

3.5.1 Newton's laws of motion

Learning outcomes	Additional guidance
Learners should be able to demonstrate and apply their knowledge and understanding of:	
(a) Newton's three laws of motion	HSW7
(b) linear momentum; $p = mv$; vector nature of momentum	
(c) net force = rate of change of momentum; $F = \frac{\Delta p}{\Delta t}$	Learners are expected to know that $F = ma$ is a special case of this equation. HSW9, 10 M2.1, M3.9
(d) impulse of a force; impulse = $F\Delta t$	
(e) impulse is equal to the area under a force–time graph.	Learners will also be expected to estimate the area under non-linear graphs. HSW3 Using a spreadsheet to determine impulse from F – t graph. M3.8, M4.3

3.5.2 Collisions

Learning outcomes	Additional guidance
Learners should be able to demonstrate and apply their knowledge and understanding of:	
(a) the principle of conservation of momentum	HSW7
(b) collisions and interaction of bodies in one dimension and in two dimensions	Two-dimensional problems will only be assessed at A level. HSW11, 12
(c) perfectly elastic collision and inelastic collision.	HSW1, 2, 6

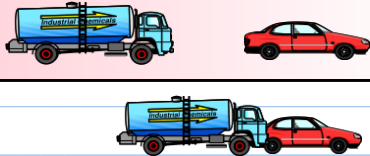
- (6) M - Recall the law of conservation of momentum
- (7) S - Apply the equation for linear momentum.
- (8) C - Analysis collisions that occur in 2 dimensions.

Collisions in 2D

STARTER: A truck of mass 50 kg travelling with a velocity of 3.0 m s^{−1} collides with a stationary truck of mass 30 kg and **they move on together**.

- a** Calculate their velocity after the collision.
- b** Is the collision elastic or inelastic?

Extension: Try Lowe ex7.6



a Step 2

Find the velocity after collision by applying the law of conservation of momentum.

$$m_1 u_1 + m_2 u_2 = (m_1 + m_2) v$$
$$(50 \times 3.0) + (30 \times 0) = (50 + 30) v$$
$$150 + 0 = 80 v$$
$$v = \frac{150}{80}$$
$$v = 1.9 \text{ m s}^{-1} \text{ (to two significant figures)}$$

b Step 3

To decide whether the collision is elastic or inelastic, you need to calculate the kinetic energy before and after the collision, and compare the values.

$$E_K = \frac{1}{2} m v^2$$

Before collision:

$$E_K = \frac{1}{2} m_1 u_1^2 + \frac{1}{2} m_2 u_2^2$$
$$= \left(\frac{1}{2} \times 50 \times 3^2\right) + \left(\frac{1}{2} \times 30 \times 0^2\right)$$
$$= 230 \text{ J}$$

- (6) M - Recall the law of conservation of momentum
- (7) S - Apply the equation for linear momentum.
- (8) C - Analyse collisions that occur in 2 dimensions.

Reminder.....

- 23 When a gardener aims water from a hosepipe at the ground, he notices that the water always splashes in many directions. Fig. 22.1 shows the splashes produced by a vertical jet of water hitting the ground.

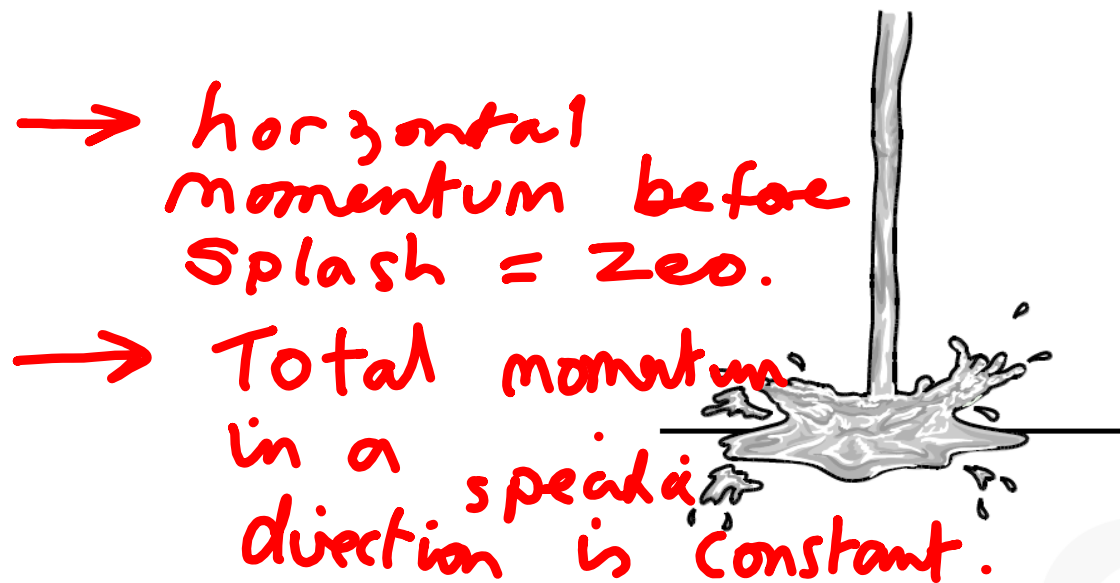


Fig. 22.1

- horizontal momentum before splash = zero.
- Total momentum in a specific direction is constant.
- Water splashing in opposite direction means equal & opposite momentum in opposite direction.

- (a) Using ideas about momentum explain why the water splashes in many directions.

The total momentum is a **specific direction** remains constant, as long as no external forces act.

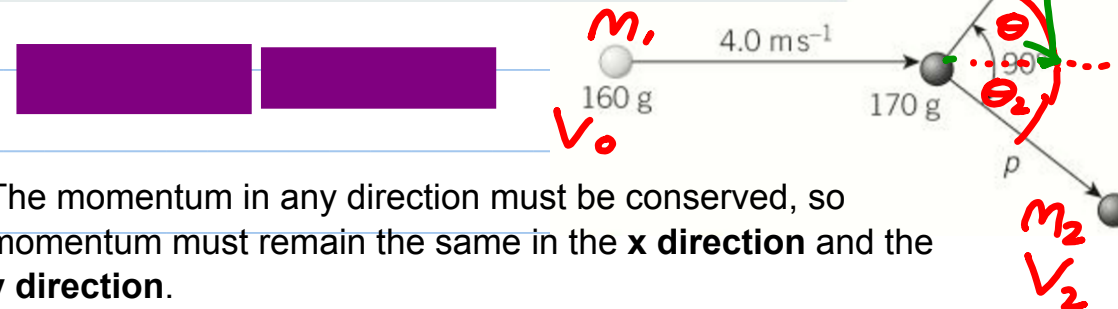
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Snooker example - Resolving momentum



Worked example: Snooker balls

A 160 g white ball travelling at 4.0 ms^{-1} hits a stationary 170 g black ball (Figure 3). After the impact, the balls move apart at approximately 90° to each other, with the white ball travelling at 2.5 ms^{-1} . Calculate the magnitude of the final velocity of the black ball.



1. The momentum in any direction must be conserved, so momentum must remain the same in the **x direction** and the **y direction**.
2. In x: The total momentum before = total momentum after.

$$m_1 v_0 = m_1 v_1 \cos \theta_1 + m_2 v_2 \cos \theta_2$$

$$V_{2x} = 2.97 \text{ ms}^{-1}$$

3. In y: The total momentum before = total momentum after.

$$0 = m_1 v_1 \sin \theta_1 + m_2 v_2 \sin \theta_2$$

$$V_{2y} =$$

4. check this Q - seems wrong - check angles

change question.

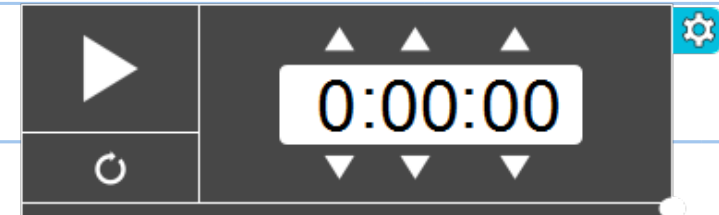


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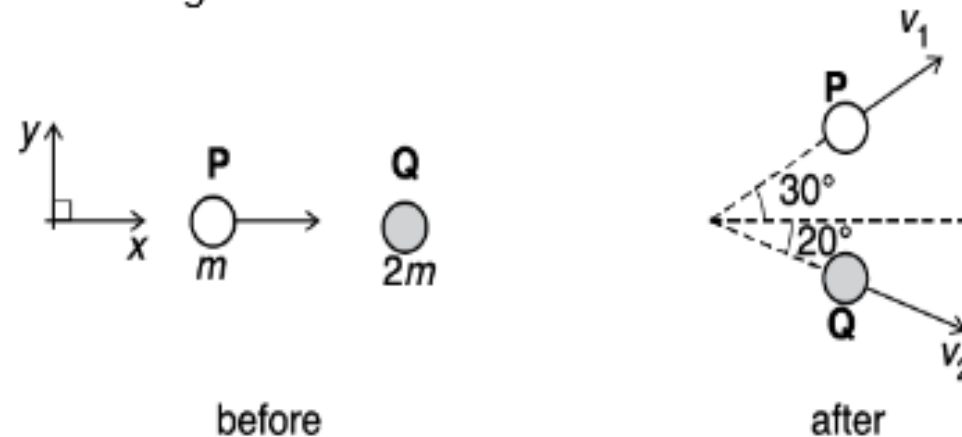
ACTIVITY 1: Complete the summary questions
ACTIVITY 2: Complete Q8 P113

Extension: Try Lowe ex7.6

- (6) M - Recall the law of conservation of momentum
 (7) S - Apply the equation for linear momentum.
 (8) C - Analysis collisions that occur in 2 dimensions.



A ball **P** of mass m has a velocity in the positive x -direction. It makes a collision with a stationary ball **Q** of mass $2m$. After the collision, the ball **P** has velocity v_1 , ball **Q** has velocity v_2 and the balls travel in the directions shown in the diagram below.



After the collision, the total momentum of the balls in the x -direction is p_x and the total momentum in the y -direction is p_y .

Which row is correct for p_x and p_y ?

	p_x	p_y
A	$2mv_2 \cos 20^\circ + mv_1 \cos 30^\circ$	0
B	$2mv_2 \sin 20^\circ + mv_1 \sin 30^\circ$	0
C	$2mv_2 \cos 20^\circ + mv_1 \cos 30^\circ$	$2mv_2 \sin 30^\circ + mv_1 \sin 20^\circ$
D	$2mv_2 \sin 20^\circ + mv_1 \sin 30^\circ$	$2mv_2 \cos 30^\circ + mv_1 \cos 20^\circ$