



--	--	--

Semester One 2022 Examination Period

Faculty of Business & Economics

EXAM CODES: ETC3550/ETC5550 - PAPER 1

TITLE OF PAPER: Applied Forecasting

EXAM DURATION: 2 hours 40 minutes

READING TIME: 0 minutes

THIS PAPER IS FOR STUDENTS STUDYING AT: (tick where applicable)

- ☐ Caulfield ☒ Clayton ☐ Parkville ☐ Peninsula
☐ Monash Extension ☐ Off Campus Learning ☐ Malaysia ☐ South Africa
☐ Other (specify)

During an exam, you must not have in your possession any item/material that has not been authorised for your exam. This includes books, notes, paper, electronic device/s, mobile phone, smart watch/device, calculator, pencil case, or writing on any part of your body. Any authorised items are listed below. Items/materials on your desk, chair, in your clothing or otherwise on your person will be deemed to be in your possession.

No examination materials are to be removed from the room. This includes retaining, copying, memorising or noting down content of exam material for personal use or to share with any other person by any means following your exam.

Failure to comply with the above instructions, or attempting to cheat or cheating in an exam is a discipline offence under Part 7 of the Monash University (Council) Regulations, or a breach of instructions under Part 3 of the Monash University (Academic Board) Regulations.

AUTHORISED MATERIALS

OPEN BOOK ☒ YES ☐ NO

CALCULATORS ☒ YES ☐ NO
Only HP 10bII+ or Casio FX82 (any suffix) calculator permitted

SPECIFICALLY PERMITTED ITEMS ☐ YES ☒ NO
if yes, items permitted are:

Candidates must complete this section if required to write answers within this paper

STUDENT ID: _____

DESK NUMBER: _____

The exam contains FIVE questions. ALL questions must be answered. The exam is worth 100 marks in total.

SECTION A

Write about a quarter of a page each on any **four** of the following topics. Clearly state if you agree or disagree with each statement.

1. Events like COVID-19 show that forecasting is never a good idea because the future is too unpredictable.
2. Taking logarithms of the data is useful for stabilizing the variance of a time series.
3. Regression models are better than ARIMA models because the coefficients are more interpretable.
4. The best forecasting model has white noise residuals.
5. Choosing a model using the AICc is better than choosing a model on the basis of a test set because it involves all the data.
6. The MAPE is the best accuracy measure because it is easy to understand and is independent of the scale of the data.

Total: 20 marks

— END OF SECTION A —

SECTION B

Figures 1, 2 and 3 relate to the daily page views on the OTexts website from 1 January 2018 to 10 April 2022.

1. Using Figures 1, 2 and 3, describe the daily page views on the OTexts website. Carefully comment on the interesting features of all three plots.

6 marks

```
otexts %>%
  autoplot(Pageviews) +
  labs(subtitle = "Daily Pageviews on OTexts.com", y = "Thousands")
```

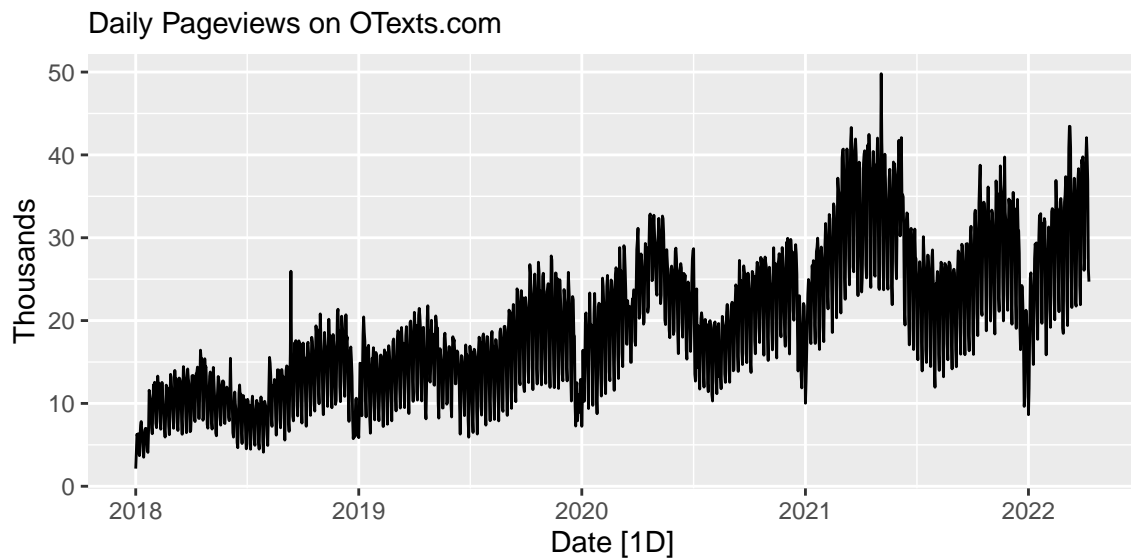


Figure 1:

```
otexts %>%
  gg_season(Pageviews, period = "year") +
  labs(subtitle = "Daily Pageviews on OTexts.com", y = "Thousands")
```

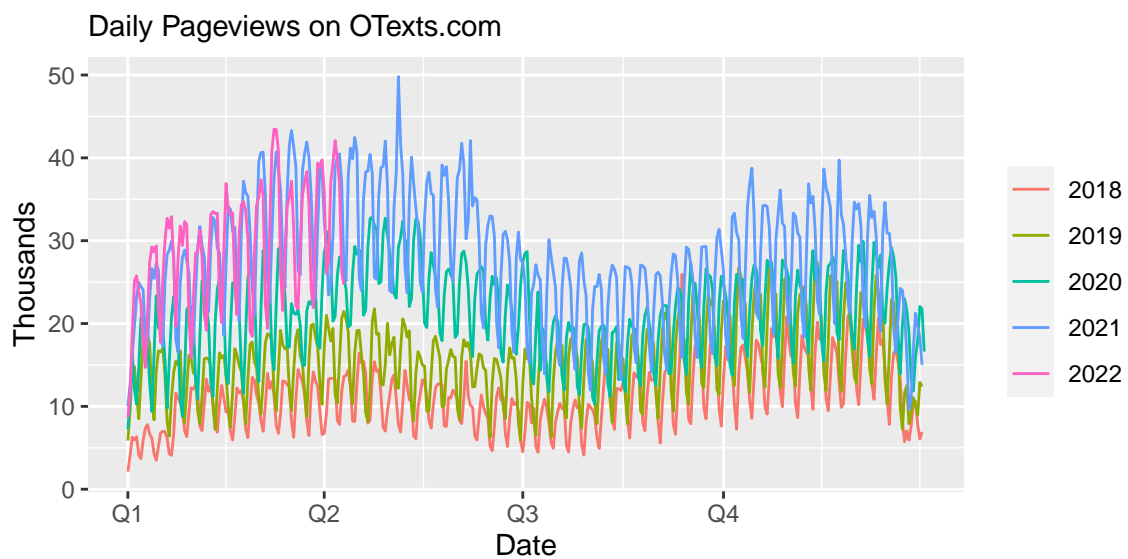


Figure 2:

```
otexts %>%
  gg_season(Pageviews, period = "week") +
  labs(subtitle = "Daily Pageviews on OTexts.com", y = "Thousands")
```

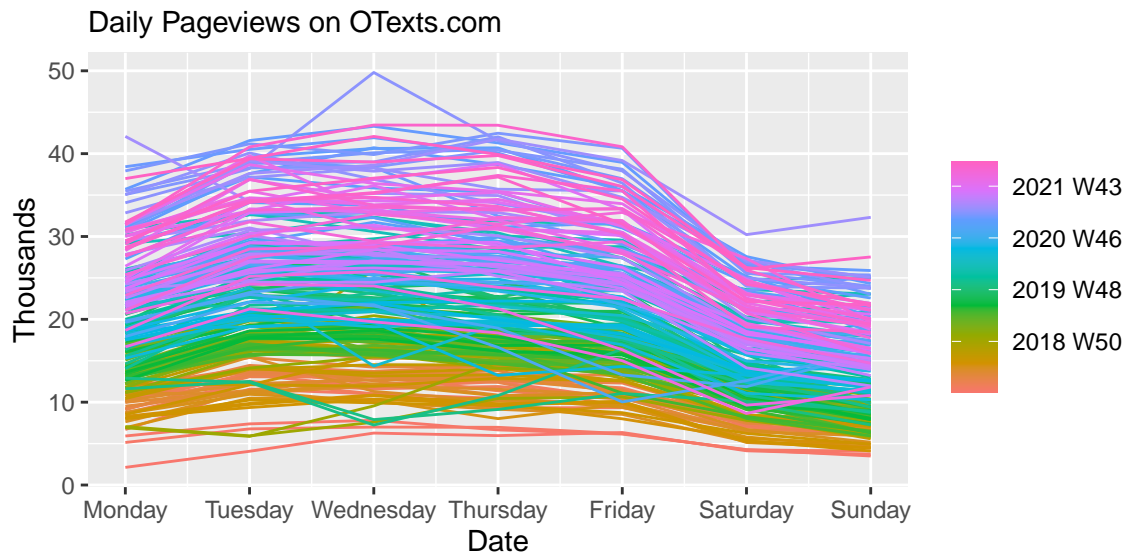


Figure 3:

2. Figure 4 was created using the code below. Why has a logarithm been used? Comment on the choice of the window argument in each term. What would you expect if the window values were substantially changed?

4 marks

```
otexts %>%
  model(STL(log(Pageviews) ~ trend(window = 99) +
    season(period = "week", window = 99) +
    season(period = "year", window = 9),
    robust = TRUE
  )) %>%
  components() %>%
  autoplot()
```

STL decomposition

'log(Pageviews)' = trend + season_week + season_year + remainder

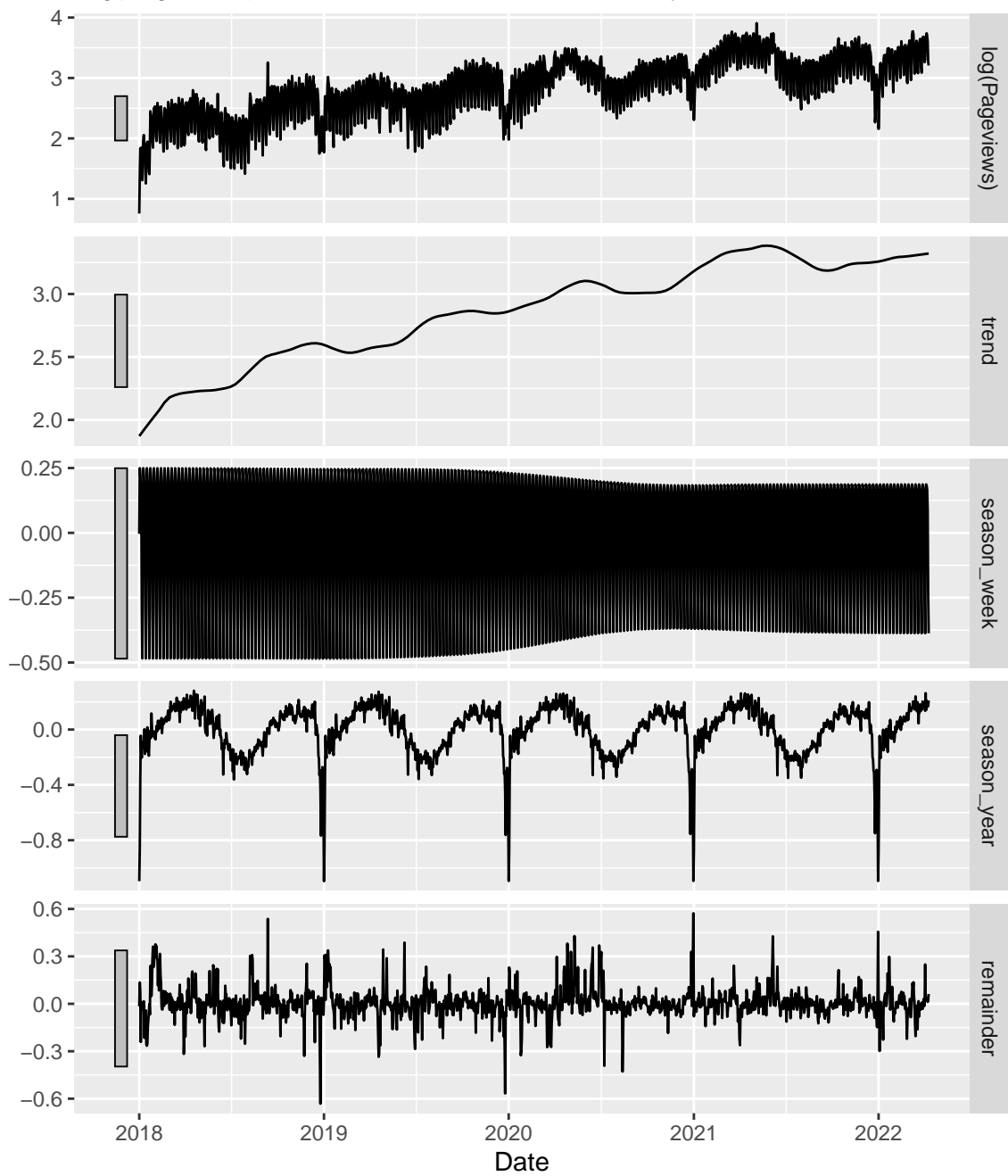


Figure 4:

3. You have been asked to provide forecasts for the next four weeks for OTexts pageviews.

Consider applying each of the methods and models below. Comment, in a few words each, on whether each one is appropriate for forecasting the data. No marks will be given for simply guessing whether a method or a model is appropriate without justifying your choice.

Start your response by stating: **suitable** or **not suitable**.

- (a) Seasonal naïve method using annual seasonality.
- (b) Seasonal naïve method using weekly seasonality.
- (c) An STL decomposition on the log transformed data combined with an ETS to forecast the seasonally adjusted component, and seasonal naïve methods for both seasonal components.
- (d) Holt-Winters method with damped trend and multiplicative weekly seasonality.
- (e) ETS(A,N,A).
- (f) ETS(M,A,M) with annual seasonality.
- (g) ARIMA(2,2,2)(0,0,0)₇ applied to the log transformed data.
- (h) ARIMA(0,1,1)(0,1,1)₇ applied to the log transformed data.
- (i) Regression with time and Fourier terms for both weekly and annual seasonality.
- (j) Dynamic regression on the log transformed data with Fourier terms for the annual seasonality and a seasonal ARIMA model to handle the weekly seasonality and other dynamics.

10 marks

Total: 20 marks

— END OF SECTION B —

SECTION C

The output below shows the results of fitting an ETS model to the Pageviews variable.

```
fit <- otexts %>%
  model(ETS(Pageviews))
report(fit)

## Series: Pageviews
## Model: ETS(M,A,M)
## Smoothing parameters:
##   alpha = 0.5737414
##   beta  = 0.0001000033
##   gamma = 0.1266783
##
## Initial states:
##   l[0]    b[0]    s[0]    s[-1]    s[-2]    s[-3]    s[-4]    s[-5]
## 3.605899 0.1449521 0.6318171 0.7210449 1.035443 1.163588 1.300494 1.20237
##   s[-6]
## 0.9452431
##
## sigma^2: 0.0101
##
##      AIC      AICc      BIC
## 13337.34 13337.54 13401.58
```

1. Write down the observation and state equations for the model, specifying which is the observation equation, what parameters have been optimized, and explaining why this particular model was chosen.
2. Figure 5 shows the components of the model. Explain what has been plotted, and how these plots relate to the equations shown earlier. Explain how the values of beta and gamma shown earlier correspond to features of these plots.

6 marks

5 marks

```
fit %>%
  components() %>%
  autoplot()
```

ETS(M,A,M) decomposition

$$\text{Pageviews} = (\text{lag}(\text{level}, 1) + \text{lag}(\text{slope}, 1)) * \text{lag}(\text{season}, 7) * (1 + \text{remainder})$$

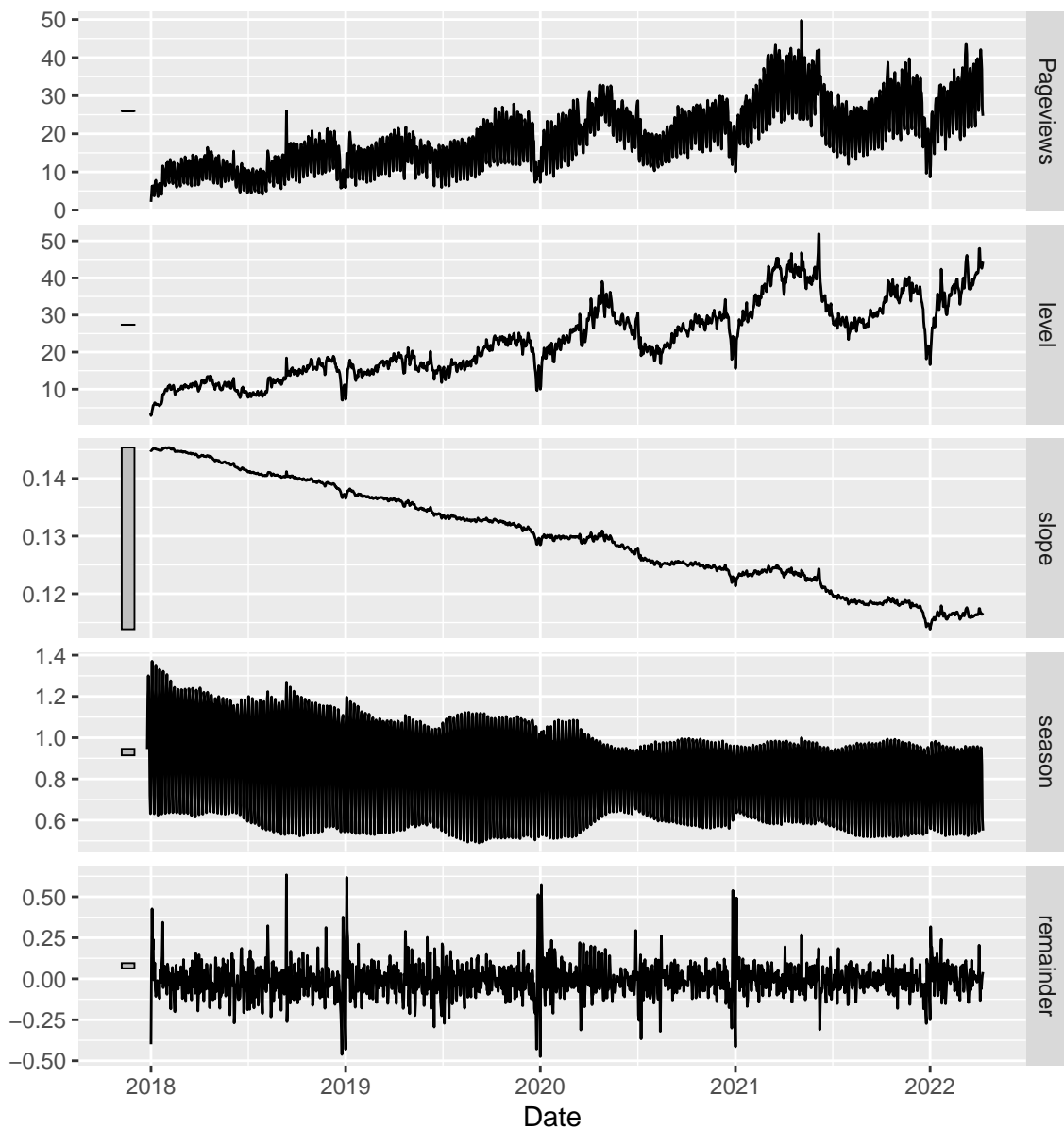


Figure 5:

3. How have the annual and weekly seasonalities been handled by this ETS model?

3 marks

4. Comment on the large residuals seen at the end of each year, and the dip in the level at the end of each year. What is causing these?

2 marks

5. Do you expect this model to produce good forecasts for the next 3 weeks? What about for the next 12 months? Explain.

4 marks

Total: 20 marks

— END OF SECTION C —

SECTION D

It is decided to fit a dynamic regression model to the data, with Fourier terms to handle the annual seasonality, and a seasonal ARIMA error to handle the weekly seasonality.

```
fit_arima <- otexits %>%  
  model(  
    dr = ARIMA(log(Pageviews) ~ fourier(period = "year", K = 4) + PDQ(period = "week"))  
  )  
report(fit_arima)
```

```
## Series: Pageviews  
## Model: LM w/ ARIMA(1,0,2)(2,1,1)[7] errors  
## Transformation: log(Pageviews)  
##  
## Coefficients:  
##          ar1      ma1      ma2      sar1      sar2      sma1  
##      0.8858 -0.1213 -0.1750  0.1600  0.0247 -0.9046  
## s.e.  0.0236  0.0361  0.0341  0.0307  0.0298  0.0182  
##      fourier(period = "year", K = 4)C1_365  
##                                0.0071  
## s.e.                                0.0318  
##      fourier(period = "year", K = 4)S1_365  
##                                0.0928  
## s.e.                                0.0319  
##      fourier(period = "year", K = 4)C2_365  
##                                -0.1580  
## s.e.                                0.0251  
##      fourier(period = "year", K = 4)S2_365  
##                                -0.0818  
## s.e.                                0.0255  
##      fourier(period = "year", K = 4)C3_365  
##                                -0.0440  
## s.e.                                0.0228  
##      fourier(period = "year", K = 4)S3_365  
##                                0.0183  
## s.e.                                0.0229  
##      fourier(period = "year", K = 4)C4_365  
##                                -0.0575  
## s.e.                                0.0208  
##      fourier(period = "year", K = 4)S4_365  
##                                0.0018  
## s.e.                                0.0209  
##  
## sigma^2 estimated as 0.009012:  log likelihood=1456.1  
## AIC=-2882.21   AICc=-2881.9   BIC=-2801.98
```

1. Write down the model using backshift notation.

6 marks

2. Comment on the model diagnostics shown in Figure 6 and the output below. How might the model be improved? Do you think the resulting forecasts will be reliable?

5 marks

```
augment(fit_arma) %>%
  gg_tsdisplay(.innov, "histogram")
```

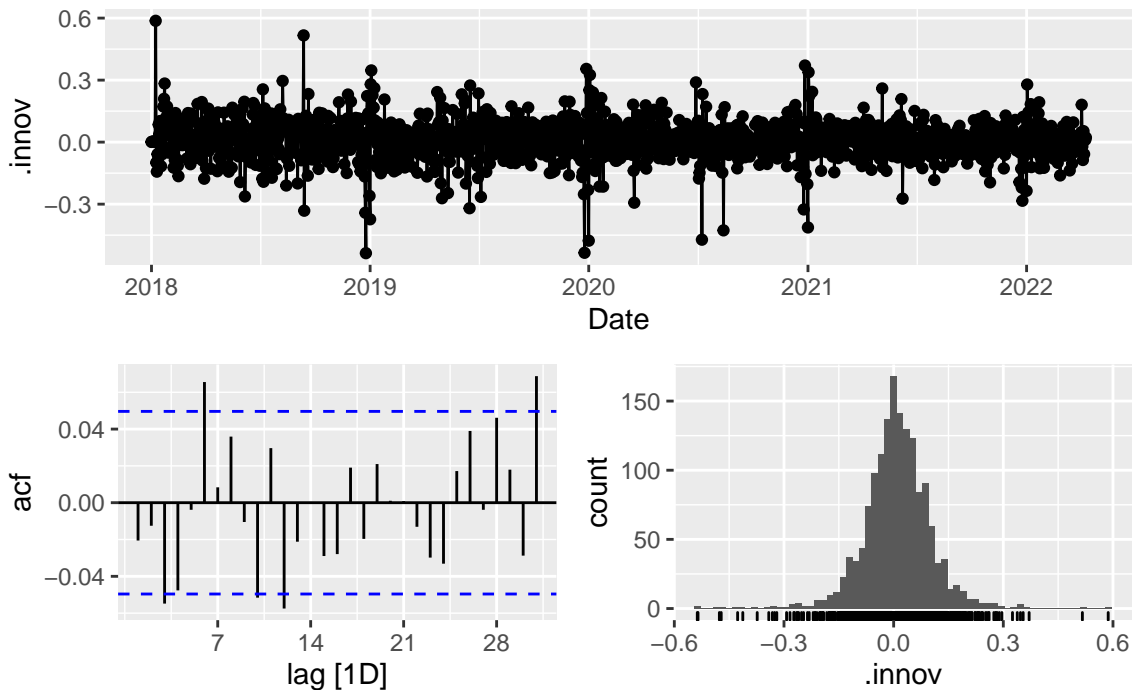


Figure 6:

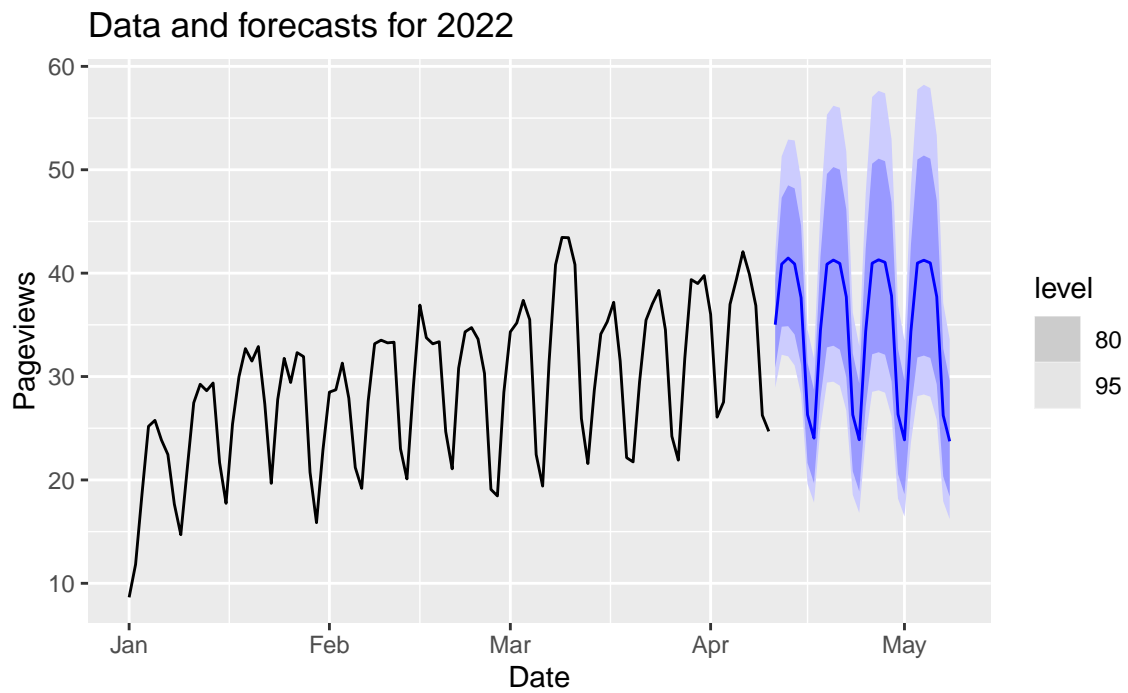
```
augment(fit_arma) %>%
  features(.innov, lbjung_box, lag = 28, dof = 14)
```

```
## # A tibble: 1 x 3
##   .model lb_stat lb_pvalue
##   <chr>   <dbl>   <dbl>
## 1 dr      43.9 0.0000617
```

3. Figure 7 shows forecasts with prediction intervals for the next four weeks, along with the data from 2022. The forecasts appear to have no trend. Why is that? If you wanted to include a *local* trend, how would you modify the model?

3 marks

```
fit_arma %>%
  forecast(h = "4 weeks") %>%
  autoplot(otexts %>% filter(year(Date) == 2022)) +
  labs(title = "Data and forecasts for 2022")
```



4. The one-step-ahead forecast is 35.0 pageviews. Give a 95% prediction interval assuming Gaussian innovation residuals.

4 marks

5. It is thought that pageviews will be higher during teaching semesters. How would you modify this model to allow for a semester effect?

2 marks

Total: 20 marks

— END OF SECTION D —

SECTION E

1. You decide to compare three different models on this data set: (a) the ETS model from Section C; (b) the dynamic regression model from Section D; and (c) the STL decomposition shown in Figure 4 with ETS applied to the seasonally adjusted data, and seasonal naive methods applied to both seasonal components.

The following code uses a test set of the last 4 weeks to compare the three models, along with two benchmark methods.

```
fit <- otexts %>%
  head(-28) %>%
  model(
    ets = ETS(Pageviews),
    dr = ARIMA(log(Pageviews) ~ fourier(period = "year", K = 4) +
              PDQ(period = "week")),
    stl = decomposition_model(
      STL(log(Pageviews) ~ trend(window = 99) +
        season(period = "week", window = 99) +
        season(period = "year", window = 9),
        robust = TRUE),
      ETS(season_adjust)
    ),
    naive = NAIVE(Pageviews),
    snaive = SNAIVE(Pageviews ~ lag("week"))
  )
fc <- fit %>%
  forecast(h = 28)
fc %>%
  accuracy(otexts, measures=list(RMSE=RMSE, MAPE=MAPE)) %>%
  arrange(RMSE)
```

```
## # A tibble: 5 x 4
##   .model .type RMSE MAPE
##   <chr>  <chr> <dbl> <dbl>
## 1 dr    Test   3.19  7.75
## 2 ets   Test   3.67  9.87
## 3 stl   Test   3.96  9.72
## 4 snaive Test   4.50 11.1
## 5 naive Test  12.8 31.4
```

What do you conclude from the above output about the five models? Explain the two accuracy measures used. Why is the naive method so bad?

4 marks

2. An alternative approach to comparing the forecast accuracy of models would be to use time series cross-validation. Explain the concept of time series cross-validation. You may use an annotated diagram.

6 marks

3. **ETC3550 students only:** You decide the naive model is good enough even though it is not as accurate as the first three models. Let the observations be y_1, \dots, y_T and the residual variance be denoted by σ^2 . Write down the forecast distribution for an h -step forecast. What assumptions have you made?

5 marks

4. **ETC5550 students only:** Someone proposes a fancy new forecasting method that uses some predictor variables such as the number of students in each university that is using an OTexts book as a recommended text, and the relative wealth of the countries they live in. This new method reduces the cross-validated one-step RMSE by 2%, but takes about a day to estimate the forecasts. Would you recommend using the new method? Explain your reasons.

5 marks

5. OTexts also needs forecasts of the maximum monthly traffic that could arise, in order to make sure their internet server will cope with the extreme demand. They want to choose an internet plan that allows for a maximum of P pageviews per month, and they are happy to allow a 1% chance of being above this level. Explain how you would choose P based on forecasts over the next 12 months.

5 marks

Total: 20 marks

— END OF SECTION E —