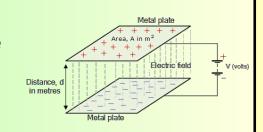
| Capacitors | | Capacitors 2 - connecting capacitors | |
|---------------------|--------------|--|--|
| Learning objectives | MUST (C) | plain how the structure of a capacitor affects its properties | |
| | SHOULD (B) | Understand the derivation of the rule for finding total capacitances for capacitors in series/parallel | |
| | COULD (A/A*) | Calculate the capacitances of different capacitor combinations | |

STARTER: We know that the amount of charge that a capacitor can store is expressed by its **capacitance** (C). What physical features of a capacitor do you think affect its capacitance?



EXTENSION: What factors do you think an equation to calculate capacitance would contain, and how would they relate (proportional, inverse...) to the capacitance?

$$C = \frac{\varepsilon A}{d}$$
Where,

C = Capacitance in Farads

 ϵ = Permittivity of dielectric (absolute, not relative)

A = Area of plate overlap in square meters

d = Distance between plates in meters

Why is d inversely proportional to C?

Because the further apart the plates, the lower the electrostatic field between them.

Capacitors 1 homework: answers

- 1. C
- 2. C
- 3. D
- 4. A
- 5. D
- 6. B
- 7. D
- 8. B

Capacitors

Capacitors 2 - connecting capacitors

MUST (C)

Explain how the structure of a capacitor affects its properties

The equation for capacitance for a parallel plate capacitor with a vacuum between the plates is:

$$C = \frac{\varepsilon_0 A}{d}$$

 ϵ_0 is permittivity of free space, 8.854 x 10⁻¹² F m⁻¹

A is area of overlap, d is separation: convert units to m

When an insulator (or dielectric) other than a vacuum is used, the equation used is:

$$C = \frac{\varepsilon A}{d}$$

$$\varepsilon = \varepsilon_r \varepsilon_0$$

where $\ensuremath{\varepsilon} = \ensuremath{\varepsilon_r} \ensuremath{\varepsilon_0}$ and $\ensuremath{\varepsilon_{\scriptscriptstyle r}}$ is **relative** permittivity.

Material 1 (by definition) vacuum 1.0006 air 3.3 perspex 4.0 paper 7.0 mica 1200 barium titanate

ε is the permittivity for the insulator.



Two square completely overlapping plates with side length 1 cm, 2 mm apart, with a perspex dielectric. What is the capacitance? ϵ_0 is 8.854 x 10⁻¹² F m⁻¹



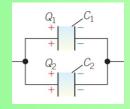


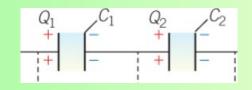
Capacitance Capacitors 2 - connecting capacitors

SHOULD (B)

Understand the derivation of the rule for finding total capacitances for capacitors in parallel/series

Connecting capacitors in parallel and in series; will the overall capacitance increase or decrease?







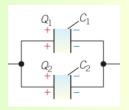
Capacitors in parallel: the same V is across both capacitors.

Total charge $Q = Q_1 + Q_2$ (conservation of charge)

Recalling that Q = CV

If C is total capacitance, $CV = C_1V + C_2V$

V is the same in each case, so cancels out: $C = C_1 + C_2$





Total capacitance of capacitors in parallel = sum of the capacitances

Capacitors

Capacitors 2 - connecting capacitors

SHOULD (7)

Understand the derivation of the rule for finding total capacitances for capacitors in parallel/series

Capacitors in series

Potential difference split between the two capacitors.

Q is the same for all capacitors

Total p.d.
$$V = V_1 + V_2$$

$$V = Q/C$$

$$Q/C = Q/C_1 + Q/C_2$$

Cancel out by Q throughout to give: $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2}$

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2}$$

Capacitors

Capacitors 2 - connecting capacitors

COULD (A/A*)

Calculate the capacitances of different capacitor combinations

Complete:

Summary questions 1-3 in section 21.2.

Summary questions 4-6 in section 21.2.

Key points:

Series: Q is constant, and $1/C = 1/C_1 + 1/C_2...$

Parallel: V is constant, and $C = C_1 + C_2$

21.2

1 Parallel: $C = C_1 + C_2 = 100 + 100 = 200 \,\mathrm{pF}$ [1]

Series:
$$C = (C_1^{-1} + C_2^{-1})^{-1} = (100^{-1} + 100^{-1})^{-1}$$
 [1]

$$C = 50 \,\mathrm{pF} \tag{1}$$

The total capacitance for the parallel circuit is **twice** the capacitance of a single capacitor [1] and the total capacitance for the series circuit is **half** the capacitance of a single capacitor. [1]

2
$$C = (C_1^{-1} + C_2^{-1})^{-1} = (120^{-1} + 120^{-1})^{-1}$$
 [1]

$$C = 60 \,\mathrm{nF} \tag{1}$$

$$Q = VC = 60 \times 10^{-9} \times 1.5$$
 [1]

$$Q = 9.0 \times 10^{-8} \,\mathrm{C} \tag{1}$$

3 Total capacitance of *N* identical 1000 μF capacitors in parallel = $N \times 1000$ μF [1]

Therefore,
$$N \times 1000 \times 10^{-6} = 4000$$
 [1]

$$N = 4 \times 10^6$$
 (4 million) in parallel [1]

4
$$C_1 = (100^{-1} + 500^{-1})^{-1} = 83.3 \mu F$$
 [2]

$$C_2 = (50^{-1} + 200^{-1})^{-1} = 40 \mu F$$
 [2]

0:05:00

Total capacitance =
$$C_1 + C_2 = 83.3 + 40 \approx 123 \,\mu\text{F}$$
 [1]

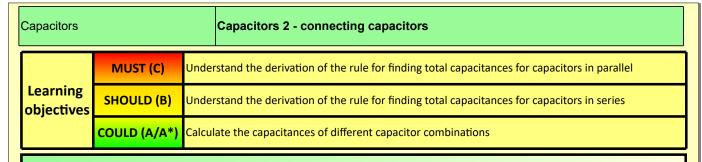
across the combination is 6.0 V. [1]
$$V = \frac{Q}{C} \propto \frac{1}{C}$$
, hence the p.d. across the capacitor with capacitor 2C will be half the p.d. across the capacitor with capacitance C. [1]

Therefore, p.d. across C = 4.0 V [1] and the p.d. across 2C = 2.0 V.

$$6 \quad \frac{1}{17} = \frac{1}{C} + \frac{1}{20}$$
 [1]

$$\frac{1}{C} = \frac{1}{17} - \frac{1}{20}$$
 [1]

$$C = 113 \,\text{nF} \approx 110 \,\text{nF}$$
 [1]



PLENARY: Three capacitors are in series: $10\mu F$, $20\mu F$ and $40\mu F$. Which (if any) has the highest potential difference across it? Why?

EXTENSION: What do we know about the total capacitance? Answer without any calculation.

