

**STARTER:** In our last lesson, we looked at capacitor discharge. Capacitors discharge through a resistor; how and why can we control the speed of discharge by varying the resistor?

**EXTENSION:** How could you redesign a defibrillator to make it safer for use on children?



Capacitance

Capacitors 4

MUST (C)

Recall the equation for the discharge of capacitors and the meaning of time constant

We can recall that:

$$Q = Q_0 e^{-rac{t}{CR}}$$
 (Q can be replaced with V or I)

When t = CR, the equation reads:

$$Q = Q_0 e^{-1}$$

 $e^{-1}$  is approx. 0.37; so at t = CR  $Q = 0.37Q_0$ 

$$Q = 0.37Q_0$$

$$\frac{Q}{Q_0} = e^{-\frac{t}{CR}}$$

$$\frac{Q}{Q_0} = e^{-\frac{t}{CR}} \qquad ln\left(\frac{Q}{Q_0}\right) = -\frac{t}{CR}$$

- 1. A 100 μF capacitor being discharged through a 1.5 MΩ resistor has an initial charge of 3C. What is its charge at 250 seconds?
- 2. The same capacitor is discharged through another resistor. It takes 200 seconds for the charge to halve. Approximately what is the resistor's value?

Capacitors

Capacitance 4

SHOULD (B)

Explain and apply the equation for current and p.d. when charging capacitors

Charging a capacitor is also an exponential process; the rate of charge is initially fast, but drops with progressive charging.

When the switch S is closed, the capacitor charges. Initially, the current flow is high, as electrons move onto the capacitor plates. As the p.d. across C increases, the current decreases.

When p.d. across  $C = V_0$ , I = 0.

$$I = I_0 e^{-\frac{t}{CR}}$$

How will the p.d. across the resistor vary?

As V = IR..... 
$$V = V_0 e^{-\frac{t}{CR}}$$



We know that  $V_R + V_C = V_0$ , so

$$V_C = V_0 - V_R$$

$$V_C = V_0 - V_0 e^{-\frac{t}{CR}}$$

$$V_C = V_0 - V_0 e^{-\frac{t}{CR}}$$
  $V_C = V_0 (1 - e^{-\frac{t}{CR}})$ 









