

$$\begin{pmatrix} 1 & \theta & \theta & \theta \\ \theta & -\sin[\theta] \cos[\phi] & \sin[\theta] \sin[\phi] & \cos[\theta] \\ \theta & \cos[\theta] \cos[\phi] & -\sin[\phi] \cos[\theta] & \sin[\theta] \\ \theta & \sin[\phi] & \cos[\phi] & \theta \end{pmatrix} \cdot \begin{pmatrix} \gamma & \gamma\beta & 0 & 0 \\ \gamma\beta & \gamma & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}.$$

$$\begin{pmatrix} 1 & \theta & \theta & \theta \\ \theta & \sin[\theta] \cos[\phi] & \sin[\theta] \sin[\phi] & \cos[\theta] \\ \theta & \cos[\theta] \cos[\phi] & \sin[\phi] \cos[\theta] & -\sin[\theta] \\ \theta & -\sin[\phi] & \cos[\phi] & \theta \end{pmatrix} // \text{MatrixForm} // \text{FullSimplify}$$

$$\begin{pmatrix} \gamma & \beta\gamma \cos[\phi] \sin[\theta] & & \\ -\beta\gamma \cos[\phi] \sin[\theta] & -\gamma \cos[\phi]^2 \sin[\theta]^2 + \cos[\theta] (-1 + \cos[\phi] \sin[\theta]) \sin[\phi] & -\gamma \cos[\phi] \sin[\theta] & \\ \beta\gamma \cos[\theta] \cos[\phi] & \gamma \cos[\theta] \cos[\phi]^2 \sin[\theta] - (\cos[\theta]^2 \cos[\phi] + \sin[\theta]) \sin[\phi] & -\cos[\theta]^2 \sin[\theta] & \\ \beta\gamma \sin[\phi] & \cos[\phi] (\cos[\theta] \cos[\phi] + \gamma \sin[\theta] \sin[\phi]) & & \sin[\phi] \end{pmatrix}$$