

OpenSeismoMatlab

Software for strong ground motion data processing

-

Contents

- [Help](#)
- [Examples](#)
- [Verification](#)
- [Copyright](#)

Help

Help section of the OpenSeismoMatlab functions

-

[baselineCorr.m](#)

Baseline correction of acceleration time history

-

[BLKIN.m](#)

Bilinear kinematic hysteretic model with elastic viscous damping

-

[CDReSp.m](#)

Constant Ductility Response Spectra

-

[CSReSp.m](#)

Constant Strength Response Spectra

-

[DRHA.m](#)

Dynamic Response History Analysis

-

[FASp.m](#)

Fourier amplitude spectrum

-

[ffft.m](#)

Fast Finite Fourier Transform

-

[HalfStep.m](#)

Reproduce signal with half time step

-

[IDA.m](#)

Incremental Dynamic Analysis

-

[iffft.m](#)

Inverse Fast Finite Fourier Transform

-

[LReSp.m](#)

Linear Elastic Response Spectra

-

[LIDA.m](#)

Linear Implicit Dynamic Analysis

-

[NLIDABLKIN.m](#)

Non Linear Implicit Dynamic Analysis of a BiLinear KINematic hardening hysteretic structure with elastic damping

-

[OpenSeismoMatlab.m](#)

Seismic parameters and processing of an acceleration time history

-

[PulseDecomp.m](#)

Pulse decomposition of a velocity time history

-

[RPSReSp.m](#)

Rigid Plastic Sliding Response Spectra

-

Examples

Examples of various OpenSeismoMatlab applications

-

[example_baselineCorr](#)

Perform baseline correction

-

[example_CDReSp](#)

Calculate constant ductility response spectra of an artificially generated acceleration time history

-

[example_Constant_ductility_response_spectra](#)

Calculate constant ductility response spectra of a suite of ground motions

-

[example_Fourier_spectra](#)

Calculate Fourier spectra of a suite of ground motions

-

[example_general](#)

Test all functionalities of OpenSeismoMatlab in a single script

-

[example_LEReSp](#)

Calculate linear elastic response spectra of an artificially generated acceleration time history

-

[example_Linear_elastic_response_spectra.m](#)

Calculate the linear elastic response spectra of an earthquake suite

-

[PulseDecomp.m](#)

Pulse decomposition of a velocity time history

-

[RPSReSp.m](#)

Calculate rigid plastic sliding response spectra

-

[example_Spectra_comparison_1.m](#)

Comparison of elastic and constant ductility response spectra for $\mu=1$

-

[example_Spectra_comparison_2.m](#)

Comparison of constant ductility response spectra for $\mu=2$

-

Verification

Validation of OpenSeismoMatlab results against the literature

[verification_CDRS](#)

Verification of a constant ductility response spectrum

Reference: Chopra (2020)

-

[verification_CSRS1](#)

Verification of a constant strength response spectrum

Reference: Tena-Colunga, A. (1999)

-

[verification_CSRS2](#)

Verification of a constant strength response spectrum

Reference: Tena-Colunga, A. (1999)

-

[verification_DRHA](#)

Calculate linear dynamic response of a MDOF shear building

Reference: Chopra (2020)

-

[verification_filter1](#)

Verify the high pass Butterworth filter of OpenSeismoMatlab

Reference: Boore (2005)

-

[verification_filter2](#)

Verify the low- and high- pass Butterworth filter of OpenSeismoMatlab

Reference: Graizer (2012)

-

[verification_Fourier_spectrum1](#)

Verify the Fourier amplitude spectrum of the San Fernando earthquake (1971) - Component N11E

Reference: California Institute of Technology, EERL (1974)

-

[verification_Fourier_spectrum2](#)

Verify the Fourier amplitude spectrum of the San Fernando earthquake (1971) - Component N79W

Reference: California Institute of Technology, EERL (1974)

-

[verification_IDA1](#)

Verify the incremental dynamic analysis for an acceleration time history with given duration D_5_75 and spectral acceleration

Reference: Mashayekhi et al. (2020)

-

[verification_IDA2](#)

Verify the incremental dynamic analysis for an earthquake suite

Reference: Deng et al. (2017)

-

[verification_IDA3](#)

Verify the incremental dynamic analysis for the Loma Prieta earthquake (1989)

Reference: Vamvatsikos & Cornell (2002)

-

[verification_IDA4](#)

Verify the incremental dynamic analysis bias due to fitting of the capacity curve of a SDOF system with an elastoplastic bilinear fit according to FEMA-440

Reference: De Luca et al. (2011)

-

[verification_LIDA](#)

Calculate the dynamic response of a linear SDOF oscillator

Reference: Chopra (2020)

-

[verification_LIDA_NLIDABLKIN](#)

Compare the output of LIDA.m and NLIDABLKIN.m for a linear SDOF oscillator in terms of seismic input energy per unit mass.

Reference: None

-

[verification_NLIDABLKIN](#)

Verify the energy time history of SDOF oscillator

Reference: Chopra (2020)

-

[verification_NLIDABLKIN2](#)

Verify the energy time histories of a nonlinear SDOF oscillator

Reference: Uang, C. M., & Bertero, V. V. (1990)

-

[verification_NLIDABLKIN3](#)

Verify the strength ductility relation of an elastoplastic system

Reference: Mahin, S. A., & Lin, J. (1983)

-

[verification_PulseDecomp1](#)

Verify the extraction of the velocity pulse of a strong motion velocity time history

Reference: Baker, J. W. (2007)

-

[verification_PulseDecomp2](#)

Verify the extraction of the velocity pulses of a strong motion velocity time history and sum them to reconstruct the original ground motion

Reference: Shahi, S. K., & Baker, J. W. (2014)

-

[verification_SIH1952](#)

Calculate the spectral intensity as defined by Housner (1952)

Reference: Housner, G. W. (1952)

-

[verification_SRS1](#)

Calculate the rigid plastic sliding response spectrum

Reference: Garini, E., & Gazetas, G. (2016)

-

[verification_SRS2](#)

Calculate the rigid plastic sliding response spectrum

Reference: Paglietti, A., & Porcu, M. C. (2001)

-

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example baselineCorr

Apply baseline correction in OpenSeismoMatlab

Contents

- [Earthquake motion](#)
- [Integrate without baseline correction](#)
- [Integrate with baseline correction](#)
- [Plot corrected and uncorrected acceleration](#)
- [Plot corrected and uncorrected velocity](#)
- [Plot corrected and uncorrected displacement](#)
- [Copyright](#)

Earthquake motion

Load earthquake data

```
fid=fopen('Imperial_Valley_El_Centro_9_EW.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
time=text{1,1};
xgttl=text{1,2};
dt=time(2)-time(1);
```

Integrate without baseline correction

Calculate the velocity and displacement time histories

```
xgt1 = cumtrapz(time,xgttl);
xg1 = cumtrapz(time,xgt1);
```

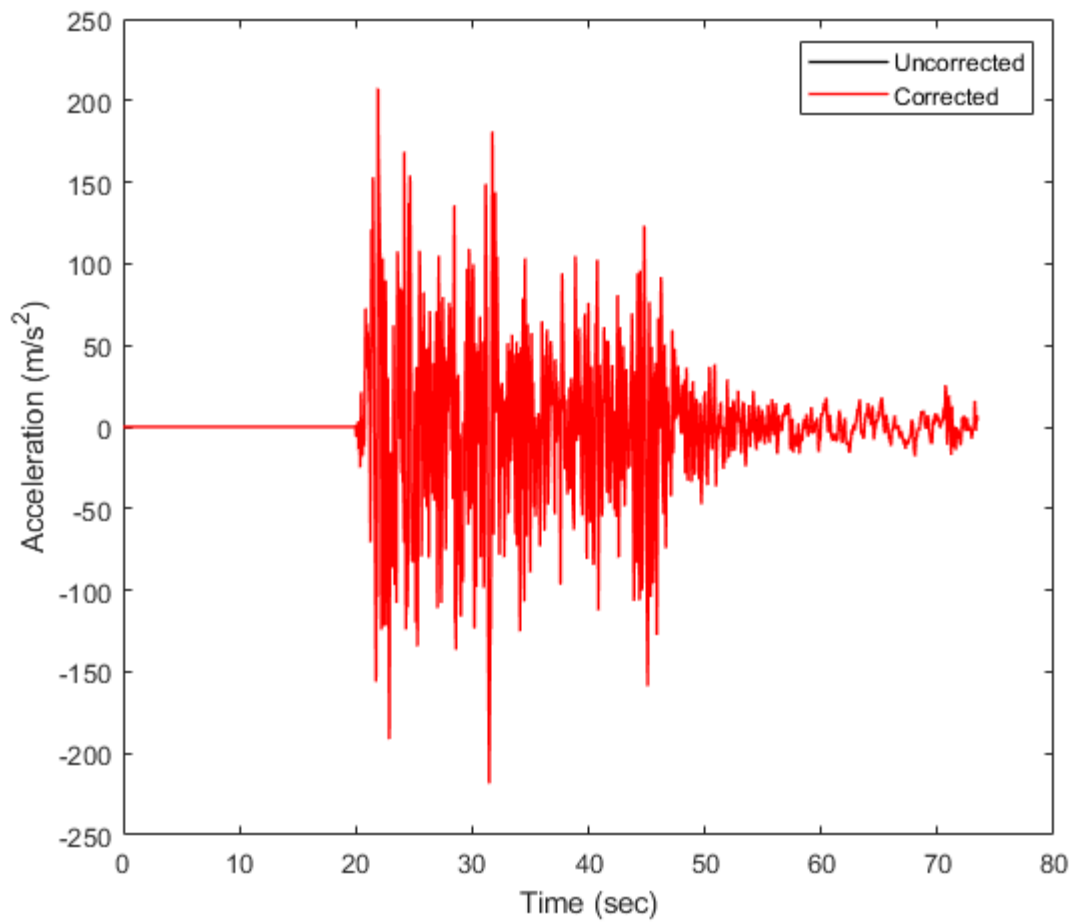
Integrate with baseline correction

Calculate the displacement, velocity and acceleration time histories

```
[xg2, xgt2, xgtt2] = baselineCorr(time,xgttl);
```

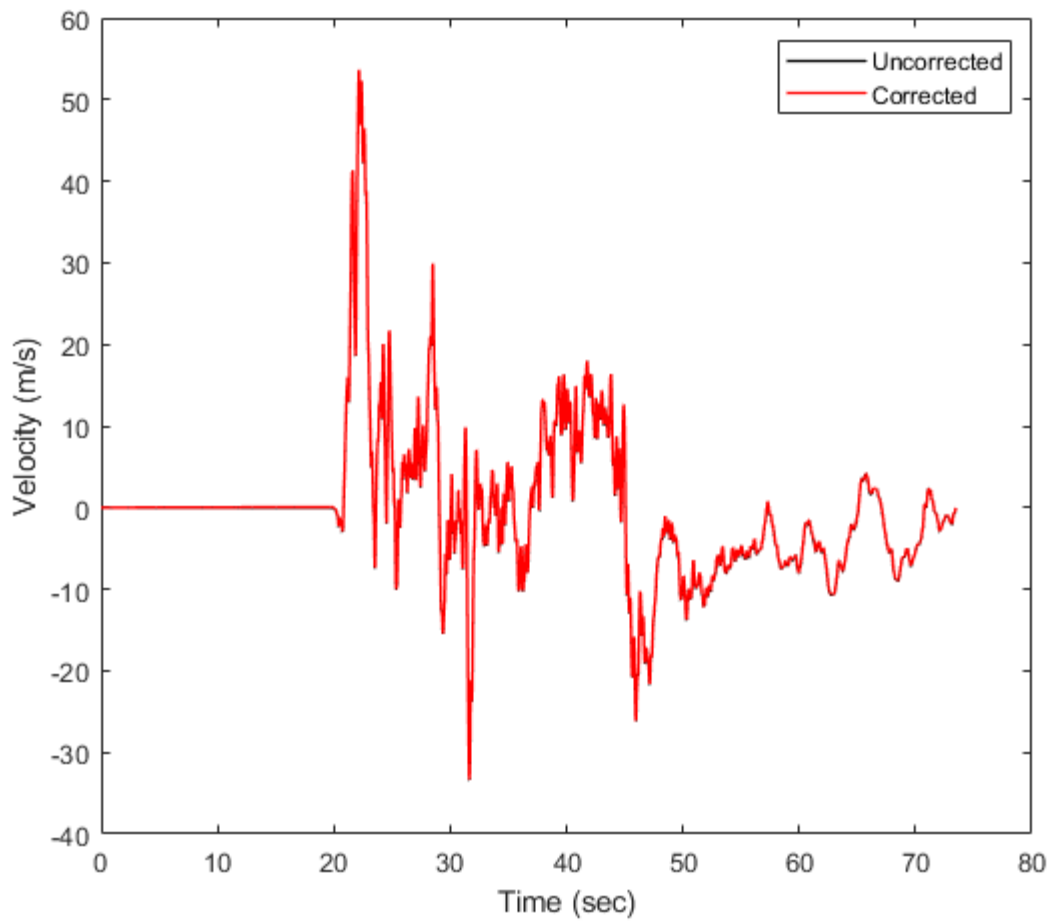
Plot corrected and uncorrected acceleration

```
figure()
plot(time,xgttl,'k','LineWidth',1)
hold on
plot(time,xgtt2,'r','LineWidth',1)
hold off
ylabel('Acceleration (m/s^2)')
xlabel('Time (sec)')
legend('Uncorrected','Corrected')
drawnow;
pause(0.1)
```



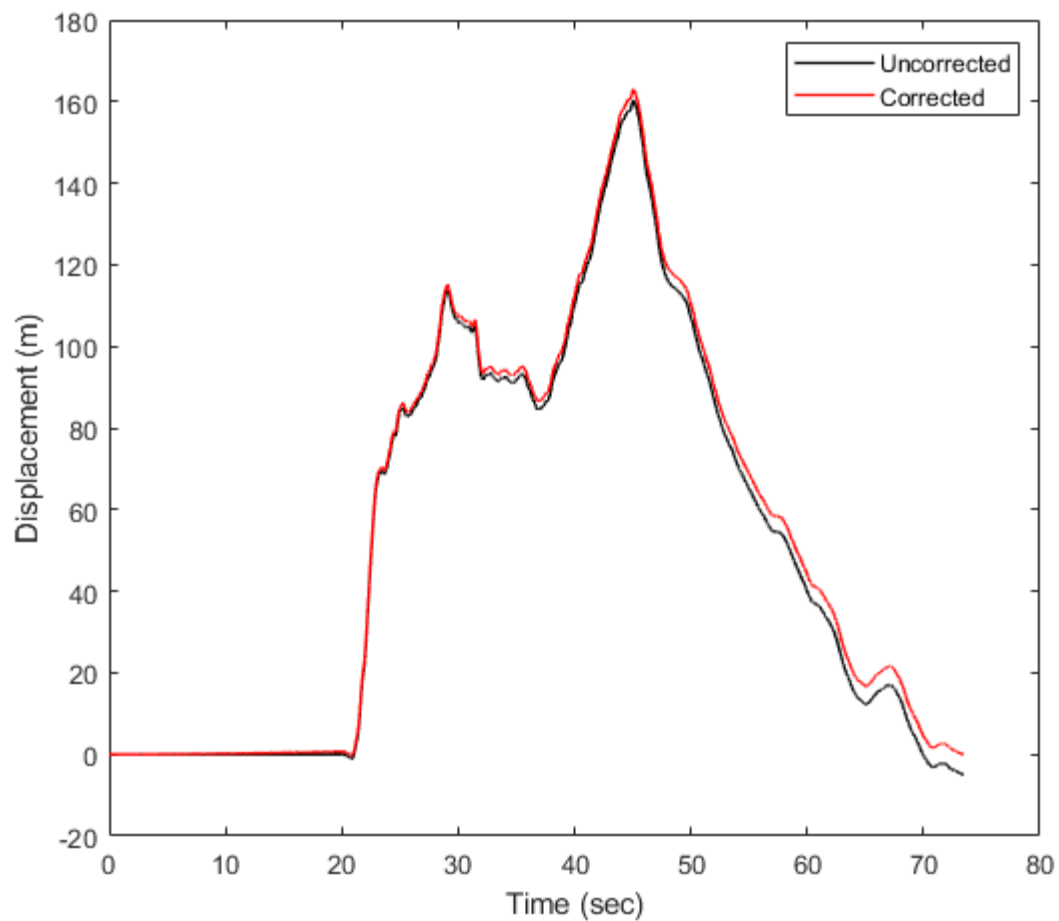
Plot corrected and uncorrected velocity

```
figure()
plot(time,xgt1,'k','LineWidth',1)
hold on
plot(time,xgt2,'r','LineWidth',1)
hold off
ylabel('Velocity (m/s)')
xlabel('Time (sec)')
legend('Uncorrected','Corrected')
drawnow;
pause(0.1)
```



Plot corrected and uncorrected displacement

```
figure()
plot(time,xg1,'k','LineWidth',1)
hold on
plot(time,xg2,'r','LineWidth',1)
hold off
ylabel('Displacement (m)')
xlabel('Time (sec)')
legend('Uncorrected','Corrected')
drawnow;
pause(0.1)
```



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example CDRSp

Calculate constant ductility response spectra in OpenSeismoMatlab

Contents

- [Earthquake motion](#)
- [Setup parameters for CDRSp function](#)
- [Calculate spectra and pseudospectra](#)
- [Plot the spectra](#)
- [Copyright](#)

Earthquake motion

For reproducibility

```
rng(0)
```

Generate earthquake data

```
dt=0.02;  
N=10;  
a=rand(N,1)-0.5;  
b=100*pi*rand(N,1);  
c=pi*(rand(N,1)-0.5);  
t=(0:dt:(100*dt))';  
xgtt=zeros(size(t));  
for i=1:N  
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));  
end
```

Setup parameters for CDRSp function

Eigenperiods

```
T=(0.04:0.04:4)';
```

Critical damping ratio

```
ksi=0.05;
```

Ductility

```
mu=2;
```

Maximum number of iterations

```
n=50;
```

Tolerance for convergence to target ductility

```
tol=0.01;
```

Post-yield stiffness factor

```
pysf=0.1;
```

Maximum ratio of the integration time step to the eigenperiod

```
dtTol=0.02;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance of convergence for time integration algorithm

```
maxtol=0.01;
```

Maximum number of iterations per integration time step

```
jmax=200;
```

Infinitesimal acceleration

```
dak=eps;
```

Calculate spectra and pseudospectra

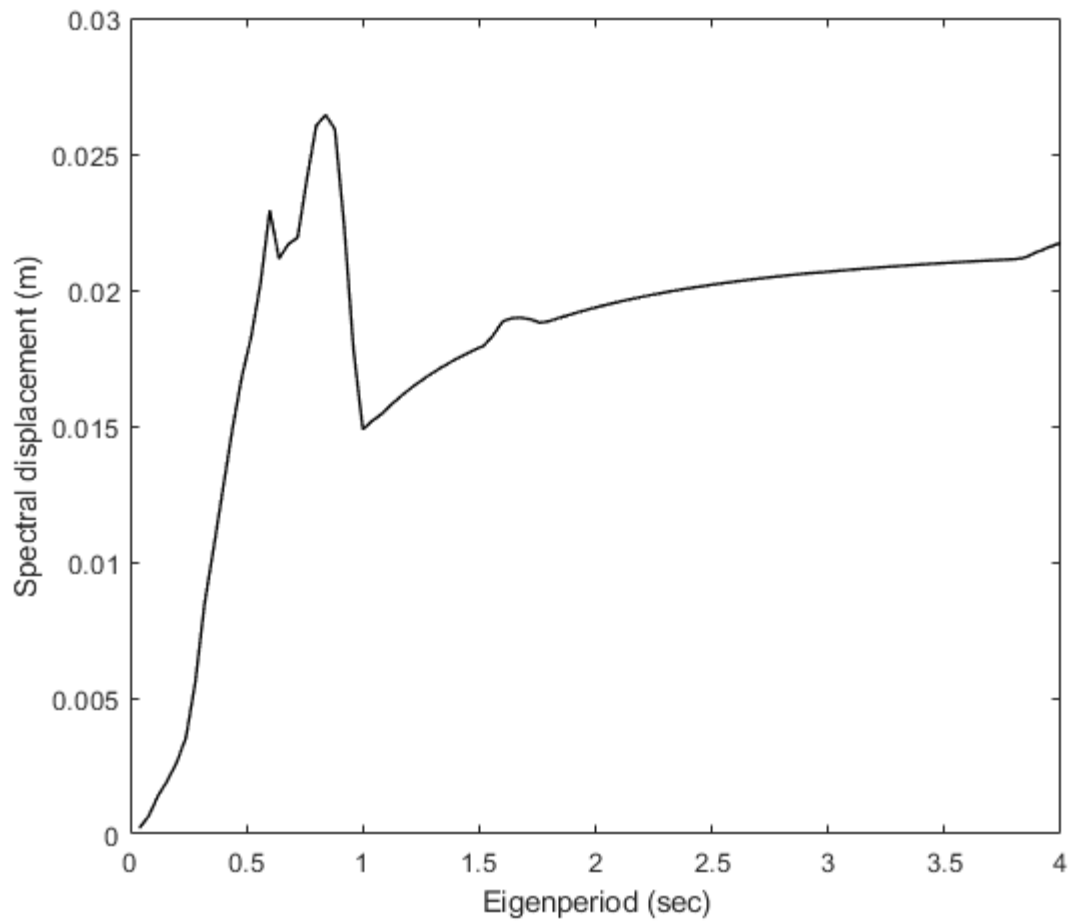
Apply CDRSp

```
[CDPSa,CDPSv,CDSd,CDSv,CDSa,fyK,muK,iterK]=CDReSp(dt,xgdt,T,ksi,...  
mu,n,tol,pysf,dtTol,AlgID,rinf,maxtol,jmax,dak);
```

Plot the spectra

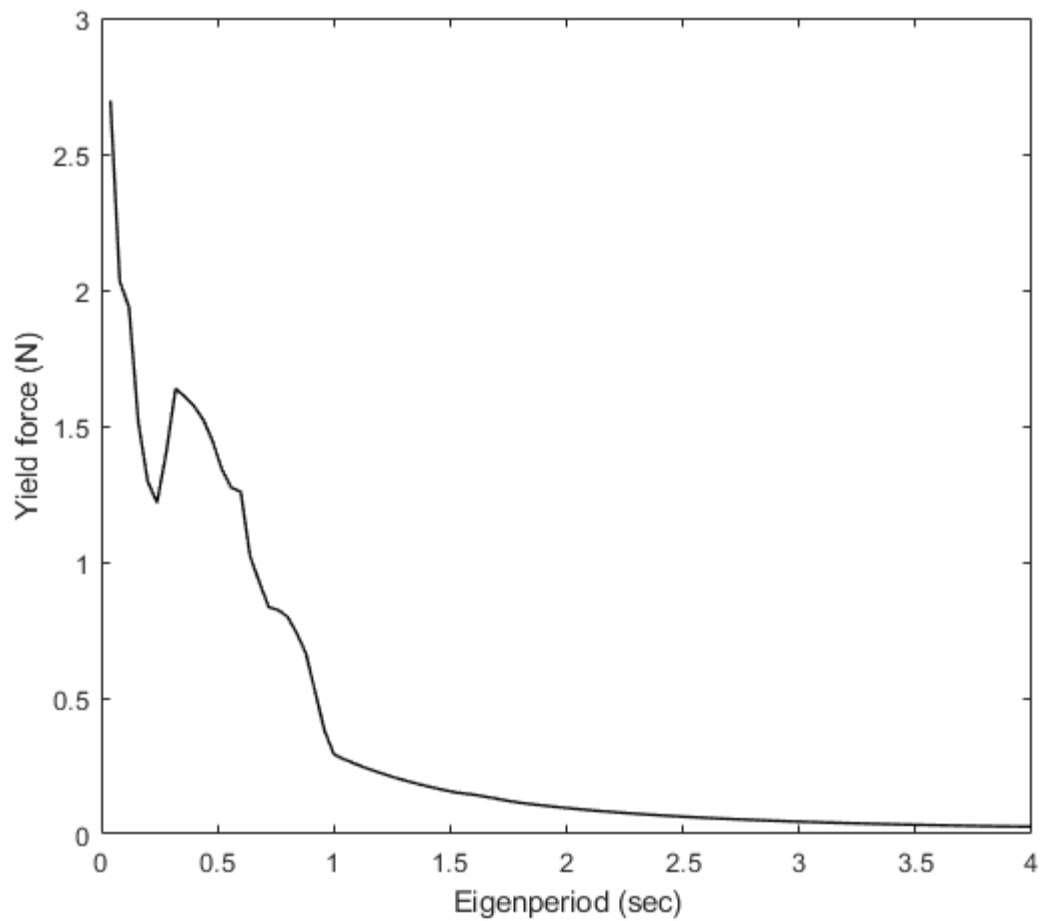
Constant ductility displacement spectrum

```
figure()
plot(T,CDSd,'k','LineWidth',1)
ylabel('Spectral displacement (m)')
xlabel('Eigenperiod (sec)')
drawnow;
pause(0.1)
```



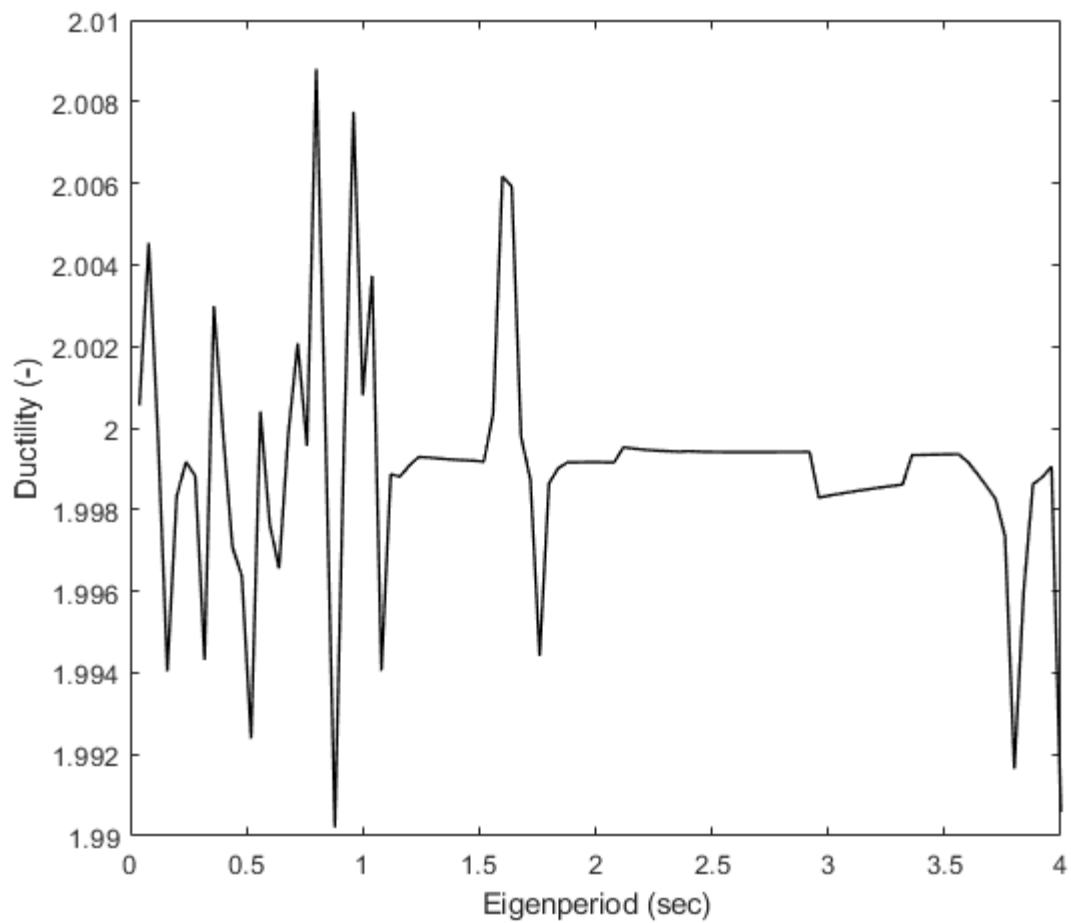
Constant ductility yield force spectrum

```
figure()
plot(T,fyK,'k','LineWidth',1)
ylabel('Yield force (N)')
xlabel('Eigenperiod (sec)')
drawnow;
pause(0.1)
```



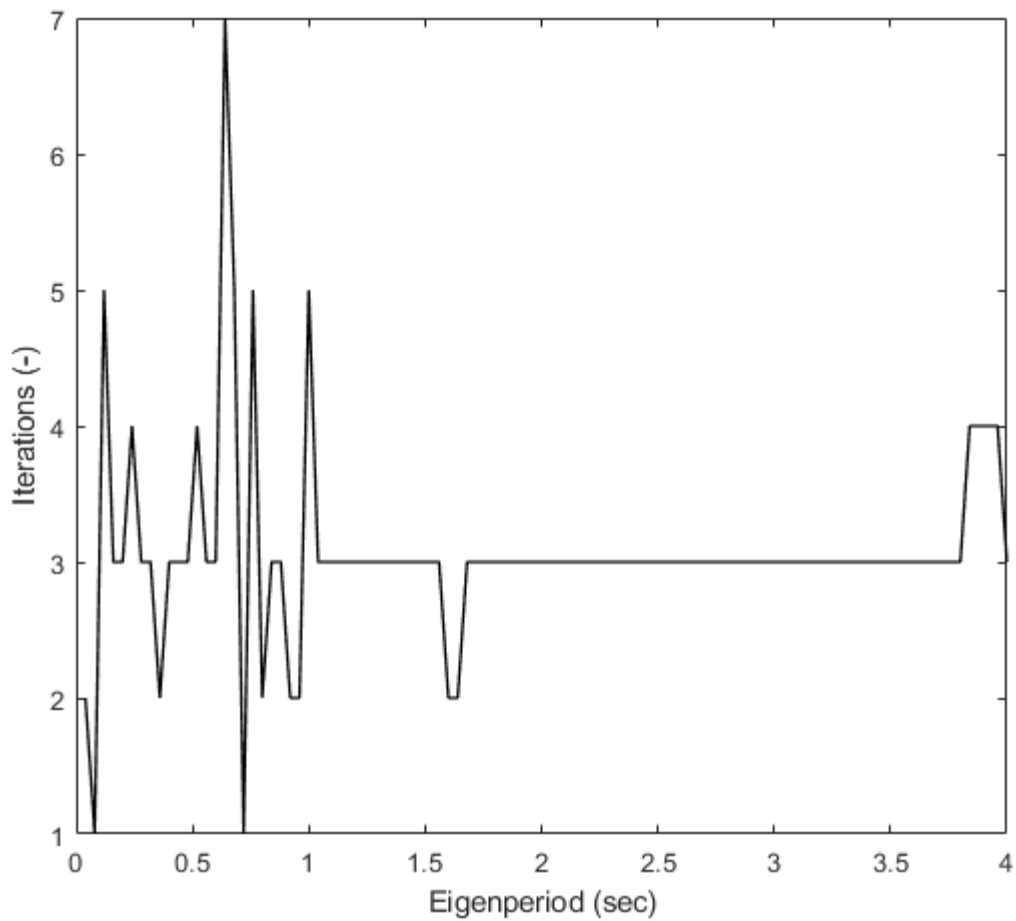
Achieved ductility

```
figure()
plot(T,muK,'k','LineWidth',1)
ylabel('Ductility (-)')
xlabel('Eigenperiod (sec)')
drawnow;
pause(0.1)
```

Iterations

```
figure()
plot(T,iterK,'k','LineWidth',1)
ylabel('Iterations (-)')
xlabel('Eigenperiod (sec)')
drawnow;
pause(0.1)
```



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example Constant ductility response spectra

Generate the constant ductility response spectra and associated results of an earthquake suite using OpenSeismoMatlab.

Contents

- [Input](#)
- [Calculation](#)
- [Output](#)
- [Copyright](#)

Input

earthquake motions

```
eqmotions={'Imperial Valley'; % Imperial valley 1979
           'Kocaeli';
           'Loma Prieta';
           'Northridge';
           'San Fernando';
           'Spitak';
           'Cape Mendocino';
           'ChiChi';
           'elcentro_NS_trunc'; % Imperial valley 1940
           'Hollister';
           'Kobe'};
```

Set the eigenperiod range for which the response spectra will be calculated.

```
Tspectra=(0.08:0.08:4)';
```

Set critical damping ratio of the response spectra to be calculated.

```
ksi=0.05;
```

Set the target ductility (not used here)

```
mu=2;
```

Set the postyield stiffness factor for each earthquake

```
p=[0.02;0.01;0.02;0.01;0.01;0.01;0.02;0.01;0.01;0.01;0.01];
```

Extract nonlinear response spectra

```
sw='cdrs';
```

Calculation

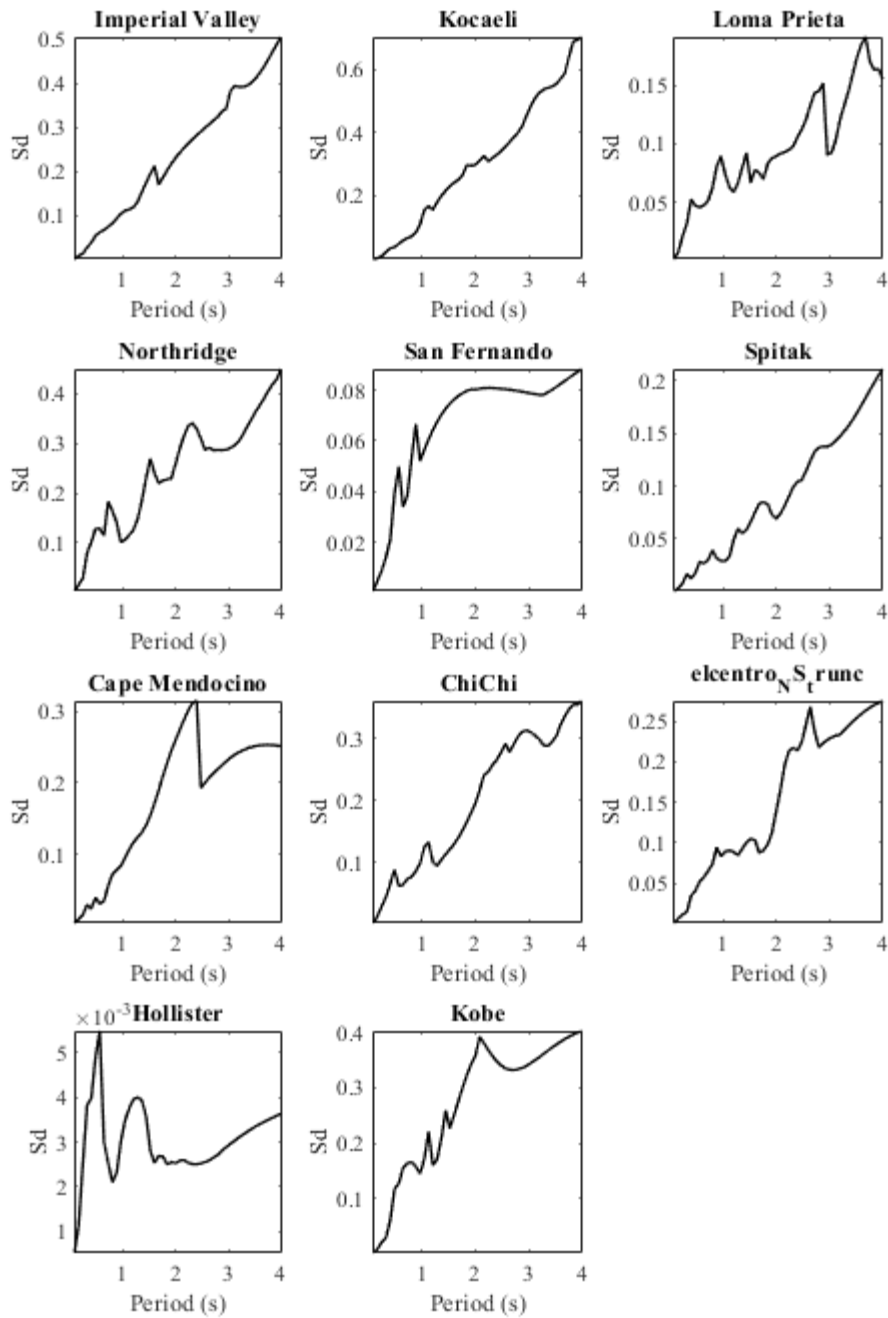
Initialize CDRS

```
CDRS=cell(numel(eqmotions),1);
% Calculation of peak values
for i=1:numel(eqmotions)
    % earthquake
    data=load([eqmotions{i},'.dat']);
    t=data(:,1);
    dt=t(2)-t(1);
    xgtt=data(:,2);
    S=OpenSeismoMatlab(dt,xgtt,sw,Tspectra,ksi,mu,p(i));
    CDRS{i}=[S.Period,S.CDSd,S.CDSv,S.CDPSa,S.fyK,S.muK,S.iterK];
end
```

Output

Plot constant ductility spectral displacement

```
Fig1 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(CDRS{i}(:,1),CDRS{i}(:,2),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('Sd','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
    axis tight
end
drawnow;
pause(0.1)
```



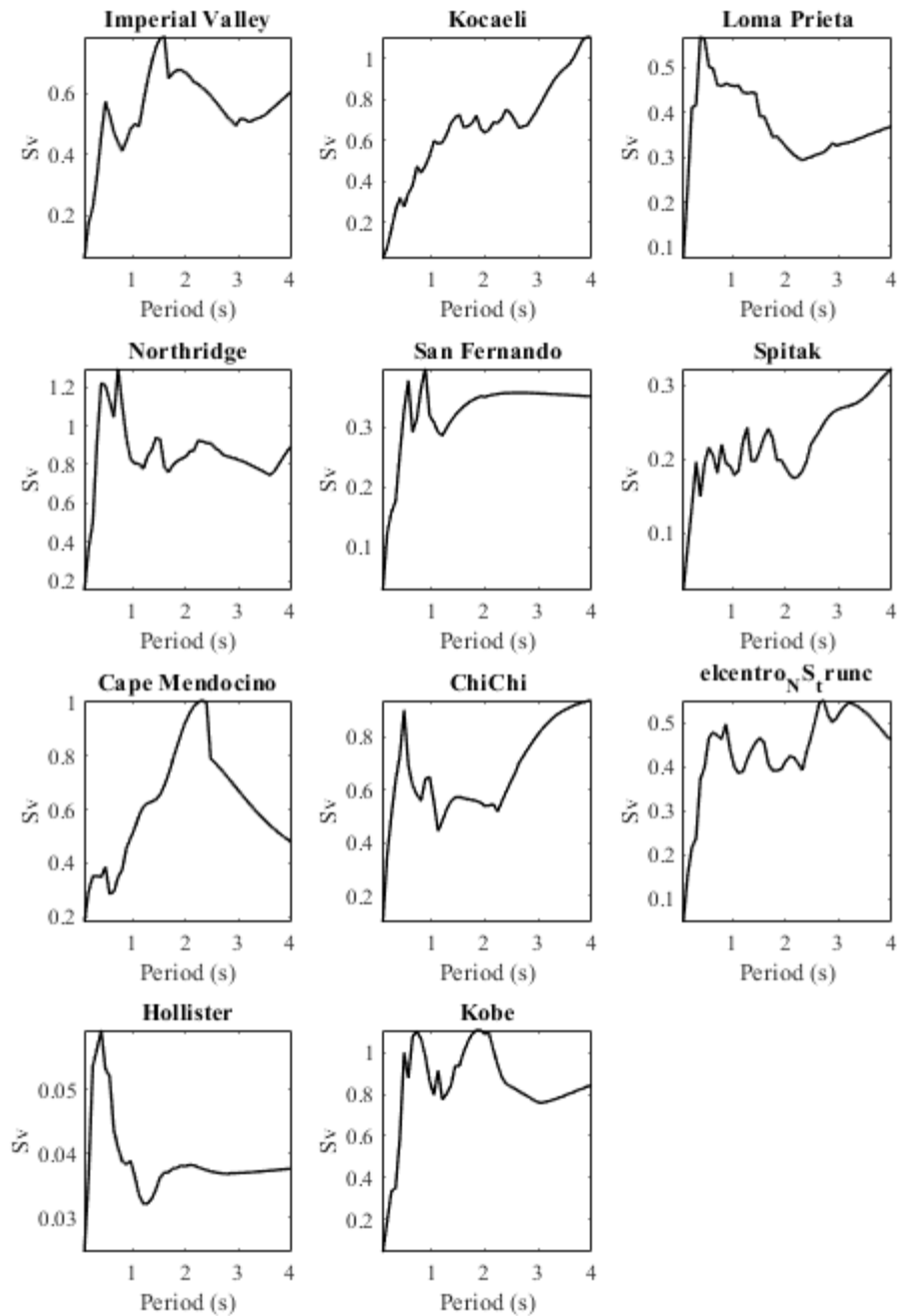
Plot constant ductility spectral velocity

```
Fig2 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(CDRS{i}(:,1),CDRS{i}(:,3),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('Sv','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
```

```

axis tight
end
drawnow;
pause(0.1)

```



Plot constant ductility spectral acceleration

```

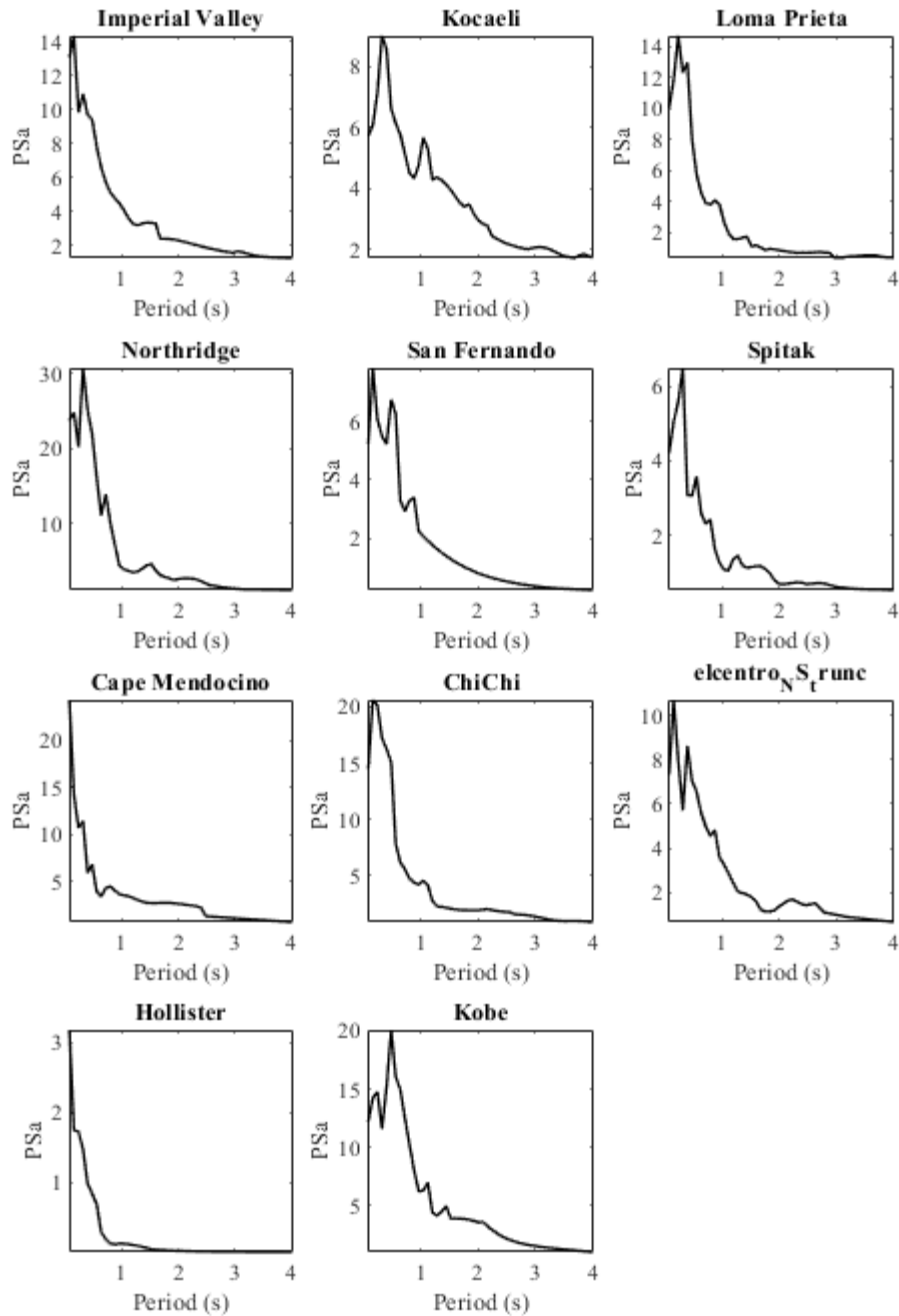
Fig3 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)

```

```

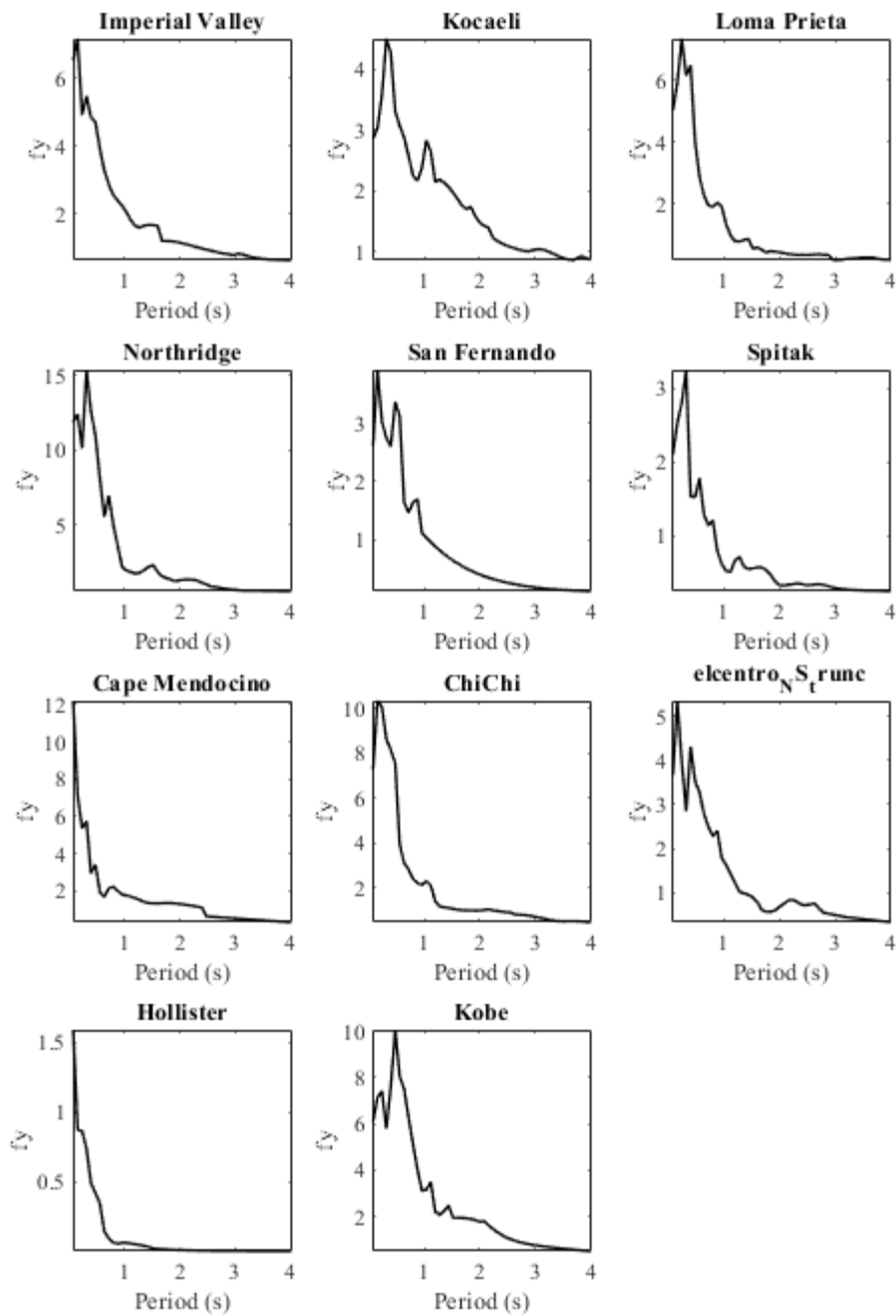
subplot(4,3,i)
plot(CDRS{i}(:,1),CDRS{i}(:,4),'k','LineWidth',1);
set(gca,'FontName','Times New Roman')
title(egmotions{i},'FontName','Times New Roman')
ylabel('PSa','FontName','Times New Roman')
xlabel('Period (s)','FontName','Times New Roman')
axis tight
end
drawnow;
pause(0.1)

```



Plot constant ductility spectral yield limit

```
Fig4 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(CDRS{i}(:,1),CDRS{i}(:,5),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('fy','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
    axis tight
end
drawnow;
pause(0.1)
```

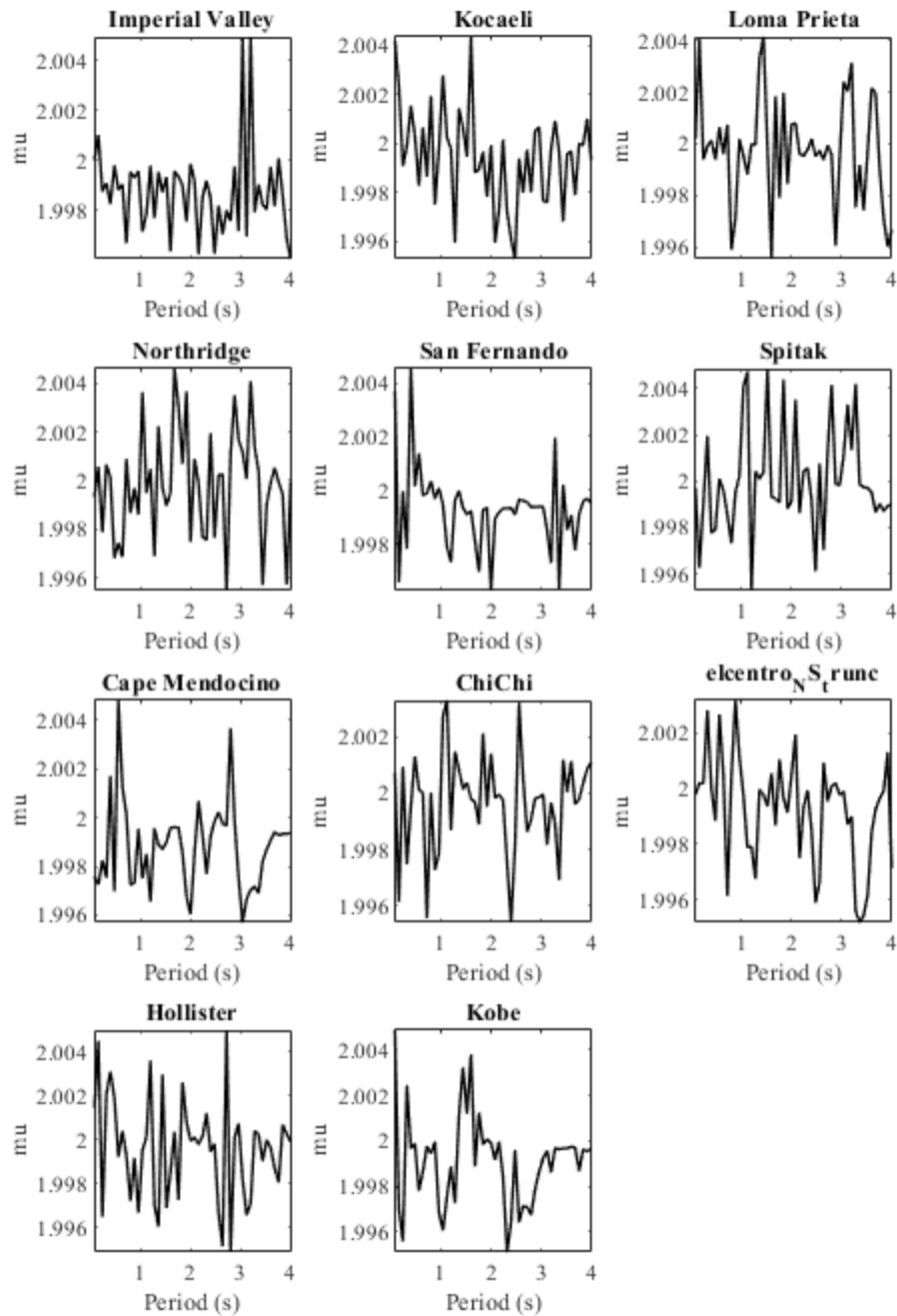
Plot constant ductility spectral achieved ductility

```
Fig5 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(CDRS{i}(:,1),CDRS{i}(:,6),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('mu','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
```

```

axis tight
end
drawnow;
pause(0.1)

```



Plot constant ductility spectral number of iterations needed for convergence

```

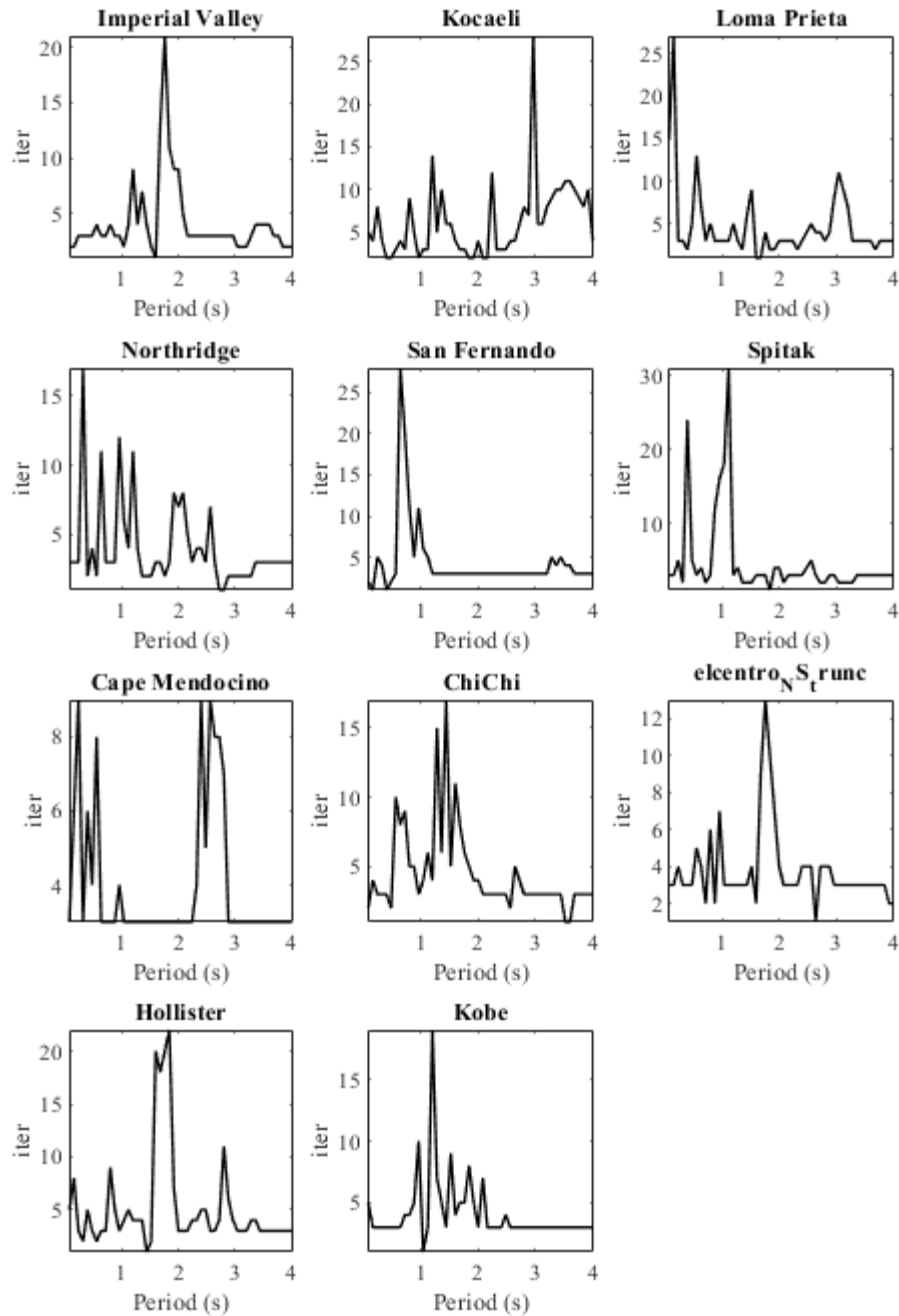
Fig6 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)

```

```

subplot(4,3,i)
plot(CDRS{i}(:,1),CDRS{i}(:,7),'k','LineWidth',1);
set(gca,'FontName','Times New Roman')
title(egmotions{i},'FontName','Times New Roman')
ylabel('iter','FontName','Times New Roman')
xlabel('Period (s)','FontName','Times New Roman')
axis tight
end
drawnow;
pause(0.1)

```



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example Fourier spectra

Generate the Fourier spectra of an earthquake suite using OpenSeismoMatlab

Contents

- [Input](#)
- [Extract fourier spectra](#)
- [Output](#)
- [Copyright](#)

Input

earthquake motions

```
eqmotions={'Imperial Valley'; % Imperial valley 1979
           'Kocaeli';
           'Loma Prieta';
           'Northridge';
           'San Fernando';
           'Spitak';
           'Cape Mendocino';
           'ChiChi';
           'elcentro_NS_trunc'; % Imperial valley 1940
           'Hollister';
           'Kobe'};
```

Switch

```
sw='fas';
```

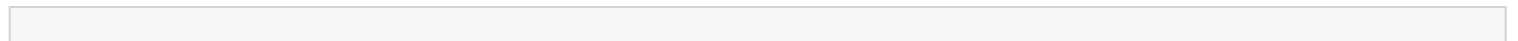
Extract fourier spectra

Initialize cell of Fourier spectra

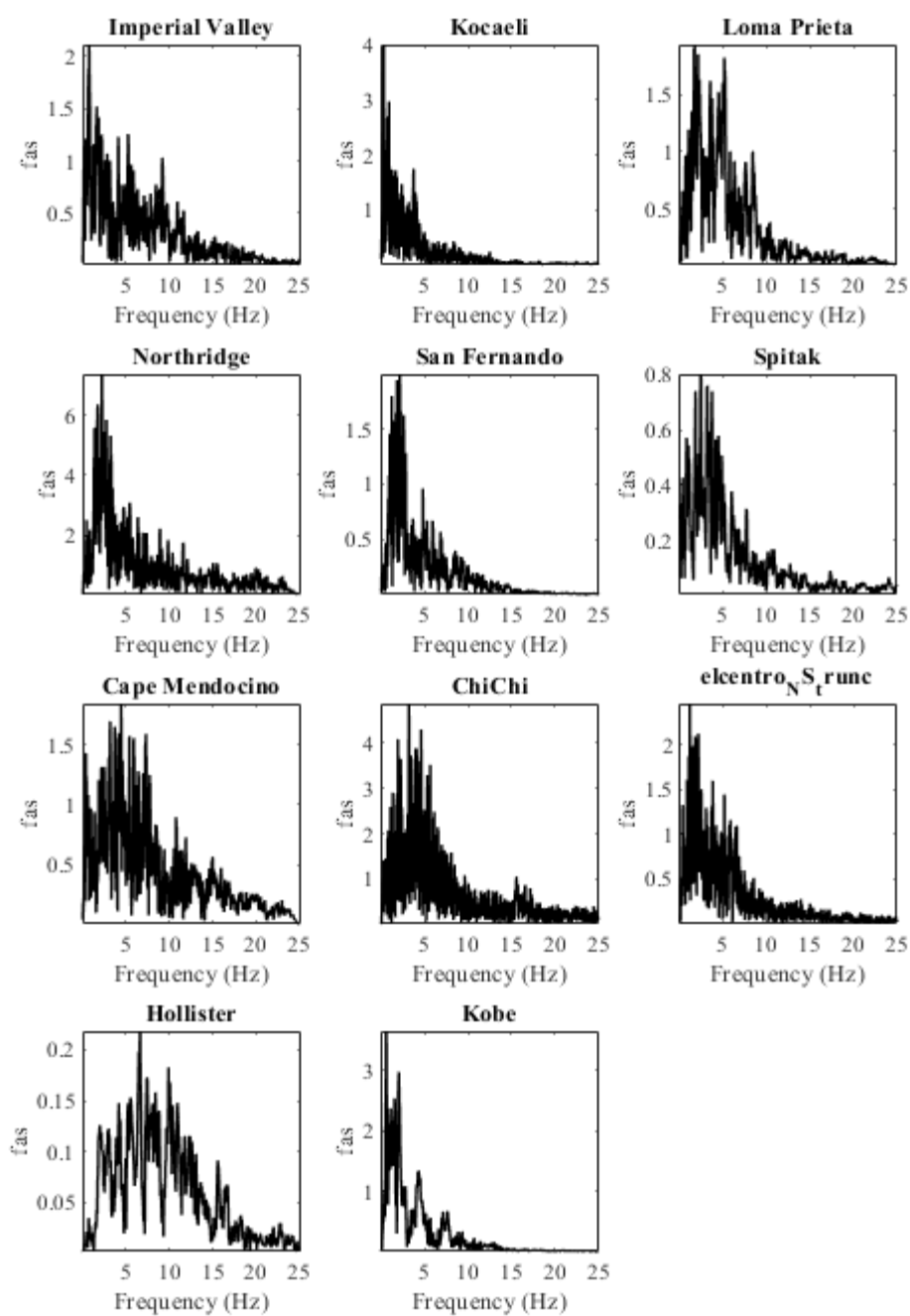
```
Fourier=cell(numel(eqmotions),1);
% Calculation of Fourier spectra
for i=1:numel(eqmotions)
    % earthquake
    data=load([eqmotions{i},'.dat']);
    t=data(:,1);
    dt=t(2)-t(1);
    xgtt=data(:,2);
    S=OpenSeismoMatlab(dt,xgtt,sw);
    Fourier{i}=[S.freq,S.FAS];
end
```

Output

Plot Fourier amplitude



```
Fig1 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);  
% Scan all subplots  
for i=1:numel(eqmotions)  
    subplot(4,3,i)  
    plot(Fourier{i}(:,1),Fourier{i}(:,2),'k','LineWidth',1);  
    set(gca,'FontName','Times New Roman')  
    title(eqmotions{i},'FontName','Times New Roman')  
    ylabel('fas','FontName','Times New Roman')  
    xlabel('Frequency (Hz)','FontName','Times New Roman')  
    axis tight  
end  
drawnow;  
pause(0.1)
```



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example General demonstration of the OpenSeismoMatlab capabilities

This is to demonstrate the capabilities of OpenSeismoMatlab and also to verify that OpenSeismoMatlab works properly for all of its possible options and types of application, and yields meaningful results. **All** capabilities of OpenSeismoMatlab are tested in this example

Contents

- [Load earthquake data](#)
- [Time histories without baseline correction](#)
- [Time histories with baseline correction](#)
- [Resample acceleration time history from 0.02 sec to 0.01 sec.](#)
- [PGA](#)
- [PGV](#)
- [PGD](#)
- [Total cumulative energy, Arias intensity and significant duration](#)
- [Pulse decomposition](#)
- [Linear elastic response spectra and pseudospectra](#)
- [Rigid plastic sliding displacement response spectra](#)
- [Constant ductility response spectra and pseudospectra](#)
- [Constant strength response spectra](#)
- [Fourier amplitude spectrum and mean period](#)
- [High pass Butterworth filter](#)
- [Low pass Butterworth filter](#)
- [Incremental dynamic analysis](#)
- [Effective peak ground acceleration](#)
- [Spectral intensity according to Housner \(1952\)](#)
- [Spectral intensity according to Nau & Hall \(1984\)](#)
- [Copyright](#)

Load earthquake data

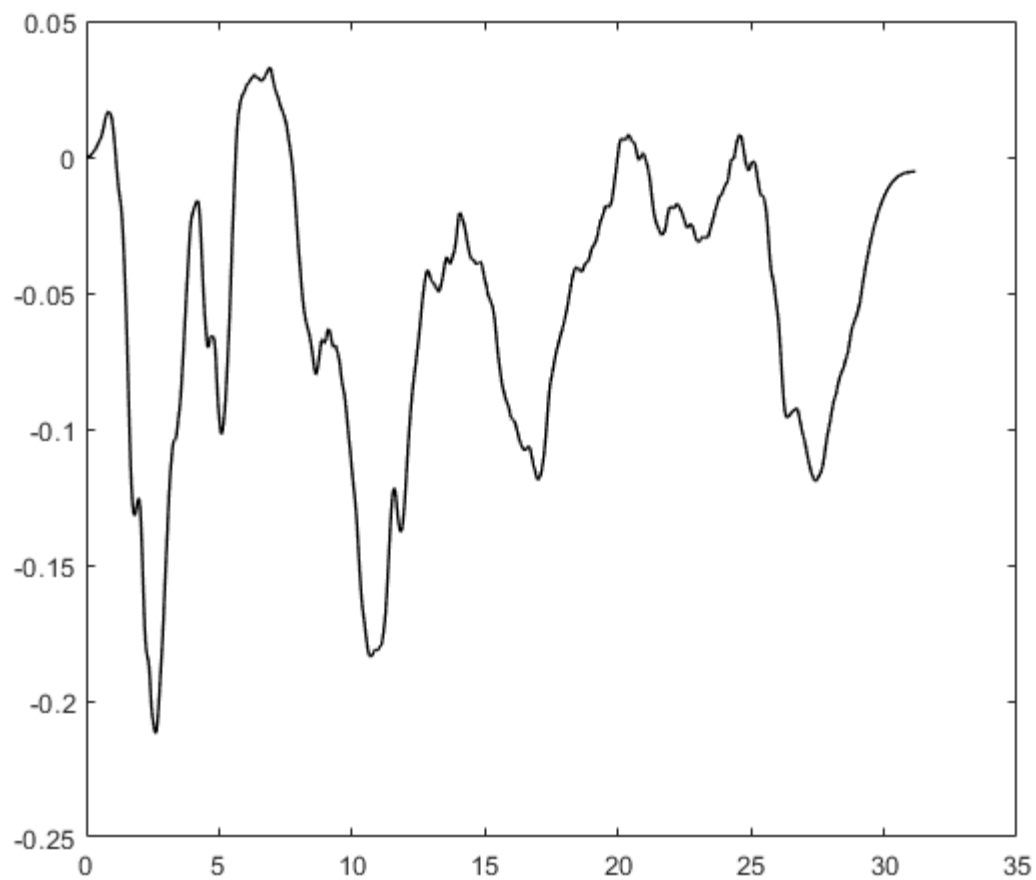
Earthquake acceleration time history of the El Centro earthquake will be used (El Centro, 1940, El Centro Terminal Substation Building)

```
fid=fopen('elcentro_NS_trunc.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtt=text{1,2};
```

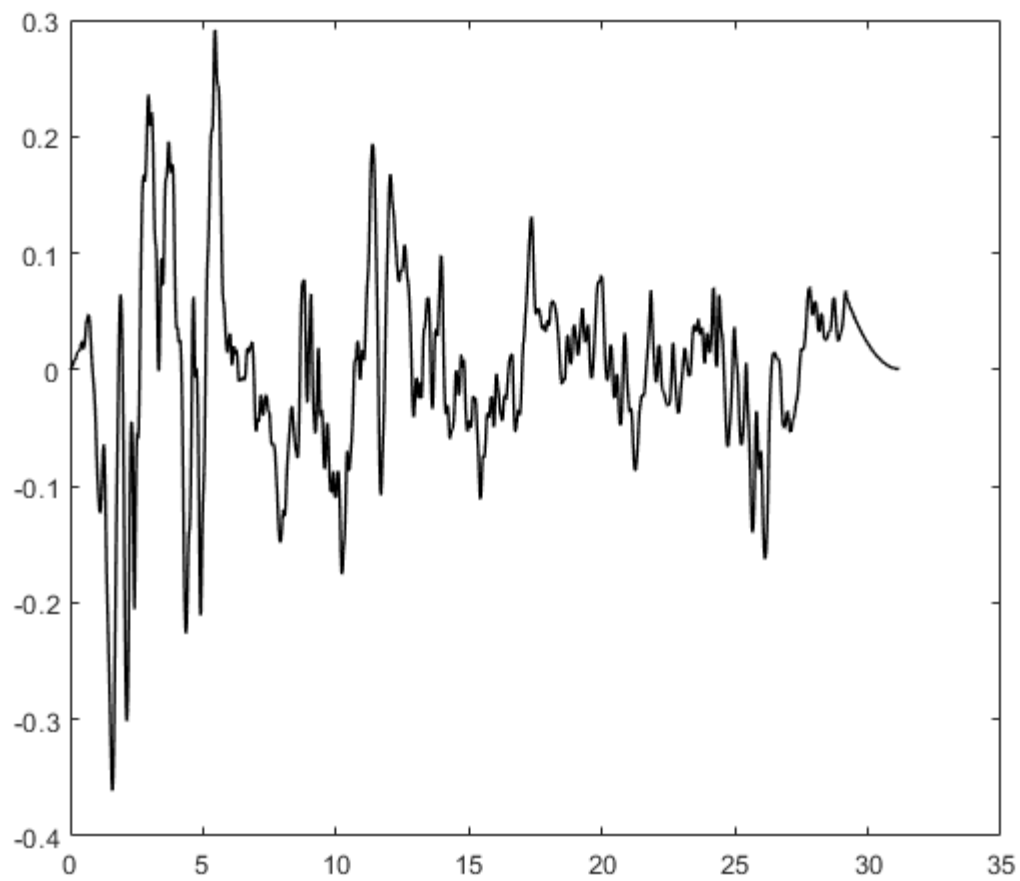
Time histories without baseline correction

```
sw='timehist';
baselineSw=false;
S1=OpenSeismoMatlab(dt,xgtt,sw,baselineSw);
```

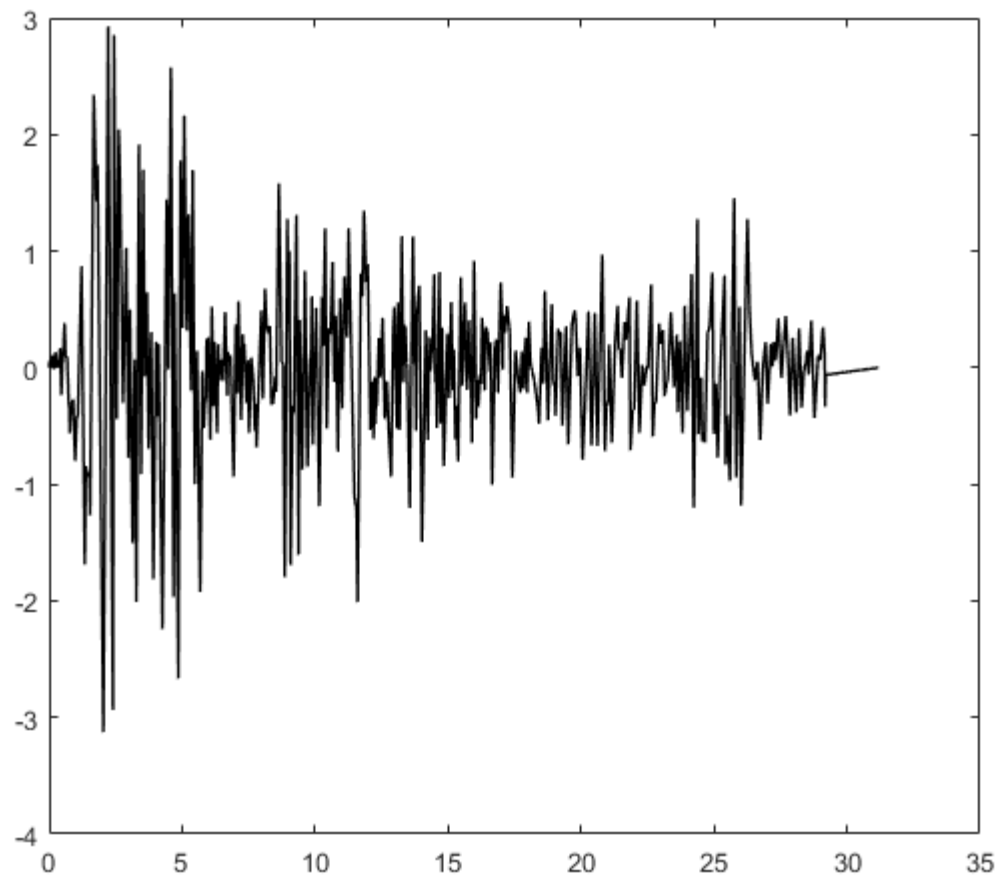
```
figure()
plot(S1.time,S1.disp,'k','LineWidth',1)
drawnow;
pause(0.1)
```



```
figure()
plot(S1.time,S1.vel,'k','LineWidth',1)
drawnow;
pause(0.1)
```



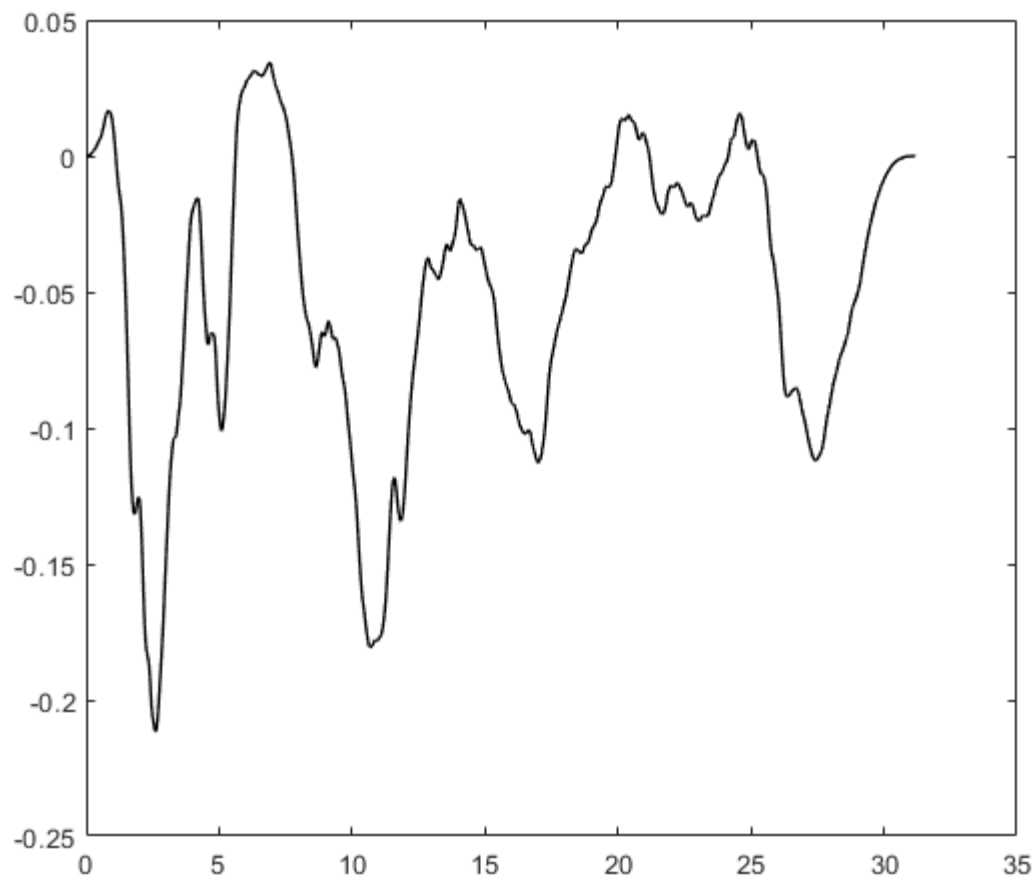
```
figure()  
plot(S1.time,S1.acc,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



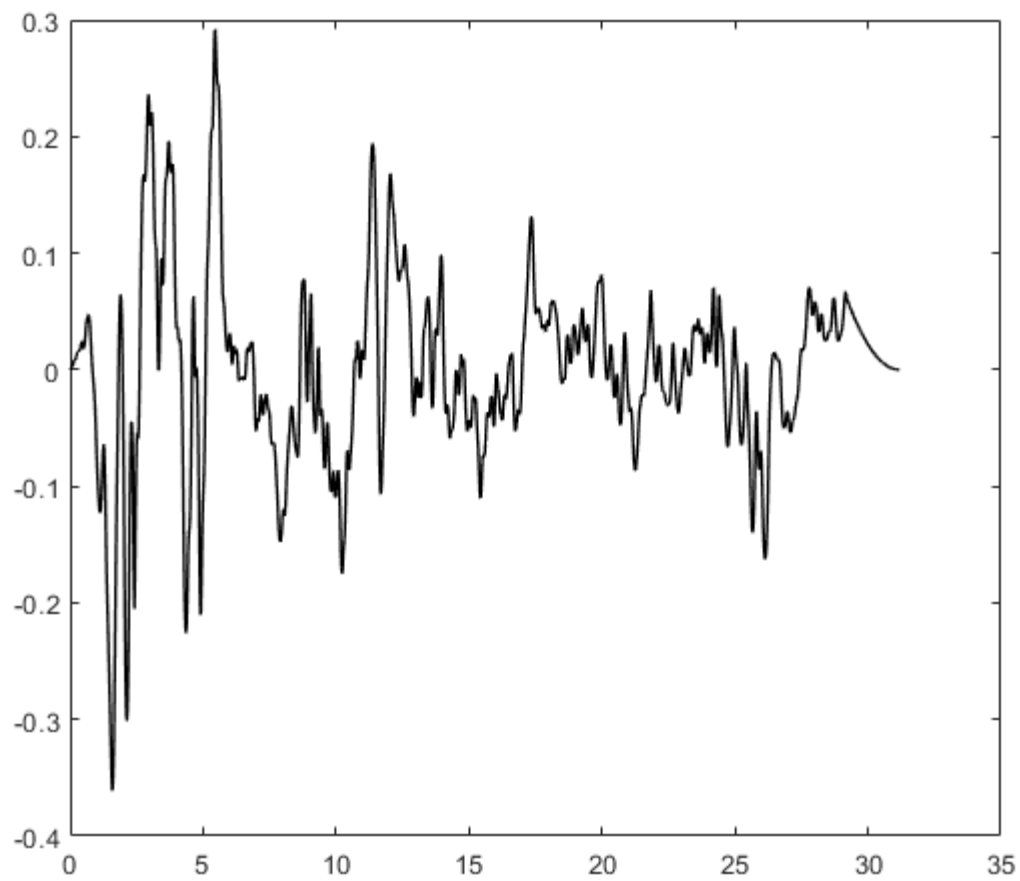
Time histories with baseline correction

```
sw='timehist';  
baselineSw=true;  
S2=OpenSeismoMatlab(dt,xgtt,sw,baselineSw);
```

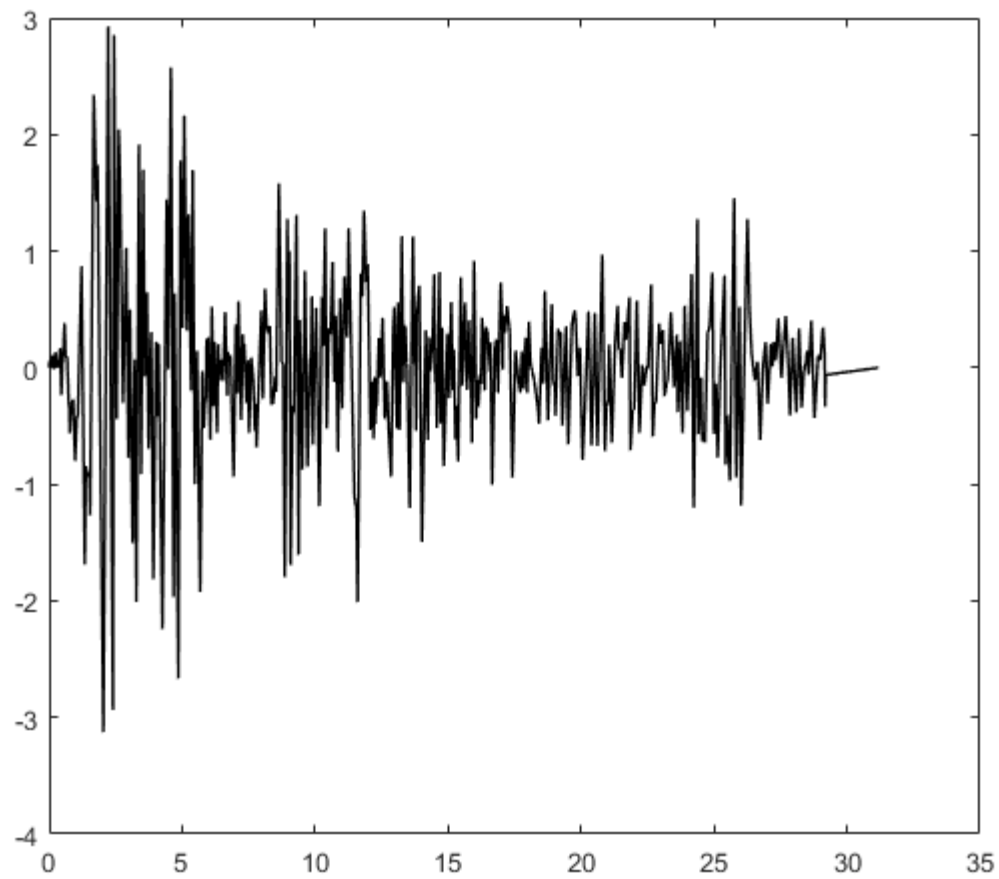
```
figure()  
plot(S2.time,S2.disp,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



```
figure()
plot(S2.time,S2.vel,'k','LineWidth',1)
drawnow;
pause(0.1)
```



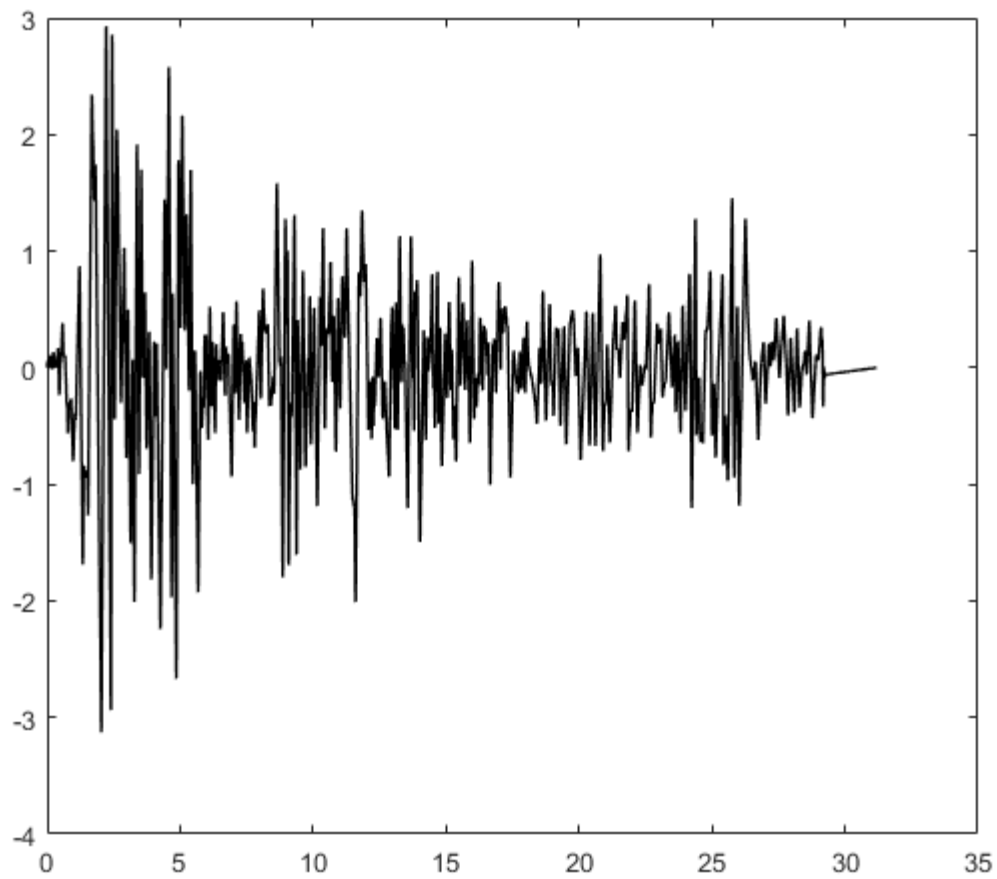
```
figure()  
plot(S2.time,S2.acc,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



Resample acceleration time history from 0.02 sec to 0.01 sec.

```
sw='resample';  
dti=0.01;  
S3=OpenSeismoMatlab(dt,xgtt,sw,dti);
```

```
figure()  
plot(S3.time,S3.acc,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



PGA

```
sw='pga';  
S4=OpenSeismoMatlab(dt,xgtt,sw);
```

```
S4.PGA
```

```
ans =
```

```
3.1276242
```

PGV

```
sw='pgv';  
S5=OpenSeismoMatlab(dt,xgtt,sw);
```

```
S5.PGV
```

```
ans =
```


0.360920691

PGD

```
sw='pgd';  
S6=OpenSeismoMatlab(dt,xgtt,sw);
```

```
S6.PGD
```

```
ans =
```

```
0.211893410160001
```

Total cumulative energy, Arias intensity and significant duration

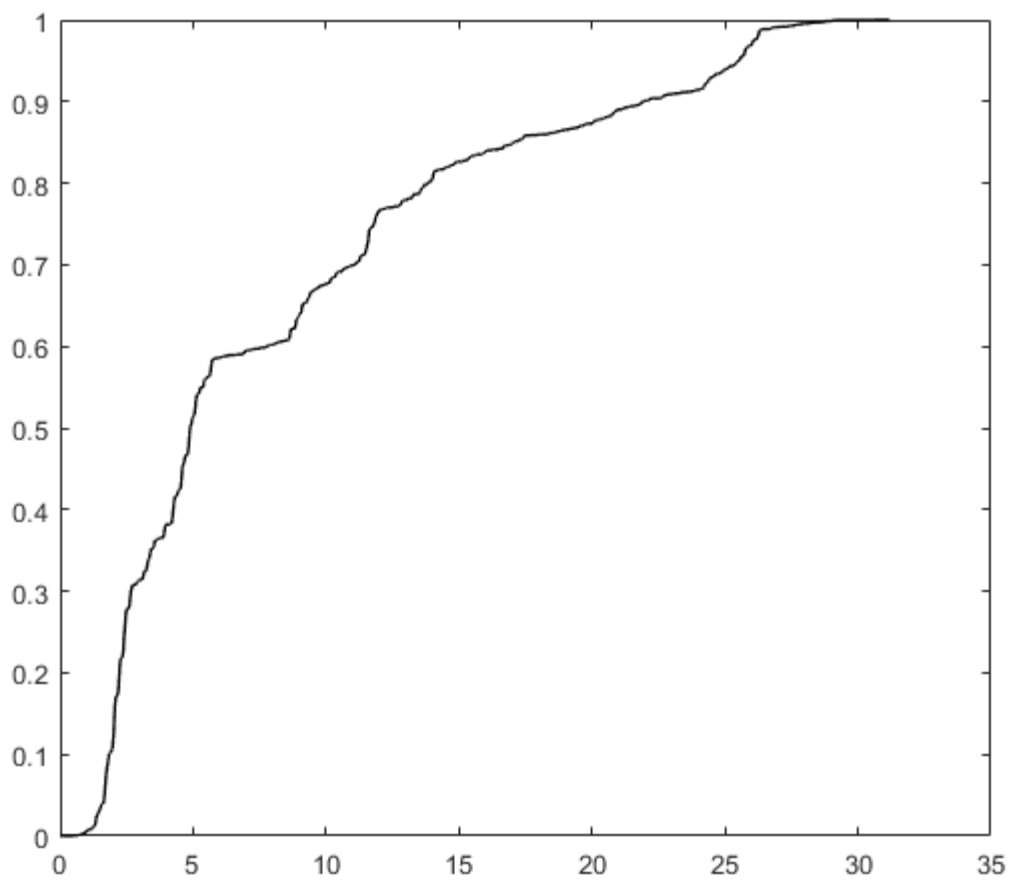
```
sw='arias';  
S7=OpenSeismoMatlab(dt,xgtt,sw);
```

```
S7.Ecum
```

```
ans =
```

```
11.251388628142
```

```
figure()  
plot(S7.time,S7.EcumTH,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



S7.t_5_95

ans =

1.68

25.5

S7.Td_5_95

ans =

23.84

S7.t_5_75

ans =

1.68

11.8

```
S7.Td_5_75
```

```
ans =
```

```
10.14
```

```
S7.arias
```

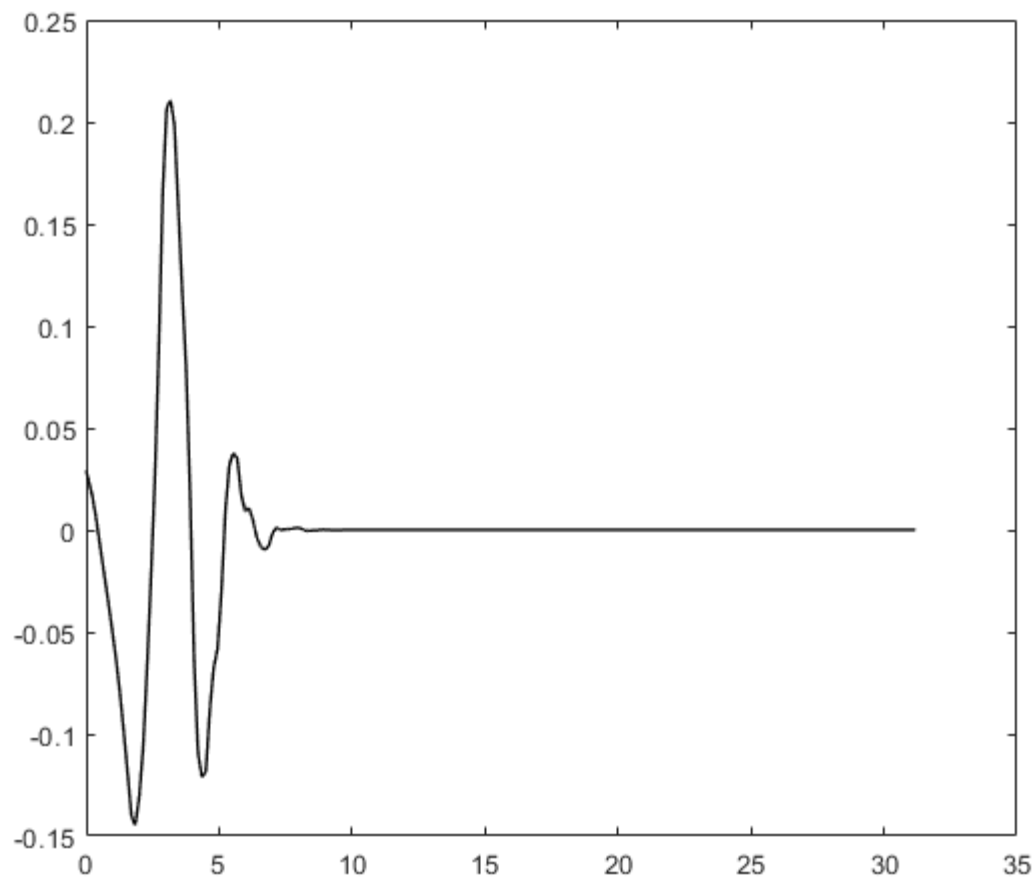
```
ans =
```

```
1.80159428424335
```

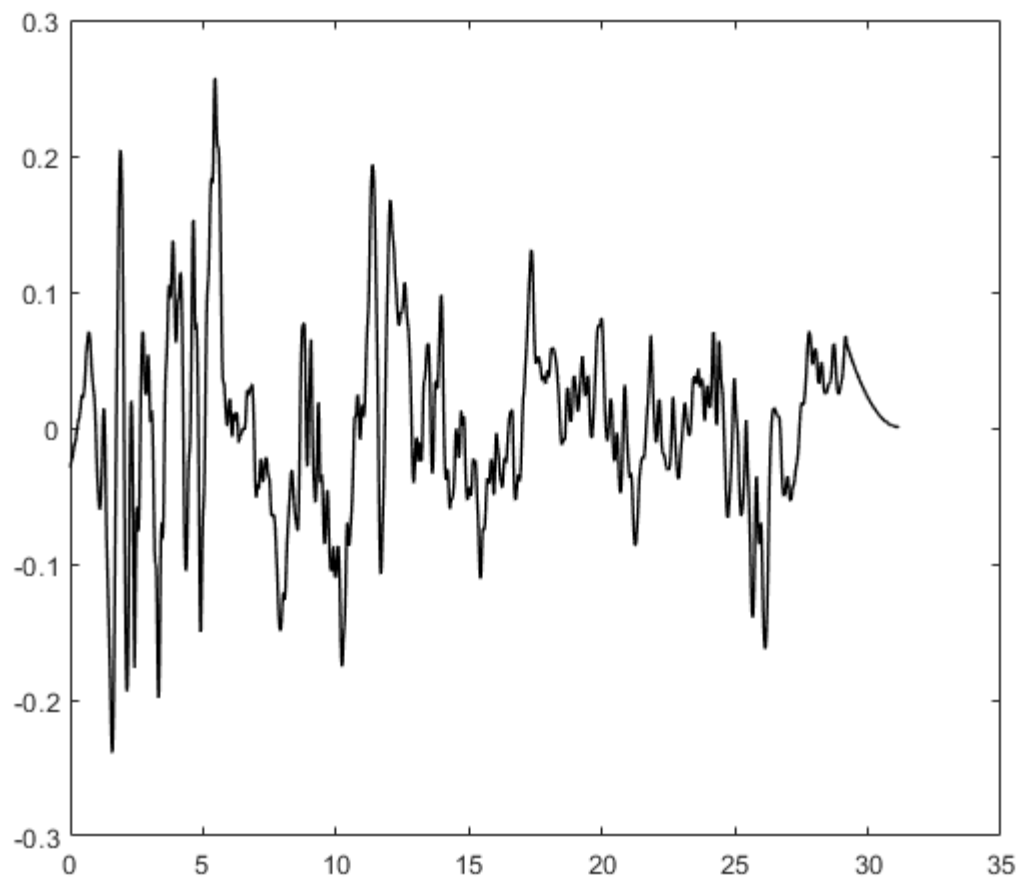
Pulse decomposition

```
xgt=S1.vel;  
sw='pulsedecomp';  
S8=OpenSeismoMatlab(dt,xgt,sw);
```

```
figure()  
plot(S8.time,S8.pulseTH,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



```
figure()  
plot(S8.time,S8.resTH,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



S8.Tp

ans =

3.304

S8.wavScale

ans =

118

S8.wavCoefs

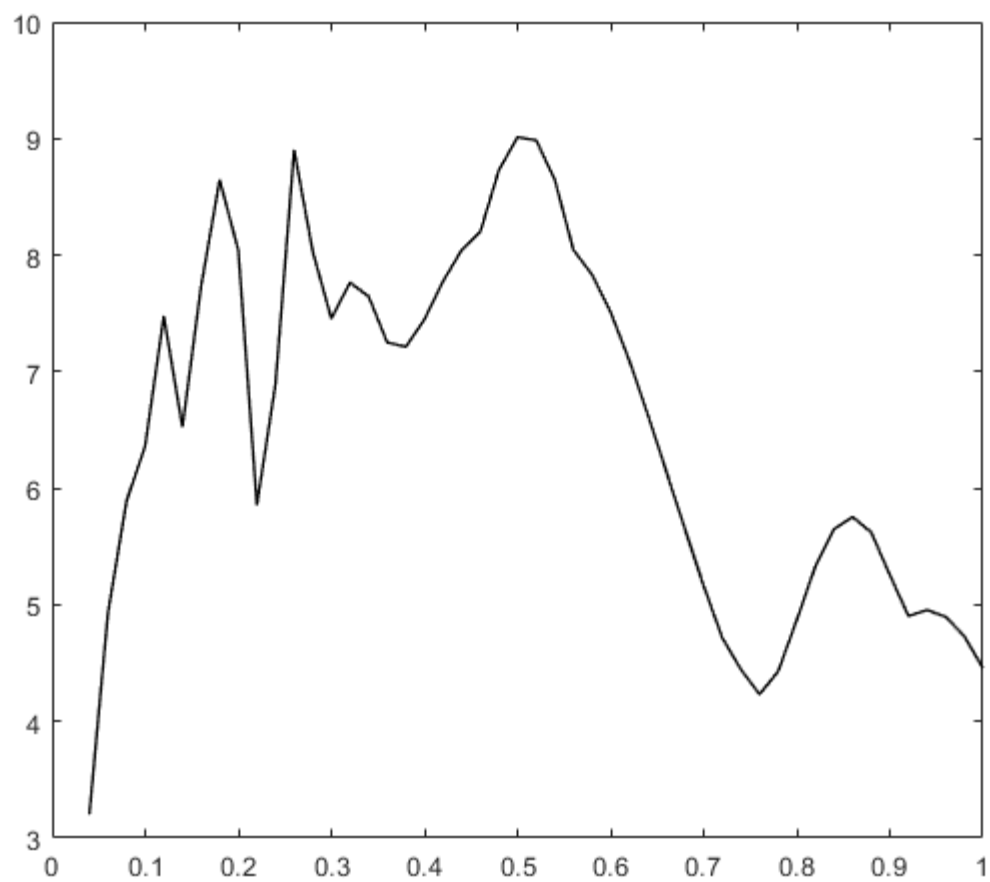
ans =

1.71247132221248

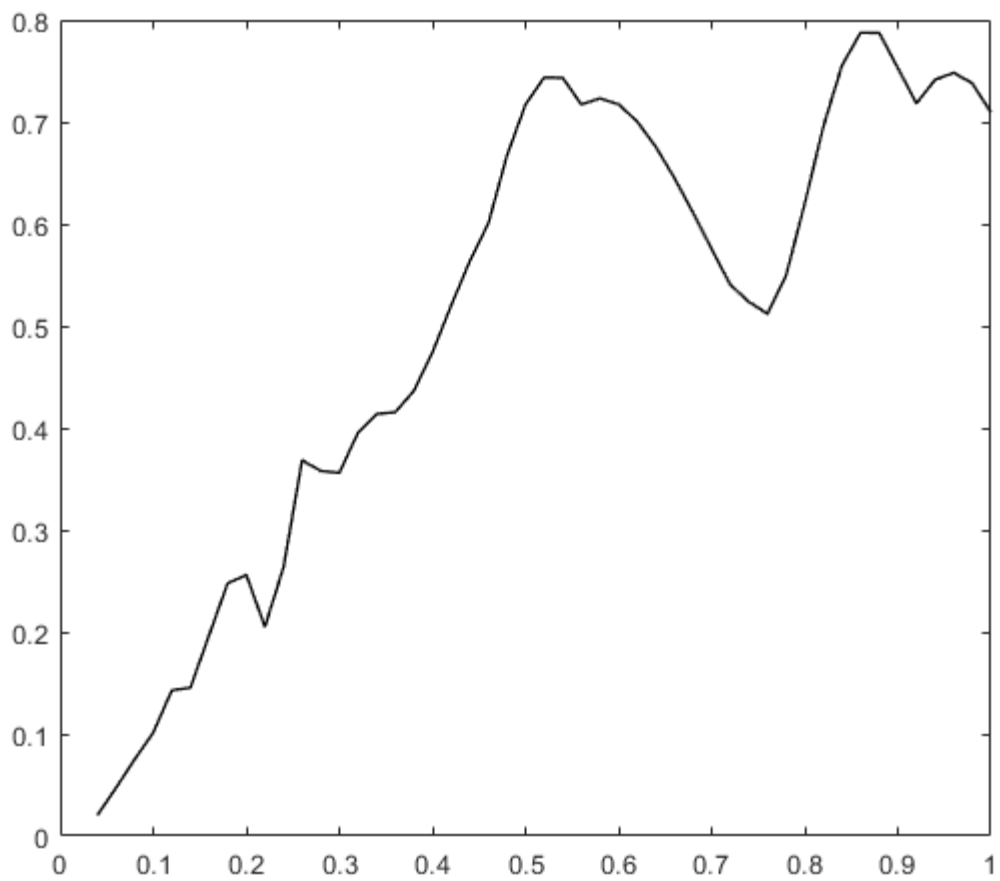
Linear elastic response spectra and pseudospectra

```
sw='elrs';  
ksi=0.05;  
T=0.04:0.02:1;  
S9=OpenSeismoMatlab(dt,xgtd,sw,T,ksi);
```

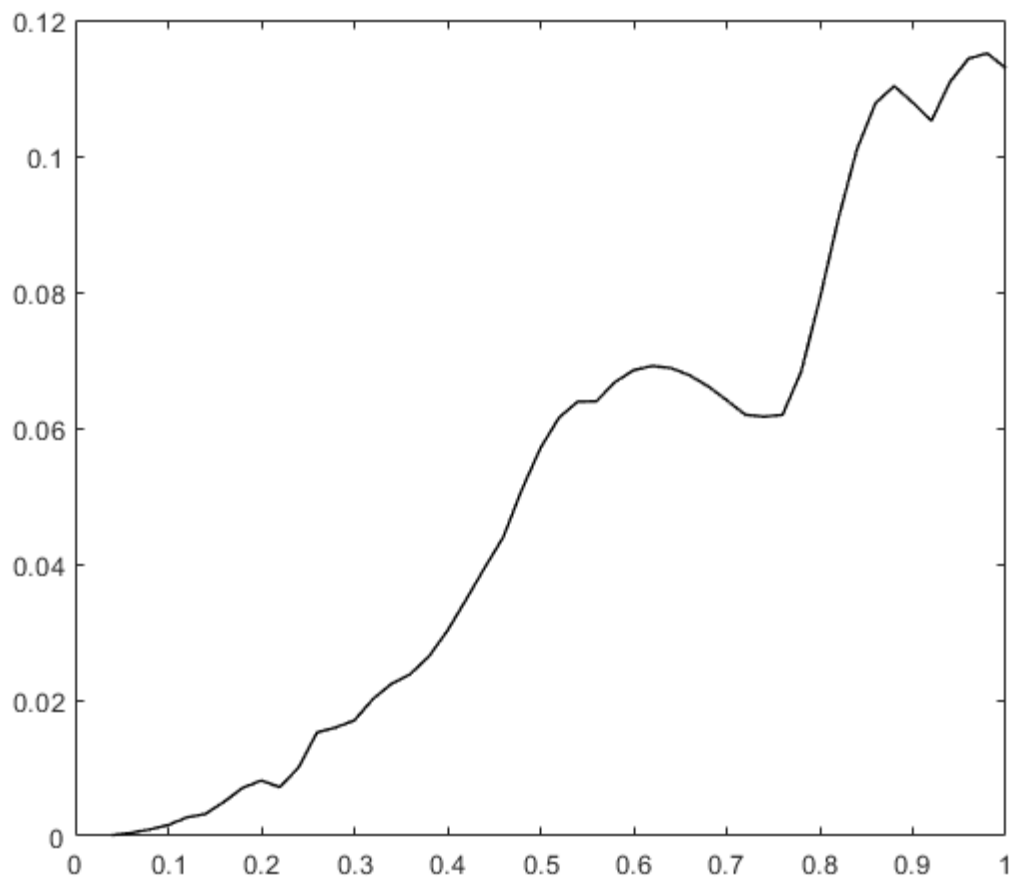
```
figure()  
plot(S9.Period,S9.PSa,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



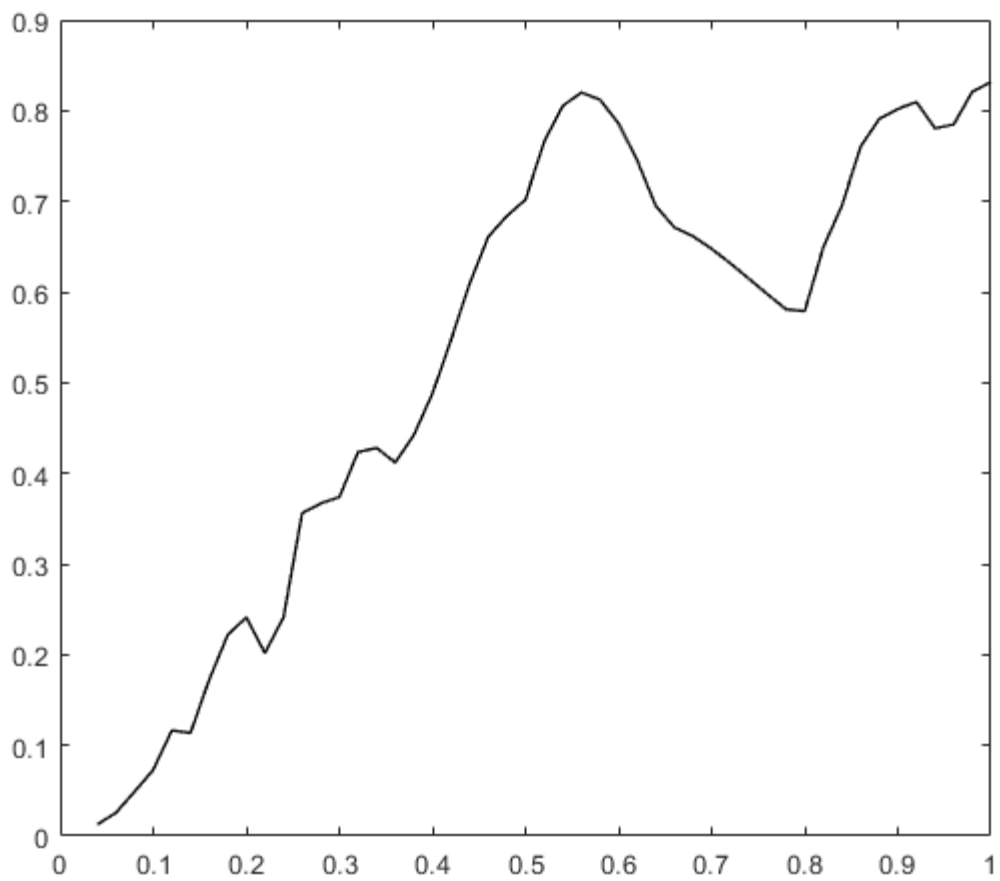
```
figure()  
plot(S9.Period,S9.PSv,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



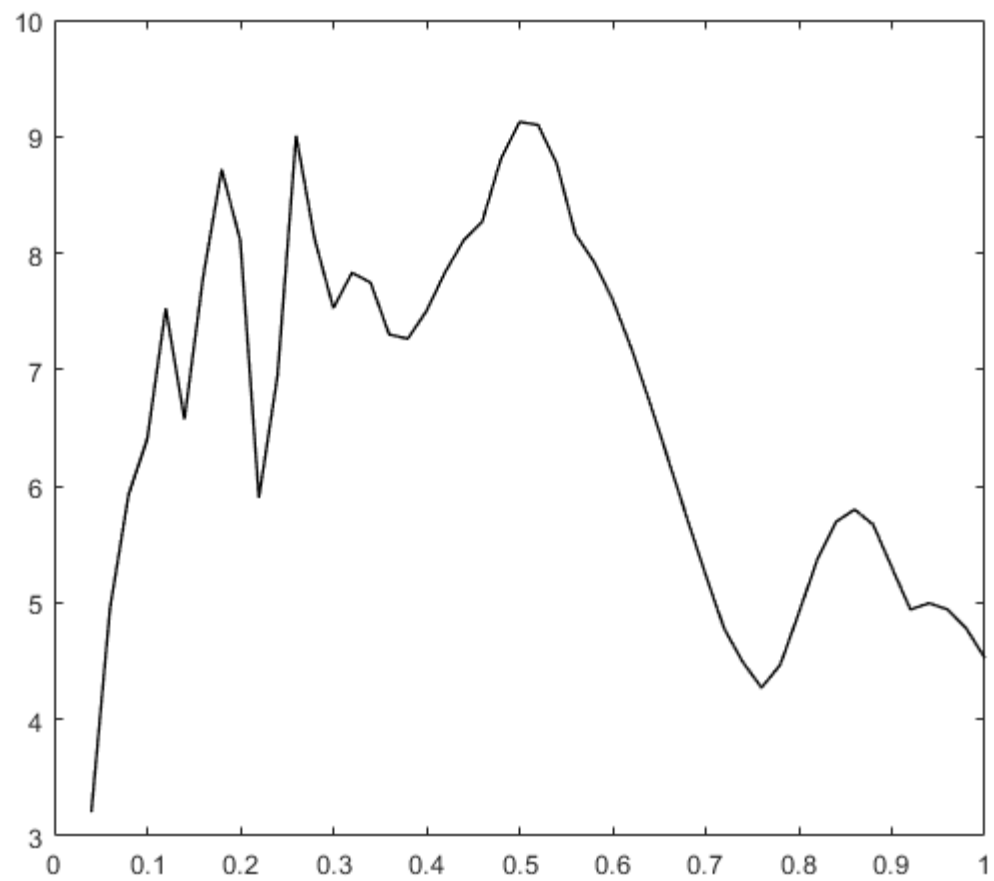
```
figure()  
plot(S9.Period,S9.Sd,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



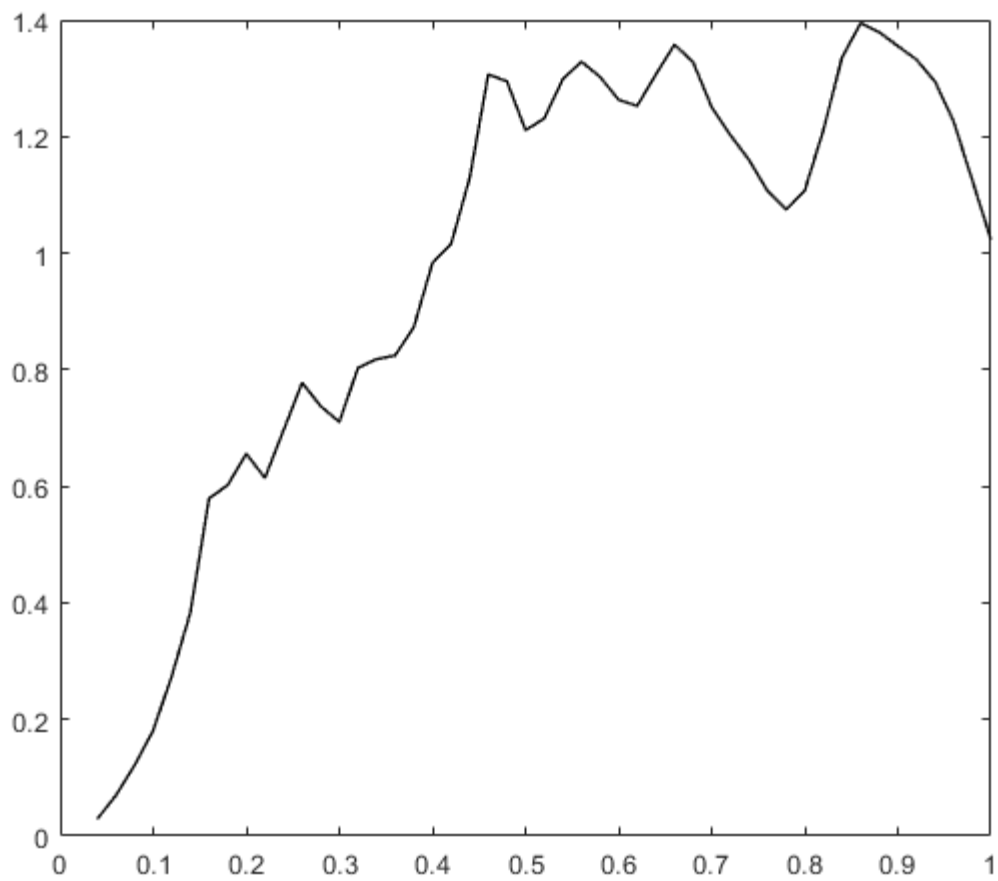
```
figure()  
plot(S9.Period,S9.Sv,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```

```
figure()  
plot(S9.Period,S9.Sa,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



```
figure()  
plot(S9.Period,S9.Siev,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



```
S9.PredPSa
```

```
ans =
```

```
9.01181525615902
```

```
S9.PredPeriod
```

```
ans =
```

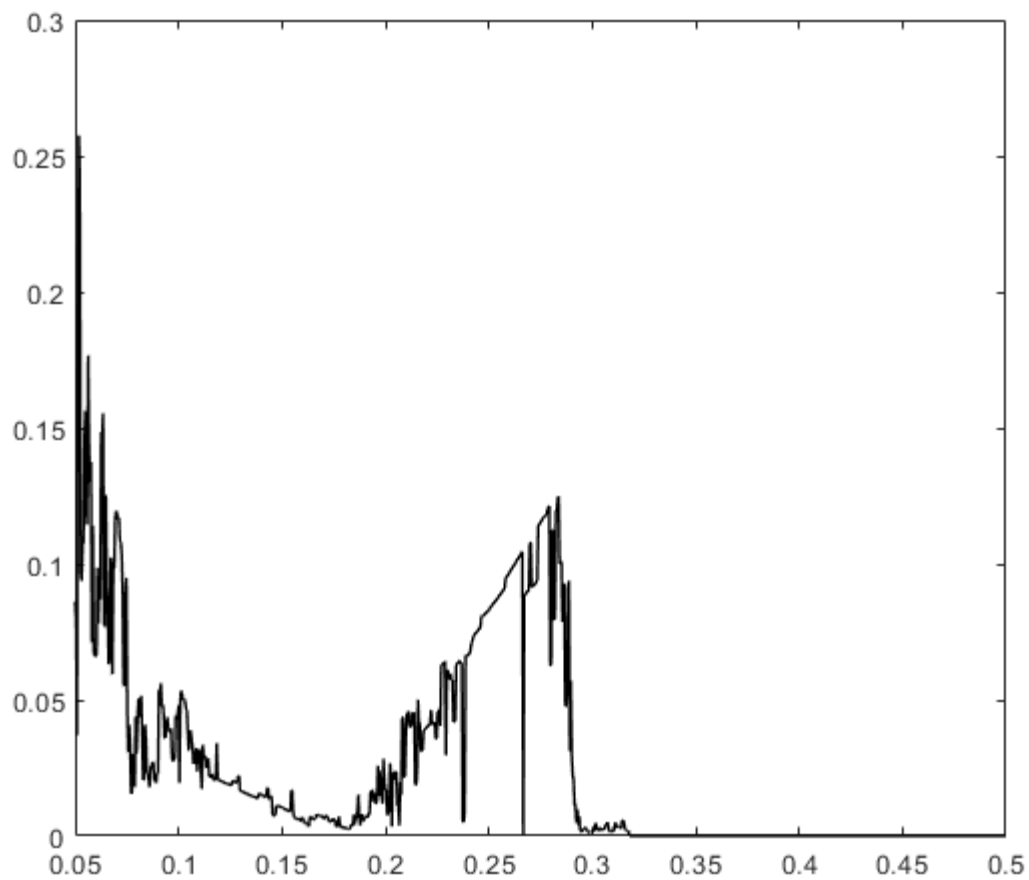
```
0.5
```

Rigid plastic sliding displacement response spectra

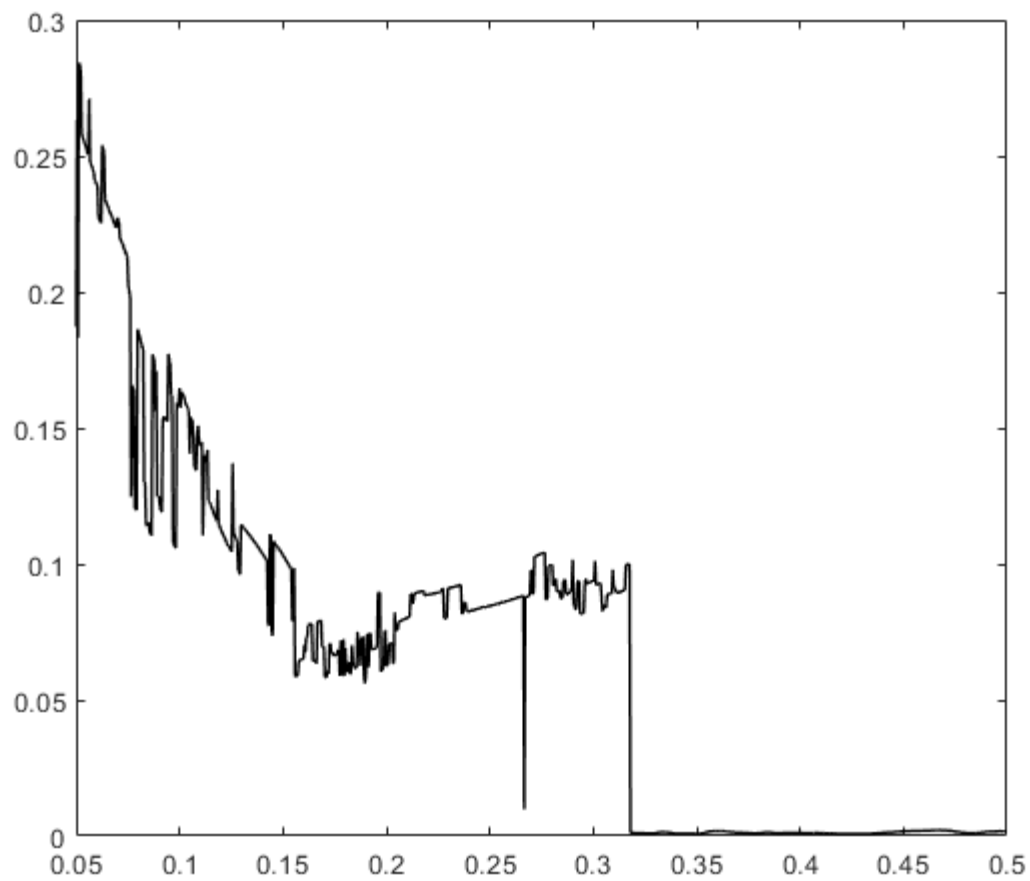
```
sw='rpsrs';  
S10=OpenSeismoMatlab(dt,xgtd,sw);
```

```
figure()
```

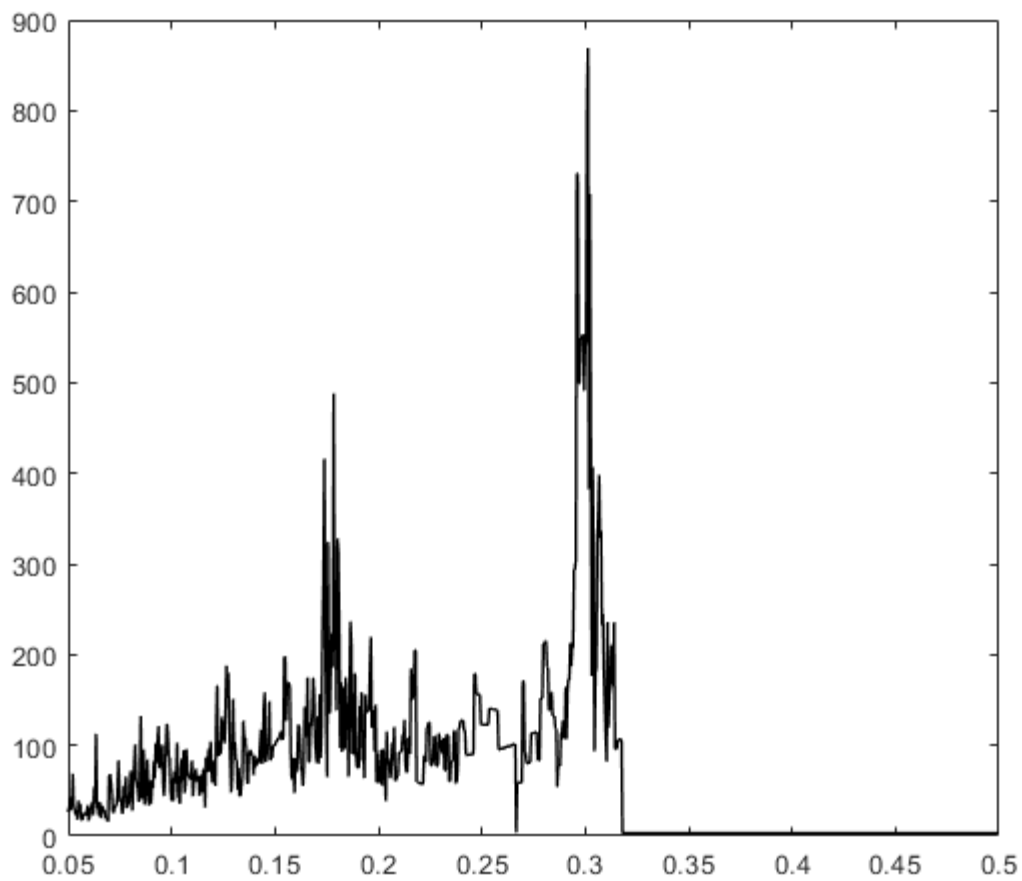
```
plot(S10.CF,S10.RPSSd,'k','LineWidth',1)
drawnow;
pause(0.1)
```



```
figure()
plot(S10.CF,S10.RPSSv,'k','LineWidth',1)
drawnow;
pause(0.1)
```



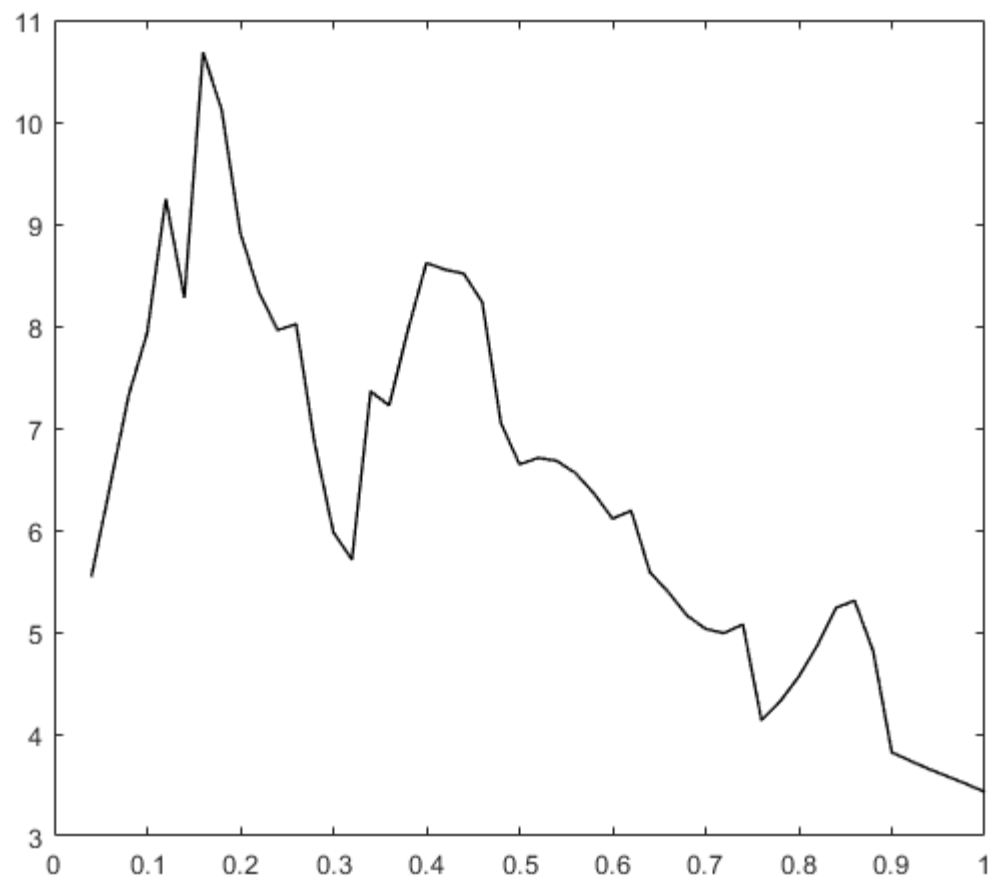
```
figure()  
plot(S10.CF,S10.RPSSa,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



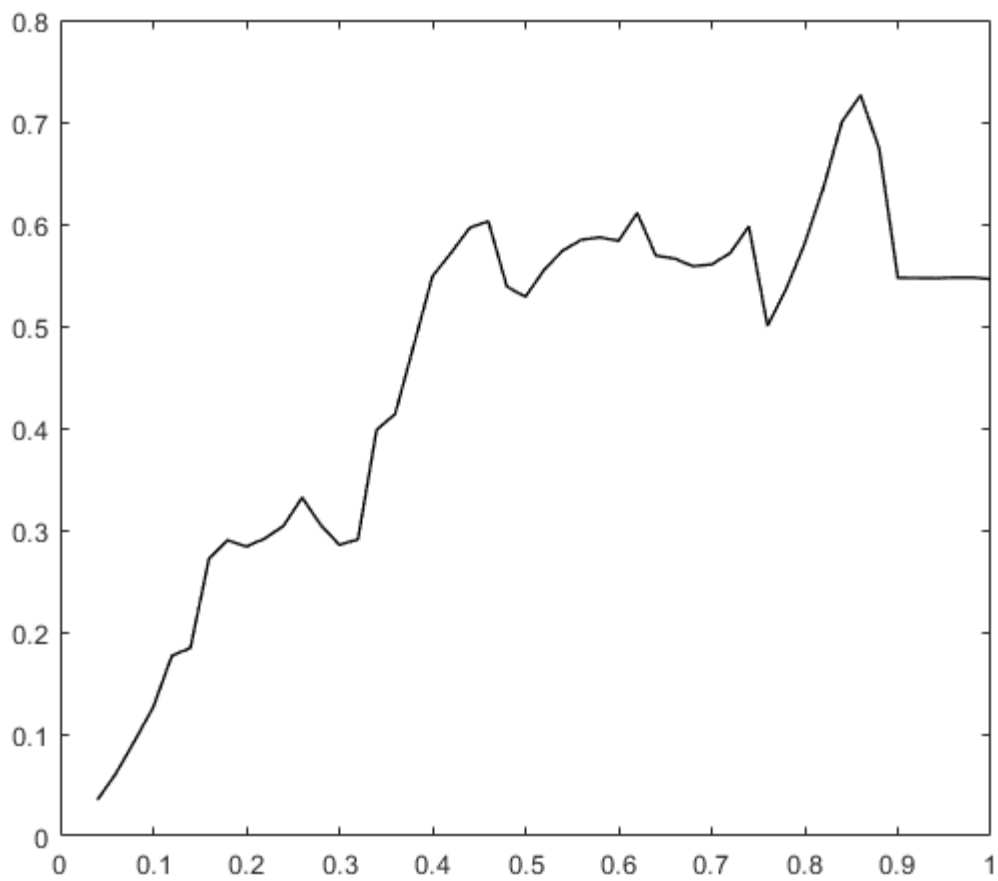
Constant ductility response spectra and pseudospectra

```
sw='cdrs';  
ksi=0.05;  
T=0.04:0.02:1;  
mu=2;  
S11=OpenSeismoMatlab(dt,xgtd,sw,T,ksi,mu);
```

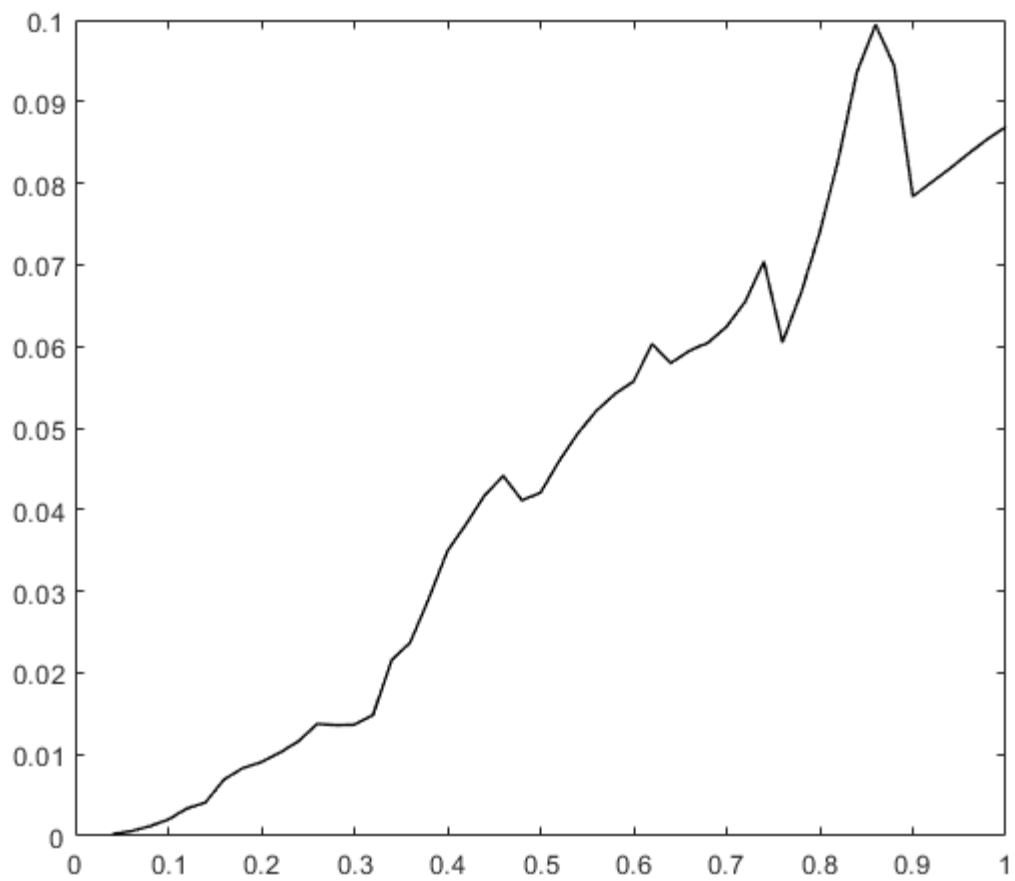
```
figure()  
plot(S11.Period,S11.CDPSa,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



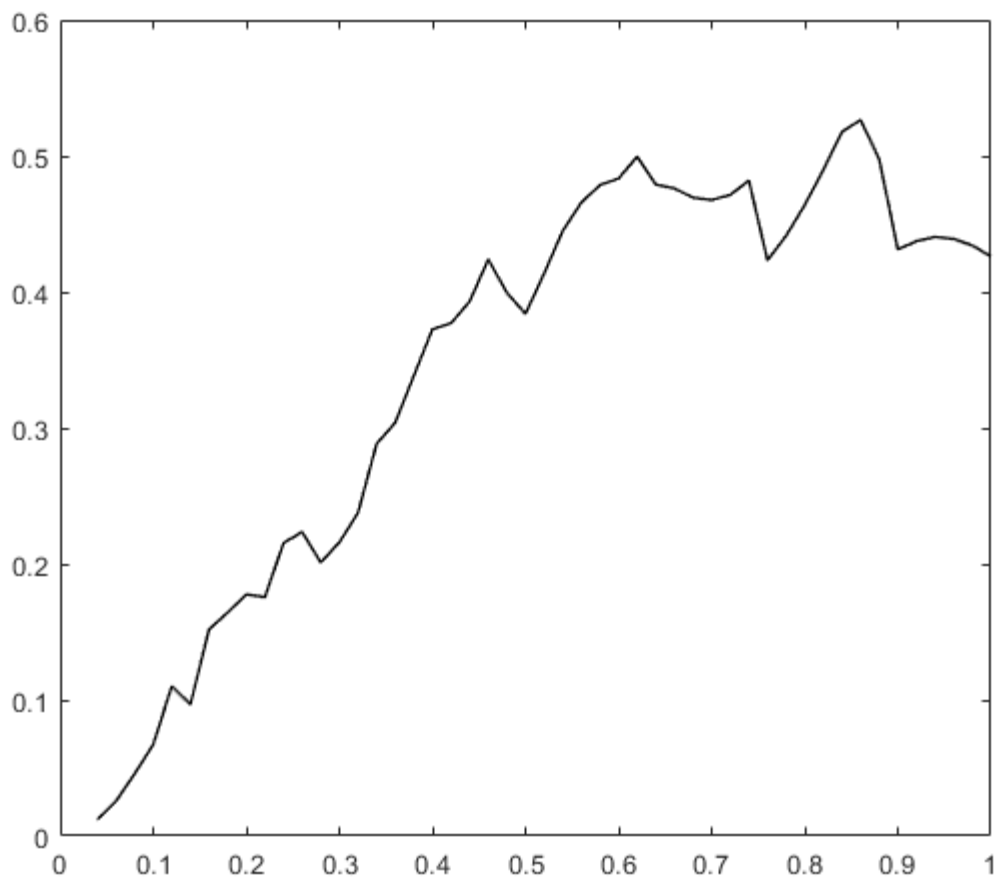
```
figure()  
plot(S11.Period,S11.CDPSv,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



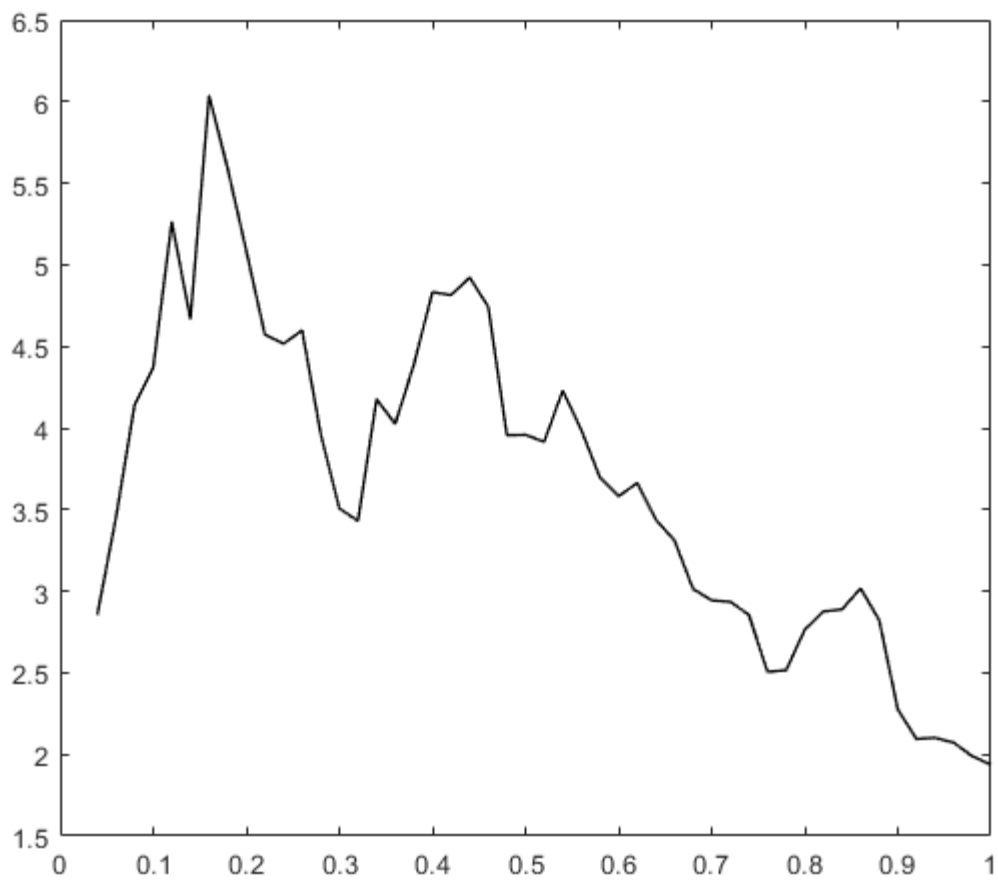
```
figure()  
plot(S11.Period,S11.CDSd,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```

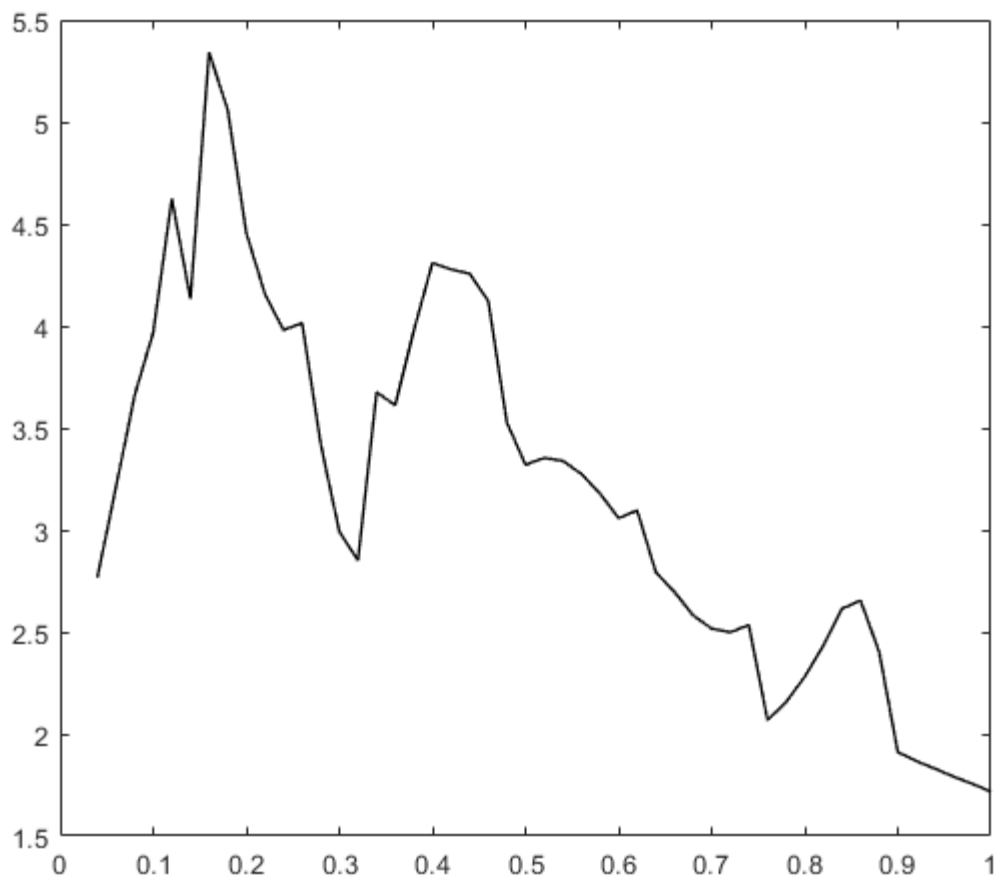
```
figure()  
plot(S11.Period,S11.CDSv,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



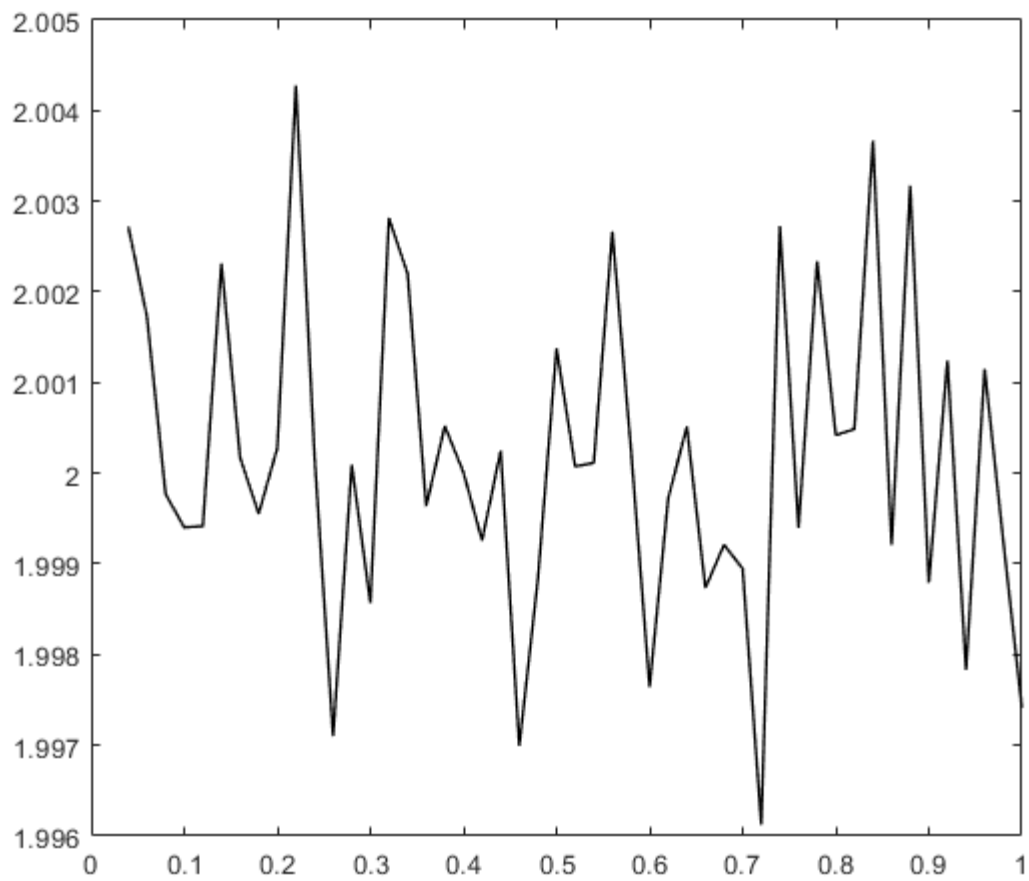
```
figure()  
plot(S11.Period,S11.CDSa,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



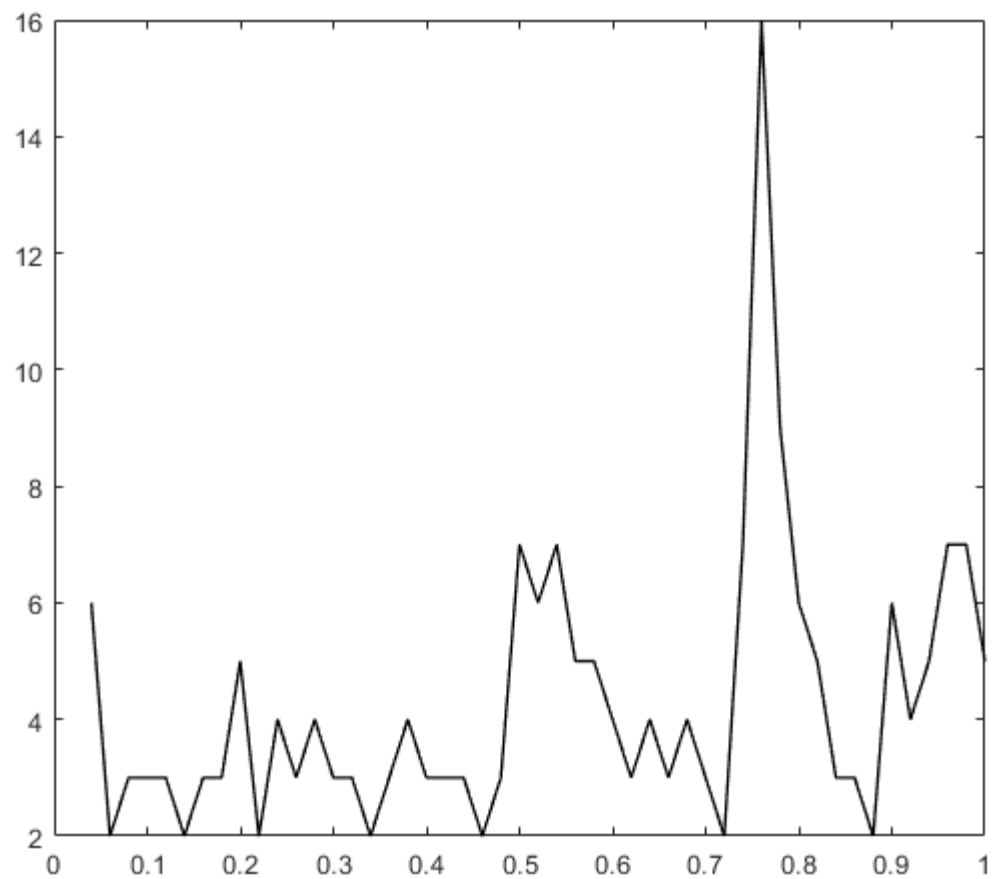
```
figure()  
plot(S11.Period,S11.fyK,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



```
figure()  
plot(S11.Period,S11.muK,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



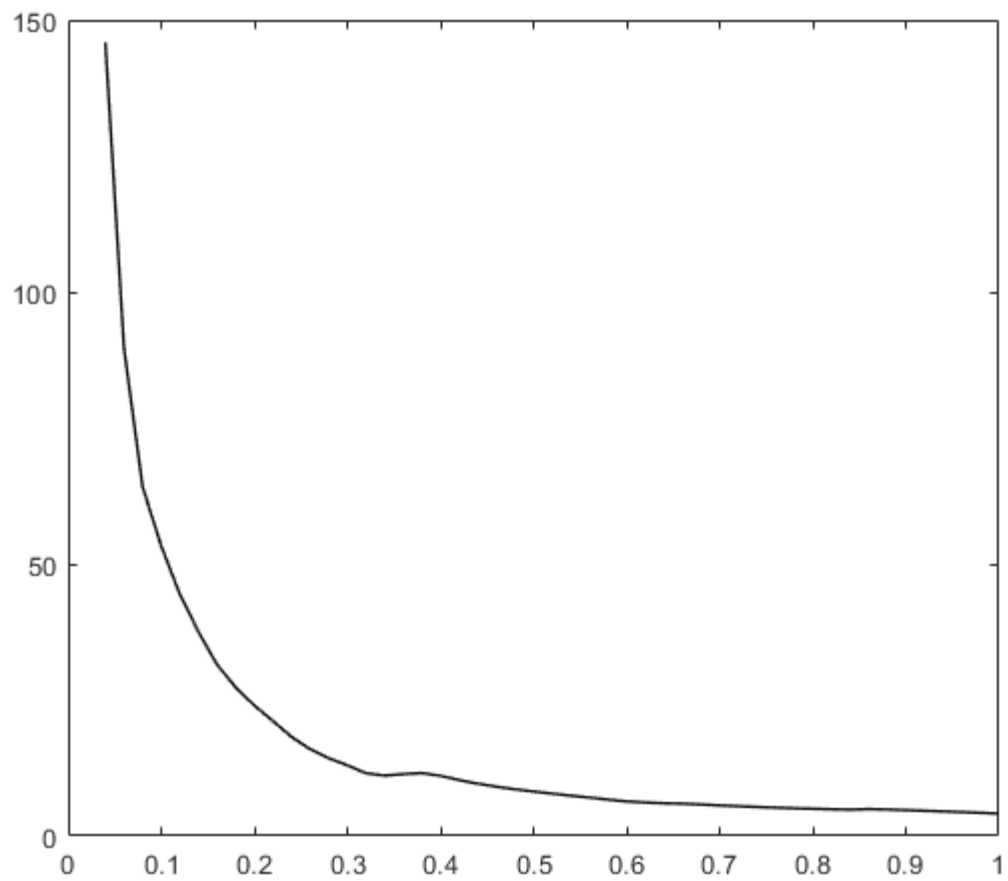
```
figure()  
plot(S11.Period,S11.iterK,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



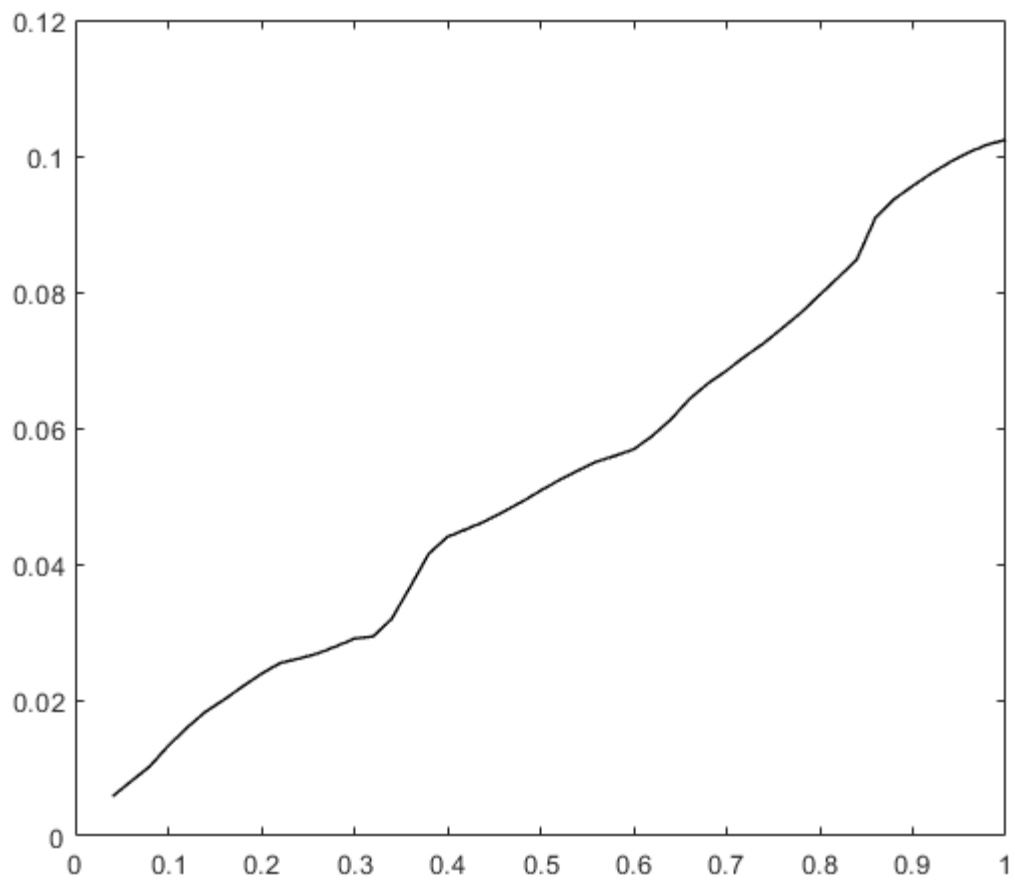
Constant strength response spectra

```
sw='csrs';  
ksi=0.05;  
T=0.04:0.02:1;  
fyR=0.1;  
S12=OpenSeismoMatlab(dt,xgtt,sw,T,ksi,fyR);
```

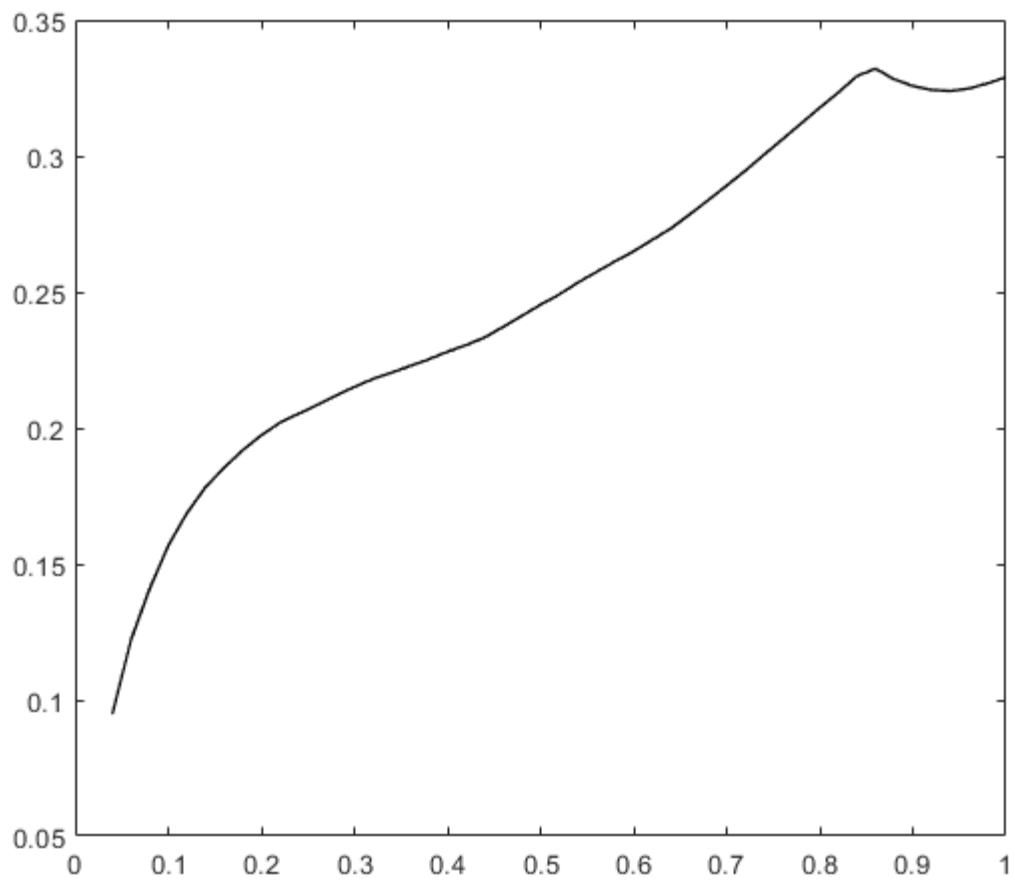
```
figure()  
plot(S12.Period,S12.CSSmu,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



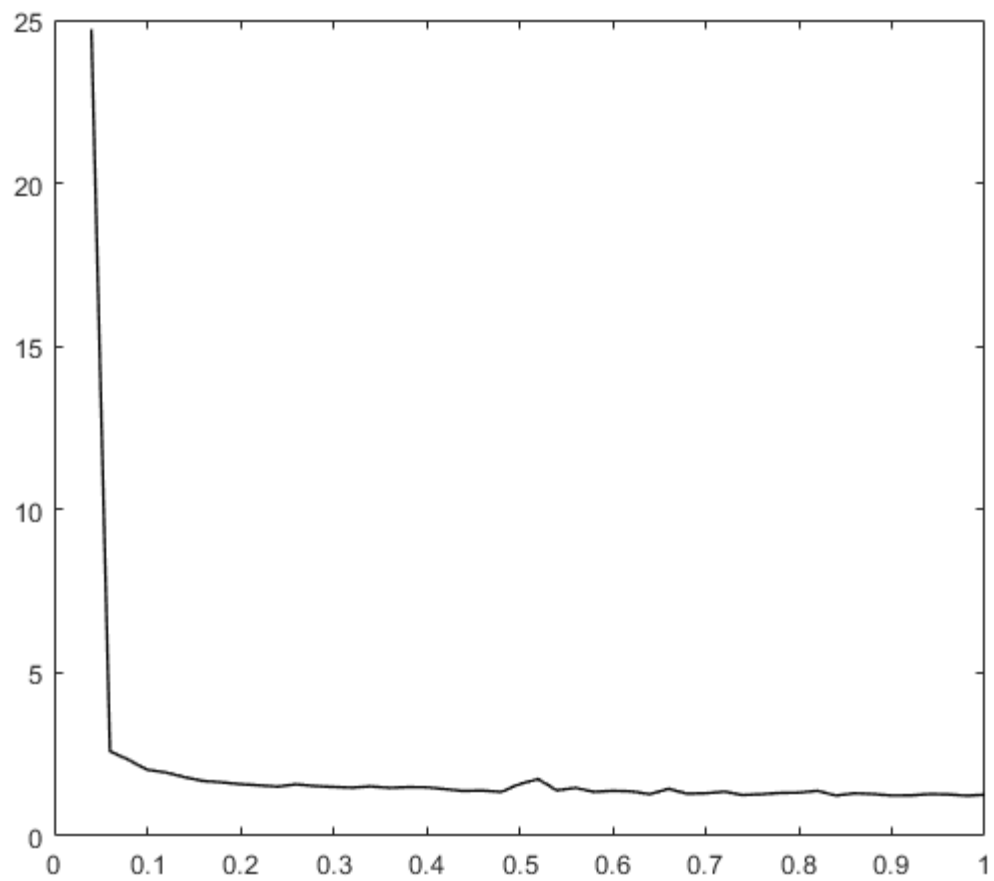
```
figure()  
plot(S12.Period,S12.CSSd,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



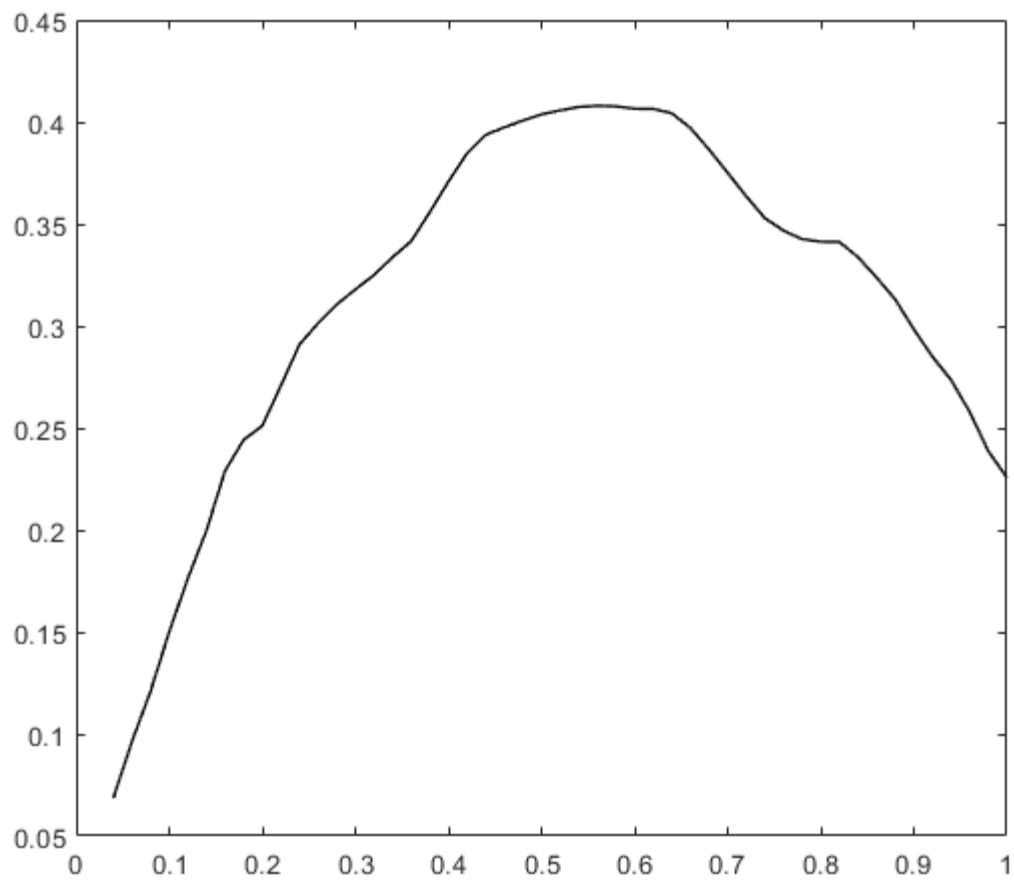
```
figure()  
plot(S12.Period,S12.CSSv,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```

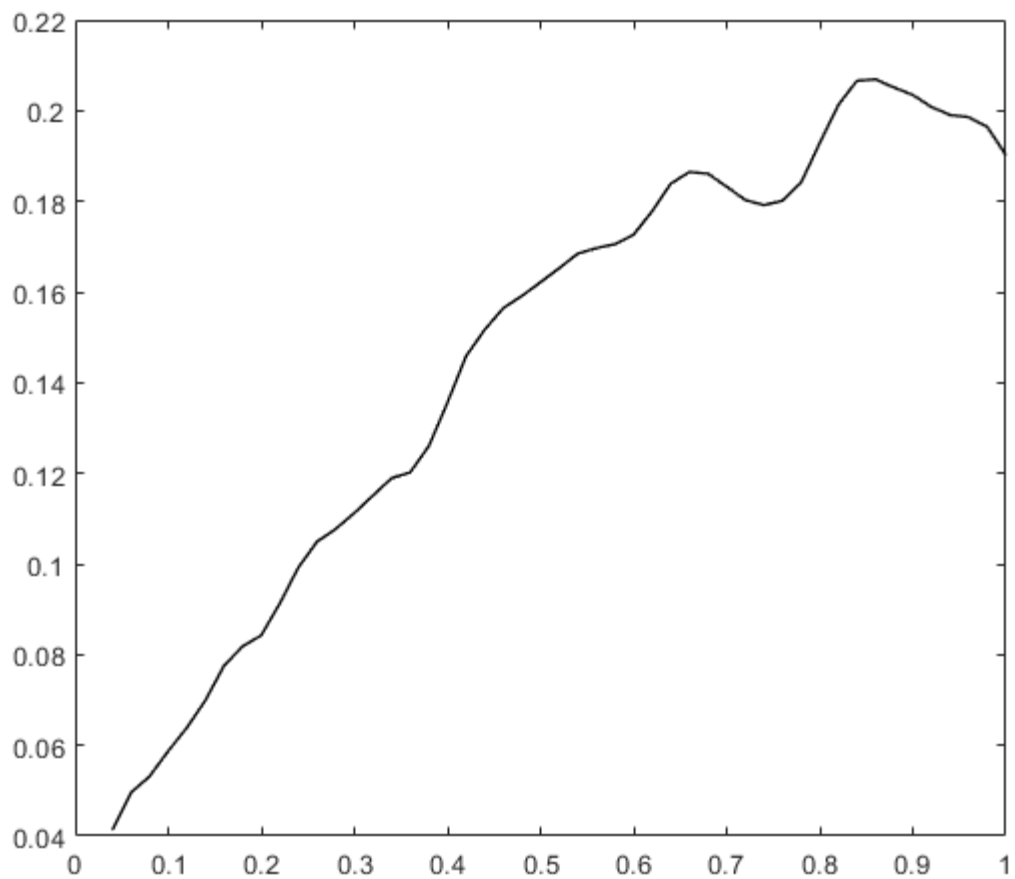
```
figure()  
plot(S12.Period,S12.CSSa,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



```
figure()  
plot(S12.Period,S12.CSSey,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



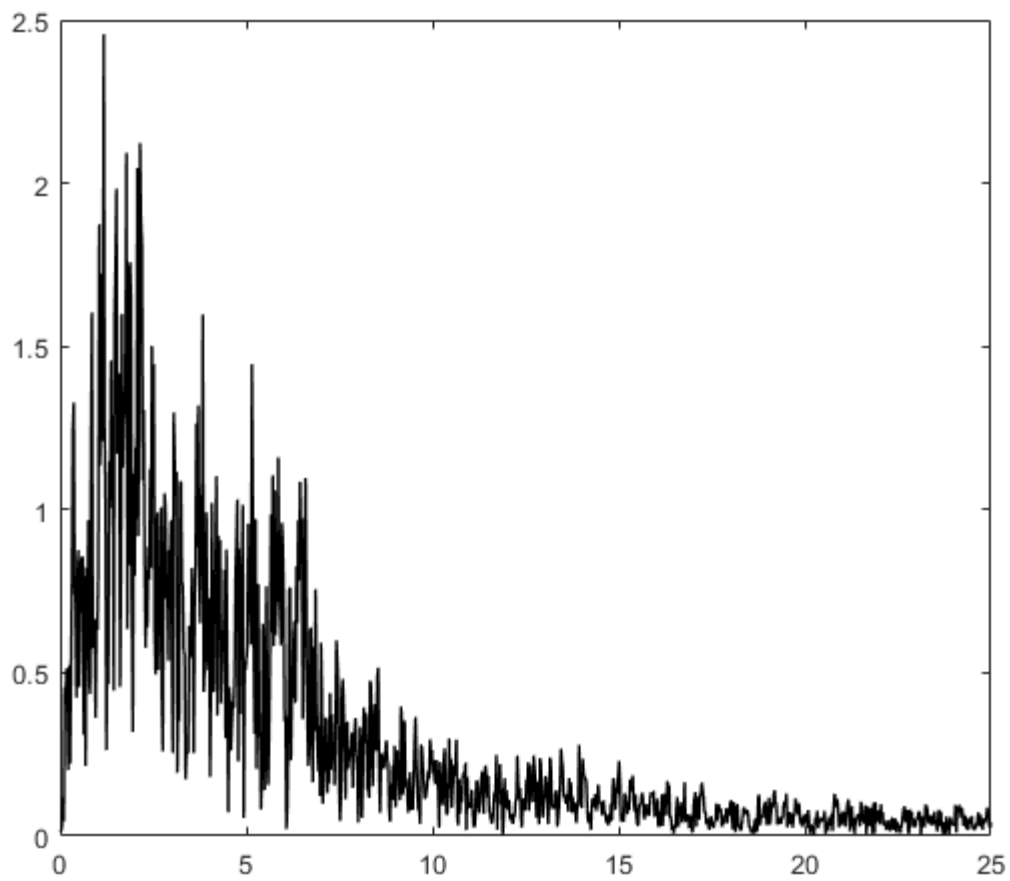
```
figure()  
plot(S12.Period,S12.CSSed,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



Fourier amplitude spectrum and mean period

```
sw='fas';  
S13=OpenSeismoMatlab(dt,xgtt,sw);
```

```
figure()  
plot(S13.freq,S13.FAS,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



S13.Tm

ans =

0.533389590787328

S13.Fm

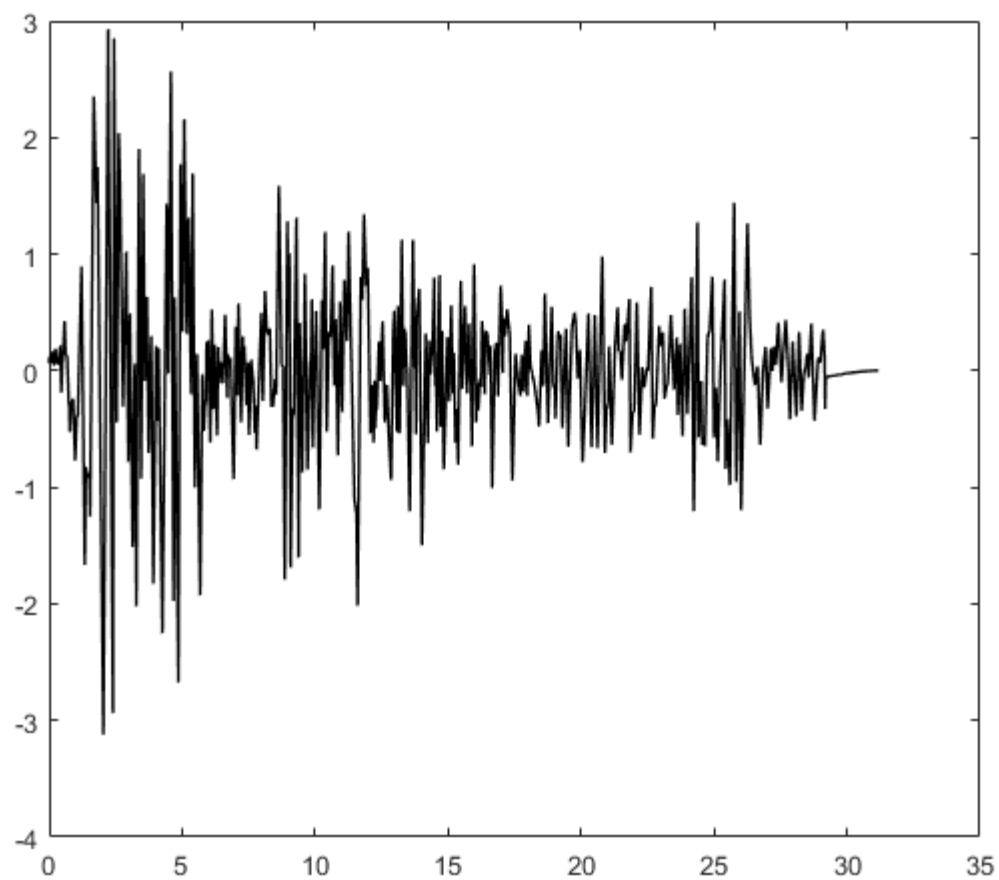
ans =

3.29375516366188

High pass Butterworth filter

```
sw='butterworthhigh';  
bOrder=4;  
flc=0.1;  
S14=OpenSeismoMatlab(dt,xgtt,sw,bOrder,flc);
```

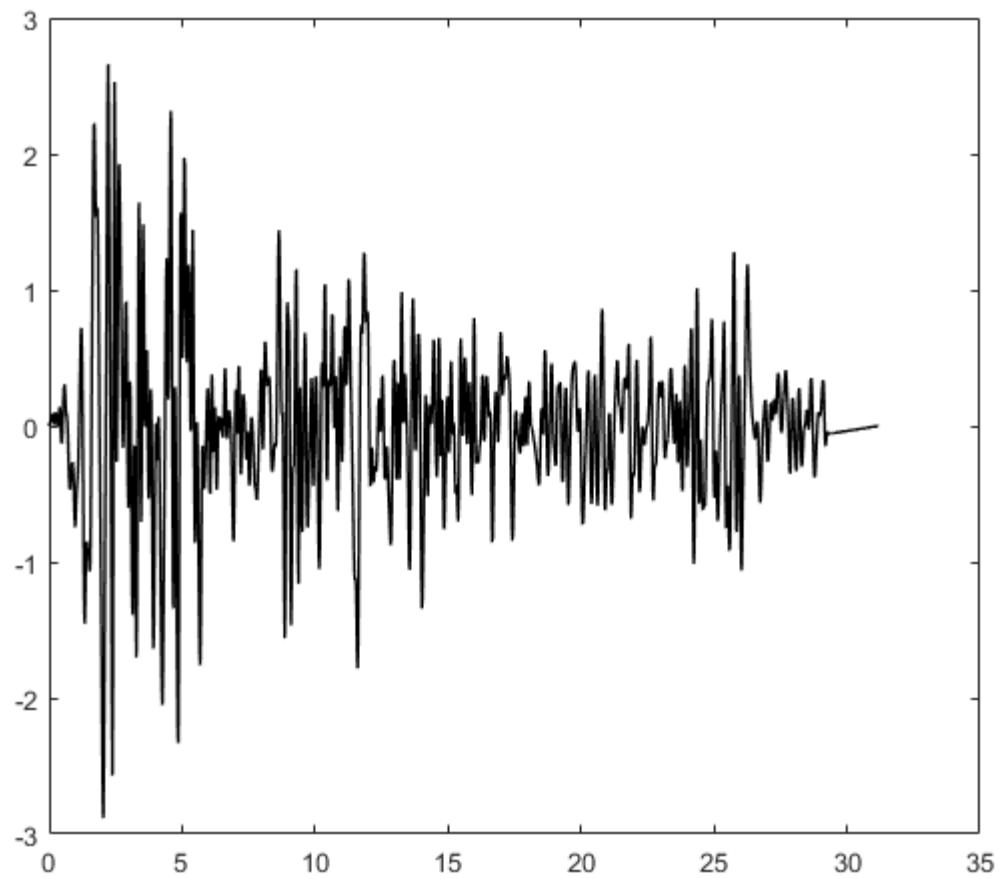
```
figure()
plot(S14.time,S14.acc,'k','LineWidth',1)
drawnow;
pause(0.1)
```



Low pass Butterworth filter

```
sw='butterworthlow';
bOrder=4;
fhc=10;
S15=OpenSeismoMatlab(dt,xgtt,sw,bOrder,fhc);
```

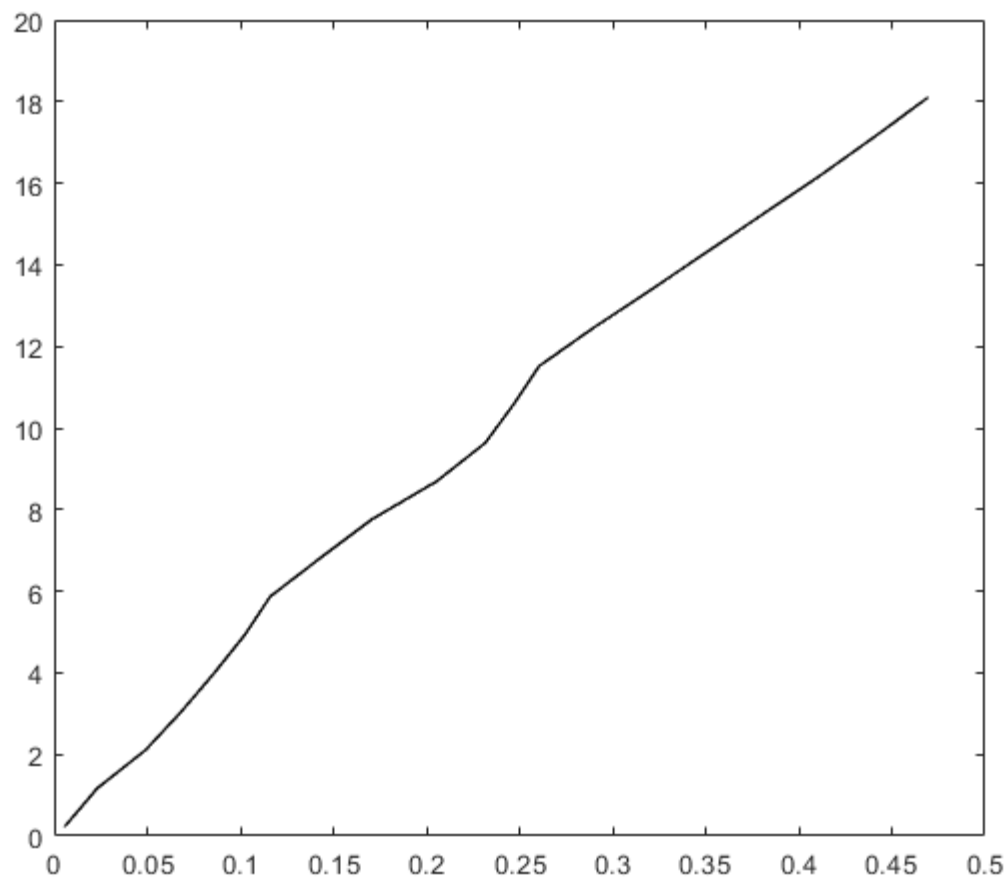
```
figure()
plot(S15.time,S15.acc,'k','LineWidth',1)
drawnow;
pause(0.1)
```



Incremental dynamic analysis

```
sw='ida';  
S16=OpenSeismoMatlab(dt,xgtt,sw);
```

```
figure()  
plot(S16.DM,S16.IM,'k','LineWidth',1)  
drawnow;  
pause(0.1)
```



Effective peak ground acceleration

```
sw='epga';  
S17=OpenSeismoMatlab(dt,xgtt,sw);
```

```
S17.EPGA
```

```
ans =  
  
3.09546779631066
```

Spectral intensity according to Housner (1952)

```
sw='sih1952';  
S18=OpenSeismoMatlab(dt,xgtt,sw);
```

```
S18.SI
```

```
ans =
```


1.24373311662318

Spectral intensity according to Nau & Hall (1984)

```
sw='sinh1984';  
S19=OpenSeismoMatlab(dt,xgtt,sw);
```

```
S19.SI
```

```
ans =
```

```
0.530561283239986
```

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- Major, Infrastructure Engineer, Hellenic Air Force
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example LEReSp

Calculate linear elastic response spectra in OpenSeismoMatlab

Contents

- [Generate earthquake motion](#)
- [Plot the generated time history](#)
- [Setup parameters for LEReSp function](#)
- [Calculate spectra and pseudospectra](#)
- [Plot the spectra and pseudospectra](#)
- [Copyright](#)

Generate earthquake motion

For reproducibility

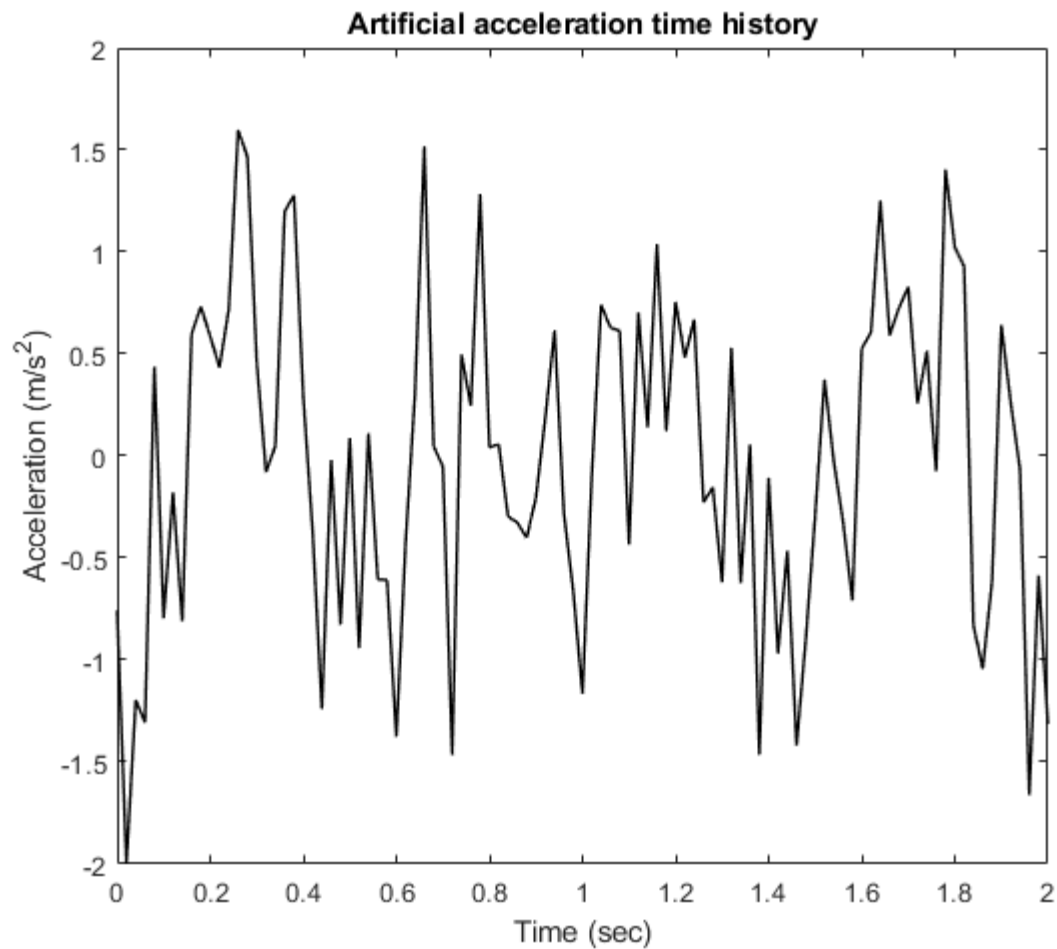
```
rng(0)
```

Generate earthquake acceleration time history

```
dt=0.02;  
N=10;  
a=rand(N,1)-0.5;  
b=100*pi*rand(N,1);  
c=pi*(rand(N,1)-0.5);  
t=(0:dt:(100*dt))';  
xgtt=zeros(size(t));  
for i=1:N  
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));  
end
```

Plot the generated time history

```
figure()  
plot(t,xgtt,'k','LineWidth',1)  
ylabel('Acceleration (m/s^2)')  
xlabel('Time (sec)')  
title('Artificial acceleration time history')  
drawnow;  
pause(0.1)
```



Setup parameters for LEReSp function

Eigenperiods

```
T=logspace(log10(0.02),log10(5),1000)';
```

Critical damping ratio

```
ksi=0.05;
```

Maximum ratio of the integration time step to the eigenperiod

```
dtTol=0.02;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Calculate spectra and pseudospectra

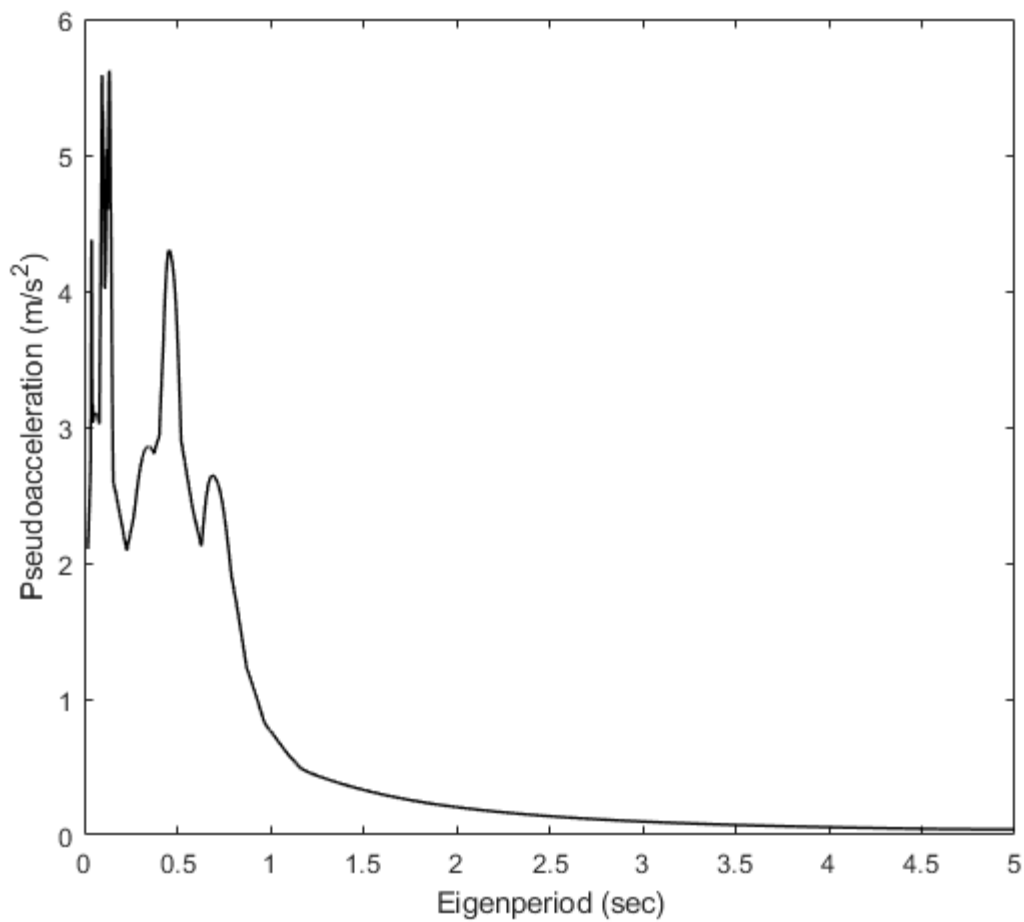
Apply LEReSp

```
[PSa,PSv,Sd,Sv,Sa,Siev]=LEReSp(dt,xgtd,T,ksi,dtTol,AlgID,rinf);
```

Plot the spectra and pseudospectra

Pseudoacceleration spectrum

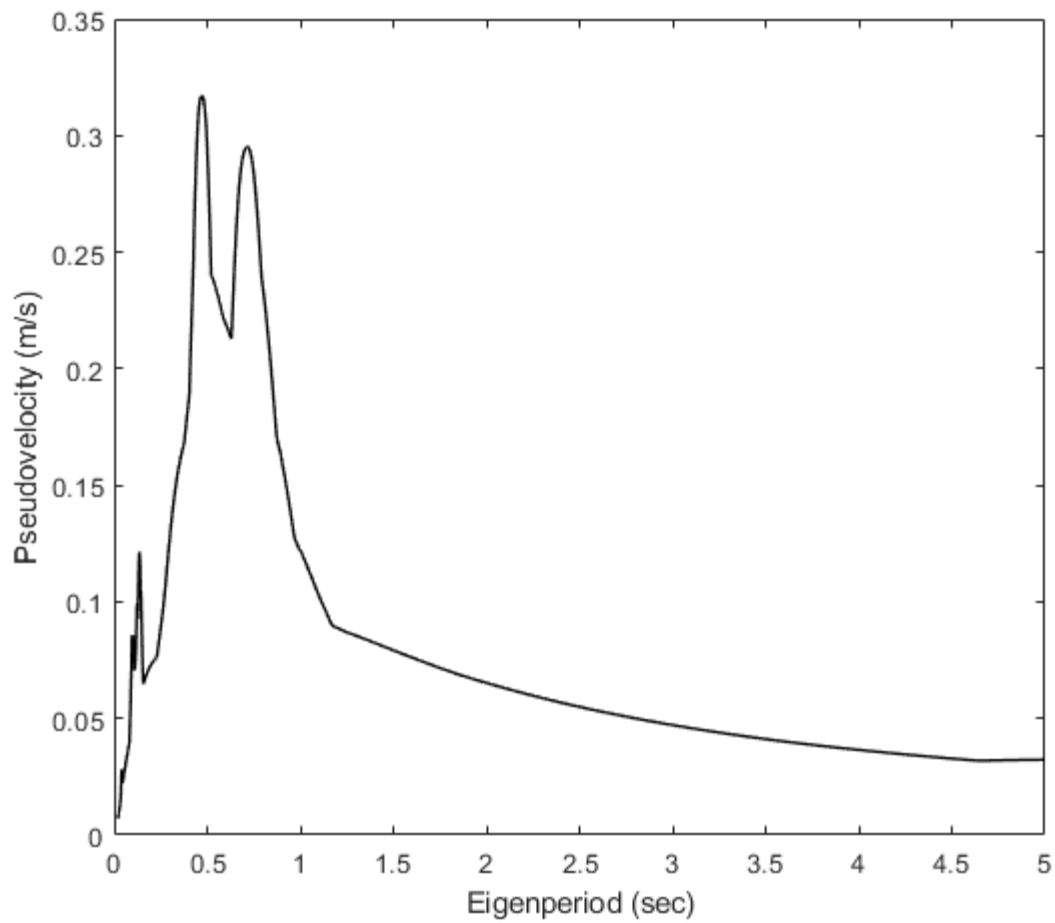
```
figure()  
plot(T,PSa,'k','LineWidth',1)  
ylabel('Pseudoacceleration (m/s^2)')  
xlabel('Eigenperiod (sec)')  
drawnow;  
pause(0.1)
```



Pseudovelocity spectrum

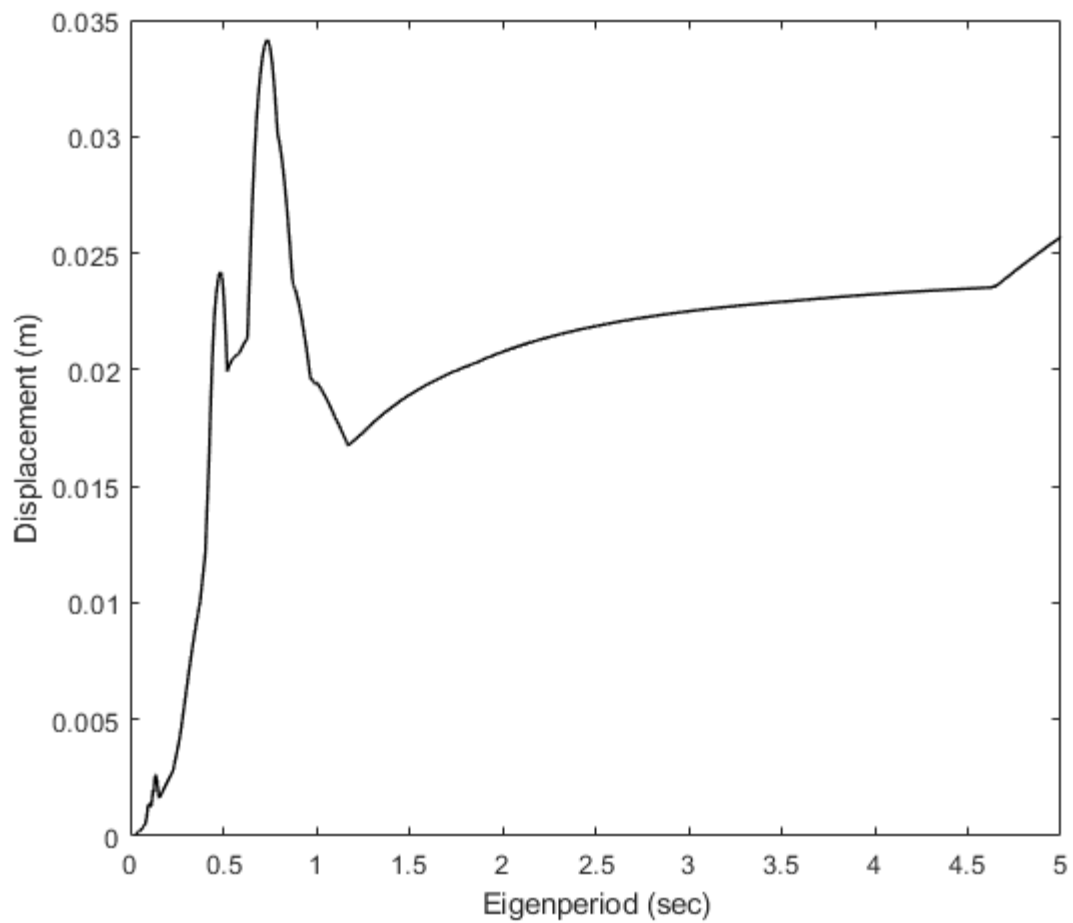
```
figure()  
plot(T,PSv,'k','LineWidth',1)
```

```
ylabel('Pseudovelocity (m/s)')
xlabel('Eigenperiod (sec)')
drawnow;
pause(0.1)
```



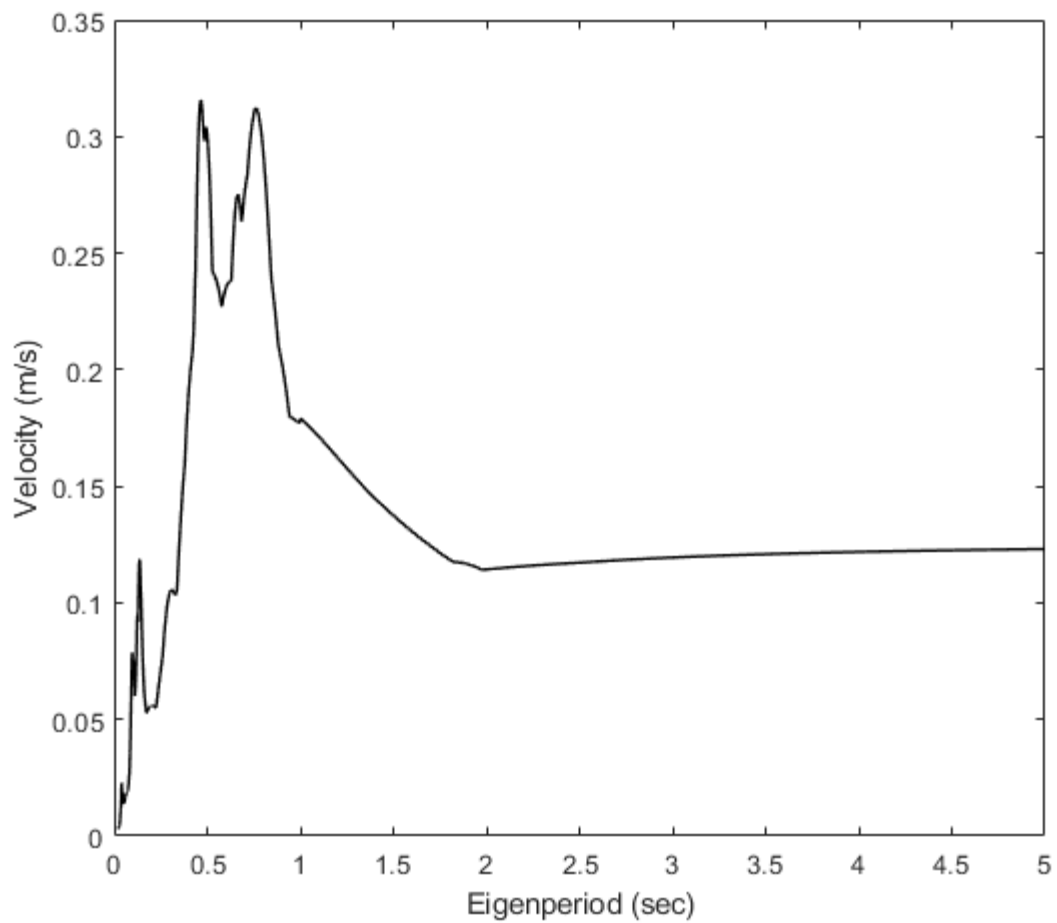
Displacement spectrum

```
figure()
plot(T,Sd,'k','LineWidth',1)
ylabel('Displacement (m)')
xlabel('Eigenperiod (sec)')
drawnow;
pause(0.1)
```



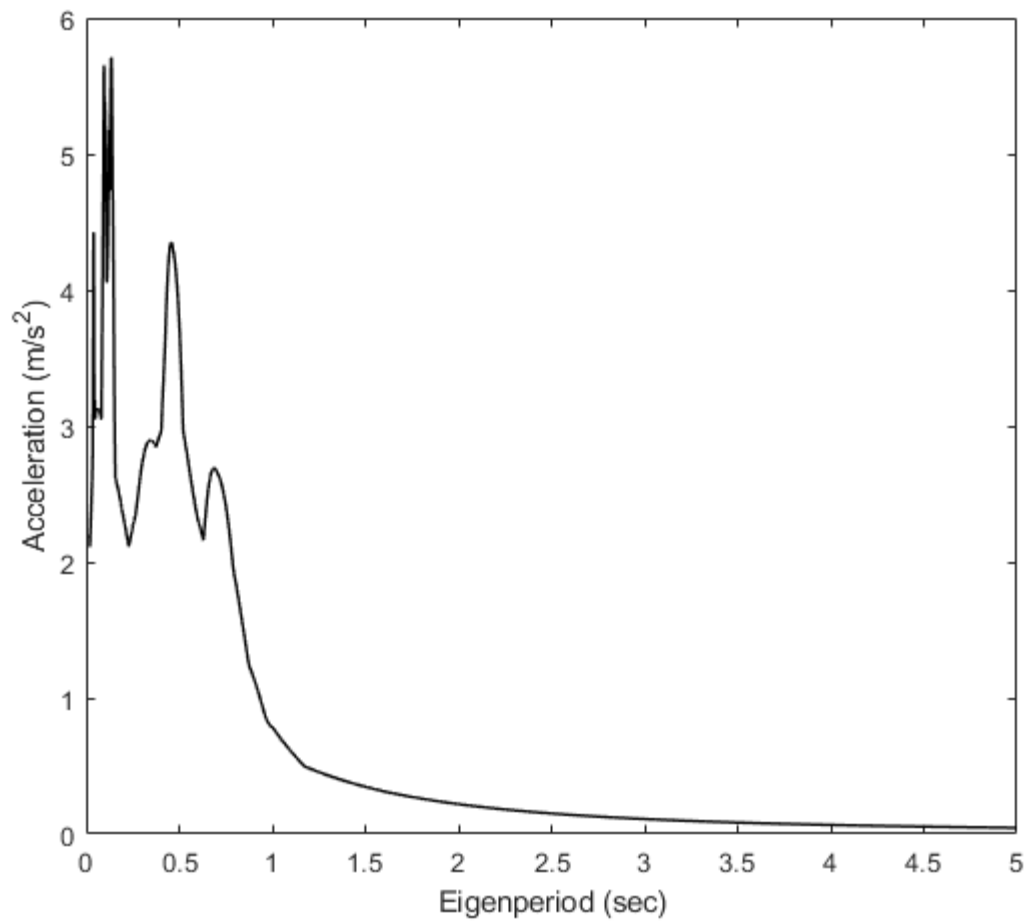
Velocity spectrum

```
figure()
plot(T,Sv,'k','LineWidth',1)
ylabel('Velocity (m/s)')
xlabel('Eigenperiod (sec)')
drawnow;
pause(0.1)
```



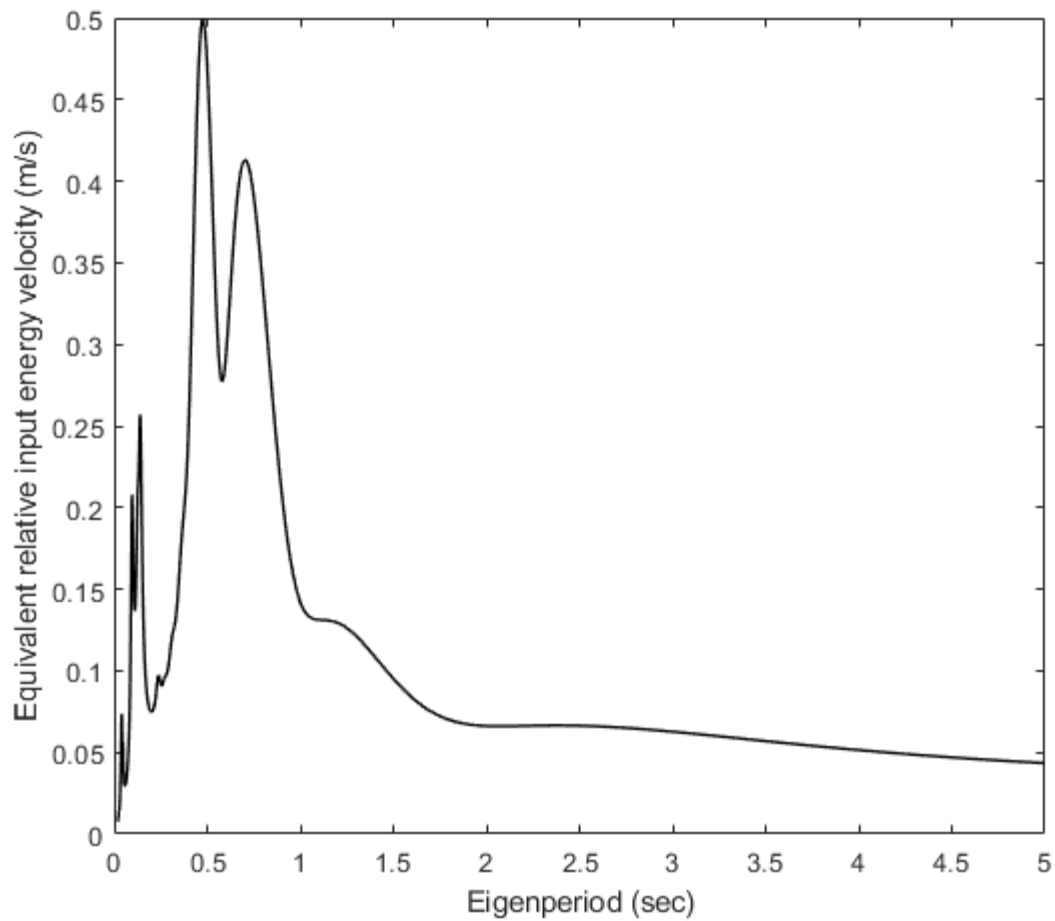
Acceleration spectrum

```
figure()
plot(T,Sa,'k','LineWidth',1)
ylabel('Acceleration (m/s^2)')
xlabel('Eigenperiod (sec)')
drawnow;
pause(0.1)
```



Equivalent relative input energy velocity

```
figure()
plot(T,Siev,'k','LineWidth',1)
ylabel('Equivalent relative input energy velocity (m/s)')
xlabel('Eigenperiod (sec)')
drawnow;
pause(0.1)
```

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- Major, Infrastructure Engineer, Hellenic Air Force
- Civil Engineer, M.Sc., Ph.D.
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example Linear elastic response spectra

Generate the linear elastic response spectra of an earthquake suite using OpenSeismoMatlab.

Contents

- [Input](#)
- [Calculation](#)
- [Output](#)
- [Copyright](#)

Input

Earthquake motions

```
eqmotions={'Imperial Valley'; % Imperial valley 1979
           'Kocaeli';
           'Loma Prieta';
           'Northridge';
           'San Fernando';
           'Spitak';
           'Cape Mendocino';
           'ChiChi';
           'elcentro_NS_trunc'; % Imperial valley 1940
           'Hollister';
           'Kobe'};
```

Set the eigenperiod range for which the response spectra will be calculated.

```
Tspectra=(0.01:0.01:4)';
```

Set critical damping ratio of the response spectra to be calculated.

```
ksi=0.05;
```

Extract linear elastic response spectra

```
sw='elrs';
```

Calculation

Initialize LERS

```
LERS=cell(numel(eqmotions),1);
```

Calculation of peak values

```

for i=1:numel(eqmotions)
    % earthquake
    data=load([eqmotions{i},'.dat']);
    t=data(:,1);
    dt=t(2)-t(1);
    xgtt=data(:,2);
    S=OpenSeismoMatlab(dt,xgtt,sw,Tspectra,ksi);
    LERS{i}=[S.Period,S.Sd,S.PSv,S.PSa];
end

```

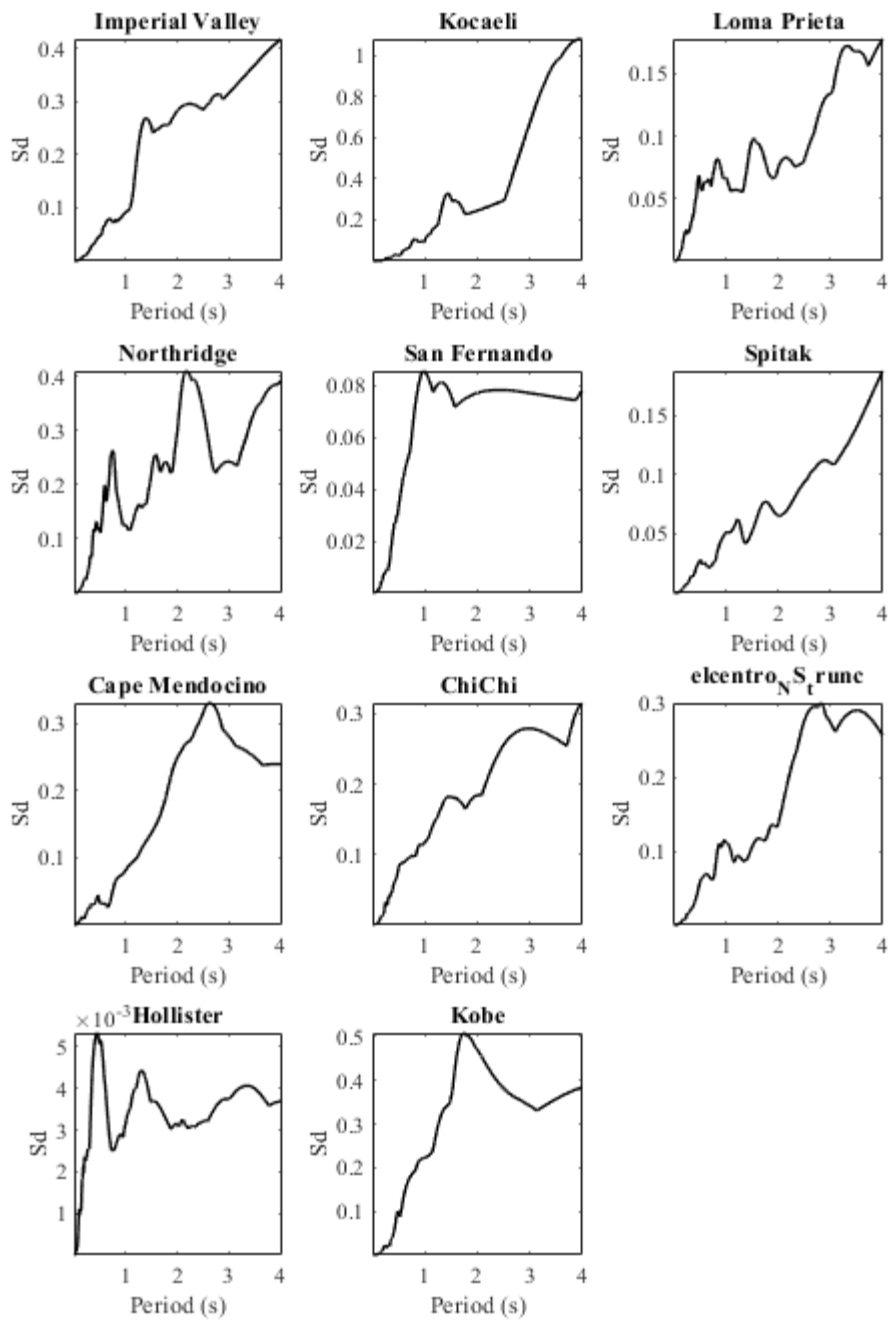
Output

Plot displacement response spectra

```

Fig1 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(LERS{i}(:,1),LERS{i}(:,2),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('Sd','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
    axis tight
end
drawnow;
pause(0.1)

```



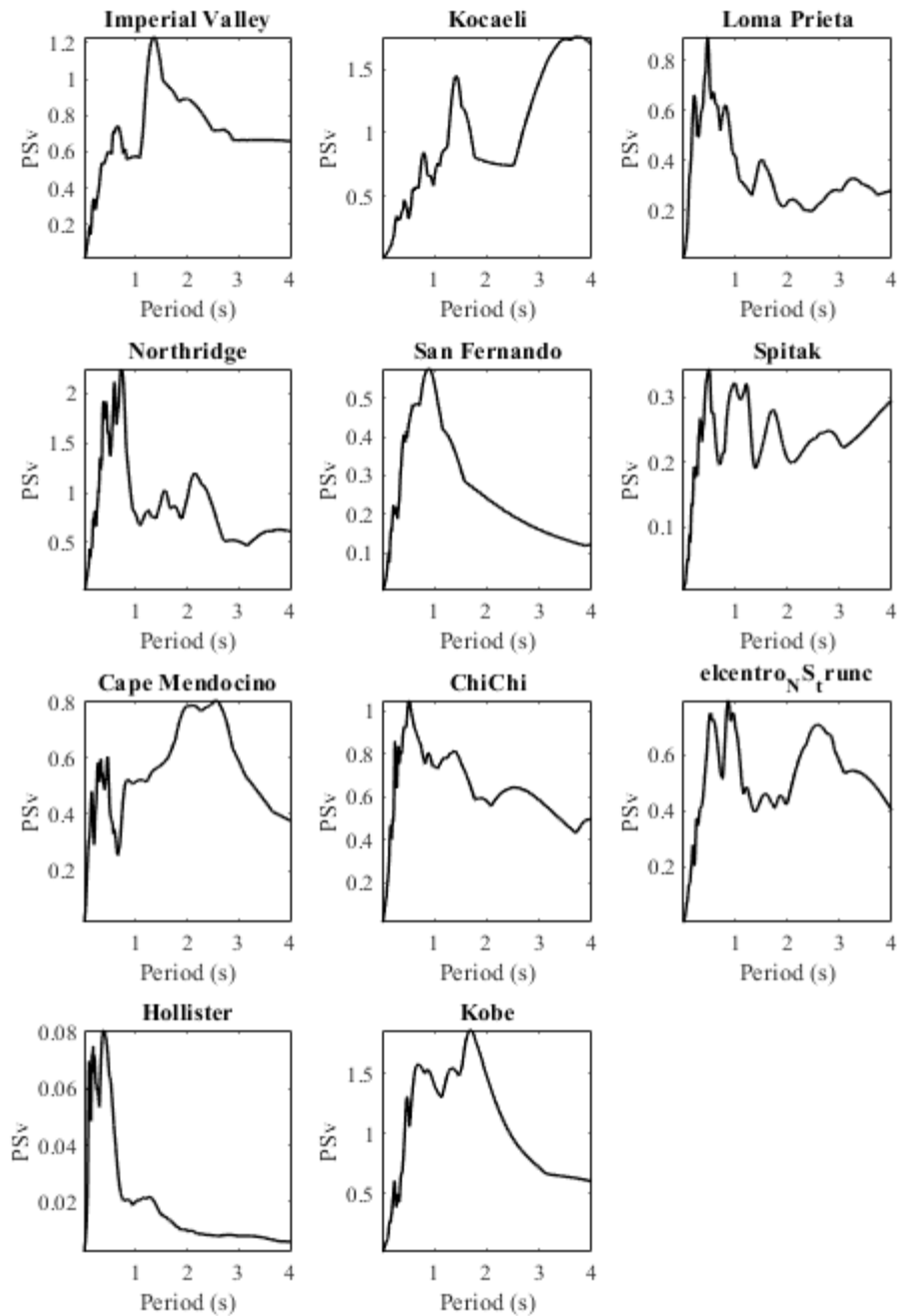
Plot pseudo-velocity response spectra

```
Fig2 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(LERS{i}(:,1),LERS{i}(:,3),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('PSv','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
```

```

axis tight
end
drawnow;
pause(0.1)

```



Plot pseudo-acceleration response spectra

```

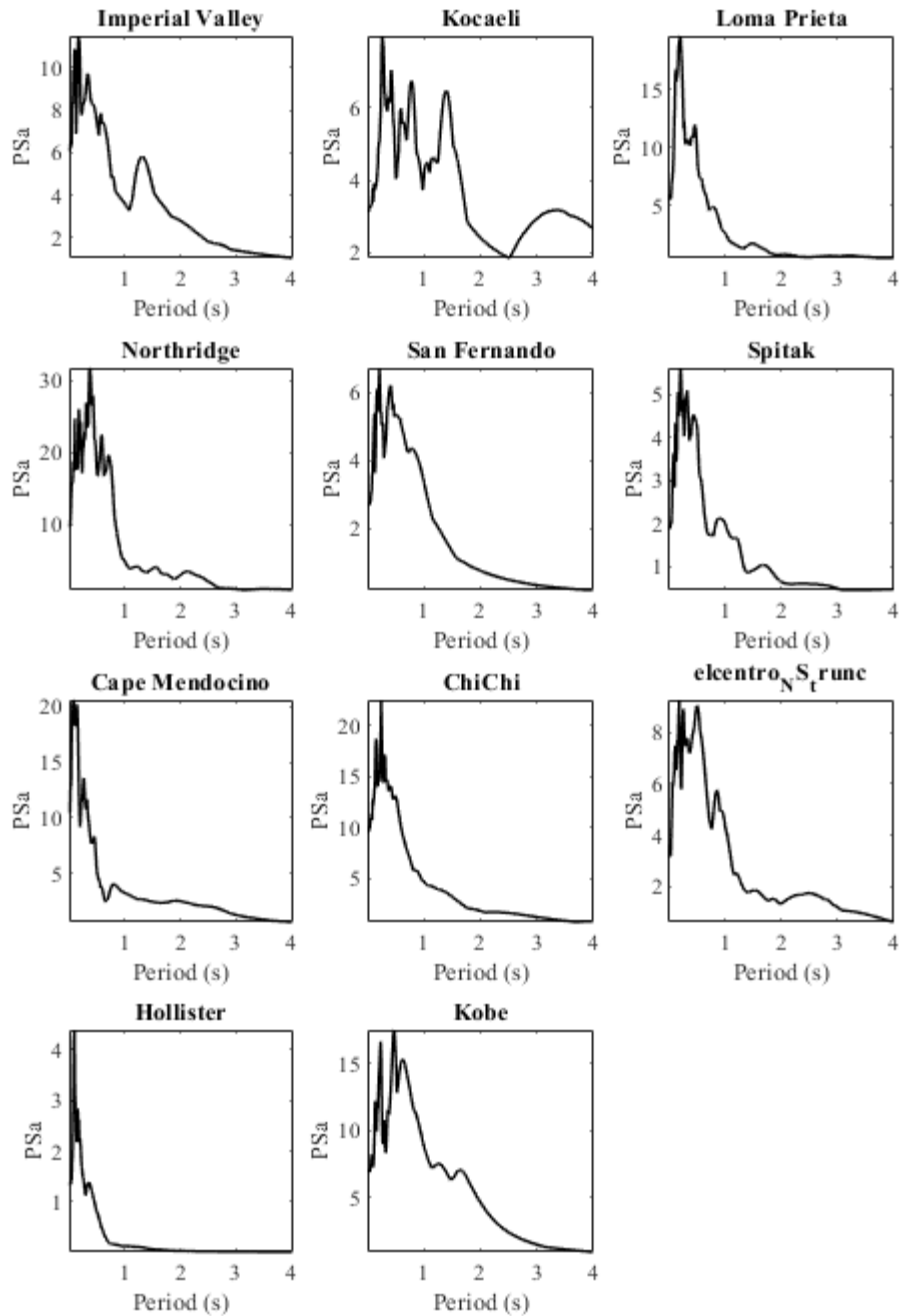
Fig3 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)

```

```

subplot(4,3,i)
plot(LERS{i}(:,1),LERS{i}(:,4),'k','LineWidth',1);
set(gca,'FontName','Times New Roman')
title(egmotions{i},'FontName','Times New Roman')
ylabel('PSa','FontName','Times New Roman')
xlabel('Period (s)','FontName','Times New Roman')
axis tight
end
drawnow;
pause(0.1)

```



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example PulseDecomp

Pulse decomposition of a velocity time history in OpenSeismoMatlab

Contents

- [Generate earthquake motion](#)
- [Setup parameters for PulseDecomp function](#)
- [Calculate Pulse and residual motion](#)
- [Plot the initial, pulse and residual time histories](#)
- [Copyright](#)

Generate earthquake motion

For reproducibility

```
rng(0)
```

Generate earthquake velocity time history with a pulse

```
duration = 10;  
dt = 0.01;  
t = linspace(0, duration, duration / dt)';  
num_sin_components = 3;  
xgt = zeros(length(t),1);  
for i = 1:num_sin_components  
    s = rand * sin(2 * pi * 0.5*rand * t + rand);  
    xgt = xgt + s;  
end
```

Setup parameters for PulseDecomp function

Wavelet family to be considered as the contained pulse

```
wname = 'db4';
```

Minimum pulse period for the continuous 1-D wavelet transform

```
TpMin = 0.25;
```

Minimum pulse period for the continuous 1-D wavelet transform

```
TpMax = 15;
```

Number of pulse period values between TpMin and TpMax

```
nScales = 50;
```


Calculate Pulse and residual motion

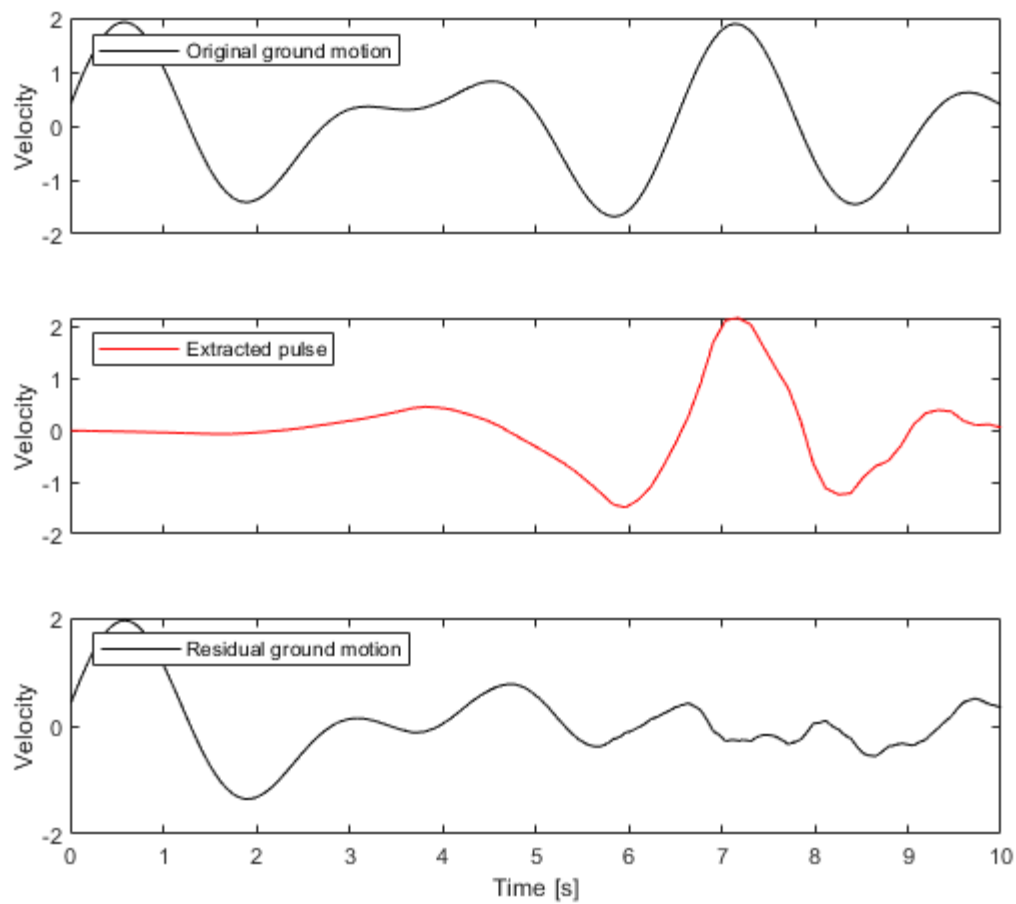
Apply PulseDecomp

```
[pulseTH, resTH, Tp, wavScale, wavCoef] = ...  
    PulseDecomp(dt, xgt, wname, TpMin, TpMax, nScales);
```

Plot the initial, pulse and residual time histories

Initialize figure

```
np = length(xgt);  
time = dt:dt:dt*np;  
fig = figure();  
% Initial velocity time history  
subplot(3,1,1)  
plot(time, xgt, '-k')  
legend('Original ground motion', 'location', 'northwest')  
ylabel('Velocity');  
set(gca, 'xticklabel', [])  
% Pulse velocity time history  
subplot(3,1,2)  
plot(time, pulseTH, '-r')  
legend('Extracted pulse', 'location', 'northwest')  
ylabel('Velocity');  
set(gca, 'xticklabel', [])  
% Residual velocity time history  
subplot(3,1,3)  
plot(time, resTH, '-k')  
legend('Residual ground motion', 'location', 'northwest')  
hy = ylabel('Velocity');  
hx = xlabel('Time [s]');  
drawnow;  
pause(0.1)
```



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example RPSReSp

Calculate rigid plastic sliding response spectra in OpenSeismoMatlab

Contents

- [Generate earthquake motion](#)
- [Plot the generated time history](#)
- [Setup parameters for RPSReSp function](#)
- [Calculate spectra](#)
- [Plot the spectra](#)
- [Copyright](#)

Generate earthquake motion

For reproducibility

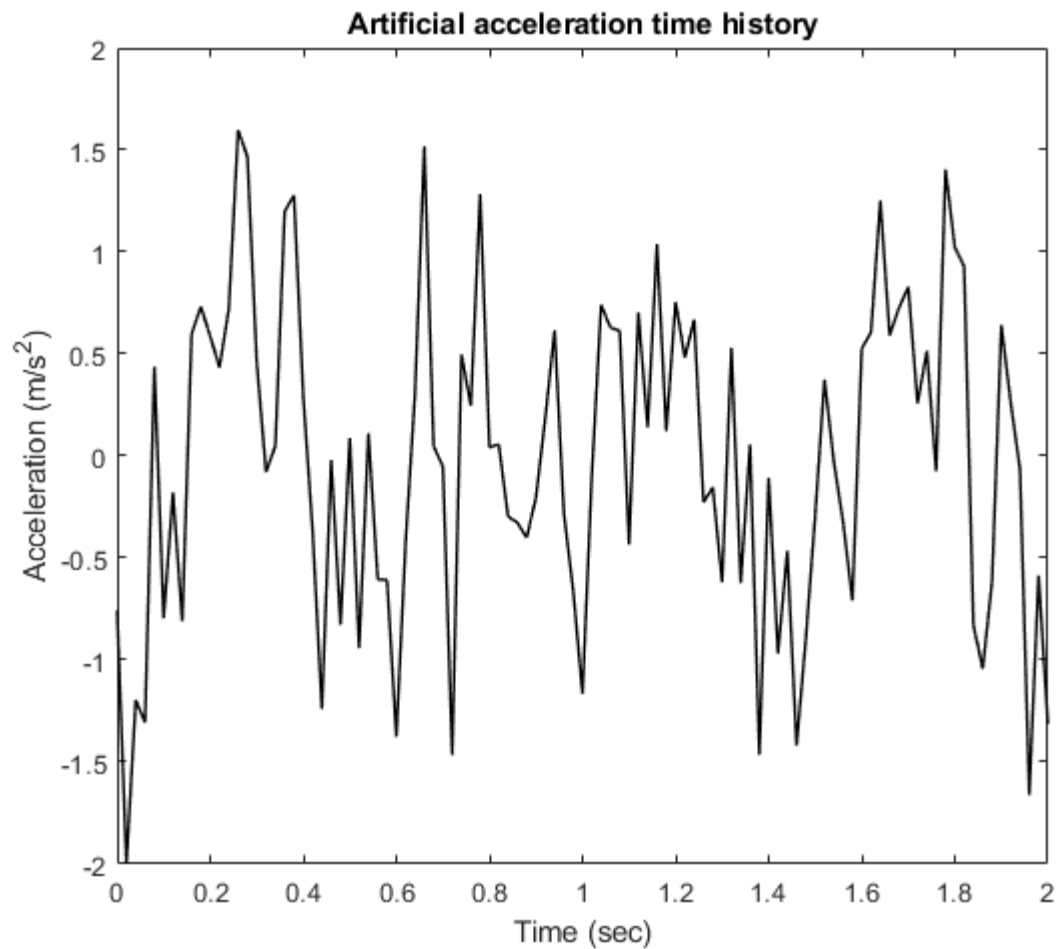
```
rng(0)
```

Generate earthquake acceleration time history

```
dt=0.02;  
N=10;  
a=rand(N,1)-0.5;  
b=100*pi*rand(N,1);  
c=pi*(rand(N,1)-0.5);  
t=(0:dt:(100*dt))';  
xgtt=zeros(size(t));  
for i=1:N  
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));  
end
```

Plot the generated time history

```
figure()  
plot(t,xgtt,'k','LineWidth',1)  
ylabel('Acceleration (m/s^2)')  
xlabel('Time (sec)')  
title('Artificial acceleration time history')  
drawnow;  
pause(0.1)
```



Setup parameters for RPSReSp function

Coulomb friction coefficients

```
CF=linspace(0.05,0.5,1000)';
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance of convergence for time integration algorithm

```
maxtol=0.01;
```

Maximum number of iterations per integration time step

```
jmax=200;
```

Infinitesimal acceleration

```
dak=eps;
```

Calculate spectra

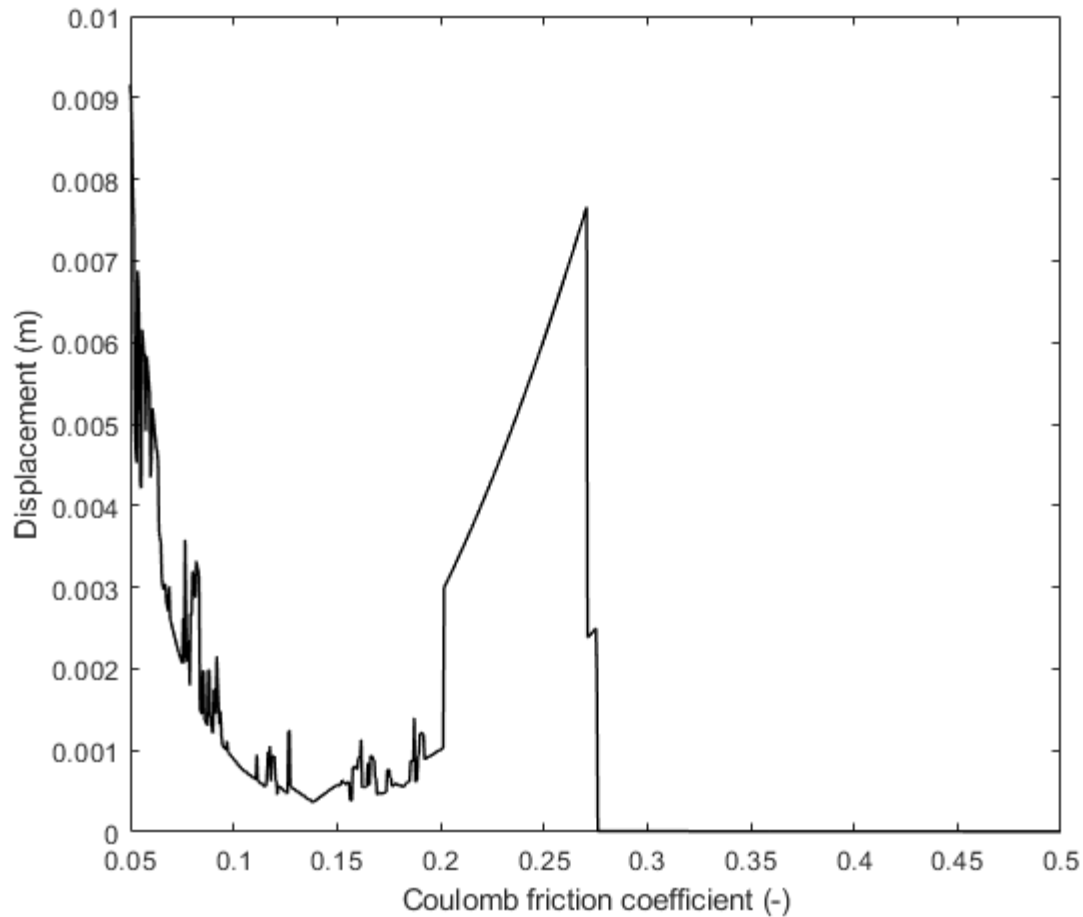
Apply RPSReSp

```
[Sd,Sv,Sa]=RPSReSp(dt,xgtt,CF,AlgID,rinf,maxtol,jmax,dak);
```

Plot the spectra

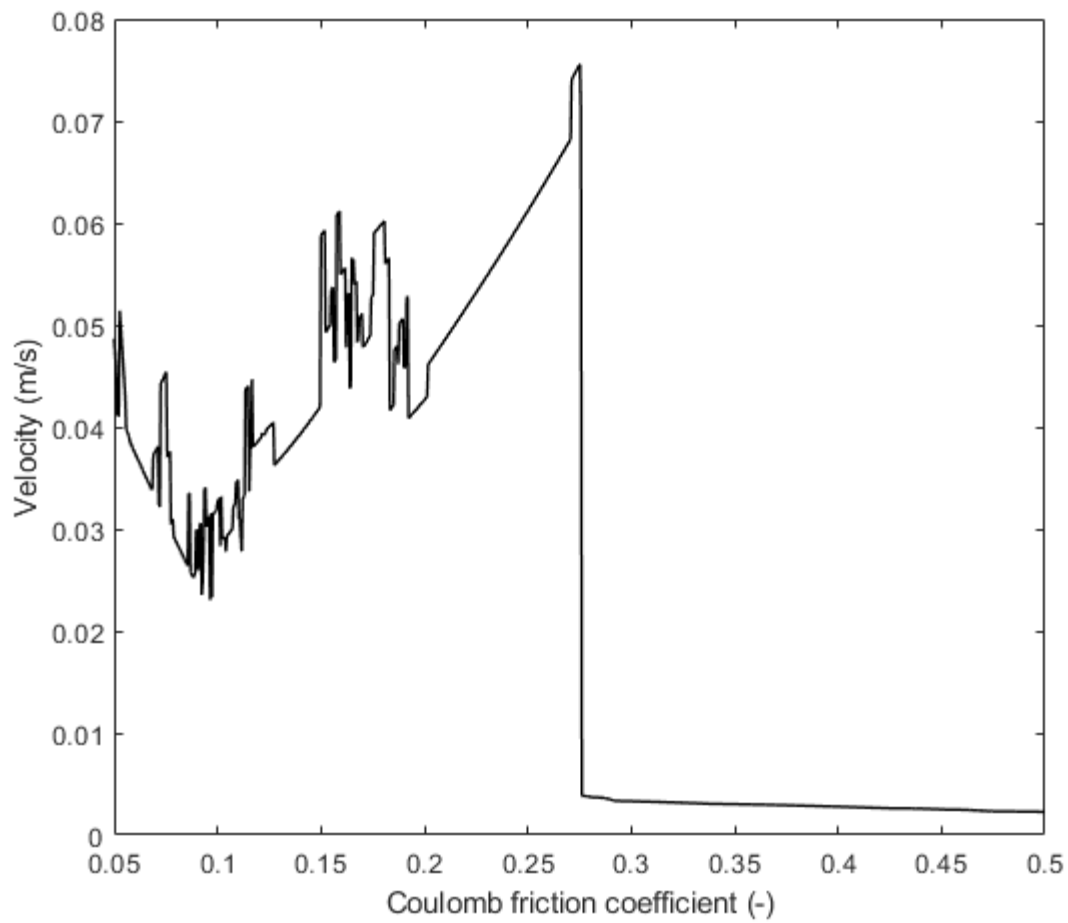
Displacement spectrum

```
figure()
plot(CF,Sd,'k','LineWidth',1)
ylabel('Displacement (m)')
xlabel('Coulomb friction coefficient (-)')
drawnow;
pause(0.1)
```



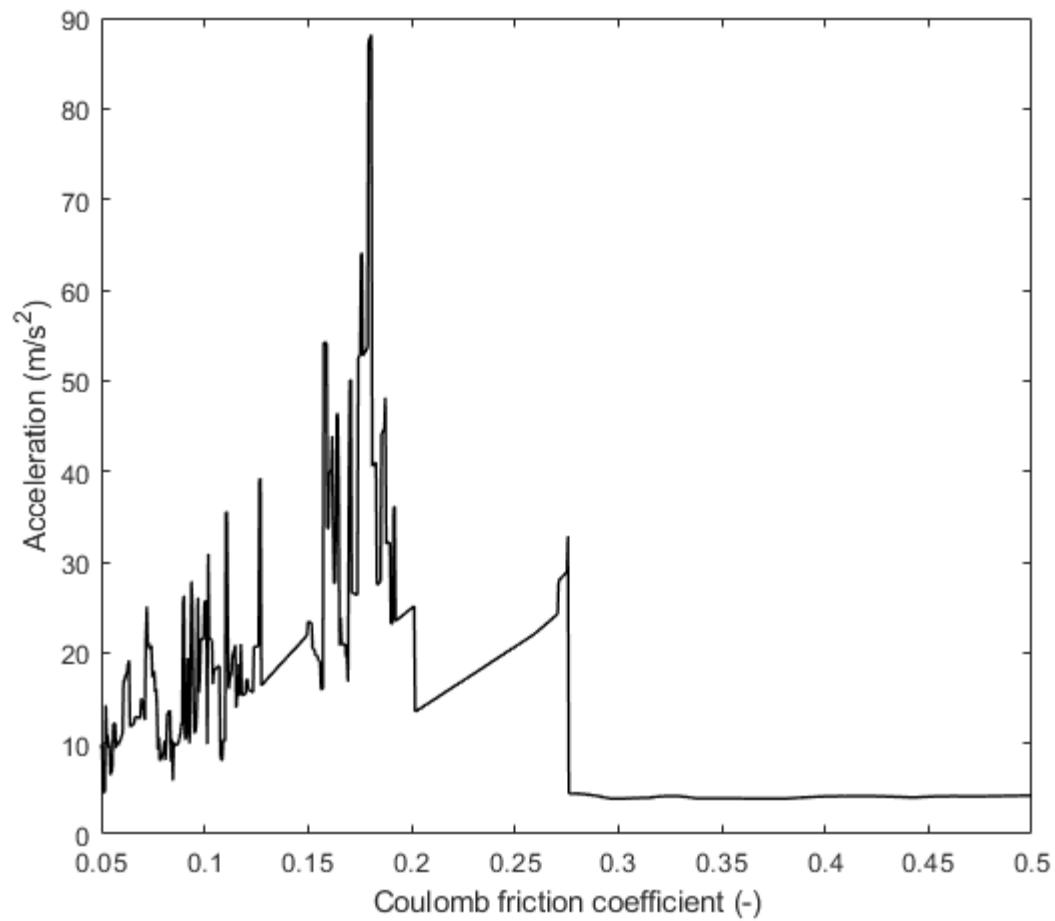
Velocity spectrum

```
figure()
plot(CF,Sv,'k','LineWidth',1)
ylabel('Velocity (m/s)')
xlabel('Coulomb friction coefficient (-)')
drawnow;
pause(0.1)
```



Acceleration spectrum

```
figure()
plot(CF,Sa,'k','LineWidth',1)
ylabel('Acceleration (m/s^2)')
xlabel('Coulomb friction coefficient (-)')
drawnow;
pause(0.1)
```



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example Comparison of elastic and constant ductility response spectra for $\mu=1$

Compare the linear elastic acceleration response spectrum and the constant ductility response spectrum for $\mu=1$ (degenerates to linear elastic). Also, compare with corresponding results of SeismoSignal software

Contents

- [Input](#)
- [First we use the CDS to calculate linear response](#)
- [Next we use ES to calculate linear response](#)
- [Results from SeismoSignal](#)
- [Output](#)
- [Copyright](#)

Input

Earthquake motion

```
eqmotions={'Imperial Valley'}; % Imperial valley 1979
data=load([eqmotions{1},'.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgtt=data(:,2);
```

Set the eigenperiod range for which the response spectra will be calculated.

```
Tspectra=(0.05:0.05:4)';
```

Set critical damping ratio of the response spectra to be calculated.

```
ksi=0.05;
```

First we use the CDS to calculate linear response

Set the target ductility

```
mu=1; % mu=1 equivalent to a linear SDoF
```

Extract constant ductility response spectra

```
sw='cdrs';
```

Calculation CDRS_i=[S.Period,S.CDSd,S.CDSv,S.CDPSa,S.fyK,S.muK,S.iterK];

```
S1=OpenSeismoMatlab(dt,xgtt,sw,Tspectra,ksi,mu);
```


Next we use ES to calculate linear response

Extract linear elastic response spectra

```
sw='elrs';
```

Initialize LERS

```
LERS=cell(numel(eqmotions),1);
```

Calculation LERS{i}=[S.Period,S.Sd,S.PSv,S.PSa];

```
S2=OpenSeismoMatlab(dt,xgdt,sw,Tspectra,ksi);
```

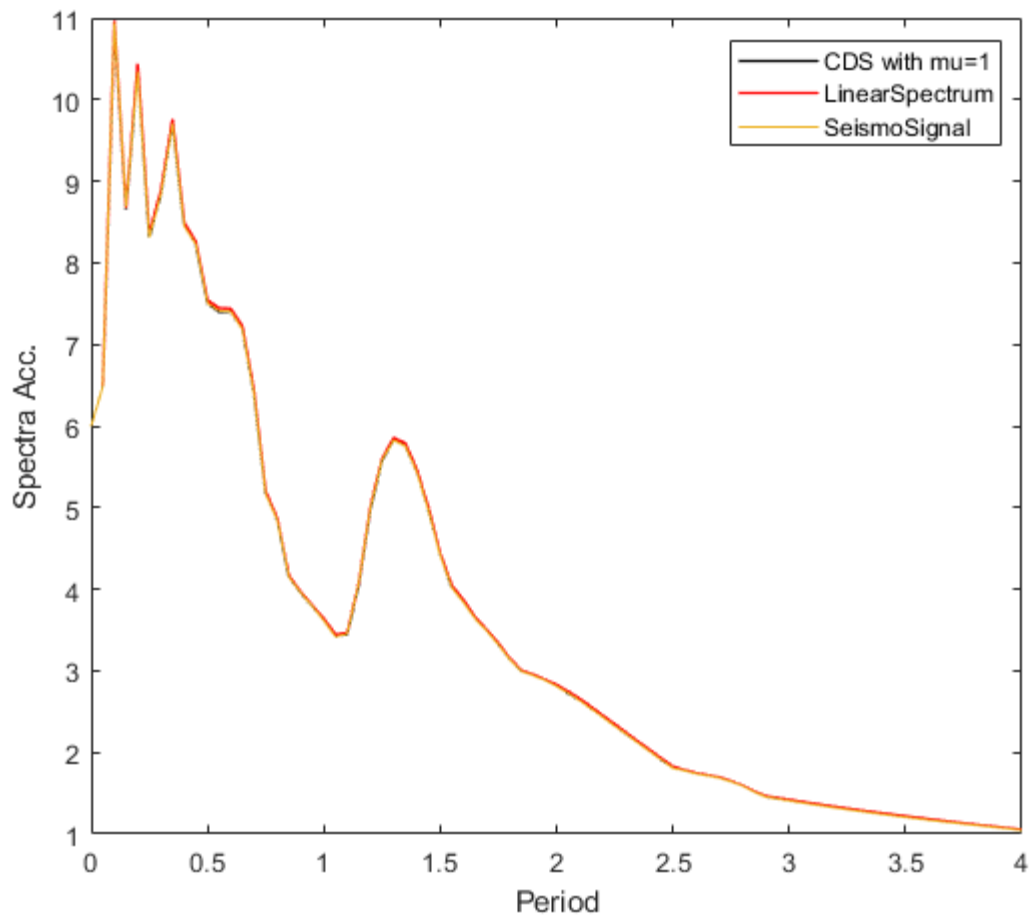
Results from SeismoSignal

```
fileID = fopen('SeismoSignal_Imperial Valley.txt');  
for idx = 1:5  
    fgetl(fileID);  
end  
C = textscan(fileID, repmat('%f',1,12));  
fclose(fileID);
```

Output

Plot spectral acceleration response spectra

```
plot(S1.Period,S1.CDSa,'k','LineWidth',1);  
hold on  
plot(S2.Period,S2.Sa,'r','LineWidth',1);  
plot(C{1},C{2})  
legend('CDS with mu=1','LinearSpectrum','SeismoSignal');  
xlabel('Period');  
ylabel('Spectra Acc.')
```



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example Comparison of constant ductility response spectra of RSN1044 for $\mu=2$

Contents

- [Input](#)
- [Results from OpenSeismoMatlab](#)
- [Results from SeismoSignal](#)
- [Output](#)
- [Copyright](#)

Input

Earthquake motions

```
GMFileLoc = 'input\';
```

A text file containing the lists of GM names

```
RecordList = ['input\Record_List.txt'];
```

Read E.Q. records name from the specifid list

```
fid = fopen (RecordList,'r');  
records = textscan(fid, '%s'); % length = num of records*1, cell  
fclose (fid);
```

Read E.Q. records name from the specifid list Return variables include record names, dt, num of points, PGA, Acc TH, Spectral Acc The acceleration-related variables (PGA, Sa, Acc TH) are in unit of g; disp-related in m If you do not specify scaling factors at this step, the default value = 1 for each GM

```
[RecordName_all, dt, numPoint_all, PGA_all, xgtd] =...  
    fn_ParseAT2File2 (GMFileLoc, records);
```

Set the eigenperiod range for which the response spectra will be calculated.

```
Tspectra=(0.05:0.05:4)';
```

Set critical damping ratio of the response spectra to be calculated.

```
ksi=0.02;
```

Results from OpenSeismoMatlab

Set the target ductility

```
mu=2; % mu=1 equivalent to a linear SDoF
```

Extract constant ductility response spectra

```
sw='cdrs';
```

Calculation $CDRS\{i\}=[S.Period,S.CDSd,S.CDSv,S.CDPSa,S.fyK,S.muK,S.iterK];$

```
S1=OpenSeismoMatlab(dt,xgtd{1},sw,Tspectra,ksi,mu);
```

Results from SeismoSignal

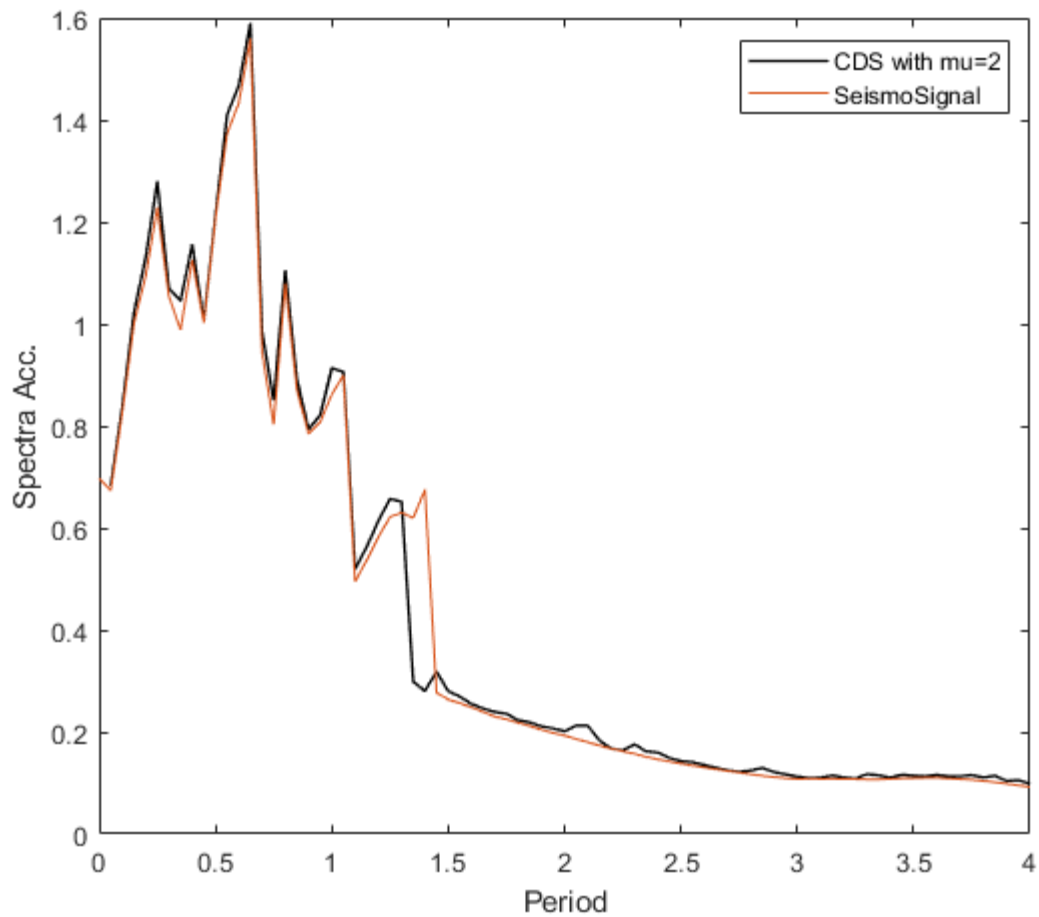
```
fileID = fopen('input/RSN1044_Damping2.txt');  
for idx = 1:5  
    fgetl(fileID);  
end  
C = textscan(fileID, repmat('%f',1,15));  
fclose(fileID);
```

Output

Plot spectral acceleration response spectra

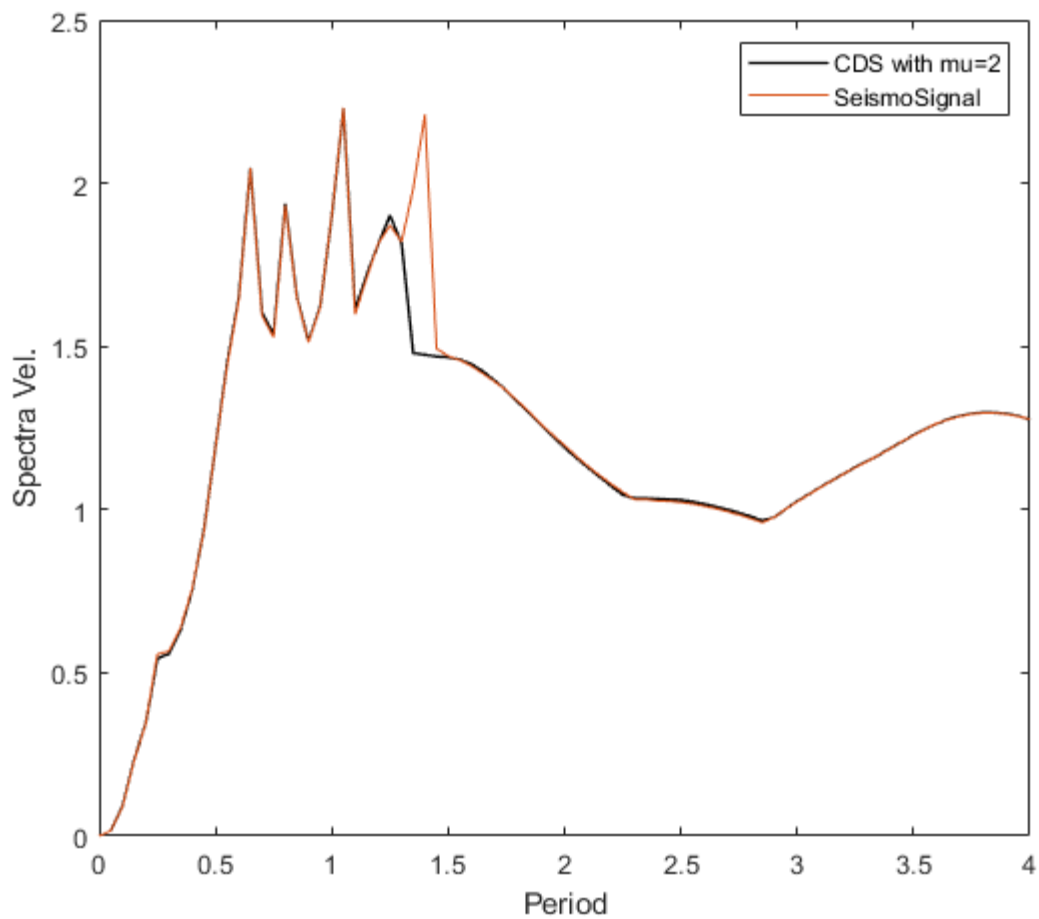
```
figure()  
plot(S1.Period,S1.CDSa/9.8,'k','LineWidth',1);  
hold on  
%plot(S2.Period,S2.Sa,'r','LineWidth',1);  
plot(C{1},C{3})  
legend('CDS with mu=2','SeismoSignal');  
xlabel('Period');  
ylabel('Spectra Acc.')
```

hold off
drawnow;
pause(0.1)



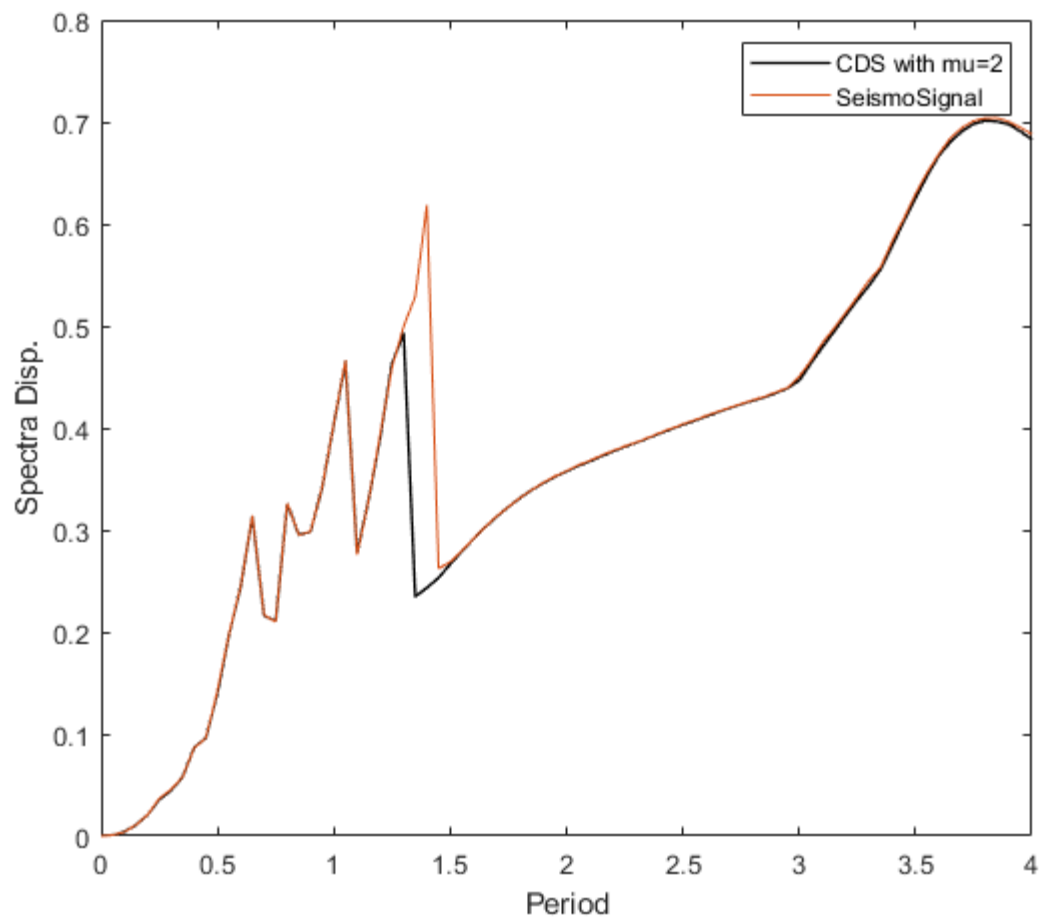
Plot spectral velocity response spectra

```
figure()
plot(S1.Period,S1.CDSv,'k','LineWidth',1);
hold on
%plot(S2.Period,S2.Sa,'r','LineWidth',1);
plot(C{1},C{7}/100)
legend('CDS with mu=2','SeismoSignal');
xlabel('Period');
ylabel('Spectra Vel.')
hold off
drawnow;
pause(0.1)
```



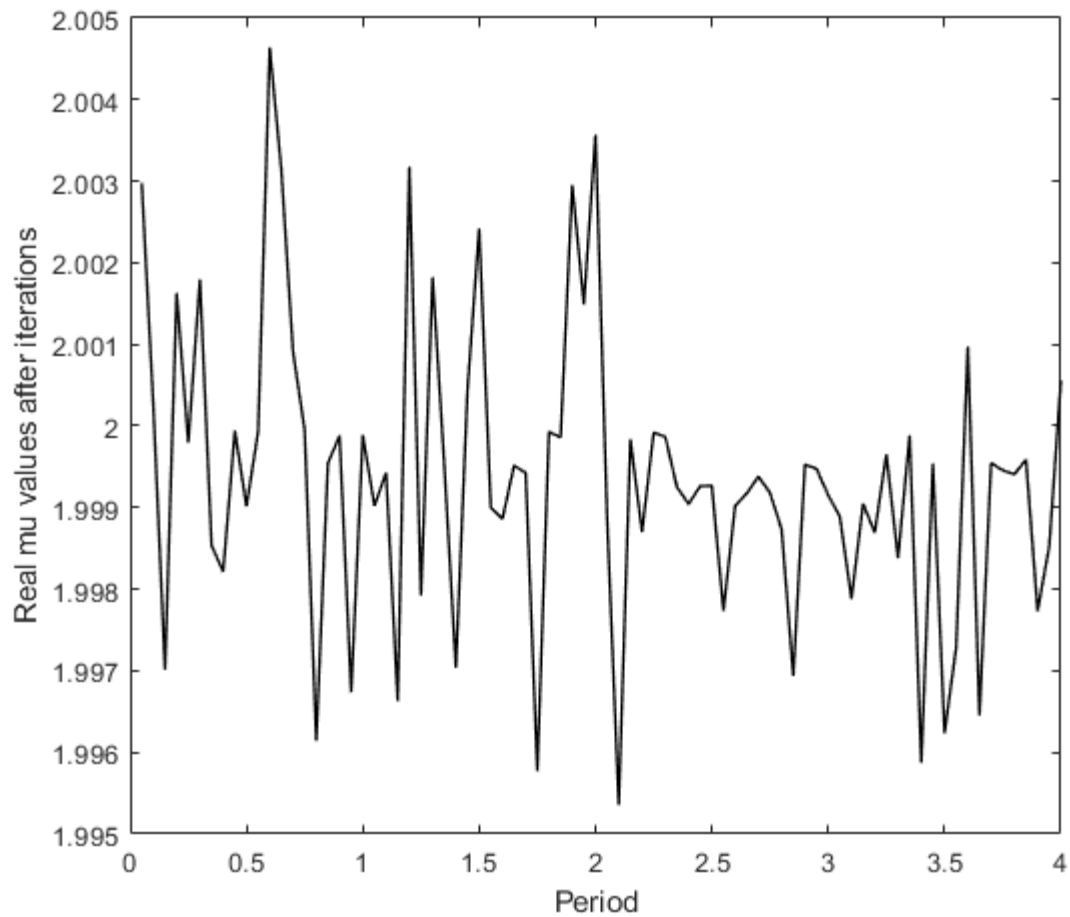
Plot spectral displacement response spectra

```
figure()
plot(S1.Period,S1.CDSd,'k','LineWidth',1);
hold on
%plot(S2.Period,S2.Sa,'r','LineWidth',1);
plot(C{1},C{11}/100)
legend('CDS with mu=2','SeismoSignal');
xlabel('Period');
ylabel('Spectra Disp.')
hold off
drawnow;
pause(0.1)
```



Plot the achieved ductility for each eigenperiod. It should be equal or close to the target ductility $\mu=2$

```
figure()
plot(S1.Period,S1.muK,'k','LineWidth',1);
xlabel('Period');
ylabel('Real mu values after iterations')
drawnow;
pause(0.1)
```



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doc baselineCorr

Documentation of the baselineCorr function.

```
helpFun('baselineCorr')
```

Baseline correction of acceleration time history

```
[COR_XG,COR_XGT,COR_XGTT] = BASELINECORR(T,XGTT)
```

Description

Linear baseline correction is performed for an uncorrected acceleration time history. Initially, first order fitting (straight line) is performed on the acceleration time history and the fitting line is subtracted from the acceleration time history, giving thus the first correction. Afterwards, the first correction of the acceleration is integrated to obtain the velocity, and then first order fitting (straight line) is performed on this velocity time history. The gradient of the straight fitting line is then subtracted from the first correction of the acceleration time history, giving thus the second correction of the acceleration time history. The second correction of the acceleration time history is then integrated to give the corrected velocity and displacement time histories.

Input parameters

T [double(1:numsteps x 1)] is the time vector of the input acceleration time history XGTT. numsteps is the length of the input acceleration time history.
XGTT [double(1:nstep x 1)]: column vector of the acceleration history of the excitation imposed at the base. nstep is the number of time steps of the dynamic response.

Output parameters

COR_XG [double(1:nstep x 1)]: time-history of displacement
COR_XGT [double(1:nstep x 1)]: time-history of velocity
COR_XGTT [double(1:nstep x 1)]: time-history of acceleration

Example

```
fid=fopen('elcentro.dat','r');  
text=textscan(fid,'%f %f');  
fclose(fid);  
time=text{1,1};  
xgttl=text{1,2};  
dt=time(2)-time(1);  
xgt1 = cumtrapz(time,xgttl);  
xg1 = cumtrapz(time,xgt1);  
[xg2, xgt2, xgtt2] = baselineCorr(time,xgttl)  
figure()  
plot(time,xgttl)  
hold on  
plot(time,xgtt2)  
figure()  
plot(time,xgt1)  
hold on  
plot(time,xgt2)  
figure()
```

```
plot(time,xg1)
hold on
plot(time,xg2)
```

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Documentation of the BLKIN function.

```
helpFun('BLKIN')
```

Bilinear kinematic hysteretic model with elastic viscous damping

```
[F,K,C,K_STATUS,D] = BLKIN(U,UT,K_HI,K_LO,UY,M,KSI,K_STATUS,D)
```

Description

Define the internal force vector, tangent stiffness matrix and tangent damping matrix of a bilinear elastoplastic hysteretic structure with elastic damping as a function of displacement and velocity.

The MDOF structure modeled with this function consists of lumped masses connected with stiffness and damping elements in series. Each lumped mass has one degree of freedom. The first degree of freedom is at the top of the structure and the last at its fixed base. However, the last degree of freedom is not included in the input arguments of the function, i.e. not contained in `ndof`, as it is always fixed. The nonlinear stiffness is virtually of the bilinear type, where an initial stiffness and a post-yield stiffness are defined. The unloading or reloading curve of this model are parallel to the initial loading curve, and a hysteresis loop is created by continuously loading and unloading the structure above its yield limit. This behavior can be viewed as hardening of the kinematic type.

An appropriate reference for this function definition is Hughes, Pister & Taylor (1979): "Implicit-explicit finite elements in nonlinear transient analysis". This function should be defined in accordance with equations (3.1), (3.2) and (3.3) of this paper. This representation has as special cases nonlinear elasticity and a class of nonlinear "rate-type" viscoelastic materials. Tangent stiffness and tangent damping matrices are the "consistent" linearized operators associated to `f` in the sense of [Hughes & Pister, "Consistent linearization in mechanics of solids", Computers and Structures, 8 (1978) 391-397].

Input parameters

`U` [double(1 x 1)] is the absolute displacement.

`UT` [double(1 x 1)] is the absolute velocity.

`K_HI` [double(1 x 1)] is the initial stiffness of the system before its first yield, i.e. the high stiffness.

`K_LO` [double(1 x 1)] is the post-yield stiffness of the system, i.e. the low stiffness.

`UY` [double(1 x 1)] is the yield limit of the structure. The structure is considered to yield, if the displacement exceeds `uy(i)`.

`M` [double(1 x 1)] is the lumped mass.

`KSI` [double(1 x 1)] is the ratio of critical viscous damping of the system, assumed to be unique for all damping elements of the structure.

`K_STATUS` [double(1 x 1)] is the is the stiffness vector which takes into account any plastic response of the structure. It is used to record the status of the structure so that it is known before the next application of this function at a next (time) step.

Initialize by setting $K_STATUS=K_HI$.

D [double(1 x 1)] is the equilibrium displacement vector which takes into account any plastic response of the structure. It is used to record the status of the structure so that it is known before the next application of this function at a next (time) step. Initialize by setting $D=zeros(ndof,1)$.

Output parameters

F [double(1 x 1)] is the internal force vector of the structure (sum of forces due to stiffness and damping) at displacement u and velocity ut

K [double(1 x 1)] is the tangent stiffness matrix (nonlinear function of displacement u and velocity ut). It is equivalent to the derivative $d(f)/d(u)$

C [double(1 x 1)] is the tangent damping matrix (nonlinear function of displacement u and velocity ut). It is equivalent to the derivative $d(f)/d(u)$

K_STATUS [double(1 x 1)] is the stiffness vector which takes into account any plastic response of the structure. It is used to record the status of the structure so that it is known before the next application of this function at a next (time) step.

D [double(1 x 1)] is the equilibrium displacement vector which takes into account any plastic response of the structure. It is used to record the status of the structure so that it is known before the next application of this function at a next (time) step.

Example

```
u=0:0.2:4;
u=[u,u(end:-1:1)];
u=[u,-u];
u=[u u];
ut=0.001*ones(1,numel(u));
ut=[ut,-ut];
ut=[ut,ut(end:-1:1)];
ut=[ut ut];
k_hi=1000;
k_lo=1;
uy=2;
M=1;
ksi=0.05;
k=k_hi;
d=0;
f=zeros(1,numel(u));
for i=1:numel(u)
    [f(i),K,C,k,d] = BLKIN(u(i),ut(i),k_hi,k_lo,uy,M,ksi,k,d);
end
figure()
plot(u,f)
```

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Documentation of the CDRSp function.

```
helpFun('CDRSp')
```

Constant Ductility Response Spectra

```
[PSA,PSV,SD,SV,SA,FYK,MUK,ITERK]=CDRESP(DT,XGTT,T,KSI,MU,N,TOL,...  
    PYSF,DTTOL,ALGID,RINF,MAXTOL,JMAX,DAK)
```

Description

The constant ductility response spectra for a given time-history of constant time step, eigenperiod range, viscous damping ratio and ductility are computed. See section 7.5 in Chopra (2012) and the notes "Inelastic Response Spectra" (CEE 541. Structural Dynamics) by Henri P. Gavin.

Input parameters

DT [double(1 x 1)] is the time step of the input acceleration time history XGTT.

XGTT [double(1:numsteps x 1)] is the input acceleration time history. numsteps is the length of the input acceleration time history.

T [double(1:numSDOFs x 1)] contains the values of eigenperiods for which the response spectra are requested. numSDOFs is the number of SDOF oscillators being analysed to produce the spectra.

KSI [double(1 x 1)] is the fraction of critical viscous damping.

MU [double(1 x 1)] is the target ductility for which the response spectra are calculated.

N [double(1 x 1)] is the maximum number of iterations that can be performed until convergence of the calculated ductility to the target ductility is achieved.

TOL [double(1 x 1)] is the tolerance for convergence for the target ductility.

PYSF [double(1 x 1)] is the post-yield stiffness factor, i.e. the ratio of the postyield stiffness to the initial stiffness. PYSF=0 is not recommended for simulation of an elastoplastic system. A small positive value is always suggested. PYSF is ignored if MU=1.

DTTOL [double(1 x 1)] is the tolerance for resampling of the input acceleration time history. For a given eigenperiod T, resampling takes place if $DT/T > dtTol$.

ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:

- 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
- 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
- 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
- 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
- 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm

'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm
 'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
 'U1-V0-Opt': Optimal numerical dissipation and dispersion first order displacement zero order velocity algorithm
 'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm
 'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order velocity algorithm
 'Newmark ACA': Newmark Average Constant Acceleration method
 'Newmark LA': Newmark Linear Acceleration method
 'Newmark BA': Newmark Backward Acceleration method
 'Fox-Goodwin': Fox-Goodwin formula

RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues of the amplification matrix. For the amplification matrix see eq.(61) in Zhou & Tamma (2004).

MAXTOL [double(1 x 1)] is the maximum tolerance of convergence of the Full Newton Raphson method for numerical computation of acceleration.

JMAX [double(1 x 1)] is the maximum number of iterations per increment. If JMAX=0 then iterations are not performed and the MAXTOL parameter is not taken into account.

DAK [double(1 x 1)] is the infinitesimal acceleration for the calculation of the derivative required for the convergence of the Newton-Raphson iteration.

Output parameters

PSA [double(1:numSDOFs x 1)] is the Pseudo-Spectral Acceleration.
 PSV [double(1:numSDOFs x 1)] is the Pseudo-Spectral Velocity.
 SD [double(1:numSDOFs x 1)] is the Spectral Displacement.
 SV [double(1:numSDOFs x 1)] is the Spectral Velocity.
 SA [double(1:numSDOFs x 1)] is the Spectral Acceleration.
 FYK [double(1:numSDOFs x 1)] is the yield limit that each SDOF must have in order to attain ductility equal to μ_K .
 MUK [double(1:numSDOFs x 1)] is the achieved ductility for each period (each SDOF).
 ITERK [double(1:numSDOFs x 1)] is the number of iterations needed for convergence for each period (each SDOF).

Example

```
dt=0.02;
N=10;
a=rand(N,1)-0.5;
b=100*pi*rand(N,1);
c=pi*(rand(N,1)-0.5);
t=(0:dt:(100*dt))';
xgtt=zeros(size(t));
for i=1:N
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));
end
figure()
```

```

plot(t,xgtt)
T=(0.04:0.04:4)';
ksi=0.05;
mu=2;
n=50;
tol=0.01;
pysf=0.1;
dtTol=0.02;
AlgID='U0-V0-Opt';
rinf=1;
maxtol=0.01;
jmax=200;
dak=eps;
[CDPSa,CDPSv,CDSd,CDSv,CDSa,fyK,muK,iterK]=CDReSp(dt,xgtt,T,ksi,...
    mu,n,tol,pysf,dtTol,AlgID,rinf,maxtol,jmax,dak);
figure()
plot(T,CDSd)
figure()
plot(T,fyK)
figure()
plot(T,muK)
figure()
plot(T,iterK)

```

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Documentation of the CSReSp function.

```
helpFun('CSReSp')
```

Constant Strength Response Spectra

```
[SMU, SD, SV, SA, SEY, SED]=CSRESP(DT, XGTT, T, KSI, FYR, PYSF, DTTOL, ...  
    ALGID, RINF, MAXTOL, JMAX, DAK)
```

Description

The constant strength response spectra for a given time-history of constant time step, eigenperiod range, viscous damping ratio and yield strength ratio (yield shear to weight, V/W) are computed.

Input parameters

DT [double(1 x 1)] is the time step of the input acceleration time history XGTT.

XGTT [double(1:numsteps x 1)] is the input acceleration time history. numsteps is the length of the input acceleration time history.

T [double(1:numSDOFs x 1)] contains the values of eigenperiods for which the response spectra are requested. numSDOFs is the number of SDOF oscillators being analysed to produce the spectra.

KSI [double(1 x 1)] is the fraction of critical viscous damping.

FYR [double(1 x 1)] is the yield strength ratio (yield shear to weight, V/W) for which the response spectra are calculated.

PYSF [double(1 x 1)] is the post-yield stiffness factor, i.e. the ratio of the postyield stiffness to the initial stiffness. PYSF=0 is not recommended for simulation of an elastoplastic system. A small positive value is always suggested.

DTTOL [double(1 x 1)] is the tolerance for resampling of the input acceleration time history. For a given eigenperiod T, resampling takes place if DT/T>dtTol.

ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:

- 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
- 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
- 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
- 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
- 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
- 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
- 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
- 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm

'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
 'U1-V0-Opt': Optimal numerical dissipation and dispersion first order displacement zero order velocity algorithm
 'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm
 'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order velocity algorithm
 'Newmark ACA': Newmark Average Constant Acceleration method
 'Newmark LA': Newmark Linear Acceleration method
 'Newmark BA': Newmark Backward Acceleration method
 'Fox-Goodwin': Fox-Goodwin formula

RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues of the amplification matrix. For the amplification matrix see eq.(61) in Zhou & Tamma (2004).

MAXTOL [double(1 x 1)] is the maximum tolerance of convergence of the Full Newton Raphson method for numerical computation of acceleration.

JMAX [double(1 x 1)] is the maximum number of iterations per increment. If JMAX=0 then iterations are not performed and the MAXTOL parameter is not taken into account.

DAK [double(1 x 1)] is the infinitesimal acceleration for the calculation of the derivative required for the convergence of the Newton-Raphson iteration.

Output parameters

SMU [double(1:numSDOFs x 1)] is the Spectral ductility.
 SD [double(1:numSDOFs x 1)] is the Spectral Displacement.
 SV [double(1:numSDOFs x 1)] is the Spectral Velocity.
 SA [double(1:numSDOFs x 1)] is the Spectral Acceleration.
 SEY [double(1:numSDOFs x 1)] is the Spectral yield energy.
 SED [double(1:numSDOFs x 1)] is the Spectral damping energy.

Example

```
dt=0.02;
N=10;
a=rand(N,1)-0.5;
b=100*pi*rand(N,1);
c=pi*(rand(N,1)-0.5);
t=(0:dt:(100*dt))';
xgtt=zeros(size(t));
for i=1:N
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));
end
figure()
plot(t,xgtt)
T=(0.04:0.04:4)';
ksi=0.05;
fyR=0.1;
pysf=0.1;
dtTol=0.02;
AlgID='U0-V0-Opt';
rinf=1;
maxtol=0.01;
jmax=200;
dak=eps;
[Smu,Sd,Sv,Sa,Sey,Sed]=CSReSp(dt,xgtt,T,ksi,fyR,pysf,dtTol,...
    AlgID,rinf,maxtol,jmax,dak);
```

```
figure()  
plot(T,Smu)  
figure()  
plot(T,Sd)  
figure()  
plot(T,Sv)  
figure()  
plot(T,Sa)  
figure()  
plot(T,Sey)  
figure()  
plot(T,Sed)
```

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Documentation of the DRHA function.

```
helpFun('DRHA')
```

Dynamic Response History Analysis

```
[U,V,A,F,ES,ED] = DRHA(K,M,DT,XGTT,KSI,U0,UT0,ALGID,RINF)
```

Description

Calculate the dynamic response of a linear MDOF system using modal analysis. This function is part of the OpenSeismoMatlab software. It can be used as standalone, however attention is needed for the correctness of the input arguments, since no checks are performed in this function. See the example `example_DRHA.m` for more details about how this function can be implemented.

Input parameters

K [double(:inf x 1)] is the stiffness of the system.
M [double(:inf x 1)] is the lumped masses of the structure.
DT [double(1 x 1)] is the time step of the dynamic response history analysis
XGTT [double(1:nstep x 1)]: column vector of the acceleration history of the excitation imposed at the base. nstep is the number of time steps of the dynamic response.
KSI [double(1 x 1)] is the ratio of critical damping of the SDOF system.
U0 [double(:inf x 1)] is the initial displacement of the SDOF system.
UT0 [double(:inf x 1)] is the initial velocity of the SDOF system.
ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:

- 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
- 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
- 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
- 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
- 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
- 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
- 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
- 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm
- 'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
- 'U1-V0-Opt': Optimal numerical dissipation and dispersion

first order displacement zero order velocity algorithm
'U1-V0-CA': Continuous acceleration (zero spurious root at
the low frequency limit) first order displacement zero order
velocity algorithm
'U1-V0-DA': Discontinuous acceleration (zero spurious root at
the high frequency limit) first order displacement zero order
velocity algorithm
'Newmark ACA': Newmark Average Constant Acceleration method
'Newmark LA': Newmark Linear Acceleration method
'Newmark BA': Newmark Backward Acceleration method
'Fox-Goodwin': Fox-Goodwin formula

RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues
of the amplification matrix. For the amplification matrix see
eq.(61) in Zhou & Tamma (2004).

Output parameters

U [double(1 x 1:nstep)]: displacement time history.
V [double(1 x 1:nstep)]: velocity time history.
A [double(1 x 1:nstep)]: acceleration time history.
F [double(1 x 1:nstep)]: equivalent static force time history.
ES [double(1 x 1:nstep)]: time-history of the recoverable
strain energy of the system (total and not incremental).
ED [double(1 x 1:nstep)]: time-history of the energy
dissipated by viscoelastic damping during each time step
(incremental). cumsum(Ed) gives the time history of the total
energy dissipated at dof i from the start of the dynamic
analysis.

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Documentation of the FASp function.

```
helpFun('FASp')
```

Fourier amplitude spectrum

```
[F,U] = FASP(DT,XGTT)
```

Description

Fourier amplitude spectrum of an acceleration time history.

Input parameters

DT [double(1 x 1)] is the time step of the input acceleration time history XGTT.

XGTT [double(1:numsteps x 1)] is the input acceleration time history. numsteps is the length of the input acceleration time history.

Output parameters

F [double(1:2^(nextpow2(length(XGTT))-1) x 1)] is the frequency range in which the Fourier amplitudes are calculated.

U [double(1:2^(nextpow2(length(XGTT))-1) x 1)] contains the Fourier amplitudes

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Documentation of the fft function.

```
helpFun('ffft')
```

Fast Finite Fourier Transform

```
Y = FFFT(X)
```

Description

Fourier transform of an input signal.

Input parameters

X [double(:inf x 1)] is the input signal.

Output parameters

Y [double(:inf x 1)] is the Fourier-transformed signal

Example

```
% Sampling frequency
Fs = 1000;
% Sampling period
dt = 1/Fs;
% Length of signal
L = 6000;
% Time vector
t = (0:L-1) '*dt;
% Signal
S = 0.7*sin(2*pi*50*t) + sin(2*pi*120*t);
xgtt = S + 2*randn(size(t));
% Apply the fft function of Matlab
NFFT = 2^nextpow2(L);
FASsignal=fft(xgtt,NFFT)*dt;
% Apply the fft function of OpenSeismoMatlab
FASsignal3=ffft(xgtt)*dt;
% Difference between results
max(abs(FASsignal-FASsignal3))
```

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doc HalfStep

Documentation of the HalfStep function.

```
helpFun('HalfStep')
```

Reproduce signal with half time step

```
UNEW = HALFSTEP(U)
```

Input parameters

U [double(1:n x 1)] is the input signal with time step dt.

Output parameters

UNEW [double(1:n x 1)] is the output signal with time step dt/2.

Verification:

```
u=0.2:0.2:4;  
uNew=HalfStep(u);  
figure()  
plot((1:numel(u)),u)  
hold on  
plot((1:0.5:numel(u)),uNew)
```

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Documentation of the IDA function.

```
helpFun('IDA')
```

Incremental Dynamic Analysis

```
[DM, IM]=IDA(DT, XGTT, T, LAMBD AF, IM_DM, M, UY, PYSF, KSI, ALGID, U0, UT0, ...
    RINF, MAXTOL, JMAX, DAK)
```

Description

This function performs incremental dynamic analysis of a given acceleration time history and SDOF oscillator.

Input parameters

DT [double(1 x 1)] is the time step of the input acceleration time history XGTT.

XGTT [double(:inf x 1)] is the input acceleration time history. numsteps is the length of the input acceleration time history.

T [double(1 x 1)] contains the eigenperiod of the SDOF system for which the incremental dynamic analysis response curve is requested.

LAMBD AF [double(:inf x 1)] contains the values of the scaling factor (lambda factor) for the incremental dynamic analysis.

IM_DM [char(1 x :inf)] is the Intensity Measure (IM) - Damage Measure (DM) pair that is to be calculated from the incremental dynamic analysis. IM_DM can take one of the following values (strings are case insensitive):

- 'SA_MU': Spectral acceleration-ductility
- 'PGD_MU': Peak displacement-ductility
- 'PGV_MU': Peak velocity-ductility
- 'PGA_MU': Peak acceleration-ductility
- 'SA_DISP': Spectral acceleration-displacement
- 'PGD_DISP': Peak displacement-displacement
- 'PGV_DISP': Peak velocity-displacement
- 'PGA_DISP': Peak acceleration-displacement
- 'SA_VEL': Spectral acceleration-velocity
- 'PGD_VEL': Peak displacement-velocity
- 'PGV_VEL': Peak velocity-velocity
- 'PGA_VEL': Peak acceleration-velocity
- 'SA_ACC': Spectral acceleration-acceleration
- 'PGD_ACC': Peak displacement-acceleration
- 'PGV_ACC': Peak velocity-acceleration
- 'PGA_ACC': Peak acceleration-acceleration

M [double(1 x 1)] is the mass of the SDOF oscillator.

UY [double(1 x 1)] is the yield displacement of the SDOF oscillator.

PYSF [double(1 x 1)] is the post-yield stiffness factor, i.e. the ratio of the postyield stiffness to the initial stiffness. PYSF=0 is not recommended for simulation of an elastoplastic system. A small positive value is always suggested. PYSF is ignored if MU=1.

KSI [double(1 x 1)] is the fraction of critical viscous damping.

ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:

'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm
 'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
 'U1-V0-Opt': Optimal numerical dissipation and dispersion first order displacement zero order velocity algorithm
 'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm
 'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order velocity algorithm
 'Newmark ACA': Newmark Average Constant Acceleration method
 'Newmark LA': Newmark Linear Acceleration method
 'Newmark BA': Newmark Backward Acceleration method
 'Fox-Goodwin': Fox-Goodwin formula

U0 [double(1 x 1)] is the initial displacement of the SDOF oscillator.

UT0 [double(1 x 1)] is the initial velocity of the SDOF oscillator.

RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues of the amplification matrix. For the amplification matrix see eq.(61) in Zhou & Tamma (2004). Default value 0.

MAXTOL [double(1 x 1)] is the maximum tolerance of convergence of the Full Newton Raphson method for numerical computation of acceleration.

JMAX [double(1 x 1)] is the maximum number of iterations per increment. If JMAX=0 then iterations are not performed and the MAXTOL parameter is not taken into account.

DAK [double(1 x 1)] is the infinitesimal acceleration for the calculation of the derivative required for the convergence of the Newton-Raphson iteration.

Output parameters

DM [double(:inf x 1)] is the Damage Measure.

IM [double(:inf x 1)] is the Intensity Measure.

Example

```
eqmotions={'elcentro'};
data=load([eqmotions{1},'.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgtd=data(:,2);
sw='ida';
```

```
T=1;
lambdaF=logspace(log10(0.001),log10(10),100);
IM_DM='Sa_disp';
m=1;
uy = 0.082*9.81/(2*pi/T)^2;
pysf=0.01;
ksi=0.05;
S5=OpenSeismoMatlab(dt,xgtd,sw,T,lambdaF,IM_DM,m,uy,pysf,ksi);
figure()
plot(S5.DM*1000,S5.IM/9.81,'k','LineWidth',1)
grid on
xlabel('Displacement (mm)')
ylabel('Sa(T1,5%) [g]')
xlim([0,200])
ylim([0,0.7])
```

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Documentation of the iffft function.

```
helpFun('iffft')
```

Inverse Fast Finite Fourier Transform

$Y = \text{IFFFT}(X)$

Description

Inverse Fourier transform of an input signal.

Input parameters

X [double(:inf x 1)] is the input signal.

Output parameters

Y [double(:inf x 1)] is the inverse Fourier-transformed signal

Example

```
% Sampling frequency
Fs = 1000;
% Sampling period
dt = 1/Fs;
% Length of signal
L = 6000;
% Time vector
t = (0:L-1) '*dt;
% Signal
S = 0.7*sin(2*pi*50*t) + sin(2*pi*120*t);
xgtt = S + 2*randn(size(t));
% Pad with zero so that the first value of xgtt is not lost in the
% Fourier transformations
xgtt=[0;xgtt];
% Apply the fft function of OpenSeismoMatlab
FASsignalOSM=fft(xgtt)*dt;
% Calculate inverse Fourier transform
y=iffft(FASsignalOSM/dt);
y=y(1:L-1);
% Plot the initial ground motion and the inverse Fourier transform
% of the Fourier-transformed motion
plot(real(y))
hold on
plot(xgtt(2:L))
hold off
% Difference between results
max(abs(real(y)-xgtt(2:L)))
```

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Documentation of the LEReSp function.

```
helpFun('LEReSp')
```

Linear Elastic Response Spectra

```
[PSA,PSV,SD,SV,SA,SIEV]=LERESP(DT,XGTT,T,KSI,DTTOL,...  
    ALGID,RINF)
```

Description

The linear elastic response spectra for a given time-history of constant time step, a given eigenperiod range and a given viscous damping ratio are computed. These spectra include the spectral acceleration, spectral velocity, spectral displacement, pseudoacceleration, pseudovelocity, absolute equivalent input energy velocity and relative equivalent input energy velocity. This function is part of the OpenSeismoMatlab software. It can be used as standalone, however attention is needed for the correctness of the input arguments, since no checks are performed in this function. See the example `example_LEReSp.m` for more details about how this function can be implemented.

Input parameters

DT [double(1 x 1)] is the time step of the input acceleration time history XGTT.

XGTT [double(1:numsteps x 1)] is the input acceleration time history. numsteps is the length of the input acceleration time history.

T [double(1:numSDOFs x 1)] contains the values of eigenperiods for which the response spectra are requested. numSDOFs is the number of SDOF oscillators being analysed to produce the spectra.

KSI [double(1 x 1)] is the fraction of critical viscous damping.

DTTOL [double(1 x 1)] is the maximum ratio of the integration time step to the eigenperiod.

ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:

- 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
- 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
- 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
- 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
- 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
- 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
- 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
- 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order

```

velocity algorithm
'U0-V1-DA': Discontinuous acceleration (zero spurious root at
the high frequency limit) zero order displacement first order
velocity algorithm
'U1-V0-Opt': Optimal numerical dissipation and dispersion
first order displacement zero order velocity algorithm
'U1-V0-CA': Continuous acceleration (zero spurious root at
the low frequency limit) first order displacement zero order
velocity algorithm
'U1-V0-DA': Discontinuous acceleration (zero spurious root at
the high frequency limit) first order displacement zero order
velocity algorithm
'Newmark ACA': Newmark Average Constant Acceleration method
'Newmark LA': Newmark Linear Acceleration method
'Newmark BA': Newmark Backward Acceleration method
'Fox-Goodwin': Fox-Goodwin formula
RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues
of the amplification matrix. For the amplification matrix see
eq.(61) in Zhou & Tamma (2004).

```

Output parameters

```

PSA [double(1:numSDOFs x 1)] is the Pseudo Acceleration Spectrum.
PSV [double(1:numSDOFs x 1)] is the Pseudo Velocity Spectrum.
SD [double(1:numSDOFs x 1)] is the Spectral Displacement.
SV [double(1:numSDOFs x 1)] is the Spectral Velocity.
SA [double(1:numSDOFs x 1)] is the Spectral Acceleration.
SIEV [double(1:numSDOFs x 1)] is the equivalent relative input
energy velocity. See: {Uang, C. M., & Bertero, V. V. (1990).
Evaluation of seismic energy in structures. Earthquake
engineering & structural dynamics, 19(1), 77-90} for more
details.

```

Example

```

dt=0.02;
N=10;
a=rand(N,1)-0.5;
b=100*pi*rand(N,1);
c=pi*(rand(N,1)-0.5);
t=(0:dt:(100*dt))';
xgtt=zeros(size(t));
for i=1:N
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));
end
T=logspace(log10(0.02),log10(50),1000)';
ksi=0.05;
dtTol=0.02;
AlgID='U0-V0-Opt';
rinf=1;
[PSa,PSv,Sd,Sv,Sa,Siev]=LEReSp(dt,xgtt,T,ksi,dtTol,...
    AlgID,rinf);

```

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Documentation of the LIDA function.

```
helpFun('LIDA')
```

Linear Implicit Dynamic Analysis

```
[U,UT,UTT,EI] = LIDA(DT,XGTT,OMEGA,KSI,U0,UT0,ALGID,RINF)
```

Description

Linear implicit direct time integration of second order differential equation of motion of dynamic response of linear elastic SDOF systems. The General Single Step Single Solve (GSSSS) family of algorithms published by X.Zhou & K.K.Tamma (2004) is employed for direct time integration of the general linear or nonlinear structural Single Degree of Freedom (SDOF) dynamic problem. The optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm designed according to the above journal article, is used in this routine. This algorithm encompasses the scope of Linear Multi-Step (LMS) methods and is limited by the Dahlquist barrier theorem (Dahlquist,1963). The force - displacement - velocity relation of the SDOF structure is linear. This function is part of the OpenSeismoMatlab software. It can be used as standalone, however attention is needed for the correctness of the input arguments, since no checks are performed in this function. See the example example_LIDA.m for more details about how this function can be implemented.

Input parameters

DT [double(1 x 1)] is the time step
XGTT [double(1:nstep x 1)] is the column vector of the acceleration history of the excitation imposed at the base. nstep is the number of time steps of the dynamic response.
OMEGA [double(1 x 1)] is the eigenfrequency of the structure in rad/sec.
KSI [double(1 x 1)] is the ratio of critical damping of the SDOF system.
U0 [double(1 x 1)] is the initial displacement of the SDOF system.
UT0 [double(1 x 1)] is the initial velocity of the SDOF system.
ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:
 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order

```

velocity algorithm
'U0-V1-Opt': Optimal numerical dissipation and dispersion
zero order displacement first order velocity algorithm
'U0-V1-CA': Continuous acceleration (zero spurious root at
the low frequency limit) zero order displacement first order
velocity algorithm
'U0-V1-DA': Discontinuous acceleration (zero spurious root at
the high frequency limit) zero order displacement first order
velocity algorithm
'U1-V0-Opt': Optimal numerical dissipation and dispersion
first order displacement zero order velocity algorithm
'U1-V0-CA': Continuous acceleration (zero spurious root at
the low frequency limit) first order displacement zero order
velocity algorithm
'U1-V0-DA': Discontinuous acceleration (zero spurious root at
the high frequency limit) first order displacement zero order
velocity algorithm
'Newmark ACA': Newmark Average Constant Acceleration method
'Newmark LA': Newmark Linear Acceleration method
'Newmark BA': Newmark Backward Acceleration method
'Fox-Goodwin': Fox-Goodwin formula
RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues
of the amplification matrix. For the amplification matrix see
eq.(61) in Zhou & Tamma (2004).

```

Output parameters

```

U [double(1:nstep x 1)] is the time-history of displacement
UT [double(1:nstep x 1)] is the time-history of velocity
UTT [double(1:nstep x 1)] is the time-history of acceleration
EI [double(1:nstep x 1)] is the time-history of the seismic input
energy per unit mass. See: {Uang, C. M., & Bertero, V. V. (1990).
Evaluation of seismic energy in structures. Earthquake
engineering & structural dynamics, 19(1), 77-90} for more
details.

```

Example (Figure 6.6.1 in Chopra, $T_n=1\text{sec}$)

```

dt=0.02;
fid=fopen('elcentro.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
xgtt=text{1,2};
Tn=1;
omega=2*pi/Tn;
ksi=0.02;
u0=0;
ut0=0;
AlgID='U0-V0-Opt';
rinf=1;
[u,ut,utt] = LIDA(dt,xgtt,omega,ksi,u0,ut0,AlgID,rinf);
D=max(abs(u))/0.0254

```

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doc NLIDABLKIN

Documentation of the NLIDABLKIN function.

```
helpFun('NLIDABLKIN')
```

Non Linear Implicit Dynamic Analysis of a BiLinear KiNematic hardening hysteretic structure with elastic damping

```
[U,UT,UTT,FS,EY,ES,ED,JITER] = NLIDABLKIN(DT,XGTT,M,K_HI,K_LO,UY,...  
      KSI,ALGID,U0,UT0,RINF,MAXTOL,JMAX,DAK)
```

Description

General linear implicit direct time integration of second order differential equations of a bilinear elastoplastic hysteretic SDOF dynamic system with elastic damping, with lumped mass. The General Single Step Single Solve (GSSSS) family of algorithms published by X.Zhou & K.K.Tamma (2004) is employed for direct time integration of the general linear or nonlinear structural Single Degree of Freedom (SDOF) dynamic problem. Selection among 9 algorithms, all designed according to the above journal article, can be made in this routine. These algorithms encompass the scope of Linear Multi-Step (LMS) methods and are limited by the Dahlquist barrier theorem (Dahlquist,1963).

Input parameters

DT [double(1 x 1)] is the time step of the integration
XGTT [double(1:NumSteps x 1)] is the acceleration time history which is imposed at the lumped mass of the SDOF structure.
M [double(1 x 1)] is the lumped masses of the structure. Define the lumped masses from the top to the bottom, excluding the fixed dof at the base
K_HI [double(1 x 1)] is the initial stiffness of the system before its first yield, i.e. the high stiffness. Give the stiffness of each storey from top to bottom.
K_LO [double(1 x 1)] is the post-yield stiffness of the system, i.e. the low stiffness. Give the stiffness of each storey from top to bottom.
UY [double(1 x 1)] is the yield limit of the stiffness elements of the structure. The element is considered to yield, if the interstorey drift between degrees of freedom i and i+1 exceeds UY(i). Give the yield limit of each storey from top to bottom.
KSI [double(1 x 1)] is the ratio of critical viscous damping of the system, assumed to be unique for all damping elements of the structure.
ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:
 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm

'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm
 'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
 'U1-V0-Opt': Optimal numerical dissipation and dispersion first order displacement zero order velocity algorithm
 'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm
 'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order velocity algorithm
 'Newmark ACA': Newmark Average Constant Acceleration method
 'Newmark LA': Newmark Linear Acceleration method
 'Newmark BA': Newmark Backward Acceleration method
 'Fox-Goodwin': Fox-Goodwin formula

U0 [double(1 x 1)] is the initial displacement.

UT0 [double(1 x 1)] is the initial velocity.

RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues of the amplification matrix. For the amplification matrix see eq.(61) in Zhou & Tamma (2004).

MAXTOL [double(1 x 1)] is the maximum tolerance of convergence of the Full Newton Raphson method for numerical computation of acceleration.

JMAX [double(1 x 1)] is the maximum number of iterations per increment. If JMAX=0 then iterations are not performed and the MAXTOL parameter is not taken into account.

DAK [double(1 x 1)] is the infinitesimal acceleration for the calculation of the derivative required for the convergence of the Newton-Raphson iteration.

Output parameters

U [double(1 x 1:NumSteps)] is the time-history of displacement

UT [double(1 x 1:NumSteps)] is the time-history of velocity

UTT [double(1 x 1:NumSteps)] is the time-history of acceleration

FS [double(1 x 1:NumSteps)] is the time-history of the internal force of the structure analysed.

EY [double(1 x 1:NumSteps)] is the time history of the sum of the energy dissipated by yielding during each time step and the recoverable strain energy of the system (incremental).

cumsum(EY)-ES gives the time history of the total energy dissipated by yielding from the start of the dynamic analysis.

ES [double(1 x 1:NumSteps)] is the time-history of the recoverable strain energy of the system (total and not incremental).

ED [double(1 x 1:NumSteps)] is the time-history of the energy dissipated by viscoelastic damping during each time step (incremental). cumsum(ED) gives the time history of the total energy dissipated from the start of the dynamic analysis.

JITER [double(1 x 1:NumSteps)] is the iterations per increment

Notation in the code

u=displacement
un=displacement after increment n
ut=velocity
utn=velocity after increment n
utt=acceleration
uttn=acceleration after increment n

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doc OpenSeismoMatlab

Documentation of the OpenSeismoMatlab function.

```
helpFun('OpenSeismoMatlab')
```

Seismic parameters and processing of an acceleration time history

Syntax

```
PARAM=OpenSeismoMatlab(DT,XGTT,SW,___)
PARAM=OpenSeismoMatlab(DT,XGTT,'PGA')
PARAM=OpenSeismoMatlab(DT,XGTT,'EPGA')
PARAM=OpenSeismoMatlab(DT,XGTT,'PGV')
PARAM=OpenSeismoMatlab(DT,XGTT,'PGD')
PARAM=OpenSeismoMatlab(DT,XGTT,'ARIAS')
PARAM=OpenSeismoMatlab(DT,XGTT,'SIH1952')
PARAM=OpenSeismoMatlab(DT,XGTT,'SINH1984')
PARAM=OpenSeismoMatlab(DT,XGTT,'TIMEHIST',BASELINESW)
PARAM=OpenSeismoMatlab(DT,XGTT,'RESAMPLE',DTI)
PARAM=OpenSeismoMatlab(DT,XGT,'PULSEDECOMP',WNAME,TPMIN,TPMAX,...
    NSCALES)
PARAM=OpenSeismoMatlab(DT,XGTT,'ELRS',T,KSI,ALGID,RINF,DTTOL)
PARAM=OpenSeismoMatlab(DT,XGTT,'RPSRS',CF,ALGID,RINF,MAXTOL,JMAX,DAK)
PARAM=OpenSeismoMatlab(DT,XGTT,'CDRS',T,KSI,MU,PYSF,DTTOL,ALGID,...
    RINF,MAXTOL,JMAX,DAK)
PARAM=OpenSeismoMatlab(DT,XGTT,'CSRS',T,KSI,FYR,PYSF,DTTOL,ALGID,...
    RINF,MAXTOL,JMAX,DAK)
PARAM=OpenSeismoMatlab(DT,XGTT,'FAS')
PARAM=OpenSeismoMatlab(DT,XGTT,'BUTTERWORTHHIGH',BORDER,FLC)
PARAM=OpenSeismoMatlab(DT,XGTT,'BUTTERWORTHLOW',BORDER,FHC)
PARAM=OpenSeismoMatlab(DT,XGTT,'IDA',T,LAMBDAF,IM_DM,M,UY,PYSF,...
    KSI,ALGID,U0,UT0,RINF,MAXTOL,JMAX,DAK)
Omit or set as empty ([]) the input arguments for which default
values are desired.
```

Description

This function calculates the seismic parameters, develops various spectra and performs various analyses from an acceleration time history. More specifically, it calculates the following:

- 1) Peak ground acceleration
- 2) Effective peak ground acceleration
- 3) Peak ground velocity
- 4) Peak ground displacement
- 5) Total cumulative energy and normalized cumulative energy vs time
- 6) Significant duration D_{5-95} according to Trifunac & Brady (1975)
- 7) Significant duration D_{5-75}
- 8) Total Arias intensity (I_a)
- 9) Velocity time history (with baseline correction or not)
- 10) Displacement time history (with baseline correction or not)
- 11) Resampled acceleration time history (i.e. the input acceleration time history with modified time step size)
- 12) Linear elastic pseudo-acceleration response spectrum
- 13) Linear elastic pseudo-velocity response spectrum
- 14) Linear elastic displacement response spectrum
- 15) Linear elastic velocity response spectrum
- 16) Linear elastic acceleration response spectrum

- 17) Rigid plastic sliding displacement response spectrum
- 18) Rigid plastic sliding velocity response spectrum
- 19) Rigid plastic sliding acceleration response spectrum
- 20) Constant ductility displacement response spectrum
- 21) Constant ductility velocity response spectrum
- 22) Constant ductility acceleration response spectrum
- 23) Fourier amplitude spectrum
- 24) Mean period (T_m)
- 25) Lowpass Butterworth-filtered acceleration time history
- 26) Highpass Butterworth-filtered acceleration time history
- 27) Incremental Dynamic Analysis (IDA) of SDOF system excited with the input acceleration time history
- 28) Spectral intensity according to Housner (1952)
- 29) Spectral intensity according to Nau & Hall (1984)

Depending on the value of SW, which determines the type of analysis that OpenSeismoMatlab performs, various additional parameters are needed as input by the user. All possible syntaxes appear above.

Input parameters

DT [double(1 x 1)] is the size of the time step of the input acceleration time history xgtt.

XGTT [double(:inf x 1)] is the input acceleration time history.

XGT [double(:inf x 1)] is the input velocity time history.

SW [char(1 x :inf)] is a string which determines which parameters, spectras or analyses of the input acceleration time history will be calculated. SW can take one of the following values (strings are case insensitive):

- 'TIMEHIST': the displacement, velocity and acceleration time histories are calculated.
- 'RESAMPLE': the acceleration time history with modified time step size is calculated.
- 'PGA': The peak ground acceleration is calculated.
- 'PGV': The peak ground velocity is calculated.
- 'PGD': The peak ground displacement is calculated.
- 'ARIAS': The total cumulative energy, significant duration D_{5_95} according to Trifunac & Brady (1975), significant duration D_{5_75} and Arias intensity are calculated.
- 'PULSEDECOMP': the (velocity) time history is decomposed into a pulse and a residual motion
- 'ELRS': The linear elastic response spectra and pseudospectra are calculated.
- 'RPSRS': The rigid plastic sliding response spectra are calculated.
- 'CDRS': The constant ductility response spectra are calculated.
- 'CSRS': The constant strength response spectra are calculated.
- 'IDA': Incremental Dynamic Analysis of an elastoplastic SDOF system excited by the input acceleration time history is performed.
- 'FAS': The Fourier amplitude spectrum and the mean period are calculated.
- 'BUTTERWORTHHIGH': The high-pass Butterworth filtered acceleration time history is calculated.
- 'BUTTERWORTHLOW': The low-pass Butterworth filtered acceleration time history is calculated.
- 'EPGA': Effective Peak Ground Acceleration.
- 'SIH1952': Spectral Intensity according to Housner (1952).
- 'SINH1984': Spectral Intensity according to Nau & Hall (1984).

Additional required parameters

ALGID [char(1 x :inf)] is the algorithm to be used for the time integration, if applicable. It can be one of the following

strings for superior optimally designed algorithms (strings are case sensitive):

'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm
'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
'U1-V0-Opt': Optimal numerical dissipation and dispersion first order displacement zero order velocity algorithm
'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm
'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order velocity algorithm
'Newmark ACA': Newmark Average Constant Acceleration method
'Newmark LA': Newmark Linear Acceleration method
'Newmark BA': Newmark Backward Acceleration method
'Fox-Goodwin': Fox-Goodwin formula

Default value 'U0-V0-Opt'.

BASELINE_{SW} [logical(1 x 1)] determines if baseline correction will be applied for the calculation of the various time histories.

BORDER [double(1 x 1)] is the order of the Butterworth filter that is applied for filtering of the acceleration time history.

CF [double(1:numSDOFs x 1)] contains the values of the Coulomb friction coefficient for which the response spectra are requested. numSDOFs is the number of SDOF oscillators being analysed to produce the spectra.

DAK [double(1 x 1)] is the infinitesimal acceleration for the calculation of the derivative required for the convergence of the Newton-Raphson iteration.

DTI [double(1 x 1)] is the new time step size for resampling of the input acceleration time history.

DTTOL [double(1 x 1)] is the tolerance for resampling of the input acceleration time history. For a given eigenperiod T, resampling takes place if $DT/T > dtTol$. Default value 0.02.

FHC [double(1 x 1)] is the high cutoff frequency for the low-pass Butterworth filter.

FLC [double(1 x 1)] is the low cutoff frequency for the high-pass Butterworth filter.

FYR [double(1 x 1)] is the yield strength ratio (yield shear to weight, V/W).

IM_DM [char(1 x :inf)] is the Intensity Measure (IM) - Damage Measure

(DM) pair that is to be calculated from the incremental dynamic analysis. IM_DM can take one of the following values (strings are case insensitive):

- 'SA_MU': Spectral acceleration-ductility
- 'PGD_MU': Peak displacement-ductility
- 'PGV_MU': Peak velocity-ductility
- 'PGA_MU': Peak acceleration-ductility
- 'SA_DISP': Spectral acceleration-displacement
- 'PGD_DISP': Peak displacement-displacement
- 'PGV_DISP': Peak velocity-displacement
- 'PGA_DISP': Peak acceleration-displacement
- 'SA_VEL': Spectral acceleration-velocity
- 'PGD_VEL': Peak displacement-velocity
- 'PGV_VEL': Peak velocity-velocity
- 'PGA_VEL': Peak acceleration-velocity
- 'SA_ACC': Spectral acceleration-acceleration
- 'PGD_ACC': Peak displacement-acceleration
- 'PGV_ACC': Peak velocity-acceleration
- 'PGA_ACC': Peak acceleration-acceleration

JMAX [double(1 x 1)] is the maximum number of iterations per increment. If JMAX=0 then iterations are not performed and the MAXTOL parameter is not taken into account.

KSI [double(1 x 1)] is the fraction of critical viscous damping.

LAMBDADF [double(:inf x 1)] contains the values of the scaling factor (lambda factor) for the incremental dynamic analysis.

M [double(1 x 1)] is the mass of the SDOF oscillator.

MAXTOL [double(1 x 1)] is the maximum tolerance of convergence of the Full Newton Raphson method for numerical computation of acceleration.

MU [double(1 x 1)] is the specified ductility for which the constant ductility response spectra are calculated.

NSCALES [double(1 x 1)] is the number of pulse period values between TPMIN and TPMAX to be considered for the continuous 1-D wavelet transform of XGT

PYSF [double(1 x 1)] is the post-yield stiffness factor, i.e. the ratio of the postyield stiffness to the initial stiffness. PYSF=0 is not recommended for simulation of an elastoplastic system; a small positive value is always suggested due to numerical reasons. PYSF is ignored if MU=1. Default value 0.01.

RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues of the amplification matrix. For the amplification matrix see eq.(61) in Zhou & Tamma (2004). Default value 0.

T [double(:inf x 1)] contains the values of eigenperiods for which the response spectra are requested. Its length is the number of SDOF oscillators being analysed to produce the spectra. T must be a vector if SW='ELRS' or SW='CDRS'. T must be scalar if SW='IDA'.

TPMAX [double(1 x 1)] is the maximum pulse period to be considered for the continuous 1-D wavelet transform of XGT

TPMIN [double(1 x 1)] is the minimum pulse period to be considered for the continuous 1-D wavelet transform of XGT

U0 [double(1 x 1)] is the initial displacement of the SDOF oscillator.

UT0 [double(1 x 1)] is the initial velocity of the SDOF oscillator.

UY [double(1 x 1)] is the yield displacement of the SDOF oscillator.

WNAME [char(1 x :inf)] is the wavelet family short name to be used for the decomposition of the velocity time history. See the Matlab function waveinfo.m for more details.

Output parameters

PARAM (structure) has the following fields:

PARAM.acc [double(:inf x 1)] Acceleration time history
 PARAM.arias [double(1 x 1)] Total Arias intensity (Ia)
 PARAM.CDPSa [double(:inf x 1)] Constant ductility
 pseudo-acceleration response spectrum
 PARAM.CDPSv [double(:inf x 1)] Constant ductility pseudo-velocity
 response spectrum
 PARAM.CDSa [double(:inf x 1)] Constant ductility acceleration
 response spectrum
 PARAM.CDSd [double(:inf x 1)] Constant ductility displacement
 response spectrum
 PARAM.CDSv [double(:inf x 1)] Constant ductility velocity
 response spectrum
 PARAM.disp [double(:inf x 1)] Displacement time history
 param.DM [double(:inf x 1)] is the damage measure (DM) of the
 incremental dynamic analysis
 PARAM.Ecum [double(1 x 1)] Total cumulative energy
 PARAM.EcumTH [double(:inf x 1)] Normalized cumulative
 energy vs time
 PARAM.EPGA [double(1 x 1)] Effective peak ground acceleration
 PARAM.FAS [double(1:2^(nextpow2(length(xgtt))-1) x 1)] Fourier
 amplitude spectrum
 PARAM.Fm [double(1 x 1)] Mean frequency (Fm)
 PARAM.fyK [double(:inf x 1)] yield limit that each SDOF must have
 in order to attain ductility equal to PARAM.muK.
 param.IM [double(:inf x 1)] is the intensity measure (IM) of the
 incremental dynamic analysis
 PARAM.iterK [double(:inf x 1)] number of iterations needed for
 convergence for each period (each SDOF).
 PARAM.muK [double(:inf x 1)] achieved ductility for each period
 (each SDOF).
 PARAM.PGA [double(1 x 1)] Peak ground acceleration
 PARAM.PGD [double(1 x 1)] Peak ground displacement
 PARAM.PGV [double(1 x 1)] Peak ground velocity
 PARAM.PredPeriod [double(1 x 1)] Predominant period of the PSa
 spectrum
 PARAM.PredPSa [double(1 x 1)] Predominant acceleration of the PSa
 spectrum
 PARAM.PSa [double(:inf x 1)] Linear elastic pseudo-acceleration
 response spectrum
 PARAM.PSv [double(:inf x 1)] Linear elastic pseudo-velocity
 response spectrum
 PARAM.pulseTH [double(:inf x 1)] Time history of the pulse
 contained in velocity time history
 PARAM.restTH [double(:inf x 1)] Time history of the residual
 motion after subtracting the pulse from the velocity time
 history
 PARAM.RPSSa [double(:inf x 1)] Rigid plastic sliding response
 spectral acceleration
 PARAM.RPSSd [double(:inf x 1)] Rigid plastic sliding response
 spectral displacement
 PARAM.RPSSv [double(:inf x 1)] Rigid plastic sliding response
 spectral velocity
 PARAM.Sa [double(:inf x 1)] Linear elastic acceleration response
 spectrum
 PARAM.Sd [double(:inf x 1)] Linear elastic displacement response
 spectrum
 PARAM.SI [double(1 x 1)] Spectral intensity
 PARAM.Siev [double(:inf x 1)] Linear elastic relative input
 energy equivalent velocity spectrum
 PARAM.Sv [double(:inf x 1)] Linear elastic velocity response

spectrum
PARAM.t_5_75 [double(1 x 2)] Time instants at which 5% and 75% of
cumulative energy have occurred
PARAM.t_5_95 [double(1 x 2)] Time instants at which 5% and 95% of
cumulative energy have occurred
PARAM.Td_5_75 [double(1 x 1)] Time between when 5% and 75% of
cumulative energy has occurred
PARAM.Td_5_95 [double(1 x 1)] Time between when 5% and 95% of
cumulative energy has occurred (significant duration
according to Trifunac-Brady (1975))
PARAM.time [double(:inf x 1)] Time
PARAM.Tm [double(1 x 1)] Mean period (Tm)
PARAM.Tp [double(1 x 1)] Period of the pulse
PARAM.vel [double(:inf x 1)] Velocity time history
PARAM.wavCoefs [double(1 x 1)] Coefficient for the extracted
wavelet
PARAM.wavScale [double(1 x 1)] Scale at which the largest wavelet
was found

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doc PulseDecomp

Documentation of the PulseDecomp function.

```
helpFun('PulseDecomp')
```

Pulse decomposition of a velocity time history

```
[PULSETH, RESTH, TP, WAVSCALE, WAVCOEFS]=PulseDecomp(DT, XGT, WNAME, TPMIN, ...  
    TPMAX, NSCALES)
```

Description

This function decomposes an input velocity time history record into a pulse motion and a residual motion. The shape of the pulse depends on the value of the WNAME parameter. To obtain the velocity time history of a given acceleration record use the command:

```
PARAM=OpenSeismoMatlab(DT, XGTT, 'TIMEHIST', BASELINESW)
```

To extract more than one pulse wavelets from a velocity time history (let's say N), apply this function repetitively N times where at each time (except for the first) this function is applied to the residual motion of the previous time:

```
[PULSETH1, RESTH1, ~, ~, ~]=PulseDecomp(DT, XGT, WNAME, TPMIN, TPMAX, ...  
    NSCALES)
```

```
[PULSETH2, RESTH2, ~, ~, ~]=PulseDecomp(DT, RESTH1, WNAME, TPMIN, TPMAX, ...  
    NSCALES)
```

etc.

Input parameters

DT [double(1 x 1)] is the time step of the input velocity time history XGT.

XGT [double(1:numsteps x 1)] is the input velocity time history. numsteps is the length of the input velocity time history.

WNAME [char(1 x :inf)] is the wavelet family short name to be used for the decomposition of the velocity time history. See the Matlab function waveinfo.m for more details.

TPMIN [double(1 x 1)] is the minimum pulse period to be considered for the continuous 1-D wavelet transform of XGT

TPMAX [double(1 x 1)] is the maximum pulse period to be considered for the continuous 1-D wavelet transform of XGT

NSCALES [double(1 x 1)] is the number of pulse period values between TPMIN and TPMAX to be considered for the continuous 1-D wavelet transform of XGT

Output parameters

PULSETH [double(1:numsteps x 1)] is the velocity time history of the pulse contained in the input velocity time history. numsteps is the length of the input velocity time history.

RESTH [double(1:numsteps x 1)] is the velocity time history of the residual motion after subtracting the time history of the pulse from the input velocity time history. numsteps is the length of the input velocity time history.

TP [double(1 x 1)] is the period of the pulse which is extracted from the input velocity time history.

WAVSCALE [double(1 x 1)] is the scale at which the largest wavelet was found.

WAVCOEFS [double(1 x 1)] is the coefficient for the extracted

wavelet.

Example

```
rng(0)
% Duration in seconds
duration = 10;
% Time step
dt = 0.01;
% Time vector
t = linspace(0, duration, duration /dt)';
% Number of sinusoidal components
num_sin_components = 3;
% Generate a random seismic signal using a combination of sinusoids
xgt = zeros(length(t),1);
for i = 1:num_sin_components
    % Generate the sinusoidal component
    s = rand * sin(2 * pi * 0.5*rand * t + rand);
    % Add the component to the seismic signal
    xgt = xgt + s;
end
% Setup wavelet parameters
wname = 'db4';
TpMin = 0.25;
TpMax = 15;
nScales = 50;
% Apply pulse decomposition
[pulseTH,resTH,Tp,wavScale,wavCoef] = ...
    PulseDecomp(dt,xgt,wname,TpMin,TpMax,nScales);
% Plot the results
np = length(xgt);
time = dt:dt:dt*np;
fig = figure();
subplot(3,1,1)
plot(time, xgt, '-k')
legend('Original ground motion','location','northwest')
ylabel('Velocity');
set(gca, 'xticklabel', [])
subplot(3,1,2)
plot(time, pulseTH, '-r')
legend('Extracted pulse','location','northwest')
ylabel('Velocity');
set(gca, 'xticklabel', [])
subplot(3,1,3)
plot(time, resTH, '-k')
legend('Residual ground motion','location','northwest')
hy = ylabel('Velocity');
hx = xlabel('Time [s]');
```

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Documentation of the RPSReSp function.

```
helpFun('RPSReSp')
```

Rigid Plastic Sliding Response Spectra

```
[SD,SV,SA]=RPSReSp(DT,XGTT,CF,ALGID,RINF,MAXTOL,JMAX,DAK)
```

Description

The rigid plastic sliding response spectra for a given time-history of constant time step and a given Coulomb friction coefficient range are computed.

Input parameters

DT [double(1 x 1)] is the time step of the input acceleration time history XGTT.

XGTT [double(1:numsteps x 1)] is the input acceleration time history. numsteps is the length of the input acceleration time history.

CF [double(1:numSDOFs x 1)] contains the values of the Coulomb friction coefficient for which the response spectra are requested. numSDOFs is the number of SDOF oscillators being analysed to produce the spectra.

ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:

'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)

'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)

'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)

'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm

'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm

'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm

'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm

'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm

'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm

'U1-V0-Opt': Optimal numerical dissipation and dispersion first order displacement zero order velocity algorithm

'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm

'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order


```

velocity algorithm
'Newmark ACA': Newmark Average Constant Acceleration method
'Newmark LA': Newmark Linear Acceleration method
'Newmark BA': Newmark Backward Acceleration method
'Fox-Goodwin': Fox-Goodwin formula
RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues
of the amplification matrix. For the amplification matrix see
eq.(61) in Zhou & Tamma (2004).
MAXTOL [double(1 x 1)] is the maximum tolerance of convergence of the
Full Newton Raphson method for numerical computation of
acceleration.
JMAX [double(1 x 1)] is the maximum number of iterations per
increment. If JMAX=0 then iterations are not performed and the
MAXTOL parameter is not taken into account.
DAK [double(1 x 1)] is the infinitesimal acceleration for the
calculation of the derivative required for the convergence of the
Newton-Raphson iteration.

```

Output parameters

```

SD [double(1:numSDOFs x 1)] is the Spectral Displacement.
SV [double(1:numSDOFs x 1)] is the Spectral Velocity.
SA [double(1:numSDOFs x 1)] is the Spectral Acceleration.

```

Example

```

dt=0.02;
N=1;
a=rand(N,1)-0.5;
b=100*pi*rand(N,1);
c=pi*(rand(N,1)-0.5);
t=(0:dt:(100*dt))';
xgtt=zeros(size(t));
for i=1:N
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));
end
figure()
plot(t,xgtt)
CF=linspace(0.05,0.5,1000)';
AlgID='U0-V0-Opt';
rinf=1;
maxtol=0.01;
jmax=200;
dak=eps;
[Sd,Sv,Sa]=RPSReSp(dt,xgtt,CF,AlgID,rinf,maxtol,jmax,dak);
figure()
plot(CF,Sd)
figure()
plot(CF,Sv)
figure()
plot(CF,Sa)

```

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verification Constant ductility response spectrum

Contents

- [Reference](#)
- [Description](#)
- [Load earthquake data](#)
- [Calculate constant ductility response spectra of earthquake motion](#)
- [Plot the constant ductility response spectra](#)
- [Copyright](#)

Reference

Chopra, A. K. (2020). Dynamics of structures, Theory and Applications to Earthquake Engineering, 5th edition. Prentice Hall.

Description

The constant-ductility response spectra of Figure 7.5.2 of the above reference are verified. Elastic-perfectly plastic systems are considered. Damping is equal to 5% of its critical value. Target ductility factors equal to 1,1.5,2,4 and 8 are considered.

Load earthquake data

Earthquake acceleration time history of the El Centro earthquake will be used (El Centro, 1940, El Centro Terminal Substation Building)

```
fid=fopen('elcentro_NS_trunc.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtd=text{1,2};
```

Calculate constant ductility response spectra of earthquake motion

Switch

```
sw='cdrs';
```

Eigenperiods

```
T=logspace(log10(0.05),log10(3),20);
```

Critical damping ratio

```
ksi=0.05;
```

Ductilities

```
mu1=1;
```

```
mu2=1.5;  
mu3=2;  
mu4=4;  
mu5=8;
```

Post-yield stiffness factor

```
pysf=0.001;
```

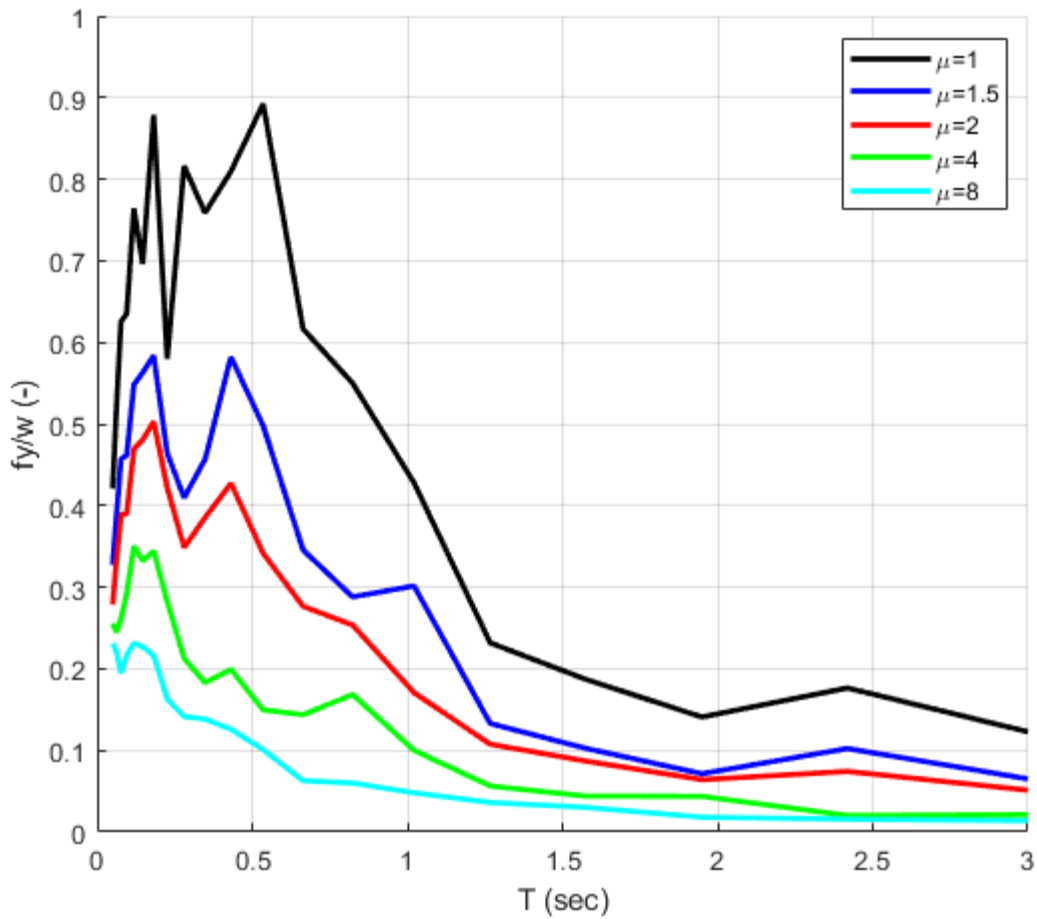
Apply OpenSeismoMatlab once for each target ductility value

```
S1=OpenSeismoMatlab(dt,xgtd,sw,T,ksi,mu1,pysf);  
S2=OpenSeismoMatlab(dt,xgtd,sw,T,ksi,mu2,pysf);  
S3=OpenSeismoMatlab(dt,xgtd,sw,T,ksi,mu3,pysf);  
S4=OpenSeismoMatlab(dt,xgtd,sw,T,ksi,mu4,pysf);  
S5=OpenSeismoMatlab(dt,xgtd,sw,T,ksi,mu5,pysf);
```

Plot the constant ductility response spectra

Initialize figure

```
figure()  
hold on  
% Plot the constant ductility response spectra  
plot(S1.Period,S1.fyK/9.81, 'k-', 'LineWidth', 2)  
plot(S2.Period,S2.fyK/9.81, 'b-', 'LineWidth', 2)  
plot(S3.Period,S3.fyK/9.81, 'r-', 'LineWidth', 2)  
plot(S4.Period,S4.fyK/9.81, 'g-', 'LineWidth', 2)  
plot(S5.Period,S5.fyK/9.81, 'c-', 'LineWidth', 2)  
hold off  
% Finalize figure  
grid on  
xlabel('T (sec)')  
ylabel('fy/w (-)')  
legend({'\mu=1', '\mu=1.5', '\mu=2', '\mu=4', '\mu=8'})  
xlim([0,3])  
ylim([0,1])  
drawnow;  
pause(0.1)
```



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verification Constant strength response spectrum

Contents

- [Reference](#)
- [Description](#)
- [Load earthquake data](#)
- [Calculate constant strength response spectra of earthquake motion](#)
- [Plot the ductility demand response spectra](#)
- [Plot the displacement demand response spectra](#)
- [Copyright](#)

Reference

Tena-Colunga, A. (1999). Simplified seismic evaluation of existing structures, 8th Canadian Conference on Earthquake Engineering, Vancouver, Canada, 317-322.

Description

In the above reference, a new type of spectrum is proposed, the constant strength response spectrum (CSRS). A displacement ductility demand spectrum (DDDS) relates peak displacement ductility demands (and other important response quantities, i.e., displacements) with structural periods of nonlinear elastic-perfectly-plastic hysteretic SDOF systems with given yield strengths. Figure 1 of the above reference is verified in this example. The SDOF system has a yield strength ratio equal to $V/W=0.15$ and the acceleration time history of the SCT-EW component recorded during the 1985 Michoacan earthquake is considered.

Load earthquake data

Earthquake acceleration time history of the 1985 Michoacan earthquake will be used (SCT-EW component). The txt file contains the following columns: time, acceleration N-S, acceleration E-W, acceleration V

```
fid=fopen('sct190985.txt','r');
text=textscan(fid,'%f %f %f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtd=9.81*text{1,3};
```

Calculate constant strength response spectra of earthquake motion

Switch

```
sw='csrs';
```

Eigenperiods

```
T=linspace(0.1,5,50);
```

Critical damping ratio

```
ksi=0.05;
```

Strength ratios

```
fyR=0.15;
```

Post-yield stiffness factor

```
pysf=0.001;
```

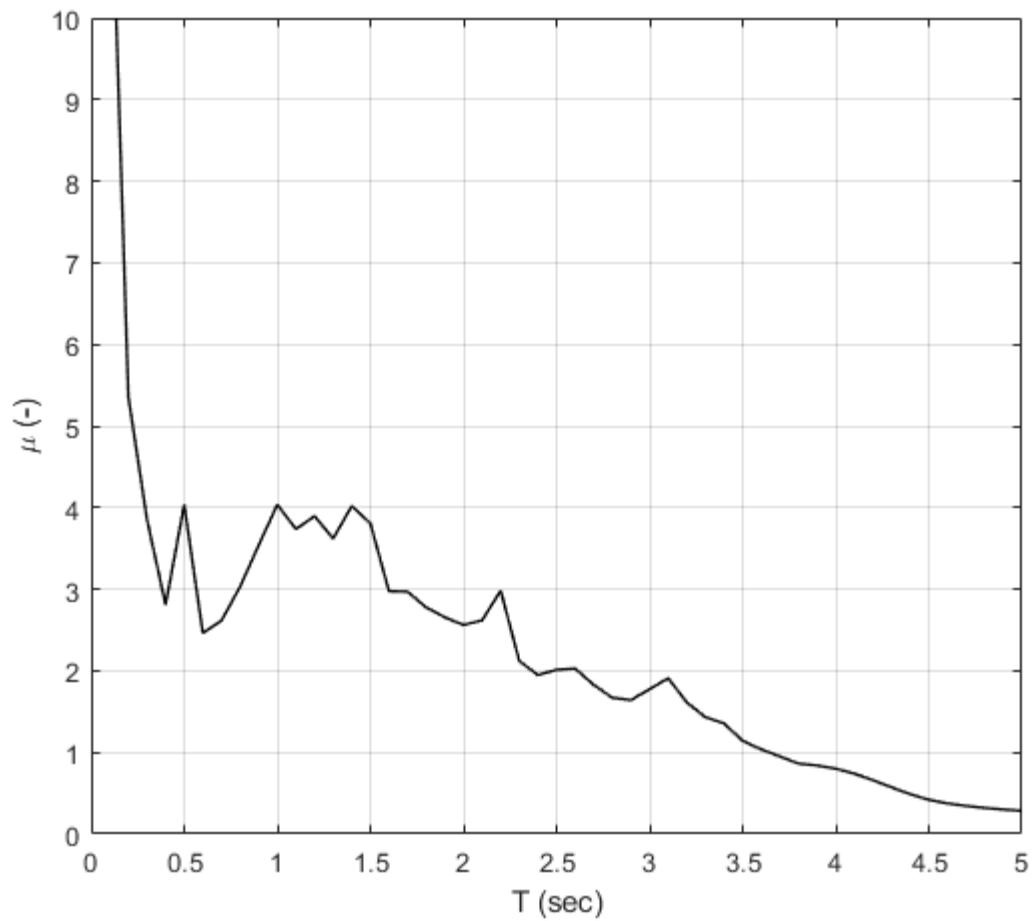
Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw,T,ksi,fyR,pysf);
```

Plot the ductility demand response spectra

Initialize figure

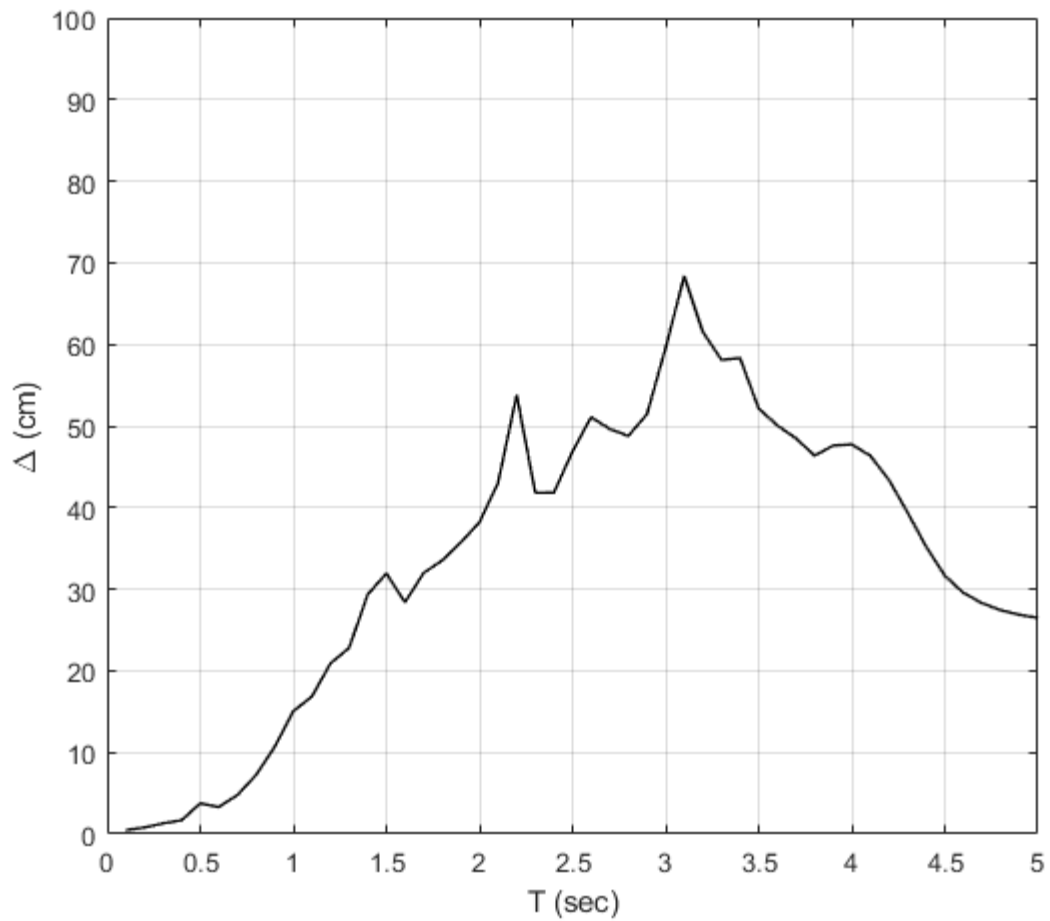
```
figure()  
% Plot the constant strength ductility demand response spectra  
plot(S1.Period,S1.CSSmu, 'k-', 'LineWidth', 1)  
% Finalize figure  
grid on  
xlabel('T (sec)')  
ylabel('\mu (-)')  
xlim([0,5])  
ylim([0,10])  
drawnow;  
pause(0.1)
```



Plot the displacement demand response spectra

Initialize figure

```
figure()
% Plot the constant strength displacement demand response spectra
plot(S1.Period,100*S1.CSSd, 'k-', 'LineWidth', 1)
% Finalize figure
grid on
xlabel('T (sec)')
ylabel('\Delta (cm)')
xlim([0,5])
ylim([0,100])
drawnow;
pause(0.1)
```

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verification Constant strength response spectrum

Contents

- [Reference](#)
- [Description](#)
- [Load earthquake data](#)
- [Calculate constant strength response spectra of earthquake motion](#)
- [Plot the ductility demand response spectra](#)
- [Plot the displacement demand response spectra](#)
- [Copyright](#)

Reference

Tena-Colunga, A. (1999). Simplified seismic evaluation of existing structures, 8th Canadian Conference on Earthquake Engineering, Vancouver, Canada, 317-322.

Description

In the above reference, a new type of spectrum is proposed, the constant strength response spectrum (CSRS). A displacement ductility demand spectrum (DDDS) relates peak displacement ductility demands (and other important response quantities, i.e., displacements) with structural periods of nonlinear elastic-perfectly-plastic hysteretic SDOF systems with given yield strengths. Figure 1 of the above reference is verified in this example. The SDOF system has a yield strength ratio equal to $V/W=0.15$ and the acceleration time history of the SCT-EW component recorded during the 1985 Michoacan earthquake is considered.

Load earthquake data

Earthquake acceleration time history of the 1985 Michoacan earthquake will be used (SCT-EW component). The txt file contains the following columns: time, acceleration N-S, acceleration E-W, acceleration V

```
fid=fopen('sct190985.txt','r');
text=textscan(fid,'%f %f %f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtd=9.81*text{1,3};
```

Calculate constant strength response spectra of earthquake motion

Switch

```
sw='csrs';
```

Eigenperiods

```
T=linspace(0.05,5,50);
```

Critical damping ratio

```
ksi=0.05;
```

Strength ratios

```
fyR=0.10;
```

Post-yield stiffness factor

```
pysf=0.001;
```

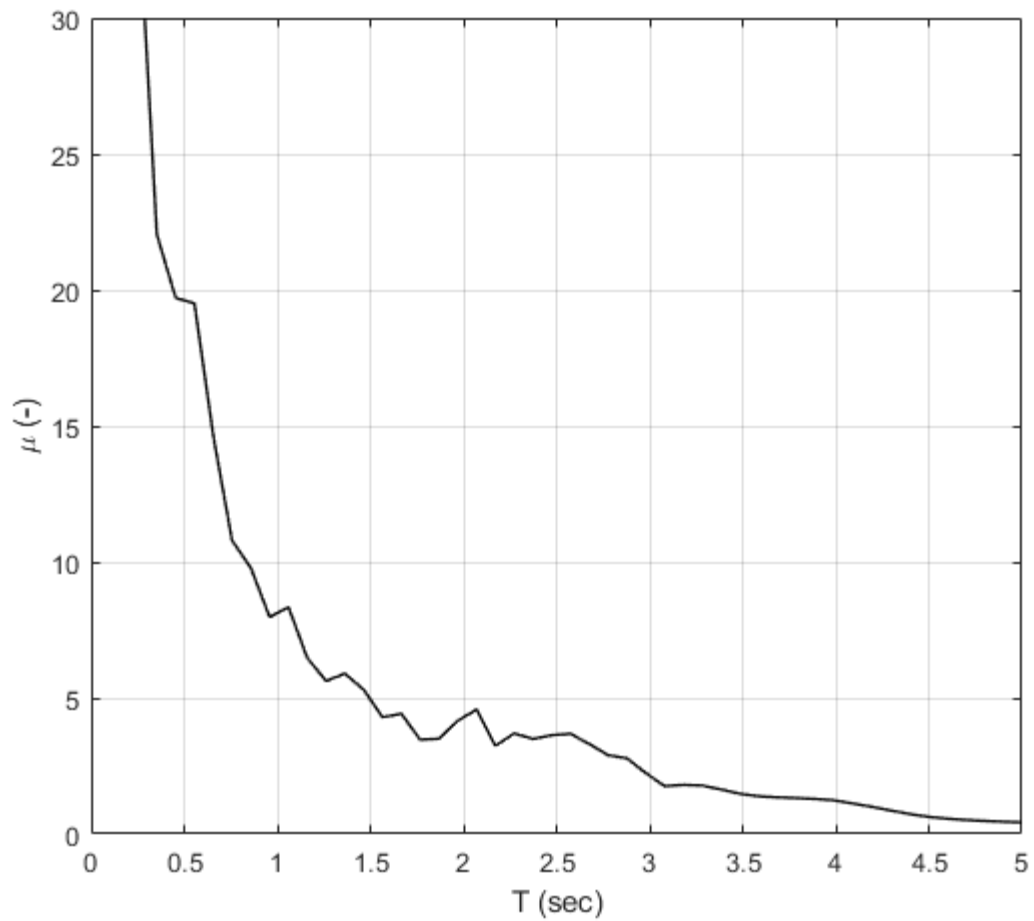
Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw,T,ksi,fyR,pysf);
```

Plot the ductility demand response spectra

Initialize figure

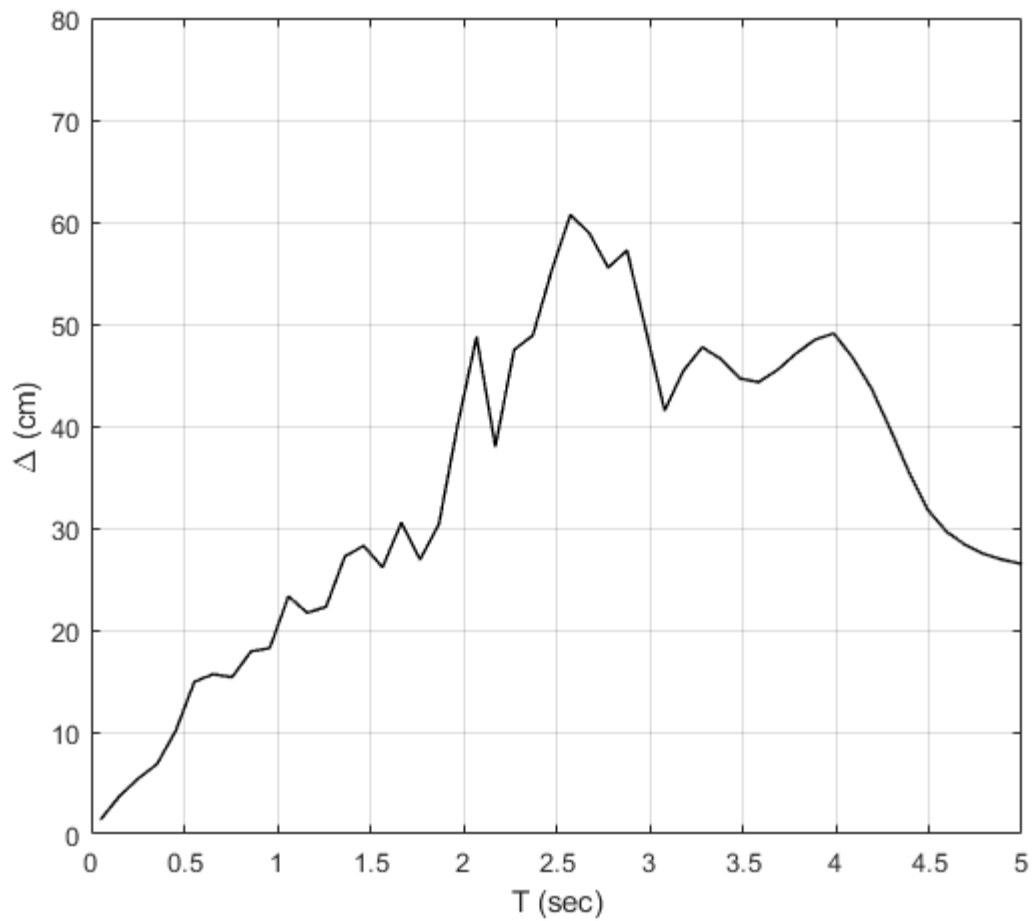
```
figure()  
% Plot the constant strength ductility demand response spectra  
plot(S1.Period,S1.CSSmu, 'k-', 'LineWidth', 1)  
% Finalize figure  
grid on  
xlabel('T (sec)')  
ylabel('\mu (-)')  
xlim([0,5])  
ylim([0,30])  
drawnow;  
pause(0.1)
```



Plot the displacement demand response spectra

Initialize figure

```
figure()
% Plot the constant strength displacement demand response spectra
plot(S1.Period,100*S1.CSSd, 'k-', 'LineWidth', 1)
% Finalize figure
grid on
xlabel('T (sec)')
ylabel('\Delta (cm)')
xlim([0,5])
ylim([0,80])
drawnow;
pause(0.1)
```



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verification Dynamic response history analysis of OpenSeismoMatlab

Calculate linear dynamic response of a MDOF shear building

Contents

- [Reference](#)
- [Description](#)
- [Load earthquake data](#)
- [Setup parameters for DRHA function](#)
- [Calculation of structural properties](#)
- [Calculate dynamic response](#)
- [Roof displacement time history](#)
- [Fifth-story shear time history](#)
- [Base shear time history](#)
- [Base moment time history](#)
- [Copyright](#)

Reference

Chopra, A. K. (2020). Dynamics of structures, Theory and Applications to Earthquake Engineering, 5th edition. Prentice Hall.

Description

The example 13.2.6 (Example: Five-Story Shear Frame) of the above reference is solved in this example. Consider the five-story shear frame of Fig.12.8.1 of the above reference, subjected to the El Centro ground motion. The lumped masses are equal to 45 Mg at each floor, the lateral stiffness of each story is 54.82 kN/cm and the height of each story is 4 m. The damping ratio for all natural modes is 0.05.

Load earthquake data

Earthquake acceleration time history of the El Centro earthquake will be used (El Centro, 1940, El Centro Terminal Substation Building)

```
fid=fopen('elcentro_NS_trunc.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgdt=text{1,2};
```

Setup parameters for DRHA function

Set the storey height of the structure in m.

```
h=4;
```

Set the number of degrees of freedom of the structure, which is equal to the number of its storeys.

```
nDOFs=5;
```

Set the lateral stiffness of each storey in N/m.

```
k=5.482e6;
```

Set the lumped mass at each floor in kg.

```
m=45e3;
```

Calculation of structural properties

Calculate the stiffness matrix of the structure in N/m.

```
K=k*ones(nDOFs,1);
```

Calculate the mass matrix of the structure.

```
M=m*ones(nDOFs,1);
```

Critical damping ratio

```
ksi=0.05;
```

Initial displacement

```
u0=zeros(nDOFs,1);
```

Initial velocity

```
ut0=zeros(nDOFs,1);
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Calculate dynamic response

Apply DRHA

```
[U,V,A,f,Es,Ed] = DRHA(K,M,dt,xgtd,ksi,u0,ut0,AlgID,rinf);
```

Base shear time history

```
FBeig=sum(f,1);
```

5th storey shear time history (5th DOF)

```
Feig=f(1,:);
```

Roof displacement time history (5th DOF)

```
Ueig=U(1,:);
```

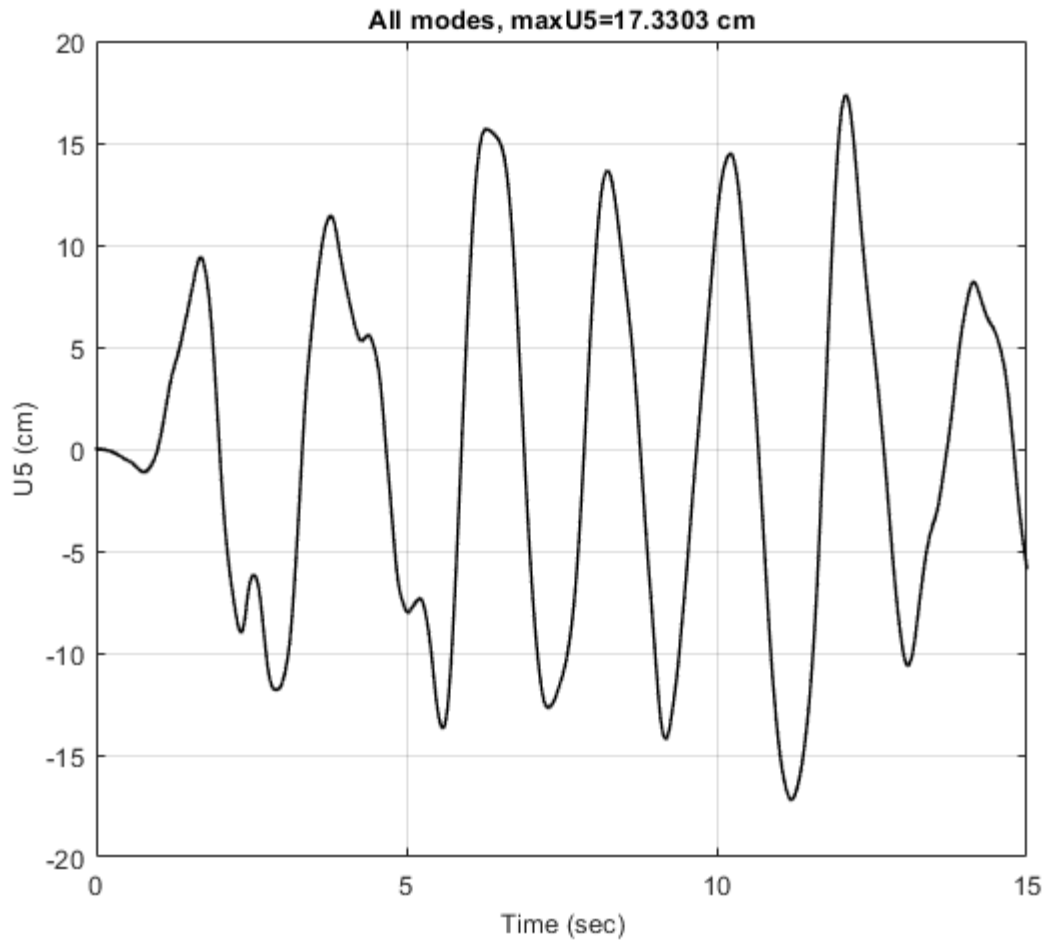
Base moment time history

```
MBeig=sum(f.*repmat((5*h:(-h):h)',1,size(f,2)),1);
```

Roof displacement time history

Plot the roof displacement time history. Convert displacements from m to cm. Verify with Figure 13.2.8 (left) of the above reference.

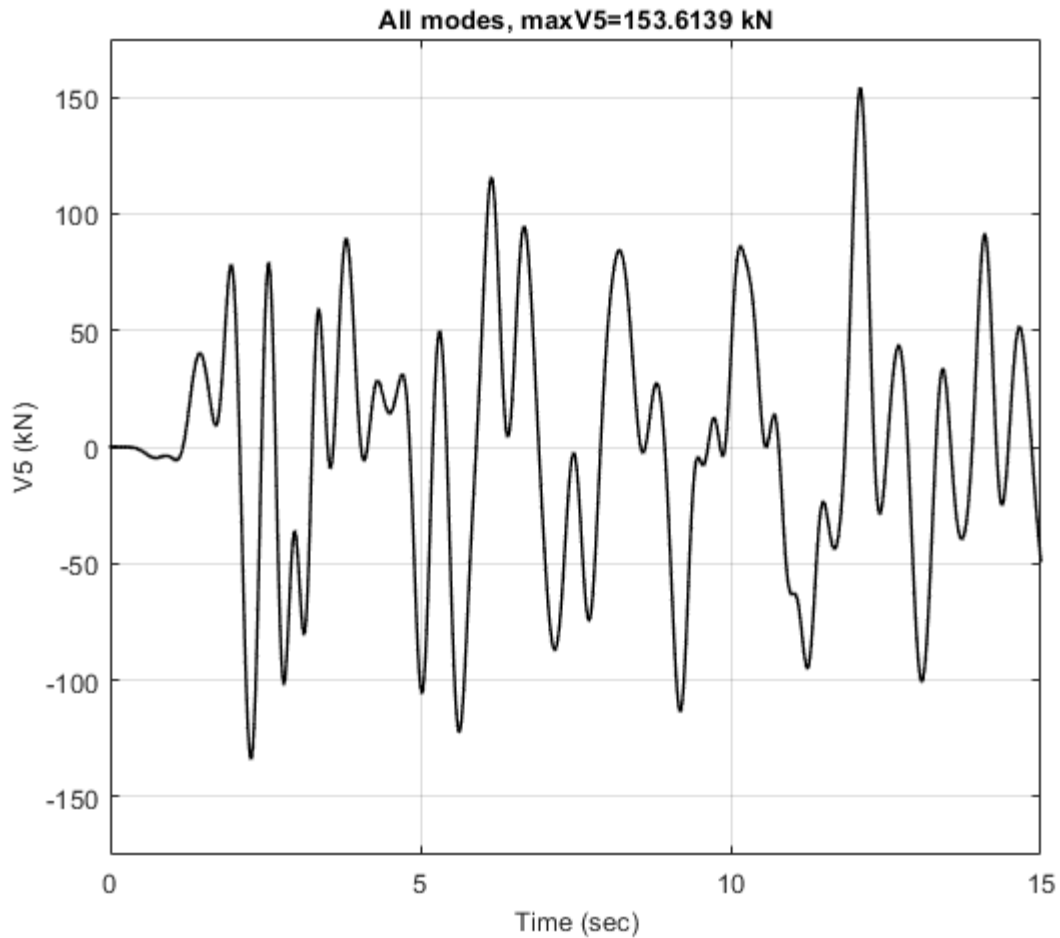
```
figure();
plot(t,100*Ueig,'LineWidth',1.5,'Marker','.',...
      'MarkerSize',1,'Color',[0 0 0],'markeredgecolor','k')
grid on
xlim([0,15])
ylim([-20,20])
xlabel('Time (sec)','FontSize',10);
ylabel('U5 (cm)','FontSize',10);
title(['All modes, maxU5=',num2str(max(abs(100*Ueig))),' cm'],...
      'FontSize',10)
drawnow;
pause(0.1)
```

Fifth-story shear time history

Plot the fifth-story shear time history. Convert forces from N to kN. Verify with Figure 13.2.7 (right) of the above reference.

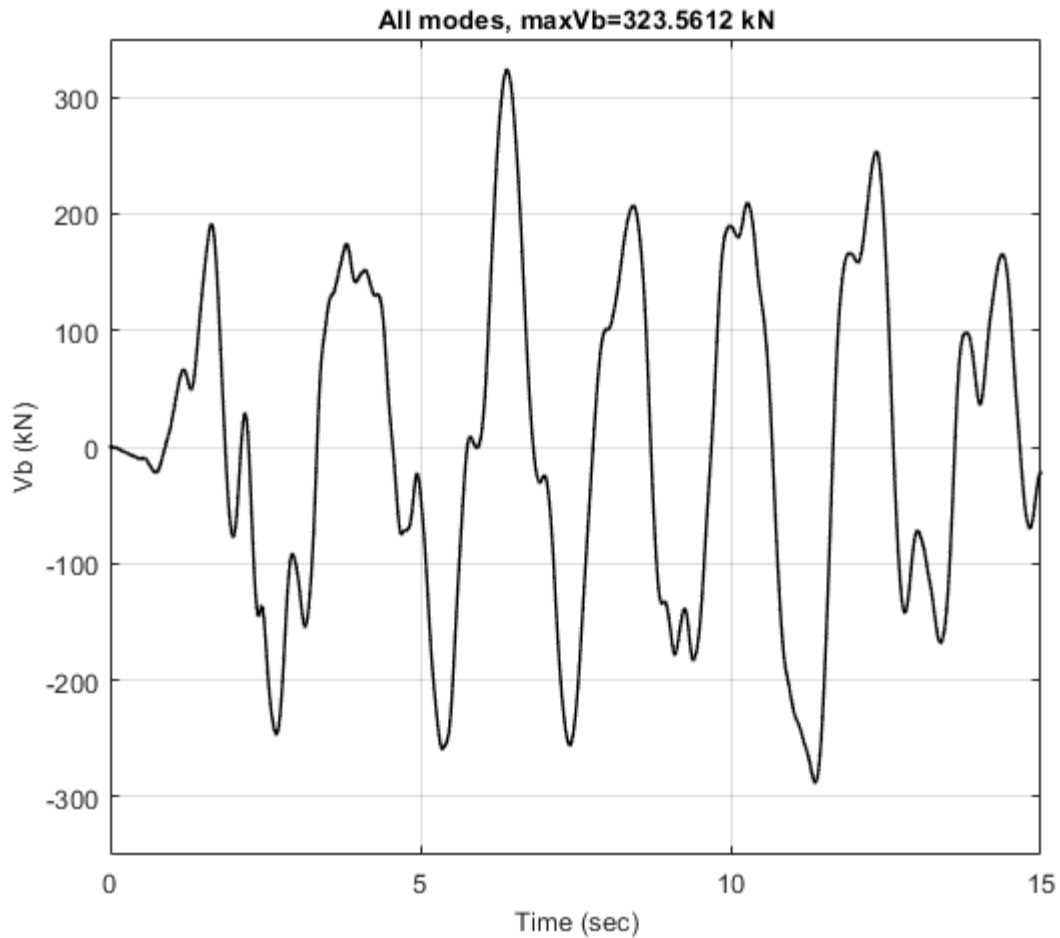
```
figure();
plot(t,Feig/1e3,'LineWidth',1.5,'Marker','.',...
     'MarkerSize',1,'Color',[0 0 0],'markeredgecolor','k')
grid on
xlim([0,15])
ylim([-175,175])
xlabel('Time (sec)','FontSize',10);
ylabel('V5 (kN)','FontSize',10);
title(['All modes, maxV5=',num2str(max(abs(Feig/1e3))),' kN'],...
      'FontSize',10)
drawnow;
pause(0.1)
```



Base shear time history

Plot the base shear time history. Convert forces from N to kN. Verify with Figure 13.2.7 (left) of the above reference

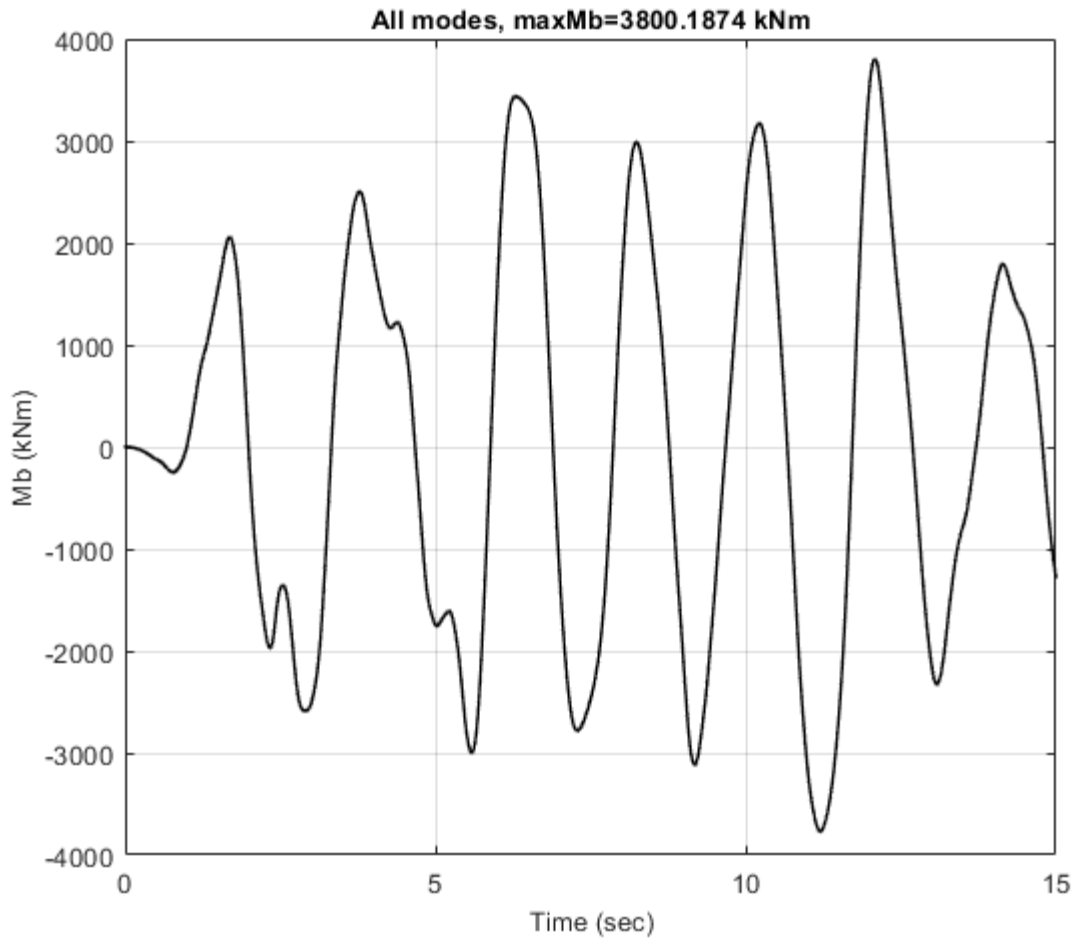
```
figure();
plot(t,FBeig/1e3,'LineWidth',1.,'Marker','.','...
      'MarkerSize',1,'Color',[0 0 0],'markeredgecolor','k')
grid on
xlim([0,15])
ylim([-350,350])
xlabel('Time (sec)','FontSize',10);
ylabel('Vb (kN)','FontSize',10);
title(['All modes, maxVb=',num2str(max(abs(FBeig/1e3))),' kN'],...
      'FontSize',10)
drawnow;
pause(0.1)
```



Base moment time history

Plot the base moment time history. Convert moments from Nm to kNm. Verify with Figure 13.2.8 (right) of the above reference

```
figure();
plot(t,MBeig/1e3,'LineWidth',1.,'Marker','.','...
      'MarkerSize',1,'Color',[0 0 0],'markeredgecolor','k')
grid on
xlim([0,15])
ylim([-4000,4000])
xlabel('Time (sec)','FontSize',10);
ylabel('Mb (kNm)','FontSize',10);
title(['All modes, maxMb=',num2str(max(abs(MBeig/1e3))),' kNm'],...
      'FontSize',10)
drawnow;
pause(0.1)
```



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verification High pass Butterworth filter of OpenSeismoMatlab

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motion](#)
- [Apply high pass Butterworth filter](#)
- [Plot the time history of the initial ground motion](#)
- [Obtain displacement and velocity time histories](#)
- [Plot the displacement time histories](#)
- [Plot the velocity time histories](#)
- [Copyright](#)

Reference

Boore, D. M. (2005). On pads and filters: Processing strong-motion data. Bulletin of the Seismological Society of America, 95(2), 745-750.

Description

Verify Figure 1 of the above reference, for the 1940 El Centro analog recording. The displacements and velocities from unfiltered and filtered accelerations are shown. Filtering is done by using two passes of a fourth-order high pass (i.e. frequencies lower than the cut-off frequency are attenuated) Butterworth filter with cut-off frequency as shown in Figure 1.

Earthquake motion

Load earthquake data

```
eqmotions={'Imperial_Valley_El_Centro_9_EW'};
data=load([eqmotions{1},'.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgtd=data(:,2);
```

Apply high pass Butterworth filter

Switch

```
sw='butterworthhigh';
```

Order of Butterworth filter

```
bOrder=4;
```

Cut-off frequency

```
flc=0.1;
```

Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw,bOrder,flc);
```

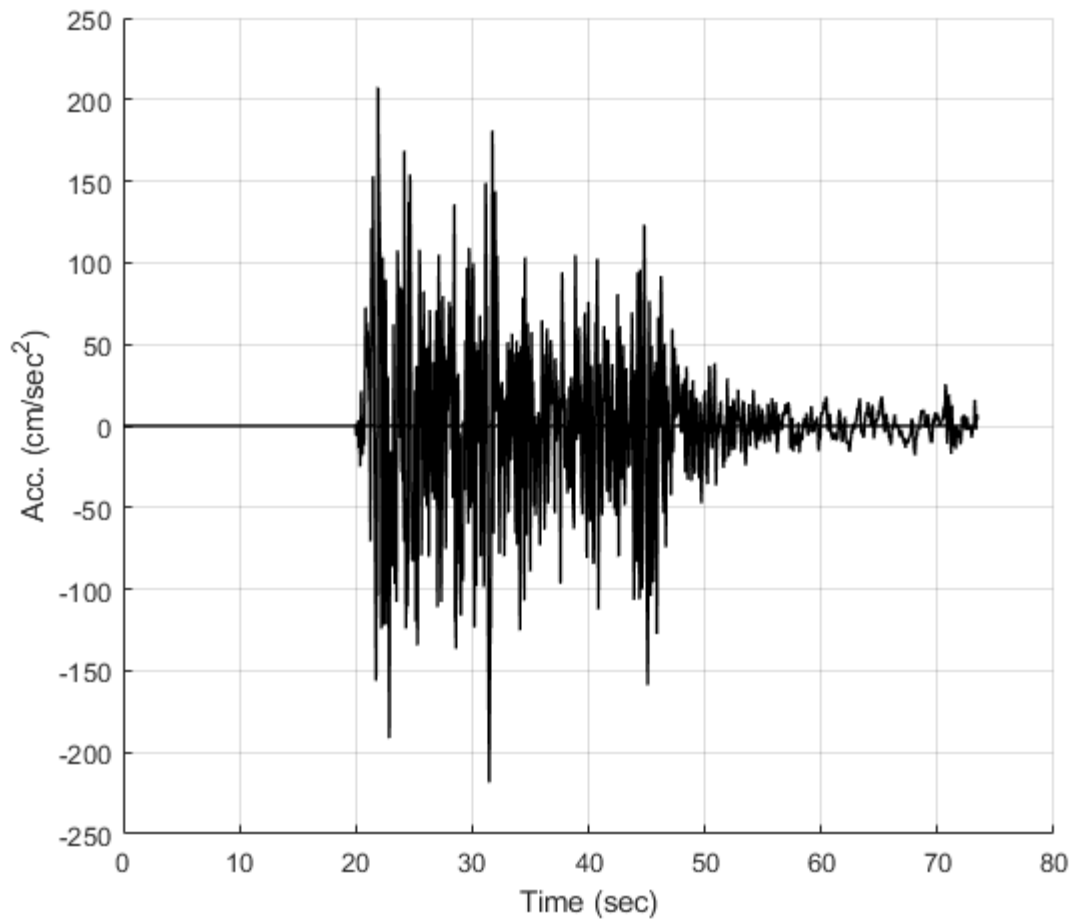
Filtered acceleration

```
cxgtt=S1.acc;
```

Plot the time history of the initial ground motion

Initialize figure

```
figure()
hold on
plot(t,zeros(size(t)),'k','LineWidth',1)
% Plot the acceleration time history of the initial ground motion
plot(t,xgtt,'k','LineWidth',1)
% Finalize figure
hold off
grid on
xlabel('Time (sec)')
ylabel('Acc. (cm/sec^2)')
drawnow;
pause(0.1)
```



Obtain displacement and velocity time histories

Switch

```
sw='timehist';
```

Do not use baseline correction

```
baselineSw=false;
```

Apply OpenSeismoMatlab to the initial ground motion

```
S2=OpenSeismoMatlab(dt,xgtt,sw,baselineSw);
```

Apply OpenSeismoMatlab to the filtered ground motion

```
S3=OpenSeismoMatlab(dt,cxgtt,sw,baselineSw);
```

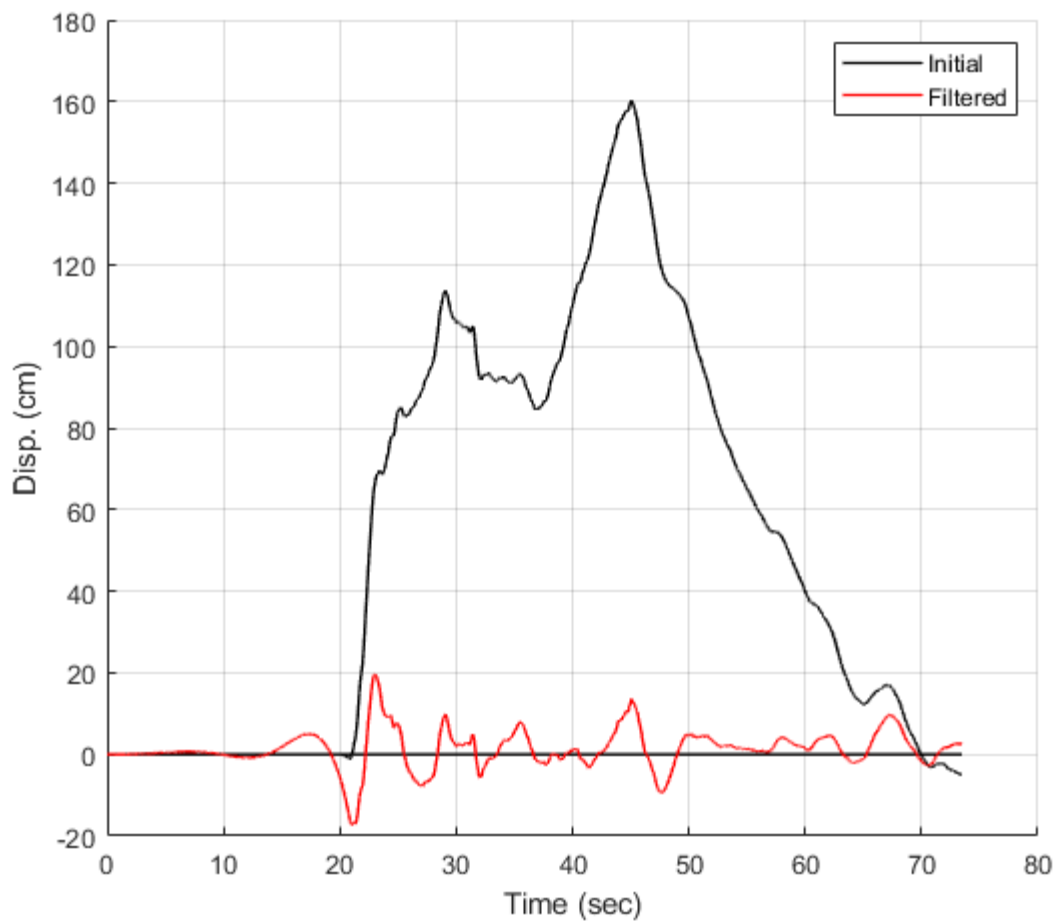
Plot the displacement time histories

Initialize figure

```

figure()
hold on
plot(S3.time,zeros(size(S3.time)),'k','LineWidth',1)
% Plot the displacement time history of the initial ground motion
p1=plot(S2.time,S2.disp,'k','LineWidth',1);
% Plot the displacement time history of the filtered ground motion
p2=plot(S3.time,S3.disp,'r','LineWidth',1);
% Finalize figure
hold off
grid on
legend([p1,p2],{'Initial','Filtered'})
xlabel('Time (sec)')
ylabel('Disp. (cm)')
drawnow;
pause(0.1)

```



Plot the velocity time histories

Initialize figure

```

figure()
hold on
plot(S3.time,zeros(size(S3.time)),'k','LineWidth',1)
% Plot the velocity time history of the initial ground motion
p1=plot(S2.time,S2.vel,'k','LineWidth',1);

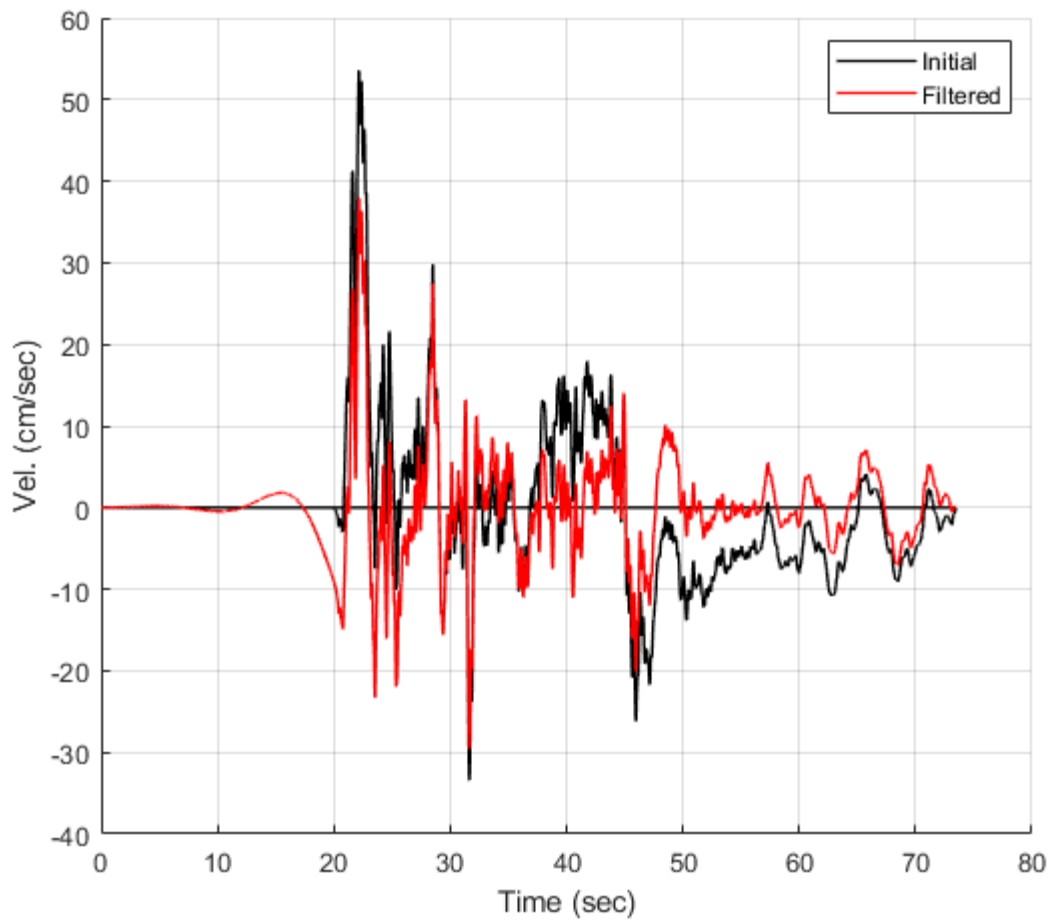
```



```

% Plot the velocity time history of the filtered ground motion
p2=plot(S3.time,S3.vel,'r','LineWidth',1);
% Finalize figure
hold off
grid on
legend([p1,p2],{'Initial','Filtered'})
xlabel('Time (sec)')
ylabel('Vel. (cm/sec)')
drawnow;
pause(0.1)

```



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verification Low- and high- pass Butterworth filter of OpenSeismoMatlab

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motion](#)
- [Apply high pass Butterworth filter](#)
- [Apply low pass Butterworth filter](#)
- [Plot the acceleration time histories](#)
- [Calculate the Fourier spectra](#)
- [Plot the Fourier spectra](#)
- [Calculate the acceleration response spectra](#)
- [Plot the acceleration response spectra](#)
- [Copyright](#)

Reference

Graizer, V. (2012, September). Effect of low-pass filtering and re-sampling on spectral and peak ground acceleration in strong-motion records. In Proceedings of the 15th World Conference of Earthquake Engineering, Lisbon, Portugal (pp. 24-28).

Description

Verify Figure 3.2 of the above reference, for the the MW 6.3 Christchurch, New Zealand earthquake at Heathcote Valley Primary School (HVSC) station, Up-component. The time histories, elastic response spectra and Fourier spectra from unfiltered and filtered accelerations are shown and compared. In the above reference, the ground motion was processed following the 1970s Caltech procedure, low-pass filtered and re-sampled to 50 samples/sec by the GeoNet New Zealand strong motion network. However in this example, Butterworth filter is applied and it gives similar results.

Earthquake motion

Load earthquake data

```
eqmotions={'Christchurch2011HVPS_UP'};
data=load([eqmotions{1},'.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgtt=data(:,2);
xgtt=[zeros(10/dt,1);xgtt];
t=(0:numel(xgtt)-1)*dt;
xgtt=xgtt/9.81;
```

Apply high pass Butterworth filter

Switch

```
sw='butterworthhigh';
```

Order of Butterworth filter

```
bOrder=4;
```

Cut-off frequency

```
flc=0.1;
```

Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw,bOrder,flc);
```

Filtered acceleration

```
cxgtt=S1.acc;
```

Apply low pass Butterworth filter

Switch

```
sw='butterworthlow';
```

Order of Butterworth filter

```
bOrder=4;
```

Cut-off frequency

```
fuc=25;
```

Apply OpenSeismoMatlab to high pass filtered filtered acceleration

```
S2=OpenSeismoMatlab(dt,cxgtt,sw,bOrder,fuc);
```

Filtered acceleration

```
cxgtt=S2.acc;
```

Plot the acceleration time histories

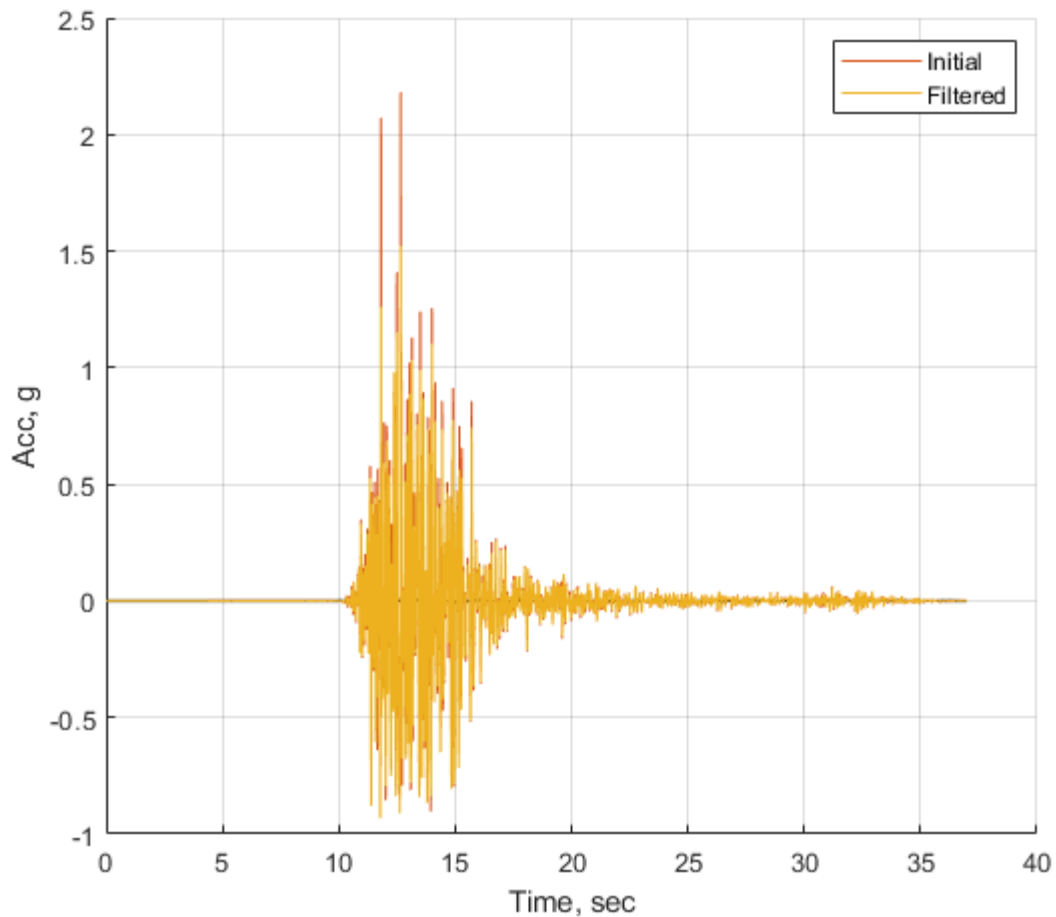
Initialize figure

```
figure()  
hold on  
plot(t,zeros(size(t)),'k','LineWidth',1)  
% Plot the acceleration time history of the initial ground motion
```

```

p1=plot(t,xgtt);
% Plot the acceleration time history of the bandpass filtered ground motion
p2=plot(t,cxgtt);
% Finalize figure
hold off
grid on
legend([p1,p2],{'Initial','Filtered'})
xlabel('Time, sec')
ylabel('Acc, g')
drawnow;
pause(0.1)

```



Calculate the Fourier spectra

Switch

```
sw='fas';
```

Apply OpenSeismoMatlab to the initial ground motion

```
S3=OpenSeismoMatlab(dt,xgtt,sw);
```

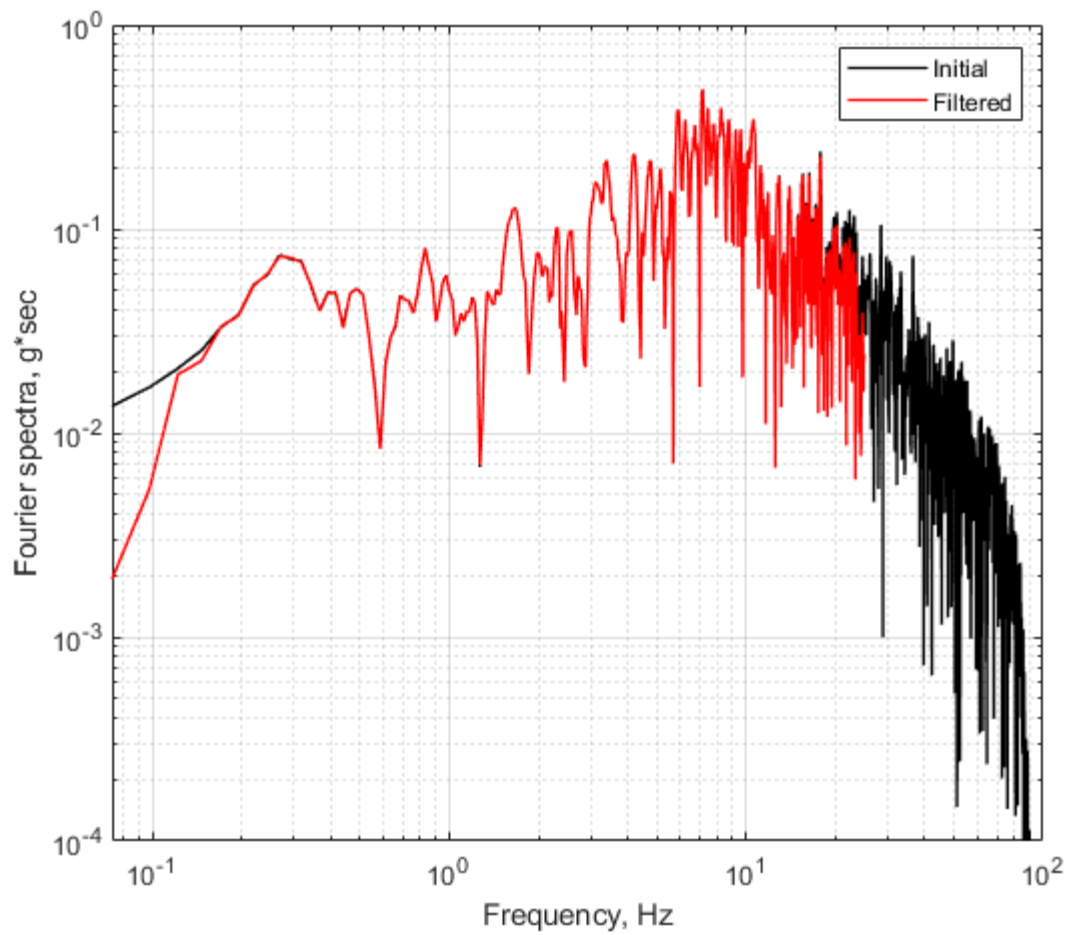
Apply OpenSeismoMatlab to the filtered ground motion

```
S4=OpenSeismoMatlab(dt,cxggtt,sw);
```

Plot the Fourier spectra

Initialize figure

```
figure()
loglog(1,1,'w')
hold on
% Plot the Fourier spectrum of the initial ground motion in logarithmic
% scale for frequencies larger than 0.05 Hz
ind10=S4.freq>=0.05;
p1=loglog(S3.freq(ind10),S3.FAS(ind10),'k','LineWidth',1);
% Plot the Fourier spectrum of the filtered ground motion in logarithmic
% scale for frequencies larger than 0.05 Hz and lower than fuc
ind11=(S4.freq<=fuc)& (S4.freq>=0.05);
p2=loglog(S4.freq(ind11),S4.FAS(ind11),'r','LineWidth',1);
% Finalize figure
hold off
grid on
ylim([1e-4,1])
legend([p1,p2],{'Initial','Filtered'})
xlabel('Frequency, Hz')
ylabel('Fourier spectra, g*sec')
drawnow;
pause(0.1)
```



Calculate the acceleration response spectra

Switch

```
sw='elrs';
```

Critical damping ratio

```
ksi=0.05;
% Period range for which the response spectrum is queried
T=logspace(1,-2,100);
```

Apply OpenSeismoMatlab to the initial ground motion

```
S5=OpenSeismoMatlab(dt,xgtt,sw,T,ksi);
```

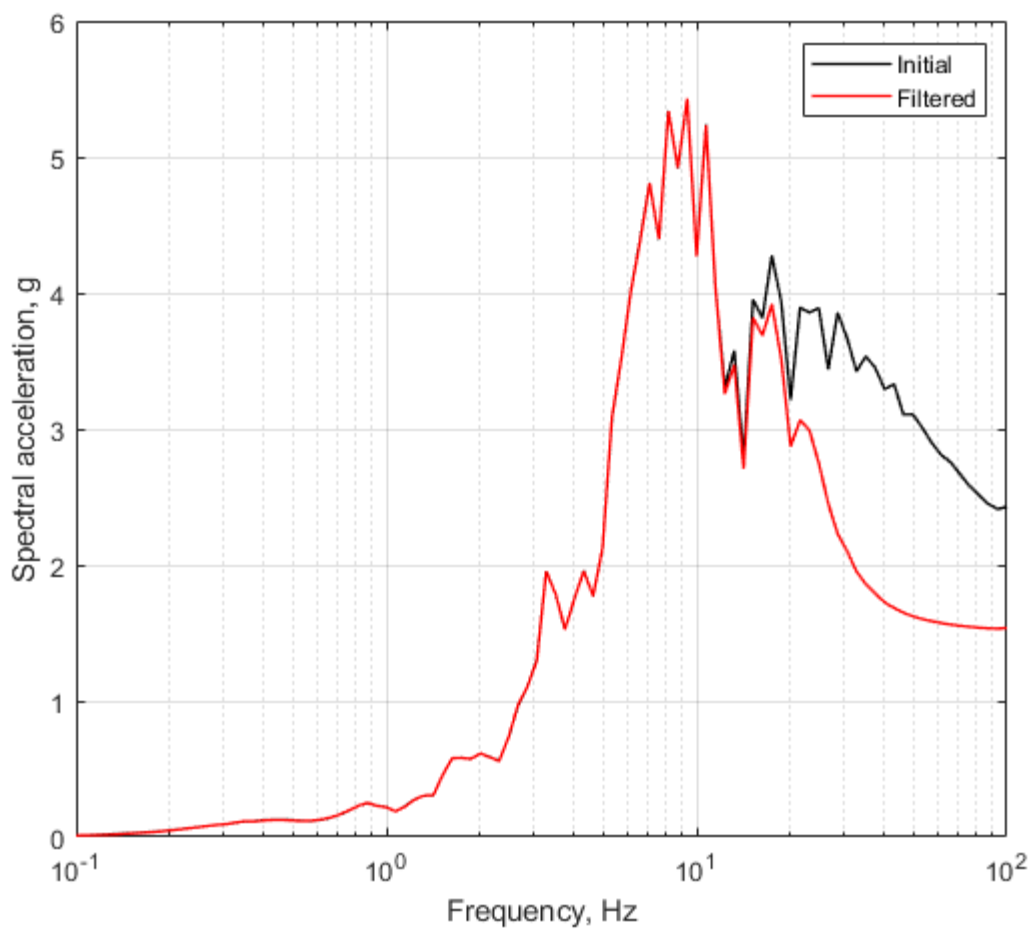
Apply OpenSeismoMatlab to the filtered ground motion

```
S6=OpenSeismoMatlab(dt,cxgtt,sw,T,ksi);
```

Plot the acceleration response spectra

Initialize figure

```
figure()
semilogx(1,1,'w')
hold on
% Plot the acceleration response spectrum of the initial ground motion in
% logarithmic scale
p1=semilogx(1./S5.Period,S5.Sa,'k','LineWidth',1);
% Plot the acceleration response spectrum of the filtered ground motion in
% logarithmic scale
p2=semilogx(1./S6.Period,S6.Sa,'r','LineWidth',1);
% Finalize figure
hold off
grid on
legend([p1,p2],{'Initial','Filtered'})
xlabel('Frequency, Hz')
ylabel('Spectral acceleration, g')
drawnow;
pause(0.1)
```



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-

verification Fourier amplitude spectrum of OpenSeismoMatlab

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motion](#)
- [Calculate the Fourier amplitude spectrum](#)
- [Plot the Fourier amplitude spectrum](#)
- [Plot the Fourier amplitude spectrum in logarithmic scale](#)
- [Copyright](#)

Reference

Analyses of strong motion earthquake accelerograms, Volume IV - Fourier Amplitude Spectra, Part H - Accelerograms I1H115 through I1H126, California Institute of Technology, Earthquake Engineering Research Laboratory, Report No. EERI 74-100, 1974.

Description

Verify the Fourier amplitude spectrum at page 12 of the above reference for the San Fernando earthquake, Feb 9, 1971, 0600 PST, IVH115 71.024.0 15250 Ventura BLVD., basement, Los Angeles, Cal. Component N11E.

Earthquake motion

Load earthquake data

```
eqmotions={'SanFernando1971VenturaBlvdBasement15250LosAngelesCalN11E'};
data=load([eqmotions{1},'.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgtt=100*data(:,2);
```

Calculate the Fourier amplitude spectrum

Switch

```
sw='fas';
```

Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw);
```

Plot the Fourier amplitude spectrum

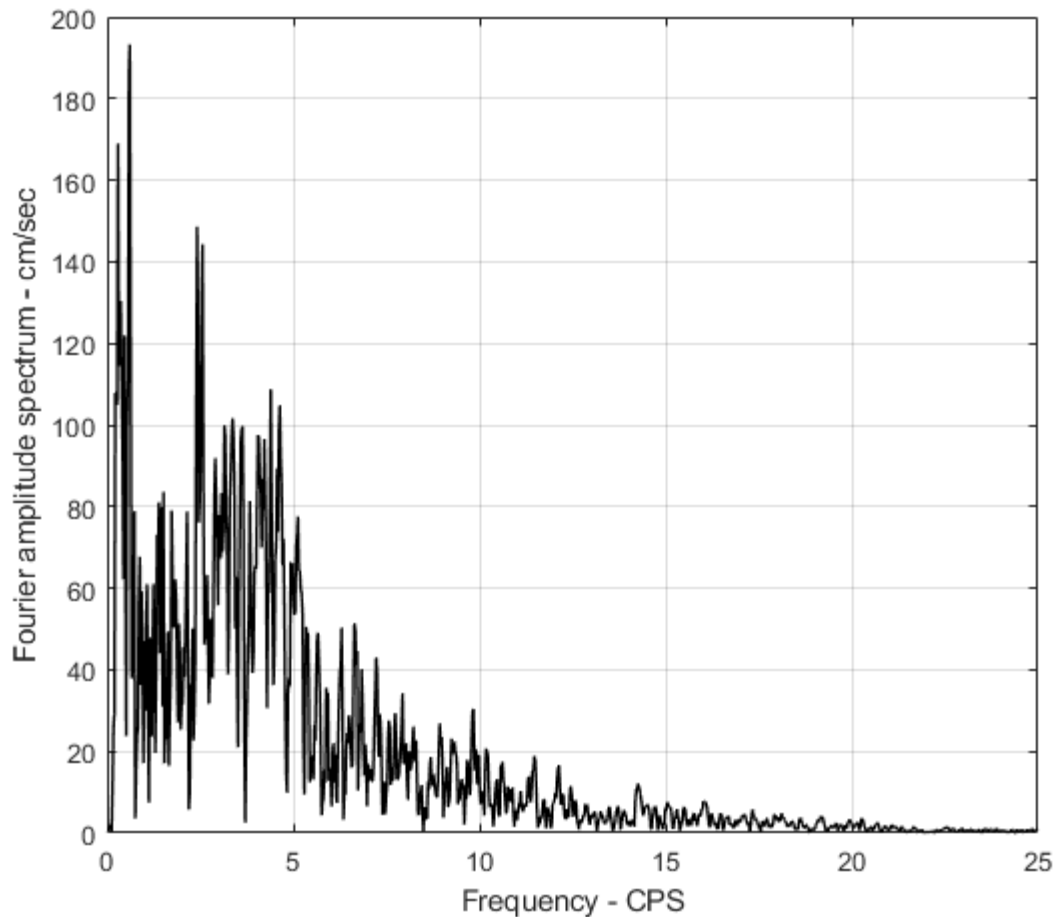
Initialize figure

```
figure()
% Plot the Fourier amplitude spectrum on page 12 of the above reference
plot(S1.freq,S1.FAS,'k','LineWidth',1)
% Finalize figure
```

```

grid on
xlabel('Frequency - CPS')
ylabel('Fourier amplitude spectrum - cm/sec')
ylim([0,200])
xlim([0,25])
drawnow;
pause(0.1)

```



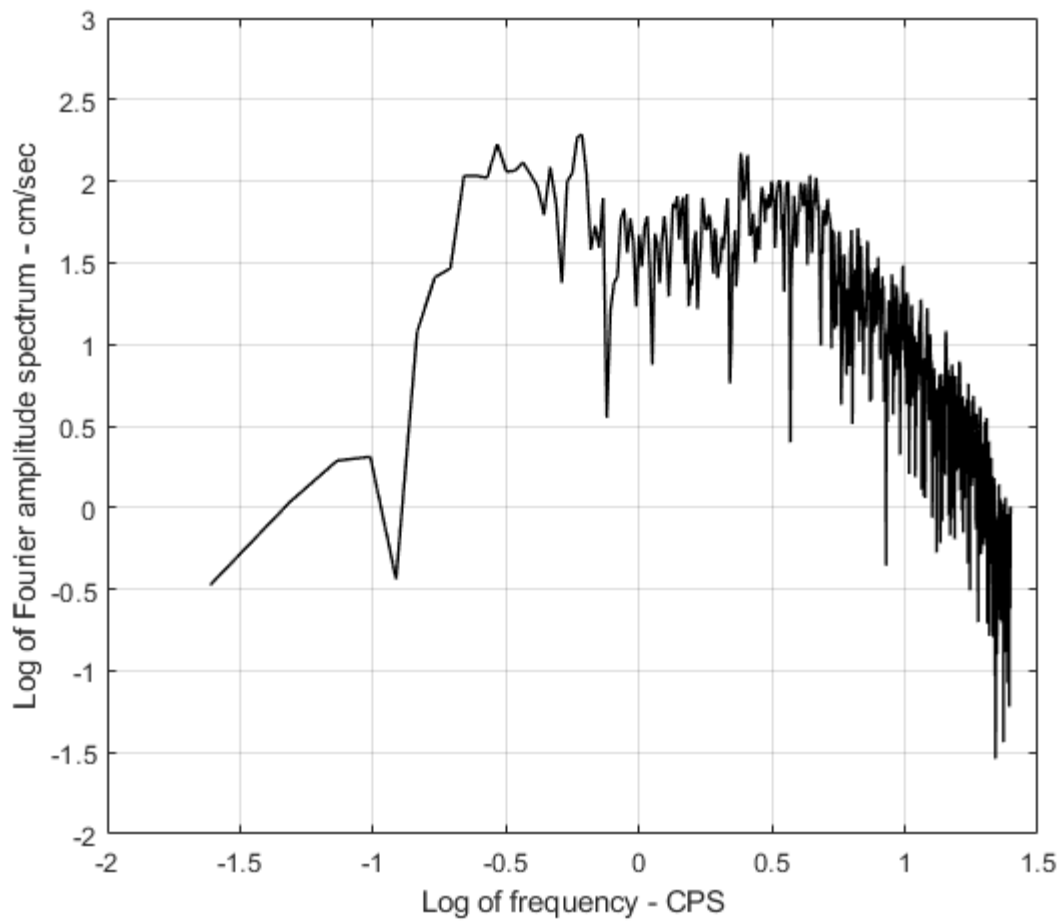
Plot the Fourier amplitude spectrum in logarithmic scale

Initialize figure

```

figure()
% Plot the Fourier amplitude spectrum on page 13 of the above reference
plot(log10(S1.freq),log10(S1.FAS),'k','LineWidth',1)
% Finalize figure
grid on
xlabel('Log of frequency - CPS')
ylabel('Log of Fourier amplitude spectrum - cm/sec')
ylim([-2,3])
xlim([-2,1.5])
drawnow;
pause(0.1)

```



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verification Fourier amplitude spectrum of OpenSeismoMatlab

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motion](#)
- [Calculate the Fourier amplitude spectrum](#)
- [Plot the Fourier amplitude spectrum](#)
- [Plot the Fourier amplitude spectrum in logarithmic scale](#)
- [Copyright](#)

Reference

Analyses of strong motion earthquake accelerograms, Volume IV - Fourier Amplitude Spectra, Part H - Accelerograms I1H115 through I1H126, California Institute of Technology, Earthquake Engineering Research Laboratory, Report No. EERI 74-100, 1974.

Description

Verify the Fourier amplitude spectrum at page 14 of the above reference for the San Fernando earthquake, Feb 9, 1971, 0600 PST, IVH115 71.024.0 15250 Ventura BLVD., basement, Los Angeles, Cal. Component N79W.

Earthquake motion

Load earthquake data

```
eqmotions={'SanFernando1971VenturaBlvdBasement15250LosAngelesCalN79W'};  
data=load([eqmotions{1},'.dat']);  
t=data(:,1);  
dt=t(2)-t(1);  
xgtt=100*data(:,2);
```

Calculate the Fourier amplitude spectrum

Switch

```
sw='fas';
```

Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw);
```

Plot the Fourier amplitude spectrum

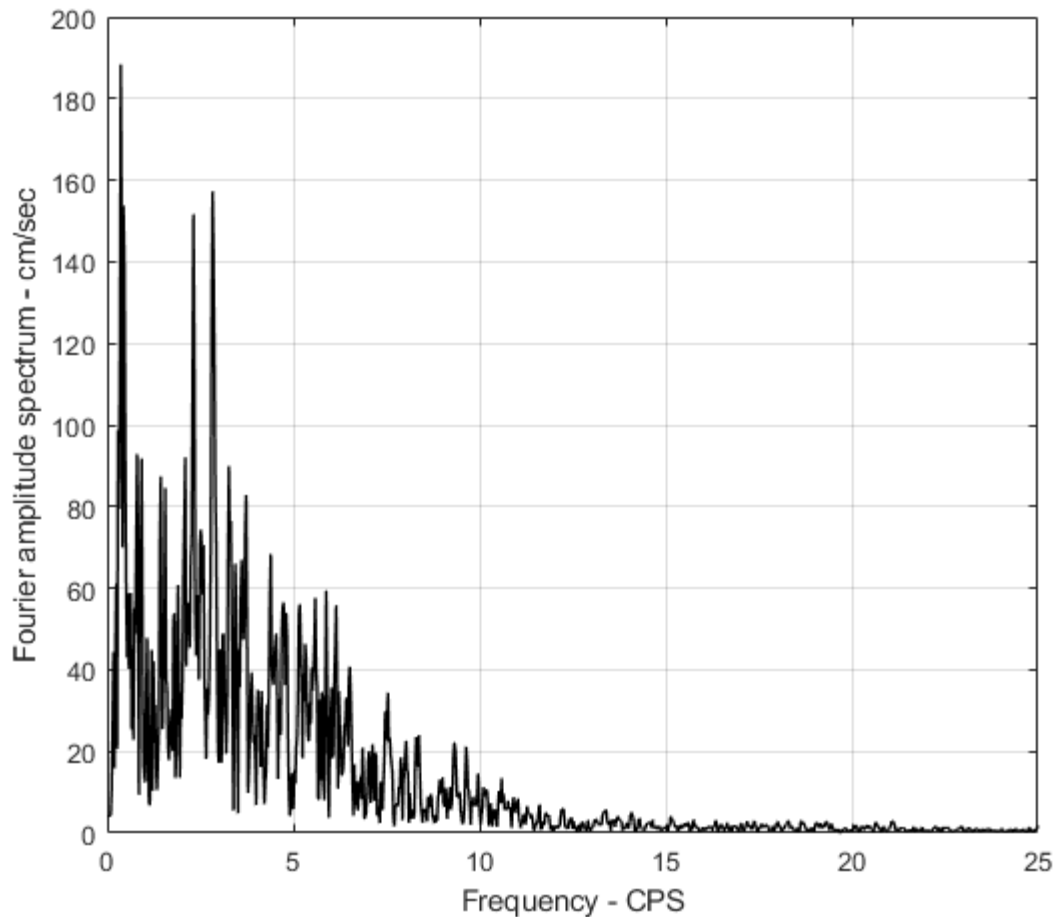
Initialize figure

```
figure()  
% Plot the Fourier amplitude spectrum on page 14 of the above reference  
plot(S1.freq,S1.FAS,'k','LineWidth',1)  
% Finalize figure
```

```

grid on
xlabel('Frequency - CPS')
ylabel('Fourier amplitude spectrum - cm/sec')
ylim([0,200])
xlim([0,25])
drawnow;
pause(0.1)

```



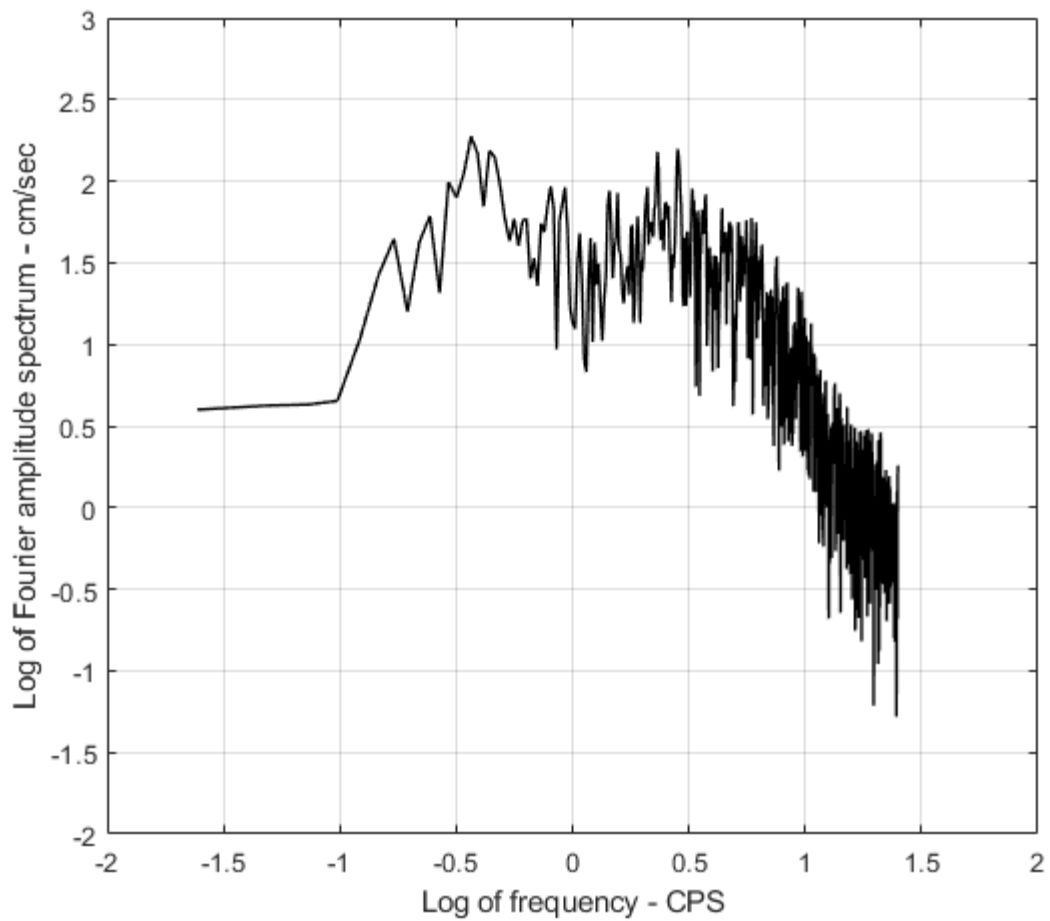
Plot the Fourier amplitude spectrum in logarithmic scale

Initialize figure

```

figure()
% Plot the Fourier amplitude spectrum on page 15 of the above reference
plot(log10(S1.freq),log10(S1.FAS),'k','LineWidth',1)
% Finalize figure
grid on
xlabel('Log of frequency - CPS')
ylabel('Log of Fourier amplitude spectrum - cm/sec')
ylim([-2,3])
xlim([-2,2])
drawnow;
pause(0.1)

```



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verification Incremental dynamic analysis of OpenSeismoMatlab

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motion](#)
- [Adjust earthquake motion to have \$D_{5_75}=8.3\text{sec}\$](#)
- [Calculate duration \$D_{5_75}\$ of adjusted earthquake motion](#)
- [Scale earthquake motion to have \$S_a\(1\text{ sec}\)=0.382g\$](#)
- [Calculate spectral acceleration of scaled earthquake motion](#)
- [Plot the acceleration time history](#)
- [Perform IDA analysis](#)
- [Plot the displacement time histories](#)
- [Copyright](#)

Reference

Mashayekhi, M., Harati, M., Darzi, A., & Estekanchi, H. E. (2020). Incorporation of strong motion duration in incremental-based seismic assessments. *Engineering Structures*, 223, 111144.

Description

Incremental dynamic analysis (IDA) is performed for a non-degrading SDOF model with eigenperiod $T=1$ sec. The employed hysteretic model is a bilinear elastoplastic model used for non-degrading SDOF systems and is shown in Figure 17(a) of the above reference. An IDA analysis is performed with a ground motion the spectral acceleration of which resembles the red line of Figure 14 of the above reference, i.e. the ground motion must have $S_a(1\text{ sec})=0.382g$ (which is the Intensity Measure - IM) and the duration D_{5_75} must be roughly equal to 8.3 sec. An acceleration time history with such characteristics is shown in Figure 16(c) of the above reference. In this example, an arbitrary ground motion acceleration is loaded, which is then adjusted so that the resulting time history has $S_a(1\text{ sec})=0.382g$ and $D_{5_75}=8.3$ sec. The adjusted time history is plotted in this example and can be compared to Figure 16(c) of the above reference. Based on the above problem statement, the median response curve of Figure 18(a) of the above reference is verified.

Earthquake motion

Load earthquake data

```
eqmotions={'LomaPrietaHallsValley90'};
data=load([eqmotions{1},'.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgtt=data(:,2);
```

Adjust earthquake motion to have $D_{5_75}=8.3\text{sec}$

Switch

```
sw='arias';
```

Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw);
```

Duration D_5_75 of the initially loaded motion

```
S1.Td_5_75
```

```
ans =
```

```
7.78
```

S.Td_5_75 must be roughly near 8.3 sec, as required in Mashayekhi et al. (2020) We manipulate the strong shaking part of the motion which corresponds to the significant duration so that S.Td_5_75 is increased to the desired value (8.3 sec)

```
id1=find(t==S1.t_5_75(1));  
id2=find(t==S1.t_5_75(2));  
xgtt(id1:id2)=0.8*xgtt(id1:id2);
```

Calculate duration D_5_75 of adjusted earthquake motion

Switch

```
sw='arias';
```

Apply OpenSeismoMatlab

```
S2=OpenSeismoMatlab(dt,xgtt,sw);
```

Duration D_5_75 of the adjusted motion

```
S2.Td_5_75
```

```
ans =
```

```
7.78
```

Scale earthquake motion to have Sa(1 sec)=0.382g

Switch

```
sw='elrs';
```

Critical damping ratio


```
ksi=0.05;
```

Period where $S_a=0.382g$

```
T=1;
```

Apply OpenSeismoMatlab

```
S3=OpenSeismoMatlab(dt,xgtt,sw,T,ksi);
```

Spectral acceleration of the adjusted motion at 1 sec

```
S3.Sa
```

```
ans =
```

```
1.42095612026039
```

S_a at 1 sec must be equal to $0.382g$, so we scale the entire acceleration time history up to this level

```
scaleF=0.382*9.81/S3.Sa;  
xgtt=xgtt*scaleF;
```

Calculate spectral acceleration of scaled earthquake motion

Switch

```
sw='elrs';
```

Critical damping ratio

```
ksi=0.05;
```

Period where $S_a=0.382g$

```
T=1;
```

Apply OpenSeismoMatlab

```
S4=OpenSeismoMatlab(dt,xgtt,sw,T,ksi);
```

Spectral acceleration of the adjusted motion at 1 sec

S4.Sa

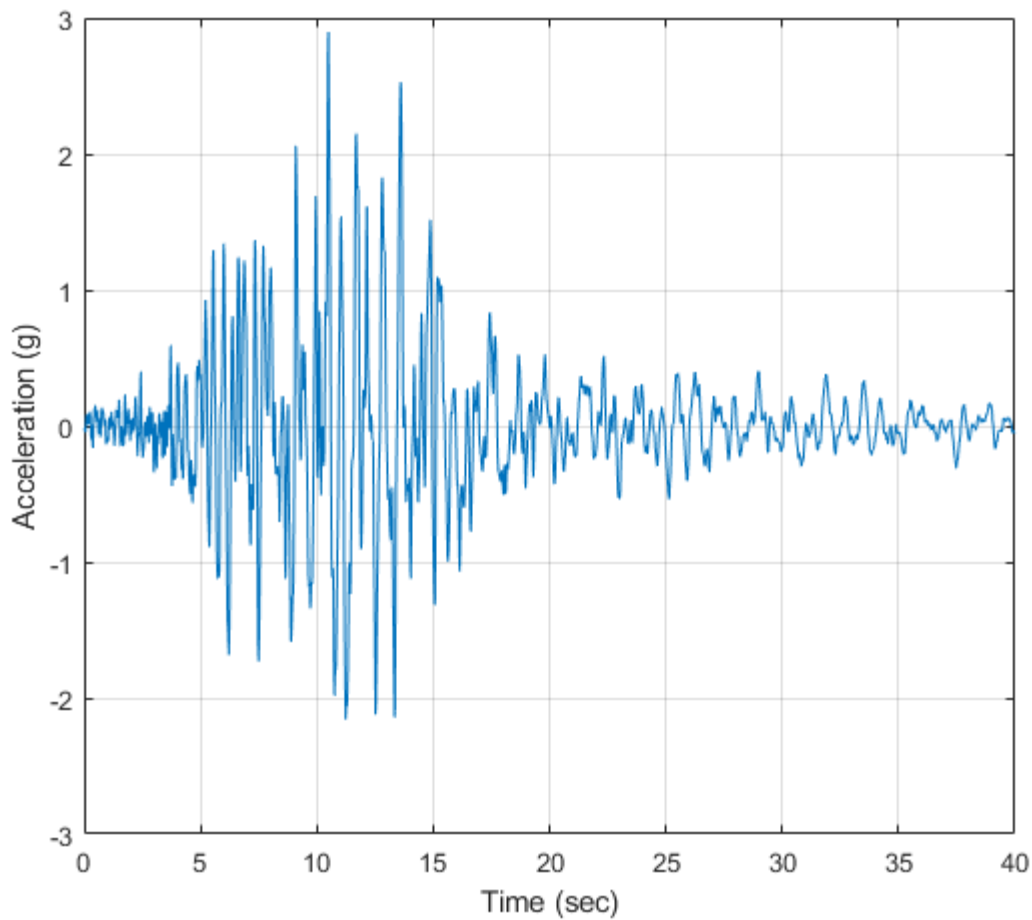
ans =

3.74742

Plot the acceleration time history

Initialize figure

```
figure()
% Plot the acceleration time history of the adjusted motion
plot(t,xgtt)
% Finalize figure
grid on
xlabel('Time (sec)')
ylabel('Acceleration (g)')
drawnow;
pause(0.1)
```



Perform IDA analysis

Switch

```
sw='ida';
```

Eigenperiod

```
T=1;
```

Scaling factors

```
lambdaF=logspace(log10(0.001),log10(10),100);
```

Type of IDA analysis

```
IM_DM='Sa_disp';
```

Mass

```
m=1;
```

Yield displacement

```
uy = 0.082*9.81/(2*pi/T)^2;
```

Post yield stiffness factor

```
pysf=0.01;
```

Fraction of critical viscous damping

```
ksi=0.05;
```

Apply OpenSeismoMatlab

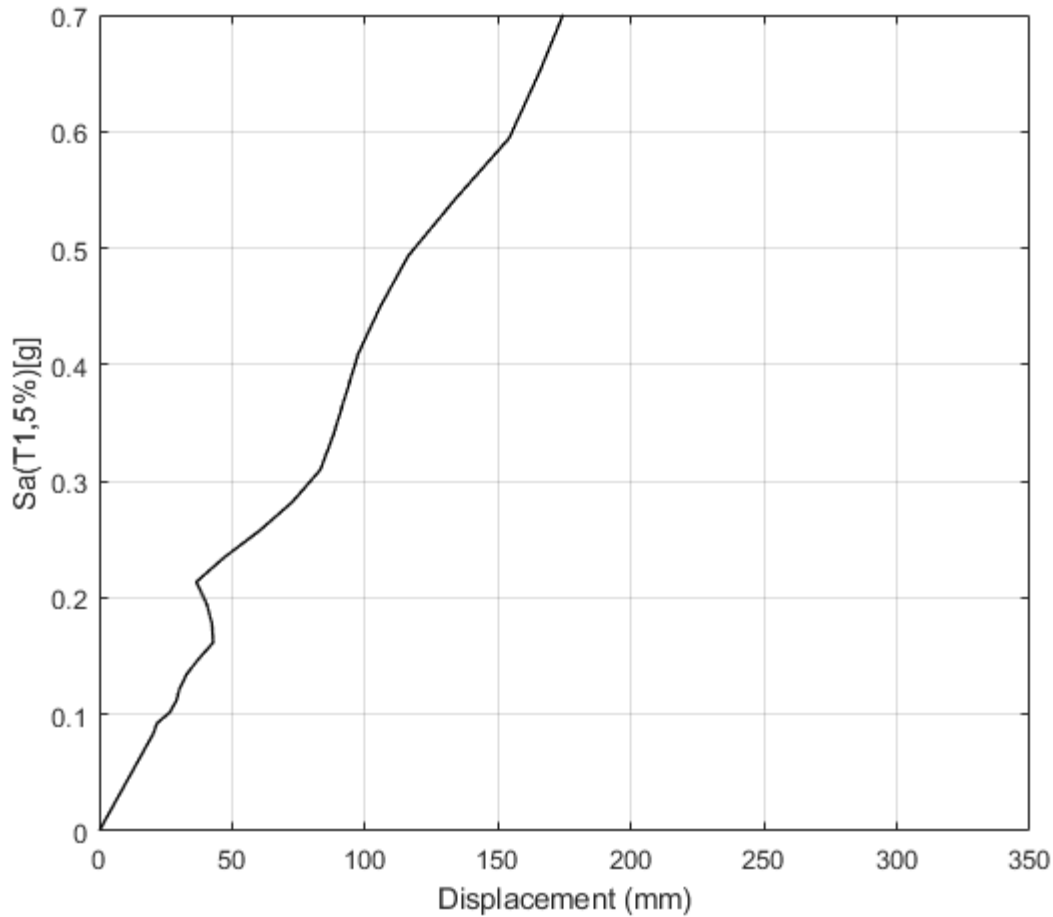
```
S5=OpenSeismoMatlab(dt,xgtt,sw,T,lambdaF,IM_DM,m,uy,pysf,ksi);
```

Plot the displacement time histories

Initialize figure

```
figure()  
% Plot the response curve of the incremental dynamic analysis  
plot(S5.DM*1000,S5.IM/9.81,'k','LineWidth',1)
```

```
% Finalize figure
grid on
xlabel('Displacement (mm)')
ylabel('Sa(T1,5%) [g]')
xlim([0,350])
ylim([0,0.7])
drawnow;
pause(0.1)
```



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verification Incremental dynamic analysis for multiple motions

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motions](#)
- [Setup parameters for IDA analysis](#)
- [Construct and plot the IDA curves in a loop](#)
- [Copyright](#)

Reference

Deng, P., Pei, S., van de Lindt, J. W., Liu, H., & Zhang, C. (2017). An approach to quantify the influence of ground motion uncertainty on elastoplastic system acceleration in incremental dynamic analysis. *Advances in Structural Engineering*, 20(11), 1744-1756.

Description

Figure 4(a) of the above reference contains the IDA curves of an elastoplastic SDOF system under the Consortium of Universities for Research in Earthquake Engineering (CUREE) GM suite (Krawinkler et al., 2001), which were constructed using the maximum acceleration. In this example, an arbitrary suite of strong ground motions is selected and the maximum acceleration IDA curves are constructed similar to Figure 4(a) of the above reference. The IDA curves of this example strongly resemble those of that figure.

Earthquake motions

Load data from a suite of earthquakes

```
GM={ 'Cape Mendocino.dat';  
      'ChiChi.dat';  
      'Christchurch2011HVPs_UP.dat';  
      'Imperial Valley.dat';  
      'Imperial_Valley_El_Centro_9_EW.dat';  
      'Kobe.dat';  
      'Kocaeli.dat';  
      'San_Fernando.dat';  
      'Spitak.dat'};  
n=size(GM,1);  
dt=cell(n,1);  
xgtd=cell(n,1);  
for i=1:n  
    fid=fopen(GM{i},'r');  
    text=textscan(fid,'%f %f');  
    fclose(fid);  
    t=text{1,1};  
    dt{i}=t(2)-t(1);  
    xgtd{i}=text{1,2};  
end
```

Setup parameters for IDA analysis

Switch

```
sw='ida';
```

Eigenperiod

```
T=1;
```

Scaling factors

```
lambdaF=logspace(log10(0.001),log10(10),100);
```

Type of IDA analysis

```
IM_DM='pgv_acc';
```

Mass

```
m=1;
```

Yield displacement

```
uy = 0.18*9.81/(2*pi/T)^2;
```

Post yield stiffness factor

```
pysf=0.01;
```

Fraction of critical viscous damping

```
ksi=0.05;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Set initial displacement

```
u0=0;
```

Set initial velocity

```
ut0=0;
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance for convergence

```
maxtol=0.01;
```

Maximum number of iterations per increment

```
jmax=200;
```

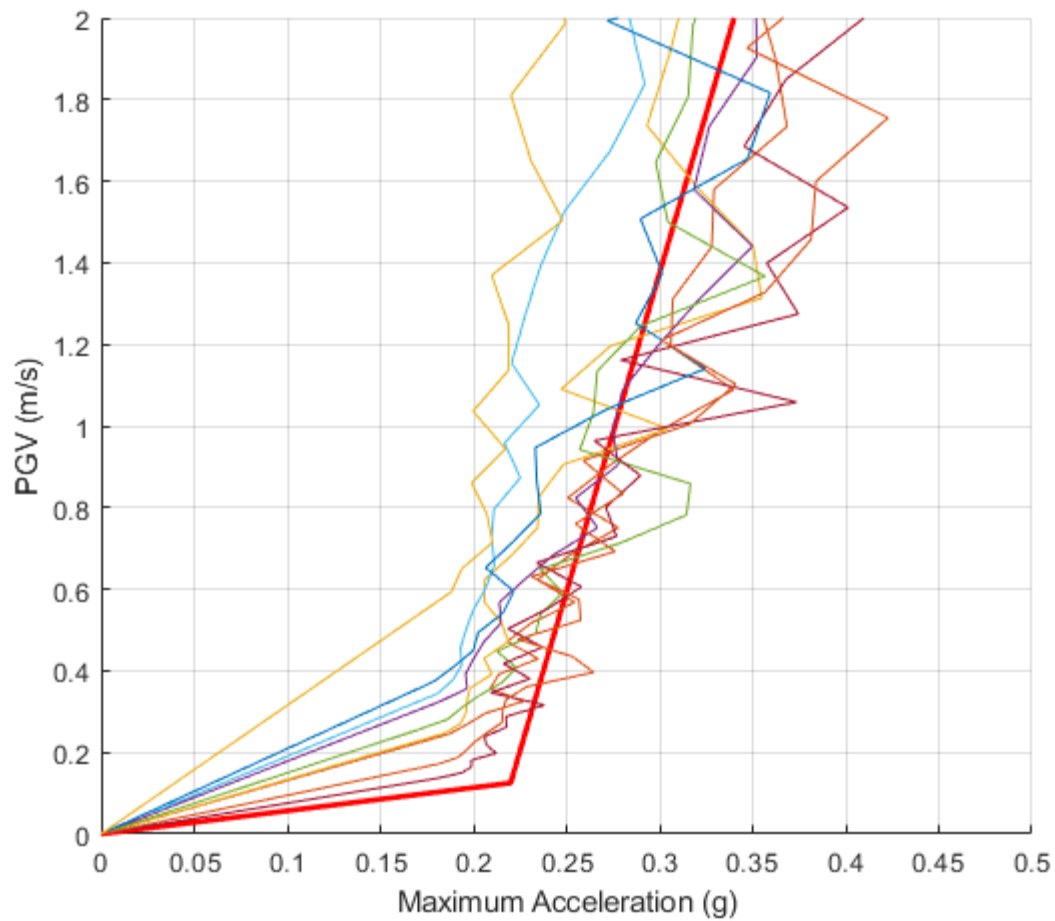
Infinitesimal variation of acceleration

```
dak=eps;
```

Construct and plot the IDA curves in a loop

Initialize figure

```
figure()
hold on
% Plot the red bold curve of Figure 4(a) of the above reference
plot([0,0.22,0.34],[0,0.125,2],'r','LineWidth',2)
for i=1:n
    % Apply OpenSeismoMatlab to calculate the ith IDA curve
    S1=OpenSeismoMatlab(dt{i},xgtt{i},sw,T,lambdaF,IM_DM,m,uy,pysf,ksi,AlgID,...
        u0,ut0,rinf,maxtol,jmax,dak);
    % Plot the ith IDA curve
    plot(S1.DM/9.81,S1.IM)
end
% Finalize figure
grid on
xlabel('Maximum Acceleration (g)')
ylabel('PGV (m/s)')
xlim([0,0.5])
ylim([0,2])
drawnow;
pause(0.1)
```



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verification Incremental dynamic analysis for ductility response

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motion](#)
- [Perform IDA analysis](#)
- [Plot the IDA curve](#)
- [Copyright](#)

Reference

Vamvatsikos, D., & Cornell, C. A. (2002). Incremental dynamic analysis. Earthquake engineering & structural dynamics, 31(3), 491-514.

Description

The ductility response IDA curve of an elastoplastic SDOF system excited by the Loma Prieta, 1989, Halls Valley earthquake (component 090) is constructed at multiple levels of shaking, and compared to the curve shown in Figure 4(a) of the above reference. The SDOF system has $T=1$ sec and critical damping ratio 5%

Earthquake motion

Load earthquake data

```
GM='LomaPrietaHallsValley90.dat';
fid=fopen(GM,'r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtd=text{1,2};
```

Perform IDA analysis

Switch

```
sw='ida';
```

Eigenperiod

```
T=1;
```

Scaling factors

```
lambdaF=logspace(log10(0.01),log10(30),100);
```

Type of IDA analysis

```
IM_DM='Sa_mu';
```

Mass

```
m=1;
```

Yield displacement

```
uy=0.25;
```

Post yield stiffness factor

```
pysf=0.01;
```

Fraction of critical viscous damping

```
ksi=0.05;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Set initial displacement

```
u0=0;
```

Set initial velocity

```
ut0=0;
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance for convergence

```
maxtol=0.01;
```

Maximum number of iterations per increment

```
jmax=200;
```

Infinitesimal variation of acceleration

```
dak=eps;
```

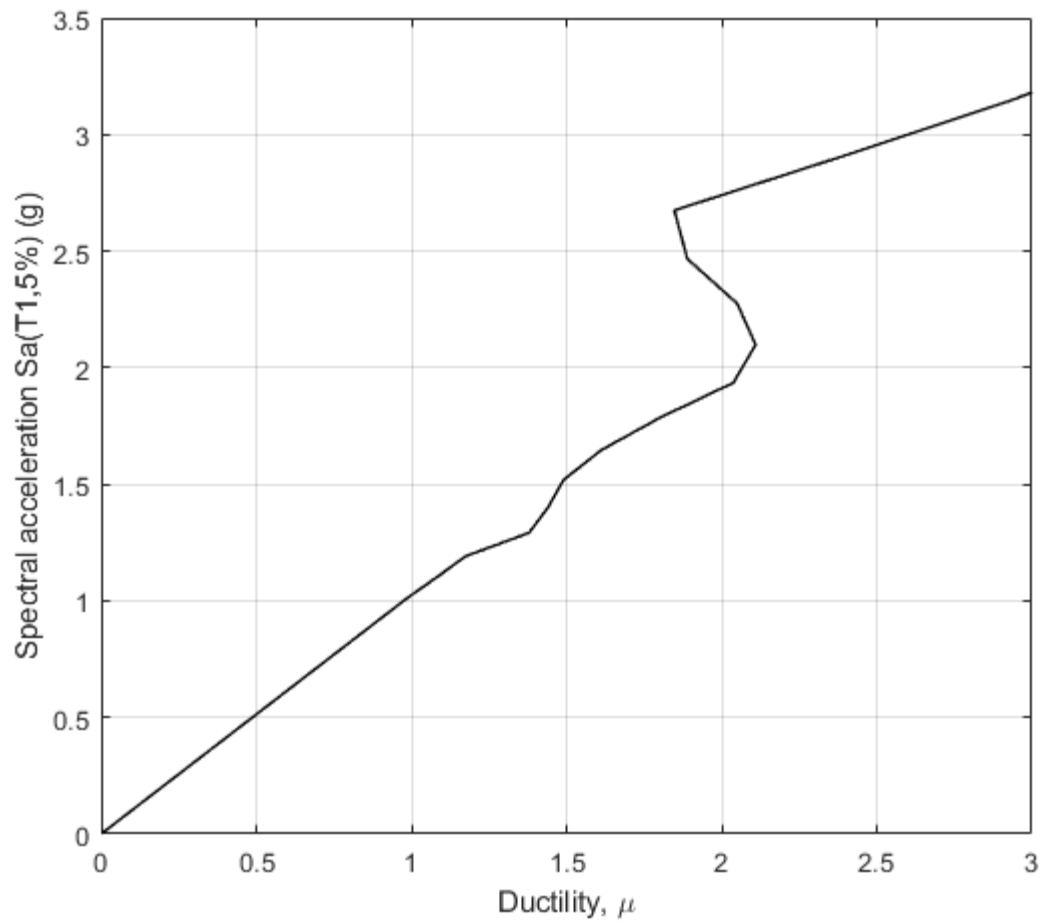
Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtd,sw,T,lambdAF,IM_DM,m,uy,pysf,ksi,AlgID,...  
    u0,ut0,rinf,maxtol,jmax,dak);
```

Plot the IDA curve

Initialize figure

```
figure()  
% Plot the IDA curve  
plot(S1.DM,S1.IM/9.81,'k','LineWidth',1)  
% Finalize figure  
grid on  
xlabel('Ductility, \mu')  
ylabel('Spectral acceleration Sa(T1,5%) (g)')  
xlim([0,3])  
ylim([0,3.5])  
drawnow;  
pause(0.1)
```



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verification Incremental dynamic analysis for ductility response

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motions](#)
- [Setup parameters for IDA analysis](#)
- [Construct and plot the IDA curves in a loop](#)
- [Copyright](#)

Reference

De Luca, F., Vamvatsikos, D., & Iervolino, I. (2011, May). Near-optimal bilinear fit of capacity curves for equivalent SDOF analysis. In Proceedings of the COMPDYN2011 Conference on Computational Methods in Structural Dynamics and Earthquake Engineering, Corfu, Greece.

Description

Figure 1(b) of the above reference presents the median IDA curves of SDOF systems with $T=0.5\text{sec}$. The actual capacity curve of the SDOF oscillator shown in Figure 1(a) of the same reference (green line), has been fitted with an elastoplastic bilinear fit according to FEMA-440 (blue line). This fitting introduces an error (bias) which appears as the blue area in Figure 1(b), which is generally conservative. In this example two arbitrary acceleration time histories are selected, then the corresponding displacement response IDA curves are plotted, based on a SDOF system with suitably selected properties, based on Figure 1(a). It is shown that both curves approximately fall into the bias (blue area) of Figure 1(b) of the above reference.

Earthquake motions

Load data from two earthquakes

```
GM={'Imperial Valley'; % Imperial valley 1979
   'Cape Mendocino'};
n=size(GM,1);
dt=cell(n,1);
xgtd=cell(n,1);
for i=1:n
    fid=fopen([GM{i},'.dat'],'r');
    text=textscan(fid,'%f %f');
    fclose(fid);
    t=text{1,1};
    dt{i}=t(2)-t(1);
    xgtd{i}=text{1,2};
end
```

Setup parameters for IDA analysis

Switch

```
sw='ida';
```

Eigenperiod

```
T=0.5;
```

Scaling factors

```
lambdaF=logspace(log10(0.01),log10(30),100);
```

Type of IDA analysis

```
IM_DM='Sa_disp';
```

Yield displacement

```
uy=0.042;
```

Initial stiffness

```
k_hi=1000/uy;
```

Mass

```
m=k_hi/(2*pi/T)^2;
```

Post yield stiffness factor

```
pysf=0.01;
```

Fraction of critical viscous damping

```
ksi=0.05;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Set initial displacement

```
u0=0;
```

Set initial velocity

```
ut0=0;
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance for convergence

```
maxtol=0.01;
```

Maximum number of iterations per increment

```
jmax=200;
```

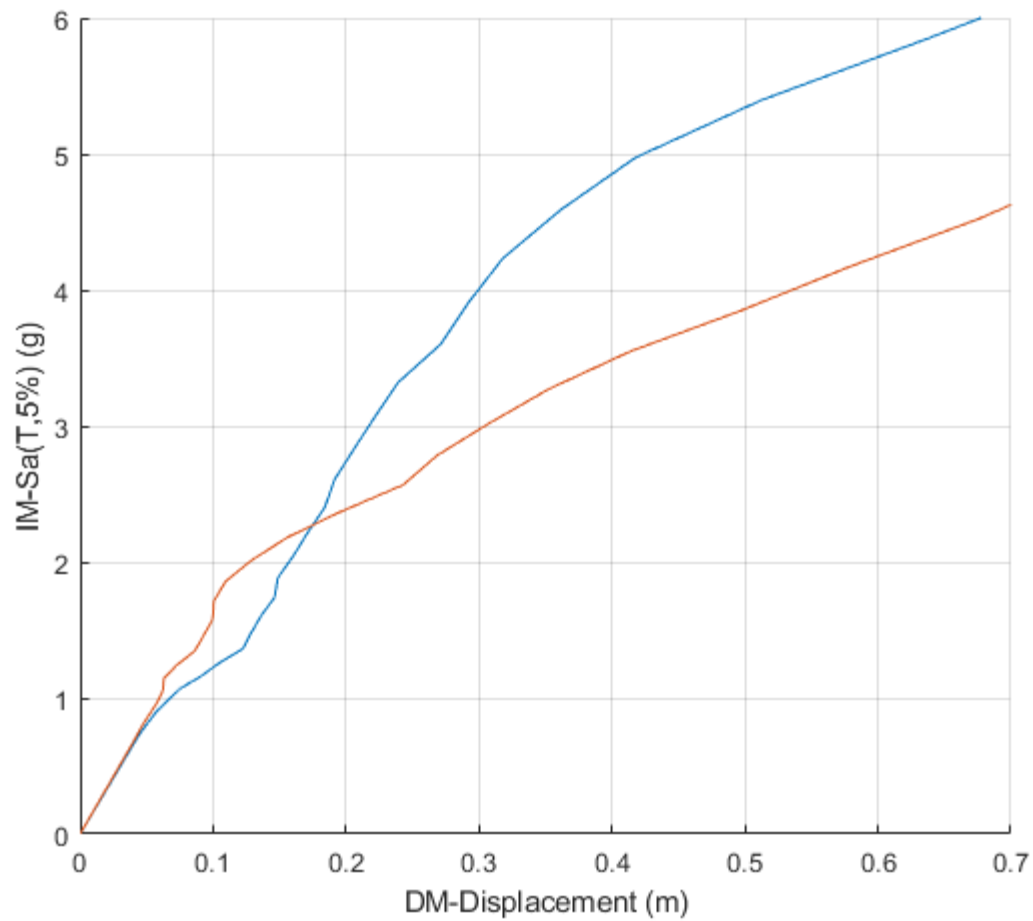
Infinitesimal variation of acceleration

```
dak=eps;
```

Construct and plot the IDA curves in a loop

Initialize figure

```
figure()
hold on
% Plot the IDA curves of Figure 1(b) of the above reference
for i=1:n
    S1=OpenSeismoMatlab(dt{i},xgtt{i},sw,T,lambdAF,IM_DM,m,uy,pysf,ksi,AlgID,...
        u0,ut0,rinf,maxtol,jmax,dak);
    plot(S1.DM,S1.IM/9.81)
end
% Finalize figure
grid on
xlabel('DM-Displacement (m)')
ylabel('IM-Sa(T,5%) (g)')
xlim([0,0.7])
ylim([0,6])
drawnow;
pause(0.1)
```



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verification Linear dynamic response of SDOF oscillator

Calculate the dynamic response of a linear SDOF oscillator. This example verifies Figure 6.6.1 in Chopra for $T_n=1\text{sec}$

Contents

- [Reference](#)
- [Earthquake motion](#)
- [Setup parameters for LIDA function](#)
- [Calculate dynamic response](#)
- [Results](#)
- [Copyright](#)

Reference

Chopra, A. K. (2020). Dynamics of structures, Theory and Applications to Earthquake Engineering, 5th edition. Prentice Hall.

Earthquake motion

Load earthquake data

```
dt=0.02;  
fid=fopen('elcentro_NS_trunc.dat','r');  
text=textscan(fid,'%f %f');  
fclose(fid);  
xgtd=text{1,2};
```

Setup parameters for LIDA function

Eigenperiod

```
Tn=1;
```

Critical damping ratio

```
ksi=0.02;
```

Initial displacement

```
u0=0;
```

Initial velocity

```
ut0=0;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Calculate dynamic response

Calculate circular eigenfrequency

```
omega=2*pi/Tn;
```

Apply LIDA

```
[u,ut,utt] = LIDA(dt,xgtt,omega,ksi,u0,ut0,AlgID,rinf);
```

Results

Maximum displacement in cm

```
D=max(abs(u))*100
```

D =

15.0632751930384

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verification of seismic input energy of linear SDOF oscillator

Compare the output of LIDA.m and NLIDABLKIN.m for a linear SDOF oscillator in terms of seismic input energy per unit mass.

Contents

- [Reference](#)
- [Description](#)
- [Load earthquake data](#)
- [Setup parameters for NLIDABLKIN function for linear SDOF](#)
- [Calculate dynamic response of linear SDOF using NLIDABLKIN.m](#)
- [Plot the energy time histories of the linear SDOF](#)
- [Calculate dynamic response of the linear SDOF using LIDA.m](#)
- [Plot the energy time history of the nonlinear SDOF](#)
- [Copyright](#)

Reference

None

Description

Calculate the time histories of the various energies that are absorbed by a linear elastic SDOF oscillator using the linear function LIDA.m and the nonlinear function NLIDABLKIN.m to which an infinite yield limit has been assigned. The time history of the seismic input energy per unit mass obtained by the LIDA.m function (Figure b) is compared to the sum of the strain, damping and kinetic energies per unit mass obtained by the NLIDABLKIN.m function (Figure a). The linear SDOF system has $T_n=0.5$ sec and $\zeta=5\%$.

Load earthquake data

Earthquake acceleration time history of the El Centro earthquake will be used (El Centro, 1940, El Centro Terminal Substation Building)

```
fid=fopen('elcentro_NS_trunc.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtd=text{1,2};
```

Setup parameters for NLIDABLKIN function for linear SDOF

Mass

```
m=1;
```

Eigenperiod

```
Tn=0.5;
```

Calculate the small-strain stiffness matrix

```
omega=2*pi/Tn;  
k_hi=m*omega^2;
```

Assign linear elastic properties

```
k_lo=k_hi;  
uy1=1e10;
```

Critical damping ratio

```
ksi=0.05;
```

Initial displacement

```
u0=0;
```

Initial velocity

```
ut0=0;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance of convergence for time integration algorithm

```
maxtol=0.01;
```

Maximum number of iterations per integration time step

```
jmax=200;
```

Infinitesimal acceleration

```
dak=eps;
```

Calculate dynamic response of linear SDOF using NLIDABLKIN.m

Apply NLIDABLKIN

```
[u,ut,utt,Fs,Ey,Es,Ed,jiter] = NLIDABLKIN(dt,xgtt,m,k_hi,k_lo,uy1,...  
ksi,AlgID,u0,ut0,rinf,maxtol,jmax,dak);
```

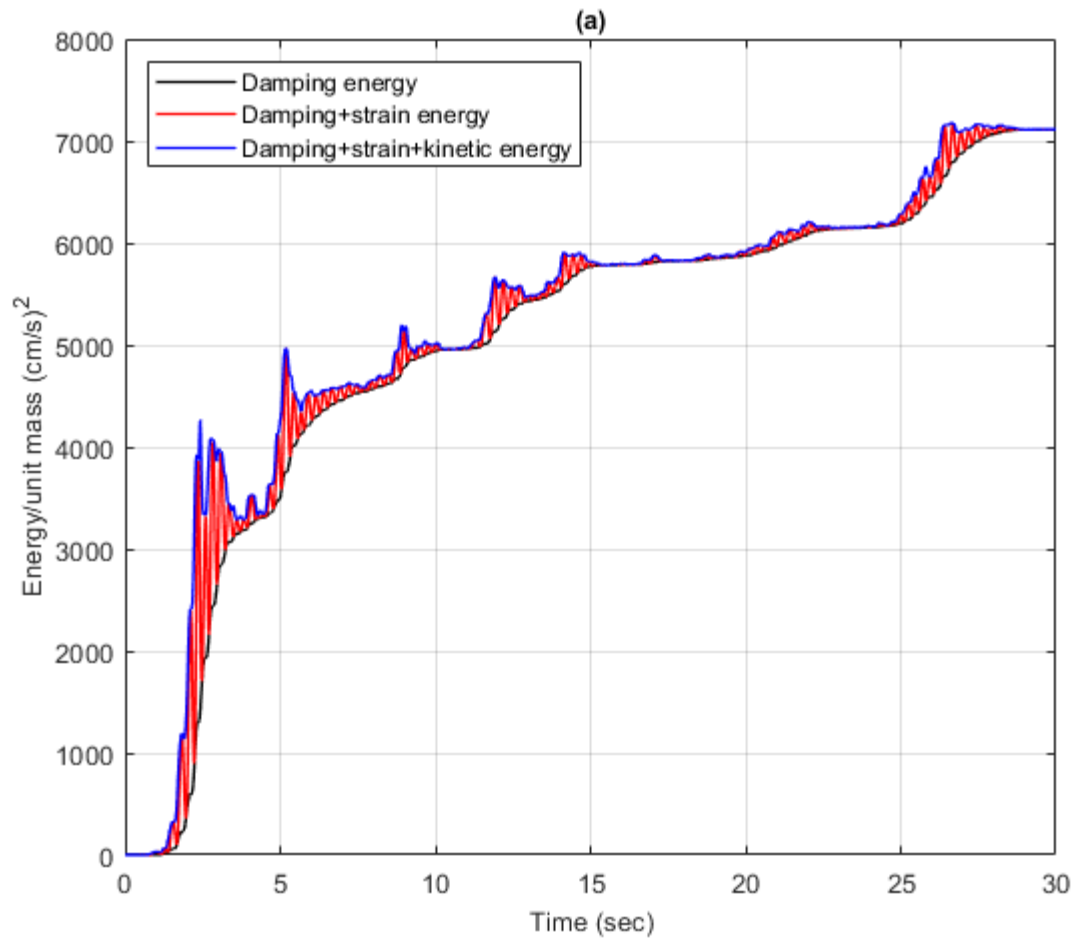
Calculate the kinetic energy of SDOF

```
Ek=1/2*m*ut.^2;
```

Plot the energy time histories of the linear SDOF

Plot the damping energy, damping plus strain energy, damping plus strain plus kinetic energy of the linearly elastic SDOF system. Convert from m to cm

```
figure()  
plot(t',cumsum(Ed)*1e4,'k','LineWidth',1)  
hold on  
plot(t',cumsum(Ed)*1e4+Es*1e4,'r','LineWidth',1)  
plot(t',cumsum(Ed)*1e4+Es*1e4+Ek*1e4,'b','LineWidth',1)  
hold off  
xlim([0,30])  
ylim([0,8000])  
xlabel('Time (sec)','FontSize',10);  
ylabel('Energy/unit mass (cm/s)^2','FontSize',10);  
title('(a)','FontSize',10)  
grid on  
legend({'Damping energy','Damping+strain energy',...  
        'Damping+strain+kinetic energy'},'location','northwest')  
drawnow;  
pause(0.1)
```



Calculate dynamic response of the linear SDOF using LIDA.m

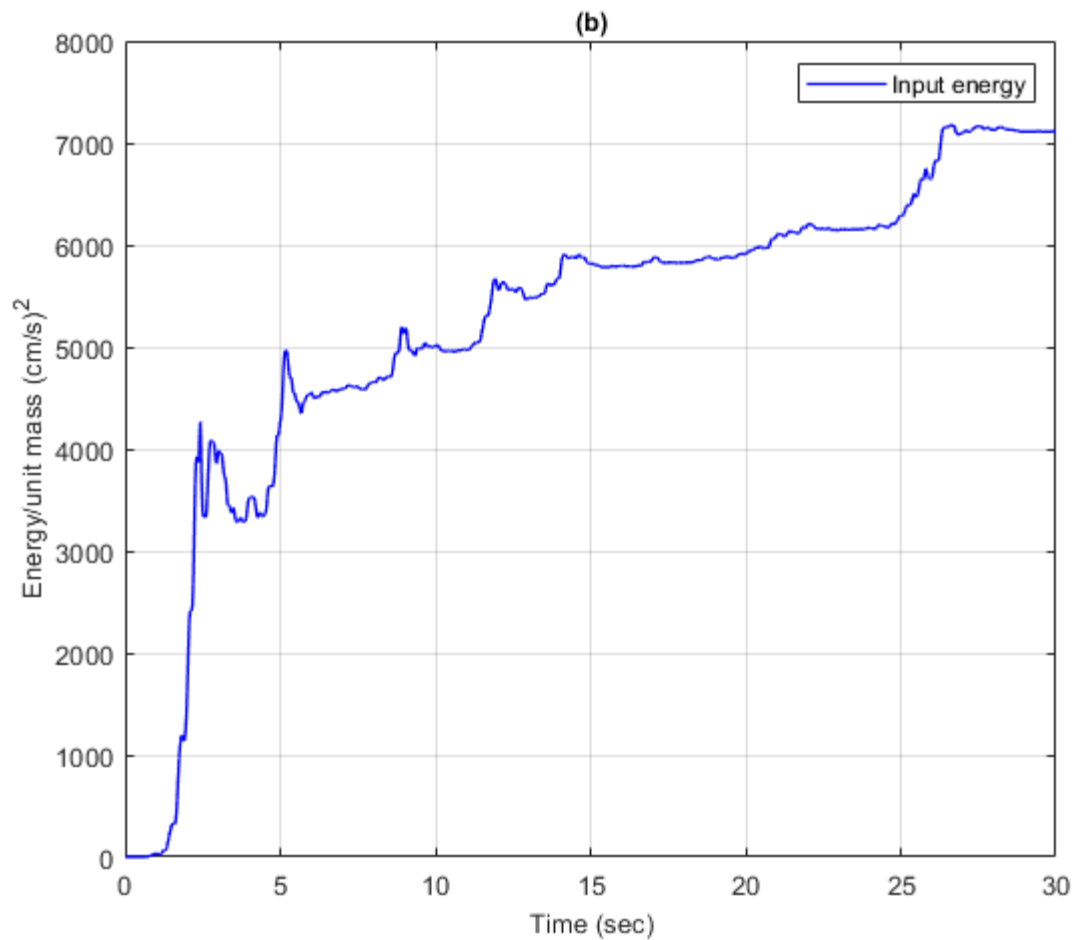
Apply the LIDA.m function for the linear SDOF

```
[u,ut,utt,Ei] = LIDA(dt,xgdt,omega,ksi,u0,ut0,AlgID,rinf);
```

Plot the energy time history of the nonlinear SDOF

Plot the damping energy, the hysteretic energy and strain energy of the nonlinear SDOF system. Convert from m to cm.

```
figure();
plot(t,cumsum(Ei)*1e4,'b','LineWidth',1)
xlim([0,30])
ylim([0,8000])
xlabel('Time (sec)','FontSize',10);
ylabel('Energy/unit mass (cm/s)^2','FontSize',10);
title('(b)','FontSize',10)
grid on
legend('Input energy')
drawnow;
pause(0.1)
```



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verification Energy time history of SDOF oscillator

Calculate the time history of the strain energy and the energy dissipated by viscous damping and yielding of a linear and a nonlinear SDOF oscillator

Contents

- [Reference](#)
- [Description](#)
- [Load earthquake data](#)
- [Setup parameters for NLIDABLKIN function for linear SDOF](#)
- [Calculate dynamic response of the linear SDOF](#)
- [Plot the energy time history of the linear SDOF](#)
- [Setup parameters for NLIDABLKIN function for nonlinear SDOF](#)
- [Calculate dynamic response of the nonlinear SDOF](#)
- [Plot the energy time history of the nonlinear SDOF](#)
- [Copyright](#)

Reference

Chopra, A. K. (2020). Dynamics of structures, Theory and Applications to Earthquake Engineering, 5th edition. Prentice Hall.

Description

Figure 7.9.1 of the above reference is reproduced in this example, for both the linear elastic and the elastoplastic SDOF systems. The linear system has $T_n=0.5$ sec and $\zeta=5\%$, whereas the elastoplastic system has $T_n=0.5$ sec, $\zeta=5\%$ and $\bar{f}_y=0.25$.

Load earthquake data

Earthquake acceleration time history of the El Centro earthquake will be used (El Centro, 1940, El Centro Terminal Substation Building)

```
fid=fopen('elcentro_NS_trunc.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtd=text{1,2};
```

Setup parameters for NLIDABLKIN function for linear SDOF

Mass

```
m=1;
```

Eigenperiod

```
Tn=0.5;
```

Calculate the small-strain stiffness matrix


```
omega=2*pi/Tn;  
k_hi=m*omega^2;
```

Assign linear elastic properties

```
k_lo=k_hi;  
uy1=1e10;
```

Critical damping ratio

```
ksi=0.05;
```

Initial displacement

```
u0=0;
```

Initial velocity

```
ut0=0;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance of convergence for time integration algorithm

```
maxtol=0.01;
```

Maximum number of iterations per integration time step

```
jmax=200;
```

Infinitesimal acceleration

```
dak=eps;
```

Calculate dynamic response of the linear SDOF

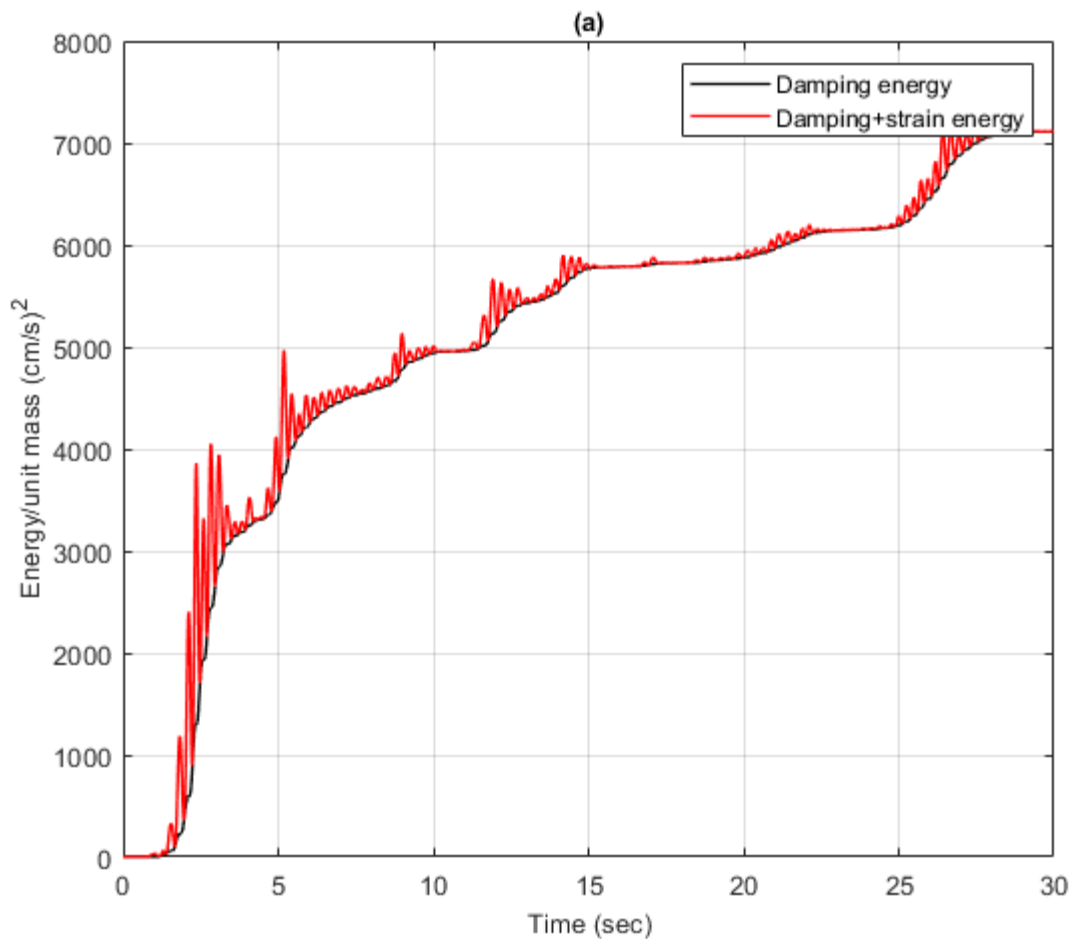
Apply NLIDABLKIN

```
[u,ut,utt,Fs,Ey,Es,Ed,jiter] = NLIDABLKIN(dt,xgtt,m,k_hi,k_lo,uyl,...
    ksi,AlgID,u0,ut0,rinf,mxtol,jmax,dak);
```

Plot the energy time history of the linear SDOF

Plot the damping energy and strain energy of the linearly elastic SDOF system. Convert from m to cm

```
figure()
plot(t',cumsum(Ed)*1e4,'k','LineWidth',1)
hold on
plot(t',cumsum(Ed)*1e4+Es*1e4,'r','LineWidth',1)
hold off
xlim([0,30])
ylim([0,8000])
xlabel('Time (sec)','FontSize',10);
ylabel('Energy/unit mass (cm/s)^2','FontSize',10);
title('(a)','FontSize',10)
grid on
legend('Damping energy','Damping+strain energy')
drawnow;
pause(0.1)
```



Setup parameters for NLIDABLKIN function for nonlinear SDOF

The properties of the nonlinear SDOF system are identical to those of the linear SDOF system, except for the yield displacement and the post-yield stiffness.

Post yield stiffness

```
k_lo=0.01*k_hi;
```

normalized yield strength

```
fybar=0.25;
```

Yield displacement for nonlinear response

```
uy2=fybar*max(abs(u));
```

Calculate dynamic response of the nonlinear SDOF

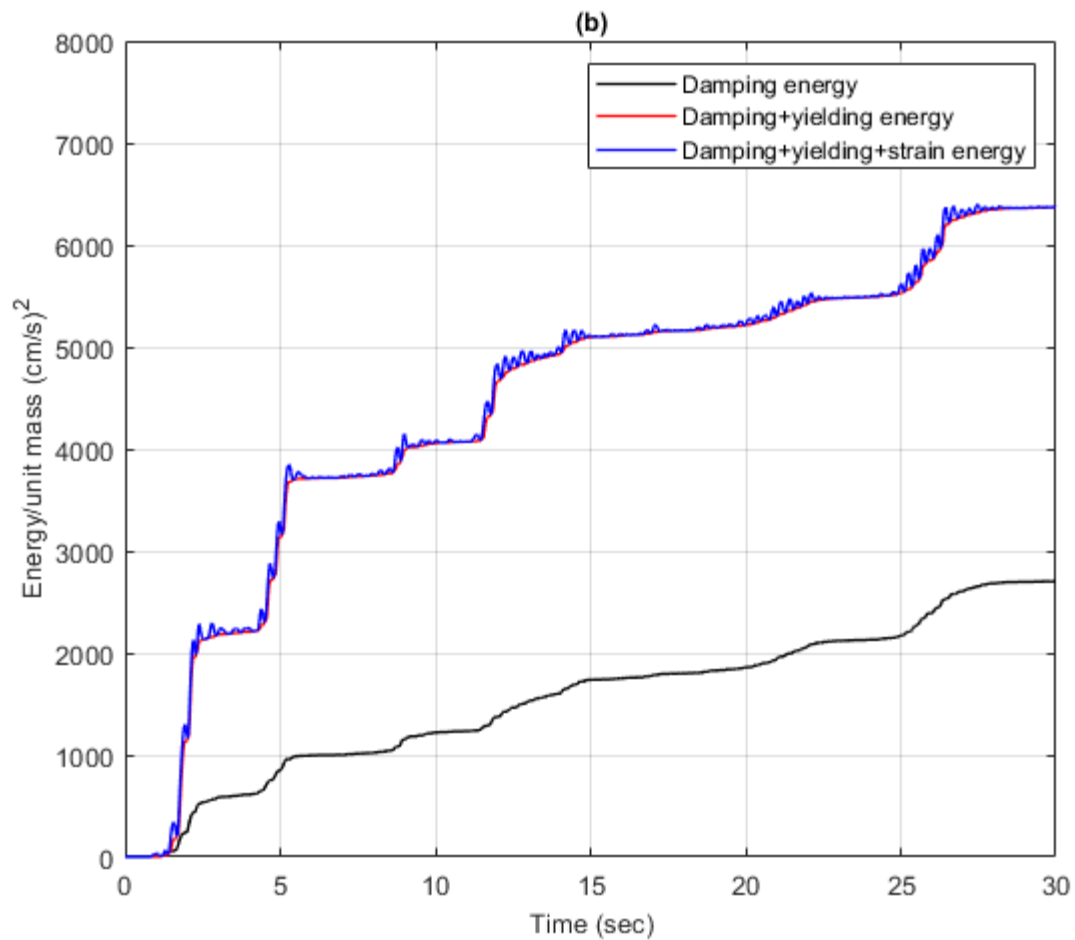
Apply NLIDABLKIN

```
[u,ut,utt,Fs,Ey,Es,Ed,jiter] = NLIDABLKIN(dt,xgdt,m,k_hi,k_lo,uy2,...  
ksi,AlgID,u0,ut0,rinf,maxtol,jmax,dak);
```

Plot the energy time history of the nonlinear SDOF

Plot the damping energy, the hysteretic energy and strain energy of the nonlinear SDOF system. Convert from m to cm.

```
figure();  
plot(t',cumsum(Ed)*1e4,'k','LineWidth',1)  
hold on  
plot(t',cumsum(Ed)*1e4+cumsum(Ey)*1e4-Es*1e4,'r','LineWidth',1)  
plot(t',cumsum(Ed)*1e4+cumsum(Ey)*1e4,'b','LineWidth',1)  
hold off  
xlim([0,30])  
ylim([0,8000])  
xlabel('Time (sec)','FontSize',10);  
ylabel('Energy/unit mass (cm/s)^2','FontSize',10);  
title('(b)','FontSize',10)  
grid on  
legend('Damping energy','Damping+yielding energy',...  
      'Damping+yielding+strain energy')  
drawnow;  
pause(0.1)
```



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verification Energy time histories of nonlinear SDOF oscillator

Calculate the time histories of the energy dissipated by damping, the energy dissipated by yielding, as well as the energy that is input to two SDOF oscillators with two different eigenperiods.

Contents

- [Reference](#)
- [Description](#)
- [Load earthquake data](#)
- [Setup parameters for NLIDABLKIN function for nonlinear SDOF with T=0.2s](#)
- [Calculate dynamic response of the nonlinear SDOF with T=0.2s](#)
- [Plot the energy time histories of the nonlinear SDOF with T=0.2s](#)
- [Setup parameters for NLIDABLKIN function for nonlinear SDOF with T=0.5s](#)
- [Calculate dynamic response of the nonlinear SDOF with T=0.5s](#)
- [Plot the energy time histories of the nonlinear SDOF with T=0.5s](#)
- [Copyright](#)

Reference

Uang, C. M., & Bertero, V. V. (1990). Evaluation of seismic energy in structures. Earthquake engineering & structural dynamics, 19(1), 77-90.

Description

Figure 3(b) of the above reference is reproduced in this example, for both linear elastic-perfectly plastic SDOF systems (short period and long period). The two eigenperiods considered are T=0.2 sec and T=5.0 sec. The damping ratio is 5% of the critical value and the ductility ratio achieved is equal to 5 for both SDOF systems. Figure 3(b) is verified in terms of damping energy (noted as E_ksi in the Figure), yielding energy (noted as E_h in the Figure) and input energy (noted as Ei in the Figure).

Load earthquake data

Earthquake acceleration time history of the 1986 San Salvador earthquake will be used (San Salvador, 10/10/1986, Geotech Investigation Center, component 90)

```
fid=fopen('SanSalvador1986GIC090.txt','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtt=text{1,2};
```

Setup parameters for NLIDABLKIN function for nonlinear SDOF with T=0.2s

Mass

```
m=1;
```

Eigenperiod

```
T=0.2;
```

Calculate the small-strain stiffness matrix

```
omega=2*pi/T;  
k_hi=m*omega^2;
```

Assign post-yield stiffness

```
k_lo=0.0001*k_hi;
```

Assign yield limit

```
uy=0.004875;
```

Critical damping ratio

```
ksi=0.05;
```

Initial displacement

```
u0=0;
```

Initial velocity

```
ut0=0;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance of convergence for time integration algorithm

```
maxtol=0.01;
```

Maximum number of iterations per integration time step

```
jmax=200;
```

Infinitesimal acceleration

```
dak=eps;
```

Calculate dynamic response of the nonlinear SDOF with T=0.2s

Apply NLIDABLKIN

```
[u,ut,utt,Fs,Ey,Es,Ed,jiter] = NLIDABLKIN(dt,xgtd,m,k_hi,k_lo,uy,...  
    ksi,AlgID,u0,ut0,rinf,maxtol,jmax,dak);
```

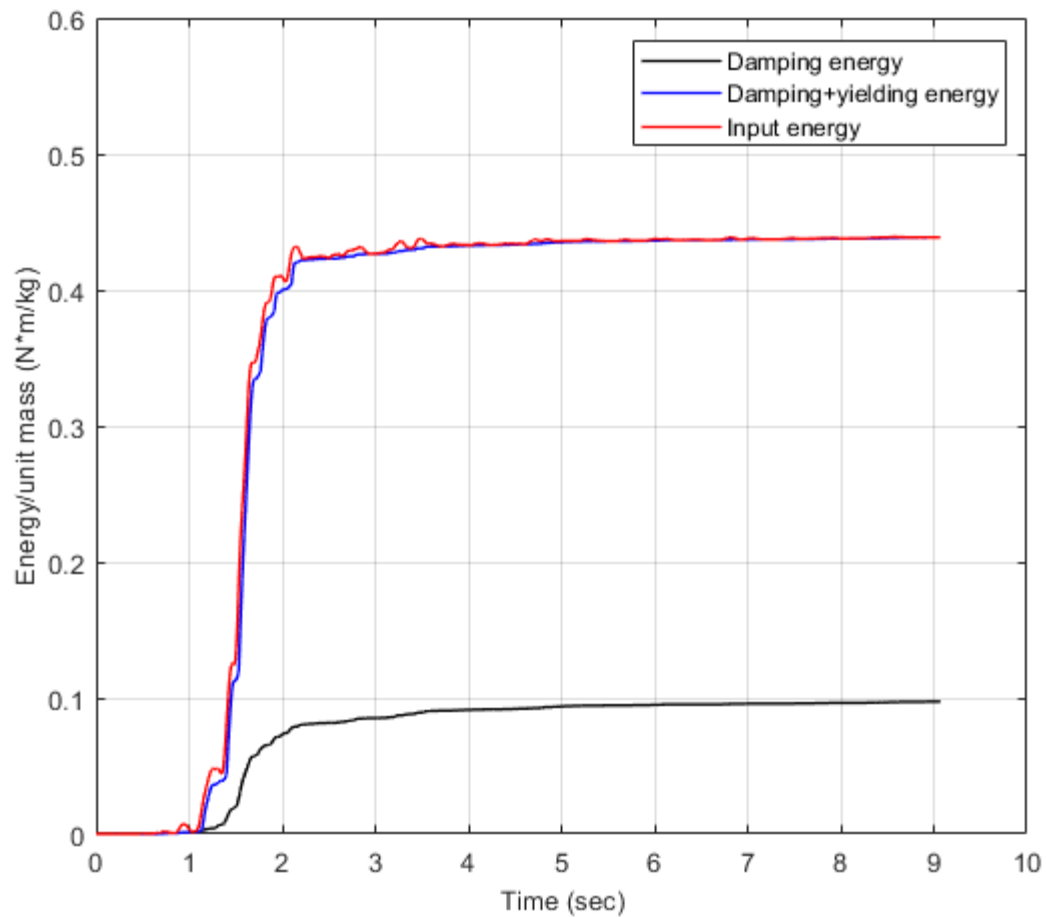
Calculate the kinetic energy of SDOF

```
Ek=1/2*m*ut.^2;
```

Plot the energy time histories of the nonlinear SDOF with T=0.2s

Plot the damping energy, yielding energy and input energy

```
figure()  
plot(t',cumsum(Ed),'k','LineWidth',1)  
hold on  
plot(t',cumsum(Ed)+cumsum(Ey)-Es,'b','LineWidth',1)  
plot(t',cumsum(Ed)+cumsum(Ey)+Ek,'r','LineWidth',1)  
hold off  
xlim([0,10])  
ylim([0,0.6])  
xlabel('Time (sec)','FontSize',10);  
ylabel('Energy/unit mass (N*m/kg)','FontSize',10);  
%title('(a)','FontSize',10)  
grid on  
legend('Damping energy','Damping+yielding energy','Input energy')  
drawnow;  
pause(0.1)
```



Show the achieved ductility factor (must be equal to 5 according to the above reference)

```
max(abs(u))/uy
```

```
ans =
```

```
5.00074829936011
```

Setup parameters for NLIDABLKIN function for nonlinear SDOF with T=0.5s

Mass

```
m=1;
```

Eigenperiod

```
T=5;
```

Calculate the small-strain stiffness matrix


```
omega=2*pi/T;  
k_hi=m*omega^2;
```

Assign post-yield stiffness

```
k_lo=0.0001*k_hi;
```

Assign yield limit

```
uy=0.023;
```

Critical damping ratio

```
ksi=0.05;
```

Initial displacement

```
u0=0;
```

Initial velocity

```
ut0=0;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance of convergence for time integration algorithm

```
maxtol=0.01;
```

Maximum number of iterations per integration time step

```
jmax=200;
```

Infinitesimal acceleration

```
dak=eps;
```

Calculate dynamic response of the nonlinear SDOF with T=0.5s

Apply NLIDABLKIN

```
[u,ut,utt,Fs,Ey,Es,Ed,jiter] = NLIDABLKIN(dt,xgtt,m,k_hi,k_lo,uy,...  
    ksi,AlgID,u0,ut0,rinf,maxtol,jmax,dak);
```

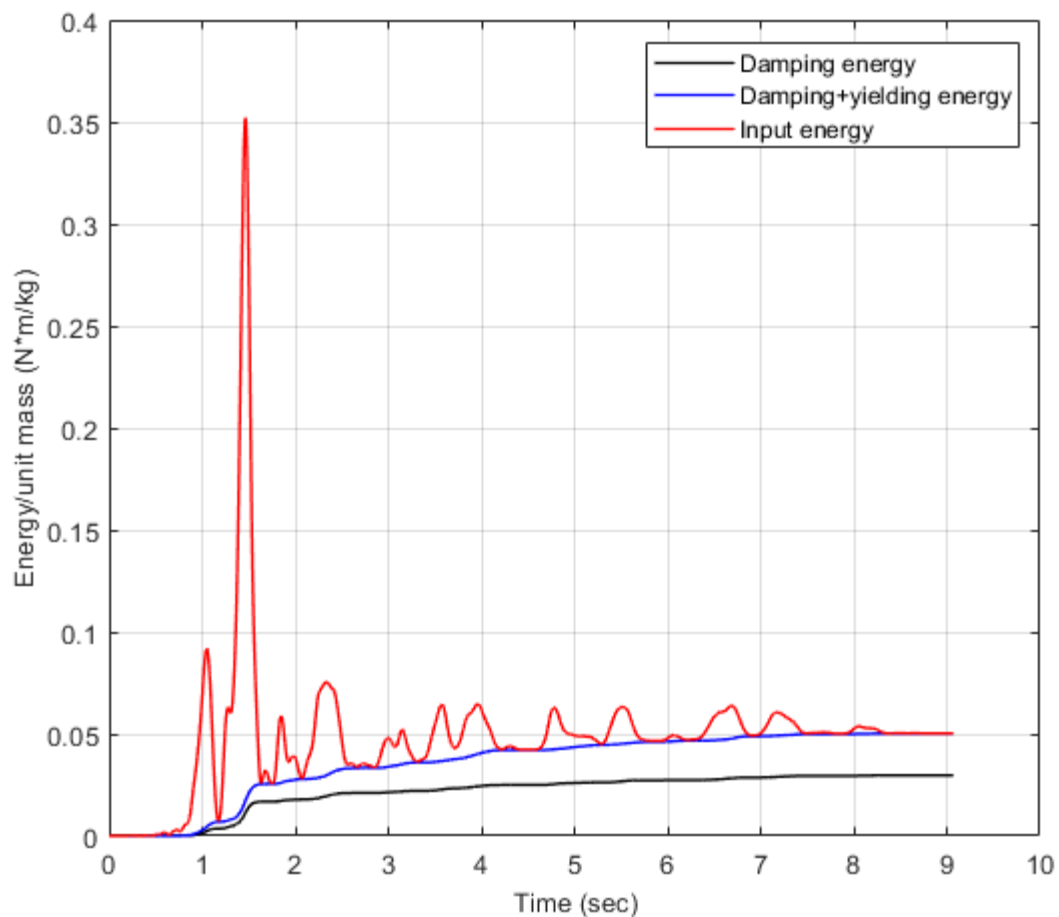
Calculate the kinetic energy of SDOF

```
Ek=1/2*m*ut.^2;
```

Plot the energy time histories of the nonlinear SDOF with T=0.5s

Plot the damping energy, yielding energy and input energy

```
figure()  
plot(t',cumsum(Ed),'k','LineWidth',1)  
hold on  
plot(t',cumsum(Ed)+cumsum(Ey)-Es,'b','LineWidth',1)  
plot(t',cumsum(Ed)+cumsum(Ey)+Ek,'r','LineWidth',1)  
hold off  
xlim([0,10])  
%ylim([0,0.6])  
xlabel('Time (sec)','FontSize',10);  
ylabel('Energy/unit mass (N*m/kg)','FontSize',10);  
%title('(a)','FontSize',10)  
grid on  
legend('Damping energy','Damping+yielding energy','Input energy')  
drawnow;  
pause(0.1)
```



Show the achieved ductility factor (must be equal to 5 according to the above reference)

```
max(abs(u))/uy
```

ans =

4.99190405960856

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verification Strength ductility relation of elastoplastic system

Contents

- [Reference](#)
- [Description](#)
- [Load earthquake data](#)
- [Setup parameters for NLIDABLKIN function for linear SDOF](#)
- [Calculate dynamic response of the linear SDOF](#)
- [Plot the energy time history of the linear SDOF](#)
- [Copyright](#)

Reference

Mahin, S. A., & Lin, J. (1983). Construction of inelastic response spectra for single-degree-of-freedom systems. Earthquake Engineering Center, University of California, Berkeley.

Description

Figure 15 of the above reference is reproduced in this example, for an elastic perfectly plastic (EPP) system with eigenperiod equal to 0.7 sec and damping ratio equal to 0.05. The NS component of the El Centro earthquake (1940) is considered. It is demonstrated that there can be more than one values of strength corresponding to a given displacement ductility.

Load earthquake data

Earthquake acceleration time history of the El Centro earthquake will be used (El Centro, 1940, NS component)

```
fid=fopen('elcentro_NS_full.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtd=9.81*text{1,2};
```

Setup parameters for NLIDABLKIN function for linear SDOF

Mass

```
m=1;
```

Eigenperiod

```
Tn=0.7;
```

Calculate the small-strain stiffness matrix

```
omega=2*pi/Tn;
k_hi=m*omega^2;
```

Assign linear elastic properties

```
k_lo=0.001*k_hi;
```

Assign yield displacement

```
eta=[0.3,0.5,0.8,0.9,1.0,1.3,1.5];  
uy=eta*max(abs(xgtt))/k_hi;
```

Critical damping ratio

```
ksi=0.05;
```

Initial displacement

```
u0=0;
```

Initial velocity

```
ut0=0;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance of convergence for time integration algorithm

```
maxtol=0.01;
```

Maximum number of iterations per integration time step

```
jmax=200;
```

Infinitesimal acceleration

```
dak=eps;
```

Calculate dynamic response of the linear SDOF

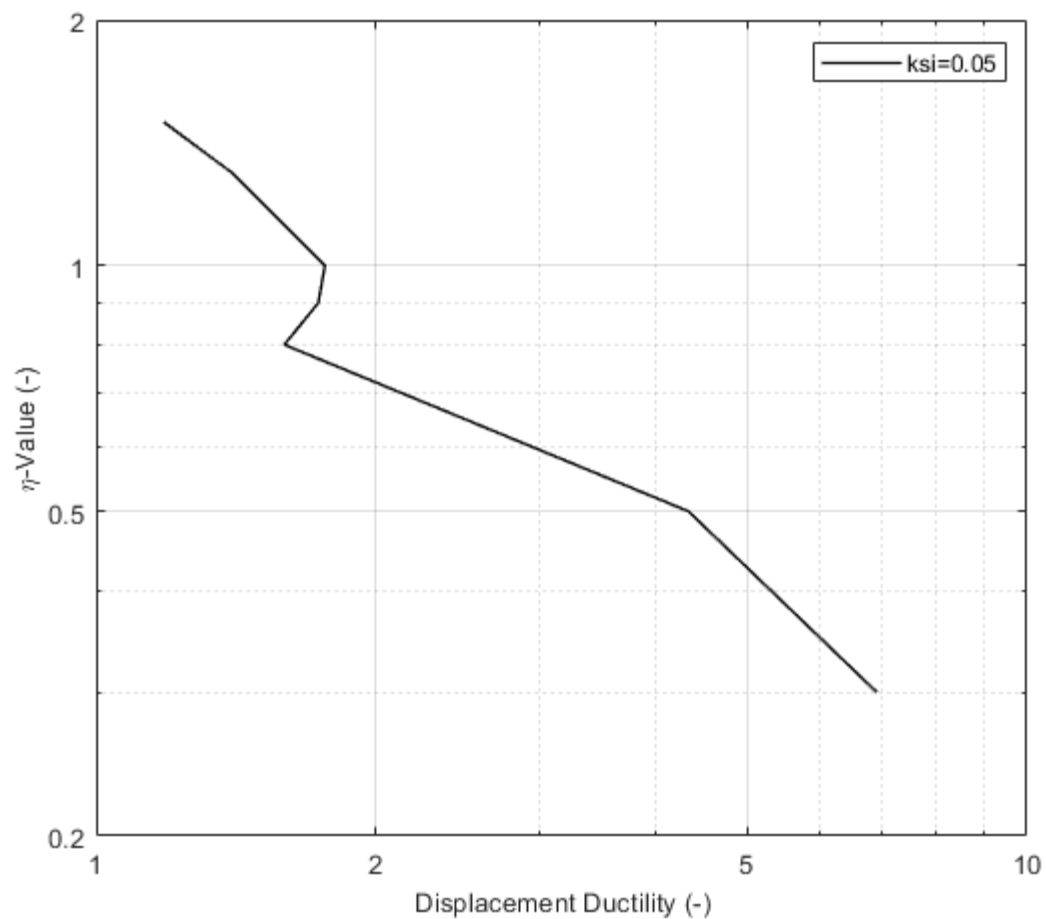
Apply NLIDABLKIN

```
mu=zeros(1,numel(uy));
for i=1:numel(uy)
[u,ut,utt,Es,Ey,Es,Ed,jiter] = NLIDABLKIN(dt,xgtd,m,k_hi,k_lo,uy(i),...
    ksi,AlgID,u0,ut0,rinf,maxtol,jmax,dak);
    mu(i)=max(abs(u))/uy(i);
end
```

Plot the energy time history of the linear SDOF

Plot the damping energy and strain energy of the linearly elastic SDOF system. Convert from m to cm

```
figure()
loglog(mu,eta,'k','LineWidth',1)
xlim([1,10])
ylim([0.2,2])
set(gca,'XTick',[1,2,5,10])
set(gca,'YTick',[0.2,0.5,1,2])
xlabel('Displacement Ductility (-)','FontSize',10);
ylabel('\eta-Value (-)','FontSize',10);
grid on
legend({'ksi=0.05'})
drawnow;
pause(0.1)
```



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verification Pulse Decomposition of OpenSeismoMatlab

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motion](#)
- [Perform pulse decomposition of earthquake motion](#)
- [Plot the velocity time histories \(initial motion and largest pulse\)](#)
- [Plot the velocity time histories \(residual motion and 2nd largest pulse\)](#)
- [Sum the 10 largest pulses extracted from the input motion](#)
- [Plot the velocity pulse using 10 largest pulses](#)
- [Plot the final residual ground motion](#)
- [Copyright](#)

Reference

Baker, J. W. (2007). Quantitative classification of near-fault ground motions using wavelet analysis. Bulletin of the seismological society of America, 97(5), 1486-1501.

Description

The velocity pulse of a strong motion velocity time history is extracted according to Figure 4 of the above reference. The velocity time history of the fault-normal component of the 1994 Northridge, Rinaldi, recording is considered. The Daubechies wavelet of order 4, shown in Figure 2c, is used as the mother wavelet. Initially, the largest velocity pulse is identified (Figure 4b). For the ground motion under consideration, the ten largest velocity pulses are extracted, the combination of which is shown in Figure 4c, and the residual ground motion after the pulses have been removed is shown (Figure 4d).

Earthquake motion

Load earthquake data of fault-normal component of the 1994 Northridge, Rinaldi, recording

```
eqmotion={'RSN1063_NORTHR_RRS228.txt'};
data=load(eqmotion{1});
t=data(:,1);
dt=t(2)-t(1);
xgt=data(:,2);
```

Perform modification so that the initial velocity time history agrees with the plot of Figure 4a of the above reference.

```
xgt=-xgt;
```

Perform pulse decomposition of earthquake motion

Switch

```
sw='pulsedecomp';
```

Wavelet family of Daubechies wavelet of order 4

```
wname = 'db4';
```

Apply OpenSeismoMatlab for 1st largest pulse decomposition

```
S1=OpenSeismoMatlab(dt,xgt,sw,wname);
```

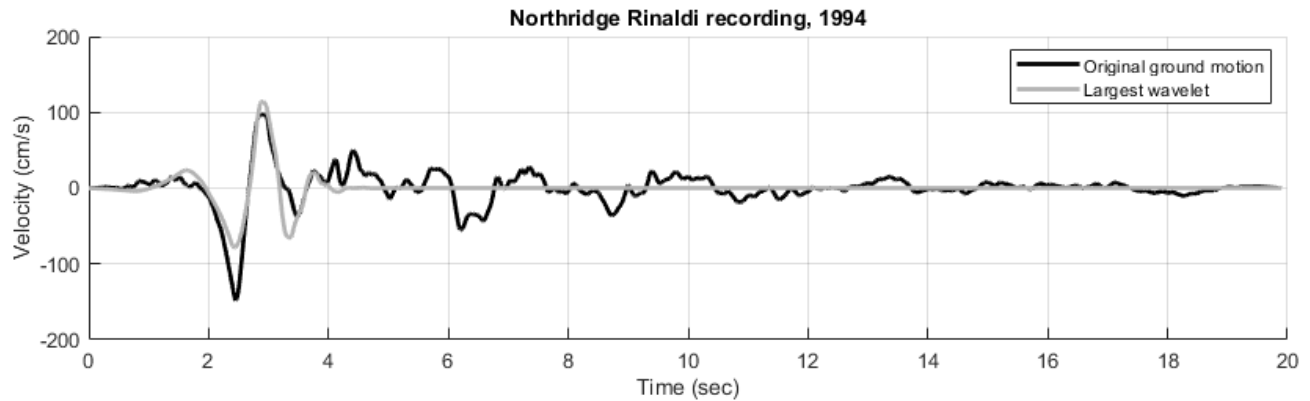
Plot the velocity time histories (initial motion and largest pulse)

Initialize figure

```
figure('Position',[7.4,508.2,1517.6,253.8],...
      'InnerPosition',[7.4,508.2,1517.6,253.8],...
      'OuterPosition',[0.2,501,1000,343.2])
hold on
```



```
% Plot the velocity time history of the initial ground motion
plot(t,xgt, 'Color', [0 0 0], 'LineWidth', 2)
% Plot the time history of the largest velocity pulse
plot(t,S1.pulseTH, 'Color', [0.7 0.7 0.7], 'LineWidth', 2)
% Finalize figure
hold off
grid on
title('Northridge Rinaldi recording, 1994')
ylim([-200,200])
xlim([0,20])
xlabel('Time (sec)')
ylabel('Velocity (cm/s)')
legend({'Original ground motion','Largest wavelet'})
drawnow;
pause(0.1)
```



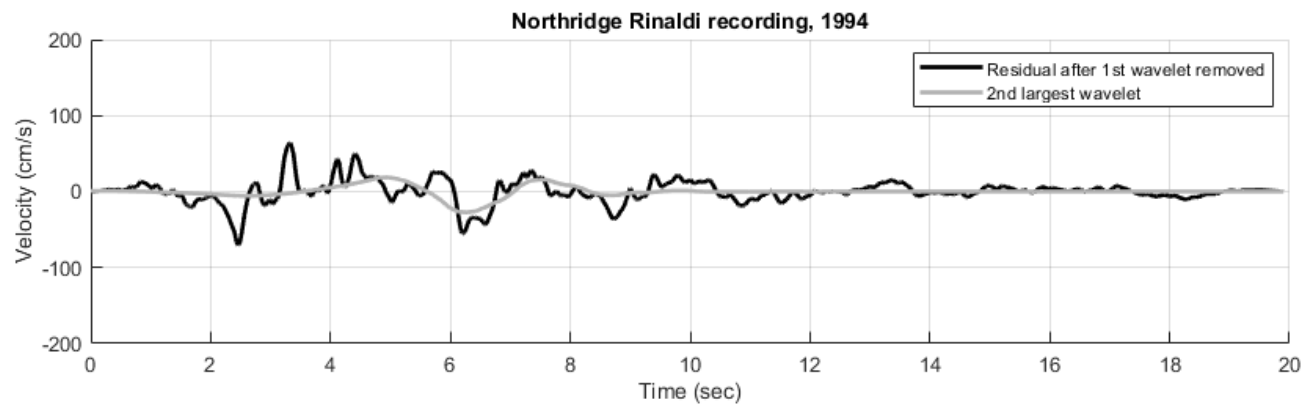
Apply OpenSeismoMatlab for extracting the 2nd up to 10th largest pulses from the residual motion after extracting the 1st pulse as above

```
Sout{1}=S1;
for i=2:10
    S1=OpenSeismoMatlab(dt,S1.resTH,sw,wname);
    Sout{i}=S1;
end
```

Plot the velocity time histories (residual motion and 2nd largest pulse)

Initialize figure

```
figure('Position',[7.4,508.2,1517.6,253.8],...
    'InnerPosition',[7.4,508.2,1517.6,253.8],...
    'OuterPosition',[0.2,501,1000,343.2])
hold on
% Plot the velocity time history of the residual ground motion
plot(t,Sout{1}.resTH, 'Color', [0 0 0], 'LineWidth', 2)
% Plot the time history of the largest velocity pulse
plot(t,Sout{2}.pulseTH, 'Color', [0.7 0.7 0.7], 'LineWidth', 2)
% Finalize figure
hold off
grid on
title('Northridge Rinaldi recording, 1994')
ylim([-200,200])
xlim([0,20])
xlabel('Time (sec)')
ylabel('Velocity (cm/s)')
legend({'Residual after 1st wavelet removed','2nd largest wavelet'})
drawnow;
pause(0.1)
```



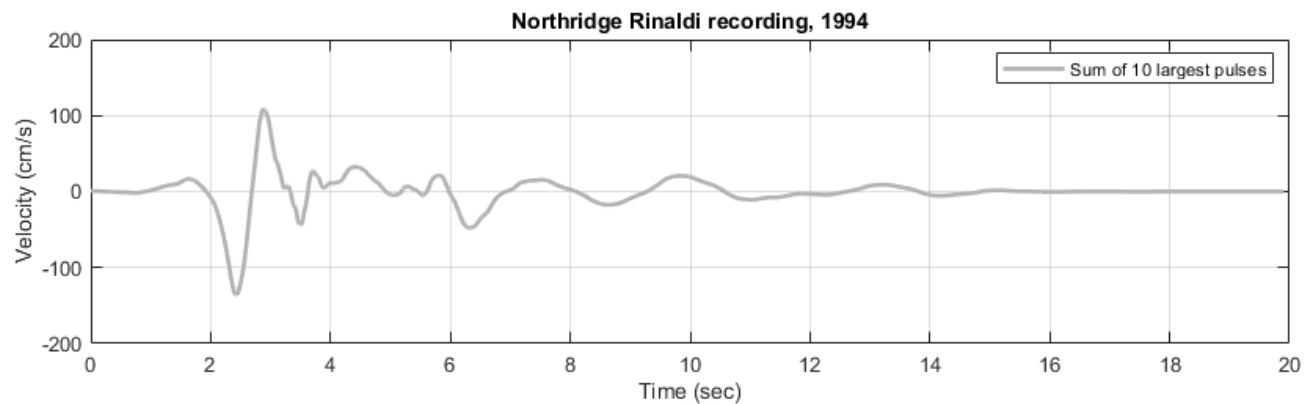
Sum the 10 largest pulses extracted from the input motion

```
sum10=zeros(size(S1.pulseTH));
for i=1:10
    sum10=sum10+Sout{i}.pulseTH;
end
```

Plot the velocity pulse using 10 largest pulses

Initialize figure

```
figure('Position',[7.4,508.2,1517.6,253.8],...
    'InnerPosition',[7.4,508.2,1517.6,253.8],...
    'OuterPosition',[0.2,501,1000,343.2])
% Plot the time history of the largest velocity pulse
plot(t,sum10, 'Color',[0.7 0.7 0.7], 'LineWidth', 2)
% Finalize figure
grid on
title('Northridge Rinaldi recording, 1994')
ylim([-200,200])
xlim([0,20])
xlabel('Time (sec)')
ylabel('Velocity (cm/s)')
legend({'Sum of 10 largest pulses'})
drawnow;
pause(0.1)
```

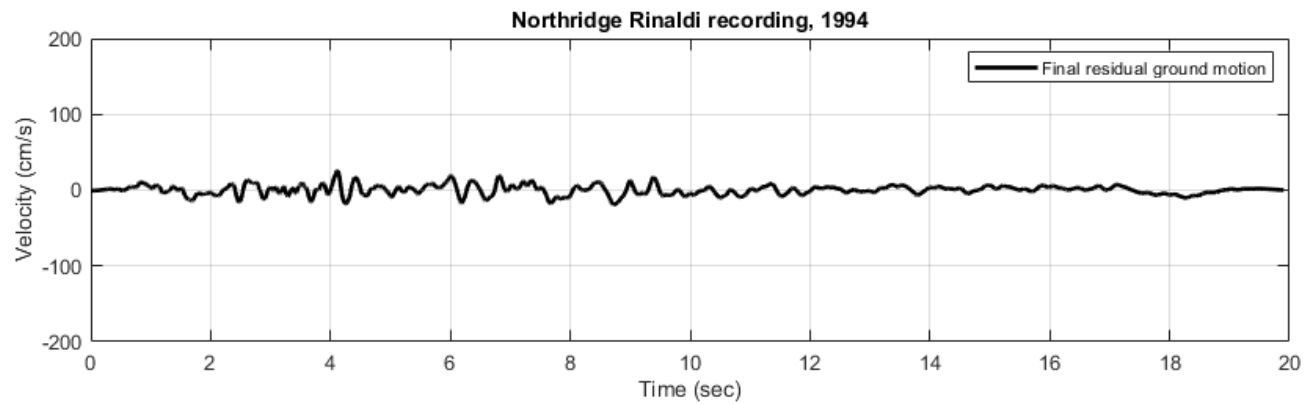


Plot the final residual ground motion

Initialize figure

```
figure('Position',[7.4,508.2,1517.6,253.8],...
    'InnerPosition',[7.4,508.2,1517.6,253.8],...
    'OuterPosition',[0.2,501,1000,343.2])
% Plot the time history of the largest velocity pulse
plot(t,S1.resTH, 'Color',[0 0 0], 'LineWidth', 2)
% Finalize figure
grid on
title('Northridge Rinaldi recording, 1994')
```

```
ylim([-200,200])  
xlim([0,20])  
xlabel('Time (sec)')  
ylabel('Velocity (cm/s)')  
legend({'Final residual ground motion'})  
drawnow;  
pause(0.1)
```



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verification Pulse Decomposition of OpenSeismoMatlab

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motion](#)
- [Perform pulse decomposition of earthquake motion](#)
- [Sum the 30 largest pulses extracted from the input motion](#)
- [Plot the velocity time histories \(original and reconstructed\)](#)
- [Plot the 30 velocity pulses in a single plot](#)
- [Copyright](#)

Reference

Shahi, S. K., & Baker, J. W. (2014). An efficient algorithm to identify strong-velocity pulses in multicomponent ground motions. Bulletin of the Seismological Society of America, 104(5), 2456-2466.

Description

The velocity pulses of a strong motion velocity time history are extracted according to Figure 3 of the above reference, and the extracted pulses are summed to give the reconstructed ground motion. There is significant agreement between the original and the reconstructed ground motions. The velocity time history of the 1979 Imperial Valley El Centro Array 4 recording is considered. The Daubechies wavelet of order 4 is used as the mother wavelet.

Earthquake motion

Load earthquake data of 1979 Imperial Valley El Centro Array 4 recording

```
eqmotion={'ImperialValleyElCentroArray4.txt'};
data=load(eqmotion{1});
t=data(:,1);
dt=t(2)-t(1);
xgt=data(:,2);
```

Perform pulse decomposition of earthquake motion

Switch

```
sw='pulsedecom';
```

Wavelet family of Daubechies wavelet of order 4

```
wname = 'db4';
```

Apply OpenSeismoMatlab for extracting the first 30 largest pulses from the initial motion

```
S1=OpenSeismoMatlab(dt,xgt,sw,wname);
Sout{1}=S1;
for i=2:30
    S1=OpenSeismoMatlab(dt,S1.resTH,sw,wname);
    Sout{i}=S1;
end
```

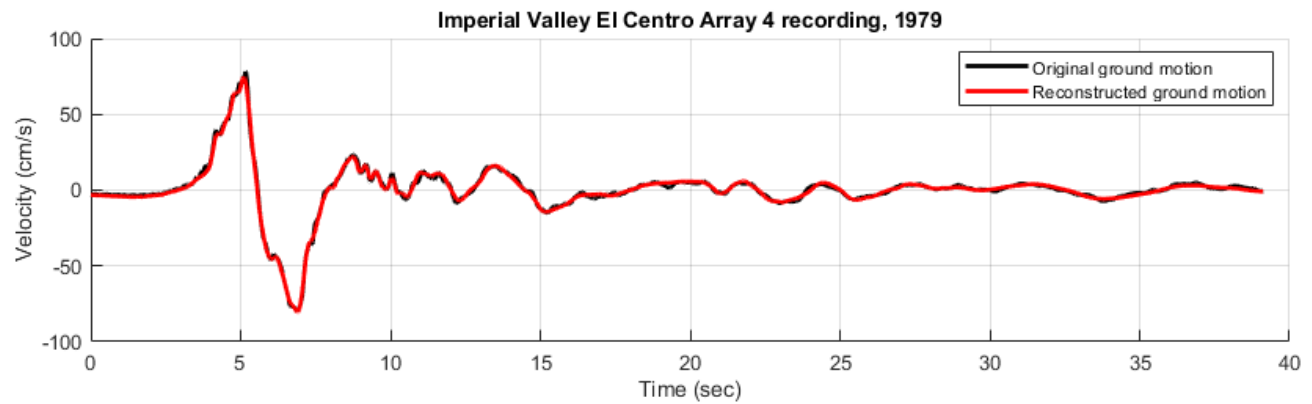
Sum the 30 largest pulses extracted from the input motion

```
sum30=zeros(size(S1.pulseTH));
for i=1:30
    sum30=sum30+Sout{i}.pulseTH;
end
```

Plot the velocity time histories (original and reconstructed)

Initialize figure

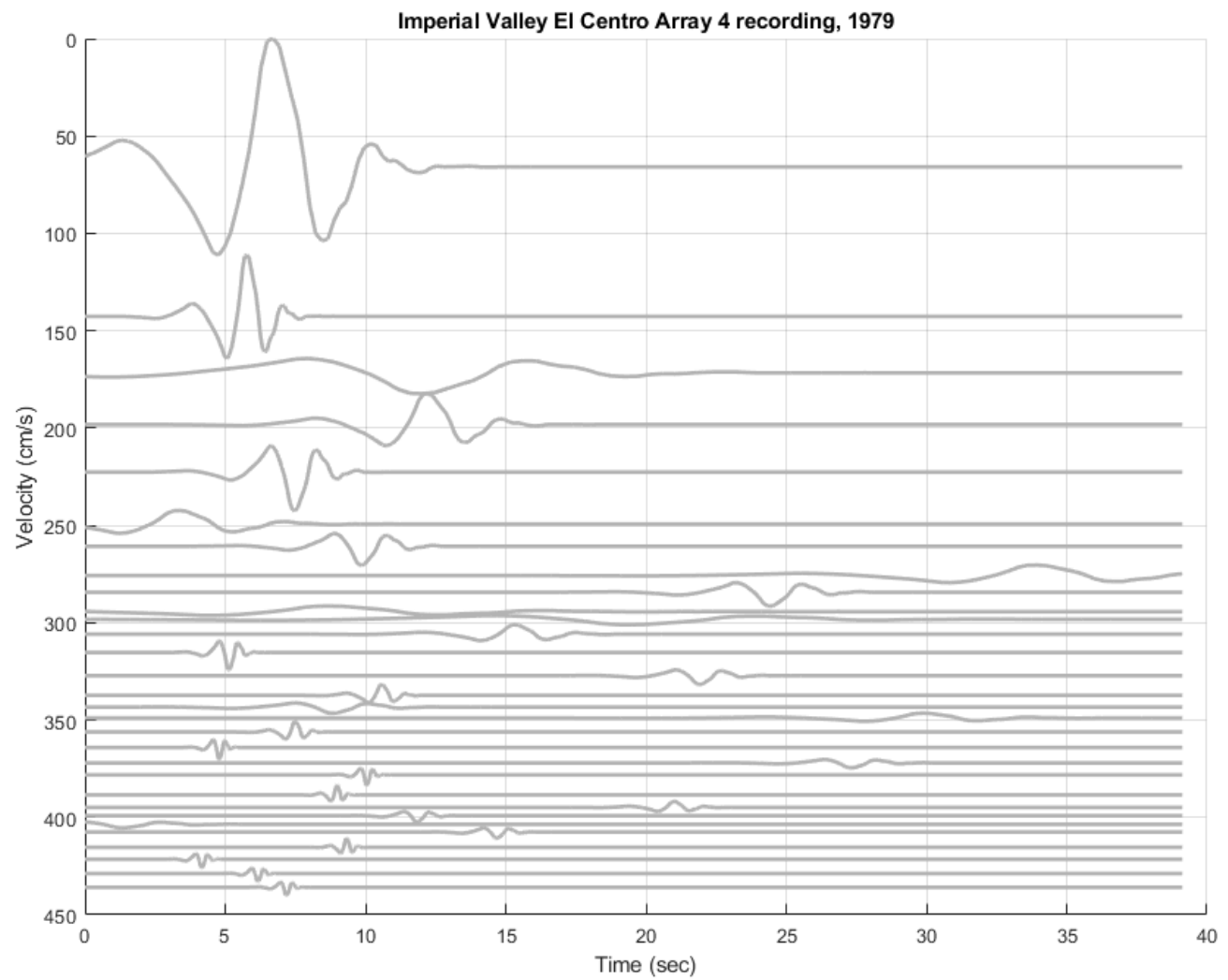
```
figure('Position',[7.4,508.2,1517.6,253.8],...
    'InnerPosition',[7.4,508.2,1517.6,253.8],...
    'OuterPosition',[0.2,501,1000,343.2])
hold on
% Plot the velocity time history of the original ground motion
plot(t,xgt, 'Color', [0 0 0], 'LineWidth', 2)
% Plot the velocity time history of the reconstructed ground motion
plot(t,sum30, 'Color', [1 0 0], 'LineWidth', 2)
% Finalize figure
hold off
grid on
title('Imperial Valley El Centro Array 4 recording, 1979')
ylim([-100,100])
xlim([0,40])
xlabel('Time (sec)')
ylabel('Velocity (cm/s)')
legend({'Original ground motion','Reconstructed ground motion'})
drawnow;
pause(0.1)
```



Plot the 30 velocity pulses in a single plot

Verify with the middle plot of Figure 3 Initialize figure

```
figure('Position',[5 50.6 1524.8 731.2],...
    'InnerPosition',[5 50.6 1524.8 731.2],...
    'OuterPosition',[-2.20 43.4 1000 820.8])
hold on
offSet=0;
for i=1:30
    offSet=offSet+abs(min(Sout{i}.pulseTH));
    plot(t,offSet+Sout{i}.pulseTH, 'Color', [0.7 0.7 0.7], 'LineWidth', 2)
    offSet=offSet+max(Sout{i}.pulseTH);
end
% Finalize figure
hold off
grid on
title('Imperial Valley El Centro Array 4 recording, 1979')
ylim([0,450])
set(gca, 'YDir','reverse')
xlim([0,40])
xlabel('Time (sec)')
ylabel('Velocity (cm/s)')
drawnow;
pause(0.1)
```



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verification Spectral Intensity according to Housner (1952)

Calculate the spectral intensity as defined by Housner (1952) using OpenSeismoMatlab

Contents

- [Reference](#)
- [Description](#)
- [Load earthquake data](#)
- [Calculate Housner Spectral Intensity](#)
- [Spectral intensities in ft](#)
- [Copyright](#)

Reference

Housner, G. W. (1952). Intensity of ground motion during strong earthquakes. California Institute of Technology, Second technical report, Office of naval research, task order 25, project NR-081-095.

Description

Table II on page 15 of the above reference is verified for the case of the El Centro, 1940 earthquake. The spectral intensity according to this table is 8.35ft for damping 0.0, 2.71ft for damping 0.2 and 1.89ft for damping 0.4. These values are verified with the present example

Load earthquake data

Earthquake acceleration time history of the El Centro earthquake will be used (El Centro, 1940, El Centro Terminal Substation Building)

```
fid=fopen('elcentro_NS_trunc.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtd=text{1,2};
```

Calculate Housner Spectral Intensity

Switch

```
sw='SIH1952';
```

First value of damping (Table II in the above reference)

```
ksi1=0.0;
```

Second value of damping (Table II in the above reference)

```
ksi2=0.2;
```

Third value of damping (Table II in the above reference)

```
ksi3=0.4;
```

Apply OpenSeismoMatlab for calculating of the spectral intensity

```
S1=OpenSeismoMatlab(dt,xgtt,sw,ksi1);  
S2=OpenSeismoMatlab(dt,xgtt,sw,ksi2);  
S3=OpenSeismoMatlab(dt,xgtt,sw,ksi3);
```

Spectral intensities in ft

For damping 0.0

```
S1.SI*3.28084
```

```
ans =
```

```
8.00634608331064
```

For damping 0.2

```
S2.SI*3.28084
```

```
ans =
```

```
2.33622318056444
```

For damping 0.4

```
S3.SI*3.28084
```

```
ans =
```

```
1.63462066423459
```

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verification Rigid plastic sliding response spectrum

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motions](#)
- [Calculate rigid plastic sliding response spectrum of earthquake motion](#)
- [Plot the acceleration time histories of the earthquake motions](#)
- [Plot the rigid plastic sliding response spectra](#)
- [Copyright](#)

Reference

Garini, E., & Gazetas, G. (2016). Rocking and Sliding Potential of the 2014 Cephalonia, Greece Earthquakes. In ICONHIC2016 1st international conference on natural hazards & infrastructure June, Chania, Greece.

Description

The rigid plastic sliding response spectra are extracted for various acceleration time histories of the 3 Feb 2014 13.34 EST Cephalonia earthquake. Three records are used: Chavriata (EW), Lixouri (EW) and Lixouri (NS). The oscillator is considered to be ideally rigid-plastic sliding on horizontal plane, as shown in Figure 4(a) of the above reference. The acceleration time histories that are used for the extraction of the spectra are plotted in this example and also shown in Figure 2 of the above reference [Chavriata (3 February) EW, Lixouri (3 February) EW, Lixouri (3 February) NS]. The rigid plastic sliding response spectra extracted in this example are compared to the corresponding spectra that appear in Figure 6 of the above reference.

Earthquake motions

Load earthquake data of Chavriata EW record

```
eqmotion={'CHV1-20140203E'};  
data=load([eqmotion{1},'.txt']);  
t1=data(:,1);  
dt1=t1(2)-t1(1);  
xgttl=data(:,2)/100;  
% Truncate the record  
ind=t1>23 & t1<33;  
xgttl=xgttl(ind);  
t1=t1(ind);
```

Load earthquake data of Lixouri EW record

```
eqmotion={'LXR1-20140203E'};  
data=load([eqmotion{1},'.txt']);  
t2=data(:,1);  
dt2=t2(2)-t2(1);  
xgttl2=data(:,2)/100;  
% Truncate the record  
ind=t2>23 & t2<33;  
xgttl2=xgttl2(ind);  
t2=t2(ind);
```

Load earthquake data of Lixouri NS record

```
eqmotion={ 'LXR1-20140203N'};  
data=load([eqmotion{1},'.txt']);  
t3=data(:,1);  
dt3=t3(2)-t3(1);  
xgtt3=data(:,2)/100;  
% Truncate the record  
ind=t3>23 & t3<33;  
xgtt3=xgtt3(ind);  
t3=t3(ind);
```

Calculate rigid plastic sliding response spectrum of earthquake motion

Switch

```
sw='rpsrs';
```

Coulomb friction coefficients

```
CF=[0.05;0.1;0.2;0.4;0.5];
```

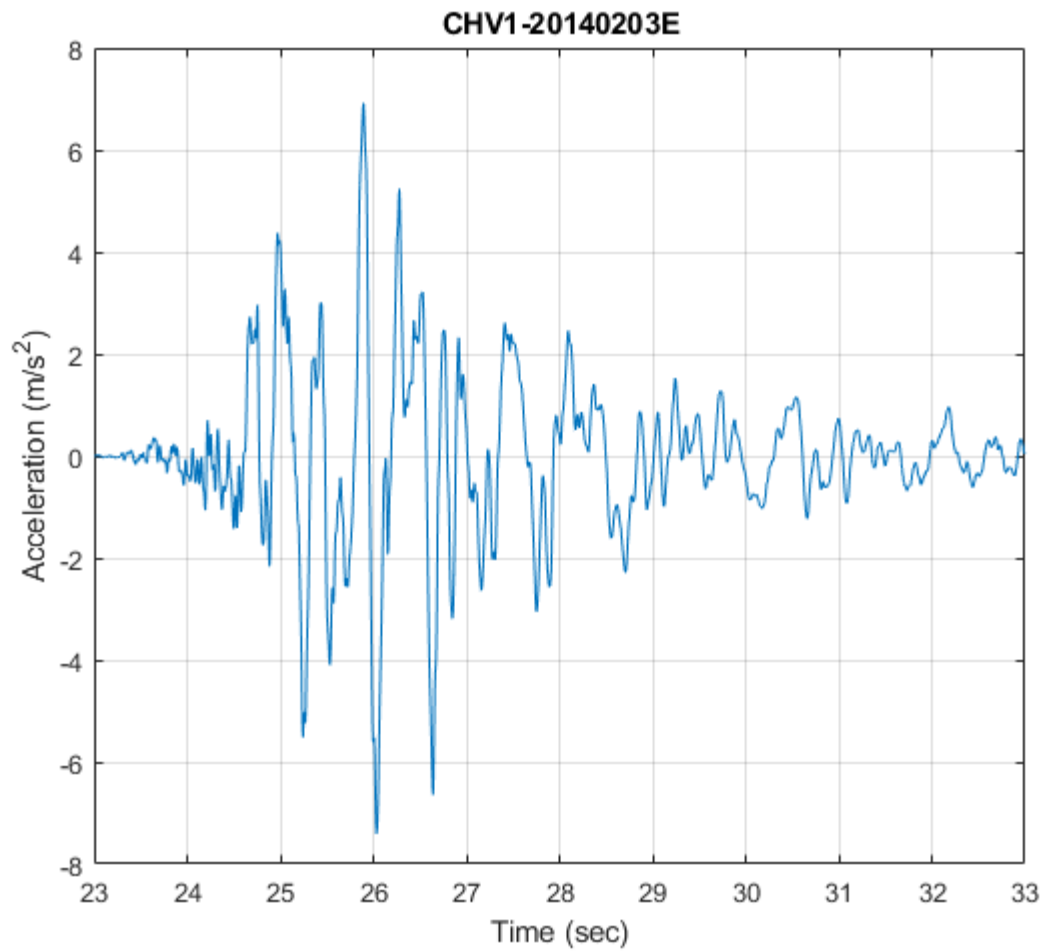
Apply OpenSeismoMatlab once for each record

```
S1=OpenSeismoMatlab(dt1,xgtt1,sw,CF);  
S2=OpenSeismoMatlab(dt2,xgtt2,sw,CF);  
S3=OpenSeismoMatlab(dt3,xgtt3,sw,CF);
```

Plot the acceleration time histories of the earthquake motions

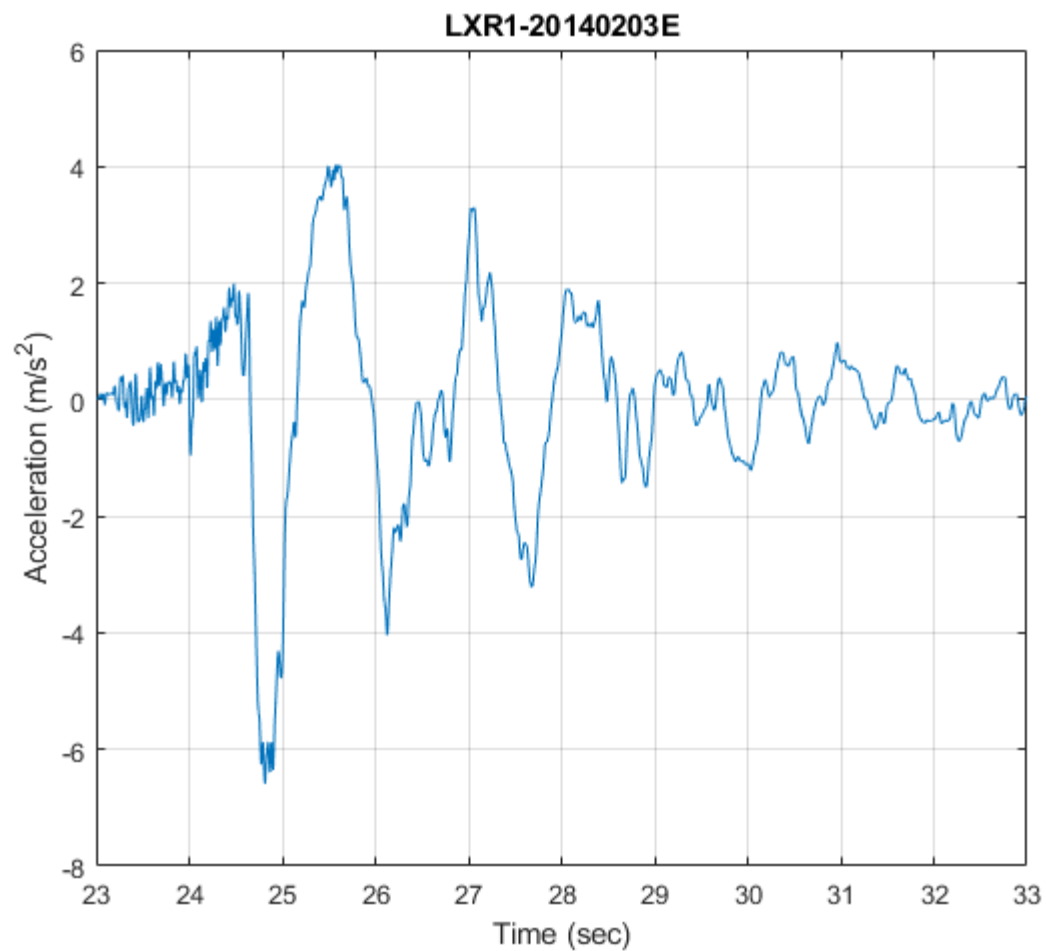
Initialize figure

```
figure()  
% Plot the acceleration time history  
plot(t1,xgtt1)  
% Finalize figure  
grid on  
title('CHV1-20140203E')  
xlabel('Time (sec)')  
ylabel('Acceleration (m/s^2)')  
drawnow;  
pause(0.1)
```



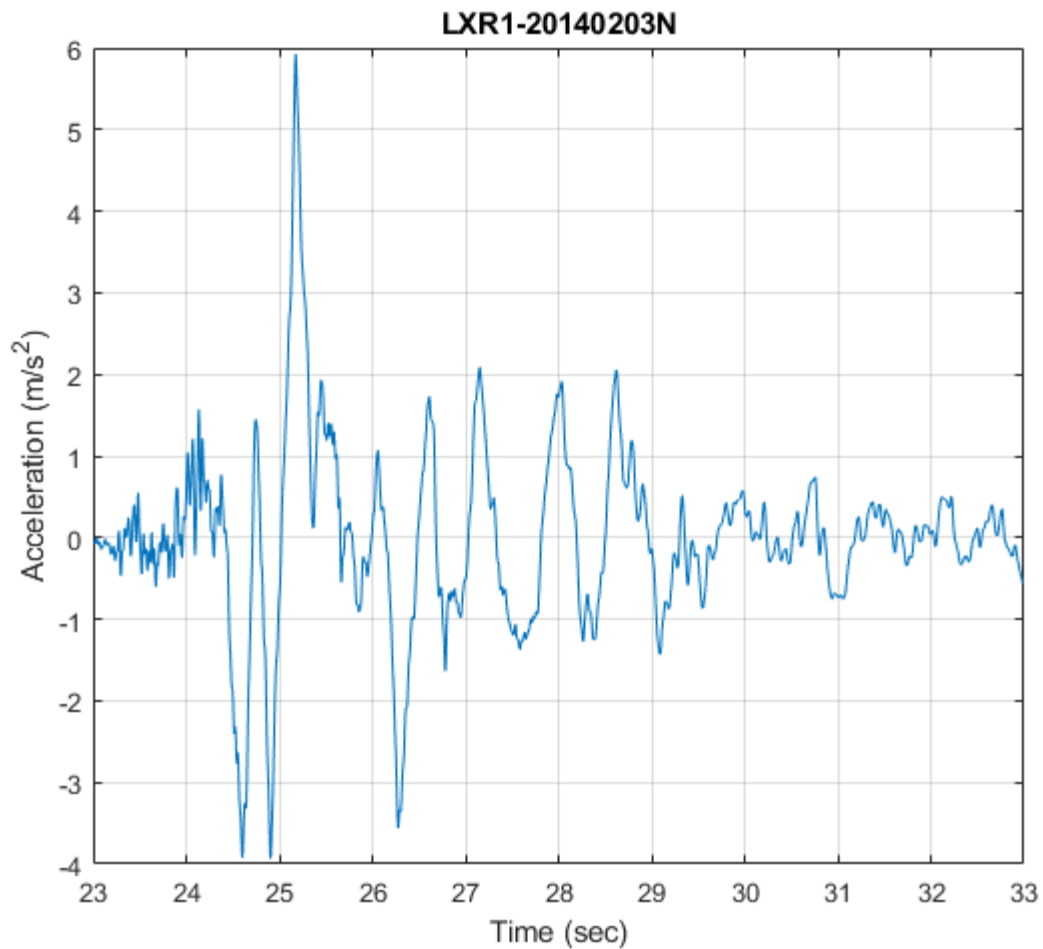
Initialize figure

```
figure()
% Plot the acceleration time history
plot(t2,xgtt2)
% Finalize figure
grid on
title('LXR1-20140203E')
xlabel('Time (sec)')
ylabel('Acceleration ( $\text{m/s}^2$ )')
drawnow;
pause(0.1)
```



Initialize figure

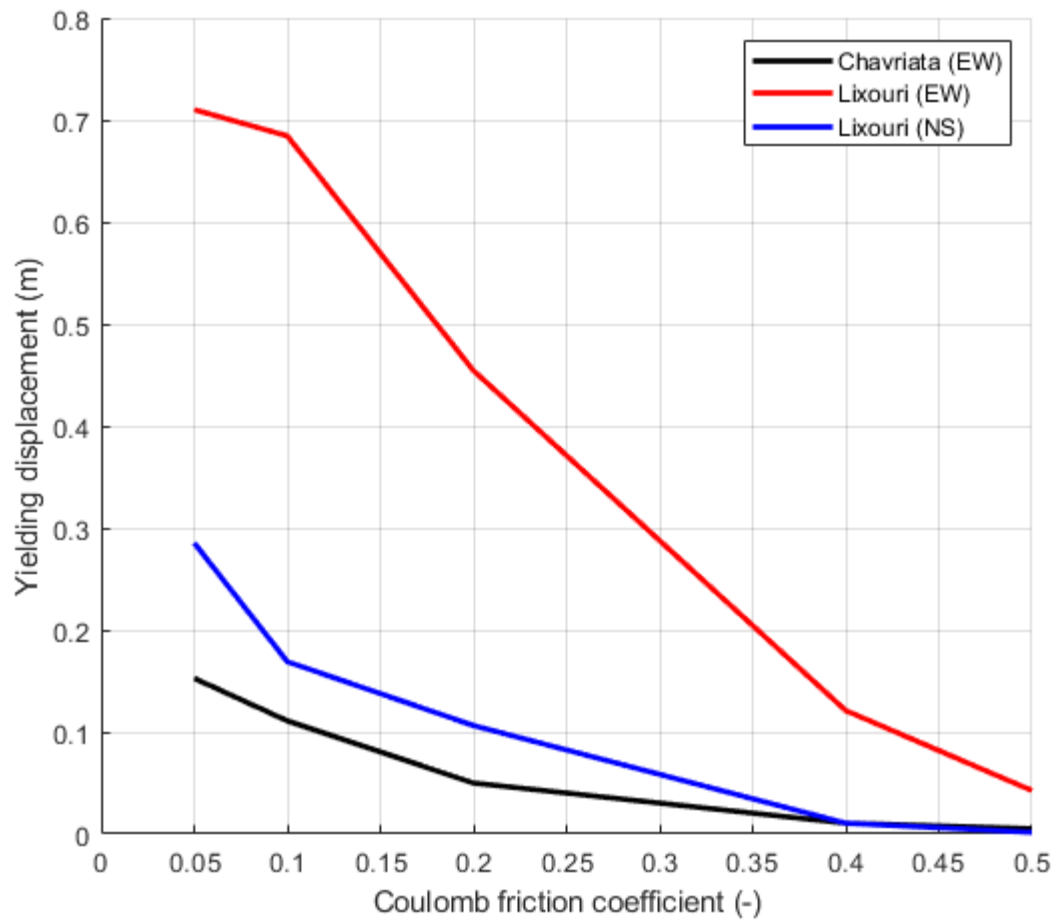
```
figure()
% Plot the acceleration time history
plot(t3,xgtt3)
% Finalize figure
grid on
title('LXR1-20140203N')
xlabel('Time (sec)')
ylabel('Acceleration (m/s^2)')
drawnow;
pause(0.1)
```



Plot the rigid plastic sliding response spectra

Initialize figure

```
figure()
hold on
% Plot the rigid plastic sliding response spectra
plot(S1.CF,S1.RPSSd, 'k-', 'LineWidth', 2)
plot(S2.CF,S2.RPSSd, 'r-', 'LineWidth', 2)
plot(S3.CF,S3.RPSSd, 'b-', 'LineWidth', 2)
hold off
% Finalize figure
grid on
xlabel('Coulomb friction coefficient (-)')
ylabel('Yielding displacement (m)')
legend({'Chavriata (EW)', 'Lixouri (EW)', 'Lixouri (NS)'})
xlim([0,0.5])
drawnow;
pause(0.1)
```



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verification Rigid plastic sliding response spectrum

Contents

- [Reference](#)
- [Description](#)
- [Earthquake motions](#)
- [Calculate rigid plastic sliding response spectrum of earthquake motion](#)
- [Plot the acceleration time histories of the earthquake motions](#)
- [Plot the rigid plastic sliding response spectra](#)
- [Copyright](#)

Reference

Paglietti, A., & Porcu, M. C. (2001). Rigid-plastic approximation to predict plastic motion under strong earthquakes. Earthquake engineering & structural dynamics, 30(1), 115-126.

Description

The rigid plastic sliding response spectra are extracted for two acceleration time histories: the Northridge (Sylmar County), Jan 1994 record and the El Centro, NS, May 1940 record, as presented in Table 1 of the above reference. The oscillator is considered to be ideally rigid-plastic sliding on horizontal plane. The acceleration time histories that are used for the extraction of the spectra are plotted in this example. The rigid plastic sliding response spectra extracted in this example are compared to the corresponding spectra that appear in Figure 6 of the above reference.

Earthquake motions

Load earthquake data of Northridge Sylmar County 1994 record

```
eqmotion={'Northridge_Sylmar_County'};
data=load([eqmotion{1},'.dat']);
t1=data(:,1);
dt1=t1(2)-t1(1);
xgtt1=data(:,2);
```

Load earthquake data of El Centro 1940 record

```
eqmotion={'elcentro_NS_trunc'};
data=load([eqmotion{1},'.dat']);
t2=data(:,1);
dt2=t2(2)-t2(1);
xgtt2=data(:,2);
```

Calculate rigid plastic sliding response spectrum of earthquake motion

Switch

```
sw='rpsrs';
```

Coulomb friction coefficients


```
CF1=[0.006;0.05;0.1;0.15;0.3;0.4;0.7;0.8];  
CF2=[0.002;0.01;0.05;0.1;0.15;0.3;0.4];
```

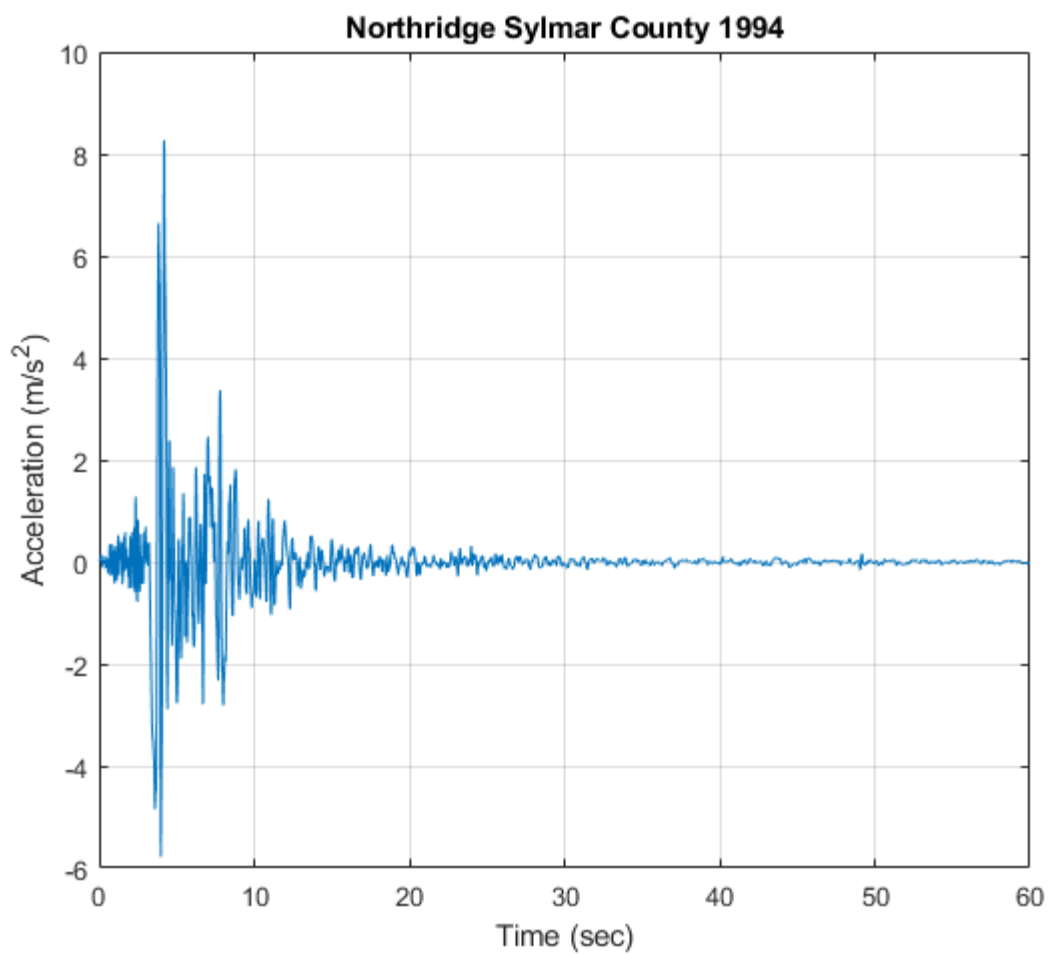
Apply OpenSeismoMatlab once for each record

```
S1=OpenSeismoMatlab(dt1,xgttl1,sw,CF1);  
S2=OpenSeismoMatlab(dt2,xgttl2,sw,CF2);
```

Plot the acceleration time histories of the earthquake motions

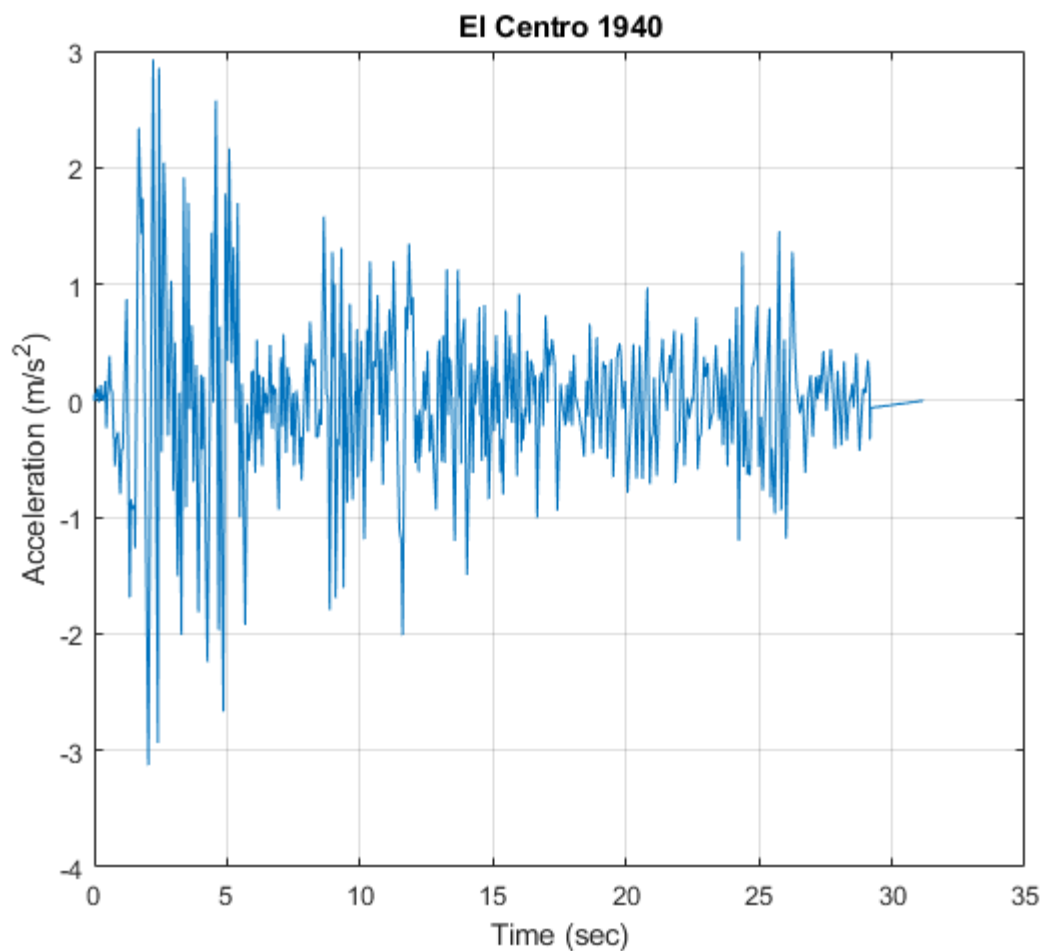
Initialize figure

```
figure()  
% Plot the acceleration time history  
plot(t1,xgttl1)  
% Finalize figure  
grid on  
title('Northridge Sylmar County 1994')  
xlabel('Time (sec)')  
ylabel('Acceleration (m/s^2)')  
drawnow;  
pause(0.1)
```



Initialize figure

```
figure()
% Plot the acceleration time history
plot(t2,xgtt2)
% Finalize figure
grid on
title('El Centro 1940')
xlabel('Time (sec)')
ylabel('Acceleration (m/s^2)')
drawnow;
pause(0.1)
```

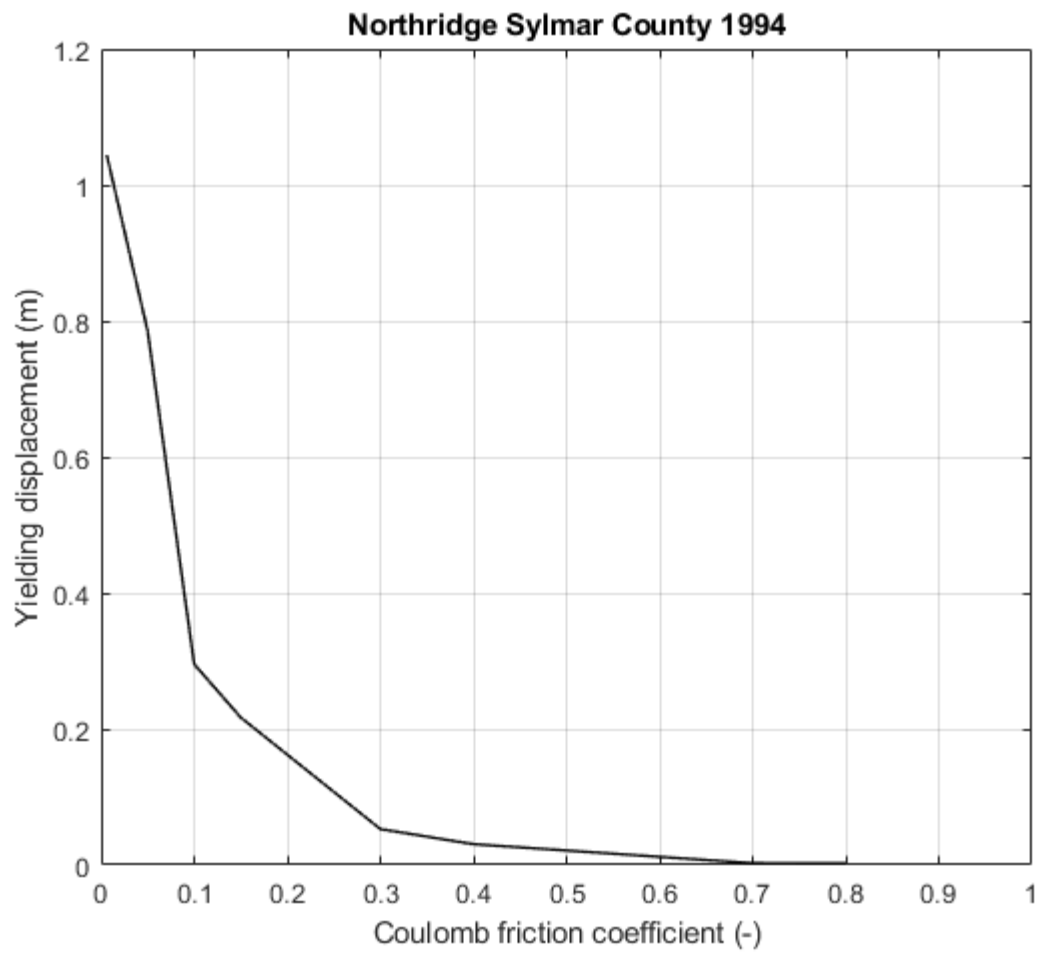


Plot the rigid plastic sliding response spectra

Initialize figure

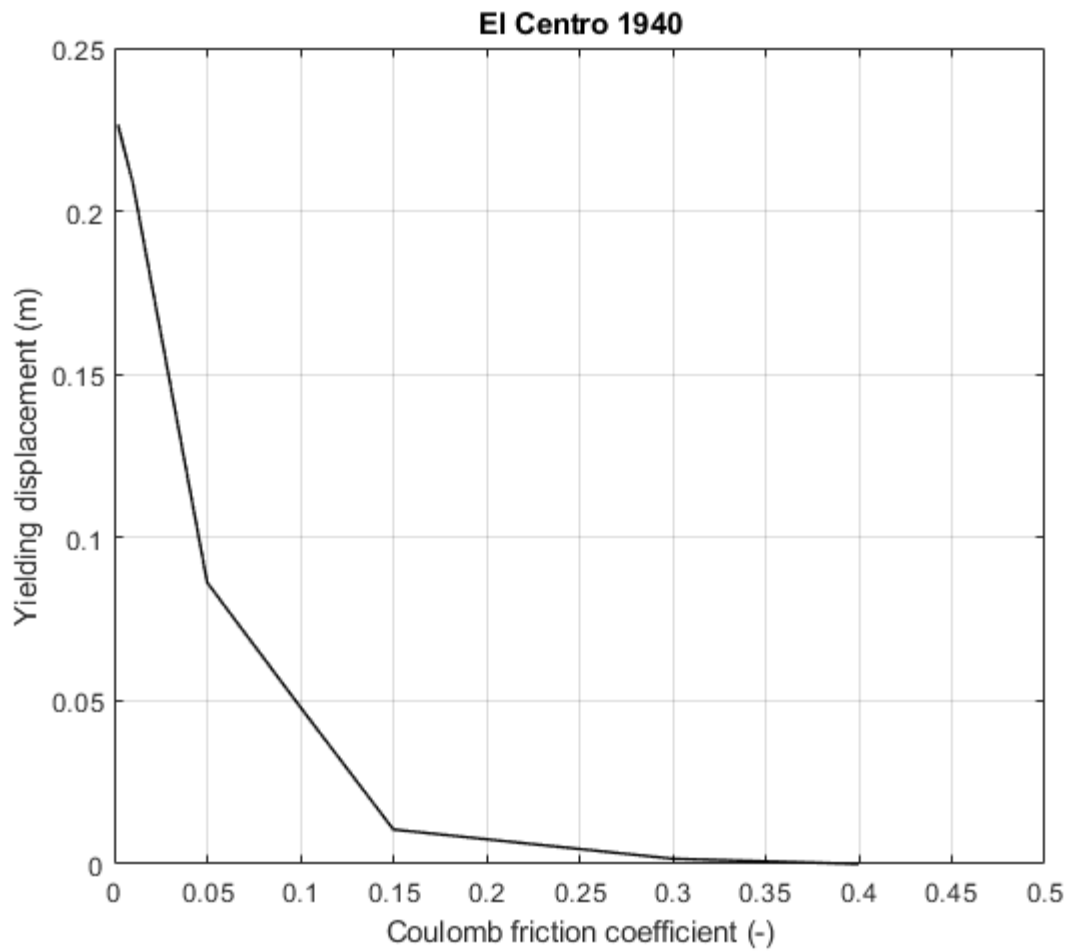
```
figure()
% Plot the rigid plastic sliding response spectra
plot(S1.CF,S1.RPSSd, 'k-', 'LineWidth', 1)
% Finalize figure
grid on
xlabel('Coulomb friction coefficient (-)')
ylabel('Yielding displacement (m)')
title('Northridge Sylmar County 1994')
xlim([0,1])
```

```
drawnow;  
pause(0.1)
```



Initialize figure

```
figure()  
% Plot the rigid plastic sliding response spectra  
plot(S2.CF,S2.RPSSd, 'k-', 'LineWidth', 1)  
% Finalize figure  
grid on  
xlabel('Coulomb friction coefficient (-)')  
ylabel('Yielding displacement (m)')  
title('El Centro 1940')  
xlim([0,0.5])  
drawnow;  
pause(0.1)
```



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