblique or y> Function in the given script that returns tuple containing components of the return type. For NxM tensor values: tensor(row,col) = tuple(M\*row + col). record: FieldFormula implements abstract type: Field:R3  $\rightarrow$  Real[n]  $R3 \to Real[n]$  Field given by runtime interpreted formula.  $\mathtt{TYPE} = \langle selection: \ Field: R3 \rightarrow Real[n]\_TYPE\_selection \rangle$ Default: FieldFormula Sub-record selection. value = <Array [1, ] of String (generic)> Default: < obligatory> String, array of strings, or matrix of strings with formulas for individual entries of scalar, vector, or tensor value respectively. For vector values, you can use just one string to enter homogeneous vector. For square NxN-matrix values, you can use: \* array of strings of size N to enter diagonal matrix \* array of strings of size (N+1)\*N/2 to enter symmetric matrix (upper triangle, row by row) \* just one string to enter (spatially variable) multiple of the unit matrix. Formula can contain variables x,y,z,t and usual operators and functions. record: FieldElementwise implements abstract type: Field:R3  $\rightarrow$  Real[n]  $R3 \to Real[n]$  Field constant in space.  $\mathtt{TYPE} = \langle selection: \ Field: R3 \rightarrow Real/n/\_TYPE\_selection \rangle$ Default: FieldElementwise Sub-record selection. gmsh\_file = <input file name> Default: < obligatory> Input file with ASCII GMSH file format.

field\_name = <String (generic)>

Default: <obliqatory>

The values of the Field are read from the \$ElementData section with field name given by this key.

### record: FieldInterpolatedP0 implements abstract type: Field:R3 $\rightarrow$ Real[n]

Field given by P0 data on another mesh. Currently defined only on boundary.

 $\mathtt{TYPE} = \langle selection: \ Field: R3 \rightarrow Real[n]\_TYPE\_selection \rangle$ 

Default: FieldInterpolatedP0 []

Sub-record selection.

 $mesh = \langle input \ file \ name \rangle$ 

Default: <obligatory>

File with the mesh from which we interpolate. (currently only GMSH supported)

raw\_data = <input file name>

Default: <obligatory>

File with raw output from flow calculation. Currently we can interpolate only pressure.

### record: TransportOperatorSplitting\_BulkData

Record to set BULK fields of the equation 'TransportOperatorSplitting'. The fields are set only on the domain specified by one of the keys: 'region', 'rid', 'r\_set' and after the time given by the key 'time'. The field setting can be overridden by any TransportOperatorSplitting\_BulkData record that comes later in the bulk data array.

 $r_set = \langle String (generic) \rangle$ 

Default: <optional>

Name of region set where to set fields.

 $region = \langle String (generic) \rangle$ 

Default: <optional>

Label of the region where to set fields.

 $rid = \langle Integer [0,] \rangle$ 

Default: <optional>

ID of the region where to set fields.

time = < Double /0, >

Default: 0.0

Apply field setting in this record after this time. These times has to form an increasing sequence.

 $init\_conc = \langle abstract\ type:\ Field:R3 \rightarrow Real[n] \rangle$ 

Default: <optional>

Initial concentrations.

 $por_m = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: <optional>

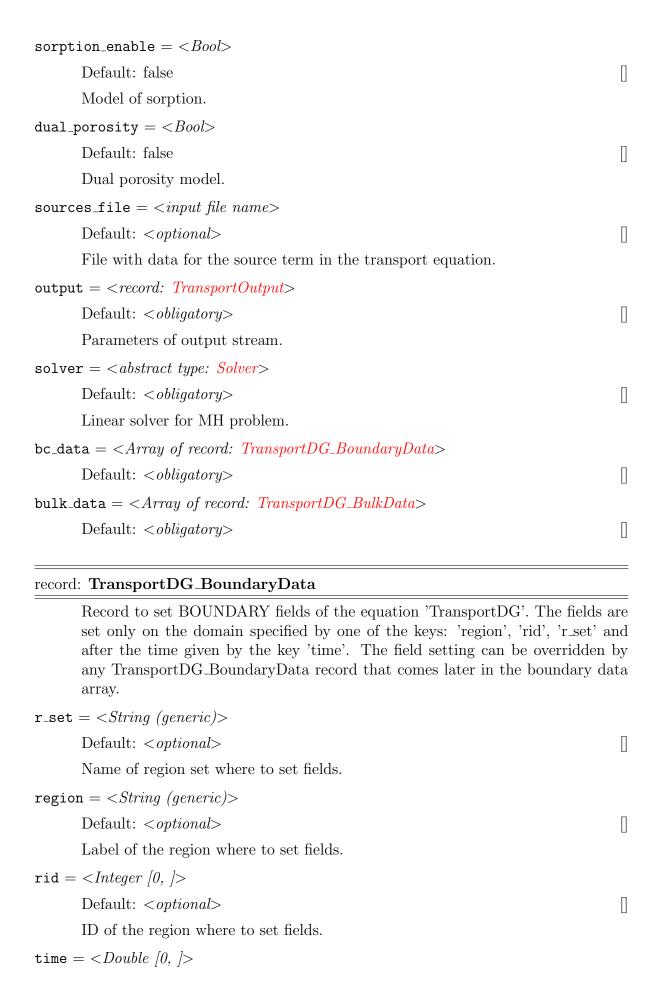
Mobile porosity

 $por_imm = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: <optional>

Immobile porosity

```
alpha = \langle abstract\ type:\ Field:R3 \rightarrow Real/n/ >
        Default: < optional>
                                                                                                  Coefficients of non-equilibrium exchange.
sorp_type = \langle abstract\ type:\ Field:R3 \rightarrow Real/n/\rangle
        Default: < optional>
                                                                                                  Type of sorption.
sorp\_coef0 = \langle abstract\ type:\ Field:R3 \rightarrow Real[n] \rangle
        Default: < optional>
                                                                                                  Coefficient of sorption.
sorp\_coef1 = \langle abstract\ type:\ Field:R3 \rightarrow Real[n] \rangle
        Default: < optional>
                                                                                                  Coefficient of sorption.
phi = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle
       Default: < optional>
                                                                                                  Solid / solid mobile.
sources_density = \langle abstract\ type: Field:R3 \rightarrow Real[n] \rangle
                                                                                                  Default: < optional>
       Density of transport sources.
sources\_sigma = \langle abstract\ type:\ Field:R3 \rightarrow Real[n] \rangle
        Default: < optional>
                                                                                                  sources\_conc = \langle abstract \ type: \ Field:R3 \rightarrow Real[n] \rangle
        Default: < optional>
                                                                                                  Concentration sources.
record: AdvectionDiffusion_DG implements abstract type: Transport
        DG solver for transport with diffusion.
\mathtt{TYPE} = \langle selection: Transport\_TYPE\_selection \rangle
        Default: AdvectionDiffusion_DG
                                                                                                  Sub-record selection.
time = <record: TimeGovernor>
        Default: < obligatory>
                                                                                                  Time governor setting for the transport model.
substances = <Array of String (generic)>
       Default: < oblique tory>
                                                                                                  Names of transported substances.
```



Default: 0.0 []

Apply field setting in this record after this time. These times has to form an

Apply field setting in this record after this time. These times has to form an increasing sequence.

 $\texttt{bc\_conc} = < abstract \ type: \ Field:R3 \rightarrow \ Real[n] >$ 

Default: <optional>

Boundary conditions for concentrations.

old\_boundary\_file = <input file name>

Default: <optional>

Input file with boundary conditions (obsolete).

 $bc\_times = <Array \ of \ Double >$ 

Default: <optional>

Times for changing the boundary conditions (obsolete).

### record: TransportDG\_BulkData

Record to set BULK fields of the equation 'TransportDG'. The fields are set only on the domain specified by one of the keys: 'region', 'rid', 'r\_set' and after the time given by the key 'time'. The field setting can be overridden by any TransportDG\_BulkData record that comes later in the bulk data array.

 $r_set = \langle String (generic) \rangle$ 

Default: <optional>

Name of region set where to set fields.

 $region = \langle String (qeneric) \rangle$ 

Default: <optional>

Label of the region where to set fields.

 $rid = \langle Integer /0, \rangle \rangle$ 

Default: <optional>

ID of the region where to set fields.

time = < Double /0, >

Default: 0.0

Apply field setting in this record after this time. These times has to form an increasing sequence.

 $init\_conc = \langle abstract\ type:\ Field:R3 \rightarrow Real[n] \rangle$ 

Default: <optional>

Initial concentrations.

 $por_m = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Default: <optional>

Mobile porosity  $disp_l = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: <optional> Longitudal dispersivity.  $disp_t = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: < optional> Transversal dispersivity.  $diff_m = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: < optional> Molecular diffusivity.  $sigma_c = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ Default: < optional> Coefficient of diffusive transfer through fractures.  $dg_{penalty} = \langle abstract\ type:\ Field:R3 \rightarrow Real \rangle$ 

Penalty parameter influencing the discontinuity of the solution.

Default: < optional>

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