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#include <iostream>
using namespace std;

int findMax(int a[], int arraySize){

    int max = a[arraySize-1];

    for (int i = arraySize-2; i >= 0; i--) This causes linear runtime, but is not the bottleneck.

        if(a[i] > max){
            max = a[i];
        }
    }

    return max;
}

int findCount(int a[], int arraySize){

    int count = 0;

    int max2 = findMax(a , arraySize);

    for(int i = 0; max2 >= 1; i++){

        max2 /= 10;

        count = i+1;

    }

    return count;
}

void Print(int a[], int arraySize){
    for(int i = 0; i < arraySize; i++){
        cout << a[i] << " ";
    }
}

void digitSort(int a[], int arraySize, int x){

    int digitcopy[10] = {0};

    int sorted[arraySize];

    for (int i = 0; i < arraySize; i++) This causes linear run time, and will be part of the bottleneck.

        digitcopy[(a[i]/x)%10]++;
    }

    for (int i = 1; i < 10; i++){
        digitcopy[i] += digitcopy[i-1];
    }
    for (int i = arraySize-1; i >= 0; i--) Linear run time once again, and causes part of the bottleneck.

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        sorted[digitcopy[(a[i]/x)%10] - 1] = a[i];
        digitcopy[(a[i]/x)%10]--;
    }
    for(int i = 0; i < arraySize; i++) Causes linear runtime yet again.
        a[i] = sorted[i];
    }
}

void Problem1Sort(int a[], int arraySize){

    int numReps = findCount(a, arraySize);

    int i = 0;

    for(int x = 1; x <= numReps; x *= 10){

        digitSort(a, arraySize, x);

        i++;

    }

}

```

The bottlenecking function in my radix sort is the digitSort function, which causes a runtime of $O(3N)$, which is essentially linear run time, as constants/coefficients do not get factored into the simplified runtime.

D. My sort is stable as I use strictly less than, meaning that duplicates will not be sorted with each other.

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    for (int i = 1; i < 10; i++){
        digitcopy[i] += digitcopy[i-1];
    }
    for(int i = arraySize-1; i >= 0; i--){ Linear run time once again, and causes part of the bottleneck.
        sorted[digitcopy[(a[i]/x)%10] - 1] = a[i];
        digitcopy[(a[i]/x)%10]--;
    }
    for(int i = 0; i < arraySize; i++){ Causes linear runtime yet again.
        a[i] = sorted[i];
    }
}

```

E. I was unable to get my algorithm to work using constant space, unfortunately. However, I know that using constant space would give the massive advantage in that the size of the array I am sorting wouldn't matter to the sort itself, meaning that if I'm sorting an array that takes half my memory, it will actually be sorted, unlike in a case where $O(N)$ space is used.