

# Python Introduction

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# Installing

## Install Anaconda

1. Download the [Anaconda Python/R Distribution](#) 2019.07 (or later).
2. When the download is complete, install into your user account.

## Install Visual Studio Code and the Python extension

1. Download VS Code and install
2. Install the Python extension by clicking on Extensions and searching for “Python”
3. Open the mfe-introduction folder created in the previous step
4. Create a file called second.py and enter

```
#%%  
  
print("Python may be harder to learn than other languages since")  
print("there is rarely a single approach to completing a task.")
```

5. Click on Run Cell

**Note** the #%% makes it a magic cell

## Install Pycharm Professional

1. Download PyCharm Professional and install using the 30-day trial. You can get a free copy using your academic email address if you want to continue after the first 30 days.
2. Open PyCharm, and create a new project called mfe-introduction
3. Open File > Setting and select Python Interpreter. Select the Anaconda interpreter if it is not already selected.
4. Create a new python file called first.py and enter

```
print("Python has a steeper curve than MATLAB but more long-run upside")
```

5. Right-click on this file, and select “Run”.

# Lesson 1

## Getting Started

This lesson covers:

- Opening a terminal window
- Launching Jupyter notebook
- Running IPython in a Terminal
- Running IPython in Jupyter QtConsole
- Executing a standalone Python file in IPython
- Optional
  - Jupyter notebooks in [VSCode](#)
  - Jupyter notebooks in [PyCharm Professional](#)

### 1.1 Opening an Anaconda Terminal

An Anaconda terminal allows python to be run directly. It also allows other useful programs, for example pip, the Python package manager to be used to install packages that are not available through Anaconda.

#### Windows

Launch Anaconda Prompt from the start menu.

#### OSX and Linux

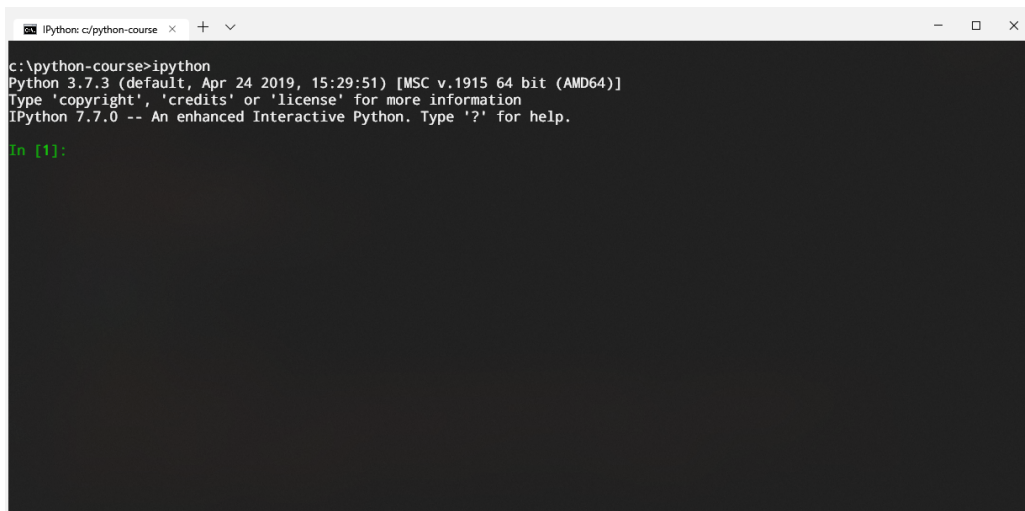
Open the terminal (instructions depend on your distribution). If you allowed conda to initialize, then you should be ready to call Anaconda's python and supporting functions. If not, you should

```
cd ~/anaconda3/bin
./conda init
```

and then reopen your terminal.

## 1.2 Running IPython in a Terminal

1. Open a terminal.
2. Run IPython by entering `ipython` in the terminal window. You should see a window like the one below with the iconic `In [1]` indicating that you are at the start of a new IPython session.

A screenshot of a Windows terminal window titled "IPython: c:\python-course". The terminal shows the command `c:\python-course>ipython` and the output: `Python 3.7.3 (default, Apr 24 2019, 15:29:51) [MSC v.1915 64 bit (AMD64)]  
Type 'copyright', 'credits' or 'license' for more information  
IPython 7.7.0 -- An enhanced Interactive Python. Type '?' for help.` The prompt `In [1]:` is visible in green text.

IPython in Windows Terminal

## 1.3 Launching Jupyter notebook

1. Launch Jupyter Notebook from the Start Menu or launcher.
2. Change directory to the location where you store your notebooks.



Jupyter Notebook

## 1.4 Executing a standalone Python file in IPython

1. Open a text editor and enter the following lines. Save the file as `lesson-2.py`. Note that Python is white-space sensitive, and so these lines should **not** be indented.



```
from math import exp, log

x = exp(1)
y = log(x)

print(f"exp(1)={x}, log(exp(1))={y}")
```

2. Run the code in an IPython session using `%run -i lesson-2.py`. Note: you should create the python file in the same directory as the notebook.

If everything works as expected, you should see

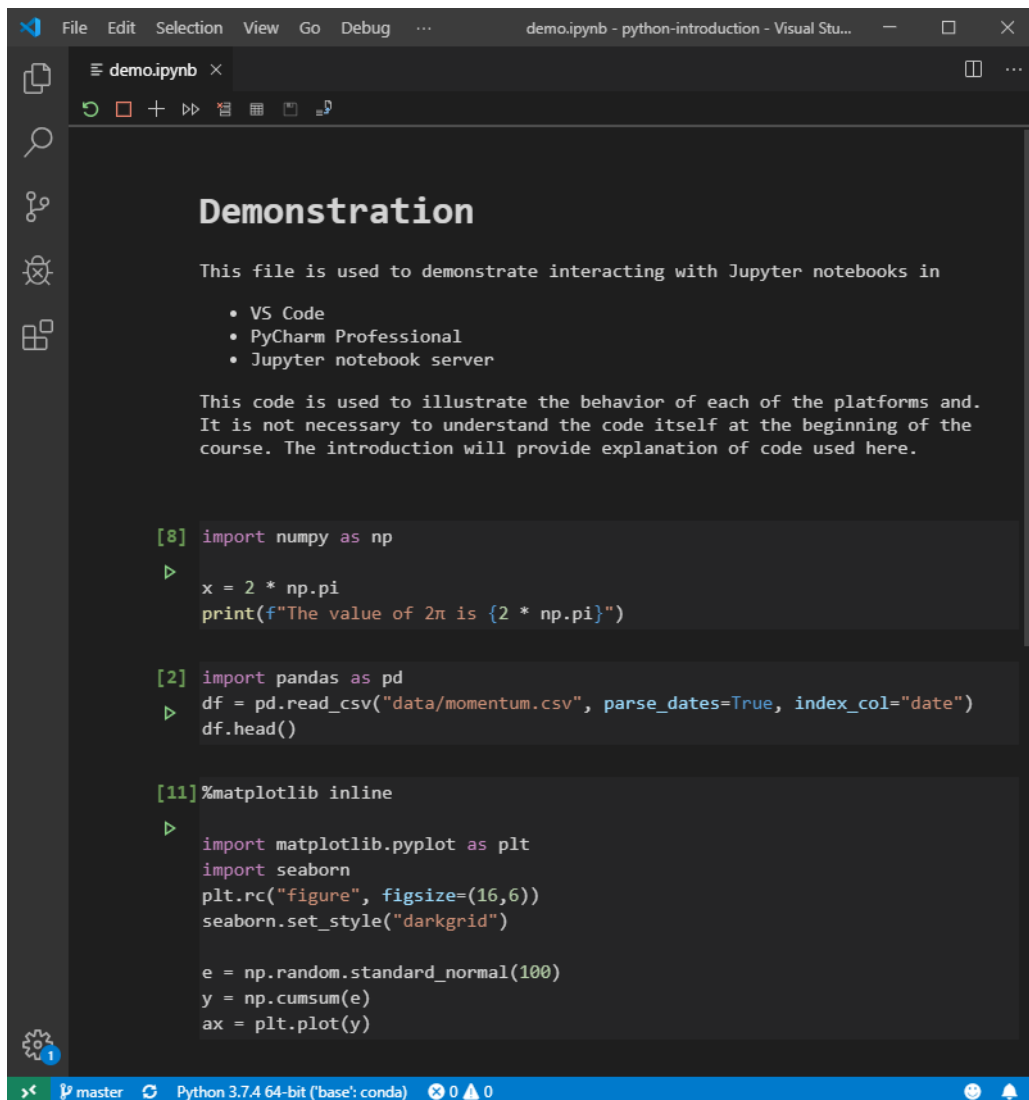
```
exp(1)=2.718281828459045, log(exp(1))=1.0
```

## 1.5 Jupyter notebooks in VSCode

[Visual Studio Code](#) (or VS Code) is a lightweight IDE that supports adding features through extensions. The key extension for working with notebooks is [Python extension for Visual Studio Code](#). With this extension installed, VS code provides native support for Jupyter notebooks.

1. Install VS Code and the Python extension
2. Open the command palette and enter “create jupyter” and select the only available item.

See the screenshot below for an example of the experience of using Jupyter notebooks in VS Code.



VS Code Notebook

## 1.6 Magic Python in VSCode

Visual Studio Code supports Magic Python mode in standard Python files that can be executed cell-by-cell.

1. Install VS Code and the Python extension
2. Select File, New and then save your file with the extension .py (e.g., file.py).
3. This is a Python file that supports a cell demarcation using `%%` for code cells and `%% [markdown]` for cells that contain markdown code. Note that markdown text **must** be either:

- Surrounded by triple quotes, e.g. `"""markdown text"""` or `"""markdown text"""`; e.g.,

## # Cell Heading

|| || ||

- ## ## Cell Heading

# Likeness darkness. That give brought creeping. Doesn't may. Fruit kind  
# midst seed. Creature, let under created void god to. Them day was Was  
# creature set it from. Fourth. Created don't man. Man. Light fourth  
# light given the he image first multiply after deep she'd great. Morning  
# likeness very have give also fowl third land beast from moving thing  
# creepeth herb creeping won't fifth. Us bring was our beast wherein our  
# void and green he fruit kind upon a given, saying fruit, moveth face  
# forth. His you it. Good beginning hath.

The screenshot displays the PyCharm IDE interface with a Jupyter notebook open. The notebook has two cells. The first cell contains code to set up the environment, including importing `os` and `get_ipython()`, and printing the current directory. The second cell contains a markdown header `# Introduction` and a list of bullet points: 

- VS Code
- PyCharm Professional
- Jupyter notebook server

 The third cell contains a code snippet that prints the value of `2x` where `x = 2 * np.pi`. The output of this cell is displayed in the interactive console on the right, showing the value `6.283185307179586`. Below the console, there is a plot of a sine wave, which is the result of the `matplotlib` magic command. The plot shows a single cycle of a sine wave from 0 to 2π.

```
# To add a new cell, type '#%%'
# To add a new markdown cell, type '#%% [markdown]'
Run Cell | Run Below | Debug Cell | Go to IPython

#%% Change working directory from the workspace root to the ipynb file location
# ms-python.python added
import os
try:
    os.chdir(os.path.join(os.getcwd(), 'course\introduction'))
    print(os.getcwd())
except:
    pass

Run Cell | Run Above | Debug cell
#%%
from IPython import get_ipython

Run Cell | Run Above
#%% [markdown]
# # Demonstration
#
# This file is used to demonstrate interacting with Jupyter notebooks
# in
#
# * VS Code
# * PyCharm Professional
# * Jupyter notebook server
#
# This code is used to illustrate the behavior of each of the platforms
# and. It is not necessary to understand the code itself at the beginning
# of the course. The introduction will provide explanation of code used
# here.

Run Cell | Run Above | Debug Cell | Go to IPython
#%%
import numpy as np

x = 2 * np.pi
print(f"The value of 2x is {2 * np.pi}")
```

This file is used to demonstrate interacting with Jupyter notebooks in

- VS Code
- PyCharm Professional
- Jupyter notebook server

This code is used to illustrate the behavior of each of the platforms and. It is not necessary to understand the code itself at the beginning of the course. The introduction will provide explanation of code used here.

```
[1] import numpy as np...
[2] The value of 2x is 6.283185307179586
[2] get_ipython().run_line_magic('matplotlib', 'inline')...
```

The value of 2x is 6.283185307179586

The plot shows a sine wave, which is the result of the `matplotlib` magic command.

Title

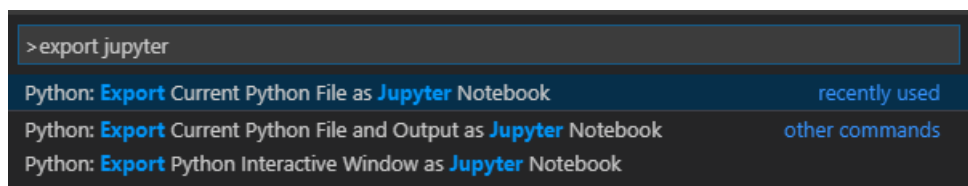
Type code here and press shift-enter to run

5

## Importing an exiting notebook into Magic Python

VS Code only understands Magic Python files as notebook-like documents, and so .ipynb files must be converted to use. The process of importing is simple:

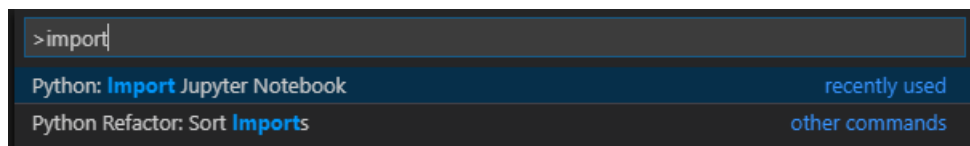
1. Open a Jupyter notebook file
2. Click on Import in the popup that appears.



VS Code Export

## Exporting Magic Python to a Jupyter notebook

To export a Magic Python file, open the command palette and enter “import jupyter”. Select the option to import the notebook.



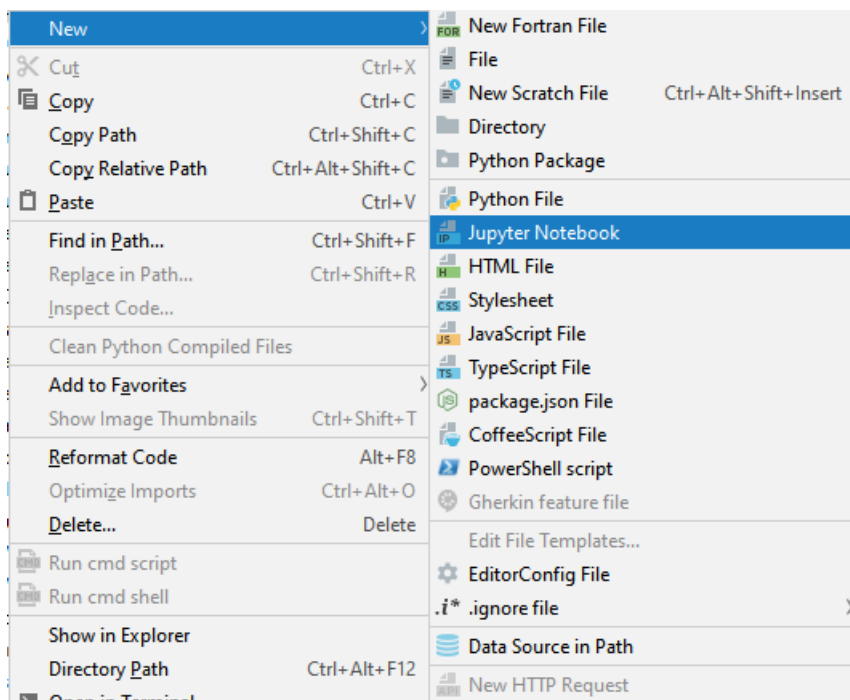
VS Code Import

## 1.7 Jupyter notebooks in PyCharm Professional

PyCharm Professional is my recommended approach if you are going to use Python throughout the course. It provides the best experience and can be acquired for free using the student program.

PyCharm Professional has deeply integrated Jupyter Notebooks. To create an IPython notebook:

1. Open PyCharm Profession
2. Open the directory where your notebooks are stored
3. Right-click on the root directory and select New > Jupyter Notebook. Give your file a meaningful name, and it will open in the main window.



PyCharm New Notebook

PyCharm uses a special syntax where cells look like code and so can be edited like text. This allows PyCharm to use introspection and code completion on the code you have written, a highly useful set of features. PyCharm stores the notebook in a Jupyter notebook file (.ipynb), which means that you can trivially open it in any other Jupyter notebook aware app. This differs from Section 1.5 which stores the file as a plain Python file (.py) and requires an explicit export to a Jupyter notebook file.

A code cell is demarcated using `#%%` and a markdown cell begins with `#%% md`. Below is a screenshot of this notebook in PyCharm.



## PyCharm Notebook

### 1.8 Magic Python in PyCharm

PyCharm supports Magic Python cell execution. To use Magic Python, you need to enable *Scientific Mode* in the View menu. You can then use `#%%` to indicate the start and end of cells. Individual Cells can be executed in the console by pressing CTRL+Enter.

1. In PyCharm, right-click on the root directory and select **New > Python File**. Give your file a meaningful name.
2. Enter

```
#%%
print("This is the first cell")

#%%
print("This is not executed when the first cell is run")
```

3. Enable Scientific Mode in the View menu.
4. Run the first cell by placing your mouse in the cell and pressing CTRL+Enter.
5. Run the second cell by clicking on the Play button (arrow) that appears in the gutter of the editor.

Note: Magic Python in PyCharm only supports python code, and so it is not possible to mix Markdown text and Python in the same file.

## Lesson 2

# Basic Python Types

This lesson covers:

- Inputting scalars and strings
- Lists
- Tuples
- Dictionaries

### Problem: Input scalar floating point and integers

1. Create a variable called `scalar_float` containing  $\pi$  to 4 digits.
2. Create a variable called `scalar_int` containing 31415.
3. Print each value using the `print` function.

### Problem: Create a string and an f-string

1. Create a variable called `a_string` containing `This is a string`
2. Create a f-string the prints `The value of scalar_float is 3.1415` using the variable created in the previous step
3. Create two string, first containing `String concatenation` and the second containing `is like addition`, and join the two using `+` to produce `String concatenation is like addition`.

### Problem: Create a list

1. Create a list containing `scalar_float` and `scalar_int`
2. Add `a_string` to the list.
3. Select the second element from the list
4. Select the the lst two elements of the list

### Problem: Create a list of lists

1. Create a list containing the two lists `[1, 2, 3]` and `[4, 5, 6]`
2. Select the element 5 from the nested list

**Problem: Create a tuple**

1. Create a tuple containing the values (1, 2.0, "c")
2. Select the element "c" from the tuple

**Problem: Convert a list to a tuple and back**

1. Convert the list-of-lists created to a tuple-of-tuples
2. Convert the tuple-of-tuples back to a list of lists

**Problem: Create a dictionary**

1. Create a dictionary containing the key-value pairs "float" and 3.1415, "int" and 31415, and "string" and "three-point-one-four-one-five".

**Problem: Lookup and Change a value**

1. Look up the value of "float".
2. Change the value of "float" to 22 / 7.

**Problem: Add and remove a key**

1. Add the new key "better\_float" with the value 3.141592.
2. Remove the key "float" and its value.

**Exercises****Exercise: Manipulating lists**

1. Create an empty list called `lst`
2. Add the elements 9, "Eight" and 7.0 (in order) to the list.
3. Extend the list with the list ["Six", 5, 4.0] using `extend`
4. Select first 4 elements of `lst`
5. Select last 3 elements of `lst`

**Exercise: Dictionary Manipulation**

1. Create a empty dictionary called `dct`
2. Add the pairs "apple" and 1, "banana" and 2.0, and "cherry" and "iii"
3. Replace the value of "apple" with "I"
4. Remove the entry for "banana"
5. Add an entry "date" with the value 4



### Exercise: Directly create a Dictionary

Using the final version of `dct` from the previous exercise:

1. Directly initialize a new dictionary called `other_dct`.
2. Use an f-string to print the values associated with each key.

**Hint** You must use both types of quotes. For example, to access a value in an f-string.

```
f"{other_dct['apple']}"
```

### Exercise: Tuple Manipulation

1. Create a tuple `tpl` containing 100 and 4
2. Convert to a list, add the elements 101 and 5
3. Convert back to a tuple



## Lesson 3

# Importing Modules

This lesson covers:

- Module import

### Problem: Importing Modules

Python is a general-purpose programming language and is not specialized for numerical or statistical computation. The core modules that enable Python to store and access data efficiently and that provide statistical algorithms are located in modules. The most important are:

- NumPy (numpy) - provide the basic array block used throughout numerical Python
- pandas (pandas) - provides DataFrames which are used to store data in an easy-to-use format
- SciPy (scipy) - Basic statistics and random number generators. The most important submodule is `scipy.stats`
- matplotlib (matplotlib) - graphics. The most important submodule is `matplotlib.pyplot`.
- statsmodels (statsmodels) - statistical models such as OLS. The most important submodules are `statsmodels.api` and `statsmodels.tsa.api`.

Begin by importing the important modules.

### Problem: Canonical Names

Use the `as` keyword to import the modules using their canonical names:

Module	Canonical Name
numpy	np
pandas	pd
scipy	sp
scipy.stats	stats
matplotlib.pyplot	plt
statsmodels.api	sm
statsmodels.tsa.api	tsa

Import the core modules using `import module as canonical`.

### Problem: Importing individual functions

1. Import `array`, `sqrt`, `log` and `exp` from NumPy.
2. Import OLS from `statsmodels.regression.linear_model`
3. Import the `stats` module from `scipy`

## Exercises

### Exercise: Import det

The determinant function is located at `numpy.linalg.det`. Access this function using:

1. `numpy`
2. `np`
3. By importing `linalg` from `numpy` and accessing it from `linalg`
4. By directly importing the function

You can `x` in the setup code to call the function as `func(x)`.

```
# Setup: A simple 2 by 2 array to use with det
import numpy as np
x = np.array([[2,3],[1,2]])
print(x)
```

## Lesson 4

# Series and DataFrames

This lesson covers:

- Constructing pandas Series and DataFrames

## Data September 2018 prices (adjusted closing prices) for the S&P 500 EFT (SPY), Apple (AAPL) and Google (GOOG) are listed below:

Date	SPY Price	AAPL Price	GOOG Price
Sept4	289.81	228.36	1197.00
Sept5	289.03	226.87	1186.48
Sept6	288.16	223.10	1171.44
Sept7	287.60	221.30	1164.83
Sept10	288.10	218.33	1164.64
Sept11	289.05	223.85	1177.36
Sept12	289.12	221.07	1162.82
Sept13	290.83	226.41	1175.33
Sept14	290.88	223.84	1172.53
Sept17	289.34	217.88	1156.05
Sept18	290.91	218.24	1161.22
Sept19	291.44	216.64	1158.78

### Prices in September 2018

#### Problem: Input a pandas Series

Create vectors for each of the days in the Section ?? named sep\_xx where xx is the numeric date. For example,

```
import pandas as pd

sep_04 = pd.Series([289.81,228.36,1197.00], index=["SPY", "AAPL", "GOOG"]);
```

Using the ticker names as the index of each series

### Problem: Create a Vector of Dates

Use the pandas function `pd.to_datetime` to convert a list of string dates to a pandas `DateTimeIndex`, which can be used to set dates in other arrays.

For example, the first two dates are

```
import pandas as pd

dates_2 = pd.to_datetime(["4-9-2018", "5-9-2018"])
print(dates_2)
```

which produces

```
DatetimeIndex(["2018-04-09", "2018-05-09"], dtype="datetime64[ns]", freq=None)
```

Create a vector containing all of the dates in the table.

### Problem: Input a Series with Dates

Create vectors for each of the ticker symbols in Section ?? named `spy`, `aapl` and `goog`, respectively. Use the variable `dates` that you created in the previous step as the index.

For example

```
goog = pd.Series([1197.00, 1186.48, 1171.44, ...], index=dates)
```

Set the name of each series as the series' ticker.

### Problem: Create a DataFrame

Create a `DataFrame` named `prices` containing Section ??. Set the column names equal to the ticker and set the index to `dates`.

```
prices = pd.DataFrame([[289.81, 228.36, 1197.00], [289.03, 226.87, 1186.48]],
                      columns = ["SPY", "AAPL", "GOOG"], index=dates_2)
```

Save the price data

This block saves prices to a HDF file for use in later lessons. The function used to save the data is covered in a later lesson.

This function uses some sophisticated features of Python. Do not worry if it is unclear at this point.

```
# Setup: Save prices, goog and sep_04 into a single file for use in other lessons

# Only run if prices has been defined
if "prices" in globals():
    import pandas as pd
    dates = pd.Series(dates)
    variables = ["sep_04", "sep_05", "sep_06", "sep_07", "sep_10", "sep_11",
```

```

        "sep_12", "sep_13", "sep_14", "sep_17", "sep_18", "sep_19",
        "spy", "goog", "aapl", "prices", "dates"]
with pd.HDFStore("data/dataframes.h5", mode="w") as h5:
    for var in variables:
        h5.put(var, globals()[var])

```

## Exercises

### Exercise: Creating DataFrames

Turn the table below into a DataFrame where the index is set as the index and the column names are used in the DataFrame.

index	Firm	Profit
A	Alcoa	3,428
B	Berkshire	67,421
C	Coca Cola	197.4
D	Dannon	-342.1





## Lesson 5

# Constructing DataFrames from Series

This lesson introduced method to construct a DataFrame from multiple Series.

This first block loads the variables created in an earlier lesson. A later lesson will cover loading and saving data.

```
# Setup: Load data created in an earlier lesson

import pandas as pd

hdf_file = "data/dataframes.h5"

sep_04 = pd.read_hdf(hdf_file, "sep_04")
sep_05 = pd.read_hdf(hdf_file, "sep_05")
sep_06 = pd.read_hdf(hdf_file, "sep_06")
sep_07 = pd.read_hdf(hdf_file, "sep_07")
sep_10 = pd.read_hdf(hdf_file, "sep_10")
sep_11 = pd.read_hdf(hdf_file, "sep_11")
sep_12 = pd.read_hdf(hdf_file, "sep_12")
sep_13 = pd.read_hdf(hdf_file, "sep_13")
sep_14 = pd.read_hdf(hdf_file, "sep_14")
sep_17 = pd.read_hdf(hdf_file, "sep_17")
sep_18 = pd.read_hdf(hdf_file, "sep_18")
sep_19 = pd.read_hdf(hdf_file, "sep_19")

spy = pd.read_hdf(hdf_file, "spy")
aapl = pd.read_hdf(hdf_file, "aapl")
goog = pd.read_hdf(hdf_file, "goog")

dates = pd.to_datetime(pd.read_hdf(hdf_file, "dates"))

prices = pd.read_hdf(hdf_file, "prices")
```

### Problem: Construct a DataFrame from rows

Create a DataFrame named `prices_row` from the row vectors previously entered such that the results are identical to `prices`. For example, the first two days worth of data are:

```
dates_2 = pd.to_datetime(["1998-09-04", "1998-09-05"])
prices_row = pd.DataFrame([sep_04, sep_05])
# Set the index after using concat to join
prices_row.index = dates_2
```

Verify that the DataFrame identical by printing the difference with `prices`

```
print(prices_row - prices)
```

### Problem: Construct a DataFrame from columns

Create a DataFrame named `prices_col` from the 3 column vectors entered such that the results are identical to `prices`.

*Note:* `.T` transposes a 2-d array since DataFrame builds the array by rows.

Verify that the DataFrame identical by printing the difference with `prices`

### Problem: Construct a DataFrame from a dictionary

Create a DataFrame named `prices_dict` from the 3 column vectors entered such that the results are identical to `prices`

Verify that the DataFrame identical by printing the difference with `prices`

## Exercises

### Exercise: Create a DataFrame from rows

Use the three series populated below to create a DataFrame using each as a row.

**Note:** Notice what happens in the resulting DataFrame since one of the Series has 4 elements while the others have 3.

```
# Setup: Data for the Exercises
import pandas as pd
index = ["Num", "Let", "Date"]
a = pd.Series([1, "A", pd.Timestamp(2018,12,31)], name="a", index=index)
b = pd.Series([2, "B", pd.Timestamp(2018,12,31)], name="b", index=index)
index = ["Num", "Let", "Date", "Float"]
c = pd.Series([3, "C", pd.Timestamp(2018,12,31), 3.0], name="c", index=index)
```

### Exercise: Build a DataFrame from Columns

Build a DataFrame from the three series where each is used as a column.

## Lesson 6

# Methods and Functions

This lesson covers:

- Calling functions with more than one input and output
- Calling functions when some inputs are not used

Read the data in momentum.csv and creating some variable. This cell uses some magic to automate repeated typing.

```
# Setup: Load the momentum data
import pandas as pd

momentum = pd.read_csv("data/momentum.csv", index_col="date", parse_dates=True)

print(momentum.head())

mom_01 = momentum["mom_01"]
mom_10 = momentum["mom_10"]
```

This data set contains 2 years of data on the 10 momentum portfolios from 2016–2018. The variables are named mom\_XX where XX ranges from 01 (work return over the past 12 months) to 10 (best return over the past 12 months).

### Problem: Calling Methods

Get used to calling methods by computing the mean, standard deviation, skewness, kurtosis, max, and min.

Use the DataFrame functions mean, std, skew and kurt, min and max to print the values for mom\_01.

In the second cell, call describe, a method that summarizes Series and DataFrames on mom\_01.

### Problem: Use NumPy and SciPy functions

Use the NumPy functions mean, std, min, max and the SciPy stats functions skew and kurtosis to produce the same output.

### Problem: Calling Functions with 2 Outputs

Some useful functions return 2 or more outputs. One example is `np.linalg.slogdet` computes the signed log determinant of a square array. It returns two output, the sign and the log of the absolute determinant. Use this function to compute the sign and log determinant of the 2 by 2 array:

```
1 2
2 9
```

### Problem: Calling Functions with 2 Inputs

Many functions take two or more inputs. Like outputs, the inputs are simply listed in order separated by commas. Use `np.linspace` to produce a series of 11 points evenly spaced between 0 and 1.

```
np.linspace(start, stop, num=50, endpoint=True, retstep=False, dtype=None, axis=0)
```

### Problem: Calling Functions using Keyword Arguments

Many functions have optional arguments. You can see these in a docstring since optional arguments take the form `variable=default`. For example, see the help for `scipy.special.comb`, which has the function signature

```
comb(N, k, exact=False, repetition=False)
```

This tells us that `N` and `k` are required and that the other 2 inputs can be omitted if you are happy with the defaults. However, if we want to change some of the optional inputs, then we can directly use the inputs name in the function call.

Compute the number of distinct combinations of 5 objects from a set of 10.

Compute the total number of combinations allowing for repetition using the `repetition=True` keyword argument.

Compute the number of combinations using the exact representation using only positional arguments for all 3 inputs. Repeat using the keyword argument for `exact`.

### Problem: Function Help

Explore the help available for calling functions ? operator. For example,

```
import scipy.stats as stats

stats.kurtosis?
```

opens a help window that shows the inputs and output, while

```
help(stats.kurtosis)
```

shows the help in the console.

**Note:** VS Code does **not** support the ? form of help

**Problem: Use help with a method**

Use help to get the help for the kurt method attached to momentum.

**Exercises****Exercise: Use info**

Use the info method on momentum to get information about this DataFrame.

**Exercise: Compute the day-by-day mean**

Compute the day-by-day mean return of the portfolios in the momentum DataFrame using the axis keyword argument. Use head and tail to show the first 5 rows and last 5 rows

**Exercise: Compute the standard deviation of mean returns**

Compute the standard deviation of the mean returns by chaining methods.

**Exercise: Compute the average standard deviation**

Compute the mean standard deviation as:

$$\sqrt{N^{-1} \sum_{i=1}^N V[r_i]}$$

where  $V[r_i]$  is the variance of portfolio  $i$ .



## Lesson 7

# Custom Functions

This lesson covers:

- Writing a custom function

### Problem: Writing a Custom Function

Custom functions will play an important role later in the course when estimating parameters. Construct a custom function that takes two arguments, mu and sigma2 and computes the likelihood function of a normal random variable.

$$f(x; \mu, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(x - \mu)^2}{2\sigma^2}\right)$$

Use def to start the function and compute the likelihood of:

$$x = 0, \mu = 0, \sigma^2 = 1.$$

The text in the triple quotes is the docstring which is optional.

## Exercises

### Exercise: Custom Function

Write a function named summary\_stats that will take a single input, x, a DataFrame and return a DataFrame with 4 columns and as many rows as there were columns in the original data where the columns contain the mean, standard deviation, skewness and kurtosis of x.

Check your function by running

```
summary_stats(momentum)
```

```
# Setup: Load the momentum data
import pandas as pd
momentum = pd.read_csv("data\momentum.csv", index_col="date", parse_dates=True)
```

Test your function using the momentum data in the next cell.

### Exercise: Custom Function

Change your previous function to return 4 outputs, each a pandas Series for the mean, standard deviation, skewness, and the kurtosis.

Returning multiple outputs uses the syntax

```
return w, x, y, z
```

Test your function using the momentum data.

Test your function using the momentum data in the next cell.



## Lesson 8

# Using DataFrames

This lesson introduces:

- Computing returns (percentage change)
- Basic mathematical operations on DataFrames

This first cell load data for use in this lesson.

```
# Setup: Load prices
import pandas as pd
prices = pd.read_hdf("data/dataframes.h5", "prices")
sep_04 = pd.read_hdf("data/dataframes.h5", "sep_04")
goog = pd.read_hdf("data/dataframes.h5", "goog")
```

### Problem: Compute Returns

Compute returns using

```
returns = prices.pct_change()
```

which computes the percentage change.

Additionally, extract returns for each name using

```
spy_returns = returns["SPY"]
```

### Problem: Compute Log Returns

```
import numpy as np

log_returns = np.log(prices).diff()
```

first difference of the natural log of the prices. Mathematically this is  $r_t = \ln(P_t) - \ln(P_{t-1}) = \ln\left(\frac{P_t}{P_{t-1}}\right) \approx \frac{P_t}{P_{t-1}} - 1$ .

## 8.1 Basic Mathematical Operations

Operation	Symbol	Precedence
Parentheses	()	4
Exponentiation	**	3
Multiplication	*	2
Division	/	2
Floor division	//	2
Modulus	%	2
Matrix multiplication	@	2
Addition	+	1
Subtraction	-	1

**Note:** Higher precedence operators are evaluated first, and ties are evaluated left to right.

### Problem: Scalar Operations

1. Add 1 to all returns
2. Square the returns
3. Multiply the price of Google by 2.
4. Extract the fractional return using floor division and modulus

### Problem: Addition of Series

Add the returns on SPY to those of AAPL

### Problem: Combining methods and mathematical operations

Using only basic mathematical operations compute the correlation between the returns on AAPL and SPY.

### Problem: Addition of DataFrames

Construct a DataFrame that only contains the SPY column from returns and add it to the return DataFrame

### Problem: Non-conformable math

Add the prices in sep\_04 to the prices of goog. What happens?

### Problem: Constructing portfolio returns

Set up a 3-element array of portfolio weights

$$w = \left( \frac{1}{3}, \frac{1}{3}, \frac{1}{3} \right)$$

and compute the return of a portfolio with weight  $\frac{1}{3}$  in each security.

## Exercises

### Exercise: Combine math with function

Add 1 to the output of `np.arange` to produce the sequence 1, 2, ..., 10.

### Exercise: Understand pandas math

Use the Series and DataFrame below to compute the sums

- `a+b`
- `a+c`
- `b+c`
- `a+b+c`

to understand how missing values are treated by pandas

```
# Setup: Data for exercise
import pandas as pd
import numpy as np

rs = np.random.RandomState(19991231)

idx = ["A", "a", "B", 3]
columns = ["A", 1, "B", 3]
a = pd.Series([1, 2, 3, 4], index=idx)
b = pd.Series([10, 9, 8, 7], index=columns)
values = rs.randint(1, 11, size=(4, 4))
c = pd.DataFrame(values, columns=columns, index=idx)
```

### Exercise: Math with duplicates

Add the Series `d` to `a` to see what happens with delays.

```
# Setup: Data for exercise

d = pd.Series([10, 101], index=["A", "A"])
```



## Lesson 9

# Common DataFrame methods

This lesson introduces the common DataFrame methods that we will repeatedly use in the course. This first cell load data for use in this lesson.

```
# Setup: Load prices
import pandas as pd
prices = pd.read_hdf("data/dataframes.h5", "prices")
sep_04 = pd.read_hdf("data/dataframes.h5", "sep_04")
goog = pd.read_hdf("data/dataframes.h5", "goog")
returns = prices.pct_change().dropna()
spy_returns = returns.SPY
aapl_returns = returns.AAPL
goog_returns = returns.GOOG
```

### Problem: Constructing portfolio returns

Compute the return of a portfolio with weight  $\frac{1}{3}$  in each security using multiplication (\*) and .sum().

**Note:** You need to use the axis keyword for the sum.

### Problem: Compute the Mean and Standard Deviation

Using the function mean, compute the mean of the three returns series one at a time. For example

```
goog_mean = goog_returns.mean()
```

Next, compute the mean of the matrix of returns using

```
retmean = returns.mean()
```

What is the relationship between these two? Repeat this exercise for the standard deviation (std()).

### Problem: Compute Correlation

Compute the correlation of the matrix of returns (corr()).

### Problem: Summing all elements

Compute the sum of the columns of returns using `.sum()`. How is this related to the mean computed in the previous step?

### Problem: Maximum and Minimum Values

Compute the minimum and maximum values of the columns of returns using the `min()` and `max()` commands.

### Problem: Rounding Up, Down and to the Closest Integer

Rounding up is handled by `ceil`, rounding down is handled by `floor` and rounding to the closest integer is handled by `round`. Try all of these commands on 100 times returns. For example,

```
rounded = (100*returns).round()
```

Use `ceil` and `floor` to round up and down, respectively.

## Exercises

### Exercise: Compute Quantiles

Compute the 5%, 25%, 50%, 75% and 95% quantiles of momentum using the `quantile` method.

```
# Setup: Load data
import pandas as pd
momentum = pd.read_csv("data/momentum.csv", index_col="date", parse_dates=True)
mom_10 = momentum.mom_10
```

### Exercise: Sorting

Use `sort_values` to sort momentum by the column `mom_10`. Verify that the sort was successful by looking at the minimum of a diff.

### Exercise: Sort Descending

Use `sort_values` to sort momentum by the column `mom_10` using a descending sort (see the help for `sort_values`). Verify the sort worked by looking at the maximum of a diff.

### Exercise: Get Number of Elements

Use the `shape` property to get the number of observations in momentum. Use it again to get the number of columns.

**Exercise: Use shift to Compute Returns**

Compute the percentage change using only `shift`, division (`/`) and subtraction (`-`) on the Series `mom_10`. Verify that your result matches what `pct_change` produces.





## Lesson 10

# Accessing Elements in DataFrames

This lesson covers:

- Assessing specific elements in Pandas Series and DataFrames

Accessing elements in an array or a DataFrame is a common task. To begin this lesson, clear the workspace set up some vectors and a  $5 \times 5$  array. These vectors and matrix will make it easy to determine which elements are selected by a command.

Start by creating 2 DataFrame and 2 Series. Define `x=np.arange(24).reshape(5,5)` which is a 5 by 5 array and `y=np.arange(5)` which is a 5-element 1-d array. We need:

- `x_df`: A default DataFrame containing `x`
- `x_named`: A DataFrame containing `x` with index "r0", "r1", ..., "r4" and columns "c0", "c1", ... "c4".
- `y_s`: A default Series containing `y`
- `y_named`: A Series containing `y` that has the index "r0", "r1", ..., "r4"

### Problem: Selecting a row by name

Select the 2nd row of `x_name` using `.loc`.

### Problem: Selecting a column by name

Select the 2nd columns of `x_name` using both `[]` and `.loc`.

### Problem: Selecting a elements of a Series by name

Select the 2nd element of `y_name` using both `[]` and `loc`.

### Problem: Selecting rows and columns by name

Select the 2nd and 4th rows and 1st and 3rd columns of `x_name`.

**Problem: DataFrame selection with default index and column names**

Select the 2nd and 4th rows and 1st and 3rd columns of `x_df`.

**Problem: Series selection with the default index**

Select the final element in `y_s`

**Problem: Subseries selection**

Select the subseries of `y_named` and `y_s` containing the first, fourth and fifth element.

Load the data in `momentum.csv`.

```
# Setup: Load the momentum data

import pandas as pd

momentum = pd.read_csv("data/momentum.csv", index_col="date", parse_dates=True)
momentum.head()
```

**Problem: Selecting data on a single day**

Select returns on February 16, 2016.

**Problem: Selecting data in a single month**

Select return in March 2016.

**Problem: Selecting data in a single year**

Select return in 2016.

**Problem: Selecting data in a date range**

Select returns between May 1, 2016, and June 15, 2016.

**Exercises****Exercise: Subset time-series**

Select the data for May 2017 for momentum portfolios 1 and 10.

**Exercise: Select using Months**

Using a slice of `YYYY-MM`, select the returns for momentum portfolio 5 in the final 6 months of 2016 as Series

**Exercise: Ensure DataFrame**

Repeat the previous problem but ensure the selection is a DataFrame.



# Lesson 11

## Accessing Elements in NumPy Arrays

This lesson covers:

- Accessing specific elements in NumPy arrays

Accessing elements in an array or a DataFrame is a common task. To begin this lesson, clear the workspace set up some vectors and a  $5 \times 5$  array. These vectors and matrix will make it easy to determine which elements are selected by a command.

Using `arange` and `reshape` to create 3 arrays:

- 5-by-5 array `x` containing the values `0,1,...,24`
- 5-element, 1-dimensional array `y` containing `0,1,...,4`
- 5-by-1 array `z` containing `0,1,...,4`

### 11.1 Zero-based indexing

Python indexing is 0 based so that the first element has position 0, the second has position 1 and so on until the last element has position  $n - 1$  in an array that contains  $n$  elements in total.

#### **Problem: Scalar selection**

Select the number 2 in all three, `x`, `y`, and `z`.

**Question:** Which index is rows and which index is columns?

#### **Problem: Scalar selection of a single row**

Select row 2 in `x` and `z` using a single integer value.

**Question:** What is the dimension of `x` and the second row of `x`

#### **Problem: Slice selection of a single row**

Use a slice to select the 2nd row of `x` and the 2nd element of `y` and `z`.

**Question:** What are the dimension selections?

**Problem: List selection of a single row**

Use a list to select the 2nd row of x and the 2nd element of y and z.

**Question:** What are the dimension selections?

**Problem: Selecting a single Column**

Select the 2nd column of x using a scalar integer, a slice and a list.

**Question:** What the the dimensions of the selected elements?

**Problem: Selecting a block of specific columns**

Select the 2nd and 3rd columns of x using a slice.

**Problem: Selecting a block of specific rows**

Select the 2nd and 4th rows of x using both a slice and a list.

**Problem: Selecting a block of specific rows and columns**

Combine these be combined to select columns 2 and 3 and rows 2 and 4.

**Problem: Use ix\_ to select rows and columns using lists**

Use ix\_ to select the 2nd and 4th rows and 1st and 3rd columns of x.

**Problem: Convert a DataFrame to a NumPy array**

Use .to\_numpy to convert a DataFrame to a NumPy array.

```
# Setup: Create a DataFrame
import pandas as pd
import numpy as np

names = ["a", "b", "c", "d", "e"]
x = np.arange(25).reshape((5,5))
x_df = pd.DataFrame(x, index=names, columns=names)
print(x_df)
```

**Problem: Use np.asarray to convert to an array**

Use np.asarray to convert a DataFrame to a NumPy array.

## Exercises

### Exercise: Block selection

Select the second and third rows of `a` and the first and last column. Use at least three different methods including all slices, `np.ix_`, and mixed slice-list selection.

```
# Setup: Data for Exercises

import numpy as np
rs = np.random.RandomState(20000214)
a = rs.randint(1, 10, (4,3))
b = rs.randint(1, 10, (6,4))

print(f"a = \n {a}")
print()
print(f"b = \n {b}")
```

### Exercise: Row Assign

Assign the first three elements of the first row of `b` to `a`.

**Note** Assignment sets one selected block in one array equal to another block.

```
x[0:2,0:3] = y[1:3,1:4]
```

### Exercise: Block Assign

Assign the block consisting the first and third columns and the second and last rows of `b` to the last two rows and last two columns of `a`





## Lesson 12

# Numeric Indexing of DataFrames

This lesson covers:

- Accessing specific elements in DataFrames using numeric indices

Accessing elements in a DataFrame is a common task. To begin this lesson, clear the workspace set up some vectors and a  $5 \times 5$  array. These vectors and matrix will make it easy to determine which elements are selected by a command.

Begin by creating:

- A 5-by-5 DataFrame `x_df` containing `np.arange(25).reshape((5,5))`.
- A 5-element Series `y_s` containing `np.arange(5)`.
- A 5-by-5 DataFrame `x_named` that is `x_df` with columns “c0”, “c1”, ..., “c4” and rows “r0”, “r1”, ..., “r4”.
- A 5-element Series `y_named` with index “r0”, “r1”, ..., “r4”.

### Problem: Picking an Element out of a DataFrame

Using double index notation, select the (0,2) and the (2,0) element of `x_named`.

### Problem: Select Elements from Series

Select the 2nd element of `y_named`.

### Problem: Selecting Rows as Series

Select the 2nd row of `x_named` using the colon (`:`) operator.

### Problem: Selecting Rows as DataFrames

1. Select the 2nd row of `x_named` using a slice so that the selection remains a DataFrame.
2. Repeat using a list of indices to retain the DataFrame.

**Problem: Selecting Entire Columns as Series**

Select the 2nd column of `x_named` using the colon `(:)` operator.

**Problem: Selecting Single Columns as DataFrames**

Select the 2nd column of `x_named` so that the selection remains a `DataFrame`.

**Problem: Selecting Specific Columns**

Select the 2nd and 3rd columns of `x_named` using a slice.

**Problem: Select Specific Rows**

Select the 2nd and 4th rows of `x_named` using a slice. Repeat the selection using a list of integers.

**Problem: Select arbitrary rows and columns**

Combine the previous selections to select columns 2 and 3 and rows 2 and 4 of `x_named`.

**Note:** This is the only important difference with NumPy. Arbitrary row/column selection using `DataFrame.iloc` is simpler but less flexible.

**Problem: Mixed selection**

Select the columns `c1` and `c2` and rows 0, 2 and 4.

**Problem: Mixed selection 2**

Select the rows `r1` and `r2` and columns 0, 2 and 4.

**Exercises****Exercise: Select fixed length block**

Compute the mean return of the momentum data in the first 66 observations and the last 66 observations.

```
# Setup: Load the momentum data

import pandas as pd

momentum = pd.read_csv("data/momentum.csv", index_col="date", parse_dates=True)
momentum.head()
```

**Exercise: Compute values using fraction of sample**

Compute the correlation of momentum portfolio 1, 5, and 10 in the first half of the sample and in the second half.

## Lesson 13

# for Loops

This lesson covers:

- for loops
- Nested loops

### Problem: Basic For Loops

Construct a for loop to sum the numbers between 1 and N for any N. A for loop that does nothing can be written:

```
n = 10
for i in range(n):
    pass
```

### Problem: Compute a compound return

The compound return on a bond that pays interest annually at rate  $r$  is given by  $c r_t = \prod_{i=1}^T (1+r) = (1+r)^T$ . Use a for loop compute the total return for £100 invested today for  $1, 2, \dots, 10$  years. Store this variable in a 10 by 1 vector  $cr$ .

### Problem: Simulate a random walk

(Pseudo) Normal random variables can be simulated using the command `np.random.standard_normal(shape)` where `shape` is a tuple (or a scalar) containing the dimensions of the desired random numbers. Simulate 100 normals in a 100 by 1 vector and name the result  $e$ . Initialize a vector  $p$  containing zeros using the function `zeros`. Add the 1st element of  $e$  to the first element of  $p$ . Use a for loop to simulate a process  $y_i = y_{i-1} + e_i$ . When finished plot the results using

```
%matplotlib inline

import matplotlib.pyplot as plt
plt.rc('figure', figsize=(16,9))
```

```
plt.plot(y)
```

### Problem: Nested Loops

Begin by loading momentum data used in an earlier lesson. Compute a 22-day moving-window standard deviation for each of the columns. Store the value at the end of the window.

When finished, plot the annualized percentage standard deviations using `plt.plot(100 * np.sqrt(252) * std_dev)`.

```
# Setup: Load the momentum data

import pandas as pd
momentum = pd.read_csv("data/momentum.csv", index_col="date", parse_dates=True)
momentum = momentum / 100 # Convert to numeric values from percentages
```

## Exercises

### Exercise

1. Simulate a 1000 by 10 matrix consisting of 10 standard random walks using both nested loops and `np.cumsum`.
2. Plot the results.

### Question to think about

If you rerun the code in this Exercise, do the results change? Why?

### Exercise: Compute Drawdown

Using the momentum data, compute the maximum drawdown over all 22-day consecutive periods defined as the smallest cumulative produce of the gross return  $(1+r)$  for 1, 2, .., 22 days.

Finally, compute the mean drawdown for each of the portfolios.

## Lesson 14

# Logical Operators

This lesson covers:

- Basic logical operators
- Compound operators

```
# Setup: Reproducible random numbers

import numpy as np
rs = np.random.RandomState(20000101)
```

### Problem: Basic Logical Statements

Create the variables (in order)

- `x` as `rs.sample()`, a uniform on  $[0, 1)$
- `y` as `rs.standard_normal()`, a standard normal  $(N(0, 1))$
- `z` as `rs.randint(1, 11)`, a uniform random integer on  $[1, 2, \dots, 10]$

Check whether each of these are above their expected value.

### Problem: Using comparison operators

1. Check if `z` is 7
2. Check if `z` is not 5
3. Check if `z` is greater than or equal to 9

### Problem: Combining booleans

1. Determine if  $2 \leq z < 8$
2. Determine if  $z < 2 \cup z \geq 8$  using `or`
3. Rewrite 2 using `not` and your result from 1.

## Exercises

```
# Setup: Data for Exercise
import numpy as np
rs = np.random.RandomState(19991213)

# Like range, lower included, upper excluded
# u in (0, 1, 2, ..., 5)
u = rs.randint(0, 6)
# v in (-2, -1, 0, 1, 2)
v = rs.randint(-2, 3)
```

### Exercise

Is the product  $uv$  0 and only one of  $u$  and  $v$  is 0?

### Exercise

Write three logical statements that will determine if  $0 \leq u \leq 2$  and  $0 \leq v \leq 2$ .

## Lesson 15

# Boolean Arrays

This lesson covers:

- Creating Boolean arrays
- Combining Boolean arrays
- all and any

Begin by loading the data in momentum.csv.

```
# Setup: Load the momentum data

import numpy as np
import pandas as pd

momentum = pd.read_csv("data/momentum.csv", index_col="date", parse_dates=True)

print(momentum.head())

mom_01 = momentum["mom_01"]
mom_10 = momentum["mom_10"]
mom_05 = momentum["mom_05"]
```

### Problem: Boolean arrays

For portfolios 1 and 10, determine whether each return is  $< 0$  (separately).

### Problem: Combining boolean arrays

Count the number of times that the returns in both portfolio 1 and portfolio 10 are negative. Next count the number of times that the returns in portfolios 1 and 10 are both greater, in absolute value, than 2 times their respective standard deviations.

### Problem: Combining boolean arrays

For portfolios 1 and 10, count the number of times either of the returns is  $< 0$ .

**Problem: Count the frequency of negative returns**

What percent of returns are negative for each of the 10 momentum portfolios?

**Problem: Use any to find large losses**

Use any to determine if any of the 10 portfolios experienced a loss greater than -5%.

Use all and negation to do the same check as any.

**Exercises****Exercise: all and any**

Use all and sum to count the number of days where all of the portfolio returns were negative. Use any to compute the number of days with at least 1 negative return and with no negative returns (Hint: use negation (~ or logical\_not)).

**Exercise: Count Extreme Days**

Count the number of days where each of the portfolio returns is less than the 5% quantile for the portfolio. Also report the fraction of days where all are in their lower 5% tail.



## Lesson 16

# Boolean Selection

This lesson covers:

- Boolean selection
- where

Begin by loading the data in momentum.csv.

```
# Setup: Load the momentum data

import numpy as np
import pandas as pd

momentum = pd.read_csv("data/momentum.csv", index_col="date", parse_dates=True)

print(momentum.head())
```

### Problem: Selecting rows with boolean conditions

Select the rows in momentum where all returns on a day are negative.

### Problem: Selecting rows

Select the rows in momentum where 50% or more of the returns on a day are negative.

### Problem: Selecting columns

Select the columns in momentum what have the smallest and second smallest average returns.

### Problem: Selecting rows and columns

Select the returns for the column with the single most negative return on days where all of the returns are negative.

### Problem: Selecting Elements using Logical Statements

For portfolio 1 and portfolio 10 compute the correlation when both returns are negative and when both are positive.

```
# Setup: Reproducible random numbers

rs = np.random.RandomState(19991231)
x = rs.randint(1, 11, size=(10,3))
x
```

**Problem: Select the columns of x that means  $\geq E[x]$**

**Problem: Select the rows of x that means  $\geq E[x]$**

**Problem: Select the rows and column of x where both have means  $< E[x]$**

**Problem: Using where**

Use where to select the index of the elements in portfolio 5 that are negative. Next, use the where command in its two output form to determine which elements of the portfolio return matrix are less than -2%.

## Exercises

**Exercise: Select the Most Volatile Portfolio**

Select the column in momentum that has the highest standard deviation.

**Exercise: Select the High Kurtosis Portfolios**

Select the columns that have kurtoses above the median kurtosis.

**Exercise: Select**

Select the rows where all of the returns in the row are less than the 25% quantile for their portfolio.

**Note:** Comparisons between DataFrames and Series works like mathematical operations (+, -, etc.).

## Lesson 17

# Conditional Statements

- if-elif-else blocks

### Problem: Print value if negative

Draw a standard normal value using `np.random.standard_normal` and print the value if it is negative.

**Note:** Rerun the cell a few time to see different output.

### Problem: Print different messages based on value

Draw a standard normal value and print “Positive” if it is positive and “Negative” if not.

### Problem:

Draw a standard t random variable with 2 degrees of freedom using `np.random.standard_t(2)` and print “Negative Outlier” if less than -2, “Positive Outlier” if larger than 2, and “Inlier” if between -2 and 2.

## Exercises

### Exercise: Classify two points

Generate two standard normal values `x` and `y` using two calls to `rs.standard_normal()`. Use an if-elif-else clause to print the quadrant they are in. The four quadrants are upper right, upper left, lower left and lower right.

### Exercise: Generate a contaminated normal

Generate a uniform using `u = rs.sample()`. Using this value and an if-else clause, generate a contaminated normal which is a draw from a  $N(0, 1)$  ( $N(\mu, \sigma^2)$ ) if  $u < 0.95$  or a draw from a  $N(0, 10)$  otherwise. Use `rs.normal` to generate the normal variable.



## Lesson 18

# Logic and Loops

This lesson covers:

- Mixing logic and loops

```
# Setup: Load the momentum data

import pandas as pd

momentum = pd.read_csv("data/momentum.csv", index_col="date", parse_dates=True)

mom_01 = momentum.mom_01
print(momentum.head())
```

### Problem: Logical Statements and for Loops

Use a for loop along with an if statement to simulate an asymmetric random walk of the form

$$y_i = y_{i-1} + e_i + I_{[e_i < 0]} e_i$$

where  $I_{[e_i < 0]}$  is known as an indicator variable that takes the value 1 if the statement in brackets is true. Plot  $y$ .  $e$  is a standard normal shock. Use `cumsum` to simulate a symmetric one ( $z$ ), and plot the two using the code in the cell below.

Plot the two random walks using the code. We will cover data visualization in a later lesson.

```
%matplotlib inline
import matplotlib.pyplot as plt
plt.plot(y)
plt.plot(z)
plt.legend(["y", "z"])
```

### Problem: Simulate the asymmetric random walk without an if-then

Use boolean multiplication to simulate the same random walk without using an if-then statement.

```
# Setup: Plot the data
%matplotlib inline
```

### Problem: Combining flow control

For momentum portfolios 1 and 10, compute the length of the runs in the series. In pseudo code,

- Start at  $i=1$  and define  $\text{run}(1) = 1$
- For  $i$  in  $2, \dots, T$ , define  $\text{run}(i) = \text{run}(i-1) + 1$  if  $\text{sgn}(r_i) = \text{sgn}(r_{i-1})$  else 1.

You will need to use `len` and `zeros`.

1. Compute the length longest run in the series and the index of the location of the longest run. Was it positive or negative?
2. How many distinct runs lasted 5 or more days?

Plot the runs using

```
%matplotlib inline

import matplotlib.pyplot as plt
plt.plot(run)
```

## Exercises

### Exercise: Simulate a Process with Heteroskedasticity

Simulate 100 observations of a time series with heteroskedasticity that follows a random walk of the form:

$$y_t = y_{t-1} + \sigma_t \epsilon_t$$

where  $\epsilon_t \sim N(0, 1)$ ,  $y_0 = 0$  and  $\sigma_t$  is:

- 0.5 if the 0 of the past 3 shocks are negative
- 1 if 1 of the past 3 shocks are negative
- 2 if 2 of the past 3 shocks are negative
- 6 if 3 of the past 3 shocks are negative

Plot the result.

### Notes

- When generating the first 3 values, treat  $\epsilon_{-1}$ ,  $\epsilon_{-2}$  and  $\epsilon_{-3}$  as 0 (non-negative).
- Re-run the simulation to see different paths.

## Lesson 19

# Importing Data

This lesson covers:

- Importing data
- Converting dates

### Problem: Reading in data with Dates

Read in the files `GS10.csv` and `GS10.xls` which have both been downloaded from [FRED](#).

### Problem: Converting Dates

1. Load the CSV file without converting the dates in `read_csv`.
2. Convert the date column, remove it from the DataFrame, and set it as the index.

## Exercises

### Exercise: Selectively Load Columns

1. Load the data in `data/fred-md.csv` in the columns `sasdate`, `RPI` and `INDPRO` using the `usecols` keyword.
2. Remove the first row by selecting the second to the end.
3. Convert `sasdate` to dates
4. Set `sasdate` as the index and remove it from the DataFrame.

### Exercise: Load and Merge multiple Sheets

1. Load the data on the sheet “Long Mat” in the Excel file “`data/exercise.xlsx`”. These are 10 and 20 year constant maturity yields.
2. Load the data on the sheet “Short Mat” in the Excel file “`data/exercise.xlsx`”. These are 1 and 3 year constant maturity yields.
3. Combine the columns in the two DataFrames by creating a dictionary of the keys in each with the values equal to the column names.





## Lesson 20

# Saving and Exporting Data

This lesson covers:

- Saving and reloading data

This first block loads the data that was used in the previous lesson.

```
# Setup: Load the data to use later
import pandas as pd

gs10_csv = pd.read_csv("data/GS10.csv", index_col="DATE", parse_dates=True)
gs10_excel = pd.read_excel("data/GS10.xls", skiprows=10,
                           index_col="observation_date")
```

### Problem: Export to Excel

Export `gs10_csv` to the Excel file `gs10-exported.xlsx`.

### Problem: Export to CSV

Export `gs10_excel` to CSV.

### Problem: Export to HDF

Export both to a single HDF file (the closest thing to a “native” format in pandas).

### Problem: Import from HDF

Import the data saved as HDF and verify it is the same as the original data.

## Exercises

### Exercise: Import, export and verify

- Import the data in “data/fred-md.csv”

- Parse the dates and set the index column to “sasdate”
- Remove first row labeled “Transform:” (**Hint:** Transpose, del and transpose back, or use drop)
- Re-parse the dates on the index
- Remove columns that have more than 10% missing values
- Save to “data/fred-md.h5” as HDF
- Load the data into the variable reloaded and verify it is identical.

### Exercise: Looping Export

Export the columns RPI, INDPRO, and HWI from the FRED-MD data to "data/*variablename.csv*" so that, e.g., RPI is exported to data/RPI.csv:

**Note** You need to complete the previous exercise first (or at least the first 4 steps).

## Lesson 21

# Graphics: Line Plots

This lesson covers:

- Basic plotting
- Subplots
- Histograms
- Scatter Plots

Plotting in notebooks requires using a magic command, which starts with %, to initialize the plotting back-end.

```
# Setup
%matplotlib inline
```

Begin by loading the data in hf.h5. This data set contains high-frequency price data for IBM and MSFT on a single day stored as two Series. IBM is stored as “IBM” in the HDF file, and MSFT is stored as "MSFT".

### Problem: Basic Plotting

1. Plot the ibm series which contains the price of IBM.
2. Add a title and label the axes.
3. Add markers and remove the line.

### Problem: Subplot

Create a 2 by 1 subplot with the price of IBM in the top subplot and the price of MSFT in the bottom subplot.

### Problem: Plot with Dates

Use matplotlib to directly plot ibm against its index. This is a repeat of a previous plot but shows how to use the plot command directly.

## Exercises

### Exercise: Change seaborn

Produce a line plot of MSFT's price using seaborn's "whitegrid" style.

### Exercise: HLOC plot

Use the HLOC data to produce a plot of MSFT's 5 minute HLOC where there are no lines, high is demarcated using a green triangle, low is demarcated using a red downward pointing triangle, open is demarcated using a light grey leftward facing triangle and close is demarcated using a right facing triangle.

**Note** Get the axes from the first, plot, and reuse this when plotting the other series.

```
# Setup: Load data and create values
import pandas as pd

msft = pd.read_hdf("data/hf.h5", "MSFT")
msft_5min = msft.resample("300S")
high = msft_5min.max()
low = msft_5min.min()
open = msft_5min.first()
close = msft_5min.last()
```

## Lesson 22

# Graphics: Other Plots

This lesson covers:

- Histograms
- Scatter Plots

Plotting in notebooks requires using a magic command, which starts with %, to initialize the plotting backend.

```
# Setup
%matplotlib inline
```

Begin by loading the data in `hf.h5`. This data set contains high-frequency price data for IBM and MSFT on a single day stored as two Series. IBM is stored as “IBM” in the HDF file, and MSFT is stored as “MSFT”.

### Problem: Histogram

Produce a histogram of MSFT 1-minute returns (Hint: you have to produce the 1-minute Microsoft returns first using `resample` and `pct_change`).

### Problem: Scatter Plot

Scatter the 5-minute MSFT returns against the 5-minute IBM returns.

*Hint:* You will need to create both 5-minute return series, merge them, and then plot using the combined DataFrame.

### Problem: Saving plots

Save the previous plot to PNG and PDF.

## Exercises

### Exercise: Visualize 5 and 10 minute returns

Produce a 2 by 1 subplot with a histogram of the 5-minute returns of IBM in the top panel and 10-minute returns of IBM in the bottom. Set an appropriate title on each of the 2 plots.

**Exercise: Export the result of the previous exercise to JPEG and PDF**

## **22.1 Exercise: Plot histograms and a scatter plot**

Produce a 2 by 2 subplot with:

- Create a square figure with a size of 10 by 10 using `plt.rc`
- Histograms of IBM and MSFT on the diagonals
- Scatter plots on the off-diagonals where the x and y line up with the histogram on the diagonal.
- Set the limits of the scatter plots to match the appropriate histogram x and y limit.
- Clean up the plot using `tight_layout`

**Exercise: Use pandas plotting tools**

Use `pandas.plotting.scatter_matrix` to produce a similar plot to the previous exercise.

# Final Exam

This self-grading notebook serves as a final exam for the introductory course. If you have grasped the contents of the course, you should be able to complete this exam.

It is essential that you answer each cell by assigning the solution to `QUESTION_#` where `#` is the question number.

We will start with a warm-up question that is already answered.

## Question 0

Create a 3-element 1-dimensional array containing the values `[1,1,1]`

*Note:* This answer is not assessed.

```
# Setup: The solution is used as a model
import numpy as np

QUESTION_0 = np.ones(3)
```

## Question 1

Construct the correlation matrix

$$\begin{bmatrix} 1 & 0.2 & 0.5 \\ 0.2 & 1 & 0.8 \\ 0.5 & 0.8 & 1 \end{bmatrix}$$

as a NumPy array.

## Question 2

Construct the correlation matrix

$$\begin{bmatrix} 1 & 0.2 & 0.5 \\ 0.2 & 1 & 0.8 \\ 0.5 & 0.8 & 1 \end{bmatrix}$$

as a DataFrame with columns and index both equal to `['A', 'B', 'C']`.

### Question 3

Load the momentum data in the CSV file `momentum.csv`, set the column `date` as the index, and ensure that `date` is a `DateTimeIndex`.

### Question 4

Construct a `DataFrame` using the data loaded in the previous question that contains the returns from momentum portfolio 5 in March and April 2016.

### Question 5

What is the standard deviation of the data:

1, 3, 1, 2, 9, 4, 5, 6, 10, 4

**Note** Use 1 degree of freedom in the denominator.

### Question 6

Compute the correlation matrix of momentum portfolios 1, 4, 6, and 10 as a `DataFrame` where the index and columns are the portfolio names (e.g., `'mom_01'`) in the order listed above.

### Question 7

Compute the percentage of returns of each of the 10 momentum portfolios that are outside of the interval

$$[\hat{\mu} - \hat{\sigma}, \hat{\mu} + \hat{\sigma}]$$

where  $\hat{\mu}$  is the mean and  $\hat{\sigma}$  is the standard deviation computed using 1 dof. The returned variable must be a `Series` where the index is the portfolio names ordered from 1 to 10.

### Question 8

Import the data the data in the sheet `question 8` in `final-exam.xlsx` into a `DataFrame` where the index contains the dates and variable name is the column name.

### Question 9

Enter the `DataFrame` in the table below and save it to HDF with the key `'question9'`. The answer to this problem must be the full path to the hdf file. The values in index should be the `DataFrame`'s index.

index	data
A	6.0
E	2.7
G	1.6
P	3.1



**Note:** If you want to get the full path to a file saved in the current directory, you can use

```
import os

file_name = 'my_file_name'
full_path = os.path.join(os.getcwd(), file_name)
```

### Question 10

Compute the cumulative return on a portfolio the longs mom\_10 and shorts mom\_01. The first value should be  $1 + \text{mom\_10.iloc}[0] - \text{mom\_01.iloc}[0]$ . The second cumulative return should be the first return times  $1 + \text{mom\_10.iloc}[1] - \text{mom\_01.iloc}[1]$ , and so on. The solution must be a Series with the name 'momentum\_factor' and index equal to the index of the momentum DataFrame.

**Note:** The data in the momentum return file is in percentages, i.e., a return of 4.2% is recorded as 4.2.

### Question 11

Write a function named QUESTION\_11 that take 1 numerical input x and returns:

- $\exp(x)$  if x is less than 0
- $\log(1 + x)$  if x is greater than or equal to 0

### Question 12

Produce a scatter plot of the momentum returns of portfolios 1 (x-axis) and 10 using only data in 2016. Set the x limits and y limits to be tight so that the lower bound is the smallest return plotted and the upper bound is the largest return plotted. Use the 'darkgrid' theme from seaborn. Assign the **figure** handle to QUESTION\_12.

### Question 13

Compute the excess kurtosis of daily, weekly (using Friday and the end of the week) and monthly returns on the 10 momentum portfolios using the pandas function kurt. The solution must be a DataFrame with the portfolio names as the index ordered from 1 to 10 and the sampling frequencies, 'daily', 'weekly', or 'monthly' as the columns (in order). When computing weekly or monthly returns from daily data, use the sum of the daily returns.

### Question 14

Simulate a random walk using 100 normal observations from a NumPy RandomState initialized with a seed of 19991231.

### Question 15

Defining

```
import numpy as np
```

```
cum_momentum = np.cumprod(1 + momentum / 100)
```

compute the ratio of the high-price to the low price in each month. The solution should be a DataFrame where the index is the last date in each month and the columns are the variables names.

### Question 16

Simulate 100 observations from the model

$$y_i = 0.2 + 1.2y_{i-1} - 0.2y_{i-2} + \epsilon_i$$

where  $\epsilon_i$  is a standard normal shock. Set  $y_0 = \epsilon_0$  and  $y_1 = \epsilon_0 + \epsilon_1$ . The solution should be a 1-d NumPy array with 100 elements. Use a RandomState with a seed value of 19991231.

### Question 17

What is the ratio of the largest eigenvalue to the smallest eigenvalue of the correlation matrix of the 10 momentum returns?

**Note:** This is called the condition number of a matrix and is a measure of how closely correlated the series are. You can compute the eigenvalues from the correlation matrix using `np.linalg.eigs`. See the help of this function for more details.

### Question 18

Write a function that takes a single input 'x' and return the string "The value of x is" and the value of x. For example, if x is 3.14, then the returned value should be "The value of x is 3.14". The function name must be QUESTION\_18.

### Question 19

Compute the percentage of days where all 10 returns are positive and subtract the percentage of days where all 10 momentum returns are negative on the same day.

### Question 20

Write the function QUESTION\_20 that will take a single input s, which is a string and will return a Series that counts the number of times each letter in s appears in s *without* regard to case. Do not include spaces. Ensure the Series returned as its index sorted.

**Hints:**

- Have a look at `value_counts` for a pandas Series.
- You can iterate across the letters of a string using

```
some_string = 'abcdefg'
for letter in some_string:
    do something with letter...
```

- `str.lower` can be used to get the lower case version of a string