

Integrate[x^2 Cos [n x], x]

$$\frac{2 x \cos [n x]}{n^2} + \frac{(-2 + n^2 x^2) \sin [n x]}{n^3}$$

Zeta[2]

$$\frac{\pi^2}{6}$$

FourierSeries[x^2, x, 3] // FullSimplify

$$\frac{\pi^2}{3} - 4 \cos [x] + \cos [2 x] - \frac{4}{9} \cos [3 x]$$

Sum[(-1)^n / (4 n^2 - 1), {n, 1, ∞}]

$$\frac{2 - \pi}{4}$$

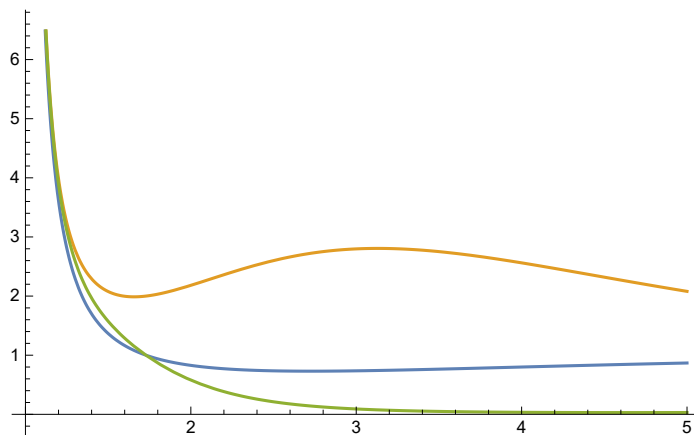
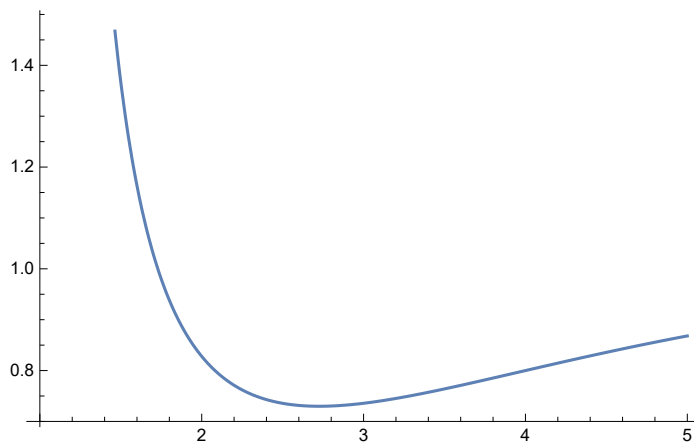
Zeta[2] / 4 // N

0.411234

Zeta[5, Zeta[5]] // N

0.868065

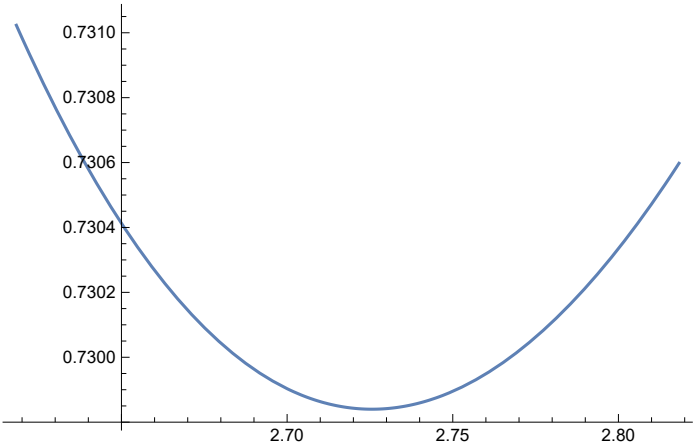
```
Plot[{Zeta[x, Zeta[x]]}, {x, 1, 5}]
Plot[{Zeta[x, Zeta[x]], Zeta[x, Zeta[x, Zeta[x]]},
      Zeta[x, Zeta[x, Zeta[x, Zeta[x]]]}], {x, 1, 5}]
```



```
Zeta[E, Zeta[E]] // N
Zeta[E + 0.01, Zeta[E + 0.01]] // N
Zeta[E - 0.01, Zeta[E - 0.01]] // N
0.729845
0.729841
0.729869
```

Maybe the minimum of an infiniteyl recursive zeta is E and it has a local max at π ????

```
Plot[{Zeta[x, Zeta[x]]}, {x, E - .1, E + .1}]
E // N
```



2.71828