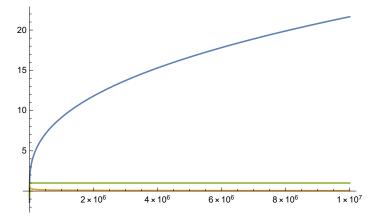
Plot
$$\left[\left\{ \frac{\sqrt{x}}{\log[x]} \left(\frac{1}{\left(1 + \frac{\log[x]}{2}\right)} \right), \frac{\log[x]}{\sqrt{x}} \left(1 + \frac{\log[x]}{2}\right), Zeta[x] \right\}, \{x, 0, 10000000\} \right]$$



$$a = \pi$$

$$\frac{\sqrt{a}}{\text{Log[a]}} \left(\frac{1}{\left(1 + \frac{\text{Log[a]}}{2}\right)} \right) // N$$

$$\frac{\text{Log[a]}}{\sqrt{a}} \left(1 + \frac{\text{Log[a]}}{2} \right) // N$$

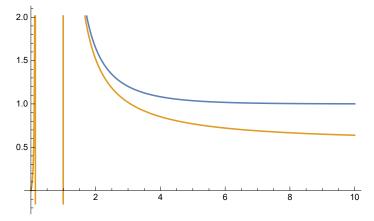
0.984733

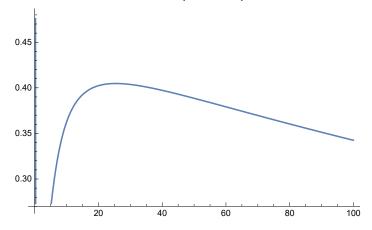
1.0155

Close apprximations? Maybe for real function both = 1 at a = pi?

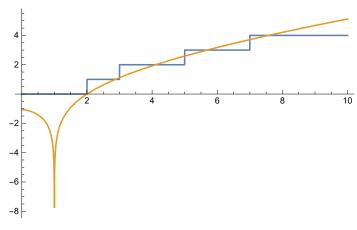
3.17222

Plot[{Zeta[x],
$$\frac{\sqrt{x}}{Log[x]} \left(\frac{1}{\left(1 + \frac{Log[x]}{2}\right)} \right)$$
}, {x, 0, 10}]





Plot[{PrimePi[x], LogIntegral[x] - LogIntegral[2]}, {x, 0, 10}]



EulerGamma // N

0.577216

LogIntegral[2] // N

1.04516