# **Density Matrix Calculation**

### Misc.

```
 \begin{tabular}{ll} $n = Length[Union[SET]] (* i.e. $n = number of unique elements in the set *) \\ $H[\alpha_-$, SET_-] := $\frac{1}{1-\alpha} Log[Sum[(prob_i)^\alpha, \{i,1,n\}]] $$ \\ $Count[\{a,b,a,d,b,c,b\},b] $$ \\ $Length[\{a,b,a,d,b,c,b\}] (* Prob of getting b at random *) $$ \\ $Length[\{a,b,a,d,b,c,b\}] (* Prob of getting b at random *) $$ \\ $Length[Union[\{a,b,a,d,b,c,b\}]] (* i.e. = number of unique elements in the set *) $$ \\ $3$ \\ $7$ \\ $4$ \\ \end{tabular}
```

### PrimePi Renyi Entropy Calc

### PCV1 Renyi Entropy Calc

### **General Definitional Terms**

```
(* M=PCV1<sub>1</sub>; *)
(* M={Join[PCV1<sub>1</sub>[[1]],PCV1<sub>2</sub>[[1]],PCV1<sub>3</sub>[[1]],PCV1<sub>4</sub>[[1]]]}; *)
(* M={Table[PCV1<sub>1</sub>[[1,i]],{i,1,64}]}; *)
lengthvec[M_] := Length[M[[1, All]]]
For[npow = 1, npow < 1000, npow++, If[lengthvec[M] < (2^(npow)), Break[]];
    FilledSize = 2^(npow + 1)];
Filler[M_] := Table[4, {i, 1, FilledSize - lengthvec[M]}]
FilledVec[M_] := Join[Flatten[M], Filler[M]]
lengthvec[M_] := Table[4, {i, 1, FilledSize - lengthvec[M]}]
Filler[M_] := Table[4, {i, 1, FilledSize - lengthvec[M]}]
FilledVec[M_] := Join[Flatten[M], Filler[M]]</pre>
```

```
For [npow = 1, npow < 1000, npow++, If [lengthvec[M] <math>\leq (2^npow), Break[]]];
(* gives npow such that 2^npow > lengthvec[M] > 2^n(npow -1) *)
FilledSize = 2^npow;
```

### PCV Type 1 samples

Renyi Entropies of PCV1 data sets

Density matric calc Using 2x2^(n/2) defn of W0 (not valid)

**Density Matrix Calculation** 

Wrong  $\rho$ 's (as inner and outer products of W, Transpose[W])

Defn of W (RUN THIS before doing the below)

Misc. Code

## Pre/detailed

### **Final**

Just pick a W and Run the blue subsection

### Constructing W's

```
To get a letter sequence go to https://www.ncbi.nlm.nih.gov/nuccore/
pick a gene from GenBank
go to FASTA
Copy + paste letter seq into data subsubsection
```

```
StringReplace[ToString[{StringReplace["ACGTAGTCAATT",
          \{ \text{"A"} \rightarrow \text{"0,", "C"} \rightarrow \text{"1,", "G"} \rightarrow \text{"2,", "T"} \rightarrow \text{"3,"} ] \} ] \text{, ",} \} \text{"} \rightarrow \text{"} \} \text{"} ] 
\{0,1,2,3,0,2,3,1,0,0,3,3\}
```

```
ToString["ACGTAGTCAATT"]
ToString[ACGTAGTCAATT]
ACGTAGTCAATT // ToString
 StringQ[ACGTAGTCAATT // ToString]
StringQ[ACGTAGTCAATT]
ACGTAGTCAATT
ACGTAGTCAATT
ACGTAGTCAATT
True
 False
  sample = "ACGTAGTCAATT" // ToString;
 StringReplace[ToString[{StringReplace[ToString[sample],
                                       \{\text{"A"} \rightarrow \text{"0,", "C"} \rightarrow \text{"1,", "G"} \rightarrow \text{"2,", "T"} \rightarrow \text{"3,"}]\}], \text{",}\}\text{"} \rightarrow \text{"}\}\text{"}]
   \{0,1,2,3,0,2,3,1,0,0,3,3\}
  lettersample = {ACGTAGTCAATT} // ToString;
  LetterDNAtoNum[Sample_] := ToExpression[StringReplace[ToString[
                                       \{StringReplace[StringReplace[ToString[\{Sample\}], \{"," \rightarrow "", " " \rightarrow "", "\{" \rightarrow "", " \} \}, ["," \rightarrow "", "], ["," \rightarrow 
                                                                             "}"→"","("→"",")"→"","["→"","]"→"",";"→"",":"→"","_"→"",
                                                                           "+" \rightarrow "", "&" \rightarrow "", "/" \rightarrow "", "." \rightarrow "", "RowBox" \rightarrow "", "Null" \rightarrow ""}],
                                                           \{ "0" \rightarrow "0,", "1" \rightarrow "1,", "2" \rightarrow "2,", "3" \rightarrow "3,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "
                                                                   "G" \rightarrow "2,", "T" \rightarrow "3,", "a" \rightarrow "0,", "c" \rightarrow "1,", "g" \rightarrow "2,", "t" \rightarrow "3,"\}] \}
                               ",}" →
                                      "}"]]
 LetterDNAtoNum[lettersample]
   \{\{0, 1, 2, 3, 0, 2, 3, 1, 0, 0, 3, 3\}\}
 numgenesample = LetterDNAtoNum[lettersample];
 Flatten[numgenesample][[3]]
  lettersample = {ACGTAGTCAATT} // ToString;
 LetterDNAtoNum[Sample_] := ToExpression[StringReplace[ToString[
                                       "}" \rightarrow "", "(" \rightarrow "", ")" \rightarrow "", "[" \rightarrow "", "]" \rightarrow "", ";" \rightarrow "", ":" \rightarrow "", "_" \rightarrow "", "+" \rightarrow "", "&" \rightarrow "", "RowBox" \rightarrow "", "Null" \rightarrow ""}],
                                                           \{"0" \rightarrow "0,", "1" \rightarrow "1,", "2" \rightarrow "2,", "3" \rightarrow "3,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "A"
                                                                    "G" \rightarrow "2,", "T" \rightarrow "3,", "a" \rightarrow "0,", "c" \rightarrow "1,", "g" \rightarrow "2,", "t" \rightarrow "3,"}]}
                             ], ",}" → "}"]]
  numgenesample = LetterDNAtoNum[lettersample];
 Flatten[numgenesample]
  \{0, 1, 2, 3, 0, 2, 3, 1, 0, 0, 3, 3\}
```

wolf genesample.txt

```
basepairs = ToString[Input["Paste the base pair sequence (ex: AAGCTATGG) here"]];
      Wgenesample = StringJoin[ToString[Input["What Gene is this?"]], " gene"]
       (*Lets us know which gene we're dealing with,
      used in pdf coding later, so be sure to name it *)
 BRCA2 mRNA Wolf gene
lettersample = {ACGTAGTCAATT} // ToString;
LetterDNAtoNum[Sample_] := ToExpression[StringReplace[ToString[
                        \{StringReplace[StringReplace[ToString[\{Sample\}], \{"," \rightarrow "", " " \rightarrow "", " \{" \rightarrow "", " \} \})\} \}
                                               " \}" \to "", " (" \to "", ")" \to "", " [" \to "", "]" \to "", ";" \to "", ":" \to "", "\_" \to "",
                                               "+" → "", "&" → "", "/" → "", "." → "", "RowBox" → "", "Null" → ""}],
                                    \{"0" \rightarrow "0,", "1" \rightarrow "1,", "2" \rightarrow "2,", "3" \rightarrow "3,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "A"
                                          "G" \rightarrow "2,", "T" \rightarrow "3,", "a" \rightarrow "0,", "c" \rightarrow "1,", "g" \rightarrow "2,", "t" \rightarrow "3,"}]}
                  ], ",}" → "}"]]
numgenesample = LetterDNAtoNum[lettersample];
{\tt Export[StringReplace["GENE\_genesample.txt", "GENE\_gene" \rightarrow {\tt Wgenesample]},}
     Flatten[numgenesample]]
```

#### Test of method of Construction of W

```
H1Avec =
```

```
1, 3, 3, 1, 2, 3, 1, 0, 2, 2, 3, 3, 3, 0, 3, 0, 1, 1, 0, 1, 3, 3, 3, 0, 3, 3, 3, 2, 2, 3, 2, 3,
  2, 1, 3, 2, 3, 2, 3, 3, 0, 2, 3, 1, 0, 1, 1, 0, 3, 2, 3, 1, 3, 2, 0, 0, 0, 1, 0, 2, 3, 2, 1, 1,
  3, 1, 1, 1, 2, 1, 1, 1, 1, 1, 2, 1, 1, 2, 1, 3, 3, 1, 3, 2, 1, 3, 2, 1, 3, 1, 1, 3, 2, 0,
  2, 0, 0, 0, 1, 1, 3, 3, 3, 0, 2, 1, 3, 2, 2, 1, 0, 0, 2, 0, 0, 2, 2, 1, 0, 0, 0, 2, 0, 0,
  0, 1, 1, 3, 2, 1, 3, 0, 0, 2, 2, 1, 3, 2, 1, 0, 2, 1, 0, 2, 1, 1, 3, 1, 1, 0, 0, 2, 0, 0,
  0, 0, 0, 0, 1, 1, 1, 2, 1, 3, 2, 2, 1, 1, 1, 3, 3, 1, 1, 2, 3, 2, 3, 1, 0, 2, 0, 2, 1, 3,
  2, 0, 3, 1, 2, 3, 2, 1, 0, 2, 2, 1, 3, 2, 1, 3, 3, 1, 1, 3, 1, 1, 3, 1, 3, 0, 0, 2, 2, 0,
  2, 1, 2, 3, 2, 2, 3, 2, 2, 3, 2, 3, 2, 3, 1, 2, 3, 3, 2, 2, 1, 0, 2, 1, 3, 1, 3, 3, 0, 0,
  0, 0, 0, 2, 2, 1, 2, 1, 3, 2, 2, 1, 2, 2, 1, 1, 2, 1, 0, 2, 2, 1, 3, 0, 1, 2, 0, 1, 2, 3,
  2, 2, 0, 2, 0, 0, 2, 0, 0, 1, 0, 0, 1, 0, 2, 1, 1, 2, 1, 0, 3, 3, 0, 0, 2, 1, 3, 2, 2, 2,
  1, 0, 3, 3, 0, 0, 2, 0, 2, 1, 1, 3, 2, 2, 3, 0, 0, 2, 1, 0, 0, 2, 2, 2, 0, 0, 1, 2, 3, 3,
  2, 2, 3, 2, 1, 0, 2, 0, 1, 0, 0, 0, 2, 2, 2, 3, 0, 1, 1, 2, 2, 0, 2, 1, 1, 3, 1, 2, 2, 2,
  3, 3, 1, 1, 3, 3, 1, 0, 0, 2, 1, 3, 1, 0, 0, 1, 0, 0, 2, 0, 0, 2, 2, 1, 2, 3, 1, 1, 3, 1,
  1, 2, 3, 2, 2, 0, 0, 0, 1, 1, 0, 0, 2, 1, 1, 1, 2, 2, 1, 2, 1, 1, 3, 1, 0, 0, 0, 2, 2, 3,
  2, 2, 1, 3, 0, 1, 0, 0, 0, 0, 0, 1, 3, 0, 0, 2, 2, 1, 0, 0, 1, 2, 2, 2, 3, 2, 1, 0, 3, 1,
  3, 0, 0, 0, 0, 0, 2, 1, 3, 1, 0, 0, 0, 0, 0, 2, 2, 1, 1, 0, 1, 2, 2, 2, 2, 2, 1, 3, 0, 2,
  1, 0, 0, 0, 0, 0, 2, 0, 2, 1, 2, 3, 1, 0, 0, 2, 0, 1, 3, 1, 1, 2, 0, 0, 0, 0, 0, 2, 2, 1,
  3, 0, 0, 0, 0, 0, 2, 1, 1, 3, 2, 1, 2, 2, 1, 0, 0, 1, 0, 0, 2, 2, 0, 0, 0, 3, 1, 1, 3, 1,
  1, 0, 0, 2, 0, 0, 3, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 3, 2, 3, 0, 0, 0,
  2, 1, 1, 1, 0, 0, 2, 0, 0, 0, 2, 3, 0, 2, 1, 3, 0, 0, 0, 0, 2, 1, 1, 1, 3, 2, 1, 3, 0,
  0, 0, 2, 1, 3, 0, 0, 2, 2, 1, 3, 2, 3, 0, 0, 0, 0, 1, 1, 1, 0, 0, 2, 2, 1, 2, 2, 1, 1,
  0, 0, 2, 2, 1, 3, 0, 2, 2, 2, 3, 2, 0, 1, 2, 0, 0, 2, 1, 1, 0, 0, 0, 2, 0, 1, 3, 2, 1,
  1, 0, 0, 0, 1, 1, 1, 0, 0, 2, 0, 0, 0, 2, 1, 2, 2, 1, 0, 1, 1, 1, 0, 0, 2, 0, 0, 0, 0,
  0, 2, 3, 0, 0, 0, 3, 3, 1, 0, 2, 3, 3, 0, 2, 0, 0, 2, 3, 3, 3, 1, 3, 3, 1, 3, 0, 2, 3,
  0, 0, 1, 1, 1, 0, 0, 1, 2, 2, 1, 3, 1, 3, 3, 3, 3, 0, 0, 2, 0, 2, 1, 1, 0, 1, 1, 3, 0}};
```

H1AW =

```
{{3, 0, 2, 2, 1, 3, 2, 1, 2, 3, 3, 2, 2, 2, 2, 1, 1, 3, 3, 3, 3, 3, 3, 3, 1, 2, 1, 0, 3, 1, 1, 3},
   {2, 1, 3, 3, 1, 2, 3, 1, 0, 2, 2, 3, 3, 3, 0, 3, 0, 1, 1, 0, 1, 3, 3, 3, 0, 3, 3, 3, 2, 2, 3, 2},
   {3, 2, 1, 3, 2, 3, 2, 3, 3, 0, 2, 3, 1, 0, 1, 1, 0, 3, 2, 3, 1, 3, 2, 0, 0, 0, 1, 0, 2, 3, 2, 1},
   {1, 3, 1, 1, 1, 2, 1, 1, 1, 1, 1, 2, 1, 1, 2, 1, 3, 3, 1, 3, 2, 1, 3, 2, 1, 3, 1, 1, 3, 2, 0, 2},
   {0, 0, 0, 1, 1, 3, 3, 3, 0, 2, 1, 3, 2, 2, 1, 0, 0, 2, 0, 0, 2, 2, 1, 0, 0, 0, 2, 0, 0, 0, 1, 1},
   \{3, 2, 1, 3, 0, 0, 2, 2, 1, 3, 2, 1, 0, 2, 1, 0, 2, 1, 1, 3, 1, 1, 0, 0, 2, 0, 0, 0, 0, 0, 0, 1\},
   {1, 1, 2, 1, 3, 2, 2, 1, 1, 1, 3, 3, 1, 1, 2, 3, 2, 3, 1, 0, 2, 0, 2, 1, 3, 2, 0, 3, 1, 2, 3, 2},
   {1, 0, 2, 2, 1, 3, 2, 1, 3, 3, 1, 1, 3, 1, 1, 3, 1, 3, 0, 0, 2, 2, 0, 2, 1, 2, 3, 2, 2, 3, 2, 2},
   {3, 2, 3, 2, 3, 1, 2, 3, 3, 2, 2, 1, 0, 2, 1, 3, 1, 3, 3, 0, 0, 0, 0, 0, 2, 2, 1, 2, 1, 3, 2, 2},
   {1, 2, 2, 1, 1, 2, 1, 0, 2, 2, 1, 3, 0, 1, 2, 0, 1, 2, 3, 2, 2, 0, 2, 0, 0, 2, 0, 0, 1, 0, 0, 1},
   \{0, 2, 1, 1, 2, 1, 0, 3, 3, 0, 0, 2, 1, 3, 2, 2, 2, 1, 0, 3, 3, 0, 0, 2, 0, 2, 1, 1, 3, 2, 2, 3\},
   \{0, 0, 2, 1, 0, 0, 2, 2, 2, 0, 0, 1, 2, 3, 3, 2, 2, 3, 2, 1, 0, 2, 0, 1, 0, 0, 0, 2, 2, 2, 3, 0\},\
   {1, 1, 2, 2, 0, 2, 1, 1, 3, 1, 2, 2, 2, 3, 3, 1, 1, 3, 3, 1, 0, 0, 2, 1, 3, 1, 0, 0, 1, 0, 0, 2},
   {0, 0, 2, 2, 1, 2, 3, 1, 1, 3, 1, 1, 2, 3, 2, 2, 0, 0, 0, 1, 1, 0, 0, 2, 1, 1, 1, 2, 2, 1, 2, 1},
   \{1, 3, 1, 0, 0, 0, 2, 2, 3, 2, 2, 1, 3, 0, 1, 0, 0, 0, 0, 1, 3, 0, 0, 2, 2, 1, 0, 0, 1, 2, 2\},\
   {2, 3, 2, 1, 0, 3, 1, 3, 0, 0, 0, 0, 0, 2, 1, 3, 1, 0, 0, 0, 0, 0, 2, 2, 1, 1, 0, 1, 2, 2, 2, 2},
   {2, 2, 1, 3, 0, 0, 0, 0, 0, 2, 1, 1, 3, 2, 1, 2, 2, 1, 0, 0, 1, 0, 0, 2, 2, 0, 0, 0, 3, 1, 1, 3},
   \{1, 1, 0, 0, 2, 0, 0, 3, 1, 1, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 3, 2, 3, 0, 0, 0, 2\},
   \{1, 1, 1, 0, 0, 2, 0, 0, 0, 2, 3, 0, 2, 1, 3, 0, 0, 0, 0, 2, 1, 1, 1, 3, 2, 1, 3, 0, 0, 0, 2, 1\},
   \{3, 0, 0, 2, 2, 1, 3, 2, 3, 0, 0, 0, 0, 1, 1, 1, 0, 0, 2, 2, 1, 2, 2, 1, 1, 0, 0, 2, 2, 1, 3, 0\},\
   \{2, 2, 2, 3, 2, 0, 1, 2, 0, 0, 2, 1, 1, 0, 0, 0, 2, 0, 1, 3, 2, 1, 1, 0, 0, 0, 1, 1, 1, 0, 0, 2\},
   \{0, 0, 0, 2, 1, 2, 2, 1, 0, 1, 1, 1, 0, 0, 2, 0, 0, 0, 0, 2, 3, 0, 0, 0, 3, 3, 1, 0, 2, 3, 3\},\
   \{0, 2, 0, 0, 2, 3, 3, 3, 1, 3, 3, 1, 3, 0, 2, 3, 0, 0, 1, 1, 1, 0, 0, 1, 2, 2, 1, 3, 1, 3, 3, 3\},\
   numgenesample = H1Avec;
M = numgenesample;
lengthvec[M ] := Length[M[[1, All]]]
For [npow = 1, npow < 1000, npow++, If [lengthvec[M] < (2^ (npow)), Break[]];
  FilledSize = 2^ (npow + 1) ];
Filler[M ] := Table[4, {i, 1, FilledSize - lengthvec[M]}]
FilledVec[M_] := Join[Flatten[M], Filler[M]]
lengthvec[M ] := Length[M[[1, All]]]
Filler[M_] := Table[4, {i, 1, FilledSize - lengthvec[M]}]
FilledVec[M_] := Join[Flatten[M], Filler[M]]
For [npow = 1, npow < 1000, npow++, If [lengthvec[M] <math>\leq (2^npow), Break[]]];
(* gives npow such that 2^npow > lengthvec[M] > 2^n(npow -1) *)
FilledSize = 2^npow;
FilledM = FilledVec[M];
```

```
npow
  Length[FilledM] (*Should be an (even) power of 2*)
  numrowsW = \sqrt{Length[FilledM]}
  10
  1024
  32
   (*Table[FilledM[[i]],{i,1,numrowsW}]
   Table[FilledM[[i]],{i,33,2*(numrowsW)}]
   Table [FilledM[[i]], \{i, (2*(numrowsW))+1,3*(numrowsW)\}]*)
  testWW = Table[Table[FilledM[[i]],
       \{i, (((j-1)*(numrowsW))+1), (j*(numrowsW))\}\}, \{j, 1, numrowsW\}\};
   Print["so this construction is valid if and only if the following:
    H1AW - testWW // Union // Flatten // Union ,
         is exactly {0}, if not something is wrong"]
   so this construction is valid if and only if the following:
       is exactly {0}, if not something is wrong
W for Wolf BRCA2 mRNA
```

#### Data

```
Source: GenBank: AB043895.5
(*lettersample={}//ToString;*)
lettersample = {AAAGAAGGTCGGCGGAGGCGGAGCCGGGGCTTGGGGGCTCTGGAAGTCGTCCCAGCCGCGGG x
\mathsf{TCGCCGAGGAAAGGAGCCTGCGGGTCAGCTTTCTGGCCGAAGTGCCGGCGCGAATTTGTTAGCCGTCTCC} \times \mathsf{TCGCCGAGGAAGGGAGCCGGAGTTTGTTAGCCGTCTCC}
\mathsf{GGCCAAAAAGAGCGGCACCTCGGAAGGCGAGTTATTTACCAAGCACTGGAGTAATATTGTAGATAAAAAT 	imes
{\sf GCCTGTTGGATGCAAAGAGGGCCAACATTTTTTGAAATTTTTAAGACGCGGTGCAATCAAGCAGATTTA}
\mathsf{GGACCAATAAGCCTTAATTGGTTTGAAGAACTTTCTTTAGAAGCTCCACCCTATAATTCTGAACCCACAG 	imes
AAGAATCTGGTTATAAAATCAGCTATGAACCAAACCTATTTAAAACACCACAAAGGAAACCTTATAATCA 	imes
{\sf GTTGGCTTCAACTCCAATAGTATTCAGAGAGCCAATATACCAACAATCTCCTTTAAAAGAATTAGATAAA}
\mathsf{TACAGATTAGATTCAGGAAAGGATATTACCGATAGTAAACATAAAAGTTGTTGCACAATGAAGTCTAAAA 	imes
\mathsf{TGGATCGAGCAAATGATGTTACCAGCCCACCTCTAAATTCTTATCTTAGTGAAAGTCCTGTTCTACGATG 	imes
\mathsf{TACACATGTAACACCACAGAGAGAAAAGTCGGTGGTATGTGGAAGCTTATTTCATACACCGAAGCTTATG 	imes
AAGGGTCAGACACCAAAACGCATTTCTGAAAGTCTAGGAGCTGAGGTGGATTCTGATATGTCTTGGTCAA 	imes
\mathsf{TGTATTTCCTAATGACACTACTGCTATTTTTAAAAGCTGTTTTTCTAACCATGATGAAAGTCTGAAGAAA 	imes
AATGATCGGTTTATCCCTTGTGGTCCAGGCAAAGAAAACAAAAATCAAAGGGAAGCTAAAAGTCAAAGTT <math>	imes
\mathsf{TGGGGAATTCATTTGGTAAAGTAAATAGCACCAAAGACCATTTTGTAAAGTCTACACCAAATGTCCTAGA 	imes
\mathsf{GGATGAAGTACATGAAAAAGTTCTAGATGTTTCTGAAGAAGAAGATAGTTTTTCATTATGTGTTCCTAAA 	imes
\mathsf{TATAAAACAAGAAATCTACAAAAAAATAAAAACTAGCAAAACTAGGAAAAATATTTTTAATGAGACAAAAA 	imes
AAATGACAGTCATCCATTAGATTGGAATGTAACACATGAGAAGCCCTTTGGGAATGGAACTGACAAAATC ×
\mathsf{TCCAAGGAAATTGTACTGTCTTCAGCCTCTGGATGTTCTGACCTAACCCTCTCAAGTCTAAATGGAGCTC}
```

 ${\sf AGATAAAGAATGCACCAACTTCATTACTTTGGAAAATTCTTGGCCACAGATTTCAAATGTACCAAAGTAT}$  $\mathsf{TCAGAGAAGACGTTAAATGAGGAAATAGTAGATAAATAAGATAAACGAAGGGCAGTGTCTTGAATCTCATG imes$  $AAGATTCCGTTGTTTCGGTAAAGCAAGCAATATATGAAACTACTTTAATAGCTTCTCCACTTCAGGGTAT \times$  $\mathsf{CAGAAAGTCTATATTCAGGATAAGAGAATCACCTGAAGGGATGTCCAATGCTAATCTCAAATAATATG imes$ ACTAATCCAAACTTTAAAGAACCTGAAGCCTCTGAAAGTGGATTGGAAAAACATACTATTTGCTCTCAGA imesAAGAGGATTCTTTATGTACAAGTTCAATTGATGATGGAAGCTGGCCAGCAACTATCAAACATACTTCTGT imesGATGAAACATCTAATCAAGGCCTGAAAACACAGAAAGACCAAGAGTCAAGACTAATTAACCTTTCGACCC ×  $AATTTGAAGCAAATGCTTTTGAAGGACCCCTGACATTTACAAATGCTGATTCAGGTTTATTGCATTCTTC \times$  $\mathsf{TTCCATCAAAAAAAACTGTTTACAGAATGACTCAGAAAAACCAGCTTTGTCTTTAACCAGCTCTTTTGGG imes$  $ACAATTCTGAGAAAAGTTTCCAGTAATGGAGCCAGTTCTCCTAATAATAAAATAATATCTCAGGATCCTG \times$ CCTAGTTGTGATGTCTAGAGGAAAAGAATCATAAAATATCAGAGAAACTAAAATGTAAGAATCATGAA imes $\mathsf{CTAAAAATGCTAAACTGTTGTCAACTGAAAAACATATAACAGTAGCATCATCTTCAGTAAAGGTTCAGTT imes$ CAACCAAAATGCAAATCTCACCACAATCCAAAAAGACCAAAAAGAAACTACTTTAATTTCAAAAATAACT <math> imes ${f GTTAATCCAAACTCTGAAGAACTTTTCCCAGATGATGAAAATAATTTTGTCTTAAAGATAACTAATGAAA imes$ AAAGATTGTTATTCATCAAGCATAGATGATCTTACAGAAAGGAACAGAAGTACCATAAAGCAACAACTAAimesAAATGACTCTAGATCAAGATTCAAAATCAGACATTACCTCAGATATAGTTAGGAAAATCAAATGGAAACAG <math> imes $\mathsf{TGATTATATGGATAATTGGGCAAGACTGTCTGATCCAATTTCAAATCACAGTTTTGAAAATGGCTTCAAA imes$ ACAGCTTCTAATAAAGAGATAAAACTCTCTGAAAACAACATTAGGAAAAGTAAAATGCTTTTCAAAGATA <math> imes $\mathsf{TTGAGGAACATTATCCTACTAACTTAGCATGTCTTGAAATTGTAAATACTTCATCATTAGAAAGTCAAAA imes$  $CAAATCGTAATTTAACTCCTAGTCAAAAGGCAGAAATTACAGAACTTTCTACTATTTTGGAAGAATCAGG \times$ AAGCCAGTTTGAATTTACACAGTTTAGAAAACCAAGCCACATAATACAGAAAAATCCATTTGAAATGCCT imes ${\sf GAAAACCAGCTGACTATCTTGAATAGCACTTCTAAGGAATGGAAAGATGATGATCTTCATCTCACAACTA}$  ${\tt ATGCTCCATCTATCAGTCAGGTAGATAGCAAGAAATCTGAAGGTATAATTGGAGGTAAGCAGAAGTTTGC} \times \\$  $\mathsf{TTGCTTGTCAAGAACCAGCTGTAACAGAAGTGCTTCTGGCTATTCAACAGATAAAAATGAAGTGGAGTTT imes$ AGAGGCTTTTATTCTGCTCGTGGCACAAAACTGAATGTTGGTAGTGAAGCATTGCAAAAAGCTAAGAAAC ×  $\mathsf{TGTTCAGTGACCTTGAGAATATCAATGAGGAAACTTCTGTAGAAGTAGAAGTTTCTCCTCAAGCAA imes$  ${f GTTACAGGAGAAATACAGAAAATGAAGGTAACCAATGTACTGACGCTGGTAGAAATACTTGTAACTCAGA} imes$ ATTGATCAGCACAACATAGATCTGAAATTATTTAGCCAGTTTATGAAGGAGGGGAACACTCAAATTAAAGimesAAGGTTTGTCAGATTTAACCTGTTTGGAAGTTATGAAAGCTGAAGAAACATCTCATGTTACTATGTCAAA imesAATGGACAGAAGAAGAATTAAATAACTTTTCAGATTCCTTGAATTCTGAATTACTTCCTGGCATAGATAT imesAGTGACCTAATTGGTACTGAAAATATATTACTGATCCTGCAGCAAAGACCAGAAAGTAAAATAAAAAAGA <math> imes $\mathsf{TCAAAGAATCTGCTGTGTTGGGTTTTCATACAGCTAGTGGGAAAAAAATAGAAATTACAAAGGAATCTTT imes$  $\mathsf{GGACAAAGTAAAAAATCTTTTTGAAGAAAAAGAGCAAGATAATAGTGAAATCACTAATTTTAGCCATCGA imes$  $\mathsf{GGGGCAAAGATGTCCAAGGACAGAAGAATGTAAAGATGGGCGTGAATTAGCTTGTGGGACAACTGAAA imes$   $\mathsf{TAACAACTACCCCAGAGTATGAAGAAACTCACAGTTCTCTAGAGAAGAAAAAACTTGTTTCTAATGAGAT imes$  $CAAATCAATCCACTTATTCAGCCATTGAAAACTCACCTTTAACATTTTACACAGGACACGGAAGAAAAAT \times$  ${\sf GAAAGAATAAATGCTGCCAAGGTTAACTGCTTAAAAGAATATCCTGATGATTACGTAGAAAATCCTTCAT}$  $\mathsf{TTATTTAAGTAATAGTACCATGTCTAACAGCTATTCATACCATCCTGGCTTTTGTCATTCTAGTGAAGTG imes$  $\mathsf{TATAATAAATCAGAATATCTTTCAAGAAGTAAAATTGATAATTCTGGTATTGAACCAGTAATAAAGAATA imes$ AAGTGTAAATGAAGATATTTGTGTTGAGAAACTTGCGACTAACTCTTCATGCAAAAAATAAAAATACAGCC imes ${ t ATTAAAGTGGCCATATCTGACTCAAATAATTTTAATACAATTCAAAAGTTGAATTCTGATTCAAATAATT imes$ AATGTTCACCTTCACATAAGGTTTTTGCTGACATTCAAAGTGAACAAACTTCACAACTTAACCAAAGTAT imes ${ t GTCTGGATTGGAGAAGTTTCTGAAACACCACCTTGTCAGATTAATTCAAAAACTTCTGATAGATGTGAA}$ CTTCCTAGGGGGAAGCTTCCCAAGTCAGTCTCTTACACAAATGCATGTGGGATTTTTAGCACAGCAAGTG ×  $\mathsf{GAAAATCTGTACAAGTATCAGATGCTGCAATACAAAAGGCAAGAGAGGTGTTTTCTAAGCTAGAAGATAG imes$  $\mathsf{TGCCAAGCAACTCTTTCCTGAAGTATCACTTAAAGATAATGAAGAACATTCAGAAAAGTTCACAAATGAA imes$ GAAAATACTGTGATATACCCCCCAAAATTTACTATCATCTGCTTTCTCTGGATTTAGGACAGCAAGTG ×  ${\sf GGAAACAAGTTCCAGTTTCTGAAAGTGCCTTATGCAAAGTTAAGGGAATGTTAGAAGAATTCAATCTGAT}$ CAGAACTGAAAGTTGTCTTCAGCATTCATCTACTTCTAGACAAGATGTATCAAAAATGCCTCCTCCTCT imes $\mathsf{TGTATTGGTAAGAGAACCCCAGAACACTCCAGAAACTCCAAATTGGATAAAGCCTGCAATAAAGAATTTA imes$  ${\sf GATTATCAAGTAACTGTAACAATCAGAGTGGTTCTTCAGAAAATCATCACTCTATTAAAGTTTCTCCATG}$  $\mathsf{TCCCTCTCAATTGAAGCGAGACAAACCACAGTTGCTAGTCGGAAGCAAAGGATCACTTGTTGAGAACATT imes$ CATCCTTTGGGAAAAGAACAAGCTTTACCTAAAAATATAAAAACAGAGATTGGGAAAGCTGAAACTTTTC ×  $AACAGAAACCGTAGAGATTGCCAAAGCTTTTATGGAAGATGGTGAGCTGACAGATTCCGAACTGCTAAGT \times$  ${\sf CATGCCAAACACTTTGTTTTTACATGCCAAAACACTAAGGAAATGGTTTTGTTAAATTCAAGAATTGGAA imes$ AAAGAAGAGGAGATGCACTTGTCTCAGTTGGAGAACCCCCAATTAAAAGAAACTTGTTAAATGAATTCGA imes $CAGGATAATAAAAAATCAAGAAACATCTTTAAAAGCTTCAAAAAGCACTCCAGACGGCATCCTAAAAGAC \times$ AGAAGCTTGTTTATGCATCATATTTCTTTAGAGCCAATTTCCTGTGGACCCTTTCGCACAACTGAGGAAC imesGGCAAGAAATACAGAATCCAAATTTCACTGCACCTGGTCAAGAATTTTTGCCTAAATCTCATTTTTATGA imes $ACACCTGGCTTCAGAAAAATCTTCAAGTAATTTATCAGTTTCACGGCAACCATTTTGTATGGTTCCTGCC \times$  $ACAGGAAATGAAAAAAGGAGACACTTGATTGCTCCAGGCAAACCAGTGAAAGTCTTTGTCCCACCTTTTA \times$ AAACTCCAAAGACATAGATGAACTTGGCTCTGGTGATAGTGAAAAAAATATTAATGACAGTGGAATCCAT imes $\mathsf{CAGCTTAAGAAAAATAACTCCAATCAAGCAGCAACTATAATATTCACAAAGAATGAAAAAGAACCTTTAG imes$ ATTTAATTACAAATCTTCAGAACGCCAGAGATATACAGGATATGCGGATTAAAAAGAAACAAAGGCAGCA imes ${\tt TATTTTCCACAGCCAGGTAGTCTGTATCTTGCAAAAACCTCCACTTTGCCTAGAATCTCTCTGAGAGAA} \times \\$  ${\sf CCTATGGTCTGGAGAAGGAATACAATTGGCTGATGGTGGATGGCTCATACCCTCCAATGATGGAAAGATT}$  $\mathsf{GGAAAAGAAGAATTTTATAGGGCTCTGTGTGACACCCCAGGTGTGGATCCAAATTGTATTTCTAGAGTTT$  $GGGTATATAATCACTATAGATGGATTATATGGAAATTGGCAGCCATGGAATTTGCCTTTCCTAAGGAATT \times$  $\mathsf{TGCTAATAGGTGTCTAAGTCCAGAAAGAGTGCTTCTTCAACTAAAATACAGATATGATGTGGAAATTGAT imes$  ${\sf AAAAGCAGAAGATCAGCTATAAAGAAGATAATGGAAAGGGATGACACAGCTGCAAAAACACTTGTTCTCT}$  $\mathsf{GTATTTCTGAAATCATTTCGTCAAGTGCAGATATATCTGAAACTTCTAGTAGTAAAACTAGTAGTGTGGG} \times$ CTCTTAGCTCTCGTAAAGAACGGGAGATTGACTGTGGGTCAGAAGATCACTATTCATGGAGCAGAACTGG ×

TACTCGTCCTGCTTGCTGGTATACCAAACTTGGATTCTCCTGATCCTAGACCTTTCCCTCTCCCCTTG × AGTGGATGGAGGGACCCCATCTGGATTATGCATATTTCGCAATGAAAGGAGGAAGAAAAGGAAGCAAC imesAAAATATGCAGAAATCCAACAAAAGAAACTAGAAGTTTTATTCAATAAAATTCAAGCAGAATTTGAAAAG <math> imesAAGATGGTGCAGAGCTTTATGAAGCAGTGACAAATGCACCAGACCCAAGTGACCTGGAGGGTTATTTTAG imes $\mathsf{TTAGAATTCAAGAAGGCTATGGAATCTGCTGAGCAAGGAGAACAAATTCTACCAAGGGATGTTACAACTG imes$ ATCACCAGATTTATATTCCCTGTTAATAGAAGGAAAGAGATACAGAATCTATCATCTTGCAGCATCACAA imes $\mathsf{TCTAAAAGTAAATCTGGAAAAGCCAACACACAGCTAACAGCAACAAAGAAAACTCAGTACCAGCAACTAC imes$ CAGCATCAGATGAAATCCTATCCCAAGTTTATCAGCCAAGGGAACCCCTTTACTTCAACAAACTGTTGGA imes $\mathsf{GGTCTTGCTCCTGTGGTCTATTTGTCAGATGAATGCCATAATTTATTGGCAATAAAGTTCTGGACTGATT imes$ ATCAGGAATTCCTACTTTATTTGCTGGAGATTTTTCCAGGTTTTCTGCCAGTCCAAAGGAGGAGCATTTT imes ${\sf CAAGAGACATTCCACAAAATGAAAAAATACTGTTGAGAATATTGGTATGTTTTACAATGATGCAGAAAACA} imes$  $AACTTGTGCATATACTTAATGCAAATGATCCCAAGTTGTCCACCCGACTAAAGACTATGCTTCAGAGCC \times$ ACACAGCTCAAATAGTCCTTGGCATAGGAAATAAATTTCTGATGTCTTCTCCCAATAATGAGATGAAT imes $\mathsf{TATCAGAGTCCTTTATCACTTTGTAAGCCAAAAGAGAAGTCTGTCCCCATACCTGGATCAACCCAAATGA imes$  $\mathsf{GGACTTTTGAGTAGAGTGCCTTTACCTCCATCTGTCAGTCCCATTTGTACATTTGTTTCTCCAGCTGCA imes$  $\mathsf{CTCCACAGATGACTCCACGTAAATTTAATGACCTTTCCCTTTTGGAAAGTGATTCAATAGCAGACGAAGA imes$ GACTCTACCAGGACTGCTCCCACGAGCTCAAAAGATTATCTTGGACTGAAAAGGCATTCTACTGCACCCG imes $\mathsf{GGGTCAGAGGACCCGAGAGCCCCAGGCCTGCACCAGGAAGCGGGAGCCCCGTGTACAGAACACAAGTGA}$  $\mathsf{TCTTATGATTGGATATGATCAAGTATATTTTACAAAGTAAACACACTTTTTCTTTAAATTGTGTCCCTAA imes$  $\mathsf{TTAAATGAAAGTAGGTTTCAAAGTACTGTTATTTTGACTCCTGTAGTTCTTTTTAGGTGACTTGGTTTTG imes$  $\mathsf{TTTTGTTTTTCGGAGGTAACCTACTATGAACCAGTTTTCCTTAATAAACGTGTTGGTTCTCTTATAGTTG imes$ 

#### **Process**

```
SpecialNote = " ";
```

```
Wgenesample = "BRCA2 mRNA Wolf gene"
(*Lets us know which gene we're dealing with,
used in pdf coding later, so be sure to name it *)
```

BRCA2 mRNA Wolf gene

```
LetterDNAtoNum[Sample_] := ToExpression[StringReplace[ToString[
                            {StringReplace[StringReplace[ToString[{Sample}], {"," \rightarrow "", " \rightarrow "", "{" \rightarrow "",
                                                        " \}" \to "", " (" \to "", ")" \to "", " [" \to "", "]" \to "", ";" \to "", ":" \to "", "\_" \to "", "
                                                        "+" \rightarrow "", "&" \rightarrow "", "/" \rightarrow "", "." \rightarrow "", "RowBox" \rightarrow "", "Null" \rightarrow ""}],
                                          \{"0" \rightarrow "0,", "1" \rightarrow "1,", "2" \rightarrow "2,", "3" \rightarrow "3,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "A" \rightarrow "0,", "A" \rightarrow "1,", "A"
                                                 "G" → "2,", "T" → "3,", "a" → "0,", "c" → "1,", "g" → "2,", "t" → "3,"}]}
                     ], ",}" → "}"]]
numgenesample = LetterDNAtoNum[lettersample];
 Export[StringReplace["GENE_genesample.txt", "GENE_gene" → Wgenesample],
      Flatten[numgenesample]]
BRCA2 mRNA Wolf genesample.txt
lengthofgeneitself = Length[Flatten[numgenesample]]
         (*To make sure no base pairs are left out *)
11190
```

#### Construction of W

Can compare to W constructen in Python file **W\_hat\_construction.py** if we want

```
lettersample = {basepairs} // ToString;
LetterDNAtoNum[Sample_] := ToExpression[StringReplace[ToString[
                    "\}" \rightarrow "", "(" \rightarrow "", ")" \rightarrow "", "[" \rightarrow "", "]" \rightarrow "", ";" \rightarrow "", ":" \rightarrow "", "
                                     "+" \rightarrow "", "&" \rightarrow "", "/" \rightarrow "", "." \rightarrow "", "RowBox" \rightarrow "", "Null" \rightarrow "", "
                                  " → "", "
 " → ""}],
                            \{"0" \rightarrow "0,", "1" \rightarrow "1,", "2" \rightarrow "2,", "3" \rightarrow "3,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "A" \rightarrow "0,", "A" \rightarrow "0,", "A" \rightarrow "1,", "A"
                                 "G" \rightarrow "2,", "T" \rightarrow "3,", "a" \rightarrow "0,", "c" \rightarrow "1,", "g" \rightarrow "2,", "t" \rightarrow "3,"}]}
              ], ",}" → "}"]]
numgenesample = LetterDNAtoNum[lettersample];
lengthofgeneitself = Length[Flatten[numgenesample]];
M = numgenesample;
For [npow = 1, npow < 1000, npow++, If [Length[M] < (2^(npow)), Break[]];
         FilledSize = 2^ (npow + 1) ];
Filler[vecvar1_] := Table[4, {i, 1, FilledSize - lengthofgeneitself}]
FilledVec[vecvar2] := Join[Flatten[vecvar2], Filler[vecvar2]]
Filler[vecvar4_] := Table[4, {i, 1, FilledSize - lengthofgeneitself}]
FilledVec[vecvar5] := Join[Flatten[vecvar5], Filler[vecvar5]]
For [npow = 1, npow < 1000, npow++, If [lengthofgeneitself \le (2^npow), Break[]]];
 (* gives npow such that 2^npow > lengthofgeneitself > 2^(npow -1) *)
FilledSize = 2^npow;
FilledM = FilledVec[M];
numrowsW = \sqrt{Length[FilledM]};
```

```
W = Table[Table[FilledM[[i]],
     \{i, (((j-1)*(numrowsW))+1), (j*(numrowsW))\}\}, \{j, 1, numrowsW\}\};
(*numgenesample=LetterDNAtoNum[lettersample];
lengthofgeneitself=Length[Flatten[numgenesample]];
M=numgenesample;
lengthvec[M_]:=Length[M[[1,All]]]
  For[npow=1,npow<1000,npow++,If[lengthvec[M]<(2^(npow)),Break[]];
   FilledSize=2^(npow+1)];
Filler[M_]:=Table[4,{i,1,FilledSize-lengthvec[M]}]
   FilledVec[M ]:=Join[Flatten[M],Filler[M]]
    lengthvec[M_]:=Length[M[[1,All]]]
     Filler[M_]:=Table[4,{i,1,FilledSize-lengthvec[M]}]
      FilledVec[M_]:=Join[Flatten[M],Filler[M]]
      For [npow=1, npow<1000, npow++, If [lengthvec[M] \le (2^npow), Break[]]];
(* gives npow such that 2^npow > lengthvec[M] > 2^n(npow -1) *)
FilledSize=2^npow;
FilledM=FilledVec[M];
numrowsW=√Length[FilledM];*)
```

### W for Human isolate NA19240 chromosome 9 genomic scaffold

Is a "genomic scaffold" a single gene?

#### Data

#### **Process**

```
SpecialNote =
```

" Not sure if this is a single gene or multiple. Also not sure if this is necessarily a set of whole genes or if it's just the DNA sequence corresponding to a particular chromosomal structure. In that case it might includes only parts of some genes (not the whole genes)";

```
Wgenesample = "Human chromosome9 scaffold gene"
(*Lets us know which gene we're dealing with,
used in pdf coding later, so be sure to name it *)
```

Human chromosome9 scaffold gene

```
LetterDNAtoNum[Sample_] := ToExpression[StringReplace[ToString[
                             {StringReplace[StringReplace[ToString[{Sample}], {"," \rightarrow "", " \rightarrow "", "{" \rightarrow "",
                                                        " \}" \to "", " (" \to "", ")" \to "", " [" \to "", "]" \to "", ";" \to "", ":" \to "", "\_" \to "", "
                                                        "+" \rightarrow "", "&" \rightarrow "", "/" \rightarrow "", "." \rightarrow "", "RowBox" \rightarrow "", "Null" \rightarrow ""}],
                                           \{"0" \rightarrow "0,", "1" \rightarrow "1,", "2" \rightarrow "2,", "3" \rightarrow "3,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "A" \rightarrow "0,", "A" \rightarrow "1,", "A"
                                                 "G" → "2,", "T" → "3,", "a" → "0,", "c" → "1,", "g" → "2,", "t" → "3,"}]}
                     ], ",}" → "}"]]
 numgenesample = LetterDNAtoNum[lettersample];
  Export[StringReplace["GENE_genesample.txt", "GENE_gene" → Wgenesample],
       Flatten[numgenesample]]
Human chromosome9 scaffold genesample.txt
lengthofgeneitself = Length[Flatten[numgenesample]]
          (*To make sure no base pairs are left out *)
 59 027
```

#### Construction of W

Can compare to W constructen in Python file **W\_hat\_construction.py** if we want

```
lettersample = {basepairs} // ToString;
LetterDNAtoNum[Sample_] := ToExpression[StringReplace[ToString[
                     \{StringReplace[StringReplace[ToString[\{Sample\}], \{"," \rightarrow "", " " \rightarrow "", "\{" \rightarrow "", " \} \})\} \}
                                       "\}" \rightarrow "", "(" \rightarrow "", ")" \rightarrow "", "[" \rightarrow "", "]" \rightarrow "", ";" \rightarrow "", ":" \rightarrow "", "
                                      "+" \rightarrow "", "&" \rightarrow "", "/" \rightarrow "", "." \rightarrow "", "RowBox" \rightarrow "", "Null" \rightarrow "", "
                                   " → "", "
 " → ""}],
                             \{"0" \rightarrow "0,", "1" \rightarrow "1,", "2" \rightarrow "2,", "3" \rightarrow "3,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "A" \rightarrow "0,", "C" \rightarrow "1,", "A" \rightarrow "0,", "A" \rightarrow "0,", "A" \rightarrow "0,", "A" \rightarrow "1,", "A"
                                  "G" \rightarrow "2,", "T" \rightarrow "3,", "a" \rightarrow "0,", "c" \rightarrow "1,", "g" \rightarrow "2,", "t" \rightarrow "3,"}]}
              ], ",}" → "}"]]
numgenesample = LetterDNAtoNum[lettersample];
lengthofgeneitself = Length[Flatten[numgenesample]];
M = numgenesample;
For [npow = 1, npow < 1000, npow++, If [Length[M] < (2^(npow)), Break[]];
         FilledSize = 2^ (npow + 1) ];
Filler[vecvar1_] := Table[4, {i, 1, FilledSize - lengthofgeneitself}]
FilledVec[vecvar2] := Join[Flatten[vecvar2], Filler[vecvar2]]
Filler[vecvar4_] := Table[4, {i, 1, FilledSize - lengthofgeneitself}]
FilledVec[vecvar5] := Join[Flatten[vecvar5], Filler[vecvar5]]
For [npow = 1, npow < 1000, npow++, If [lengthofgeneitself \le (2^npow), Break[]]];
 (* gives npow such that 2^npow > lengthofgeneitself > 2^(npow -1) *)
FilledSize = 2^npow;
FilledM = FilledVec[M];
numrowsW = \sqrt{Length[FilledM]};
```

```
W = Table [Table [FilledM[[i]],
      \{i, (((j-1)*(numrowsW))+1), (j*(numrowsW))\}], \{j, 1, numrowsW\}];
(*numgenesample=LetterDNAtoNum[lettersample];
lengthofgeneitself=Length[Flatten[numgenesample]];
M=numgenesample;
lengthvec[M_]:=Length[M[[1,All]]]
  For[npow=1,npow<1000,npow++,If[lengthvec[M]<(2^(npow)),Break[]];
   FilledSize=2^(npow+1)];
Filler[M_]:=Table[4,{i,1,FilledSize-lengthvec[M]}]
   FilledVec[M ]:=Join[Flatten[M],Filler[M]]
    lengthvec[M_]:=Length[M[[1,All]]]
     Filler[M_]:=Table[4,{i,1,FilledSize-lengthvec[M]}]
       FilledVec[M_]:=Join[Flatten[M],Filler[M]]
       For \lceil npow=1, npow<1000, npow++, If \lceil lengthvec[M] \le (2^npow), Break[] \rceil \rceil;
(* gives npow such that 2^npow > lengthvec[M] > 2^n(npow -1) *)
FilledSize=2^npow;
FilledM=FilledVec[M];
numrowsW=√Length[FilledM];*)
```

### W for PCV1 samples

### W for H1A

### Run this for output and pdf

```
Wgenesample
 \rho = (W.Transpose[W]); (* <math>\rho as inner product *)
 rhoEigens = Sort[DeleteCases[Eigenvalues[ρ] // N, 0.], Greater];
 (*DeleteCases Removes 0's from the set of Eigenvalues,
 Sort puts the list in order of greatest to least *)
           rhoEigens
       Total[rhoEigens]
 (* This is the set of nonzero normalized eigenvalues in order of greatest to least *)
 n = Length[set];
 H[\alpha_{-}] := \frac{1}{1-\alpha} Log[2, Sum[(set[[i]])^{\alpha}, \{i, 1, n\}]] // N
 H0 = Log[n] // N; (* H_0 = Hartley Entropy*)
 H1 = -Sum[((set[[i]])(Log[2, set[[i]])), {i, 1, n}] // N;
 (* H_1 = Shannon Entropy*)
 H2onward = Table[H[a], {a, 2, 20}] // N; (* H<sub>2</sub> onward *)
 RenyiEntropyofEigenvalues = Join[{H0}, {H1}, H2onward];
Human H1A gene
Null<sup>2</sup>
```

```
button =
  Button["Click here for output and pdf", Print[Style[Wgenesample, Black, Bold, 28]] x
```

```
Print[Style["The ", Blue, Italic, 18], Style[Wgenesample, Black, Italic, 18],
 Style[" has ", Blue, Italic, 18], Style[lengthofgeneitself, Black, Italic, 18],
          base pairs ", Blue, Italic, 18]] ×
 Style["
If[StringLength[SpecialNote] > 3, Print[Style["(Special Note): ", Black, Bold, 16],
  Style[SpecialNote, Black, Italic, 12]], Print[" "]] x
Print[Style["W is a ", Blue, Italic, 18], Style[Length[W], Black, Italic, 18],
 Style[" by ", Blue, Italic, 18], Style[Length[W[[1]]], Black, Italic, 18],
 Style[" matrix with ", Blue, Italic, 18],
 Style[Length[W] * Length[W[[1]]], Black, Italic, 18],
 Style[" = 2^b elements", Blue, Italic, 18], Style[" for b = ", Blue, Italic, 18],
 Style[Log[2, Length[W] * Length[W[[1]]]], Black, Italic, 18] x
If \lceil (\text{Length}[W] * \text{Length}[W[[1]]]) = (\text{Length}[W])^2,
 Print[Style["(If statement safecheck): ", Black, Bold, 12],
  Style[Length[W], Black, Italic, 12], Style[" times ", Red, Italic, 12],
  Style[Length[W[[1]]], Black, Italic, 12],
  Style["
           equals ", Red, Italic, 12], Style[(Length[W]^2), Black, Italic, 12],
  Style[" W is of the right size, you may proceed ", Red, Italic, 12]],
 Print[Style["(If statement safecheck): ", Black, Bold, 12],
  Style["Warning!!!", Red, Italic, 28],
  Style["
            W is of wrong size, STOP and check W ", Red, Italic, 12]]\times
Print["The number of nonzero eigenvalues is = ", Length[rhoEigens]] x
Do[Print["The i-th Eigenvalue "\lambda_i, " is = ", (rhoEigens)[[i]]],
 {i, 1, Length[rhoEigens]}] x
Print[Graphics[ListPlot[rhoEigens // N, AxesLabel → {Style["i", Medium, Bold],
      Style["\lambda_i", Medium, Bold]}, PlotLabel \rightarrow "Eigenvalue PLOT"]]] \times
Print[Graphics[ListLogPlot[rhoEigens // N, AxesLabel → {Style["i", Medium, Bold],
      Style["Log[\lambda_i]", Medium, Bold]}, PlotLabel \rightarrow "Eigenvalue Log PLOT"]]] \times
Print["Zooming in on the Log Plot so as to Exclude the first
   eigenvalue gives the following plot:"] \times
Print[Graphics[ListLogPlot[Table[{i, rhoEigens[[i]]}, {i, 2, Length[rhoEigens]}],
   AxesLabel \rightarrow {Style["i", Medium, Bold], Style["Log[\lambda_i]", Medium, Bold]},
   PlotRange \rightarrow {{10, 2 * rhoEigens[[2]]}}, PlotStyle \rightarrow Red,
   PlotLabel \rightarrow Style["Logplot of Eigenvalues, excluding \lambda_1", Red, Bold, 16]]]] \times
Print["The approximate linearity of the above plot tells us
   that the eigenvalues decrease exponentially. If it's
   nowhere near linear try adjusting the plot range. "]
Print[" "] ×
Print[Style[
                                                                     18]] ×
Print[" "]
Print[Style["The First normalized eigenvector is: ", Blue, Italic, 18],
 Style[set[[1]], Blue, Italic, 18]] x
Print[Style["The Second normalized eigenvector is: ", Blue, Italic, 18],
 Style[set[[2]], Blue, Italic, 18]] x
Print[Style["The Last (n-th) normalized (nonzero) eigenvector is: ",
  Blue, Italic, 18], Style[set[[n]], Blue, Italic, 16]] x
If[Total[set] == 1, Print[Style["(If statement safecheck): ", Black, Bold, 12],
  Style["Total[set] = ", Red, Italic, 12], Style[Total[set], Black, Italic, 12],
```

```
Style[" = 1, so the Eigenvalue set is properly normalized", Red, Italic, 12]],
      Print[Style["(If statement safecheck): ", Black, Bold, 12],
       Style["Warning!!!", Red, Italic, 28], Style[" Total[set] = ", Red, Italic, 12],
       Style[Total[set], Black, Italic, 12], Style[" # 1, ", Red, Italic, 12],
       Style[" so the Eigenvalue set is NOT properly normalized.", Red, Italic, 12],
       Style[" This will render the entropies invalid. Fix it. ", Red, Italic, 12]]]
    Print[" "] ×
    Print[Style[
                                                                                   ■", 18]]×
    Print[" "]
    Do[Print["The \alpha-th Renyi Entropy H_{\alpha} \rightarrow H_{i-1}, " is = ",
       \label{lem:renyientropyofeigenvalues[[i]]], i, 1, Length[RenyiEntropyofEigenvalues]}] \times \\
    Print[Graphics[Show[
        ListPlot[RenyiEntropyofEigenvalues, PlotRange → All,
         AxesLabel \rightarrow {Style["\alpha", Large, Bold], Style["H_{\alpha}", Large, Bold]}],
        ListLinePlot[RenyiEntropyofEigenvalues, PlotStyle → {Red, Thin}]
       ]]]×
    Export["rhoEigenEntropies.pdf", EvaluationNotebook[]] x
    NotebookSave[EvaluationNotebook[], "rhoCalcOutput"];
   SystemOpen["rhoEigenEntropies.pdf"]
   (*DeleteFile[StringReplace["rhoEigenEntropies.pdf", "rho" → Wgenesample]]
    RenameFile["rhoEigenEntropies.pdf",
     StringReplace["rhoEigenEntropies.pdf","rho"→ Wgenesample]]
    SystemOpen[StringReplace["rhoEigenEntropies.pdf", "rho" → Wgenesample]]*)
   , Background → Green;
nb = CreateDocument[];
Paste[nb, button]
NotebookEvaluate[nb];
```

#### Possible Issues

Be sure that W contains only integer values (e.g. 0, 1, 2, 3, 4).

Including floats (e.g. 0.0, 1.0, 2.0, 3.0, 4.0) may incorrectly make some of the eigenvalues negative or imaginary because of how mathematica handles floats differntly than it handles integers.

### H1A Renyi Entropy Calc

### General Definitional Terms (let H1A = M)

Define a 1x781 vector H1Avec which contains all the base pair info of the H1A gene

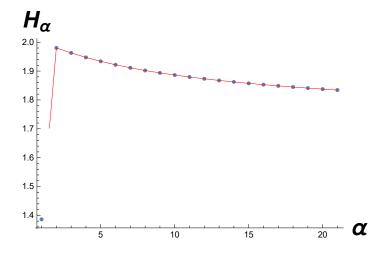
```
H1Avec =
  {{3, 0, 2, 2, 1, 3, 2, 1, 2, 3, 3, 2, 2, 2, 2, 1, 1, 3, 3, 3, 3, 3, 3, 3, 1, 2, 1, 0, 3, 1, 1, 3, 2,
     1, 3, 3, 1, 2, 3, 1, 0, 2, 2, 3, 3, 3, 0, 3, 0, 1, 1, 0, 1, 3, 3, 3, 0, 3, 3, 3, 2, 2, 3, 2, 3,
     2, 1, 3, 2, 3, 2, 3, 3, 0, 2, 3, 1, 0, 1, 1, 0, 3, 2, 3, 1, 3, 2, 0, 0, 0, 0, 1, 0, 2, 3, 2, 1, 1,
    3, 1, 1, 1, 2, 1, 1, 1, 1, 1, 2, 1, 1, 2, 1, 3, 3, 1, 3, 2, 1, 3, 2, 1, 3, 1, 1, 3, 2, 0,
     2, 0, 0, 0, 1, 1, 3, 3, 3, 0, 2, 1, 3, 2, 2, 1, 0, 0, 2, 0, 0, 2, 2, 1, 0, 0, 0, 2, 0, 0,
    0, 1, 1, 3, 2, 1, 3, 0, 0, 2, 2, 1, 3, 2, 1, 0, 2, 1, 0, 2, 1, 1, 3, 1, 1, 0, 0, 2, 0, 0,
    0, 0, 0, 0, 1, 1, 1, 2, 1, 3, 2, 2, 1, 1, 1, 3, 3, 1, 1, 2, 3, 2, 3, 1, 0, 2, 0, 2, 1, 3,
     2, 0, 3, 1, 2, 3, 2, 1, 0, 2, 2, 1, 3, 2, 1, 3, 3, 1, 1, 3, 1, 1, 3, 1, 3, 0, 0, 2, 2, 0,
    2, 1, 2, 3, 2, 2, 3, 2, 2, 3, 2, 3, 2, 3, 1, 2, 3, 3, 2, 2, 1, 0, 2, 1, 3, 1, 3, 3, 0, 0,
    0, 0, 0, 2, 2, 1, 2, 1, 3, 2, 2, 1, 2, 2, 1, 1, 2, 1, 0, 2, 2, 1, 3, 0, 1, 2, 0, 1, 2, 3,
     2, 2, 0, 2, 0, 0, 2, 0, 0, 1, 0, 0, 1, 0, 2, 1, 1, 2, 1, 0, 3, 3, 0, 0, 2, 1, 3, 2, 2, 2,
    1, 0, 3, 3, 0, 0, 2, 0, 2, 1, 1, 3, 2, 2, 3, 0, 0, 2, 1, 0, 0, 2, 2, 2, 0, 0, 1, 2, 3, 3,
     2, 2, 3, 2, 1, 0, 2, 0, 1, 0, 0, 0, 2, 2, 2, 3, 0, 1, 1, 2, 2, 0, 2, 1, 1, 3, 1, 2, 2, 2,
     3, 3, 1, 1, 3, 3, 1, 0, 0, 2, 1, 3, 1, 0, 0, 1, 0, 0, 2, 0, 0, 2, 2, 1, 2, 3, 1, 1, 3, 1,
    1, 2, 3, 2, 2, 0, 0, 0, 1, 1, 0, 0, 2, 1, 1, 1, 2, 2, 1, 2, 1, 1, 3, 1, 0, 0, 0, 2, 2, 3,
     2, 2, 1, 3, 0, 1, 0, 0, 0, 0, 0, 1, 3, 0, 0, 2, 2, 1, 0, 0, 1, 2, 2, 2, 3, 2, 1, 0, 3, 1,
    3, 0, 0, 0, 0, 0, 2, 1, 3, 1, 0, 0, 0, 0, 2, 2, 1, 1, 0, 1, 2, 2, 2, 2, 2, 1, 3, 0, 2,
     1, 0, 0, 0, 0, 0, 2, 0, 2, 1, 2, 3, 1, 0, 0, 2, 0, 1, 3, 1, 1, 2, 0, 0, 0, 0, 0, 2, 2, 1,
    3, 0, 0, 0, 0, 0, 2, 1, 1, 3, 2, 1, 2, 2, 1, 0, 0, 1, 0, 0, 2, 2, 0, 0, 0, 3, 1, 1, 3, 1,
    1, 0, 0, 2, 0, 0, 3, 1, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0, 0, 0, 1, 3, 2, 3, 0, 0, 0,
     2, 1, 1, 1, 0, 0, 2, 0, 0, 0, 2, 3, 0, 2, 1, 3, 0, 0, 0, 0, 2, 1, 1, 1, 3, 2, 1, 3, 0,
    0, 0, 2, 1, 3, 0, 0, 2, 2, 1, 3, 2, 3, 0, 0, 0, 0, 1, 1, 1, 0, 0, 2, 2, 1, 2, 2, 1, 1,
    0, 0, 2, 2, 1, 3, 0, 2, 2, 2, 3, 2, 0, 1, 2, 0, 0, 2, 1, 1, 0, 0, 0, 2, 0, 1, 3, 2, 1,
    1, 0, 0, 0, 1, 1, 1, 0, 0, 2, 0, 0, 0, 2, 1, 2, 2, 1, 0, 1, 1, 1, 0, 0, 2, 0, 0, 0, 0,
    0, 2, 3, 0, 0, 0, 3, 3, 1, 0, 2, 3, 3, 0, 2, 0, 0, 2, 3, 3, 3, 1, 3, 3, 1, 3, 0, 2, 3,
    0, 0, 1, 1, 1, 0, 0, 1, 2, 2, 1, 3, 1, 3, 3, 3, 3, 0, 0, 2, 0, 2, 1, 1, 0, 1, 1, 3, 0}};
M = H1Avec;
lengthvec[M ] := Length[M[[1, All]]]
For [npow = 1, npow < 1000, npow++, If [lengthvec[M] < (2^(npow)), Break[]];
  FilledSize = 2^ (npow + 1) ];
Filler[M ] := Table[4, {i, 1, FilledSize - lengthvec[M]}]
FilledVec[M_] := Join[Flatten[M], Filler[M]]
lengthvec[M ] := Length[M[[1, All]]]
Filler[M_] := Table[4, {i, 1, FilledSize - lengthvec[M]}]
FilledVec[M_] := Join[Flatten[M], Filler[M]]
For [npow = 1, npow < 1000, npow++, If [lengthvec[M] \leq (2^npow), Break[]]];
(* gives npow such that 2^npow > lengthvec[M] > 2^n(npow -1) *)
FilledSize = 2^npow;
H1A Renyi Entropies
Length[M[[1]]] (*Should be 781 *)
Length[FilledVec[M]](*Should be 1024 *)
781
1024
```

```
set = M[[1]];(* Define the set here,
then the following functions are defined using this set *)
set = FilledVec[M];(* Define the set here,
then the following functions are defined using this set *)
n = Length[Union[set]] (* i.e. n = number of unique elements in the set *)
prob[i_] := \frac{Count[set, Union[set][[i]]]}{Length[set]} // N
H[\alpha_{-}] := \frac{1}{1-\alpha} Log[2, Sum[(prob[i])^{\alpha}, \{i, 1, n\}]] // N
```

4

```
(* Gives a plot of the Renyi Entropies for \alpha \ge 0, RUN BLUE CELL FIRST *)
H0 = Log[n] // N; (* H_0 = Hartley Entropy*)
H1 = -Sum[((prob[i])(Log[2, prob[i])), \{i, 1, n\}]; (* H<sub>1</sub> = Shannon Entropy*)
H2onward = Table[H[a], {a, 2, 20}] // N; (* H<sub>2</sub> onward *)
RenyiEntropyofH1AData = Join[{H0}, {H1}, H2onward]
Show [
 ListPlot[RenyiEntropyofH1AData, PlotRange → All,
  AxesLabel \rightarrow {Style["\alpha", Large, Bold], Style["H_{\alpha}", Large, Bold]}],
 ListLinePlot[RenyiEntropyofH1AData, PlotStyle → {Red, Thin}]
```

```
{1.38629, 1.98039, 1.96288, 1.94741, 1.93382, 1.92189,
1.91138, 1.90206, 1.89375, 1.88627, 1.87949, 1.8733, 1.86762, 1.86237,
1.85749, 1.85296, 1.84872, 1.84475, 1.84102, 1.83752, 1.83423}
```



```
Union[set] (* prob[i] measures prob of obtaining Union[set][[i]] *)
prob[1]
prob[2]
prob[3]
prob[4]
{0, 1, 2, 3}
0.297055
0.261204
0.256082
0.185659
Table[{"The", i-1, "-th Renyi Entropy is =", RenyiEntropyofH1AData[[i]]}, {i, 1, 21}]
{{The, 0, -th Renyi Entropy is =, 1.38629},
 {The, 1, -th Renyi Entropy is =, 1.98039}, {The, 2, -th Renyi Entropy is =, 1.96288},
 {The, 3, -th Renyi Entropy is =, 1.94741}, {The, 4, -th Renyi Entropy is =, 1.93382},
 {The, 5, -th Renyi Entropy is =, 1.92189}, {The, 6, -th Renyi Entropy is =, 1.91138},
 {The, 7, -th Renyi Entropy is =, 1.90206}, {The, 8, -th Renyi Entropy is =, 1.89375},
 {The, 9, -th Renyi Entropy is =, 1.88627}, {The, 10, -th Renyi Entropy is =, 1.87949},
 {The, 11, -th Renyi Entropy is =, 1.8733}, {The, 12, -th Renyi Entropy is =, 1.86762},
 {The, 13, -th Renyi Entropy is =, 1.86237}, {The, 14, -th Renyi Entropy is =, 1.85749},
 {The, 15, -th Renyi Entropy is =, 1.85296}, {The, 16, -th Renyi Entropy is =, 1.84872},
 {The, 17, -th Renyi Entropy is =, 1.84475}, {The, 18, -th Renyi Entropy is =, 1.84102},
 {The, 19, -th Renyi Entropy is =, 1.83752}, {The, 20, -th Renyi Entropy is =, 1.83423}}
```