

(g) Hubble's law; $v = H_0 d$ for receding galaxies, where H_0 is the Hubble constant HSW7

(h) model of an expanding universe supported by galactic red shift HSW2, 7, 8, 11

(i) Hubble constant H_0 in both $\text{km s}^{-1} \text{Mpc}^{-1}$ and s^{-1} units

(d) the Cosmological principle; universe is homogeneous, isotropic and the laws of physics are universal

(6) M - Demonstrate Hubble's law and apply the equation
(7) S - Explain the model of an expanding universe is supported by galactic red shift
(8) C - Explain the significance of the Cosmological principle

Hubble's law

STARTER: Absorption spectra Q

2. The graphs below show the variations of intensity with wavelength for part of the Sun's spectrum and for the same part of the spectrum from a distant star.

a. Explain how the star's motion causes corresponding minima of intensity to occur at different wavelengths. [2]

b. Use the graphs to calculate the velocity of the star. [4]

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a. The wavelengths have been redshifted. Hence, the star must be moving away from us. [1]

b. $\frac{\Delta\lambda}{\lambda} = \frac{v}{c}$ [1]

$\frac{1.4 \text{ nm}}{410.17 \text{ nm}} = \frac{v}{3.0 \times 10^8 \text{ m s}^{-1}}$ [1]

$v = 0.0117 \times 3.0 \times 10^8$ [1]

Speed $\approx 3.5 \times 10^6 \text{ m s}^{-1}$ [1]

https://imagine.gsfc.nasa.gov/educators/hera_college/binary-model.html

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Hubble's law

Sketch the graph of Hubble's data.

Describe the trend.

$v \propto x$

$H_0 = \frac{v}{x} \quad v = H_0 \times x$

Speed of recession of galaxy is directly proportional to the distance of the galaxy.

What is the unit of the Hubble constant?
What is the unit?

$H_0 = \text{Hubble constant} = 70 \text{ km s}^{-1} \text{Mpc}^{-1}$

very distant galaxy
distant galaxy
nearby galaxy
nearby star
laboratory reference

400 500 600 wavelength/nm

1. Convert the Hubble Constant into SI units. (1 pc = $3.1 \times 10^{16} \text{ m}$)
2. How can H_0 be determined from the graph?

$H_0 = 2.3 \times 10^{-18} \text{ s}^{-1}$

Worked example: Hubble constant units

Convert $1 \text{ km s}^{-1} \text{Mpc}^{-1}$ into s^{-1} .

Step 1: Convert the speed into m s^{-1} and then divide it by the distance of 1 Mpc in metres.

$1 \text{ km s}^{-1} \text{Mpc}^{-1} = \frac{1.0 \times 10^3 \text{ m s}^{-1}}{1.0 \times 3.1 \times 10^{16} \text{ m}} = 3.2 \times 10^{-20} \text{ s}^{-1} (2 \text{ s.f.})$

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The expanding universe

1. Explain how Hubble law is evidence for the expanding universe.
2. How can Hubble law be used to find an approximate age of the universe? (what assumptions have been made?) $t \approx \frac{1}{H_0}$

Activity check:

1. Complete Q8,10,14,15,16 on the worksheet.
2. Complete the summary questions

Quick check...

16 A particular galaxy at 80 Mpc is found to have a recession speed of 6000 km s^{-1}

a Use the information given to calculate a possible value for the Hubble constant in:

i $\text{km s}^{-1} \text{Mpc}^{-1}$ [2]

ii s^{-1} [2]

b Use your answer to part a ii to show that the age of the universe is about 13 000 million years. [3]

c Hence determine the furthest observable distance in metres for the universe. [3]

16 a i $H_0 = \frac{v}{d}$ [1]

$H_0 = \frac{6000}{80} = 75 \text{ km s}^{-1} \text{Mpc}^{-1}$ [1]

ii $H_0 = \frac{75 \times 10^3}{10^8 \times 3.1 \times 10^{16}} = 2.4 \times 10^{-18} \text{ s}^{-1}$ [1]

$H_0 = 2.42 \times 10^{-18} \text{ s}^{-1} \approx 2.4 \times 10^{-18} \text{ s}^{-1}$ [1]

b Age of the universe $= (H_0)^{-1} = \frac{1}{2.42 \times 10^{-18}}$ [1]

age $= 4.13 \times 10^{17} \text{ s}$ [1]

age $= \frac{4.13 \times 10^{17}}{365 \times 24 \times 3600} = 1.31 \times 10^{10} = 13 \text{ 000 million years}$ [1]

c Furthest distance = age of universe \times speed of light [1]

furthest distance $= 4.13 \times 10^{17} \times 3.0 \times 10^8 \text{ m}$ [1]

furthest distance $= 1.24 \times 10^{26} \text{ m} \approx 1.2 \times 10^{26} \text{ m} (4000 \text{ Mpc})$ [1]

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10000 galaxies here, we use the **cosmological principle** to assume there is nothing special about this bit of the universe.

Cosmological Principle

Universe is **isotropic**

Universe is **homogenous**. Density is the same everywhere.

Laws of physics are universal.

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Plenary

MC Question:

Recent data from the European Space Agency's Planck Space Observatory gave a value for the Hubble constant of $2.20 \times 10^{-18} \text{ s}^{-1}$. A previous estimate had been $2.19 \times 10^{-18} \text{ s}^{-1}$.

What is the estimated age of the Universe using the European Space Agency data, and is this within 10% of the age calculated with previous data?

○ 14.5 billion years and this is within 10% of the previously calculated value
○ 14.4 billion years and this is within 10% of the previously calculated value
○ 14.4 billion years and this is not within 10% of the previously calculated value
○ 14.5 billion years and this is not within 10% of the previously calculated value

Ex

A star is receding from the Earth with a speed that is 2.5% of the speed of light.

A particular spectral line results from an atomic electron transition between energy levels of energy difference, ΔE .

What is the change in the wavelength, $\Delta \lambda$, of this spectral line in the star's spectrum, in terms of the Planck constant, h , the speed of light, c , and the energy difference, ΔE ?

○ $\Delta \lambda = 0.025 \times \frac{hc}{\Delta E}$
○ $\Delta \lambda = \frac{\Delta E}{(0.025 \times hc)}$
○ $\Delta \lambda = \frac{hc}{0.025 \times \Delta E}$
○ $\Delta \lambda = \frac{hc}{\Delta E}$

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