# Lab 3

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# 1 Output Files

### 1.1 Output File 1

Setting up the problem...0.021003 s

A: 1000 x 1000

B: 1000 x 1000

C: 1000 x 1000

Allocating device variables...0.173379 s
Copying data from host to device...0.004189 s
Launching kernel...0.008233 s
Copying data from device to host...0.004426 s

Copying data from device to host...0.004426 s Verifying results...TEST PASSED

Setting up the problem...0.081349 s

A: 2000 x 2000

B: 2000 x 2000

C: 2000 x 2000

Allocating device variables...0.182460 s
Copying data from host to device...0.017313 s
Launching kernel...0.060868 s
Copying data from device to host...0.012964 s
Verifying results...TEST PASSED

Setting up the problem...0.321950 s

A: 4000 x 4000

B: 4000 x 4000

C: 4000 x 4000

Allocating device variables...0.186792 s
Copying data from host to device...0.068122 s
Launching kernel...0.485511 s
Copying data from device to host...0.045862 s

#### Verifying results...TEST PASSED

Setting up the problem...1.289725 s

A: 8000 x 8000

B: 8000 x 8000

C: 8000 x 8000

Allocating device variables...0.184046 s
Copying data from host to device...0.274219 s
Launching kernel...3.888804 s
Copying data from device to host...0.182651 s
Verifying results...TEST PASSED

### 1.2 Output File 2

Setting up the problem...0.009253 s

A: 1000 x 500

B: 500 x 500

C: 1000 x 500

Allocating device variables...0.205076 s
Copying data from host to device...0.001798 s
Launching kernel...0.002227 s
Copying data from device to host...0.002273 s
Verifying results...TEST PASSED

Setting up the problem...0.031236 s

A: 2000 x 1000

B: 1000 x 1000

C: 2000 x 1000

Allocating device variables...0.186218 s
Copying data from host to device...0.006258 s
Launching kernel...0.016270 s
Copying data from device to host...0.007320 s
Verifying results...TEST PASSED

Setting up the problem...0.119207 s

A: 4000 x 2000

B: 2000 x 2000

C: 4000 x 2000

Allocating device variables...0.187957 s Copying data from host to device...0.024576 s Launching kernel...0.121746 s Copying data from device to host...0.022181 s Verifying results...TEST PASSED

Setting up the problem...0.481023 s

A: 8000 x 4000 B: 4000 x 4000 C: 8000 x 4000

Allocating device variables...0.186625 s
Copying data from host to device...0.102642 s
Launching kernel...0.971854 s
Copying data from device to host...0.098304 s
Verifying results...TEST PASSED

# 2 Performance Analysis

# 2.1 Square Matrices (n x n)

Execution Time (seconds) for Each Process							
Elements(nxn)	Setting Up	DeviceVar	Kernel	HostToDevice	DeviceToHost		
1000	0.021003	0.173379	0.008233	0.004189	0.004426		
2000	0.081349	0.182460	0.060868	0.017313	0.012964		
4000	0.321950	0.186792	0.485511	0.068122	0.045862		
8000	1.289725	0.184046	3.888804	0.274219	0.182651		

# 2.2 Rectangle Matrices $(A = m \times k \text{ and } B = k \times n)$

Execution Time (seconds) for Each Process							
Elements	Setting Up	DeviceVar	Kernel	HostToDevice	DeviceToHost		
(m,k,n)							
1000, 500, 500	0.009253	0.205076	0.002227	0.001798	0.002273		
2000, 1000, 1000	0.031236	0.186218	0.016270	0.006258	0.007320		
4000, 2000, 2000	0.119207	0.187957	0.121746	0.024576	0.022181		
8000, 4000, 4000	0.481023	0.186625	0.971854	0.102642	0.098304		

#### 2.3 Square Matrix Comparison Between Tiled vs Non-Tiled

Kernel Execution Times (seconds)					
Elements (n x n)	Tiled	Non-Tiled			
1000	0.008233	0.022178			
2000	0.060868	0.163624			
4000	0.485511	1.308468			
8000	3.888804	10.493221			

## 2.4 Tiled vs Non-Tiled Graphical Representation



#### 2.5 Comments

For the square matrices each process time followed a similar pattern except for the process of allocating of 'device variables'. The time taken to allocate device variables is approximately the same regardless of the number of elements. As the number of elements increase the time taken setting up the problem, launching the kernel, copying data from the host to the device and vice versa also increases. There is an observable direct proportional relationship between these processes and the number of elements. The same conclusion can be made for the rectangular matrices.

There is an exponential increase in the kernel execution times associated with the tiled and non-tiled. However the non-tiled line graph shows a sharp increase in kernel execution time as the number of elements increase. This can be seen by the large spike between 4000 and 8000 elements on the graph. The tiled line graph does not exhibit that spike, as the purpose of tiling is reduce the number of global memory accesses. The graph shows that tiling reduces the kernel execution time by approximately a factor of 2.7.

#### 3 Answers

## 3.1 C(i)

The execution of nvcc –ptxas-options="-v" kernel.cu revealed resource usage statistics which include 25 registers/thread, 2K (2048 bytes) of shared memory, 360 bytes of constant memory[0] and 4 bytes of constant memory[2]. There are obvious limits to the number of threads allocated to a single streaming processor as defined by hardware specifications. For the GeForce GTX 280 GPU that has a compute capability of 1.3 these specifications include: 512 threads/block, 16K shared memory/multiprocessor, 16K registers/multiprocessor, 8 blocks/multiprocessor, 1024 threads/multiprocessor and 124 registers/thread.

For this case, the block size is  $16 \times 16 = 256$  threads and therefore the number of blocks/multiprocessor would be 1024/256 = 4. However, (256 threads x 25 reg/thread x 4 blocks/multiprocessor) > 16K registers/multiprocessor. The number of registers per multiprocessor is a limiting factor and therefore only 2 blocks can run on a single microprocessor which would yield (256 x 2 x 25) < 16K and hence the total number of threads that can be simultaneously scheduled for 30 single multiprocessors would be 256 x 2 x 30 = 15360.

### 4 Main

```
********************
   *cr
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   *cr
                       University of Illinois
   *cr
                       All Rights Reserved
   *cr
   *cr
      9
  #include <stdio.h>
  #include <stdlib.h>
10
  #include "kernel.cu"
11
  #include "support.h"
12
13
  int main (int argc, char *argv[])
14
15
16
     Timer timer;
17
     cudaError_t cuda_ret;
```

```
19
        // Initialize host variables
20
21
        printf("\nSetting up the problem..."); fflush(stdout);
22
        startTime(&timer);
23
24
        float *A_h, *B_h, *C_h;
25
        float *A_d, *B_d, *C_d;
26
        size_t A_sz, B_sz, C_sz;
        unsigned matArow, matAcol;
28
        unsigned matBrow, matBcol;
29
        dim3 dim_grid, dim_block;
30
31
        if (argc == 1) {
32
            matArow = 1000;
33
            matAcol = matBrow = 1000;
34
            matBcol = 1000;
35
        } else if (argc == 2) {
            matArow = atoi(argv[1]);
37
            matAcol = matBrow = atoi(argv[1]);
            matBcol = atoi(argv[1]);
39
        } else if (argc == 4) {
            matArow = atoi(argv[1]);
41
            matAcol = matBrow = atoi(argv[2]);
42
            matBcol = atoi(argv[3]);
43
        } else {
            printf("\n
                           Invalid input parameters!"
45
          "\n
                  Usage: ./sgemm-tiled
                                                         # All matrices
46
           \hookrightarrow are 1000 x 1000"
          "\n
                  Usage: ./sgemm-tiled <m>
                                                         # All matrices
47
           \rightarrow are m x m"
                 Usage: ./sgemm-tiled <m> <k> <n>
                                                         # A: m x k, B: k
48
           \rightarrow x n, C: m x n"
          "\n");
49
            exit(0);
50
51
        A_sz = matArow*matAcol;
53
        B_sz = matBrow*matBcol;
        C_sz = matArow*matBcol;
55
        A_h = (float*) malloc( sizeof(float)*A_sz );
57
        for (unsigned int i=0; i < A_sz; i++) { A_h[i] =</pre>
        \rightarrow (rand()%100)/100.00; }
```

```
B_h = (float*) malloc( sizeof(float)*B_sz );
60
       for (unsigned int i=0; i < B_sz; i++) { B_h[i] =
61
        \rightarrow (rand()%100)/100.00; }
       C_h = (float*) malloc( sizeof(float)*C_sz );
63
       stopTime(&timer); printf("%f s\n", elapsedTime(timer));
65
                   A: %u x %u\n B: %u x %u\n
       printf("
                                                  C: %u x %u\n",

→ matArow, matAcol,

           matBrow, matBcol, matArow, matBcol);
        // Allocate device variables
69
70
       printf("Allocating device variables..."); fflush(stdout);
71
       startTime(&timer);
72
73
       //INSERT CODE HERE
74
       cuda_ret = cudaMalloc((void**)&A_d, sizeof(float)*A_sz);
               if (cuda_ret != cudaSuccess) FATAL("Unable to
76

    allocate device memory");

77
       cuda_ret = cudaMalloc((void**)&B_d, sizeof(float)*B_sz);
            if (cuda_ret != cudaSuccess) FATAL("Unable to allocate
79

    device memory");
80
       cuda_ret = cudaMalloc((void**)&C_d, sizeof(float)*C_sz);
           if (cuda_ret != cudaSuccess) FATAL("Unable to allocate
82

    device memory");
83
       cudaDeviceSynchronize();
       stopTime(&timer); printf("%f s\n", elapsedTime(timer));
85
86
       // Copy host variables to device
       printf("Copying data from host to device...");
89

    fflush(stdout);

       startTime(&timer);
90
       //INSERT CODE HERE
92
       cuda_ret = cudaMemcpy(A_d, A_h, sizeof(float)*A_sz,
        if (cuda_ret != cudaSuccess) FATAL("Unable to copy to

→ device memory");
```

```
cuda_ret = cudaMemcpy(B_d, B_h, sizeof(float)*B_sz,
96
            cudaMemcpyHostToDevice);
            if (cuda_ret != cudaSuccess) FATAL("Unable to copy to
97

    device memoy");
98
        cudaDeviceSynchronize();
100
        stopTime(&timer); printf("%f s\n", elapsedTime(timer));
101
102
        // Launch kernel using standard sgemm interface
103
        printf("Launching kernel..."); fflush(stdout);
104
        startTime(&timer);
105
        basicSgemm('N', 'N', matArow, matBcol, matBrow, 1.0f, \
106
                    A_d, matArow, B_d, matBrow, 0.0f, C_d, matBrow);
107
108
        cuda_ret = cudaDeviceSynchronize();
109
            if(cuda_ret != cudaSuccess) FATAL("Unable to launch
110

    kernel");

        stopTime(&timer); printf("%f s\n", elapsedTime(timer));
111
112
        // Copy device variables from host
113
114
        printf("Copying data from device to host...");
115

    fflush(stdout);

        startTime(&timer);
116
117
        //INSERT CODE HERE
118
        cuda_ret = cudaMemcpy(C_h, C_d, sizeof(float)*C_sz,
119
         if (cuda_ret != cudaSuccess) FATAL("Unable to copy to
120
            → host memory");
121
        cudaDeviceSynchronize();
122
        stopTime(&timer); printf("%f s\n", elapsedTime(timer));
123
124
        // Verify correctness
        printf("Verifying results..."); fflush(stdout);
127
        verify(A_h, B_h, C_h, matArow, matAcol, matBcol);
129
```

131

```
// Free memory
132
133
         free(A_h);
134
         free(B_h);
135
         free(C_h);
136
137
         //INSERT CODE HERE
138
         cudaFree(A_d);
139
         cudaFree(B_d);
140
         cudaFree(C_d);
141
         return 0;
142
143
    }
144
```

# 5 Kernel

```
*cr
   *cr
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                     University of Illinois
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   *cr
   *cr
     #include <stdio.h>
9
10
  #define TILE_SZ 16
11
12
  __global__ void mysgemm(int m, int n, int k, const float *A,
13

    const float *B, float* C) {
14
15
       16
      * Compute C = A \times B
17
       where A is a (m x k) matrix
18
        where B is a (k \times n) matrix
19
        where C is a (m x n) matrix
21
      * Use shared memory for tiling
22
23
```

```
24
        25
        // INSERT KERNEL CODE HERE
        unsigned int TiRow = threadIdx.y;
27
        unsigned int TiCol = threadIdx.x;
        unsigned int row = blockIdx.y * blockDim.y + threadIdx.y;
        unsigned int col = blockIdx.x * blockDim.x + threadIdx.x;
31
        __shared__ float As[TILE_SZ][TILE_SZ];
        __shared__ float Bs[TILE_SZ][TILE_SZ];
33
        float sum = 0;
35
36
        for(unsigned int TiNum = 0; TiNum < (k-1)/TILE_SZ+1;</pre>
38
        → TiNum++){
              if((row < m) && (TiNum * TILE_SZ + TiCol) < k)</pre>
39
                         As[TiRow] [TiCol] = A[row * k + TiNum * TILE_SZ
                         → + TiCol];
              else
                         As[TiRow][TiCol] = 0;
42
             if((TiNum * TILE_SZ + TiRow) < k && col < n)</pre>
44
                         Bs[TiRow][TiCol] = B[(TiNum * TILE_SZ +
45

→ TiRow) * n + col];

            else
                        Bs[TiRow][TiCol] = 0;
47
              __syncthreads();
48
49
            //Calculate inner product for the tile
50
            //Checking for matrix size to lower power and practice
51
            if(row < m && col < n)
                    for(unsigned int TiElem = 0; TiElem < TILE_SZ;</pre>
53

    TiElem++)

                             sum = sum +
54
                             \  \, \hookrightarrow \  \, \text{As}\,[\text{TiRow}]\,[\text{TiElem}]\,*\text{Bs}\,[\text{TiElem}]\,[\text{TiCol}]\,;
            __syncthreads();
55
            }
57
            //Prevent writing of output to an undefined block
59
            if (row < m && col < n)
                    C[row * n + col] = sum;
61
   }
```

```
63
    void basicSgemm(char transa, char transb, int m, int n, int k,
        float alpha, const float *A, int lda, const float *B, int
        ldb, float beta, float *C, int ldc)
65
        if ((transa != 'N') && (transa != 'n')) {
66
            printf("unsupported value of 'transa'\n");
67
                return;
68
        }
69
        if ((transb != 'N') && (transb != 'n')) {
71
            printf("unsupported value of 'transb'\n");
72
            return;
73
        }
74
        if ((alpha - 1.0f > 1e-10) \mid | (alpha - 1.0f < -1e-10)) {
76
            printf("unsupported value of alpha\n");
77
            return;
78
        }
80
        if ((beta - 0.0f > 1e-10) || (beta - 0.0f < -1e-10)) {
            printf("unsupported value of beta\n");
82
            return;
        }
84
85
        // Initialize thread block and kernel grid dimensions
86
         87
       //INSERT CODE HERE
        const unsigned int BLOCK_SIZE = TILE_SZ; //use 16 x 16 thread
         \hookrightarrow blocks
90
        dim3 block(BLOCK_SIZE, BLOCK_SIZE ,1);
91
        dim3 grid((n + BLOCK_SIZE - 1)/BLOCK_SIZE, (m + BLOCK_SIZE
92
         \rightarrow -1)/BLOCK_SIZE, 1);
93
94
        // Invoke CUDA kernel
        //INSERT CODE HERE
97
        mysgemm<<< grid, block>>>(m, n, k, A, B, C);
99
    }
101
```