

OpenSeismoMatlab

Software for strong ground motion data processing

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baselineCorr

Documentation of the baselineCorr function.

```
helpFun('baselineCorr')
```

Baseline correction of acceleration time history

```
[COR_XG,COR_XGT,COR_XGTT] = BASELINECORR(T,XGTT)
```

Description

Linear baseline correction is performed for an uncorrected acceleration time history. Initially, first order fitting (straight line) is performed on the acceleration time history and the fitting line is subtracted from the acceleration time history, giving thus the first correction. Afterwards, the first correction of the acceleration is integrated to obtain the velocity, and then first order fitting (straight line) is performed on this velocity time history. The gradient of the straight fitting line is then subtracted from the first correction of the acceleration time history, giving thus the second correction of the acceleration time history. The second correction of the acceleration time history is then integrated to give the corrected velocity and displacement time histories.

Input parameters

T [double(1:numsteps x 1)] is the time vector of the input acceleration time history XGTT. numsteps is the length of the input acceleration time history.
XGTT [double(1:nstep x 1)]: column vector of the acceleration history of the excitation imposed at the base. nstep is the number of time steps of the dynamic response.

Output parameters

COR_XG [double(1:nstep x 1)]: time-history of displacement
COR_XGT [double(1:nstep x 1)]: time-history of velocity
COR_XGTT [double(1:nstep x 1)]: time-history of acceleration

Example

```
fid=fopen('elcentro.dat','r');  
text=textscan(fid,'%f %f');  
fclose(fid);  
time=text{1,1};  
xgtt1=text{1,2};  
dt=time(2)-time(1);  
xgt1 = cumtrapz(time,xgtt1);  
xg1 = cumtrapz(time,xgt1);  
[xg2, xgt2, xgtt2] = baselineCorr(time,xgtt1)  
figure()  
plot(time,xgtt1)  
hold on  
plot(time,xgtt2)  
figure()  
plot(time,xgt1)  
hold on  
plot(time,xgt2)  
figure()
```

```
plot(time,xg1)
hold on
plot(time,xg2)
```

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Documentation of the BLKIN function.

```
helpFun('BLKIN')
```

Bilinear kinematic hysteretic model with elastic viscous damping

```
[F,K,C,K_STATUS,D] = BLKIN(U,UT,K_HI,K_LO,UY,M,KSI,K_STATUS,D)
```

Description

Define the internal force vector, tangent stiffness matrix and tangent damping matrix of a bilinear elastoplastic hysteretic structure with elastic damping as a function of displacement and velocity.

The MDOF structure modeled with this function consists of lumped masses connected with stiffness and damping elements in series. Each lumped mass has one degree of freedom. The first degree of freedom is at the top of the structure and the last at its fixed base. However, the last degree of freedom is not included in the input arguments of the function, i.e. not contained in `ndof`, as it is always fixed. The nonlinear stiffness is virtually of the bilinear type, where an initial stiffness and a post-yield stiffness are defined. The unloading or reloading curve of this model are parallel to the initial loading curve, and a hysteresis loop is created by continuously loading and unloading the structure above its yield limit. This behavior can be viewed as hardening of the kinematic type.

An appropriate reference for this function definition is Hughes, Pister & Taylor (1979): "Implicit-explicit finite elements in nonlinear transient analysis". This function should be defined in accordance with equations (3.1), (3.2) and (3.3) of this paper. This representation has as special cases nonlinear elasticity and a class of nonlinear "rate-type" viscoelastic materials. Tangent stiffness and tangent damping matrices are the "consistent" linearized operators associated to `f` in the sense of [Hughes & Pister, "Consistent linearization in mechanics of solids", Computers and Structures, 8 (1978) 391-397].

Input parameters

`U` [double(1 x 1)] is the absolute displacement.

`UT` [double(1 x 1)] is the absolute velocity.

`K_HI` [double(1 x 1)] is the initial stiffness of the system before its first yield, i.e. the high stiffness.

`K_LO` [double(1 x 1)] is the post-yield stiffness of the system, i.e. the low stiffness.

`UY` [double(1 x 1)] is the yield limit of the structure. The structure is considered to yield, if the displacement exceeds `uy(i)`.

`M` [double(1 x 1)] is the lumped mass.

`KSI` [double(1 x 1)] is the ratio of critical viscous damping of the system, assumed to be unique for all damping elements of the structure.

`K_STATUS` [double(1 x 1)] is the is the stiffness vector which takes into account any plastic response of the structure. It is used to record the status of the structure so that it is known before the next application of this function at a next (time) step.

Initialize by setting $K_STATUS=K_HI$.

D [double(1 x 1)] is the is the equilibrium displacement vector which takes into account any plastic response of the structure. It is used to record the status of the structure so that it is known before the next application of this function at a next (time) step. Initialize by setting $D=zeros(ndof,1)$.

Output parameters

F [double(1 x 1)] is the internal force vector of the structure (sum of forces due to stiffness and damping) at displacement u and velocity ut

K [double(1 x 1)] is the tangent stiffness matrix (nonlinear function of displacement u and velocity ut). It is equivalent to the derivative $d(f)/d(u)$

C [double(1 x 1)] is the tangent damping matrix (nonlinear function of displacement u and velocity ut). It is equivalent to the derivative $d(f)/d(u)$

K_STATUS [double(1 x 1)] is the is the stiffness vector which takes into account any plastic response of the structure. It is used to record the status of the structure so that it is known before the next application of this function at a next (time) step.

D [double(1 x 1)] is the is the equilibrium displacement vector which takes into account any plastic response of the structure. It is used to record the status of the structure so that it is known before the next application of this function at a next (time) step.

Example

```
u=0:0.2:4;
u=[u,u(end:-1:1)];
u=[u,-u];
u=[u u];
ut=0.001*ones(1,numel(u));
ut=[ut,-ut];
ut=[ut,ut(end:-1:1)];
ut=[ut ut];
k_hi=1000;
k_lo=1;
uy=2;
M=1;
ksi=0.05;
k=k_hi;
d=0;
f=zeros(1,numel(u));
for i=1:numel(u)
    [f(i),K,C,k,d] = BLKIN(u(i),ut(i),k_hi,k_lo,uy,M,ksi,k,d);
end
figure()
plot(u,f)
```

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Documentation of the CDReSp function.

```
helpFun('CDReSp')
```

Constant Ductility Response Spectra

```
[PSA,PSV,SD,SV,SA,FYK,MUK,ITERK]=CDRESP(DT,XGTT,T,KSI,MU,N,TOL,...  
    PYSF,DTTOL,ALGID,RINF,MAXTOL,JMAX,DAK)
```

Description

The constant ductility response spectra for a given time-history of constant time step, a given eigenperiod range, a given viscous damping ratio and a given ductility are computed. See section 7.5 in Chopra (2012) and the notes "Inelastic Response Spectra" (CEE 541. Structural Dynamics) by Henri P. Gavin.

Input parameters

DT [double(1 x 1)] is the time step of the input acceleration time history XGTT.

XGTT [double(1:numsteps x 1)] is the input acceleration time history. numsteps is the length of the input acceleration time history.

T [double(1:numSDOFs x 1)] contains the values of eigenperiods for which the response spectra are requested. numSDOFs is the number of SDOF oscillators being analysed to produce the spectra.

KSI [double(1 x 1)] is the fraction of critical viscous damping.

MU [double(1 x 1)] is the target ductility for which the response spectra are calculated.

N [double(1 x 1)] is the maximum number of iterations that can be performed until convergence of the calculated ductility to the target ductility is achieved.

TOL [double(1 x 1)] is the tolerance for convergence for the target ductility.

PYSF [double(1 x 1)] is the post-yield stiffness factor, i.e. the ratio of the postyield stiffness to the initial stiffness. PYSF=0 is not recommended for simulation of an elastoplastic system. A small positive value is always suggested. PYSF is ignored if MU=1.

DTTOL [double(1 x 1)] is the tolerance for resampling of the input acceleration time history. For a given eigenperiod T, resampling takes place if $DT/T > dtTol$.

ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:

- 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
- 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
- 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
- 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
- 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm

'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm
 'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
 'U1-V0-Opt': Optimal numerical dissipation and dispersion first order displacement zero order velocity algorithm
 'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm
 'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order velocity algorithm
 'Newmark ACA': Newmark Average Constant Acceleration method
 'Newmark LA': Newmark Linear Acceleration method
 'Newmark BA': Newmark Backward Acceleration method
 'Fox-Goodwin': Fox-Goodwin formula

RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues of the amplification matrix. For the amplification matrix see eq.(61) in Zhou & Tamma (2004).

MAXTOL [double(1 x 1)] is the maximum tolerance of convergence of the Full Newton Raphson method for numerical computation of acceleration.

JMAX [double(1 x 1)] is the maximum number of iterations per increment. If JMAX=0 then iterations are not performed and the MAXTOL parameter is not taken into account.

DAK [double(1 x 1)] is the infinitesimal acceleration for the calculation of the derivative required for the convergence of the Newton-Raphson iteration.

Output parameters

PSA [double(1:numSDOFs x 1)] is the Pseudo-Spectral Acceleration.
 PSV [double(1:numSDOFs x 1)] is the Pseudo-Spectral Velocity.
 SD [double(1:numSDOFs x 1)] is the Spectral Displacement.
 SV [double(1:numSDOFs x 1)] is the Spectral Velocity.
 SA [double(1:numSDOFs x 1)] is the Spectral Acceleration.
 FYK [double(1:numSDOFs x 1)] is the yield limit that each SDOF must have in order to attain ductility equal to μ_K .
 MUK [double(1:numSDOFs x 1)] is the achieved ductility for each period (each SDOF).
 ITERK [double(1:numSDOFs x 1)] is the number of iterations needed for convergence for each period (each SDOF).

Example

```
dt=0.02;
N=10;
a=rand(N,1)-0.5;
b=100*pi*rand(N,1);
c=pi*(rand(N,1)-0.5);
t=(0:dt:(100*dt))';
xgtt=zeros(size(t));
for i=1:N
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));
end
T=(0.04:0.04:4)';
```

```
ksi=0.05;  
mu=2;  
n=50;  
tol=0.01;  
pysf=0.1;  
dtTol=0.02;  
AlgID='U0-V0-Opt';  
rinf=1;  
maxtol=0.01;  
jmax=200;  
dak=eps;  
[CDPSa,CDPSv,CDSd,CDSv,CDSa,fyK,muK,iterK]=CDReSp(dt,xgtt,T,ksi,...  
    mu,n,tol,pysf,dtTol,AlgID,rinf,maxtol,jmax,dak);  
figure()  
plot(T,CDSd)  
figure()  
plot(T,fyK)  
figure()  
plot(T,muK)  
figure()  
plot(T,iterK)
```

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Documentation of the DRHA function.

```
helpFun('DRHA')
```

Dynamic Response History Analysis

```
[U,V,A,F,ES,ED] = DRHA(K,M,DT,XGTT,KSI,U0,UT0,ALGID,RINF)
```

Description

Calculate the dynamic response of a linear MDOF system using modal analysis. This function is part of the OpenSeismoMatlab software. It can be used as standalone, however attention is needed for the correctness of the input arguments, since no checks are performed in this function. See the example `example_DRHA.m` for more details about how this function can be implemented.

Input parameters

K [double(:inf x 1)] is the stiffness of the system.
M [double(:inf x 1)] is the lumped masses of the structure.
DT [double(1 x 1)] is the time step of the dynamic response history analysis
XGTT [double(1:nstep x 1)]: column vector of the acceleration history of the excitation imposed at the base. nstep is the number of time steps of the dynamic response.
KSI [double(1 x 1)] is the ratio of critical damping of the SDOF system.
U0 [double(:inf x 1)] is the initial displacement of the SDOF system.
UT0 [double(:inf x 1)] is the initial velocity of the SDOF system.
ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:
 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm
 'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
 'U1-V0-Opt': Optimal numerical dissipation and dispersion

first order displacement zero order velocity algorithm
'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm
'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order velocity algorithm
'Newmark ACA': Newmark Average Constant Acceleration method
'Newmark LA': Newmark Linear Acceleration method
'Newmark BA': Newmark Backward Acceleration method
'Fox-Goodwin': Fox-Goodwin formula

RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues of the amplification matrix. For the amplification matrix see eq.(61) in Zhou & Tamma (2004).

Output parameters

U [double(1 x 1:nstep)]: displacement time history.
V [double(1 x 1:nstep)]: velocity time history.
A [double(1 x 1:nstep)]: acceleration time history.
F [double(1 x 1:nstep)]: equivalent static force time history.
ES [double(1 x 1:nstep)]: time-history of the recoverable strain energy of the system (total and not incremental).
ED [double(1 x 1:nstep)]: time-history of the energy dissipated by viscoelastic damping during each time step (incremental). cumsum(Ed) gives the time history of the total energy dissipated at dof i from the start of the dynamic analysis.

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Documentation of the FASp function.

```
helpFun('FASp')
```

Fourier amplitude spectrum

```
[F,U] = FASP(DT,XGTT)
```

Description

Fourier amplitude spectrum of an acceleration time history.

Input parameters

DT [double(1 x 1)] is the time step of the input acceleration time history XGTT.

XGTT [double(1:numsteps x 1)] is the input acceleration time history.
numsteps is the length of the input acceleration time history.

Output parameters

F [double(1:2^(nextpow2(length(XGTT))-1) x 1)] is the frequency range in which the Fourier amplitudes are calculated.

U [double(1:2^(nextpow2(length(XGTT))-1) x 1)] contains the Fourier amplitudes

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HalfStep

Documentation of the HalfStep function.

```
helpFun('HalfStep')
```

Reproduce signal with half time step

```
UNEW = HALFSTEP(U)
```

Input parameters

U [double(1:n x 1)] is the input signal with time step dt.

Output parameters

UNEW [double(1:n x 1)] is the output signal with time step dt/2.

Verification:

```
u=0.2:0.2:4;  
uNew=HalfStep(u);  
figure()  
plot((1:numel(u)),u)  
hold on  
plot((1:0.5:numel(u)),uNew)
```

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Documentation of the IDA function.

```
helpFun('IDA')
```

Incremental Dynamic Analysis

```
[DM, IM]=IDA(DT,XGTT,T,LAMBD AF,IM_DM,M,UY,PYSF,KSI,ALGID,U0,UT0,...
    RINF,MAXTOL,JMAX,DAK)
```

Description

This function performs incremental dynamic analysis of a given acceleration time history and SDOF oscillator.

Input parameters

DT [double(1 x 1)] is the time step of the input acceleration time history XGTT.

XGTT [double(:inf x 1)] is the input acceleration time history.

numsteps is the length of the input acceleration time history.

T [double(1 x 1)] contains the eigenperiod of the SDOF system for which the incremental dynamic analysis response curve is requested.

LAMBD AF [double(:inf x 1)] contains the values of the scaling factor (lambda factor) for the incremental dynamic analysis.

IM_DM [char(1 x :inf)] is the Intensity Measure (IM) - Damage Measure (DM) pair that is to be calculated from the incremental dynamic analysis. IM_DM can take one of the following values (strings are case insensitive):

- 'SA_MU': Spectral acceleration-ductility
- 'PGD_MU': Peak displacement-ductility
- 'PGV_MU': Peak velocity-ductility
- 'PGA_MU': Peak acceleration-ductility
- 'SA_DISP': Spectral acceleration-displacement
- 'PGD_DISP': Peak displacement-displacement
- 'PGV_DISP': Peak velocity-displacement
- 'PGA_DISP': Peak acceleration-displacement
- 'SA_VEL': Spectral acceleration-velocity
- 'PGD_VEL': Peak displacement-velocity
- 'PGV_VEL': Peak velocity-velocity
- 'PGA_VEL': Peak acceleration-velocity
- 'SA_ACC': Spectral acceleration-acceleration
- 'PGD_ACC': Peak displacement-acceleration
- 'PGV_ACC': Peak velocity-acceleration
- 'PGA_ACC': Peak acceleration-acceleration

M [double(1 x 1)] is the mass of the SDOF oscillator.

UY [double(1 x 1)] is the yield displacement of the SDOF oscillator.

PYSF [double(1 x 1)] is the post-yield stiffness factor, i.e. the ratio of the postyield stiffness to the initial stiffness. PYSF=0 is not recommended for simulation of an elastoplastic system. A small positive value is always suggested. PYSF is ignored if MU=1.

KSI [double(1 x 1)] is the fraction of critical viscous damping.

ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:

'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm
 'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
 'U1-V0-Opt': Optimal numerical dissipation and dispersion first order displacement zero order velocity algorithm
 'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm
 'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order velocity algorithm
 'Newmark ACA': Newmark Average Constant Acceleration method
 'Newmark LA': Newmark Linear Acceleration method
 'Newmark BA': Newmark Backward Acceleration method
 'Fox-Goodwin': Fox-Goodwin formula

U0 [double(1 x 1)] is the initial displacement of the SDOF oscillator.

UT0 [double(1 x 1)] is the initial velocity of the SDOF oscillator.

RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues of the amplification matrix. For the amplification matrix see eq.(61) in Zhou & Tamma (2004). Default value 0.

MAXTOL [double(1 x 1)] is the maximum tolerance of convergence of the Full Newton Raphson method for numerical computation of acceleration.

JMAX [double(1 x 1)] is the maximum number of iterations per increment. If JMAX=0 then iterations are not performed and the MAXTOL parameter is not taken into account.

DAK [double(1 x 1)] is the infinitesimal acceleration for the calculation of the derivative required for the convergence of the Newton-Raphson iteration.

Output parameters

DM [double(:inf x 1)] is the Damage Measure.

IM [double(:inf x 1)] is the Intensity Measure.

Example

```
eqmotions={'elcentro'};
data=load([eqmotions{1},'.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgtd=data(:,2);
sw='ida';
```

```
T=1;
lambdaF=logspace(log10(0.001),log10(10),100);
IM_DM='Sa_disp';
m=1;
uy = 0.082*9.81/(2*pi/T)^2;
pysf=0.01;
ksi=0.05;
S5=OpenSeismoMatlab(dt,xgtt,sw,T,lambdaF,IM_DM,m,uy,pysf,ksi);
figure()
plot(S5.DM*1000,S5.IM/9.81,'k','LineWidth',1)
grid on
xlabel('Displacement (mm)')
ylabel('Sa(T1,5%)[g]')
xlim([0,200])
ylim([0,0.7])
```

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```
helpFun('LEReSp')
```

Linear Elastic Response Spectra

```
[PSA,PSV,SD,SV,SA,SIEVABS,SIEVREL]=LERESP(DT,XGTT,T,KSI,DTTOL,...  
      ALGID,RINF)
```

Description

The linear elastic response spectra for a given time-history of constant time step, a given eigenperiod range and a given viscous damping ratio are computed. These spectra include the spectral acceleration, spectral velocity, spectral displacement, pseudoacceleration, pseudovelocity, absolute equivalent input energy velocity and relative equivalent input energy velocity. This function is part of the OpenSeismoMatlab software. It can be used as standalone, however attention is needed for the correctness of the input arguments, since no checks are performed in this function. See the example `example_LEReSp.m` for more details about how this function can be implemented.

Input parameters

DT [double(1 x 1)] is the time step of the input acceleration time history XGTT.

XGTT [double(1:numsteps x 1)] is the input acceleration time history. numsteps is the length of the input acceleration time history.

T [double(1:numSDOFs x 1)] contains the values of eigenperiods for which the response spectra are requested. numSDOFs is the number of SDOF oscillators being analysed to produce the spectra.

KSI [double(1 x 1)] is the fraction of critical viscous damping.

DTTOL [double(1 x 1)] is the maximum ratio of the integration time step to the eigenperiod.

ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:

- 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
- 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
- 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
- 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
- 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
- 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
- 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
- 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order

```

velocity algorithm
'U0-V1-DA': Discontinuous acceleration (zero spurious root at
the high frequency limit) zero order displacement first order
velocity algorithm
'U1-V0-Opt': Optimal numerical dissipation and dispersion
first order displacement zero order velocity algorithm
'U1-V0-CA': Continuous acceleration (zero spurious root at
the low frequency limit) first order displacement zero order
velocity algorithm
'U1-V0-DA': Discontinuous acceleration (zero spurious root at
the high frequency limit) first order displacement zero order
velocity algorithm
'Newmark ACA': Newmark Average Constant Acceleration method
'Newmark LA': Newmark Linear Acceleration method
'Newmark BA': Newmark Backward Acceleration method
'Fox-Goodwin': Fox-Goodwin formula
RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues
of the amplification matrix. For the amplification matrix see
eq.(61) in Zhou & Tamma (2004).

```

Output parameters

```

PSA [double(1:numSDOFs x 1)] is the Pseudo Acceleration Spectrum.
PSV [double(1:numSDOFs x 1)] is the Pseudo Velocity Spectrum.
SD [double(1:numSDOFs x 1)] is the Spectral Displacement.
SV [double(1:numSDOFs x 1)] is the Spectral Velocity.
SA [double(1:numSDOFs x 1)] is the Spectral Acceleration.
SIEVABS [double(1:numSDOFs x 1)] is the equivalent absolute input
energy velocity.
SIEVREL [double(1:numSDOFs x 1)] is the equivalent relative input
energy velocity.

```

Example

```

dt=0.02;
N=10;
a=rand(N,1)-0.5;
b=100*pi*rand(N,1);
c=pi*(rand(N,1)-0.5);
t=(0:dt:(100*dt))';
xgtt=zeros(size(t));
for i=1:N
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));
end
T=logspace(log10(0.02),log10(50),1000)';
ksi=0.05;
dtTol=0.02;
AlgID='U0-V0-Opt';
rinf=1;
[PSa,PSv,Sd,Sv,Sa,SievABS,SievREL]=LEReSp(dt,xgtt,T,ksi,dtTol,...
    AlgID,rinf);

```

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Documentation of the LIDA function.

```
helpFun('LIDA')
```

Linear Implicit Dynamic Analysis

```
[U,UT,UTT] = LIDA(DT,XGTT,OMEGA,KSI,U0,UT0,ALGID,RINF)
```

Description

Linear implicit direct time integration of second order differential equation of motion of dynamic response of linear elastic SDOF systems. The General Single Step Single Solve (GSSSS) family of algorithms published by X.Zhou & K.K.Tamma (2004) is employed for direct time integration of the general linear or nonlinear structural Single Degree of Freedom (SDOF) dynamic problem. The optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm designed according to the above journal article, is used in this routine. This algorithm encompasses the scope of Linear Multi-Step (LMS) methods and is limited by the Dahlquist barrier theorem (Dahlquist,1963). The force - displacement - velocity relation of the SDOF structure is linear. This function is part of the OpenSeismoMatlab software. It can be used as standalone, however attention is needed for the correctness of the input arguments, since no checks are performed in this function. See the example `example_LIDA.m` for more details about how this function can be implemented.

Input parameters

DT [double(1 x 1)] is the time step
XGTT [double(1:nstep x 1)] is the column vector of the acceleration history of the excitation imposed at the base. nstep is the number of time steps of the dynamic response.
OMEGA [double(1 x 1)] is the eigenfrequency of the structure in rad/sec.
KSI [double(1 x 1)] is the ratio of critical damping of the SDOF system.
U0 [double(1 x 1)] is the initial displacement of the SDOF system.
UT0 [double(1 x 1)] is the initial velocity of the SDOF system.
ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:
 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order


```

velocity algorithm
'U0-V1-Opt': Optimal numerical dissipation and dispersion
zero order displacement first order velocity algorithm
'U0-V1-CA': Continuous acceleration (zero spurious root at
the low frequency limit) zero order displacement first order
velocity algorithm
'U0-V1-DA': Discontinuous acceleration (zero spurious root at
the high frequency limit) zero order displacement first order
velocity algorithm
'U1-V0-Opt': Optimal numerical dissipation and dispersion
first order displacement zero order velocity algorithm
'U1-V0-CA': Continuous acceleration (zero spurious root at
the low frequency limit) first order displacement zero order
velocity algorithm
'U1-V0-DA': Discontinuous acceleration (zero spurious root at
the high frequency limit) first order displacement zero order
velocity algorithm
'Newmark ACA': Newmark Average Constant Acceleration method
'Newmark LA': Newmark Linear Acceleration method
'Newmark BA': Newmark Backward Acceleration method
'Fox-Goodwin': Fox-Goodwin formula
RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues
of the amplification matrix. For the amplification matrix see
eq.(61) in Zhou & Tamma (2004).

```

Output parameters

```

U [double(1:nstep x 1)] is the time-history of displacement
UT [double(1:nstep x 1)] is the time-history of velocity
UTT [double(1:nstep x 1)] is the time-history of acceleration

```

Example (Figure 6.6.1 in Chopra, Tn=1sec)

```

dt=0.02;
fid=fopen('elcentro.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
xgtt=text{1,2};
Tn=1;
omega=2*pi/Tn;
ksi=0.02;
u0=0;
ut0=0;
AlgID='U0-V0-Opt';
rinf=1;
[u,ut,utt] = LIDA(dt,xgtt,omega,ksi,u0,ut0,AlgID,rinf);
D=max(abs(u))/0.0254

```

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NLIDABLKIN

Documentation of the NLIDABLKIN function.

```
helpFun('NLIDABLKIN')
```

Non Linear Implicit Dynamic Analysis of a bilinear kinematic hardening hysteretic structure with elastic damping

```
[U,UT,UTT,FS,EY,ES,ED,JITER] = NLIDABLKIN(DT,XGTT,M,K_HI,K_LO,UY,...  
      KSI,ALGID,U0,UT0,RINF,MAXTOL,JMAX,DAK)
```

Description

General linear implicit direct time integration of second order differential equations of a bilinear elastoplastic hysteretic SDOF dynamic system with elastic damping, with lumped mass. The General Single Step Single Solve (GSSSS) family of algorithms published by X.Zhou & K.K.Tamma (2004) is employed for direct time integration of the general linear or nonlinear structural Single Degree of Freedom (SDOF) dynamic problem. Selection among 9 algorithms, all designed according to the above journal article, can be made in this routine. These algorithms encompass the scope of Linear Multi-Step (LMS) methods and are limited by the Dahlquist barrier theorem (Dahlquist,1963).

Input parameters

DT [double(1 x 1)] is the time step of the integration
XGTT [double(1:NumSteps x 1)] is the acceleration time history which is imposed at the lumped mass of the SDOF structure.
M [double(1 x 1)] is the lumped masses of the structure. Define the lumped masses from the top to the bottom, excluding the fixed dof at the base
K_HI [double(1 x 1)] is the initial stiffness of the system before its first yield, i.e. the high stiffness. Give the stiffness of each storey from top to bottom.
K_LO [double(1 x 1)] is the post-yield stiffness of the system, i.e. the low stiffness. Give the stiffness of each storey from top to bottom.
UY [double(1 x 1)] is the yield limit of the stiffness elements of the structure. The element is considered to yield, if the interstorey drift between degrees of freedom i and i+1 exceeds UY(i). Give the yield limit of each storey from top to bottom.
KSI [double(1 x 1)] is the ratio of critical viscous damping of the system, assumed to be unique for all damping elements of the structure.
ALGID [char(1 x :inf)] is the algorithm to be used for the time integration. It can be one of the following strings for superior optimally designed algorithms:
 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm

'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
 'U0-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement zero order velocity algorithm
 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm
 'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
 'U1-V0-Opt': Optimal numerical dissipation and dispersion first order displacement zero order velocity algorithm
 'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm
 'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order velocity algorithm
 'Newmark ACA': Newmark Average Constant Acceleration method
 'Newmark LA': Newmark Linear Acceleration method
 'Newmark BA': Newmark Backward Acceleration method
 'Fox-Goodwin': Fox-Goodwin formula
 U0 [double(1 x 1)] is the initial displacement.
 UT0 [double(1 x 1)] is the initial velocity.
 RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues of the amplification matrix. For the amplification matrix see eq.(61) in Zhou & Tamma (2004).
 MAXTOL [double(1 x 1)] is the maximum tolerance of convergence of the Full Newton Raphson method for numerical computation of acceleration.
 JMAX [double(1 x 1)] is the maximum number of iterations per increment. If JMAX=0 then iterations are not performed and the MAXTOL parameter is not taken into account.
 DAK [double(1 x 1)] is the infinitesimal acceleration for the calculation of the derivative required for the convergence of the Newton-Raphson iteration.

Output parameters

U [double(1 x 1:NumSteps)] is the time-history of displacement
 UT [double(1 x 1:NumSteps)] is the time-history of velocity
 UTT [double(1 x 1:NumSteps)] is the time-history of acceleration
 FS [double(1 x 1:NumSteps)] is the time-history of the internal force of the structure analysed.
 EY [double(1 x 1:NumSteps)] is the time history of the sum of the energy dissipated by yielding during each time step and the recoverable strain energy of the system (incremental). cumsum(EY)-Es gives the time history of the total energy dissipated by yielding from the start of the dynamic analysis.
 ES [double(1 x 1:NumSteps)] is the time-history of the recoverable strain energy of the system (total and not incremental).
 ED [double(1 x 1:NumSteps)] is the time-history of the energy dissipated by viscoelastic damping during each time step (incremental). cumsum(ED) gives the time history of the total energy dissipated from the start of the dynamic analysis.
 JITER [double(1 x 1:NumSteps)] is the iterations per increment

Notation in the code

u=displacement
un=displacement after increment n
ut=velocity
utn=velocity after increment n
utt=acceleration
uttn=acceleration after increment n

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OpenSeismoMatlab

Documentation of the OpenSeismoMatlab function.

```
helpFun('OpenSeismoMatlab')
```

Seismic parameters and processing of an acceleration time history

Syntax

```
PARAM=OpenSeismoMatlab(DT,XGTT,SW,___)
PARAM=OpenSeismoMatlab(DT,XGTT,'PGA')
PARAM=OpenSeismoMatlab(DT,XGTT,'PGV')
PARAM=OpenSeismoMatlab(DT,XGTT,'PGD')
PARAM=OpenSeismoMatlab(DT,XGTT,'ARIAS')
PARAM=OpenSeismoMatlab(DT,XGTT,'TIMEHIST',BASELINESW)
PARAM=OpenSeismoMatlab(DT,XGTT,'RESAMPLE',DTI)
PARAM=OpenSeismoMatlab(DT,XGTT,'ES',T,KSI,ALGID,RINF,DTTOL)
PARAM=OpenSeismoMatlab(DT,XGTT,'CDS',T,KSI,MU,PYSF,DTTOL,ALGID,...
    RINF,MAXTOL,JMAX,DAK)
PARAM=OpenSeismoMatlab(DT,XGTT,'FS')
PARAM=OpenSeismoMatlab(DT,XGTT,'BUTTERWORTHHIGH',BORDER,FLC)
PARAM=OpenSeismoMatlab(DT,XGTT,'BUTTERWORTHLOW',BORDER,FHC)
PARAM=OpenSeismoMatlab(DT,XGTT,'IDA',T,LAMBDADF,IM_DM,M,UY,PYSF,...
    KSI,ALGID,U0,UT0,RINF,MAXTOL,JMAX,DAK)
Omit or set as empty ([]) the input arguments for which default
values are desired.
```

Description

This function calculates the seismic parameters, develops various spectra and performs various analyses from an acceleration time history. More specifically, it calculates the following:

- 1) Peak ground acceleration
- 2) Peak ground velocity
- 3) Peak ground displacement
- 4) Total cumulative energy and normalized cumulative energy vs time
- 5) Significant duration D_{5-95} according to Trifunac & Brady (1975)
- 6) Significant duration D_{5-75}
- 7) Total Arias intensity (I_a)
- 8) Velocity time history (with baseline correction or not)
- 9) Displacement time history (with baseline correction or not)
- 10) Resampled acceleration time history (i.e. the input acceleration time history with modified time step size)
- 11) Linear elastic pseudo-acceleration response spectrum
- 12) Linear elastic pseudo-velocity response spectrum
- 13) Linear elastic displacement response spectrum
- 14) Linear elastic velocity response spectrum
- 15) Linear elastic acceleration response spectrum
- 16) Constant ductility displacement response spectrum
- 17) Constant ductility velocity response spectrum
- 18) Constant ductility acceleration response spectrum
- 19) Fourier amplitude spectrum
- 20) Mean period (T_m)
- 21) Lowpass Butterworth-filtered acceleration time history
- 22) Highpass Butterworth-filtered acceleration time history
- 23) Incremental Dynamic Analysis (IDA) of SDOF system excited with the input acceleration time history

Depending on the value of SW, which determines the type of analysis that OpenSeismoMatlab performs, various additional parameters are needed as input by the user. All possible syntaxes appear above.

Input parameters

DT [double(1 x 1)] is the size of the time step of the input acceleration time history xgtt.

XGTT [double(:inf x 1)] is the input acceleration time history.

SW [char(1 x :inf)] is a string which determines which parameters, spectras or analyses of the input acceleration time history will be calculated. SW can take one of the following values (strings are case insensitive):

- 'TIMEHIST': the displacement, velocity and acceleration time histories are calculated.
- 'RESAMPLE': the acceleration time history with modified time step size is calculated.
- 'PGA': The peak ground acceleration is calculated.
- 'PGV': The peak ground velocity is calculated.
- 'PGD': The peak ground displacement is calculated.
- 'ARIAS': The total cumulative energy, significant duration D_{5_95} according to Trifunac & Brady (1975), significant duration D_{5_75} and Arias intensity are calculated.
- 'ES': The linear elastic response spectra and pseudospectra are calculated.
- 'CDS': The constant ductility response spectra are calculated.
- 'FS': The Fourier amplitude spectrum and the mean period are calculated.
- 'BUTTERWORTHHIGH': The high-pass Butterworth filtered acceleration time history is calculated.
- 'BUTTERWORTHLOW': The low-pass Butterworth filtered acceleration time history is calculated.
- 'IDA': Incremental Dynamic Analysis of an elastoplastic SDOF system excited by the input acceleration time history is performed.

Additional required parameters

BASELINE_{SW} [logical(1 x 1)] determines if baseline correction will be applied for the calculation of the various time histories.

DTI [double(1 x 1)] is the new time step size for resampling of the input acceleration time history.

T [double(:inf x 1)] contains the values of eigenperiods for which the response spectra are requested. Its length is the number of SDOF oscillators being analysed to produce the spectra. T must be a vector if SW='ES' or SW='CDS'. T must be scalar if SW='IDA'.

KSI [double(1 x 1)] is the fraction of critical viscous damping.

ALGID [char(1 x :inf)] is the algorithm to be used for the time integration, if applicable. It can be one of the following strings for superior optimally designed algorithms (strings are case sensitive):

- 'generalized a-method': The generalized a-method (Chung & Hulbert, 1993)
- 'HHT a-method': The Hilber-Hughes-Taylor method (Hilber, Hughes & Taylor, 1977)
- 'WBZ': The Wood-Bossak-Zienkiewicz method (Wood, Bossak & Zienkiewicz, 1980)
- 'U0-V0-Opt': Optimal numerical dissipation and dispersion zero order displacement zero order velocity algorithm
- 'U0-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement zero order velocity algorithm
- 'U0-V0-DA': Discontinuous acceleration (zero spurious root at

the high frequency limit) zero order displacement zero order velocity algorithm
 'U0-V1-Opt': Optimal numerical dissipation and dispersion zero order displacement first order velocity algorithm
 'U0-V1-CA': Continuous acceleration (zero spurious root at the low frequency limit) zero order displacement first order velocity algorithm
 'U0-V1-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) zero order displacement first order velocity algorithm
 'U1-V0-Opt': Optimal numerical dissipation and dispersion first order displacement zero order velocity algorithm
 'U1-V0-CA': Continuous acceleration (zero spurious root at the low frequency limit) first order displacement zero order velocity algorithm
 'U1-V0-DA': Discontinuous acceleration (zero spurious root at the high frequency limit) first order displacement zero order velocity algorithm
 'Newmark ACA': Newmark Average Constant Acceleration method
 'Newmark LA': Newmark Linear Acceleration method
 'Newmark BA': Newmark Backward Acceleration method
 'Fox-Goodwin': Fox-Goodwin formula

Default value 'U0-V0-Opt'.

MU [double(1 x 1)] is the specified ductility for which the constant ductility response spectra are calculated.

PYSF [double(1 x 1)] is the post-yield stiffness factor, i.e. the ratio of the postyield stiffness to the initial stiffness. PYSF=0 is not recommended for simulation of an elastoplastic system; a small positive value is always suggested due to numerical reasons. PYSF is ignored if MU=1. Default value 0.01.

BORDER [double(1 x 1)] is the order of the Butterworth filter that is applied for filtering of the acceleration time history.

FLC [double(1 x 1)] is the low cutoff frequency for the high-pass Butterworth filter.

FHC [double(1 x 1)] is the high cutoff frequency for the low-pass Butterworth filter.

LAMBDAF [double(:inf x 1)] contains the values of the scaling factor (lambda factor) for the incremental dynamic analysis.

IM_DM [char(1 x :inf)] is the Intensity Measure (IM) - Damage Measure (DM) pair that is to be calculated from the incremental dynamic analysis. IM_DM can take one of the following values (strings are case insensitive):

'SA_MU': Spectral acceleration-ductility
 'PGD_MU': Peak displacement-ductility
 'PGV_MU': Peak velocity-ductility
 'PGA_MU': Peak acceleration-ductility
 'SA_DISP': Spectral acceleration-displacement
 'PGD_DISP': Peak displacement-displacement
 'PGV_DISP': Peak velocity-displacement
 'PGA_DISP': Peak acceleration-displacement
 'SA_VEL': Spectral acceleration-velocity
 'PGD_VEL': Peak displacement-velocity
 'PGV_VEL': Peak velocity-velocity
 'PGA_VEL': Peak acceleration-velocity
 'SA_ACC': Spectral acceleration-acceleration
 'PGD_ACC': Peak displacement-acceleration
 'PGV_ACC': Peak velocity-acceleration
 'PGA_ACC': Peak acceleration-acceleration

M [double(1 x 1)] is the mass of the SDOF oscillator.

UY [double(1 x 1)] is the yield displacement of the SDOF oscillator.

U0 [double(1 x 1)] is the initial displacement of the SDOF oscillator.

UT0 [double(1 x 1)] is the initial velocity of the SDOF oscillator.

RINF [double(1 x 1)] is the minimum absolute value of the eigenvalues of the amplification matrix. For the amplification matrix see eq.(61) in Zhou & Tamma (2004). Default value 0.

MAXTOL [double(1 x 1)] is the maximum tolerance of convergence of the Full Newton Raphson method for numerical computation of acceleration.

JMAX [double(1 x 1)] is the maximum number of iterations per increment. If JMAX=0 then iterations are not performed and the MAXTOL parameter is not taken into account.

DAK [double(1 x 1)] is the infinitesimal acceleration for the calculation of the derivative required for the convergence of the Newton-Raphson iteration.

DTTOL [double(1 x 1)] is the tolerance for resampling of the input acceleration time history. For a given eigenperiod T, resampling takes place if $DT/T > dtTol$. Default value 0.02.

Output parameters

PARAM (structure) has the following fields:

PARAM.time [double(:inf x 1)] Time

PARAM.acc [double(:inf x 1)] Acceleration time history

PARAM.vel [double(:inf x 1)] Velocity time history

PARAM.disp [double(:inf x 1)] Displacement time history

PARAM.PGA [double(1 x 1)] Peak ground acceleration

PARAM.PGV [double(1 x 1)] Peak ground velocity

PARAM.PGD [double(1 x 1)] Peak ground displacement

PARAM.Ecum [double(1 x 1)] Total cumulative energy

PARAM.EcumTH [double(:inf x 1)] normalized cumulative energy vs time

PARAM.t_5_95 [double(1 x 2)] Time instants at which 5% and 95% of cumulative energy have occurred

PARAM.Td_5_95 [double(1 x 1)] Time between when 5% and 95% of cumulative energy has occurred (significant duration according to Trifunac-Brady (1975))

PARAM.t_5_75 [double(1 x 2)] Time instants at which 5% and 75% of cumulative energy have occurred

PARAM.Td_5_75 [double(1 x 1)] Time between when 5% and 75% of cumulative energy has occurred

PARAM.arias [double(1 x 1)] Total Arias intensity (Ia)

PARAM.PSa [double(:inf x 1)] Linear elastic pseudo-acceleration response spectrum

PARAM.PSv [double(:inf x 1)] Linear elastic pseudo-velocity response spectrum

PARAM.Sd [double(:inf x 1)] Linear elastic displacement response spectrum

PARAM.Sv [double(:inf x 1)] Linear elastic velocity response spectrum

PARAM.Sa [double(:inf x 1)] Linear elastic acceleration response spectrum

PARAM.SievABS [double(:inf x 1)] Linear elastic absolute input energy equivalent velocity spectrum

PARAM.SievREL [double(:inf x 1)] Linear elastic relative input energy equivalent velocity spectrum

PARAM.PredPSa [double(1 x 1)] Predominant acceleration of the PSa spectrum

PARAM.PredPeriod [double(1 x 1)] Predominant period of the PSa spectrum

PARAM.CDPSa [double(:inf x 1)] Constant ductility pseudo-acceleration response spectrum

PARAM.CDPSv [double(:inf x 1)] Constant ductility pseudo-velocity
response spectrum
PARAM.CDSd [double(:inf x 1)] Constant ductility displacement
response spectrum
PARAM.CDSv [double(:inf x 1)] Constant ductility velocity
response spectrum
PARAM.CDSa [double(:inf x 1)] Constant ductility acceleration
response spectrum
PARAM.fyK [double(:inf x 1)] yield limit that each SDOF must have
in order to attain ductility equal to PARAM.muK.
PARAM.muK [double(:inf x 1)] achieved ductility for each period
(each SDOF).
PARAM.iterK [double(:inf x 1)] number of iterations needed for
convergence for each period (each SDOF).
PARAM.FAS [double(1:2^(nextpow2(length(xgtt))-1) x 1)] Fourier
amplitude spectrum
PARAM.Tm [double(1 x 1)] Mean period (Tm)
PARAM.Fm [double(1 x 1)] Mean frequency (Fm)
param.DM [double(:inf x 1)] is the damage measure (DM) of the
incremental dynamic analysis
param.IM [double(:inf x 1)] is the intensity measure (IM) of the
incremental dynamic analysis

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baselineCorr

Apply baseline correction in OpenSeismoMatlab

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Earthquake motion

Load earthquake data

```
fid=fopen('Imperial_Valley_El_Centro_9_EW.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
time=text{1,1};
xgttl=text{1,2};
dt=time(2)-time(1);
```

Integrate without baseline correction

Calculate the velocity and displacement time histories

```
xgt1 = cumtrapz(time,xgttl);
xg1 = cumtrapz(time,xgt1);
```

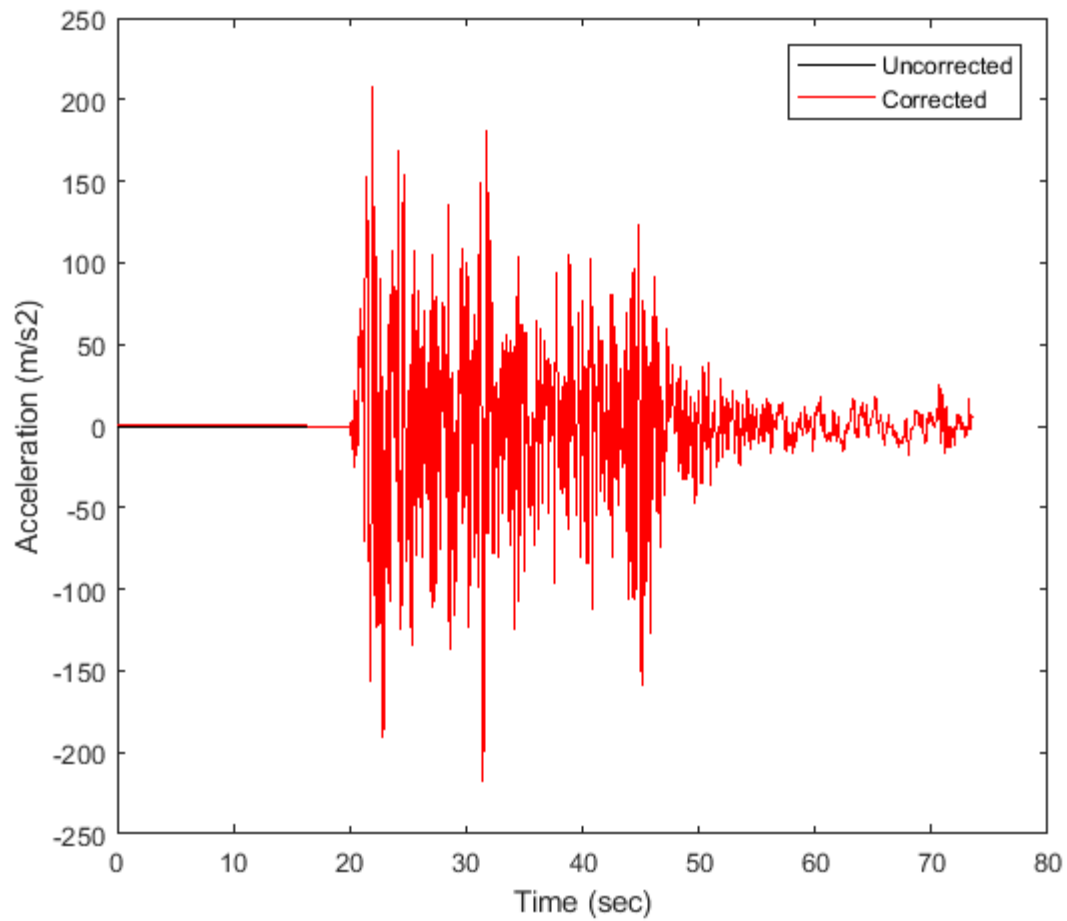
Integrate with baseline correction

Calculate the displacement, velocity and acceleration time histories

```
[xg2, xgt2, xgttl2] = baselineCorr(time,xgttl);
```

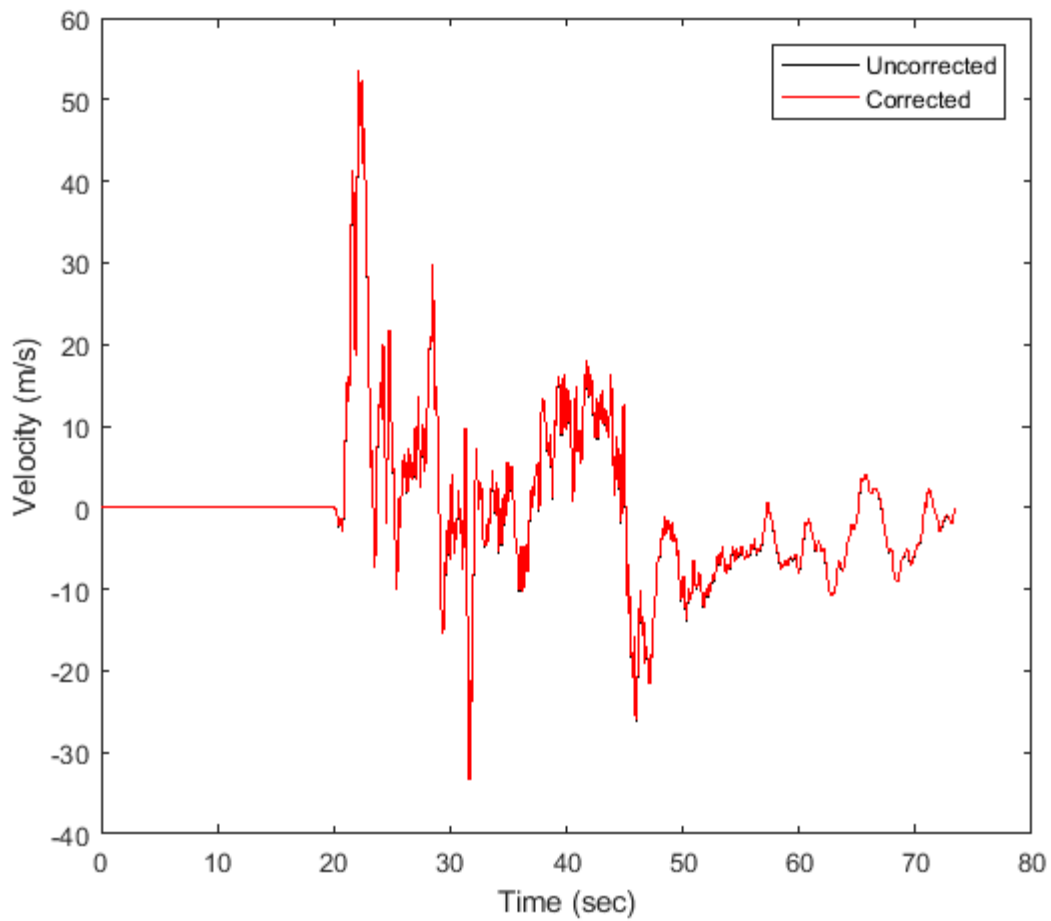
Plot corrected and uncorrected acceleration

```
figure()
plot(time,xgttl,'k','LineWidth',1)
hold on
plot(time,xgttl2,'r','LineWidth',1)
hold off
ylabel('Acceleration (m/s2)')
xlabel('Time (sec)')
legend('Uncorrected','Corrected')
```



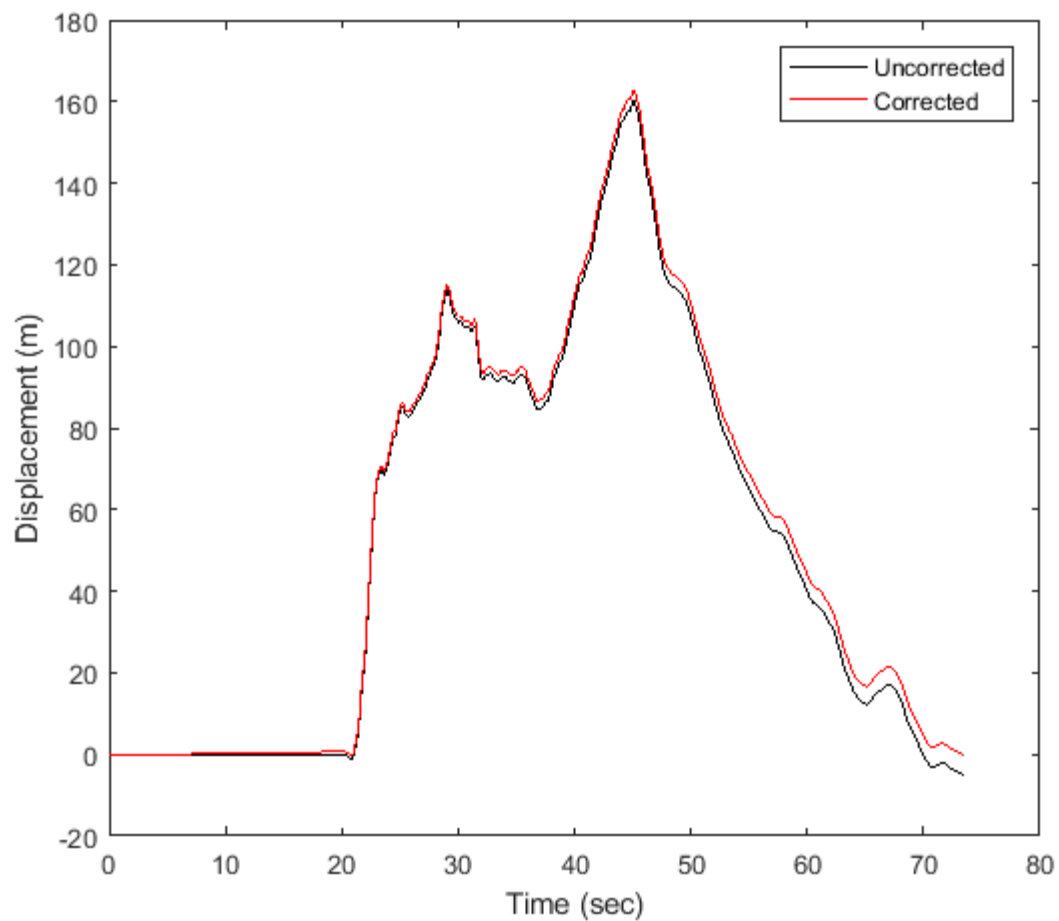
Plot corrected and uncorrected velocity

```
figure()  
plot(time,xgt1,'k','LineWidth',1)  
hold on  
plot(time,xgt2,'r','LineWidth',1)  
hold off  
ylabel('Velocity (m/s)')  
xlabel('Time (sec)')  
legend('Uncorrected','Corrected')
```



Plot corrected and uncorrected displacement

```
figure()  
plot(time,xg1,'k','LineWidth',1)  
hold on  
plot(time,xg2,'r','LineWidth',1)  
hold off  
ylabel('Displacement (m)')  
xlabel('Time (sec)')  
legend('Uncorrected','Corrected')
```



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CDReSp

Calculate constant ductility response spectra in OpenSeismoMatlab

Contents

- [Earthquake motion](#)
- [Setup parameters for CDReSp function](#)
- [Calculate spectra and pseudospectra](#)
- [Plot the spectra and pseudospectra](#)
- [Copyright](#)

Earthquake motion

For reproducibility

```
rng(0)
```

Generate earthquake data

```
dt=0.02;  
N=10;  
a=rand(N,1)-0.5;  
b=100*pi*rand(N,1);  
c=pi*(rand(N,1)-0.5);  
t=(0:dt:(100*dt))';  
xgtt=zeros(size(t));  
for i=1:N  
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));  
end
```

Setup parameters for CDReSp function

Eigenperiods

```
T=(0.04:0.04:4)';
```

Critical damping ratio

```
ksi=0.05;
```

Ductility

```
mu=2;
```

Maximum number of iterations

```
n=50;
```

Tolerance for convergence to target ductility

```
tol=0.01;
```

Post-yield stiffness factor

```
pysf=0.1;
```

Maximum ratio of the integration time step to the eigenperiod

```
dtTol=0.02;
```

Algorithm to be used for the time integration

```
AlgID= 'U0-V0-Opt' ;
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance of convergence for time integration algorithm

```
maxtol=0.01;
```

Maximum number of iterations per integration time step

```
jmax=200;
```

Infinitesimal acceleration

```
dak=eps;
```

Calculate spectra and pseudospectra

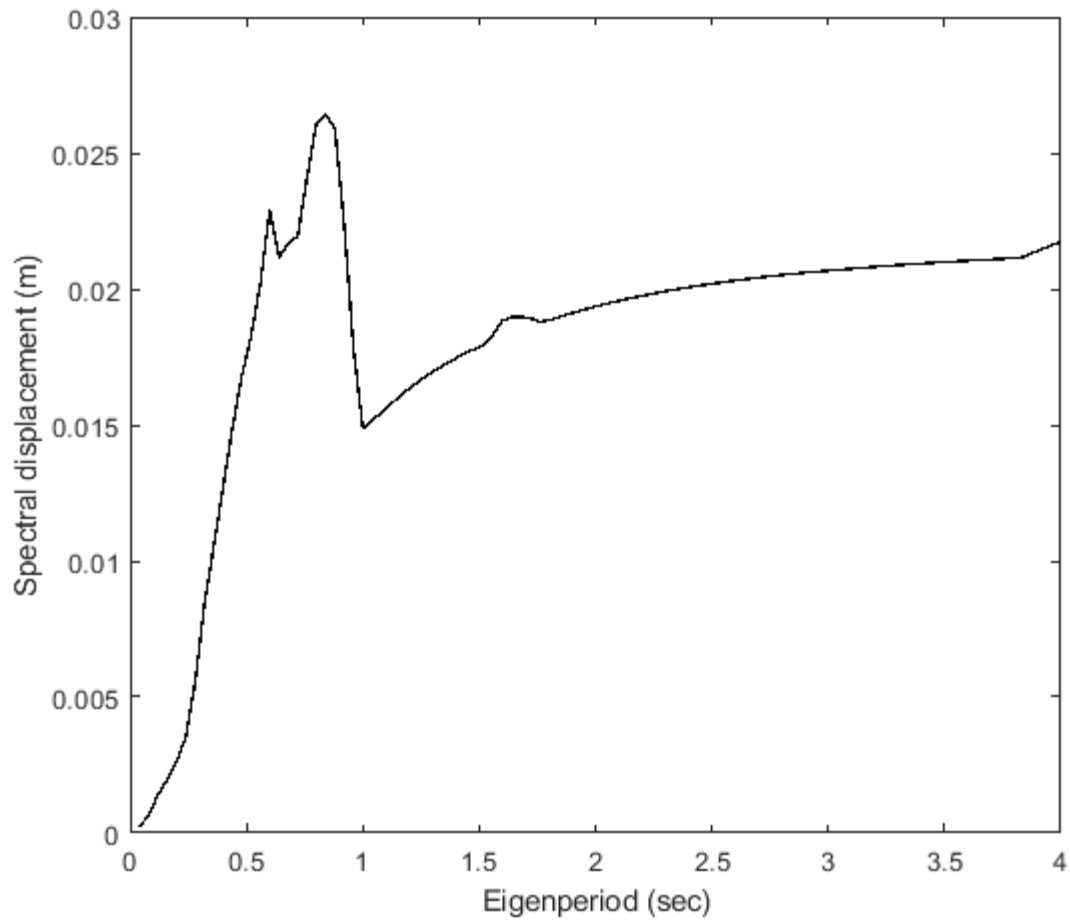
Apply CDRSp

```
[CDPSa,CDPSv,CDSd,CDSv,CDSa,fyK,muK,iterK]=CDReSp(dt,xgdt,T,ksi,...  
mu,n,tol,pysf,dtTol,AlgID,rinf,maxtol,jmax,dak);
```

Plot the spectra and pseudospectra

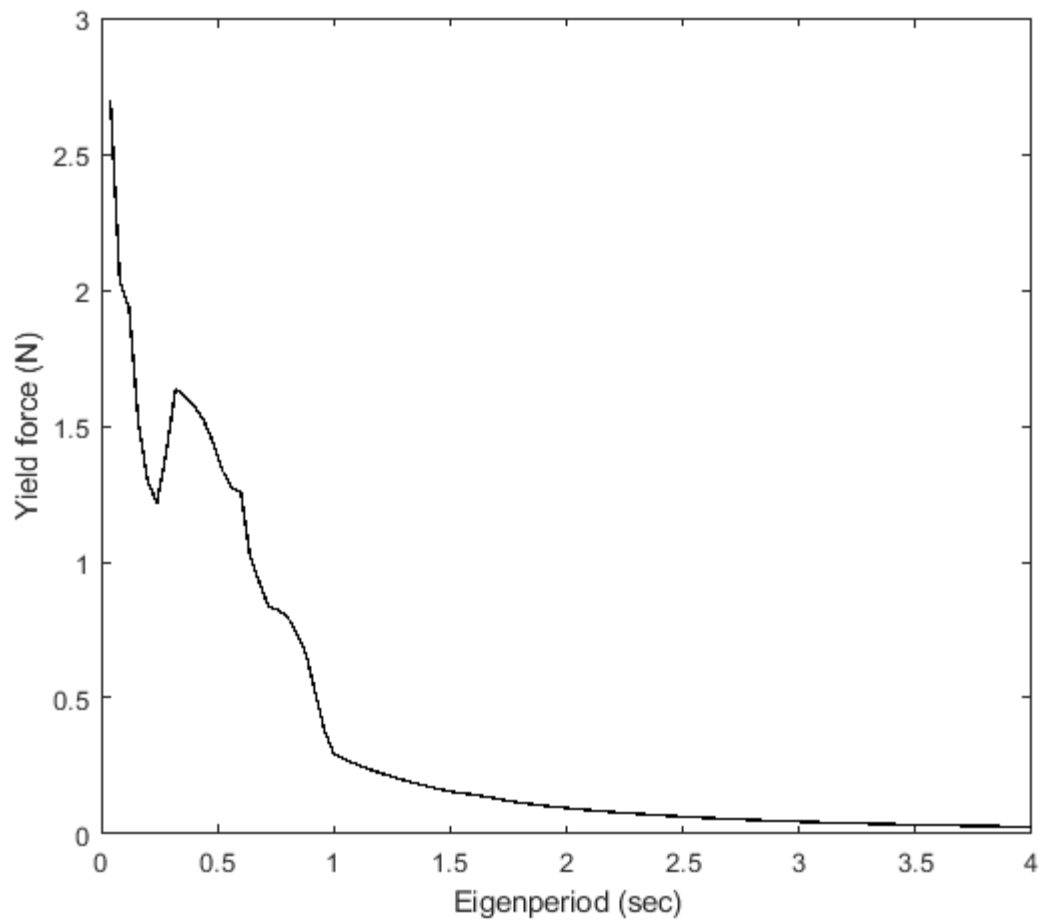
Constant ductility spectral displacement spectrum

```
figure()  
plot(T,CDSd,'k','LineWidth',1)  
ylabel('Spectral displacement (m)')  
xlabel('Eigenperiod (sec)')
```



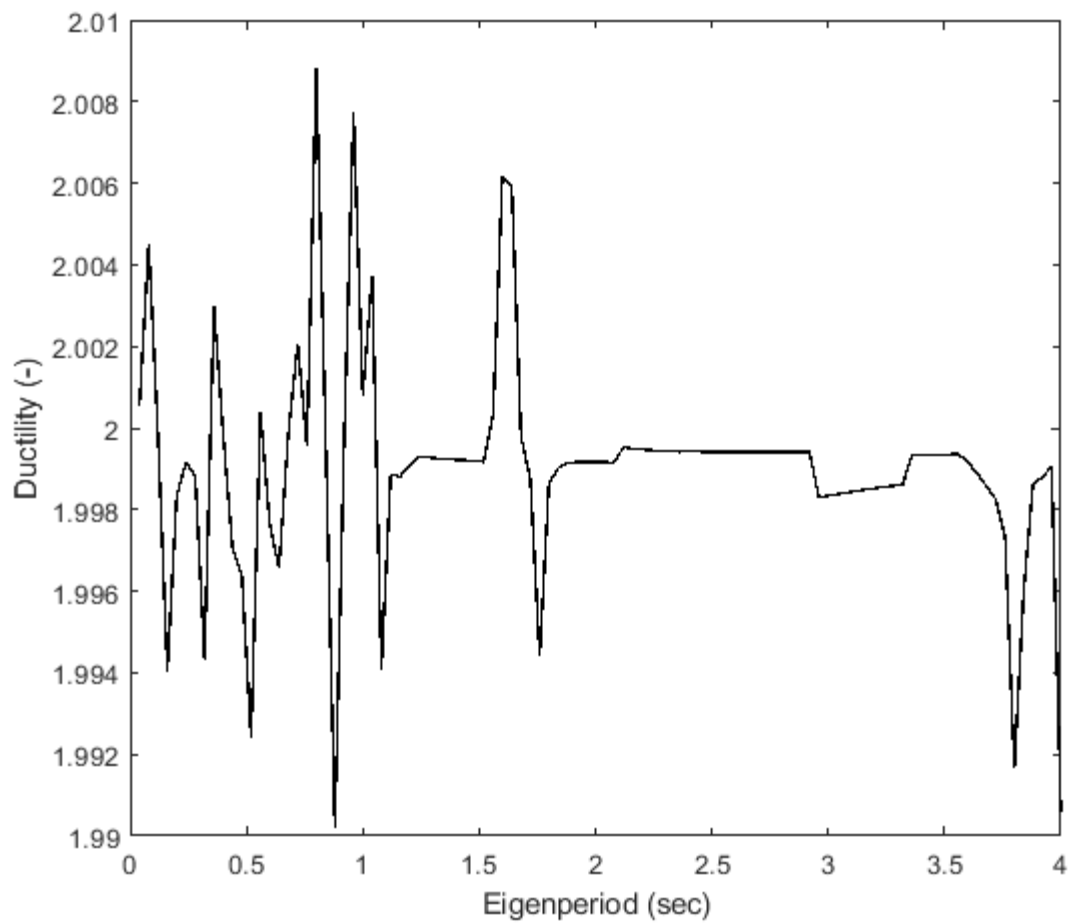
Constant ductility yield force spectrum

```
figure()  
plot(T,fyK,'k','LineWidth',1)  
ylabel('Yield force (N)')  
xlabel('Eigenperiod (sec)')
```

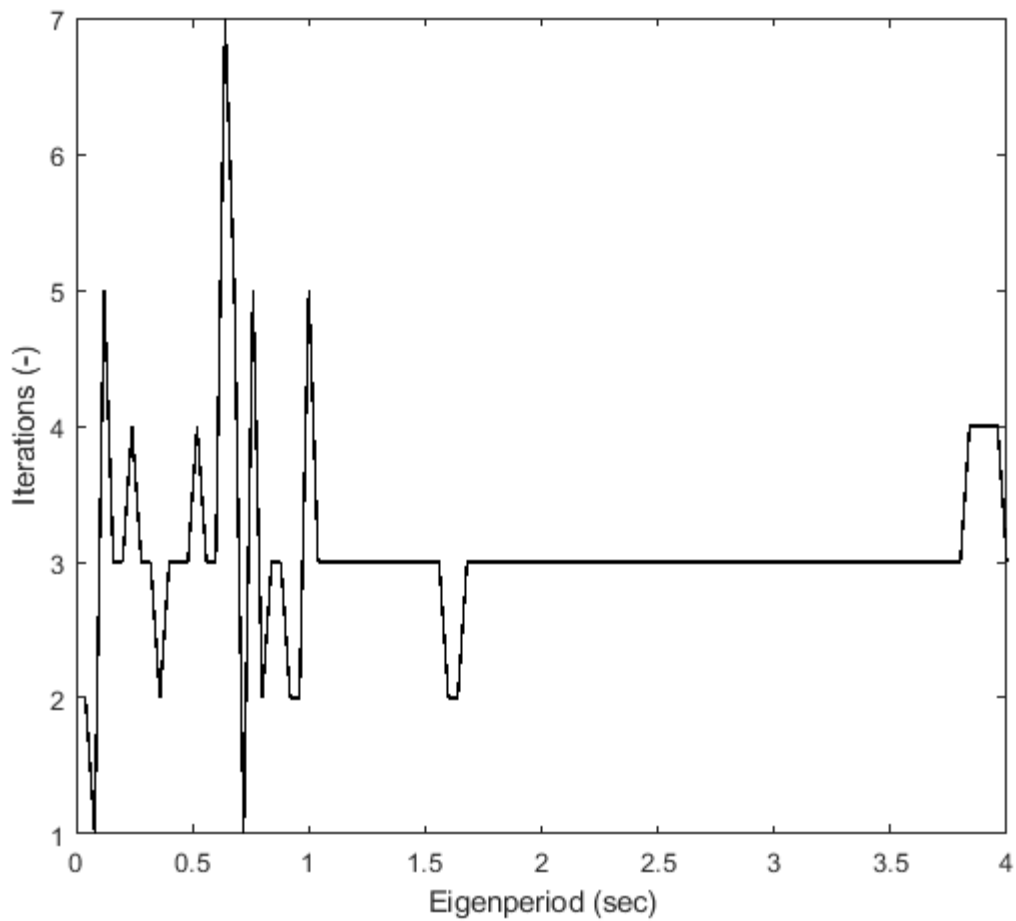
Achieved ductility

```
figure()  
plot(T,muK,'k','LineWidth',1)  
ylabel('Ductility (-)')  
xlabel('Eigenperiod (sec)')
```



Iterations

```
figure()  
plot(T,iterK,'k','LineWidth',1)  
ylabel('Iterations (-)')  
xlabel('Eigenperiod (sec)')
```



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Constant ductility response spectra

Generate the constant ductility response spectra and associated results of an earthquake suite using OpenSeismoMatlab.

Contents

- [Input](#)
- [Calculation](#)
- [Output](#)
- [Copyright](#)

Input

earthquake motions

```
eqmotions={'Imperial Valley'; % Imperial valley 1979
           'Kocaeli';
           'Loma Prieta';
           'Northridge';
           'San Fernando';
           'Spitak';
           'Cape Mendocino';
           'ChiChi';
           'El Centro'; % Imperial valley 1940
           'Hollister';
           'Kobe'};
```

Set the eigenperiod range for which the response spectra will be calculated.

```
Tspectra=(0.08:0.08:4)';
```

Set critical damping ratio of the response spectra to be calculated.

```
ksi=0.05;
```

Set the target ductility (not used here)

```
mu=2;
```

Set the postyield stiffness factor for each earthquake

```
p=[0.02;0.01;0.02;0.01;0.01;0.01;0.02;0.01;0.01;0.01;0.01];
```

Extract nonlinear response spectra

```
sw='cgs';
```

Calculation

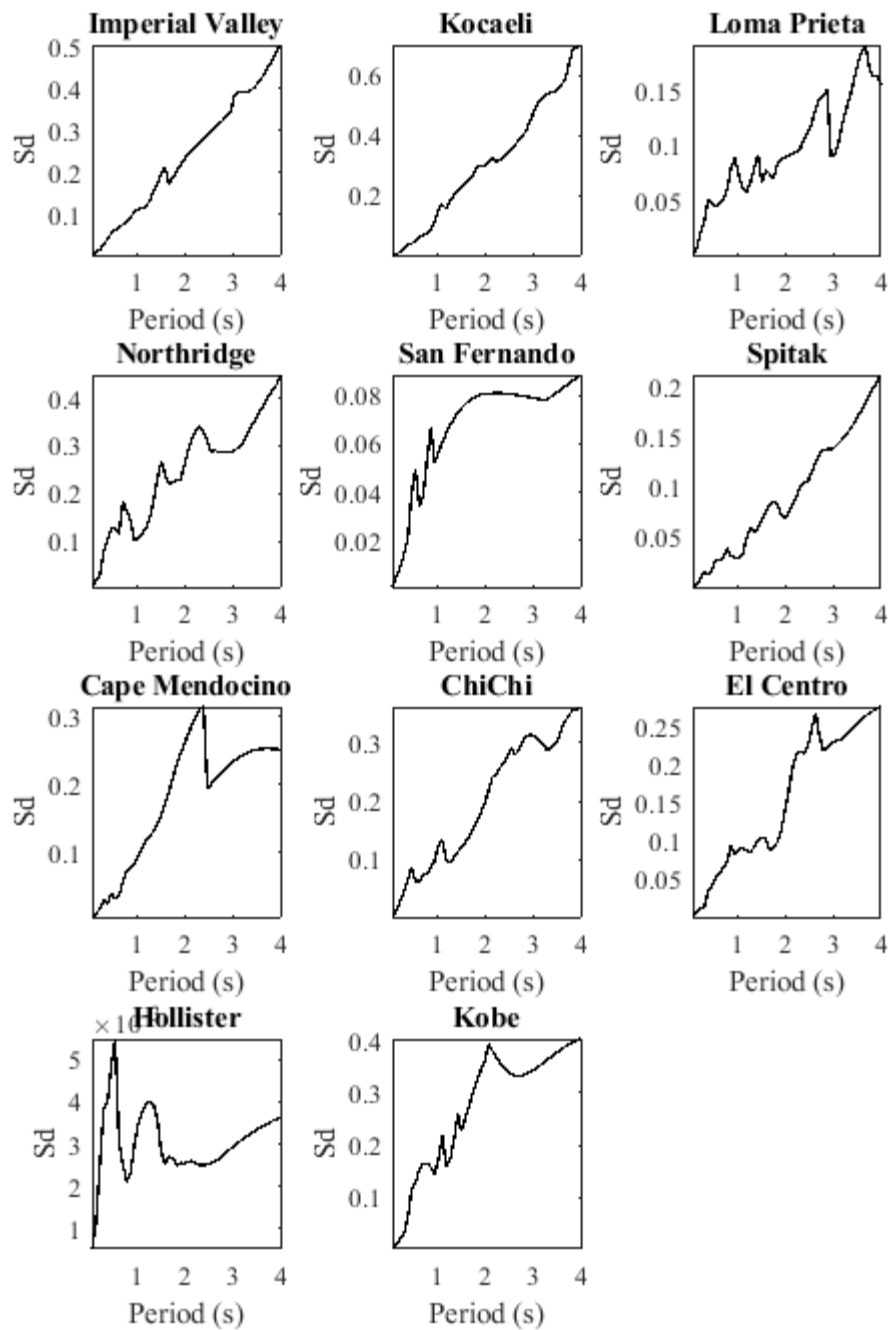
Initialize CDRS

```
CDRS=cell(numel(eqmotions),1);
% Calculation of peak values
for i=1:numel(eqmotions)
    % earthquake
    data=load([eqmotions{i},'.dat']);
    t=data(:,1);
    dt=t(2)-t(1);
    xgtt=data(:,2);
    S=OpenSeismoMatlab(dt,xgtt,sw,Tspectra,ksi,mu,p(i));
    CDRS{i}=[S.Period,S.CDSd,S.CDSv,S.CDPSa,S.fyK,S.muK,S.iterK];
end
```

Output

Plot constant ductility spectral displacement

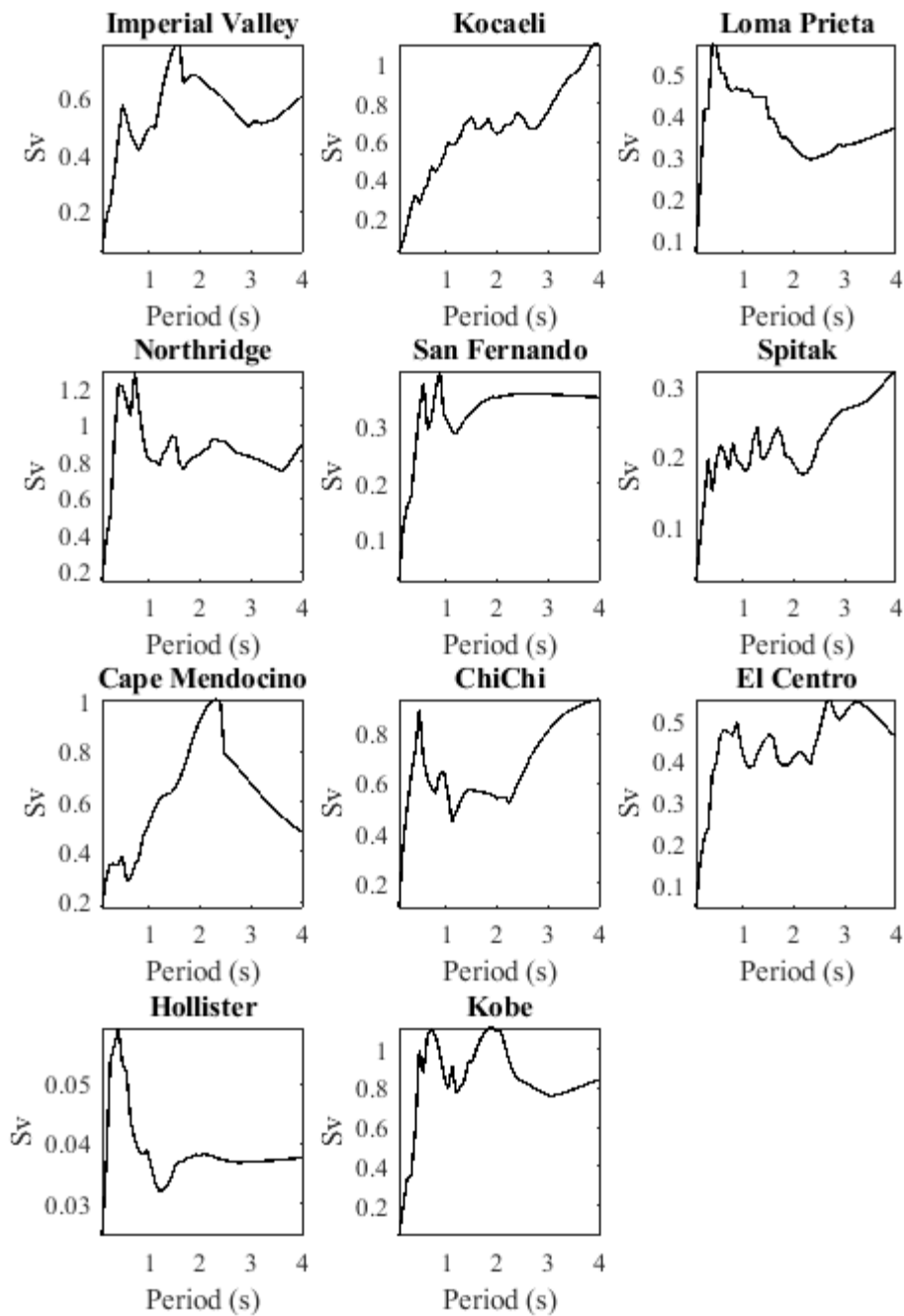
```
Fig1 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(CDRS{i}(:,1),CDRS{i}(:,2),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('Sd','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
    axis tight
end
```



Plot constant ductility spectral velocity

```
Fig2 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(CDRS{i}(:,1),CDRS{i}(:,3),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('Sv','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
```

```
axis tight
end
```



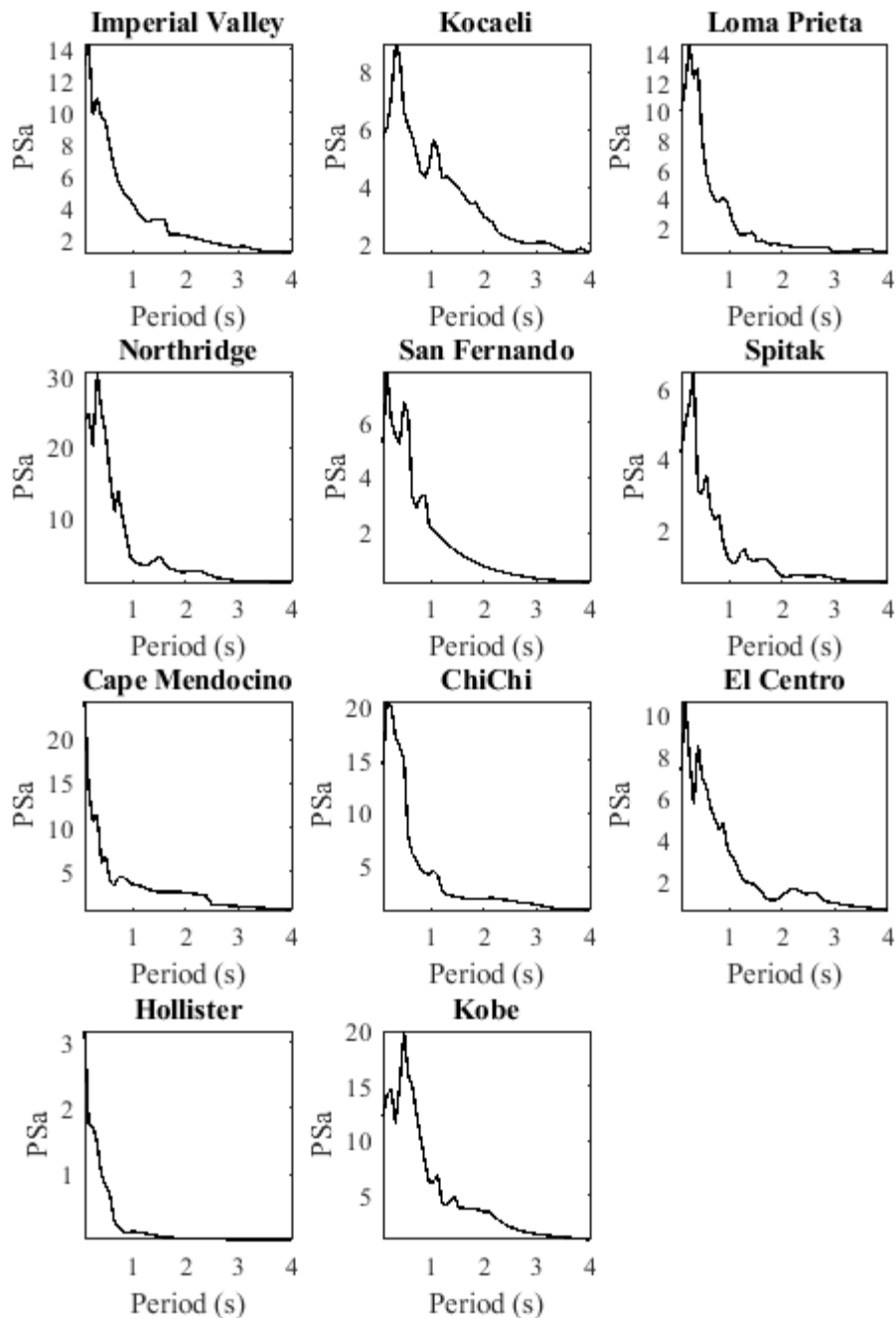
Plot constant ductility spectral acceleration

```
Fig3 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(CDRS{i}(:,1),CDRS{i}(:,4),'k','LineWidth',1);
```

```

set(gca,'FontName','Times New Roman')
title(egmotions{i},'FontName','Times New Roman')
ylabel('PSa','FontName','Times New Roman')
xlabel('Period (s)','FontName','Times New Roman')
axis tight
end

```



Plot constant ductility spectral yield limit

```

Fig4 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);

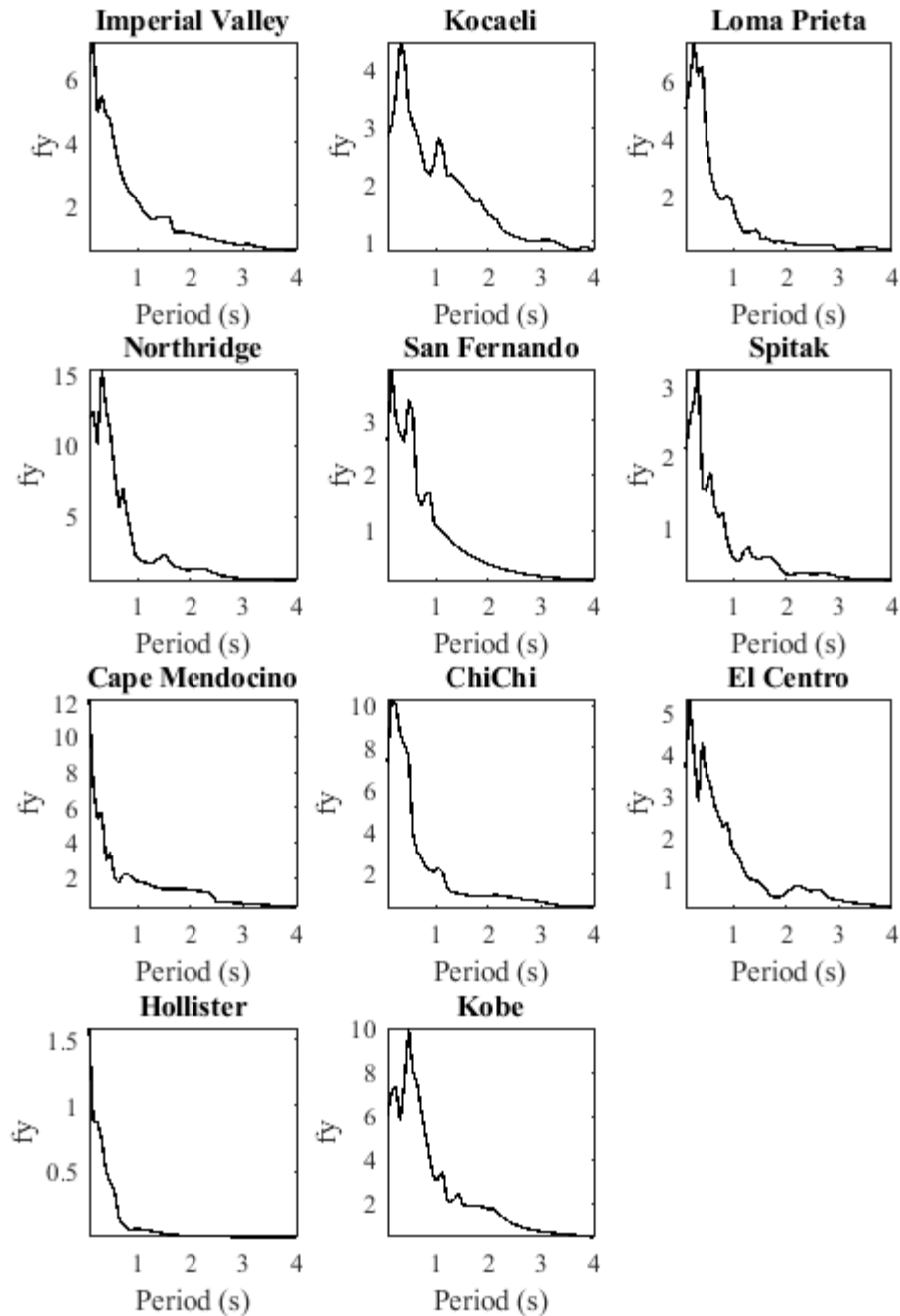
```



```

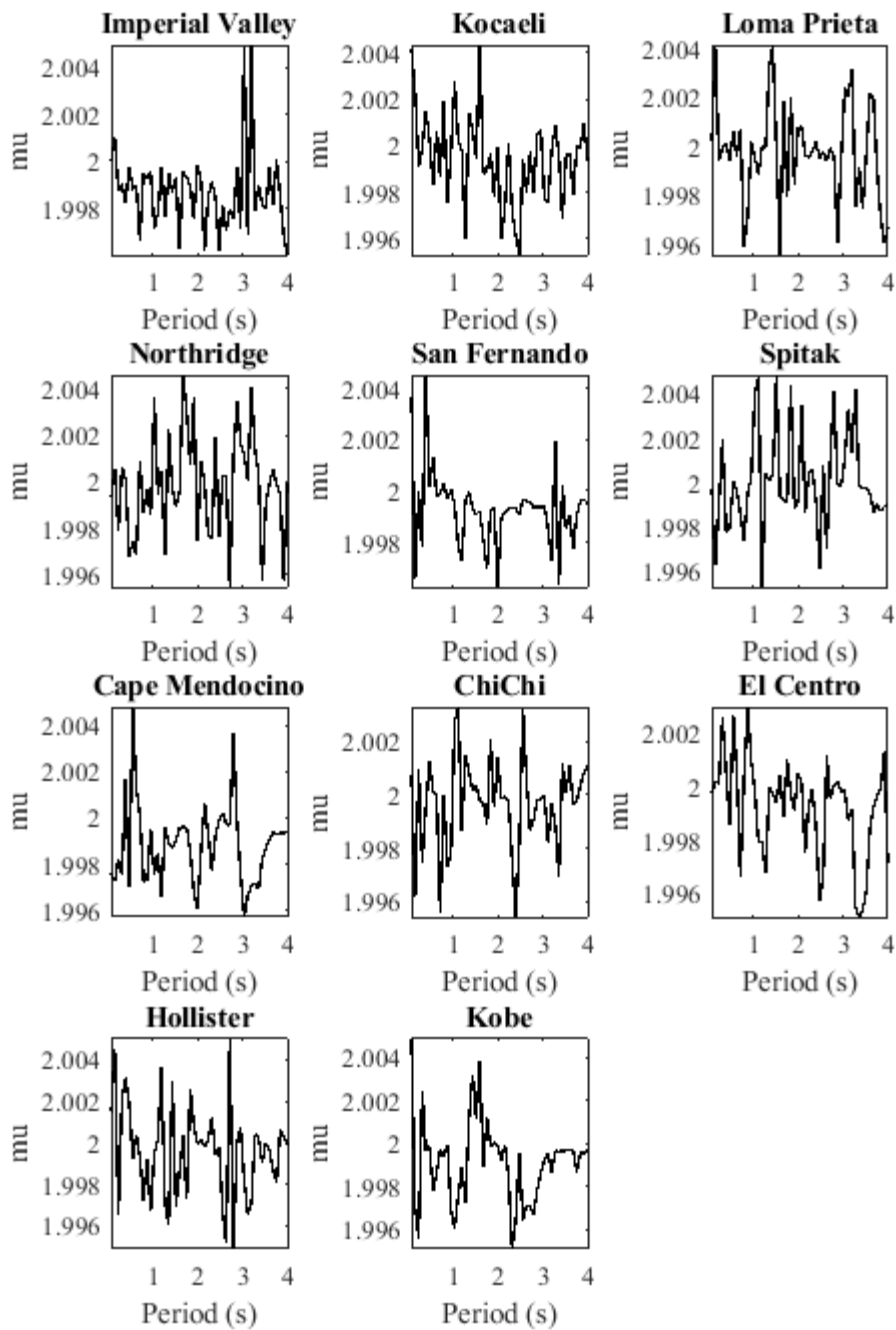
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(CDRS{i}(:,1),CDRS{i}(:,5),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('fy','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
    axis tight
end

```



Plot constant ductility spectral achieved ductility

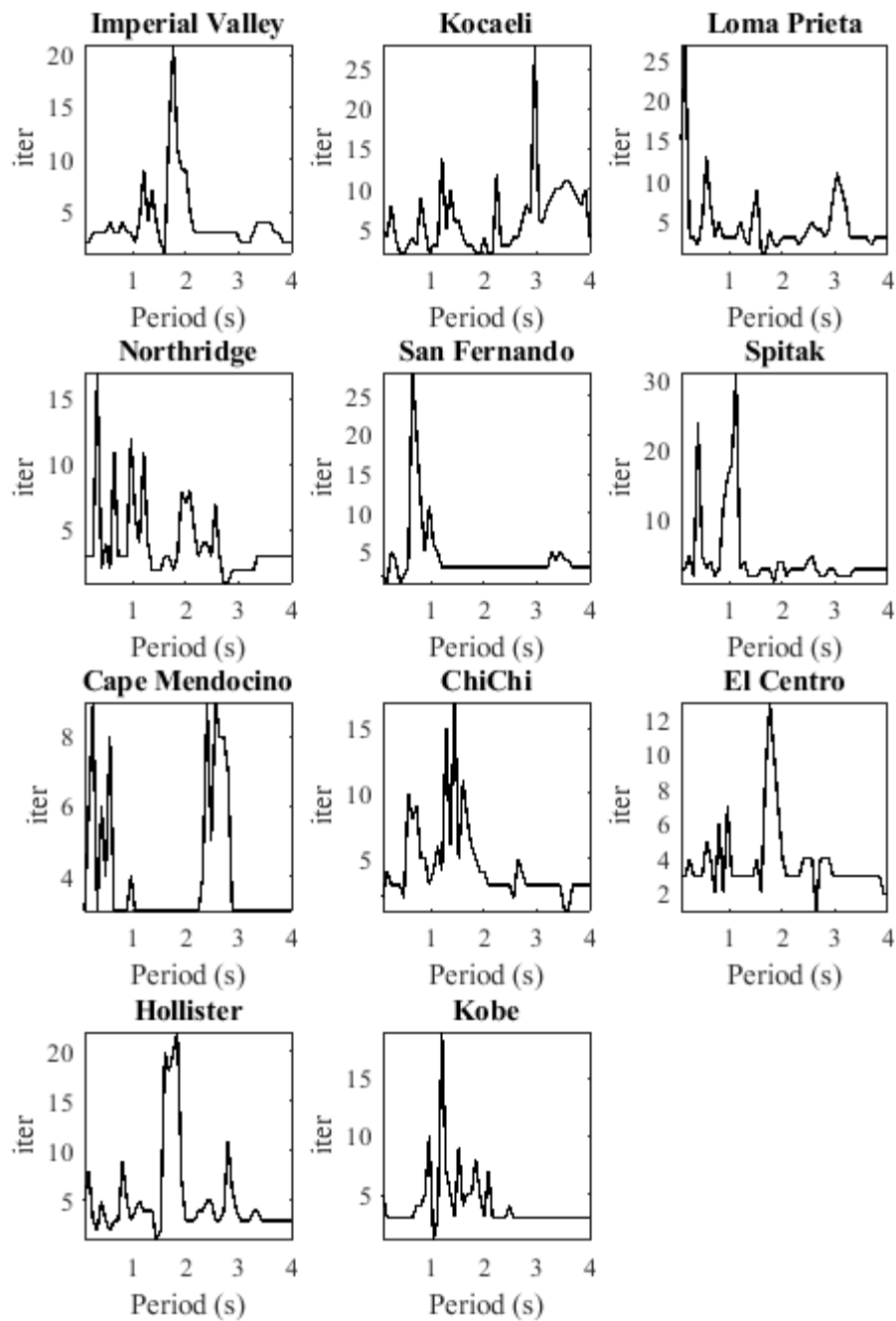
```
Fig5 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(CDRS{i}(:,1),CDRS{i}(:,6),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('mu','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
    axis tight
end
```



Plot constant ductility spectral number of iterations needed for convergence

```
Fig6 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(CDRS{i}(:,1),CDRS{i}(:,7),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('iter','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
```

```
axis tight
end
```



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Fourier spectra

Generate the Fourier spectra of an earthquake suite using OpenSeismoMatlab

Contents

- [Input](#)
- [Extract fourier spectra](#)
- [Output](#)
- [Copyright](#)

Input

earthquake motions

```
eqmotions={'Imperial Valley'; % Imperial valley 1979
           'Kocaeli';
           'Loma Prieta';
           'Northridge';
           'San Fernando';
           'Spitak';
           'Cape Mendocino';
           'ChiChi';
           'El Centro'; % Imperial valley 1940
           'Hollister';
           'Kobe'};
```

Switch

```
sw='fs';
```

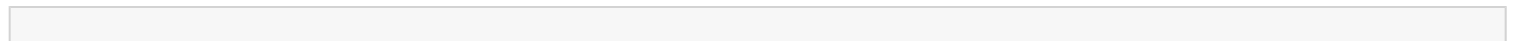
Extract fourier spectra

Initialize cell of Fourier spectra

```
Fourier=cell(numel(eqmotions),1);
% Calculation of Fourier spectra
for i=1:numel(eqmotions)
    % earthquake
    data=load([eqmotions{i},'.dat']);
    t=data(:,1);
    dt=t(2)-t(1);
    xgtt=data(:,2);
    S=OpenSeismoMatlab(dt,xgtt,sw);
    Fourier{i}=[S.freq,S.FAS];
end
```

Output

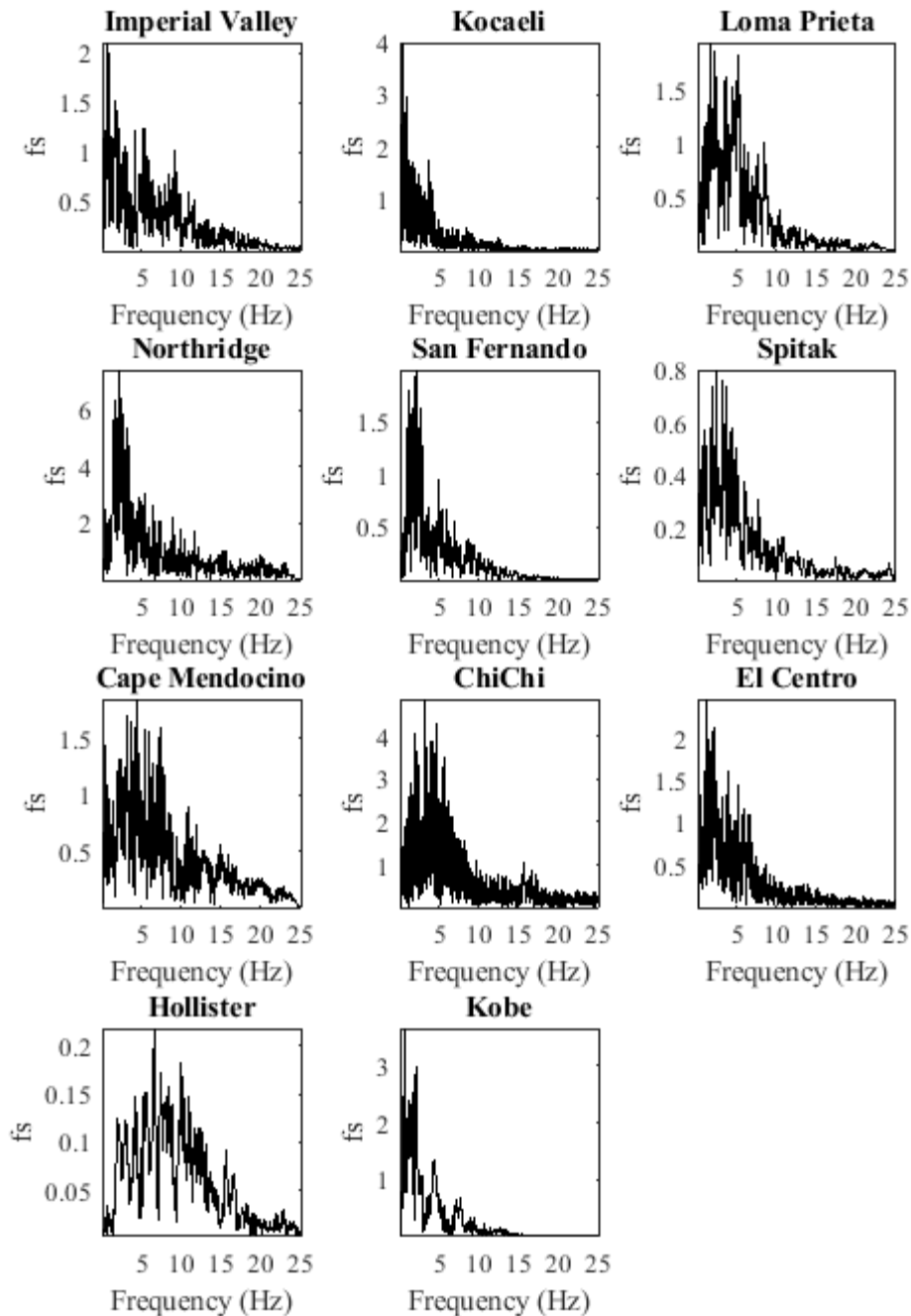
Plot Fourier amplitude



```

Fig1 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(Fourier{i}(:,1),Fourier{i}(:,2),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('fs','FontName','Times New Roman')
    xlabel('Frequency (Hz)','FontName','Times New Roman')
    axis tight
end

```



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-

Published with MATLAB® R2017b

General demonstration of the OpenSeismoMatlab capabilities

This is to demonstrate the capabilities of OpenSeismoMatlab and also to verify that OpenSeismoMatlab works properly for all of its possible options and types of application, and yields meaningful results. **All** capabilities of OpenSeismoMatlab are tested in this example

Contents

- [Load earthquake data](#)
- [Time histories without baseline correction](#)
- [Time histories with baseline correction](#)
- [Resample acceleration time history from 0.02 sec to 0.01 sec.](#)
- [PGA](#)
- [PGV](#)
- [PGD](#)
- [Total cumulative energy, Arias intensity and significant duration](#)
- [Linear elastic response spectra and pseudospectra](#)
- [Constant ductility response spectra and pseudospectra](#)
- [Fourier amplitude spectrum and mean period](#)
- [High pass Butterworth filter](#)
- [Low pass Butterworth filter](#)
- [Incremental dynamic analysis](#)
- [Copyright](#)

Load earthquake data

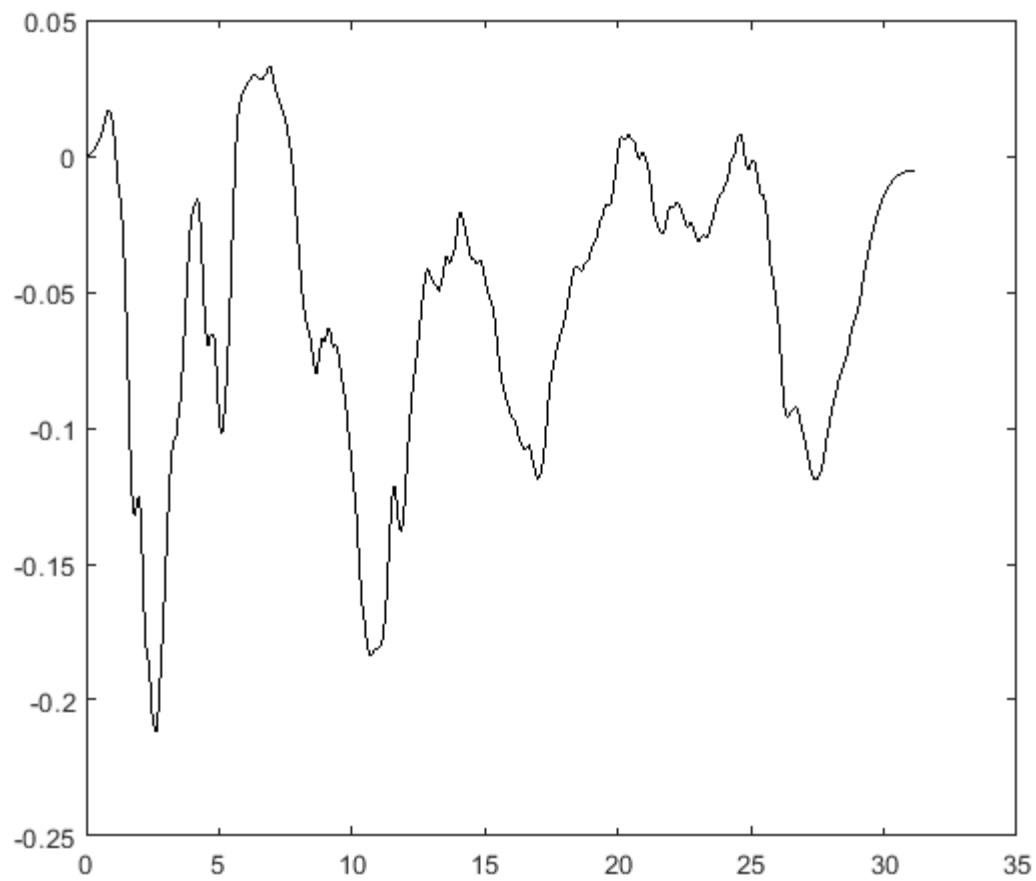
Earthquake acceleration time history of the El Centro earthquake will be used (El Centro, 1940, El Centro Terminal Substation Building)

```
fid=fopen('elcentro.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtt=text{1,2};
```

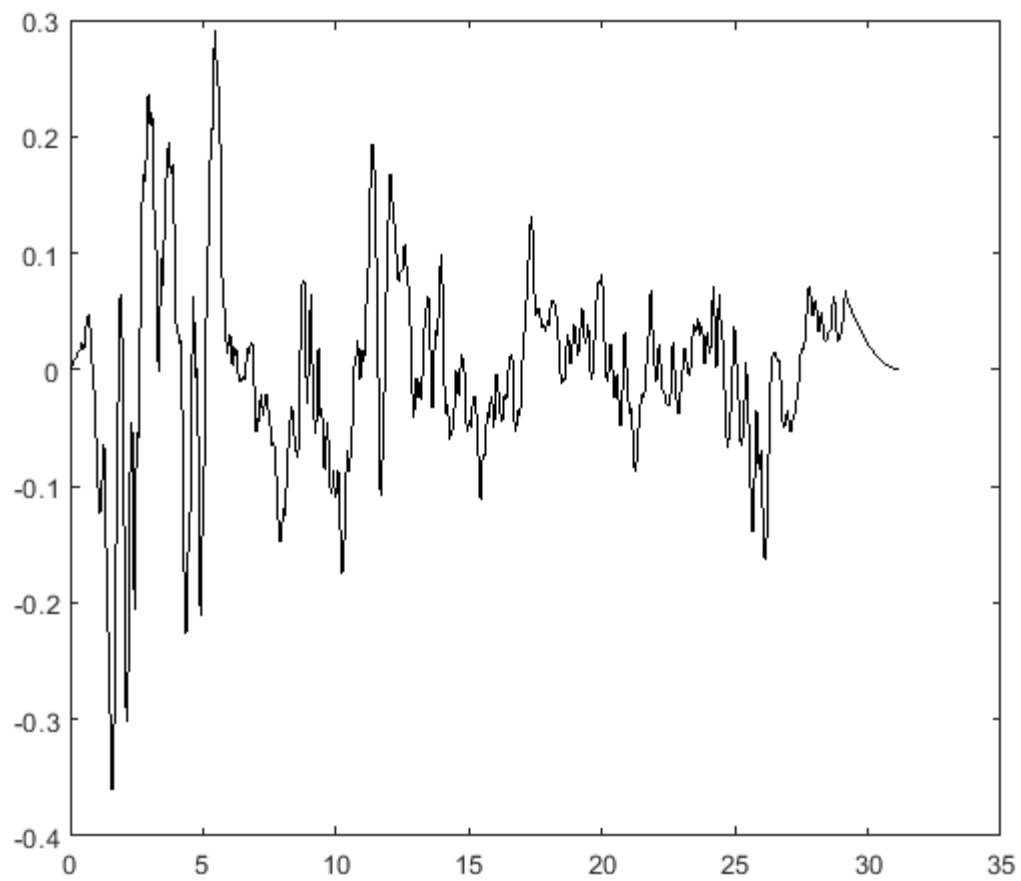
Time histories without baseline correction

```
sw='timehist';
baselineSw=false;
S1=OpenSeismoMatlab(dt,xgtt,sw,baselineSw);
```

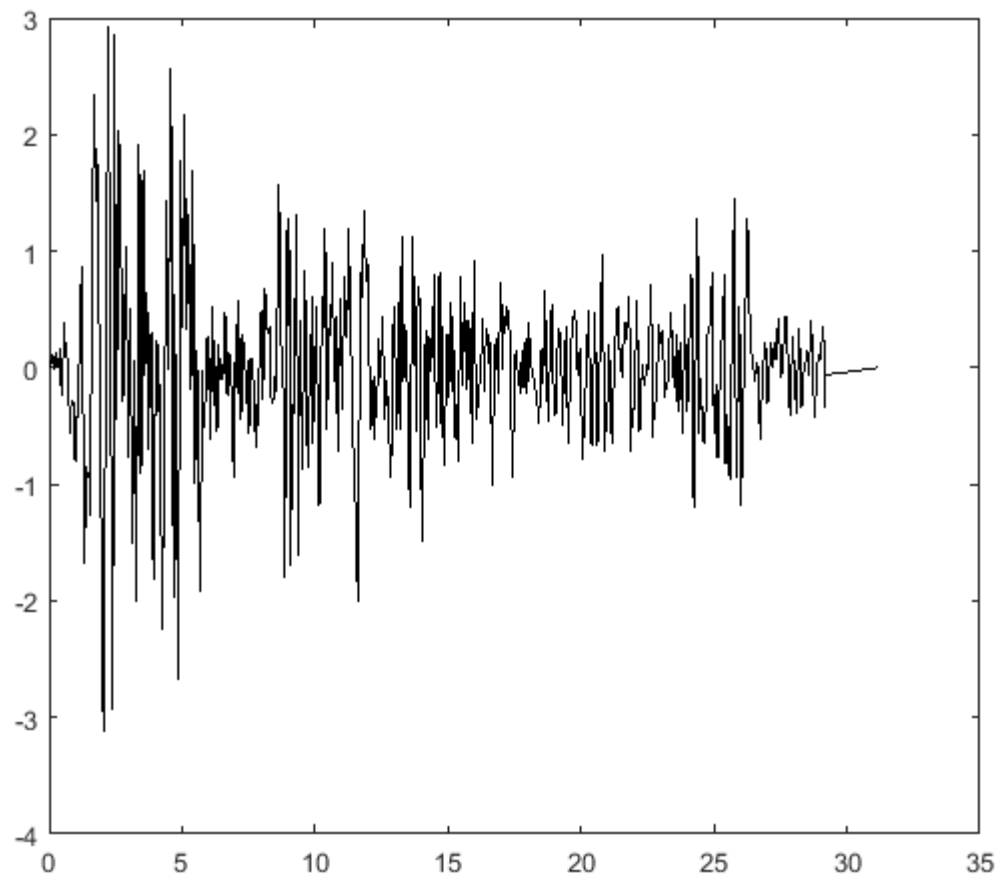
```
figure(1)
plot(S1.time,S1.disp,'k','LineWidth',1)
```



```
figure(2)
plot(S1.time,S1.vel,'k','LineWidth',1)
```



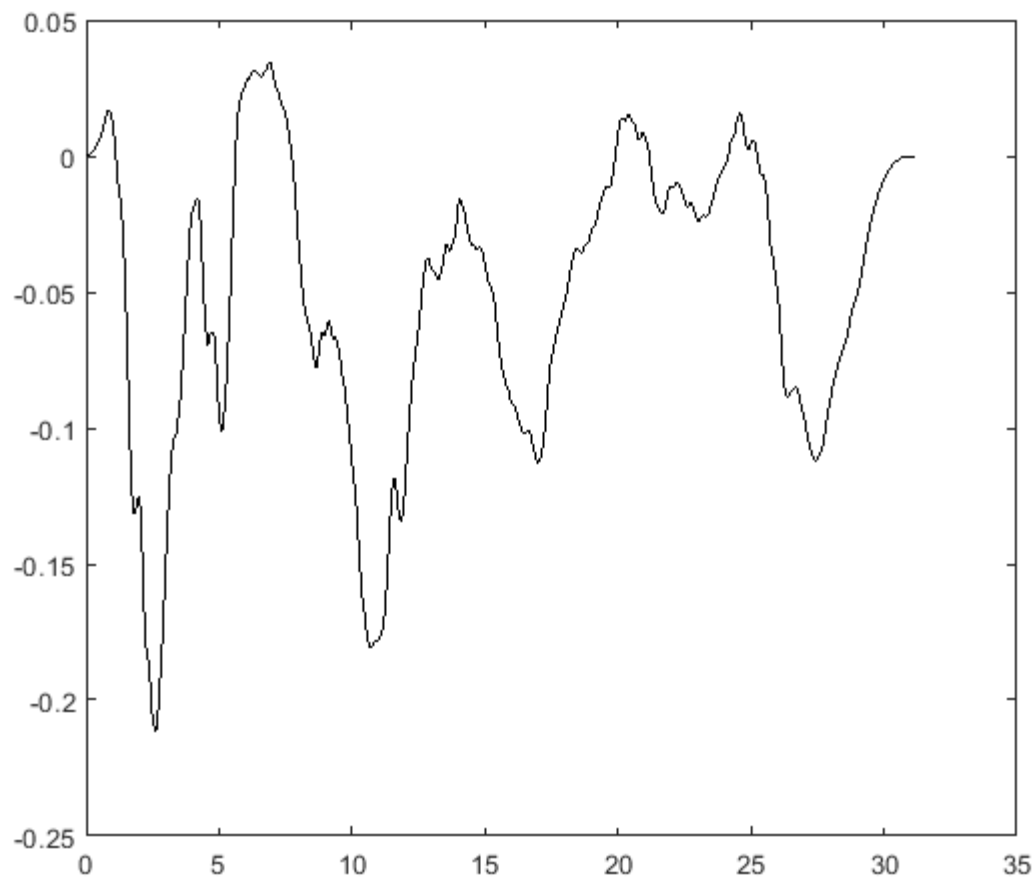
```
figure(3)
plot(S1.time,S1.acc,'k','LineWidth',1)
```



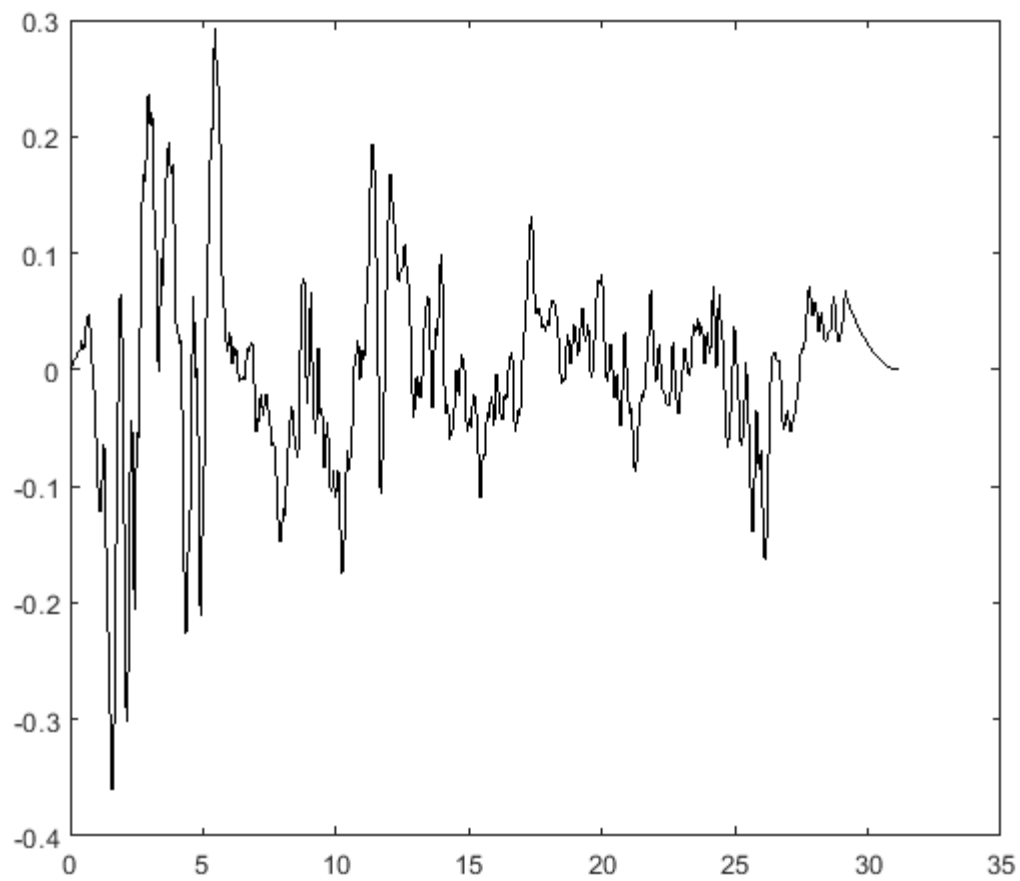
Time histories with baseline correction

```
sw='timehist';  
baselineSw=true;  
S2=OpenSeismoMatlab(dt,xgtt,sw,baselineSw);
```

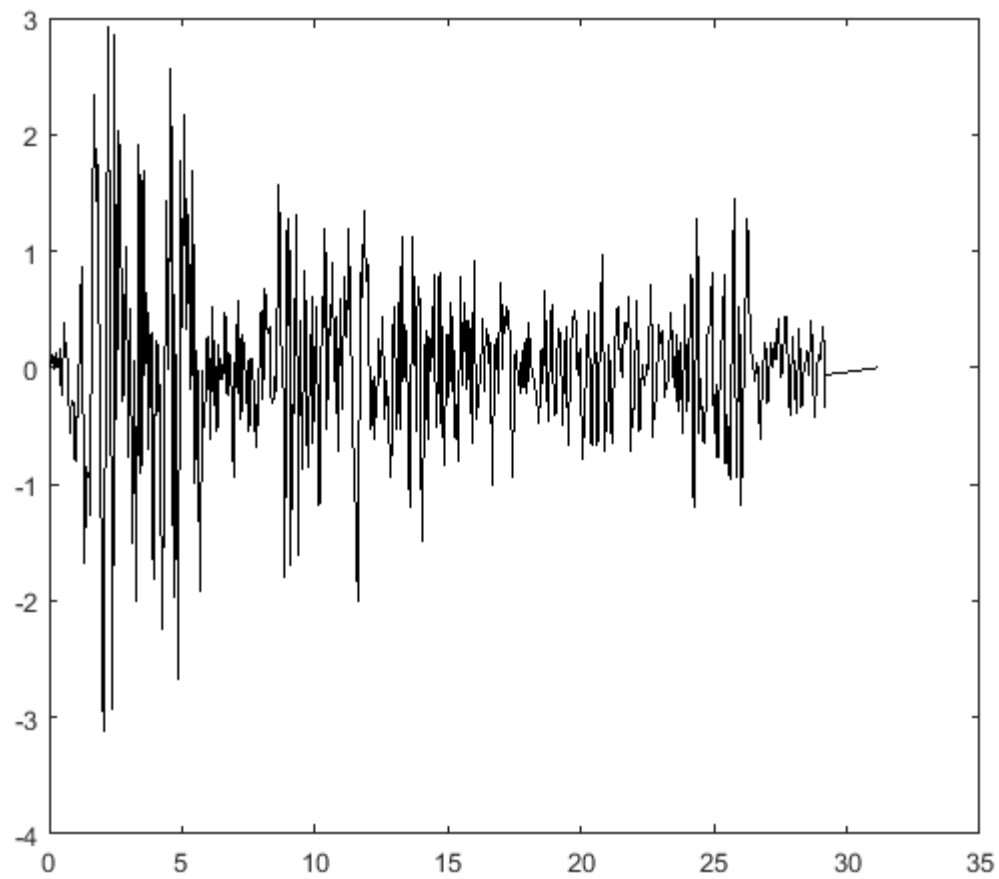
```
figure(4)  
plot(S2.time,S2.disp,'k','LineWidth',1)
```



```
figure(5)
plot(S2.time,S2.vel,'k','LineWidth',1)
```



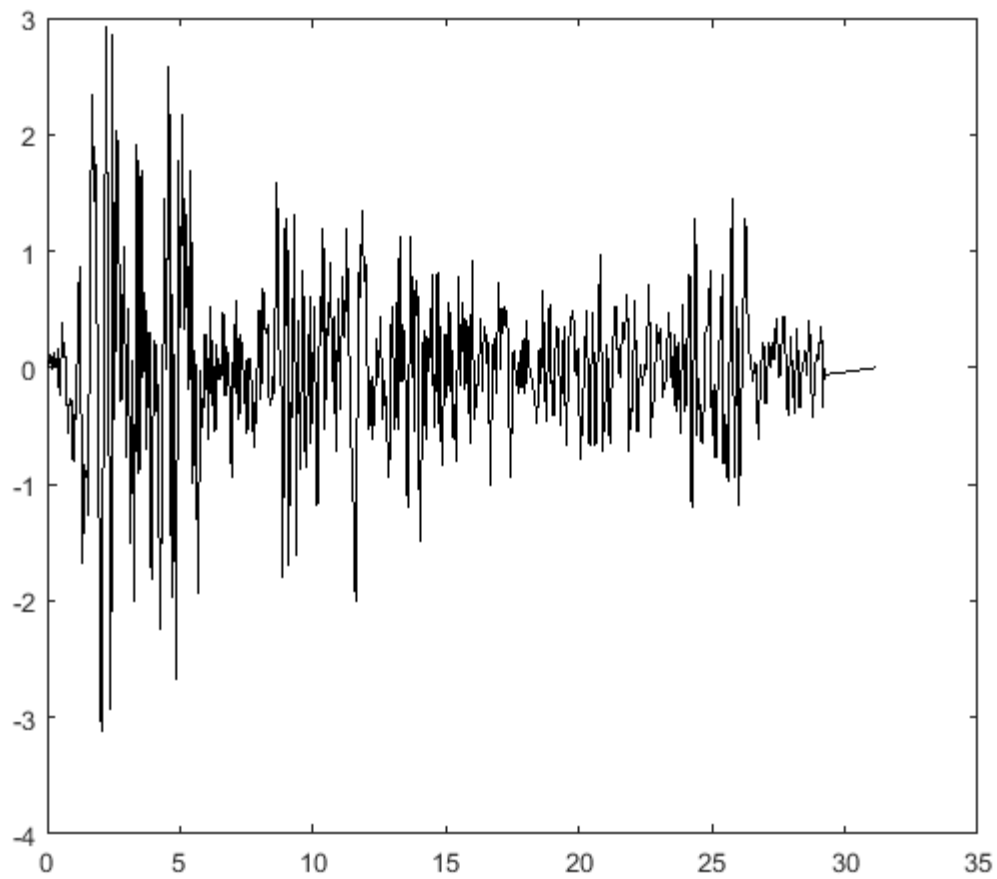
```
figure(6)
plot(S2.time,S2.acc,'k','LineWidth',1)
```



Resample acceleration time history from 0.02 sec to 0.01 sec.

```
sw='resample';  
dti=0.01;  
S3=OpenSeismoMatlab(dt,xgtd,sw,dti);
```

```
figure(7)  
plot(S3.time,S3.acc,'k','LineWidth',1)
```



PGA

```
sw='pga' ;  
S4=OpenSeismoMatlab(dt,xgtt,sw);
```

```
S4.PGA
```

```
ans =  
  
3.127624200000000
```

PGV

```
sw='pgv' ;  
S5=OpenSeismoMatlab(dt,xgtt,sw);
```

```
S5.PGV
```

```
ans =
```


0.360920691000000

PGD

```
sw='pgd';  
S6=OpenSeismoMatlab(dt,xgtt,sw);
```

S6.PGD

ans =

0.211893410160001

Total cumulative energy, Arias intensity and significant duration

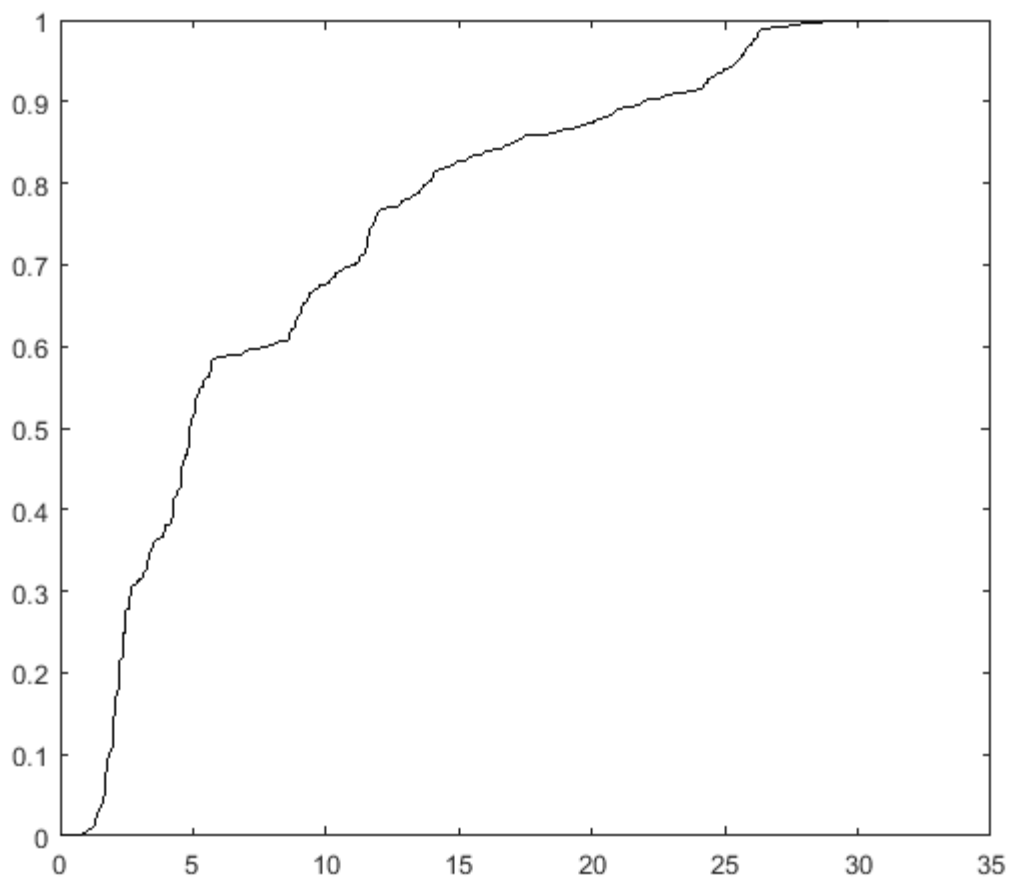
```
sw='arias';  
S7=OpenSeismoMatlab(dt,xgtt,sw);
```

S7.Ecum

ans =

11.251388628141965

```
figure(8)  
plot(S7.time,S7.EcumTH,'k','LineWidth',1)
```



S7.t_5_95

ans =

1.6800000000000000 25.500000000000000

S7.Td_5_95

ans =

23.840000000000000

S7.t_5_75

ans =

1.6800000000000000 11.779999999999999

```
S7.Td_5_75
```

```
ans =
```

```
10.119999999999999
```

```
S7.arias
```

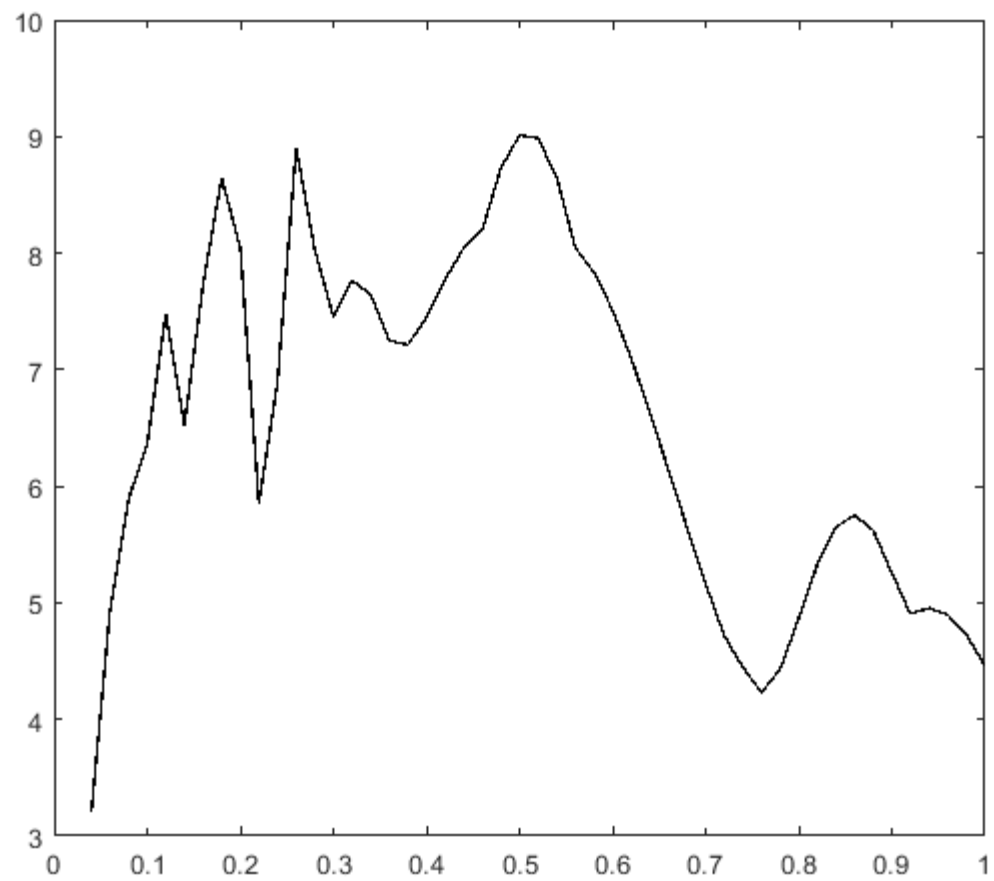
```
ans =
```

```
1.645606908074047
```

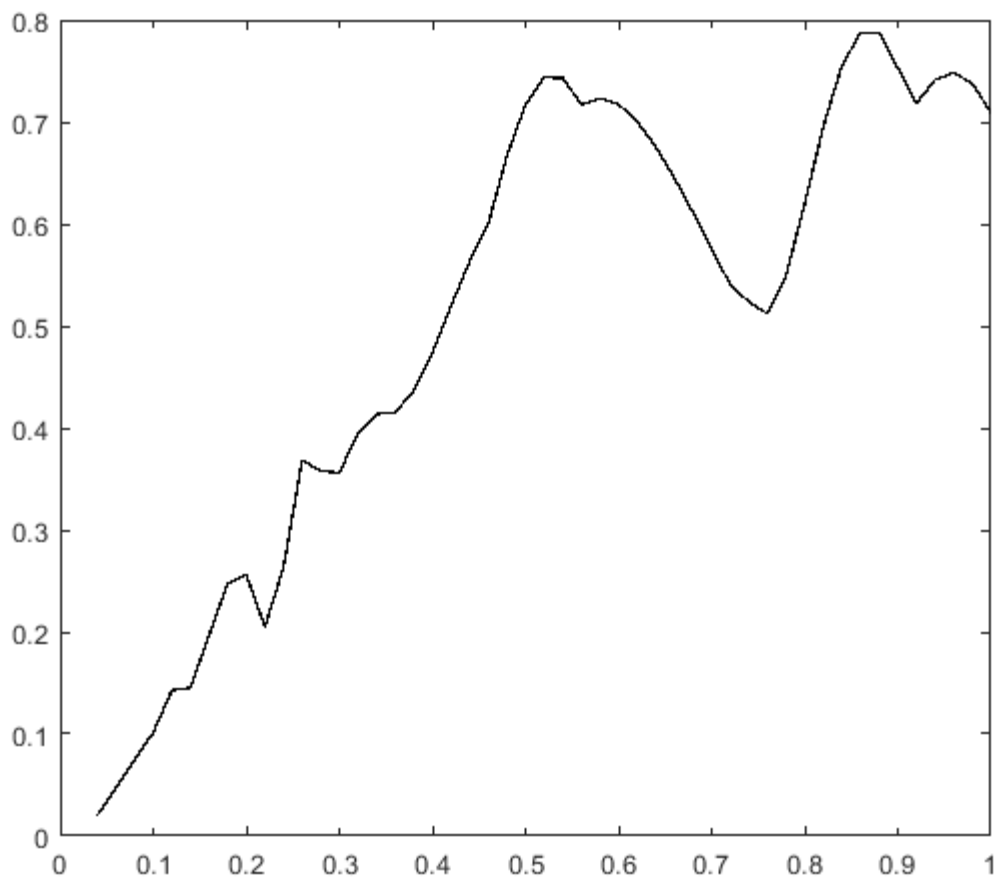
Linear elastic response spectra and pseudospectra

```
sw='es';  
ksi=0.05;  
T=0.04:0.02:1;  
S8=OpenSeismoMatlab(dt,xgtd,sw,T,ksi);
```

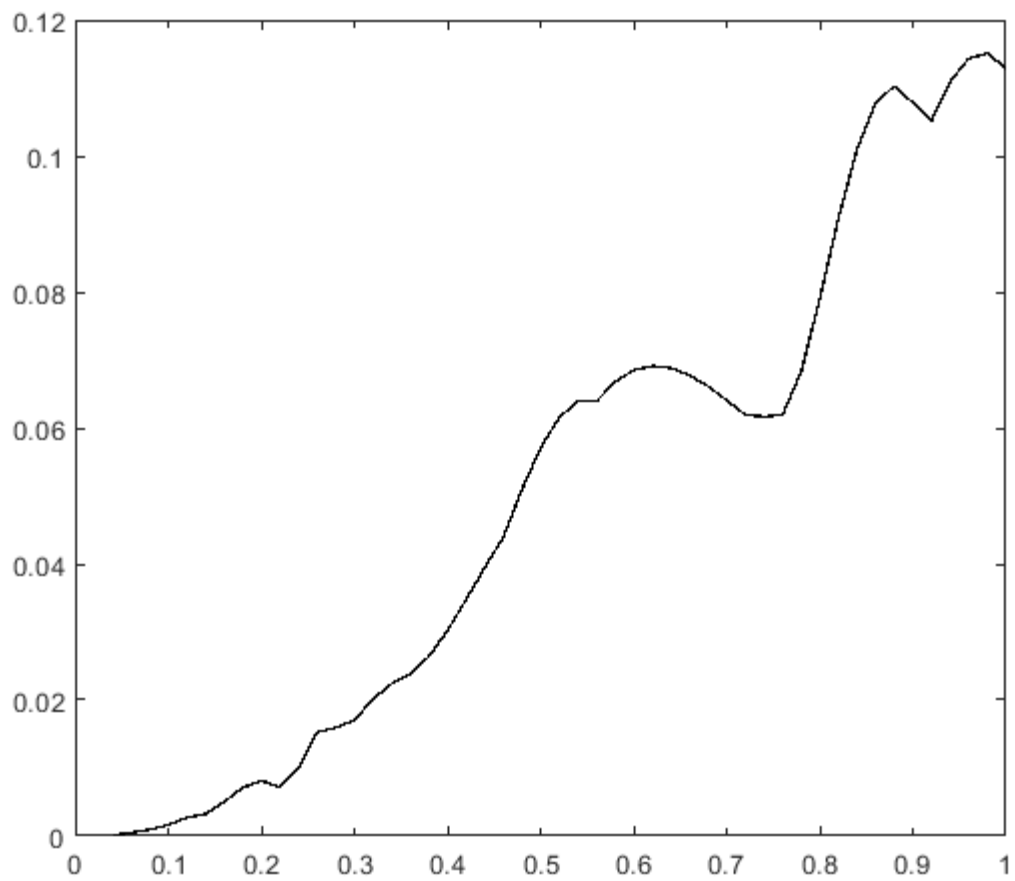
```
figure(9)  
plot(S8.Period,S8.PSa,'k','LineWidth',1)
```



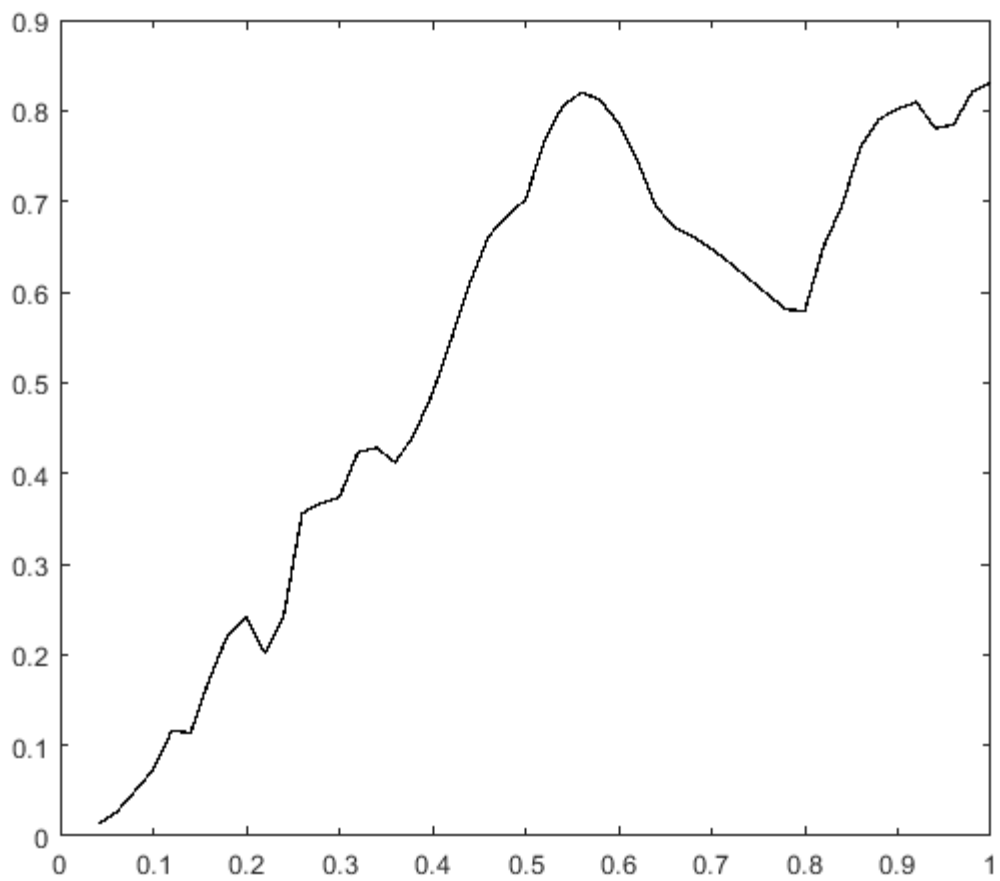
```
figure(10)
plot(S8.Period,S8.PSv,'k','LineWidth',1)
```



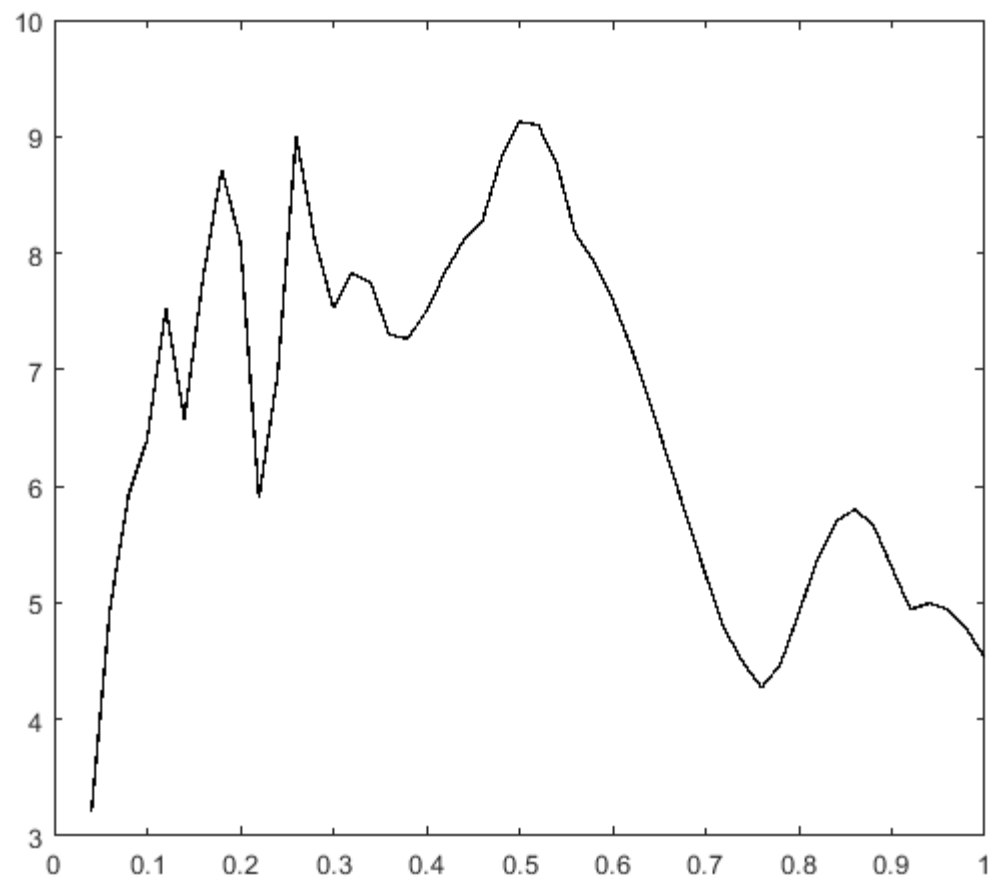
```
figure(11)
plot(S8.Period,S8.Sd,'k','LineWidth',1)
```



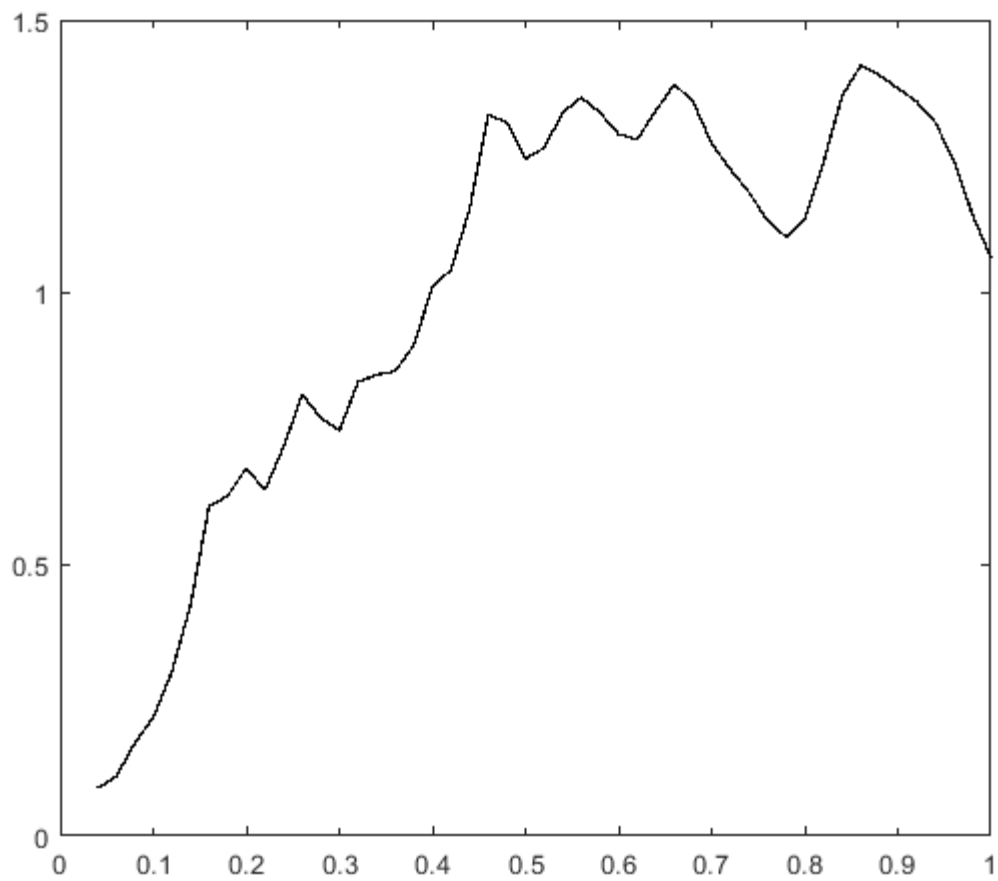
```
figure(12)
plot(S8.Period,S8.Sv,'k','LineWidth',1)
```



```
figure(13)
plot(S8.Period,S8.Sa,'k','LineWidth',1)
```

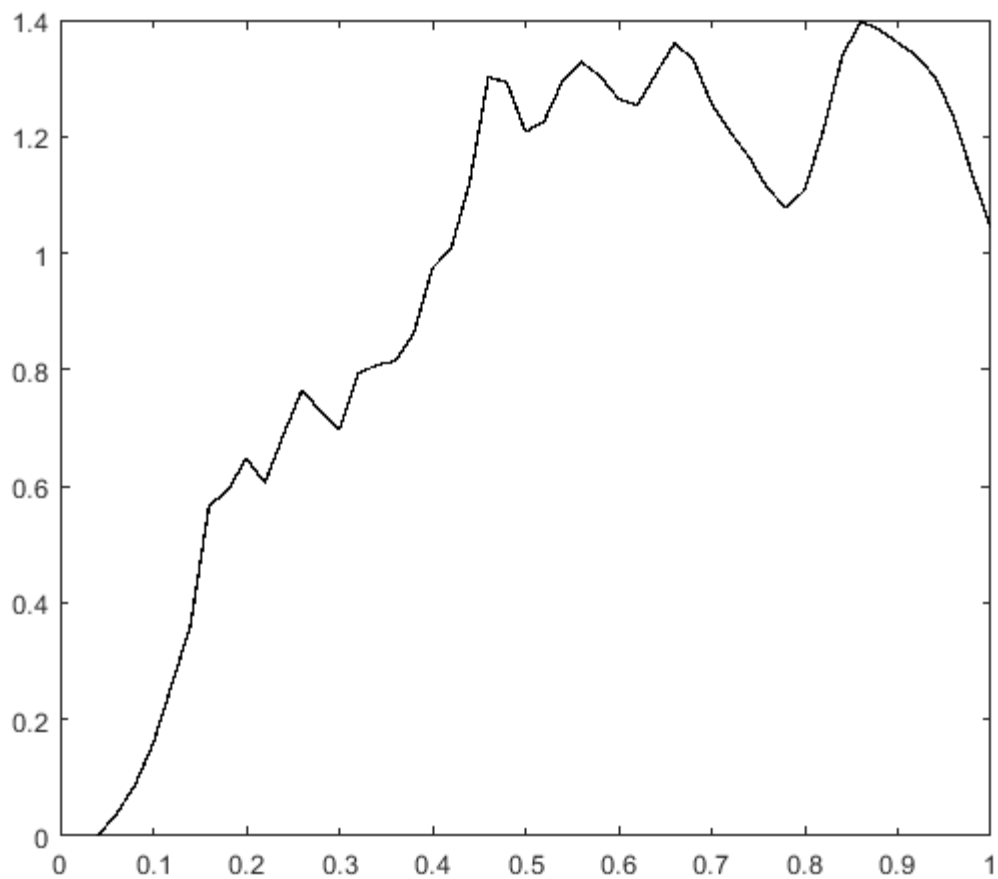


```
figure(14)
plot(S8.Period,S8.SievABS,'k','LineWidth',1)
```

```
figure(15)
plot(S8.Period,S8.SievREL,'k','LineWidth',1)
```

Warning: Imaginary parts of complex X
and/or Y arguments ignored



```
S8.PredPSa
```

```
ans =  
  
9.011815256159021
```

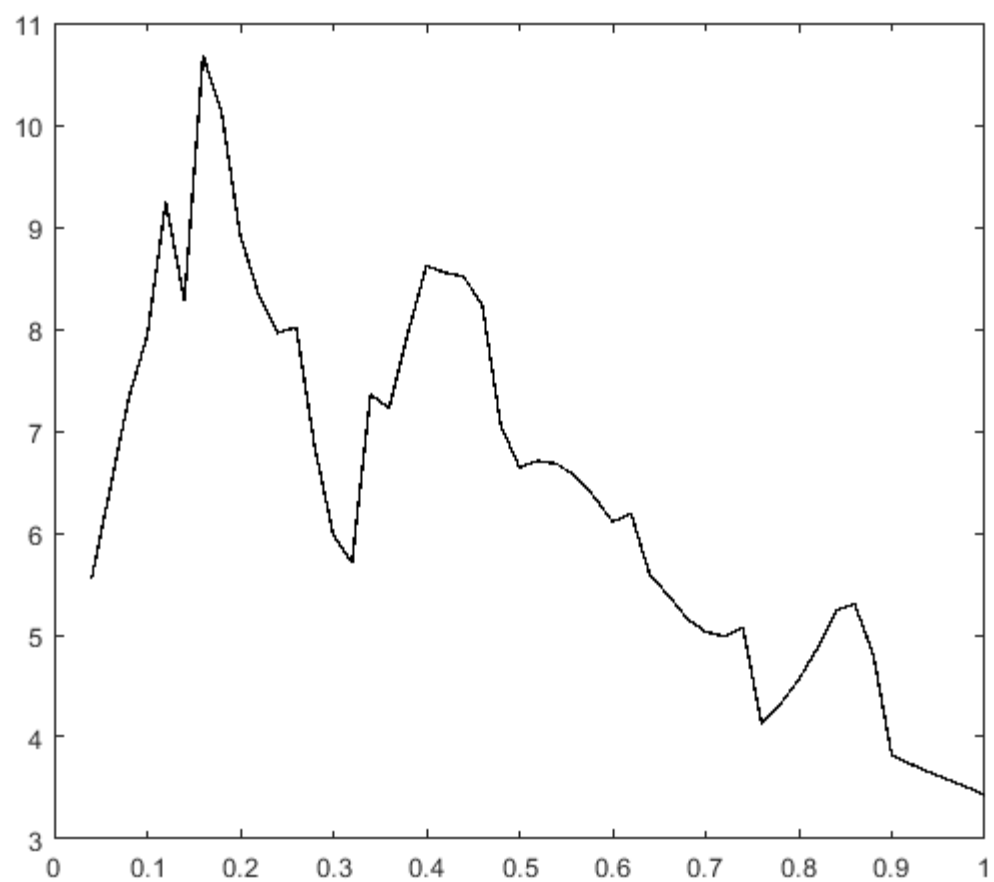
```
S8.PredPeriod
```

```
ans =  
  
0.5000000000000000
```

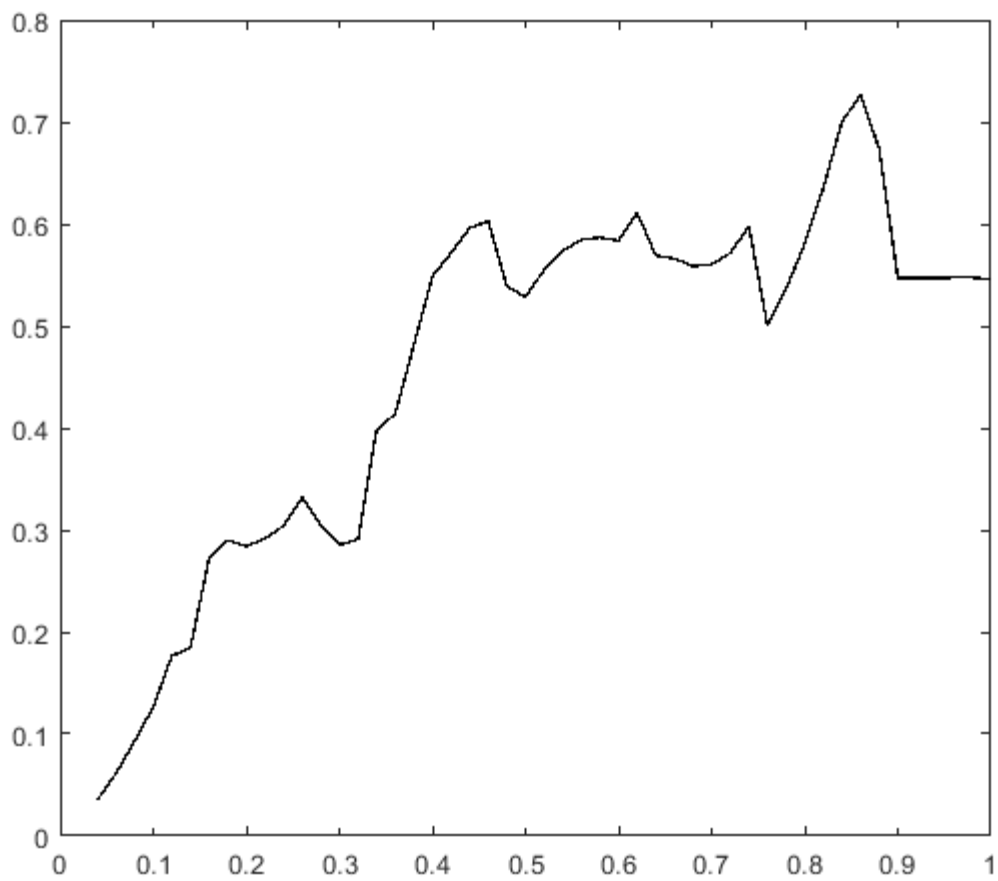
Constant ductility response spectra and pseudospectra

```
sw='cgs';  
ksi=0.05;  
T=0.04:0.02:1;  
mu=2;  
S9=OpenSeismoMatlab(dt,xgtd,sw,T,ksi,mu);
```

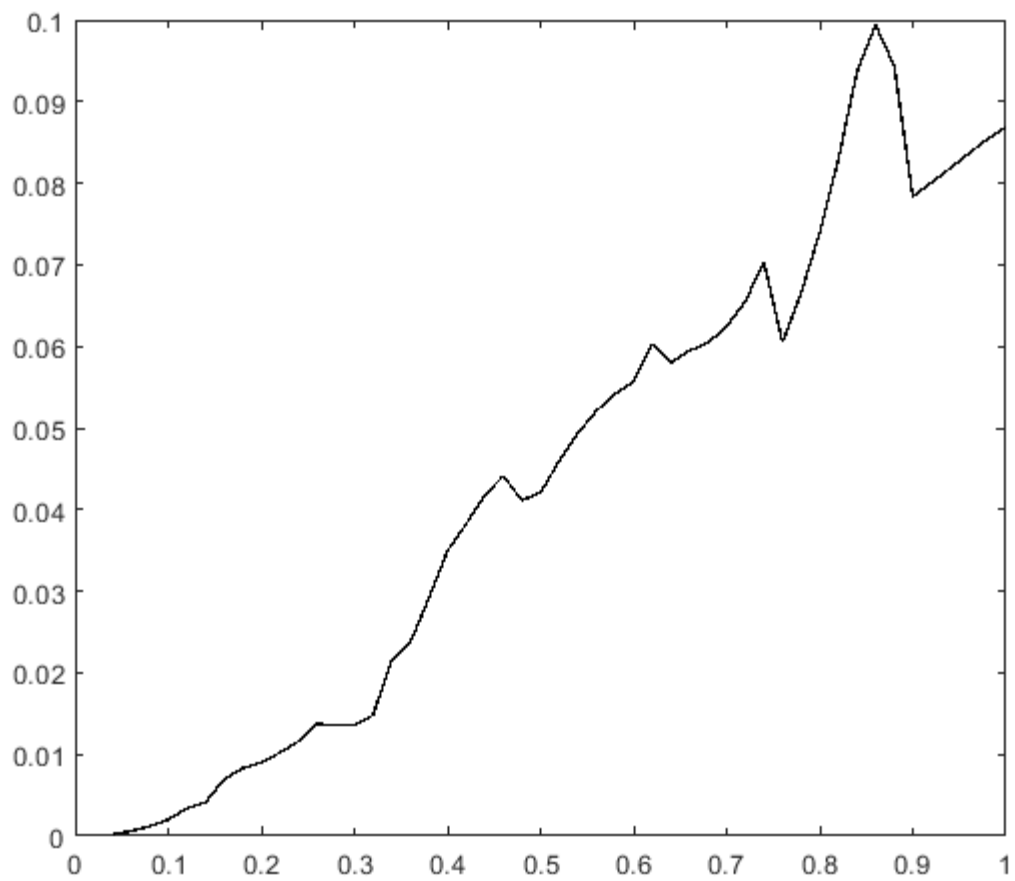
```
figure(15)
plot(S9.Period,S9.CDPSa,'k','LineWidth',1)
```



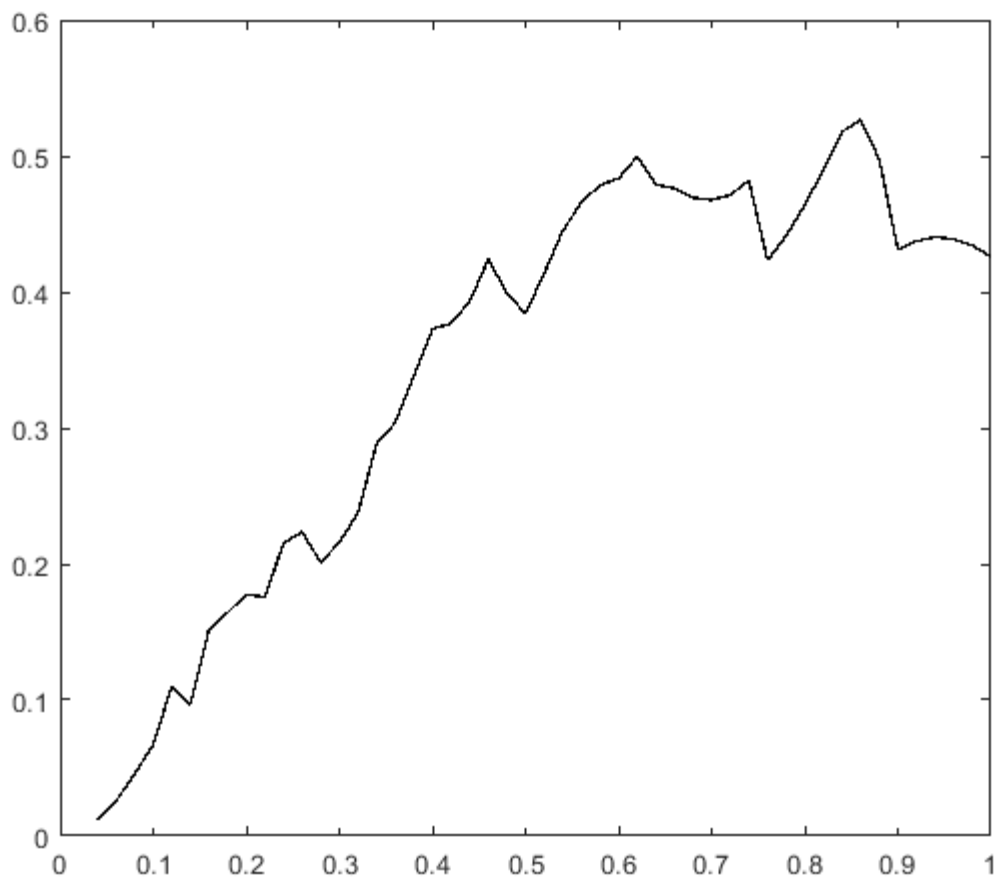
```
figure(16)
plot(S9.Period,S9.CDPSv,'k','LineWidth',1)
```



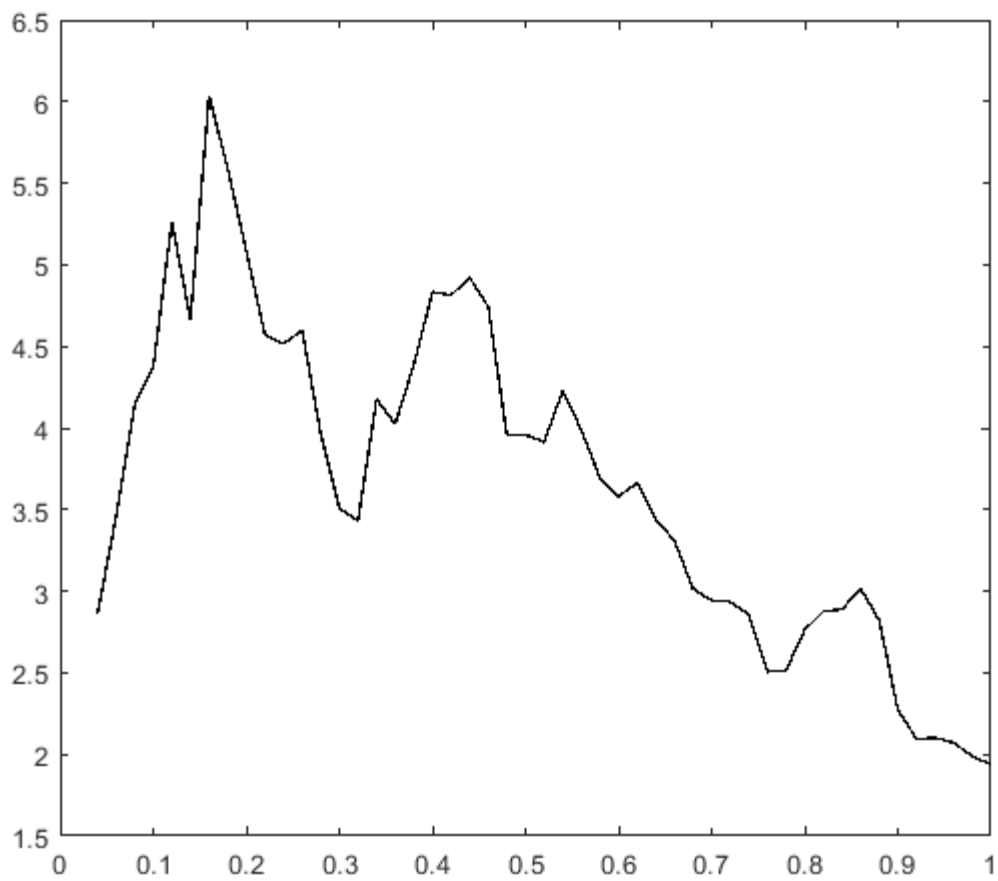
```
figure(17)
plot(S9.Period,S9.CDSd,'k','LineWidth',1)
```



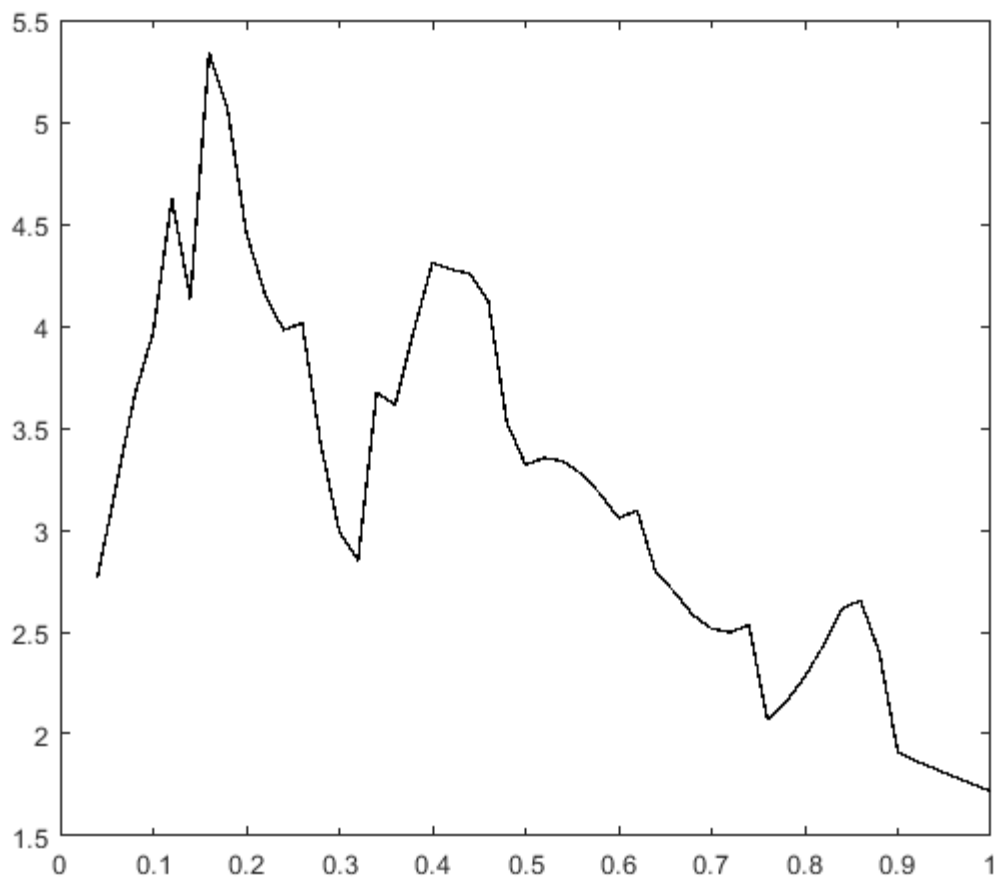
```
figure(18)
plot(S9.Period,S9.CDSv,'k','LineWidth',1)
```



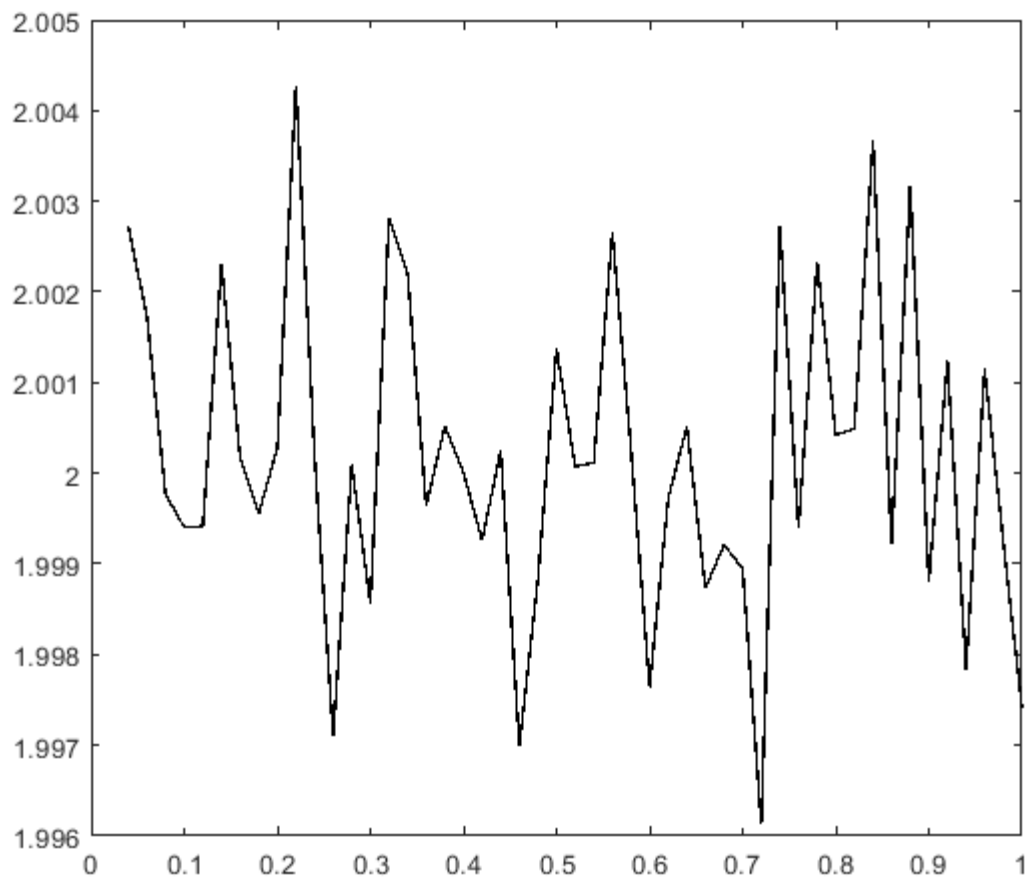
```
figure(19)
plot(S9.Period,S9.CDSa,'k','LineWidth',1)
```



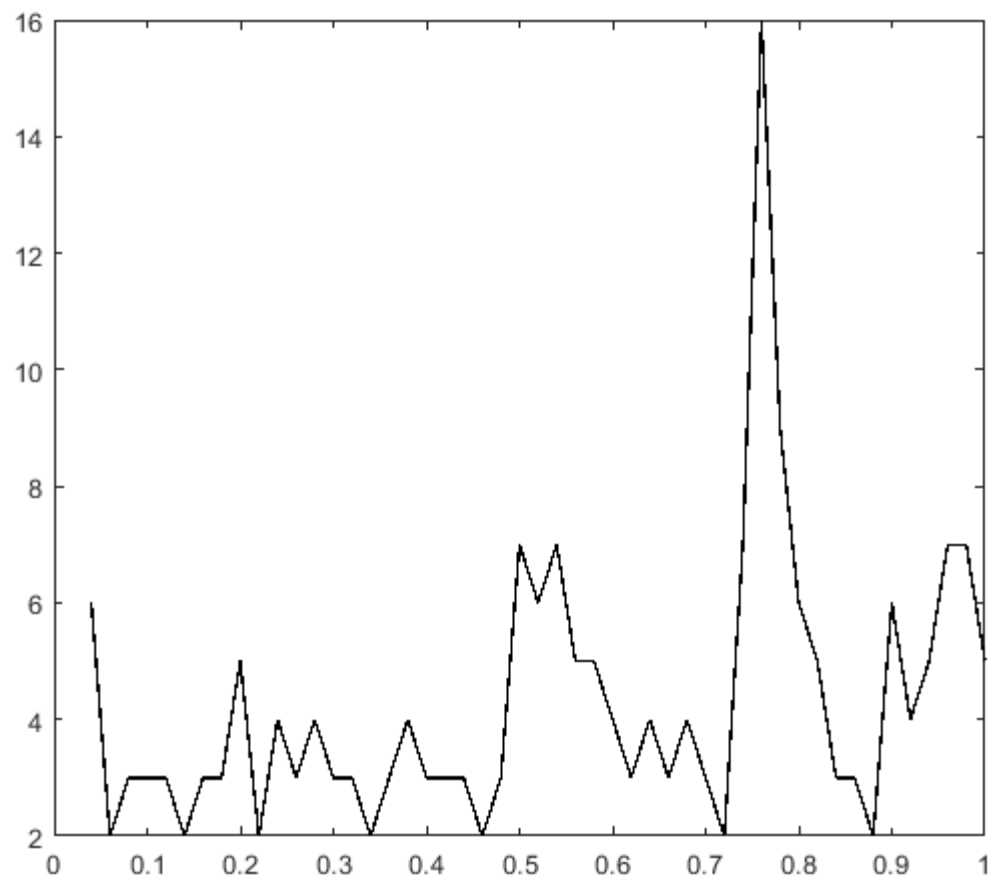
```
figure(20)
plot(S9.Period,S9.fyK,'k','LineWidth',1)
```



```
figure(21)
plot(S9.Period,S9.muK,'k','LineWidth',1)
```

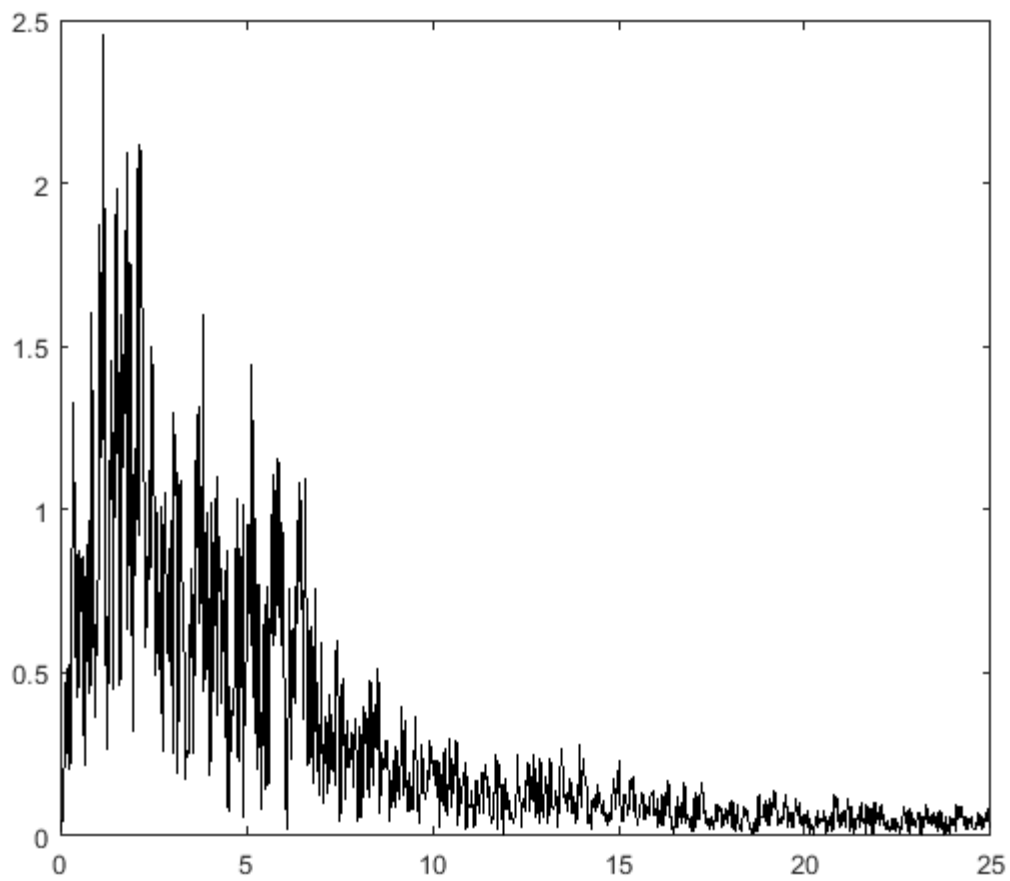
```
figure(22)
plot(S9.Period,S9.iterK,'k','LineWidth',1)
```



Fourier amplitude spectrum and mean period

```
sw='fs';  
S10=OpenSeismoMatlab(dt,xgtt,sw);
```

```
figure(23)  
plot(S10.freq,S10.FAS,'k','LineWidth',1)
```



```
S10.Tm
```

```
ans =  
  
0.533389590787339
```

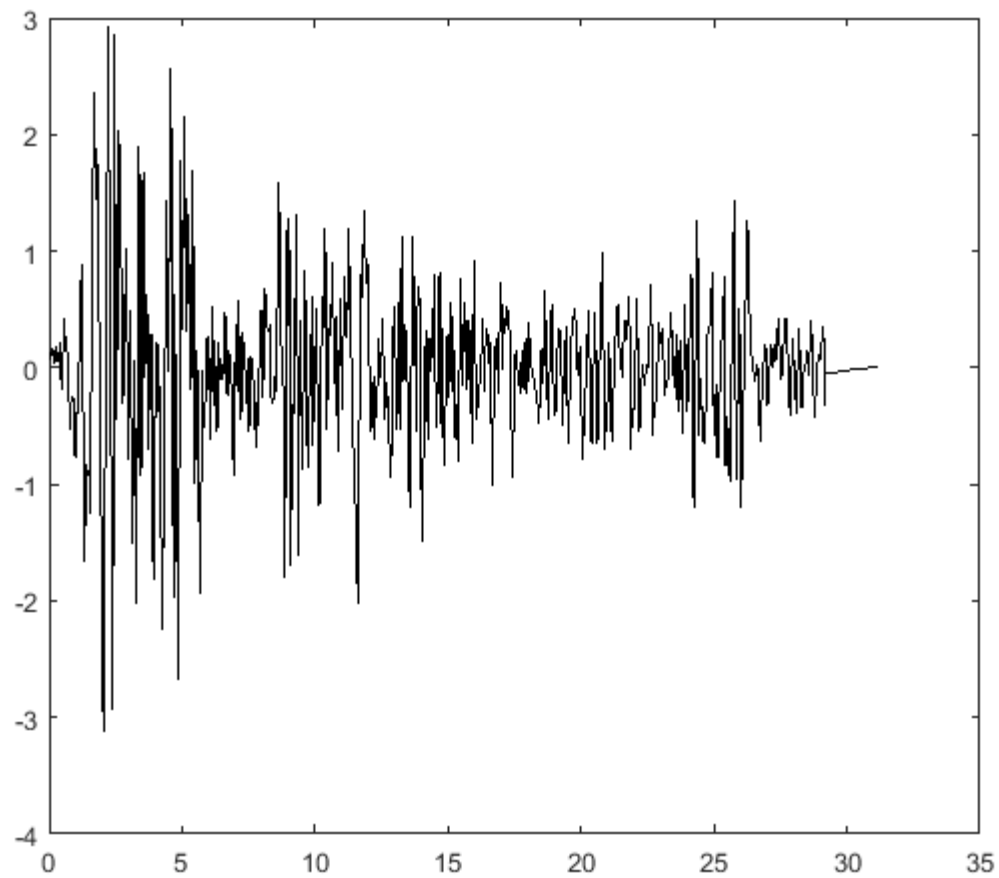
```
S10.Fm
```

```
ans =  
  
3.293755163661825
```

High pass Butterworth filter

```
sw='butterworthhigh';  
bOrder=4;  
flc=0.1;  
S11=OpenSeismoMatlab(dt,xgtt,sw,bOrder,flc);
```

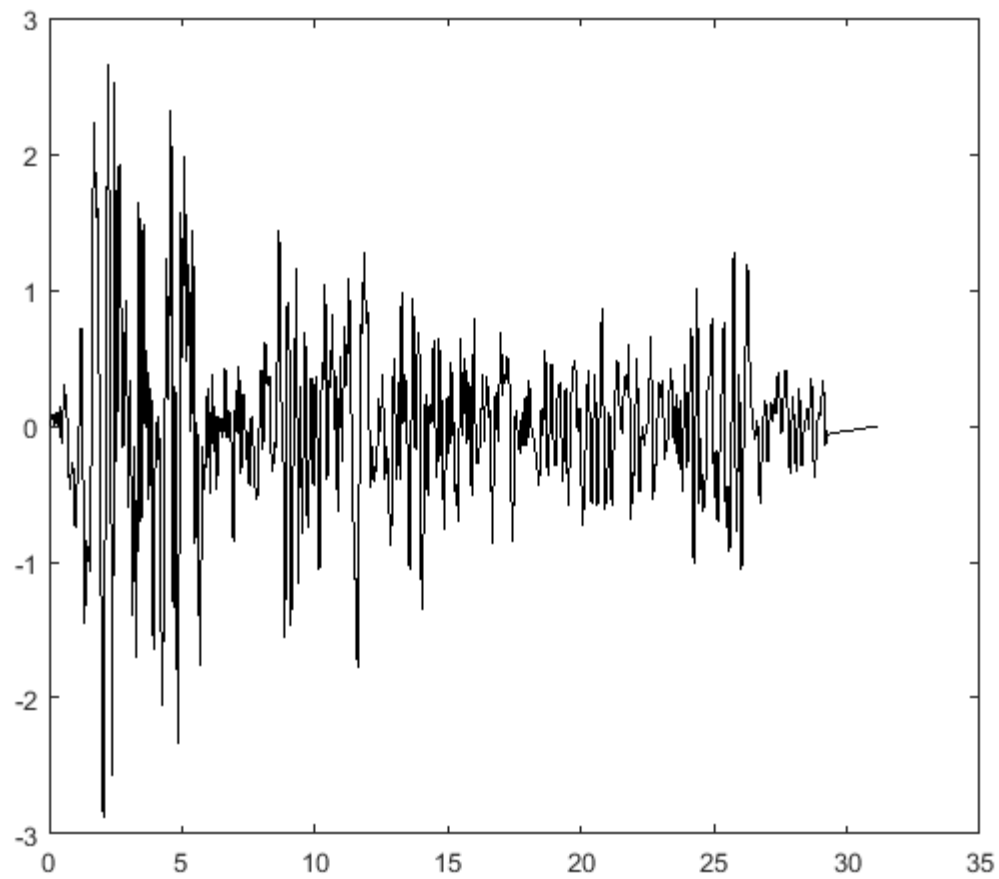
```
figure(24)
plot(S11.time,S11.acc,'k','LineWidth',1)
```



Low pass Butterworth filter

```
sw='butterworthlow';
bOrder=4;
fhc=10;
S12=OpenSeismoMatlab(dt,xgtt,sw,bOrder,fhc);
```

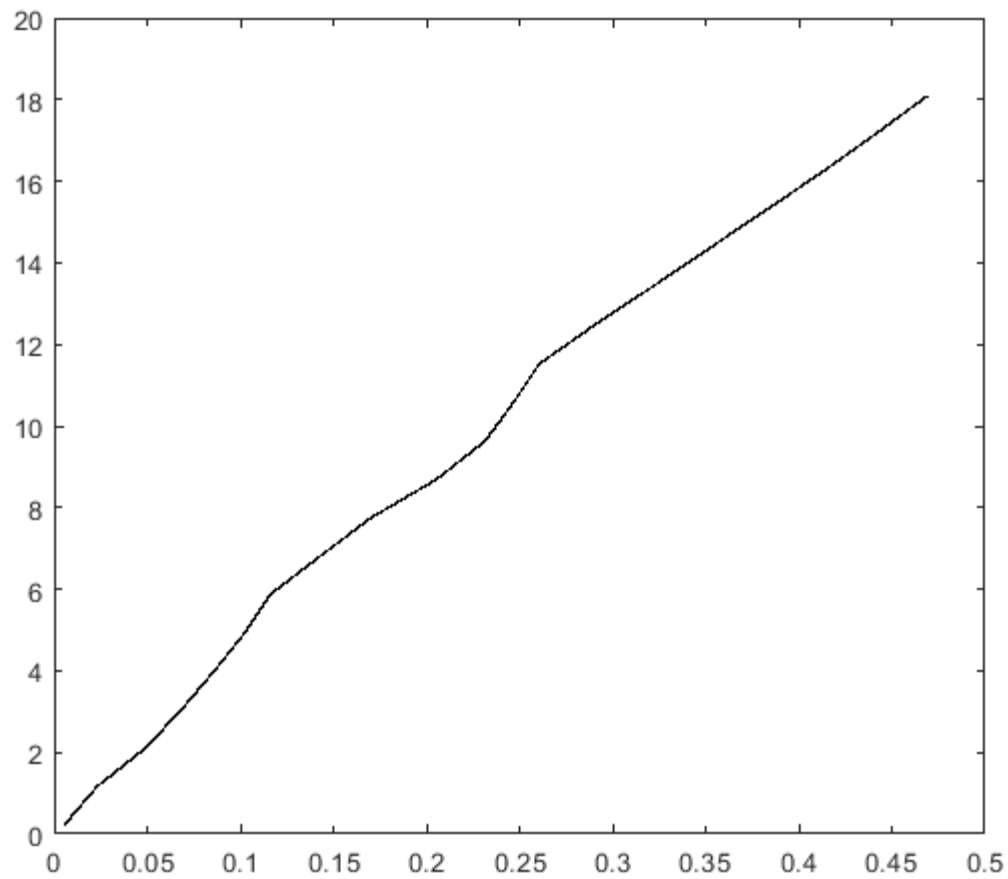
```
figure(25)
plot(S12.time,S12.acc,'k','LineWidth',1)
```



Incremental dynamic analysis

```
sw='ida';  
S13=OpenSeismoMatlab(dt,xgtt,sw);
```

```
figure(26)  
plot(S13.DM,S13.IM,'k','LineWidth',1)
```



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LEReSp

Calculate linear elastic response spectra in OpenSeismoMatlab

Contents

- [Generate earthquake motion](#)
- [Plot the generated time history](#)
- [Setup parameters for LEReSp function](#)
- [Calculate spectra and pseudospectra](#)
- [Plot the spectra and pseudospectra](#)
- [Copyright](#)

Generate earthquake motion

For reproducibility

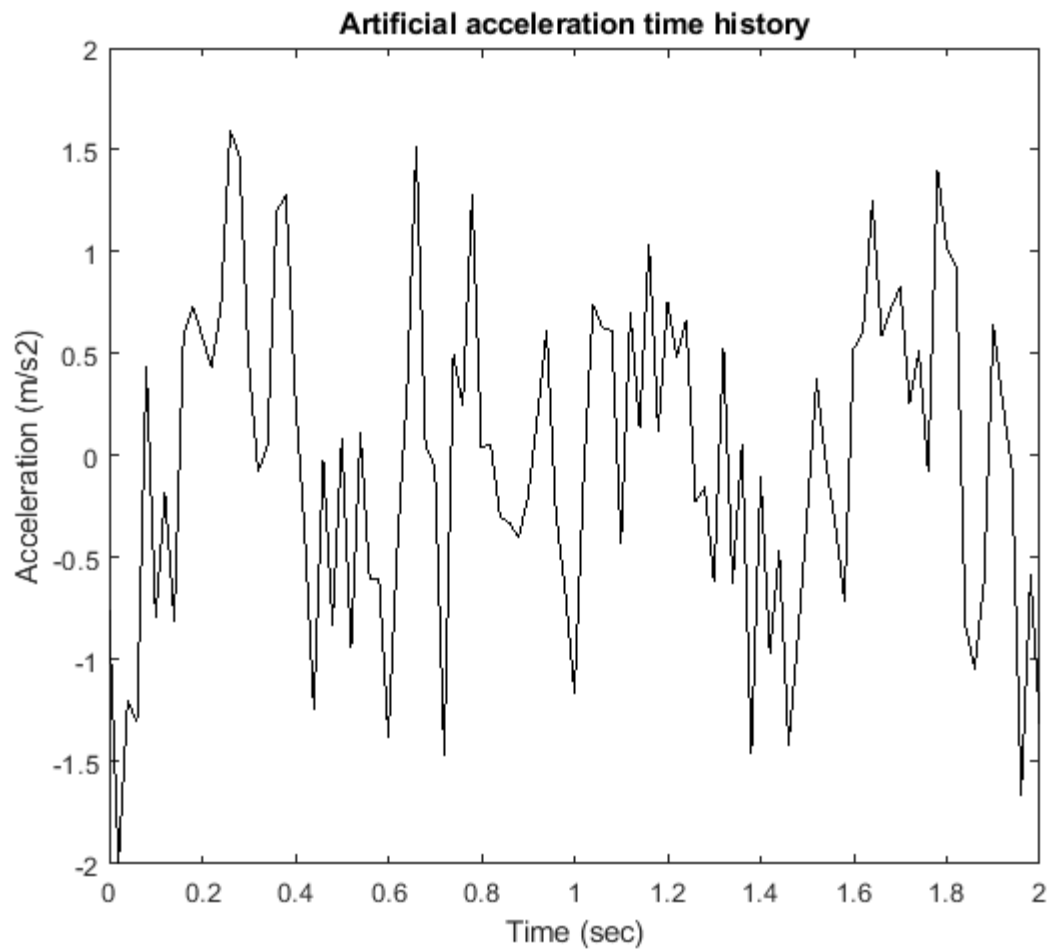
```
rng(0)
```

Generate earthquake acceleration time history

```
dt=0.02;  
N=10;  
a=rand(N,1)-0.5;  
b=100*pi*rand(N,1);  
c=pi*(rand(N,1)-0.5);  
t=(0:dt:(100*dt))';  
xgtt=zeros(size(t));  
for i=1:N  
    xgtt=xgtt+a(i)*sin(b(i)*t+c(i));  
end
```

Plot the generated time history

```
figure()  
plot(t,xgtt,'k','LineWidth',1)  
ylabel('Acceleration (m/s2)')  
xlabel('Time (sec)')  
title('Artificial acceleration time history')
```



Setup parameters for LEReSp function

Eigenperiods

```
T=logspace(log10(0.02),log10(5),1000)';
```

Critical damping ratio

```
ksi=0.05;
```

Maximum ratio of the integration time step to the eigenperiod

```
dtTol=0.02;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix


```
rinf=1;
```

Calculate spectra and pseudospectra

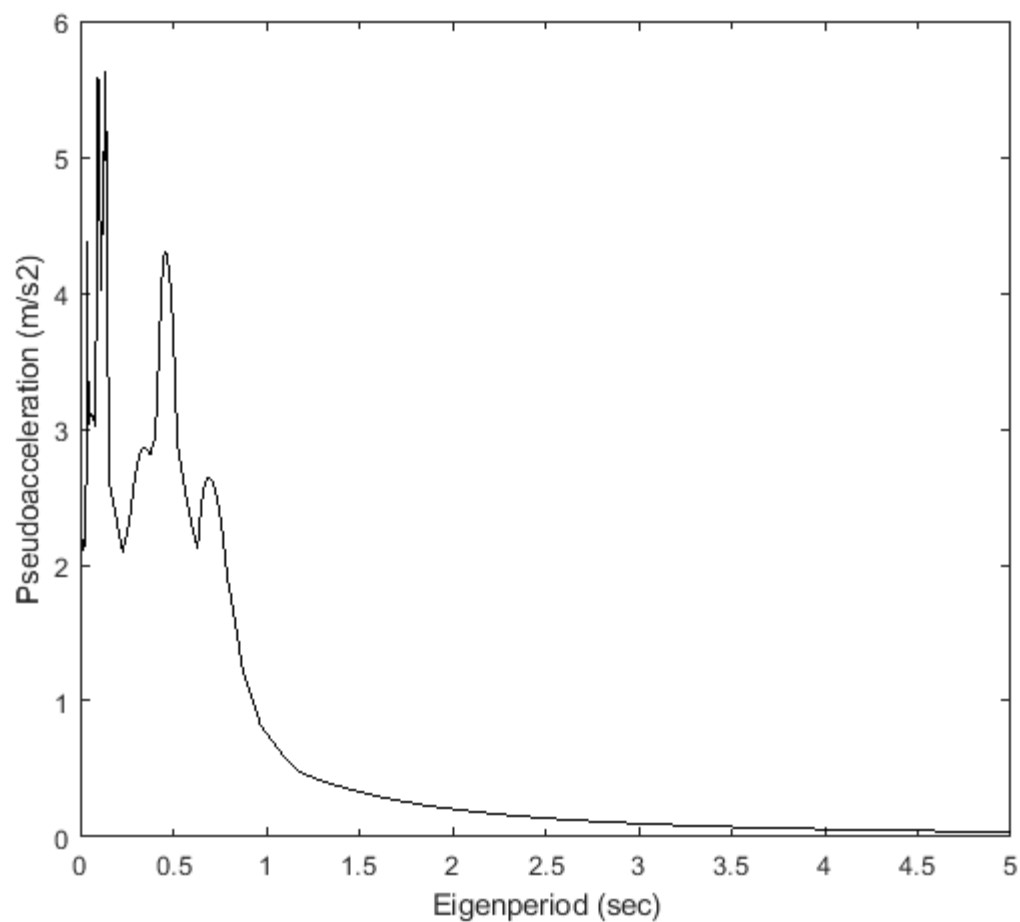
Apply LEReSp

```
[PSa,PSv,Sd,Sv,Sa,SievABS,SievREL]=LEReSp(dt,xgdt,T,ksi,dtTol,AlgID,rinf);
```

Plot the spectra and pseudospectra

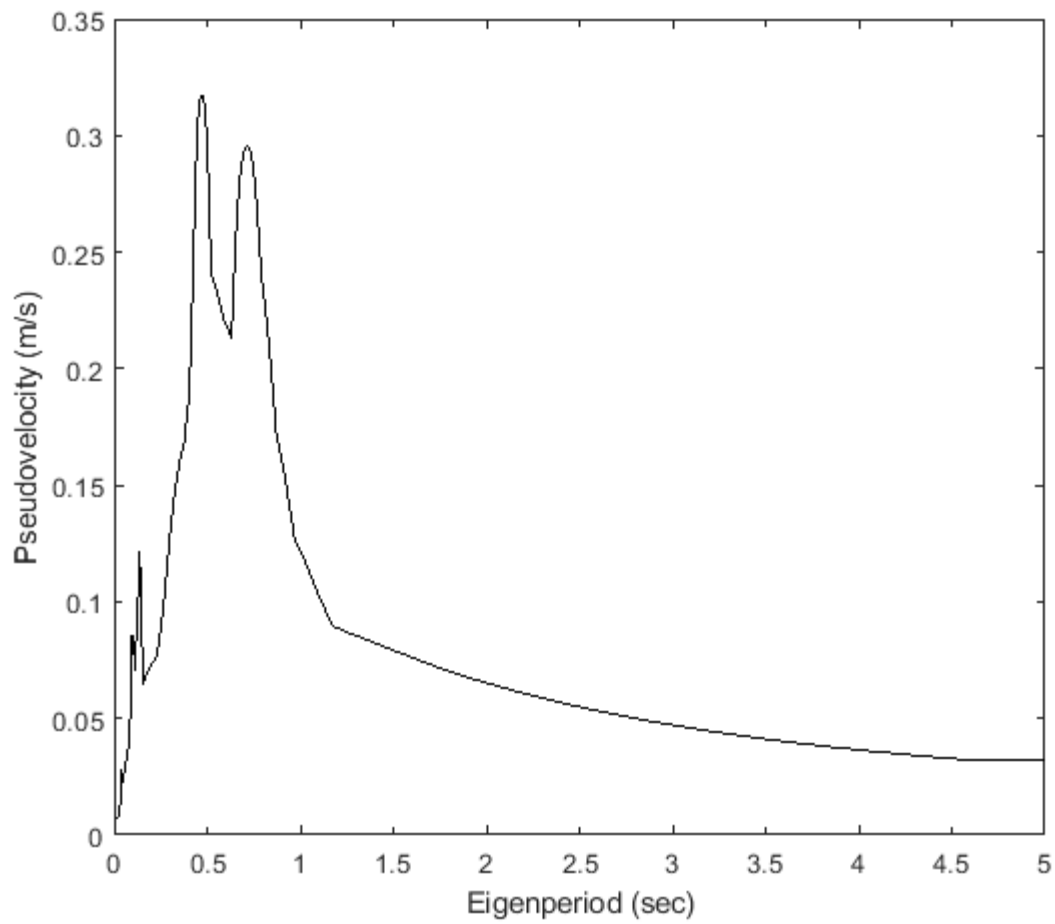
Pseudoacceleration spectrum

```
figure()  
plot(T,PSa,'k','LineWidth',1)  
ylabel('Pseudoacceleration (m/s2)')  
xlabel('Eigenperiod (sec)')
```



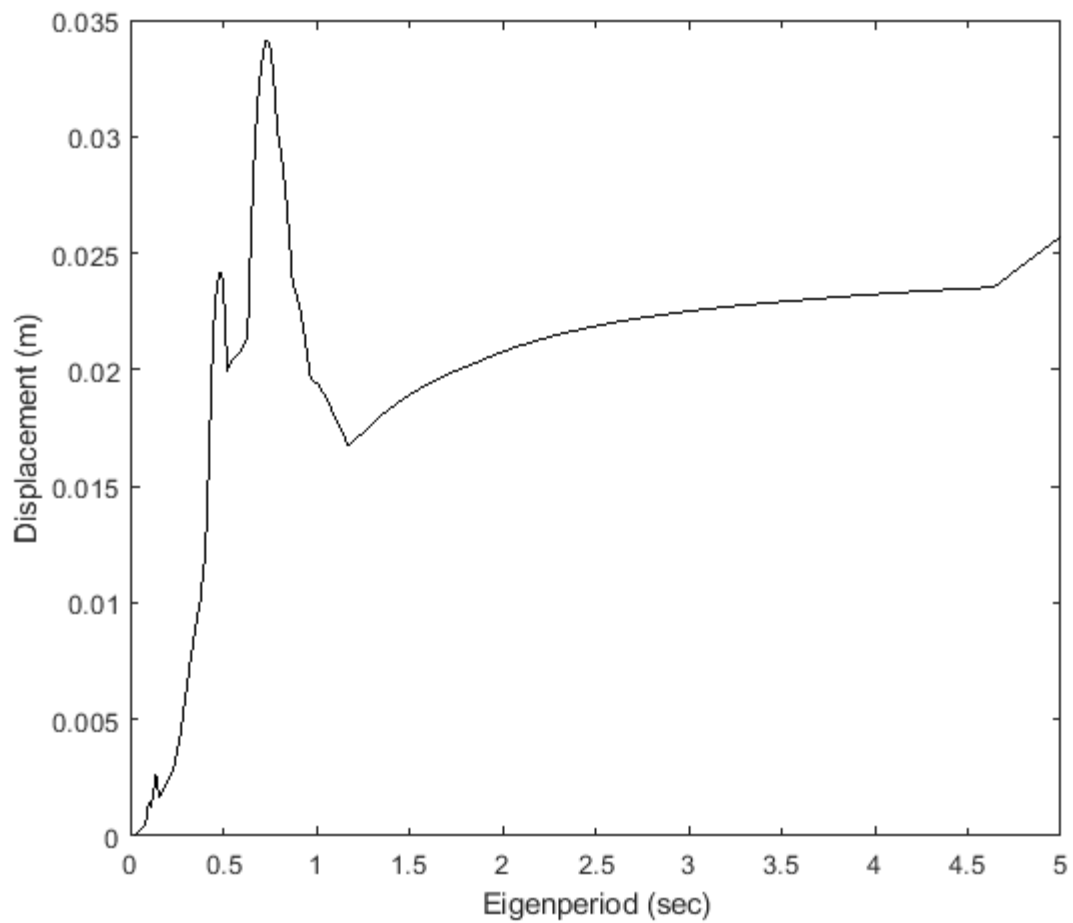
Pseudovelocity spectrum

```
figure()  
plot(T,PSv,'k','LineWidth',1)  
ylabel('Pseudovelocity (m/s)')  
xlabel('Eigenperiod (sec)')
```



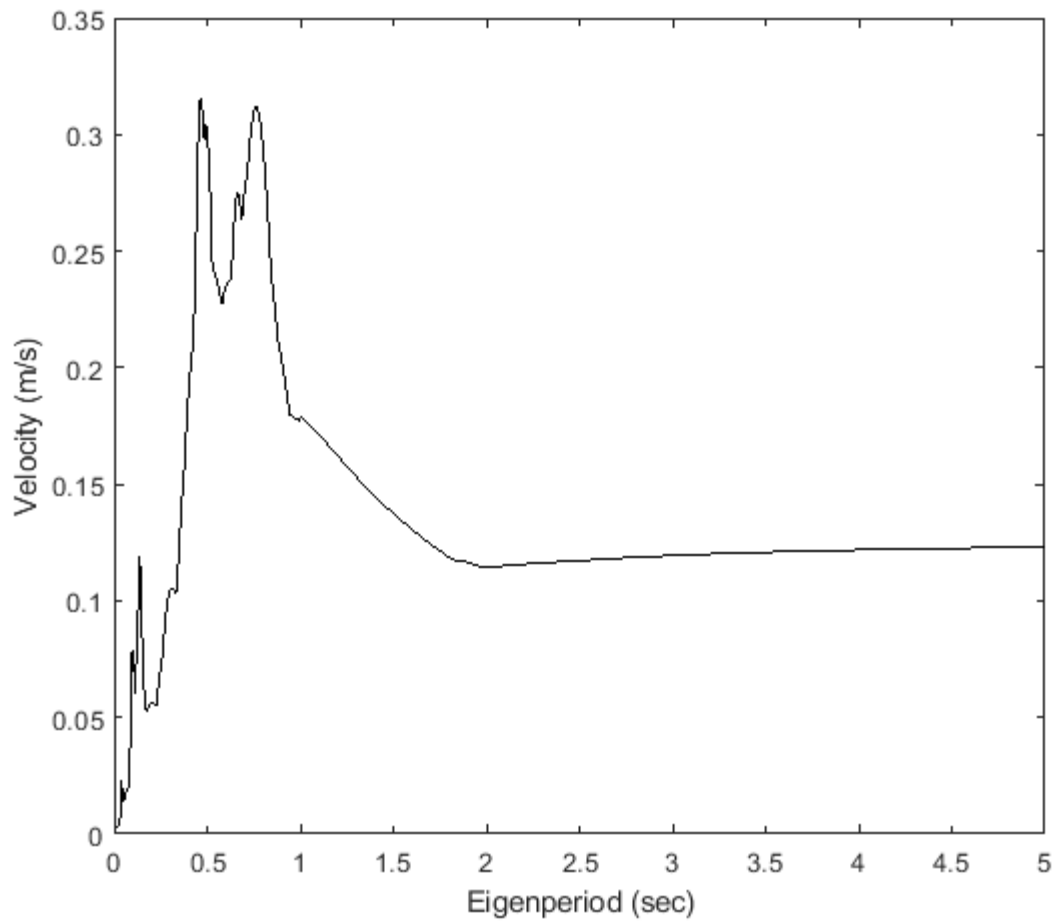
Displacement spectrum

```
figure()  
plot(T,Sd,'k','LineWidth',1)  
ylabel('Displacement (m)')  
xlabel('Eigenperiod (sec)')
```



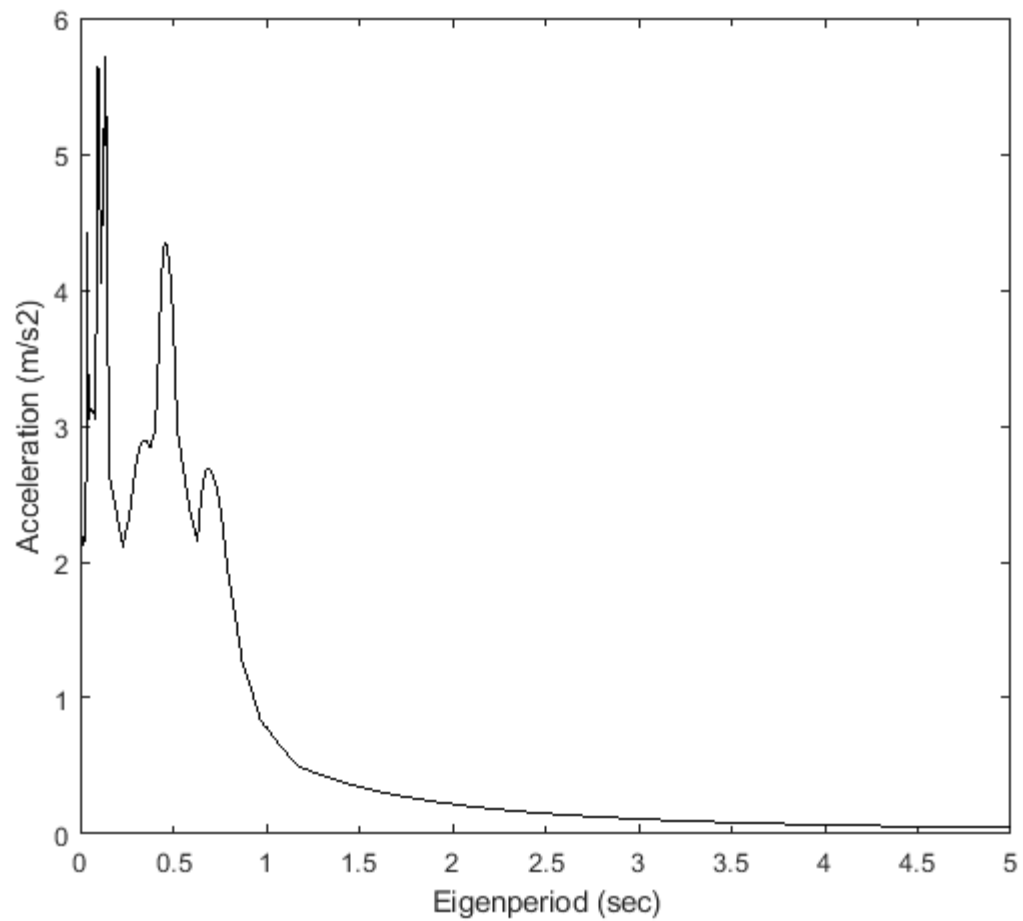
Velocity spectrum

```
figure()  
plot(T,Sv,'k','LineWidth',1)  
ylabel('Velocity (m/s)')  
xlabel('Eigenperiod (sec)')
```



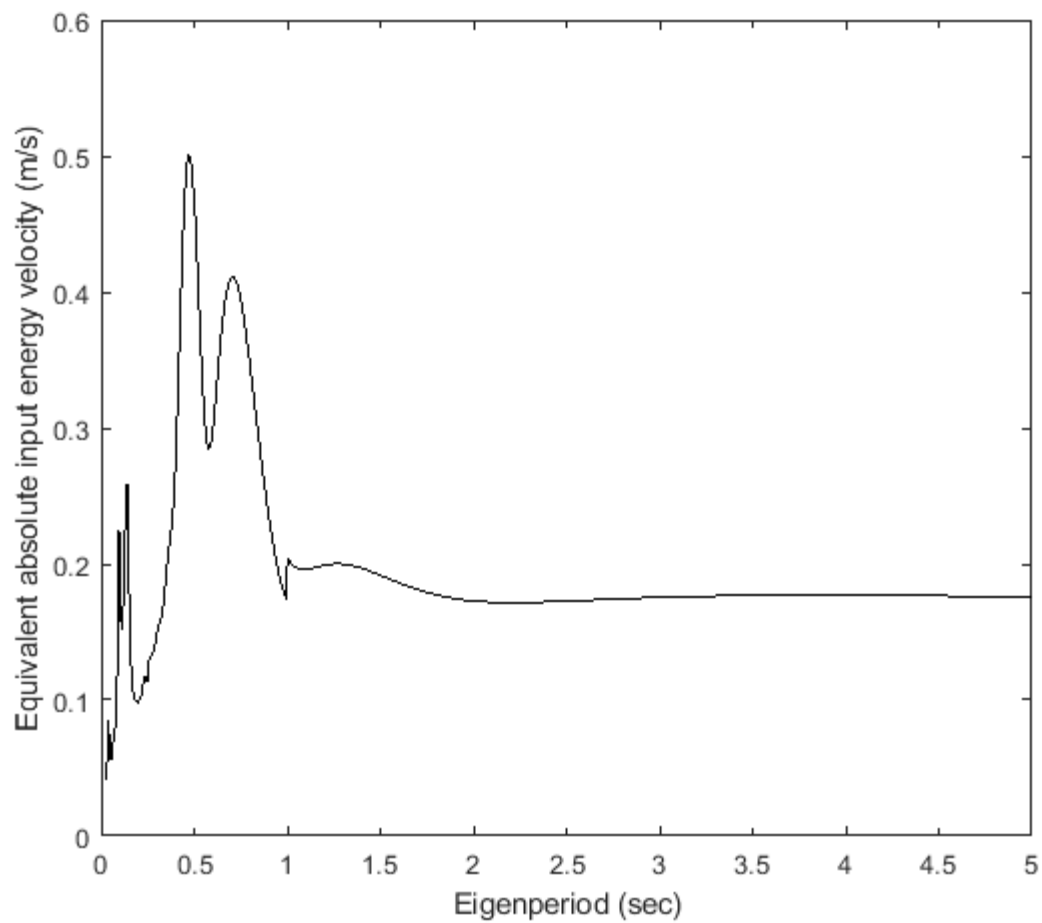
Acceleration spectrum

```
figure()  
plot(T,Sa,'k','LineWidth',1)  
ylabel('Acceleration (m/s2)')  
xlabel('Eigenperiod (sec)')
```



Equivalent absolute input energy velocity

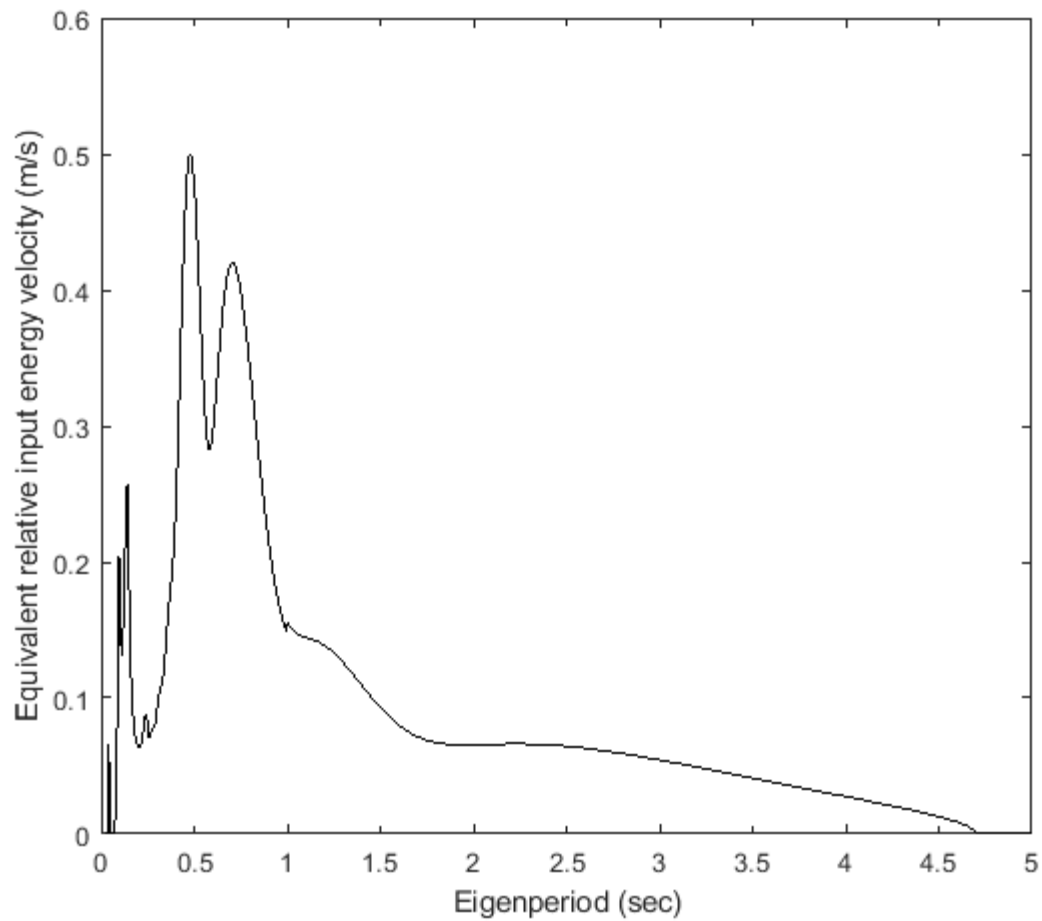
```
figure()
plot(T,SievABS,'k','LineWidth',1)
ylabel('Equivalent absolute input energy velocity (m/s)')
xlabel('Eigenperiod (sec)')
```



Equivalent relative input energy velocity

```
figure()
plot(T,SievREL,'k','LineWidth',1)
ylabel('Equivalent relative input energy velocity (m/s)')
xlabel('Eigenperiod (sec)')
```

Warning: Imaginary parts of complex X
and/or Y arguments ignored



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Linear elastic response spectra

Generate the linear elastic response spectra of an earthquake suite using OpenSeismoMatlab.

Contents

- [Input](#)
- [Calculation](#)
- [Output](#)
- [Copyright](#)

Input

Earthquake motions

```
eqmotions={'Imperial Valley'; % Imperial valley 1979
           'Kocaeli';
           'Loma Prieta';
           'Northridge';
           'San Fernando';
           'Spitak';
           'Cape Mendocino';
           'ChiChi';
           'El Centro'; % Imperial valley 1940
           'Hollister';
           'Kobe'};
```

Set the eigenperiod range for which the response spectra will be calculated.

```
Tspectra=(0.01:0.01:4)';
```

Set critical damping ratio of the response spectra to be calculated.

```
ksi=0.05;
```

Extract linear elastic response spectra

```
sw='es';
```

Calculation

Initialize LERS

```
LERS=cell(numel(eqmotions),1);
```

Calculation of peak values


```

for i=1:numel(eqmotions)
    % earthquake
    data=load([eqmotions{i},'.dat']);
    t=data(:,1);
    dt=t(2)-t(1);
    xgtt=data(:,2);
    S=OpenSeismoMatlab(dt,xgtt,sw,Tspectra,ksi);
    LERS{i}=[S.Period,S.Sd,S.PSv,S.PSa];
end

```

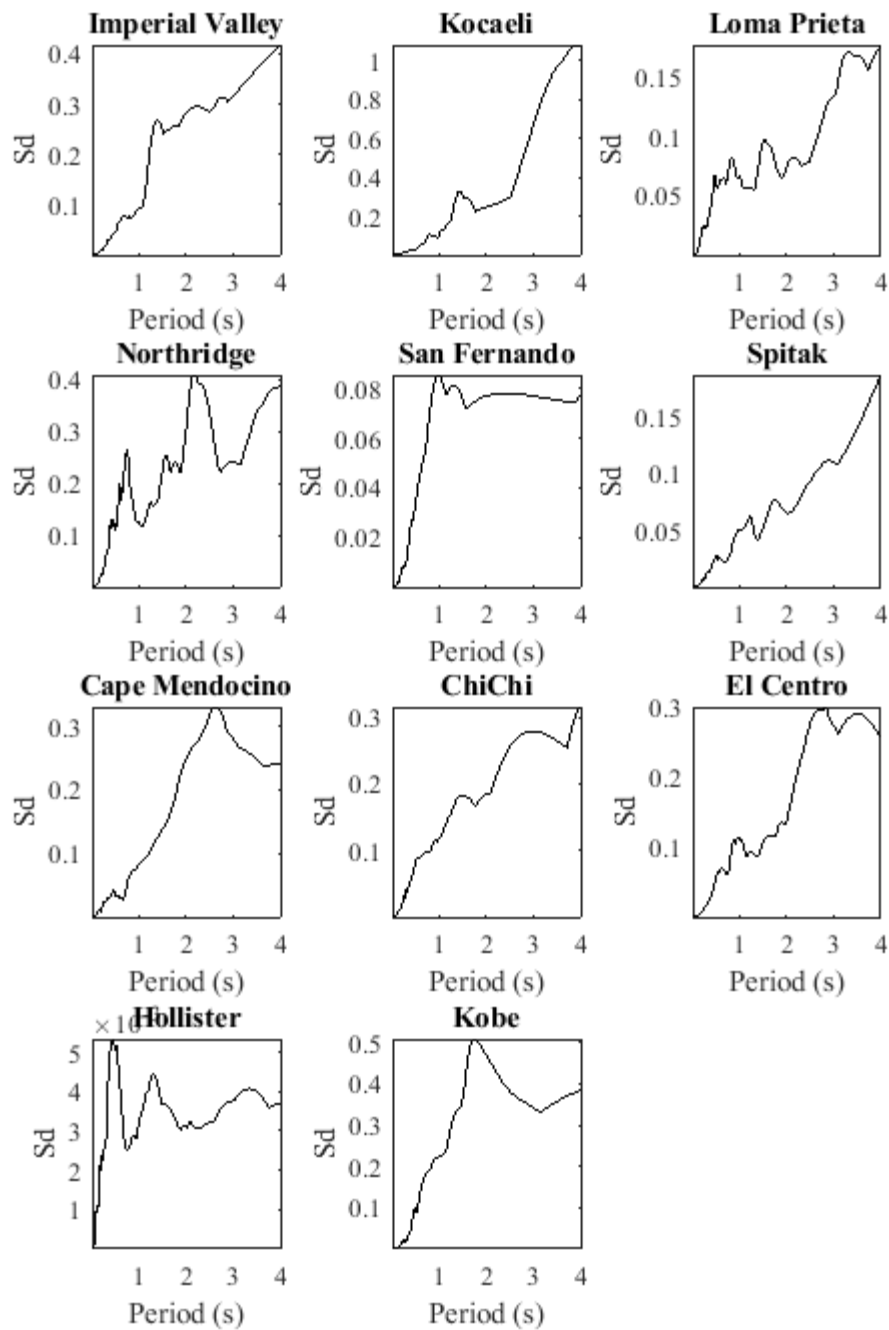
Output

Plot displacement response spectra

```

Fig1 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(LERS{i}(:,1),LERS{i}(:,2),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('Sd','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
    axis tight
end

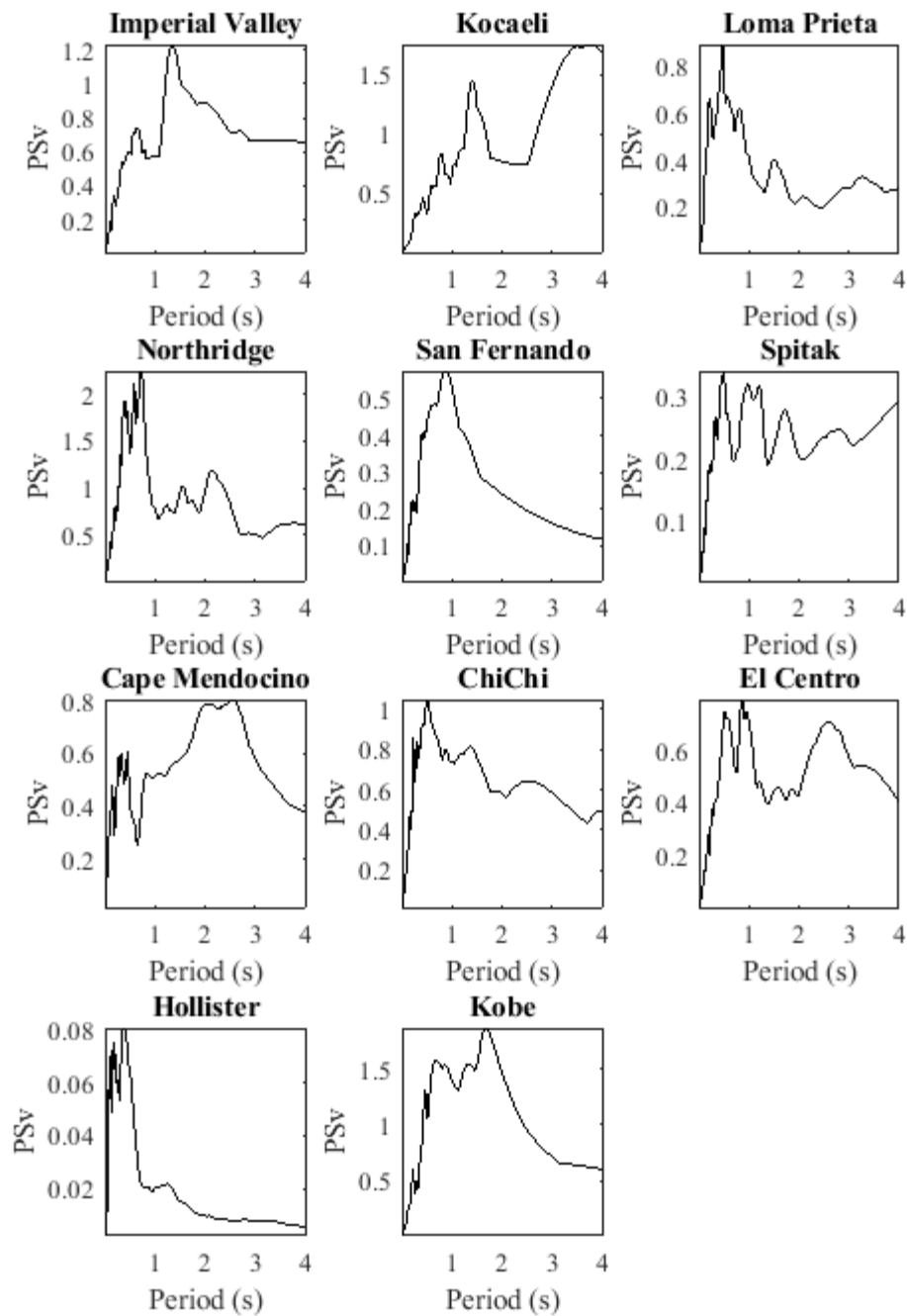
```



Plot pseudo-velocity response spectra

```
Fig2 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(LEERS{i}(:,1),LEERS{i}(:,3),'k','LineWidth',1);
    set(gca,'FontName','Times New Roman')
    title(eqmotions{i},'FontName','Times New Roman')
    ylabel('PSv','FontName','Times New Roman')
    xlabel('Period (s)','FontName','Times New Roman')
```

```
axis tight
end
```



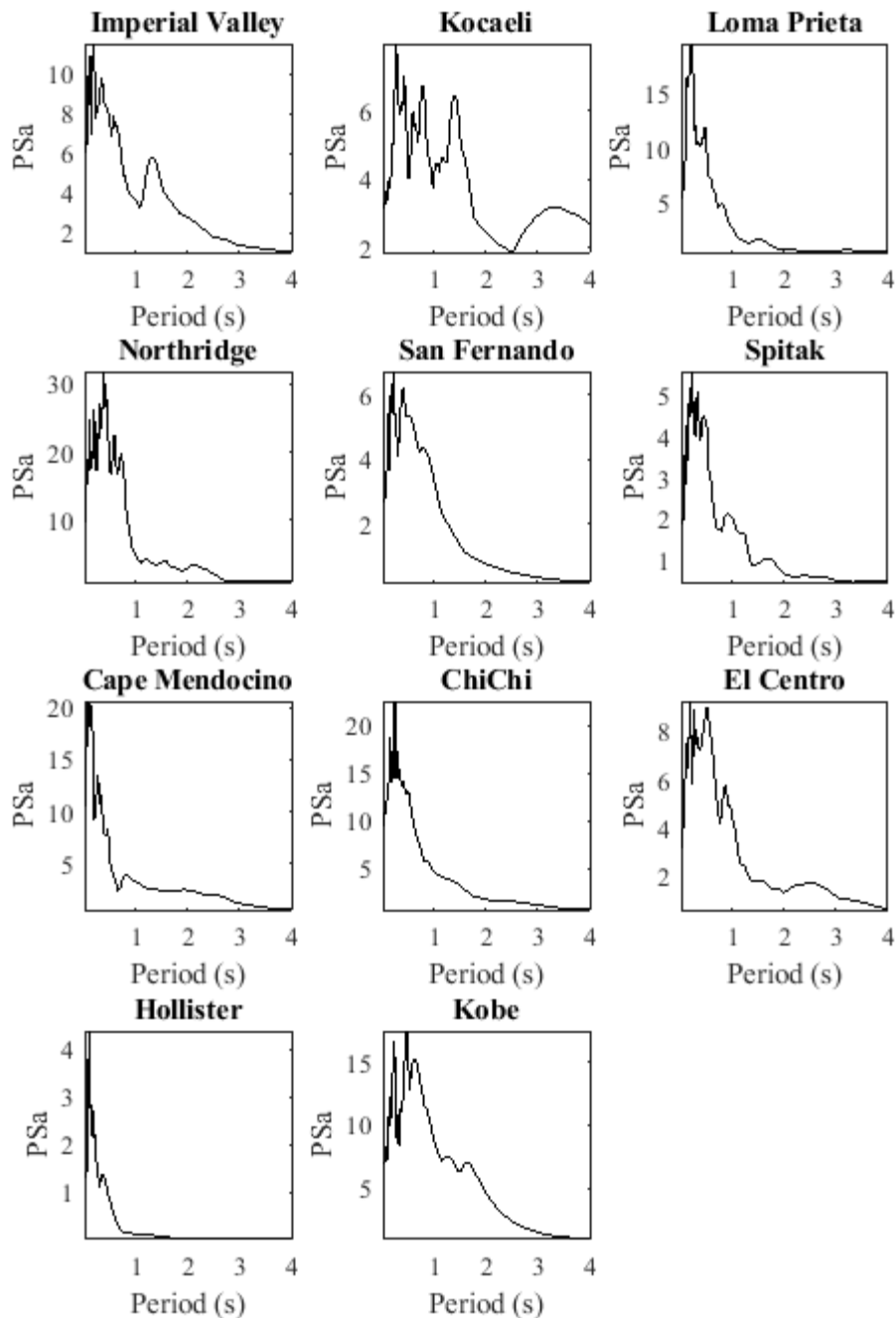
Plot pseudo-acceleration response spectra

```
Fig3 = figure('units', 'centimeters', 'Position', [0,0, 20/sqrt(2), 20]);
% Scan all subplots
for i=1:numel(eqmotions)
    subplot(4,3,i)
    plot(LERS{i}(:,1),LERS{i}(:,4),'k','LineWidth',1);
```

```

set(gca,'FontName','Times New Roman')
title(egmotions{i},'FontName','Times New Roman')
ylabel('PSa','FontName','Times New Roman')
xlabel('Period (s)','FontName','Times New Roman')
axis tight
end

```



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Comparison of elastic and constant ductility response spectra for $\mu=1$

Compare the linear elastic acceleration response spectrum and the constant ductility response spectrum for $\mu=1$ (degenerates to linear elastic). Also, compare with corresponding results of SeismoSignal software

Contents

- [Input](#)
- [First we use the CDS to calculate linear response](#)
- [Next we use ES to calculate linear response](#)
- [Results from SeismoSignal](#)
- [Output](#)

Input

Earthquake motion

```
eqmotions={'Imperial Valley'}; % Imperial valley 1979
data=load([eqmotions{1},'.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgtd=data(:,2);
```

Set the eigenperiod range for which the response spectra will be calculated.

```
Tspectra=(0.05:0.05:4)';
```

Set critical damping ratio of the response spectra to be calculated.

```
ksi=0.05;
```

First we use the CDS to calculate linear response

Set the target ductility

```
mu=1; % mu=1 equivalent to a linear SDoF
```

Extract constant ductility response spectra

```
sw='cds';
```

Calculation CDRS{i}=[S.Period,S.CDSd,S.CDSv,S.CDPSa,S.fyK,S.muK,S.iterK];

```
S1=OpenSeismoMatlab(dt,xgtd,sw,Tspectra,ksi,mu);
```

Next we use ES to calculate linear response

Extract linear elastic response spectra

```
sw='es';
```

Initialize LERS

```
LERS=cell(numel(eqmotions),1);
```

Calculation LERS{i}=[S.Period,S.Sd,S.PSv,S.PSa];

```
S2=OpenSeismoMatlab(dt,xgtd,sw,Tspectra,ksi);
```

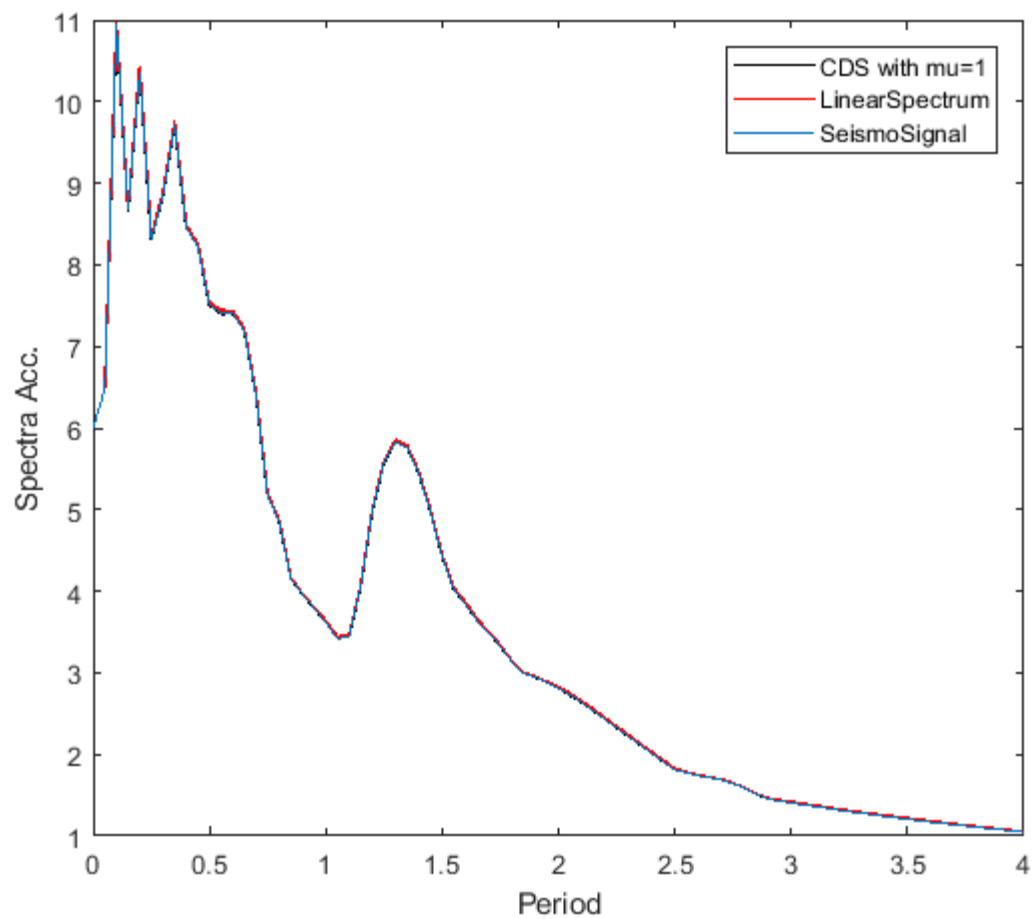
Results from SeismoSignal

```
fileID = fopen('SeismoSignal_Imperial Valley.txt');  
for idx = 1:5  
    fgetl(fileID);  
end  
C = textscan(fileID, repmat('%f',1,12));  
fclose(fileID);
```

Output

Plot spectral acceleration response spectra

```
plot(S1.Period,S1.CDSa,'k','LineWidth',1);  
hold on  
plot(S2.Period,S2.Sa,'r','LineWidth',1);  
plot(C{1},C{2})  
legend('CDS with mu=1','LinearSpectrum','SeismoSignal');  
xlabel('Period');  
ylabel('Spectra Acc.')
```



Comparison of constant ductility response spectra of RSN1044 for $\mu=2$

Contents

- [Input](#)
- [Results from OpenSeismoMatlab](#)
- [Results from SeismoSignal](#)
- [Output](#)

Input

Earthquake motions

```
GMFileLoc = 'input\';
```

A text file containing the lists of GM names

```
RecordList = ['input\Record_List.txt'];
```

Read E.Q. records name from the specifid list

```
fid = fopen (RecordList,'r');  
records = textscan(fid, '%s'); % length = num of records*1, cell  
fclose (fid);
```

Read E.Q. records name from the specifid list Return variables include record names, dt, num of points, PGA, Acc TH, Spectral Acc The accelration-related variables (PGA, Sa, Acc TH) are in unit of g; disp-related in m If you do not specify scaling factors at this step, the default value = 1 for each GM

```
[RecordName_all, dt, numPoint_all, PGA_all, xgtd] =...  
    fn_ParseAT2File2(GMFileLoc, records);
```

Set the eigenperiod range for which the response spectra will be calculated.

```
Tspectra=(0.05:0.05:4)';
```

Set critical damping ratio of the response spectra to be calculated.

```
ksi=0.02;
```

Results from OpenSeismoMatlab

Set the target ductility

```
mu=2; % mu=1 equivalent to a linear SDoF
```

Extract constant ductility response spectra

```
sw='cds' ;
```

Calculation CDRS{i}=[S.Period,S.CDSd,S.CDSv,S.CDPSa,S.fyK,S.muK,S.iterK];

```
S1=OpenSeismoMatlab(dt,xgtt{1},sw,Tspectra,ksi,mu);
```

Results from SeismoSignal

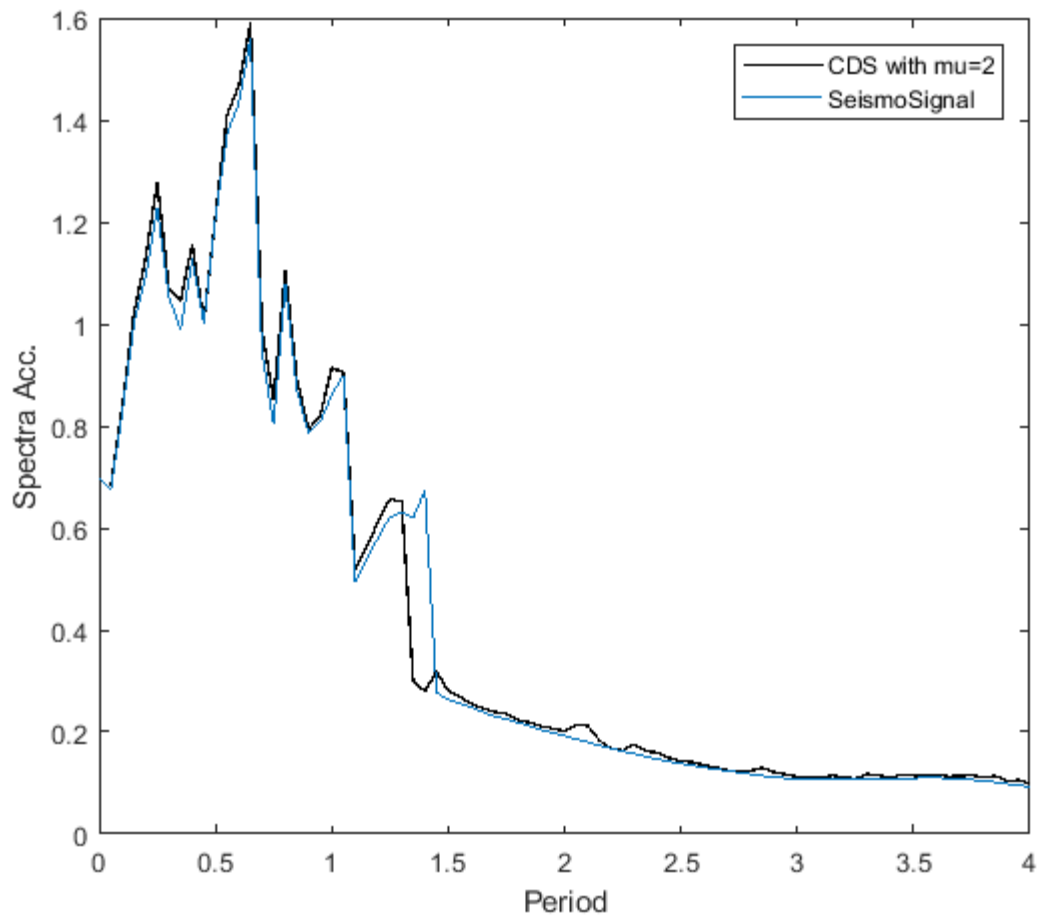
```
fileID = fopen('input/RSN1044_Damping2.txt');  
for idx = 1:5  
    fgetl(fileID);  
end  
C = textscan(fileID, repmat('%f',1,15));  
fclose(fileID);
```

Output

Plot spectral acceleration response spectra

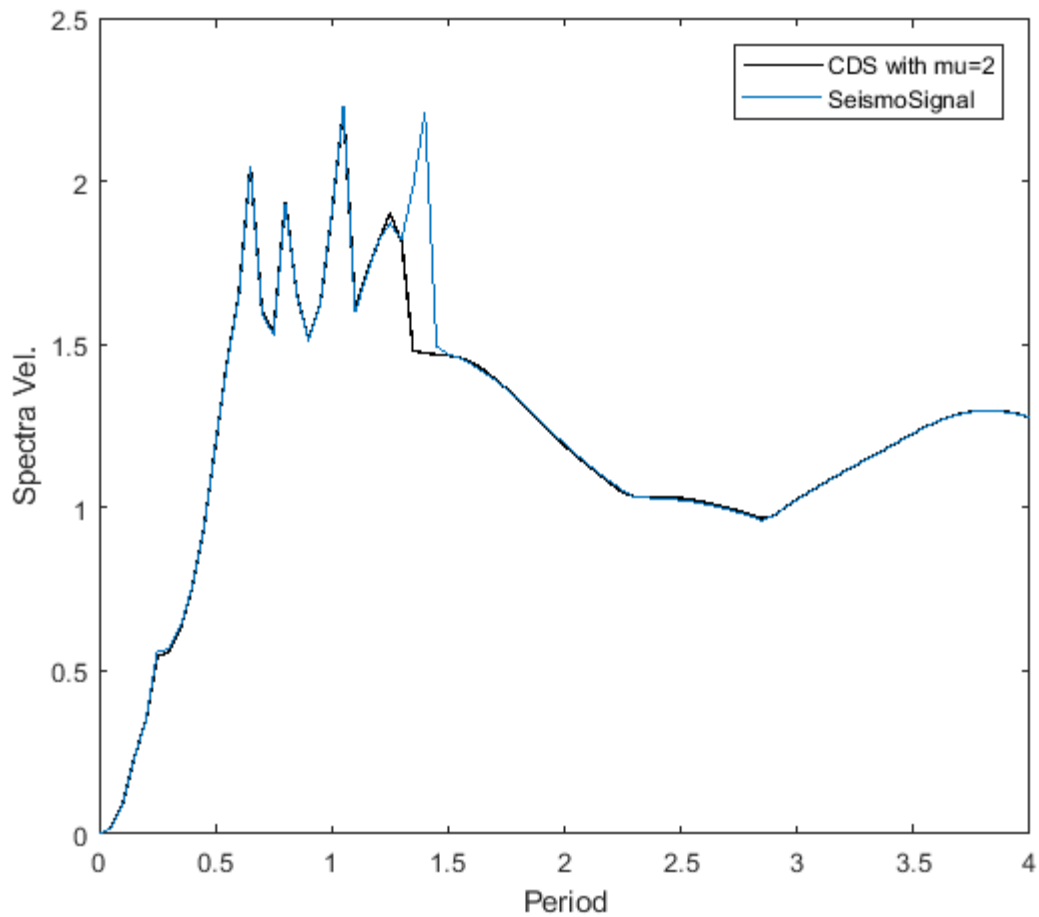
```
figure()  
plot(S1.Period,S1.CDSa/9.8,'k','LineWidth',1);  
hold on  
%plot(S2.Period,S2.Sa,'r','LineWidth',1);  
plot(C{1},C{3})  
legend('CDS with mu=2','SeismoSignal');  
xlabel('Period');  
ylabel('Spectra Acc.')
```

```
hold off
```



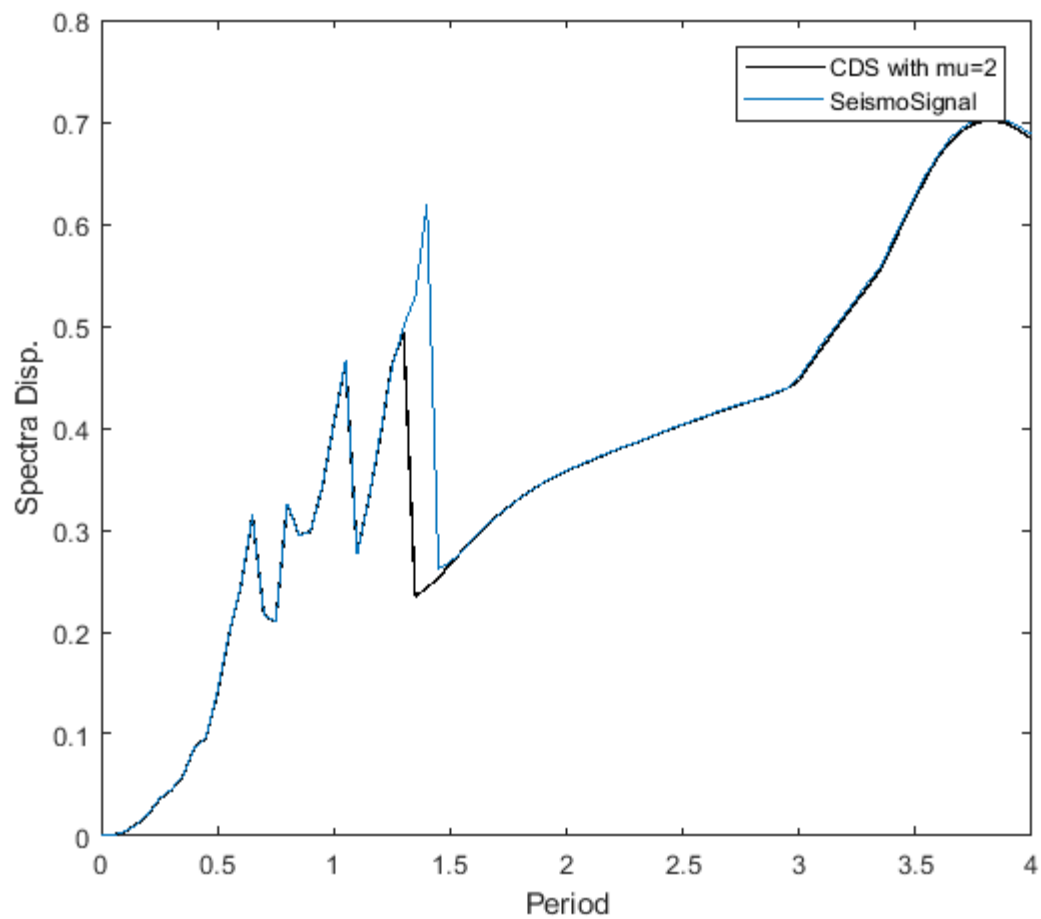
Plot spectral velocity response spectra

```
figure()
plot(S1.Period,S1.CDSv,'k','LineWidth',1);
hold on
%plot(S2.Period,S2.Sa,'r','LineWidth',1);
plot(C{1},C{7}/100)
legend('CDS with mu=2','SeismoSignal');
xlabel('Period');
ylabel('Spectra Vel.')
hold off
```



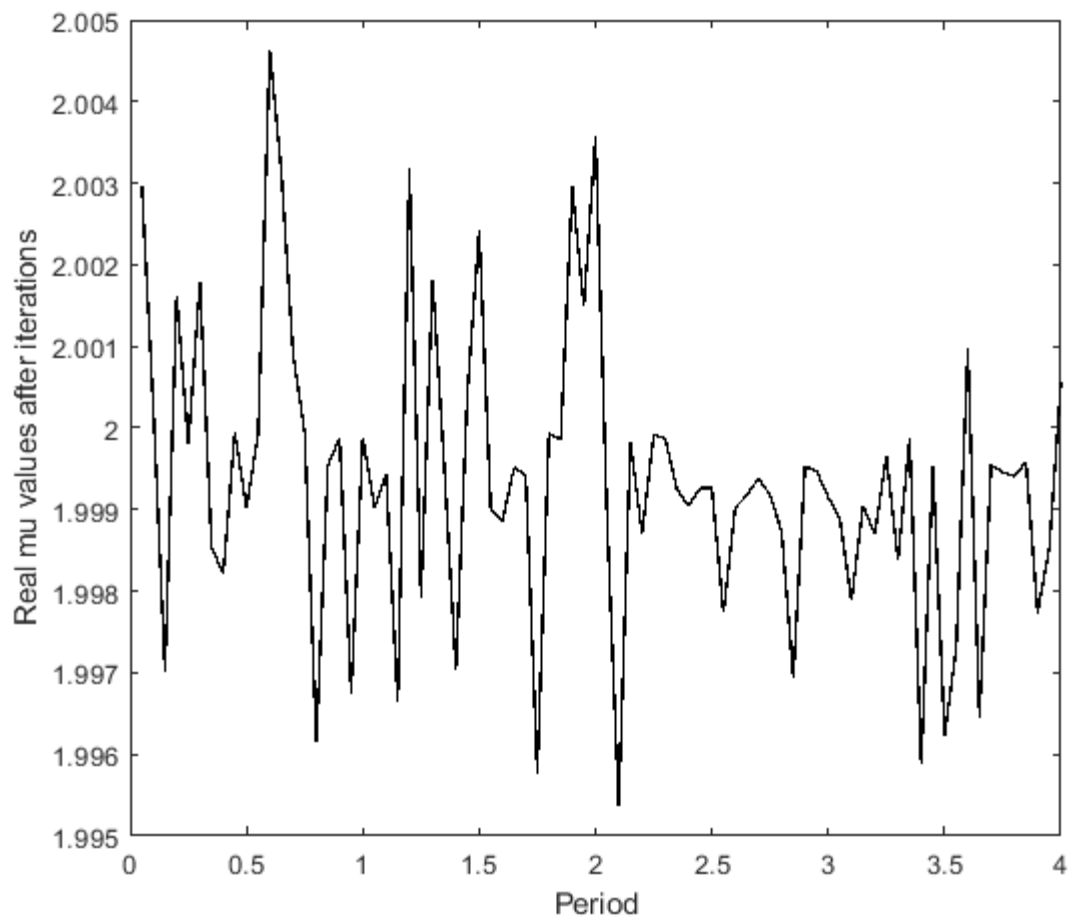
Plot spectral displacement response spectra

```
figure()
plot(S1.Period,S1.CDSd,'k','LineWidth',1);
hold on
%plot(S2.Period,S2.Sa,'r','LineWidth',1);
plot(C{1},C{11}/100)
legend('CDS with mu=2','SeismoSignal');
xlabel('Period');
ylabel('Spectra Disp.')
hold off
```



Plot the achieved ductility for each eigenperiod. It should be equal or close to the target ductility $\mu=2$

```
figure()
plot(S1.Period,S1.muK,'k','LineWidth',1);
xlabel('Period');
ylabel('Real mu values after iterations')
```



Verify the dynamic response history analysis of OpenSeismoMatlab

Calculate linear dynamic response of a MDOF shear building

Contents

- [Reference](#)
- [Description](#)
- [Load earthquake data](#)
- [Setup parameters for DRHA function](#)
- [Calculation of structural properties](#)
- [Calculate dynamic response](#)
- [Roof displacement time history](#)
- [Fifth-story shear time history](#)
- [Base shear time history](#)
- [Base moment time history](#)
- [Copyright](#)

Reference

Chopra, A. K. (2020). Dynamics of structures, Theory and Applications to Earthquake Engineering, 5th edition. Prentice Hall.

Description

The example 13.2.6 (Example: Five-Story Shear Frame) of the above reference is solved in this example. Consider the five-story shear frame of Fig.12.8.1 of the above reference, subjected to the El Centro ground motion. The lumped masses are equal to 45 Mg at each floor, the lateral stiffness of each story is 54.82 kN/cm and the height of each story is 4 m. The damping ratio for all natural modes is 0.05.

Load earthquake data

Earthquake acceleration time history of the El Centro earthquake will be used (El Centro, 1940, El Centro Terminal Substation Building)

```
fid=fopen('elcentro.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtt=text{1,2};
```

Setup parameters for DRHA function

Set the storey height of the structure in m.

```
h=4;
```

Set the number of degrees of freedom of the structure, which is equal to the number of its storeys.

```
nDOFs=5;
```

Set the lateral stiffness of each storey in N/m.

```
k=5.482e6;
```

Set the lumped mass at each floor in kg.

```
m=45e3;
```

Calculation of structural properties

Calculate the stiffness matrix of the structure in N/m.

```
K=k*ones(nDOFs,1);
```

Calculate the mass matrix of the structure.

```
M=m*ones(nDOFs,1);
```

Critical damping ratio

```
ksi=0.05;
```

Initial displacement

```
u0=zeros(nDOFs,1);
```

Initial velocity

```
ut0=zeros(nDOFs,1);
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Calculate dynamic response

Apply DRHA

```
[U,V,A,f,Es,Ed] = DRHA(K,M,dt,xgtd,ksi,u0,ut0,AlgID,rinf);
```

Base shear time history

```
FBeig=sum(f,1);
```

5th storey shear time history (5th DOF)

```
Feig=f(1,:);
```

Roof displacement time history (5th DOF)

```
Ueig=U(1,:);
```

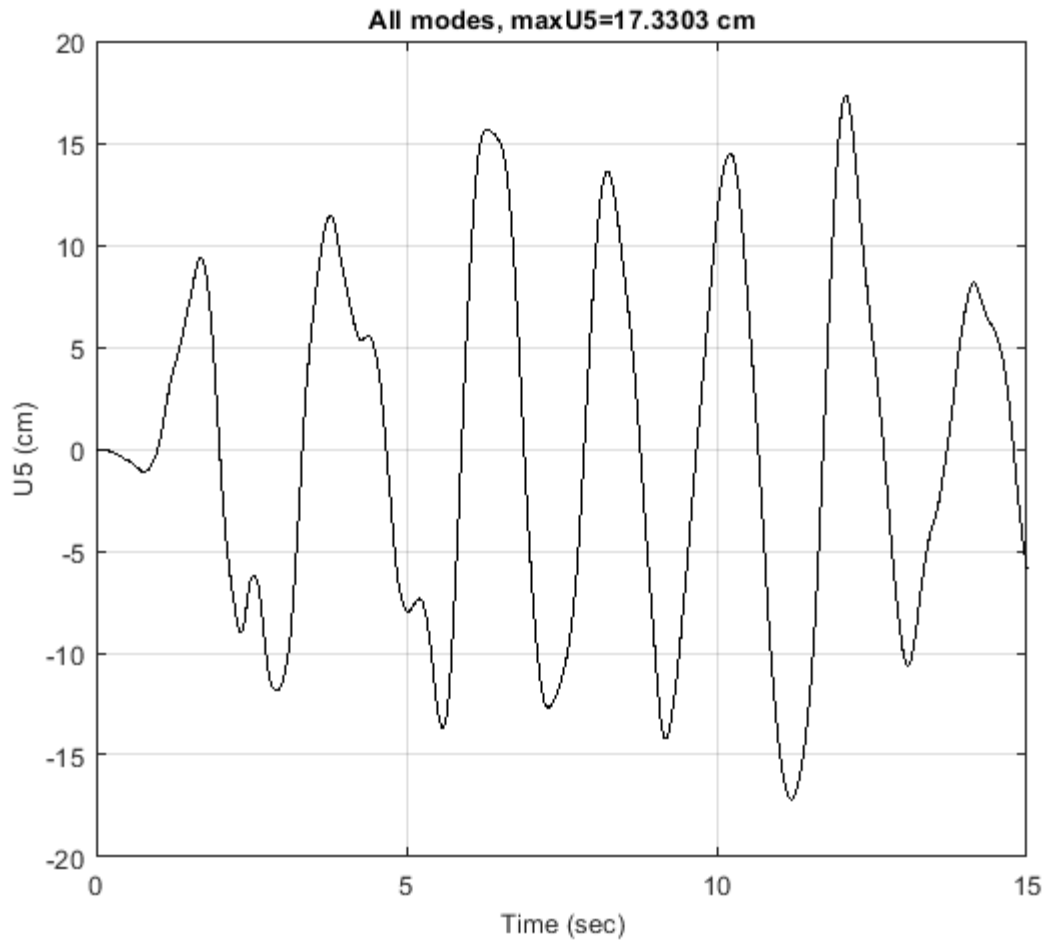
Base moment time history

```
MBeig=sum(f.*repmat((5*h:(-h):h)',1,size(f,2)),1);
```

Roof displacement time history

Plot the roof displacement time history. Convert displacements from m to cm. Verify with Figure 13.2.8 (left) of the above reference.

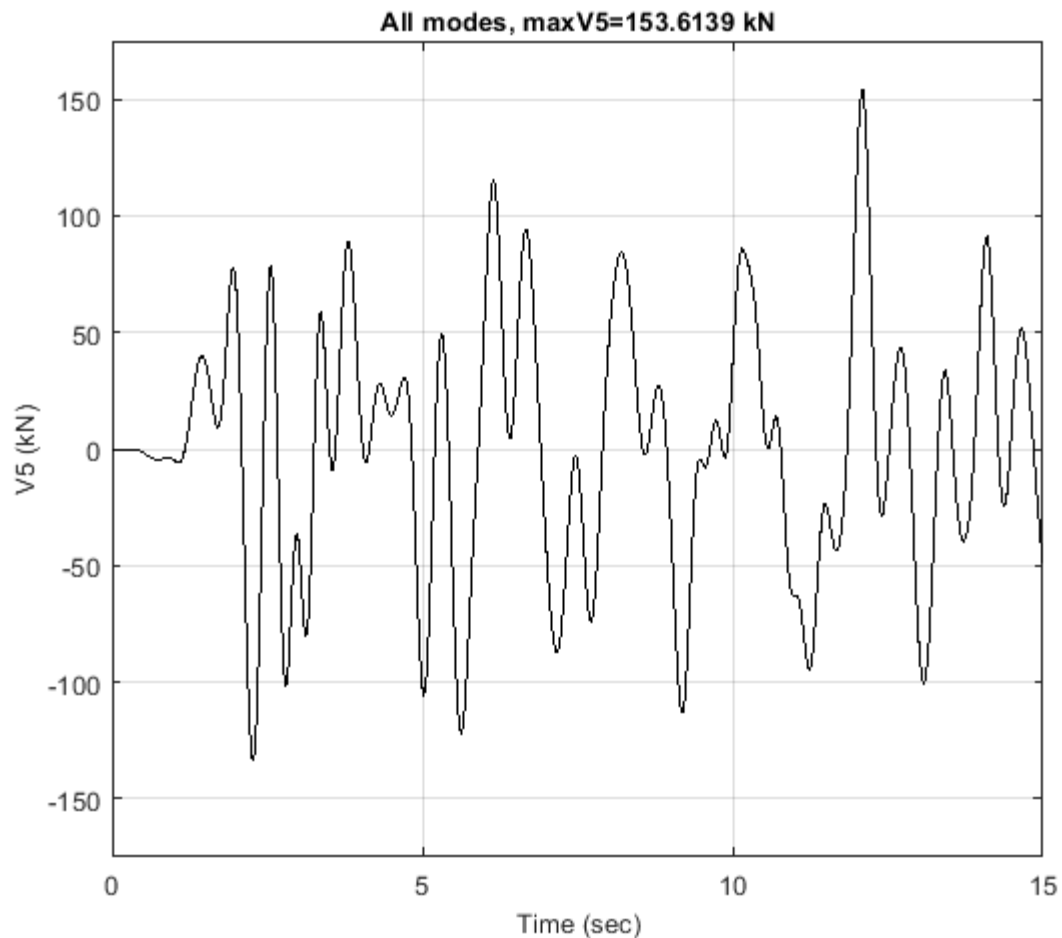
```
figure();
plot(t,100*Ueig,'LineWidth',1.5,'Marker','.',...
      'MarkerSize',1,'Color',[0 0 0],'markeredgecolor','k')
grid on
xlim([0,15])
ylim([-20,20])
xlabel('Time (sec)','FontSize',10);
ylabel('U5 (cm)','FontSize',10);
title(['All modes, maxU5=',num2str(max(abs(100*Ueig))),' cm'],...
      'FontSize',10)
```



Fifth-story shear time history

Plot the fifth-story shear time history. Convert forces from N to kN. Verify with Figure 13.2.7 (right) of the above reference.

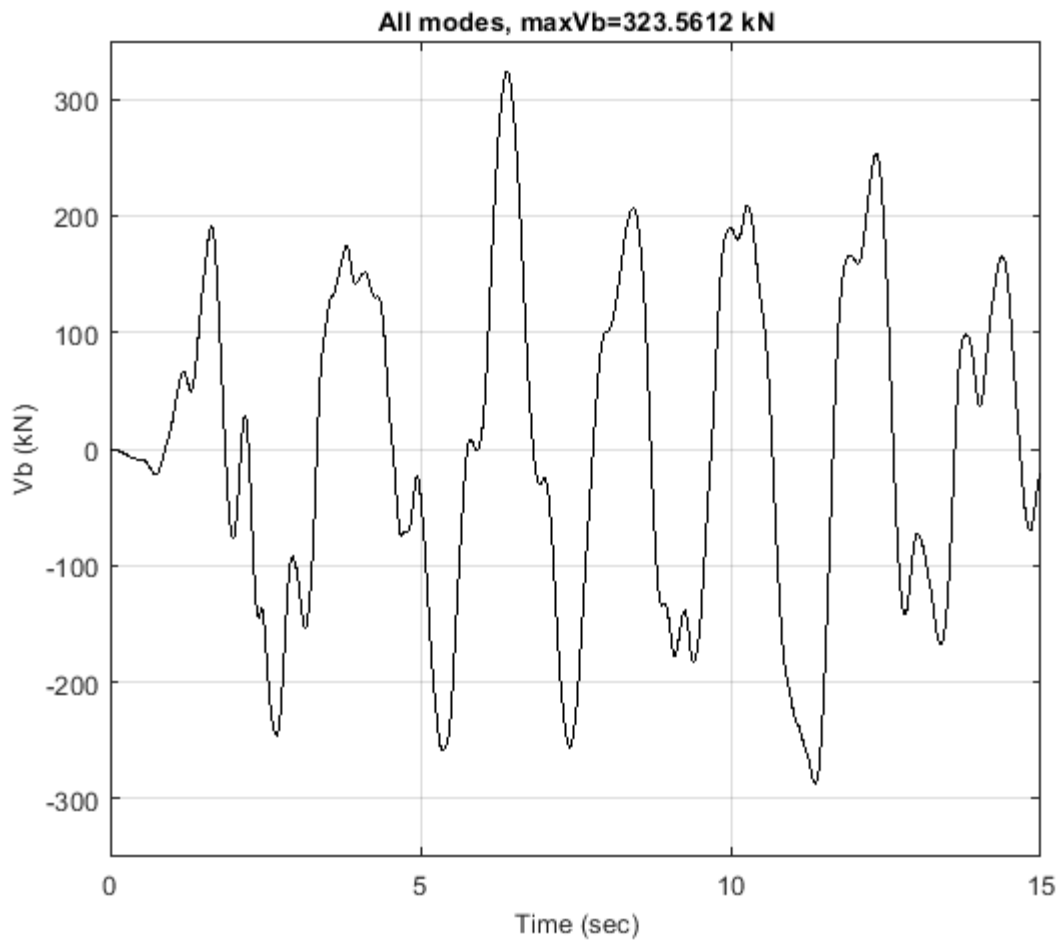
```
figure();
plot(t,Feig/1e3,'LineWidth',1.5,'Marker','.',...
     'MarkerSize',1,'Color',[0 0 0],'markeredgecolor','k')
grid on
xlim([0,15])
ylim([-175,175])
xlabel('Time (sec)','FontSize',10);
ylabel('V5 (kN)','FontSize',10);
title(['All modes, maxV5=',num2str(max(abs(Feig/1e3))),' kN'],...
      'FontSize',10)
```



Base shear time history

Plot the base shear time history. Convert forces from N to kN. Verify with Figure 13.2.7 (left) of the above reference

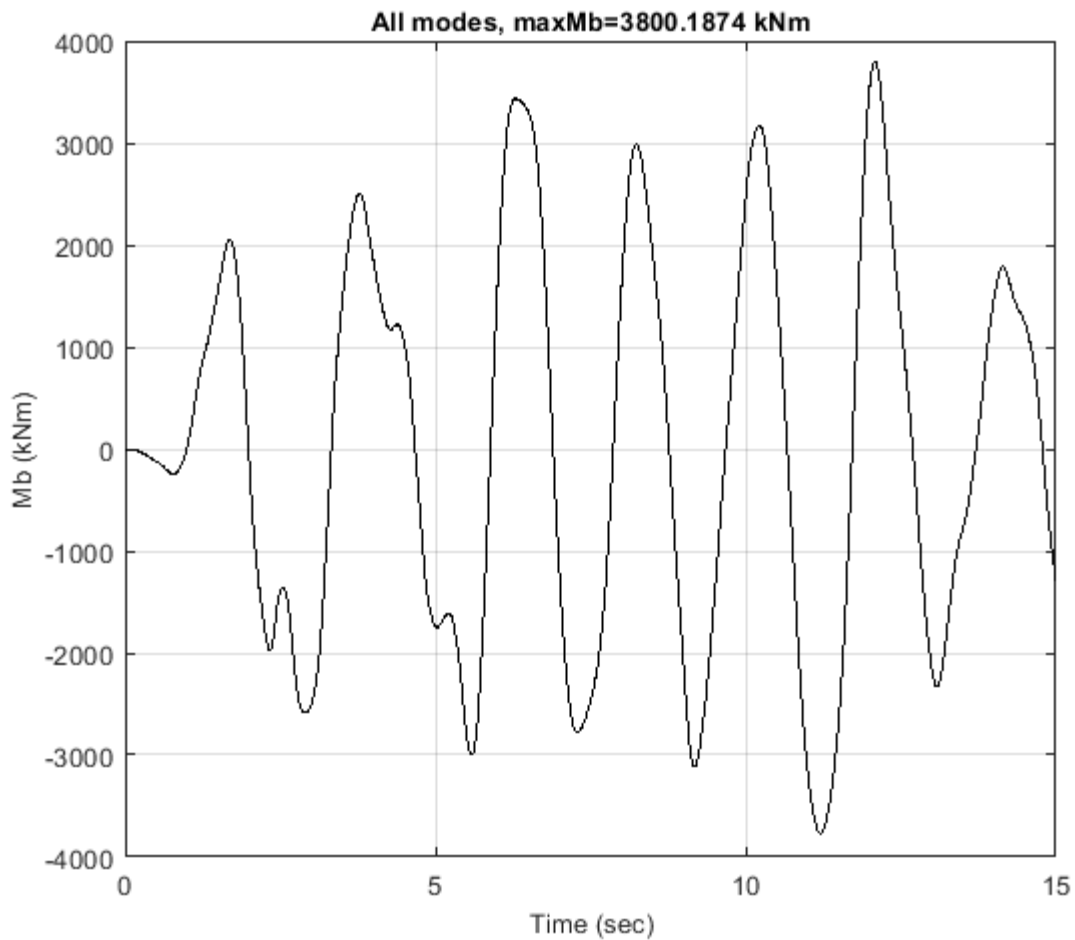
```
figure();
plot(t,FBeig/1e3,'LineWidth',1.5,'Marker','.',...
     'MarkerSize',1,'Color',[0 0 0],'markeredgecolor','k')
grid on
xlim([0,15])
ylim([-350,350])
xlabel('Time (sec)','FontSize',10);
ylabel('Vb (kN)','FontSize',10);
title(['All modes, maxVb=',num2str(max(abs(FBeig/1e3))),' kN'],...
      'FontSize',10)
```



Base moment time history

Plot the base moment time history. Convert moments from Nm to kNm. Verify with Figure 13.2.8 (right) of the above reference

```
figure();
plot(t,MBeig/1e3,'LineWidth',1.5,'Marker','.',...
     'MarkerSize',1,'Color',[0 0 0],'markeredgecolor','k')
grid on
xlim([0,15])
ylim([-4000,4000])
xlabel('Time (sec)','FontSize',10);
ylabel('Mb (kNm)','FontSize',10);
title(['All modes, maxMb=',num2str(max(abs(MBeig/1e3))),' kNm'],...
      'FontSize',10)
```



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Verify the high pass Butterworth filter of OpenSeismoMatlab

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Reference

Boore, D. M. (2005). On pads and filters: Processing strong-motion data. Bulletin of the Seismological Society of America, 95(2), 745-750.

Description

Verify Figure 1 of the above reference, for the 1940 El Centro analog recording. The displacements and velocities from unfiltered and filtered accelerations are shown. Filtering is done by using two passes of a fourth-order high pass (i.e. frequencies lower than the cut-off frequency are attenuated) Butterworth filter with cut-off frequency as shown in Figure 1.

Earthquake motion

Load earthquake data

```
eqmotions={'Imperial_Valley_El_Centro_9_EW'};
data=load([eqmotions{1},'.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgtt=data(:,2);
```

Apply high pass Butterworth filter

Switch

```
sw='butterworthhigh';
```

Order of Butterworth filter

```
bOrder=4;
```

Cut-off frequency

```
flc=0.1;
```

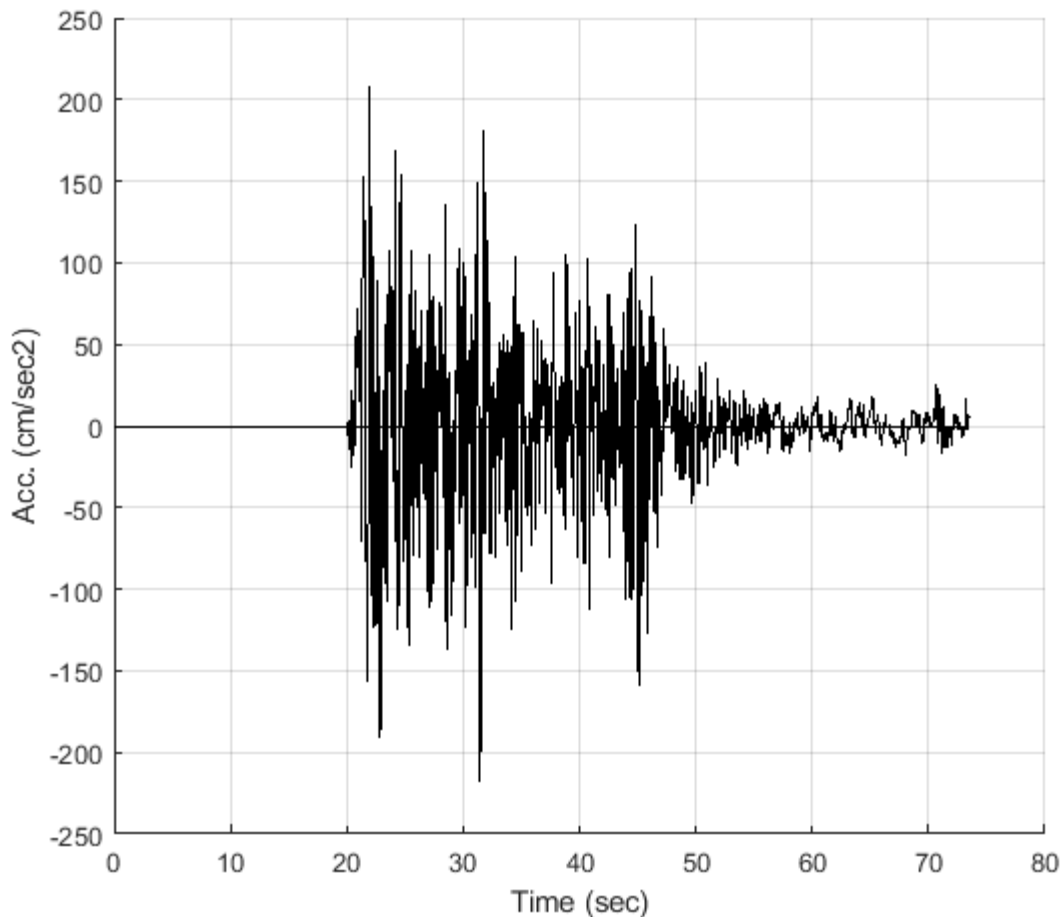
```
S1=OpenSeismoMatlab(dt,xgtt,sw,bOrder,flc);
```

Filtered acceleration

```
cxgtt=S1.acc;
```

Plot the time history of the initial ground motion

```
% Initialize figure
figure()
hold on
plot(t,zeros(size(t)),'k','LineWidth',1)
% Plot the acceleration time history of the initial ground motion
plot(t,xgtt,'k','LineWidth',1)
% Finalize figure
hold off
grid on
xlabel('Time (sec)')
ylabel('Acc. (cm/sec2)')
```



Obtain displacement and velocity time histories

Switch

```
sw='timehist';
```

Do not use baseline correction

```
baselineSw=false;
```

Apply OpenSeismoMatlab to the initial ground motion

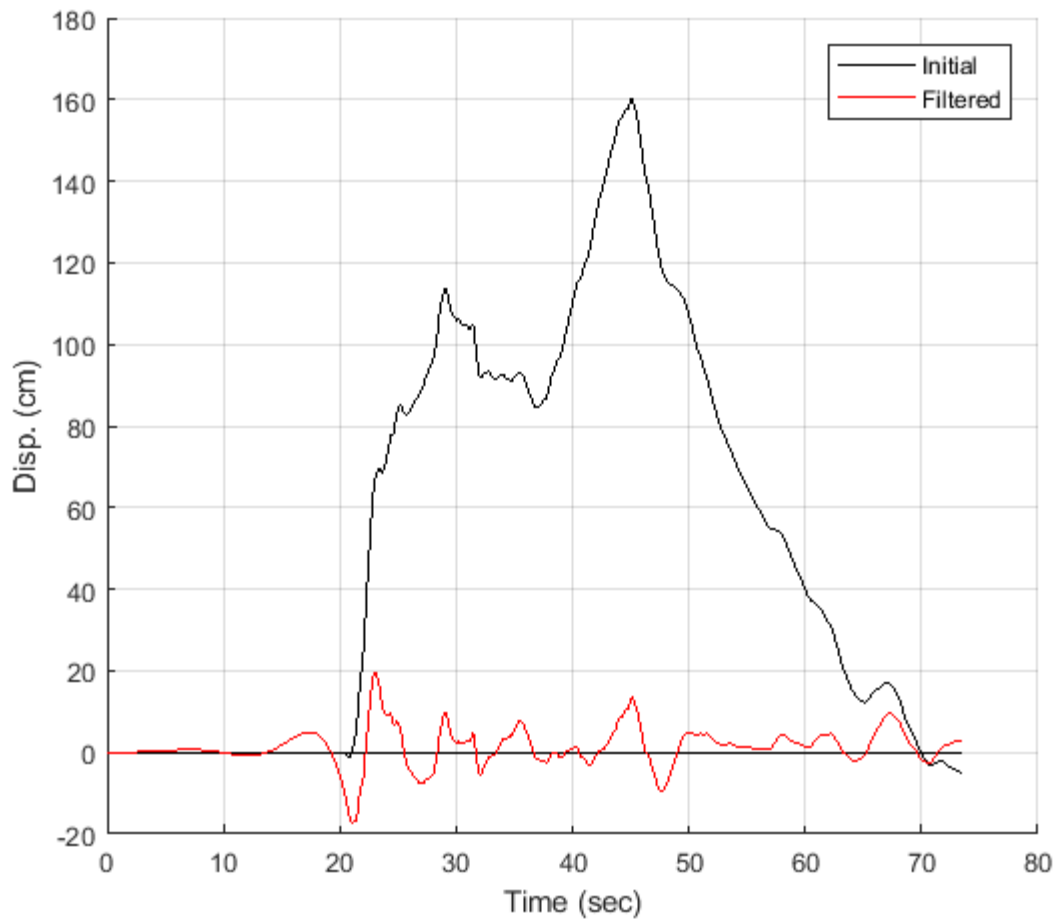
```
S2=OpenSeismoMatlab(dt,xgtt,sw,baselineSw);
```

Apply OpenSeismoMatlab to the filtered ground motion

```
S3=OpenSeismoMatlab(dt,cxgtt,sw,baselineSw);
```

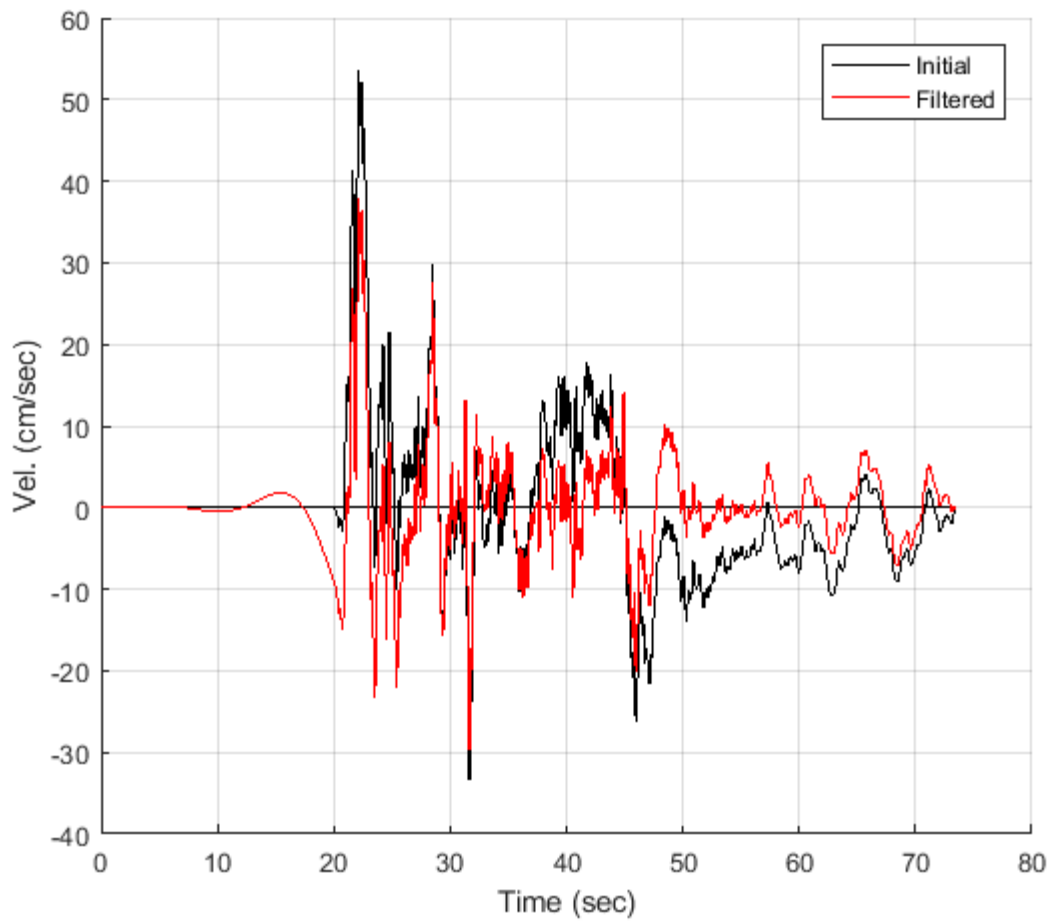
Plot the displacement time histories

```
% Initialize figure
figure()
hold on
plot(S3.time,zeros(size(S3.time)),'k','LineWidth',1)
% Plot the displacement time history of the initial ground motion
p1=plot(S2.time,S2 DISP,'k','LineWidth',1);
% Plot the displacement time history of the filtered ground motion
p2=plot(S3.time,S3 DISP,'r','LineWidth',1);
% Finalize figure
hold off
grid on
legend([p1,p2],{'Initial','Filtered'})
xlabel('Time (sec)')
ylabel('Disp. (cm)')
```

Plot the velocity time histories

```
% Initialize figure
figure()
hold on
plot(S3.time,zeros(size(S3.time)),'k','LineWidth',1)
% Plot the velocity time history of the initial ground motion
p1=plot(S2.time,S2.vel,'k','LineWidth',1);
% Plot the velocity time history of the filtered ground motion
p2=plot(S3.time,S3.vel,'r','LineWidth',1);
% Finalize figure
hold off
grid on
legend([p1,p2],{'Initial','Filtered'})
xlabel('Time (sec)')
ylabel('Vel. (cm/sec)')
```



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Verify the low- and high- pass Butterworth filter of OpenSeismoMatlab

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- [Plot the Fourier spectra](#)
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- [Plot the acceleration response spectra](#)
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Reference

Graizer, V. (2012, September). Effect of low-pass filtering and re-sampling on spectral and peak ground acceleration in strong-motion records. In Proceedings of the 15th World Conference of Earthquake Engineering, Lisbon, Portugal (pp. 24-28).

Description

Verify Figure 3.2 of the above reference, for the the MW 6.3 Christchurch, New Zealand earthquake at Heathcote Valley Primary School (HVSC) station, Up-component. The time histories, elastic response spectra and Fourier spectra from unfiltered and filtered accelerations are shown and compared. In the above reference, the ground motion was processed following the 1970s Caltech procedure, low-pass filtered and re-sampled to 50 samples/sec by the GeoNet New Zealand strong motion network. However in this example, Butterworth filter is applied and it gives similar results.

Earthquake motion

Load earthquake data

```
eqmotions={'Christchurch2011HVPS_UP'};
data=load([eqmotions{1},'.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgtt=data(:,2);
xgtt=[zeros(10/dt,1);xgtt];
t=(0:numel(xgtt)-1)*dt;
xgtt=xgtt/9.81;
```

Apply high pass Butterworth filter

Switch

```
sw='butterworthhigh';
```

Order of Butterworth filter

```
bOrder=4;
```

Cut-off frequency

```
flc=0.1;
```

Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw,bOrder,flc);
```

Filtered acceleration

```
cxgtt=S1.acc;
```

Apply low pass Butterworth filter

Switch

```
sw='butterworthlow';
```

Order of Butterworth filter

```
bOrder=4;
```

Cut-off frequency

```
fuc=25;
```

Apply OpenSeismoMatlab to high pass filtered filtered acceleration

```
S2=OpenSeismoMatlab(dt,cxgtt,sw,bOrder,fuc);
```

Filtered acceleration

```
cxgtt=S2.acc;
```

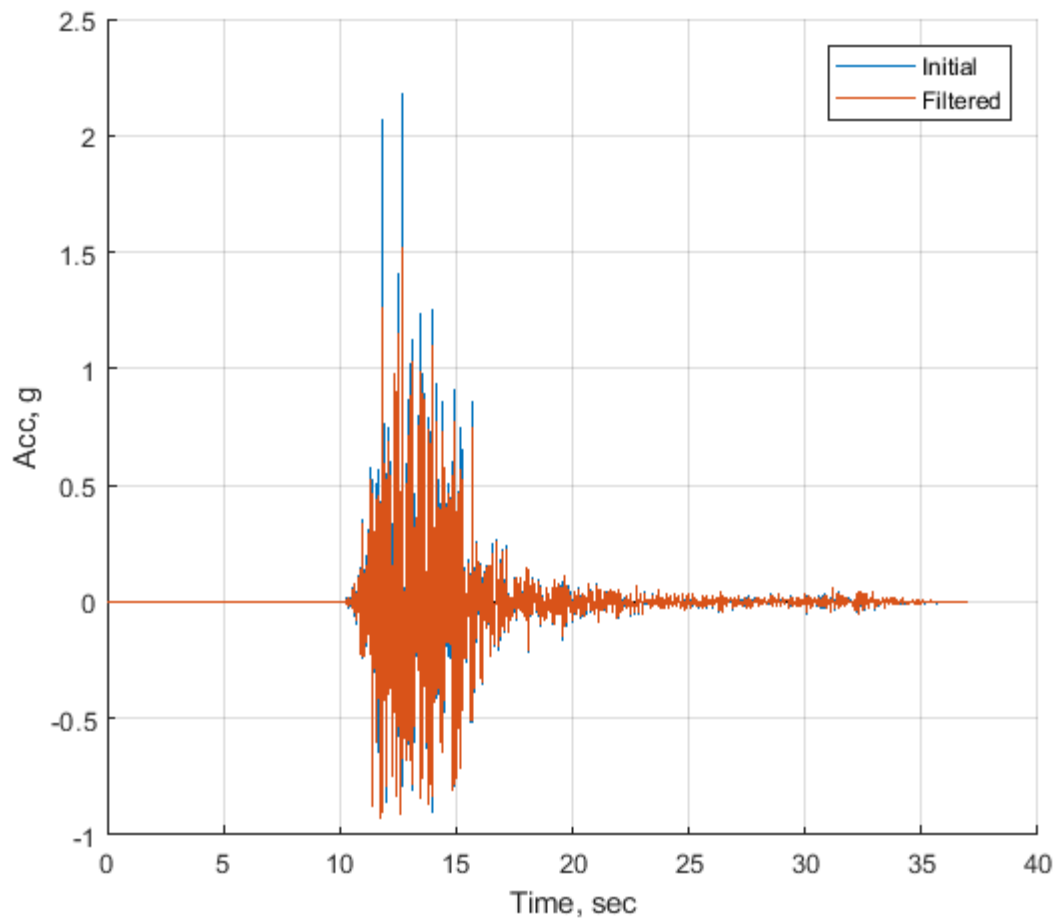
Plot the acceleration time histories

```
% Initialize figure
figure()
hold on
plot(t,zeros(size(t)),'k','LineWidth',1)
% Plot the acceleration time history of the initial ground motion
p1=plot(t,xgtt);
% Plot the acceleration time history of the bandpass filtered ground motion
```

```

p2=plot(t,cxgtt);
% Finalize figure
hold off
grid on
legend([p1,p2],{'Initial','Filtered'})
xlabel('Time, sec')
ylabel('Acc, g')

```



Calculate the Fourier spectra

Switch

```
sw='fs';
```

Apply OpenSeismoMatlab to the initial ground motion

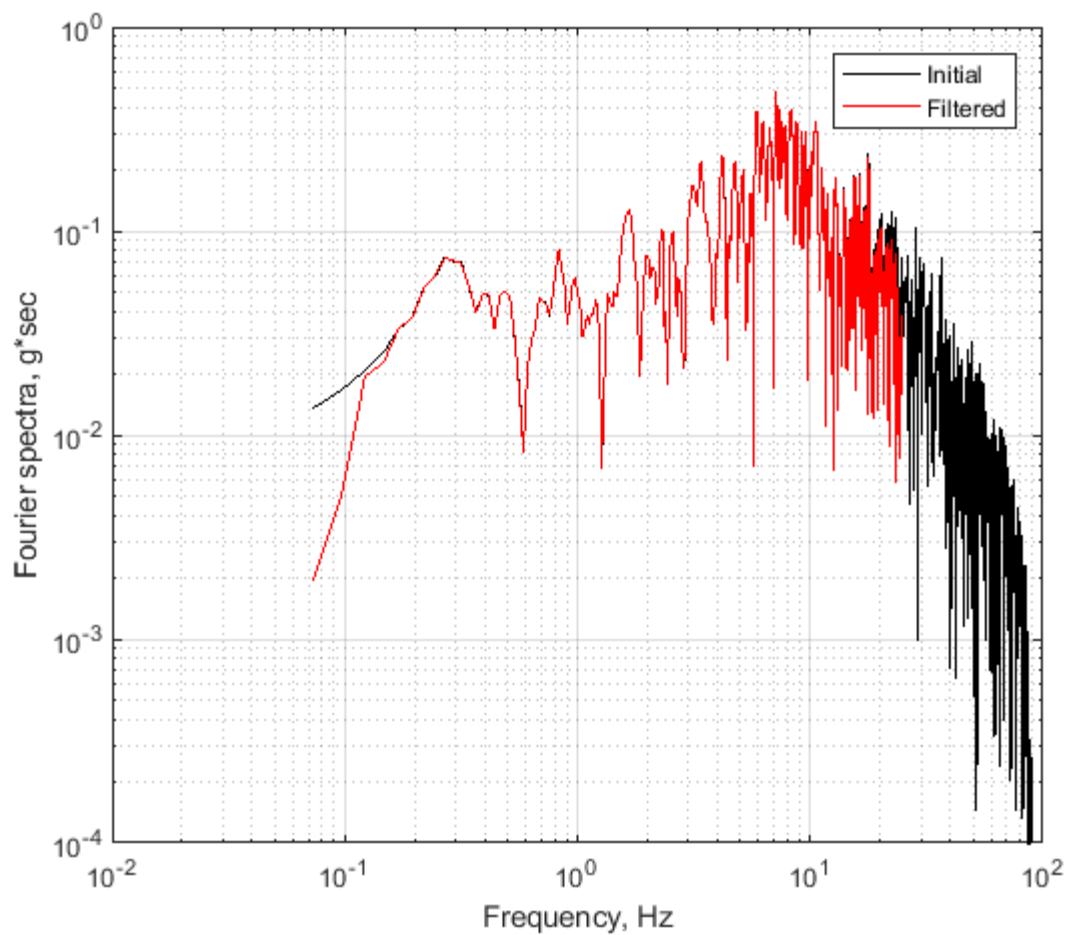
```
S3=OpenSeismoMatlab(dt,xgtt,sw);
```

Apply OpenSeismoMatlab to the filtered ground motion

```
S4=OpenSeismoMatlab(dt,cxgtt,sw);
```

Plot the Fourier spectra

```
% Initialize figure
figure()
loglog(1,1,'w')
hold on
% Plot the Fourier spectrum of the initial ground motion in logarithmic
% scale for frequencies larger than 0.05 Hz
ind10=S4.freq>=0.05;
p1=loglog(S3.freq(ind10),S3.FAS(ind10),'k','LineWidth',1);
% Plot the Fourier spectrum of the filtered ground motion in logarithmic
% scale for frequencies larger than 0.05 Hz and lower than fuc
ind11=(S4.freq<=fuc)& (S4.freq>=0.05);
p2=loglog(S4.freq(ind11),S4.FAS(ind11),'r','LineWidth',1);
% Finalize figure
hold off
grid on
ylim([1e-4,1])
legend([p1,p2],{'Initial','Filtered'})
xlabel('Frequency, Hz')
ylabel('Fourier spectra, g*sec')
```



Calculate the acceleration response spectra

Switch

```
sw='es';
```

Critical damping ratio

```
ksi=0.05;  
% Period range for which the response spectrum is queried  
T=logspace(1,-2,100);
```

Apply OpenSeismoMatlab to the initial ground motion

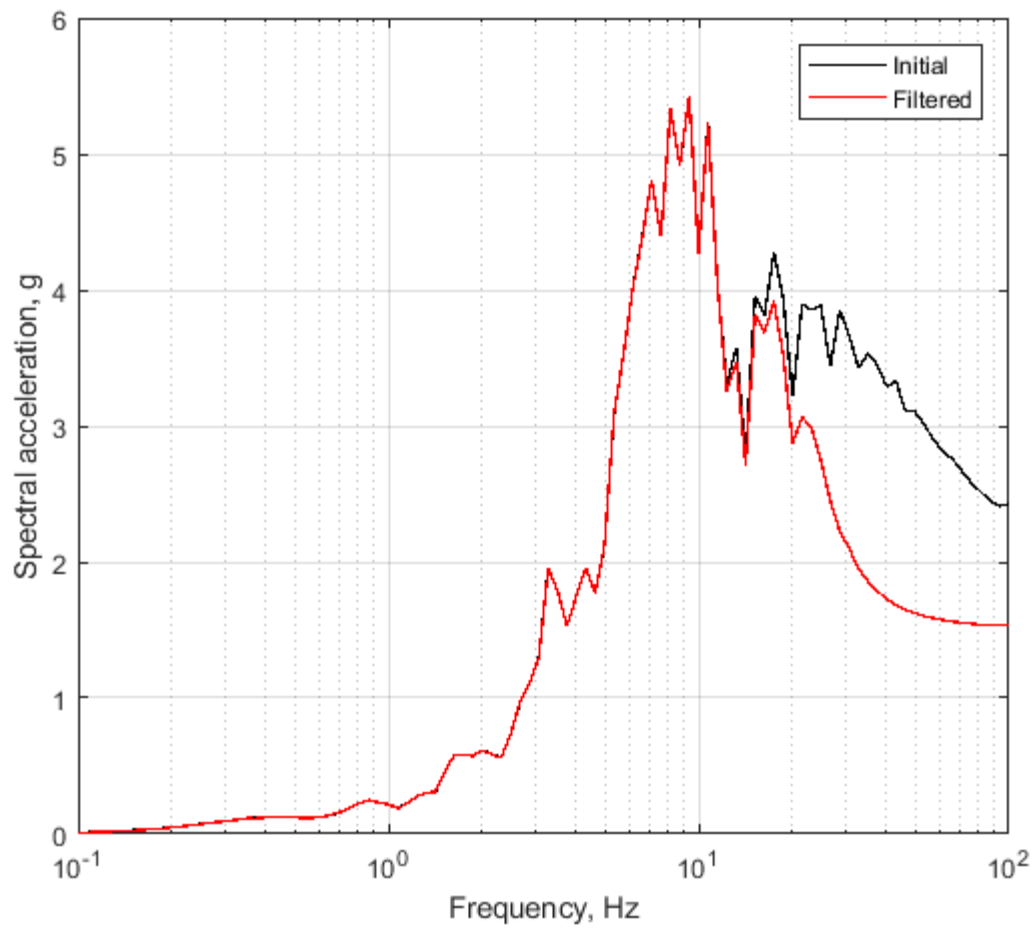
```
S5=OpenSeismoMatlab(dt,xgtt,sw,T,ksi);
```

Apply OpenSeismoMatlab to the filtered ground motion

```
S6=OpenSeismoMatlab(dt,cxgtt,sw,T,ksi);
```

Plot the acceleration response spectra

```
% Initialize figure  
figure()  
semilogx(1,1,'w')  
hold on  
% Plot the acceleration response spectrum of the initial ground motion in  
% logarithmic scale  
p1=semilogx(1./S5.Period,S5.Sa,'k','LineWidth',1);  
% Plot the acceleration response spectrum of the filtered ground motion in  
% logarithmic scale  
p2=semilogx(1./S6.Period,S6.Sa,'r','LineWidth',1);  
% Finalize figure  
hold off  
grid on  
legend([p1,p2],{'Initial','Filtered'})  
xlabel('Frequency, Hz')  
ylabel('Spectral acceleration, g')
```



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Verify the Fourier amplitude spectrum of OpenSeismoMatlab

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Reference

Analyses of strong motion earthquake accelerograms, Volume IV - Fourier Amplitude Spectra, Part H - Accelerograms I1H115 through I1H126, California Institute of Technology, Earthquake Engineering Research Laboratory, Report No. EERI 74-100, 1974.

Description

Verify the Fourier amplitude spectrum at page 12 of the above reference for the San Fernando earthquake, Feb 9, 1971, 0600 PST, IVH115 71.024.0 15250 Ventura BLVD., basement, Los Angeles, Cal. Component N11E.

Earthquake motion

Load earthquake data

```
eqmotions={'SanFernando1971VenturaBlvdBasement15250LosAngelesCalN11E'};  
data=load([eqmotions{1},'.dat']);  
t=data(:,1);  
dt=t(2)-t(1);  
xgtt=100*data(:,2);
```

Calculate the Fourier amplitude spectrum

Switch

```
sw='fs';
```

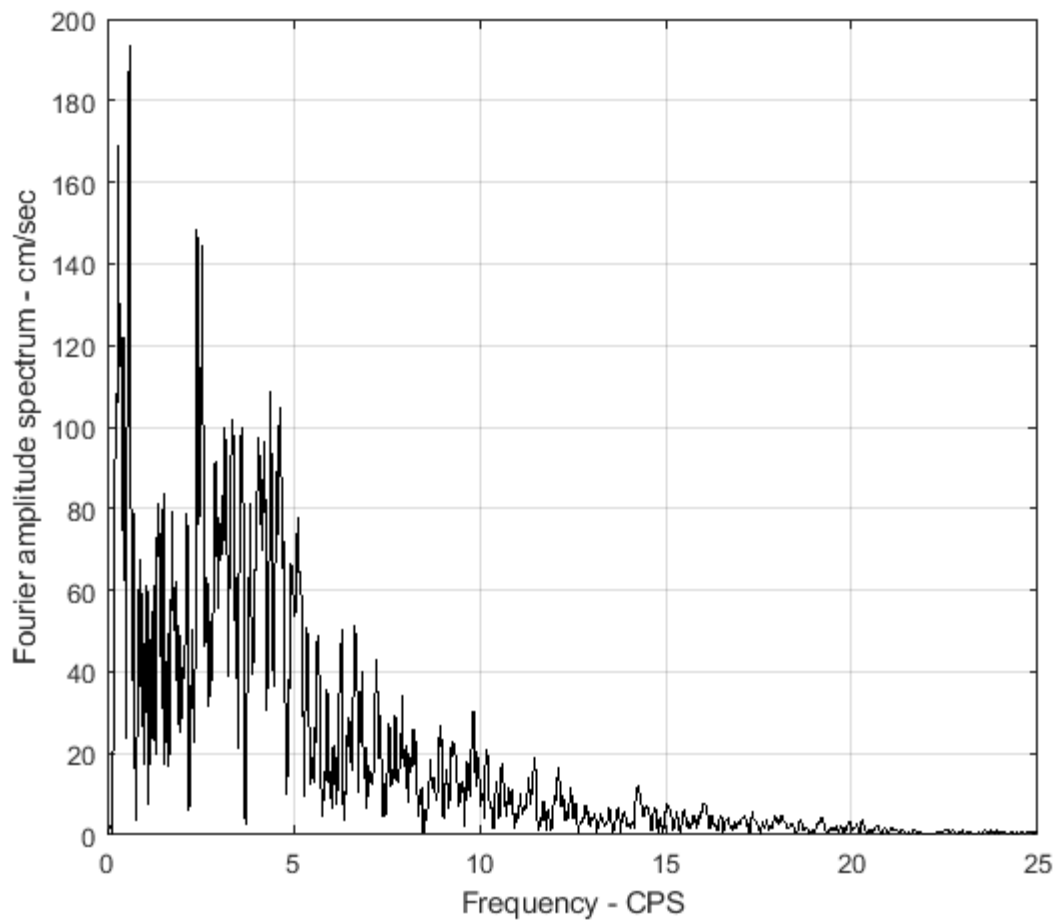
Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw);
```

Plot the Fourier amplitude spectrum

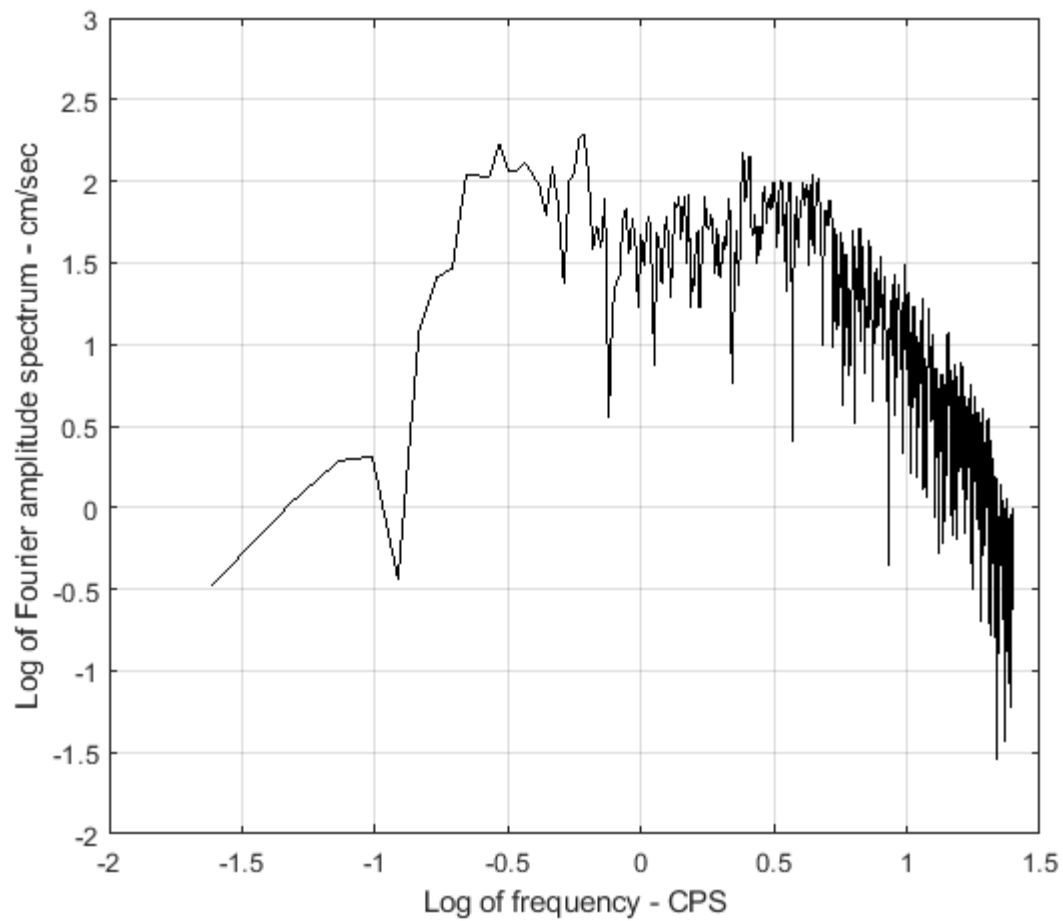
```
% Initialize figure  
figure()  
% Plot the Fourier amplitude spectrum on page 12 of the above reference  
plot(S1.freq,S1.FAS,'k','LineWidth',1)  
% Finalize figure  
grid on
```

```
xlabel('Frequency - CPS')
ylabel('Fourier amplitude spectrum - cm/sec')
ylim([0,200])
xlim([0,25])
```



Plot the Fourier amplitude spectrum in logarithmic scale

```
% Initialize figure
figure()
% Plot the Fourier amplitude spectrum on page 13 of the above reference
plot(log10(S1.freq),log10(S1.FAS),'k','LineWidth',1)
% Finalize figure
grid on
xlabel('Log of frequency - CPS')
ylabel('Log of Fourier amplitude spectrum - cm/sec')
ylim([-2,3])
xlim([-2,1.5])
```



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Reference

Analyses of strong motion earthquake accelerograms, Volume IV - Fourier Amplitude Spectra, Part H - Accelerograms I1H115 through I1H126, California Institute of Technology, Earthquake Engineering Research Laboratory, Report No. EERI 74-100, 1974.

Description

Verify the Fourier amplitude spectrum at page 14 of the above reference for the San Fernando earthquake, Feb 9, 1971, 0600 PST, IVH115 71.024.0 15250 Ventura BLVD., basement, Los Angeles, Cal. Component N79W.

Earthquake motion

Load earthquake data

```
eqmotions={'SanFernando1971VenturaBlvdBasement15250LosAngelesCalN79W'};  
data=load([eqmotions{1},'.dat']);  
t=data(:,1);  
dt=t(2)-t(1);  
xgtt=100*data(:,2);
```

Calculate the Fourier amplitude spectrum

Switch

```
sw='fs';
```

Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw);
```

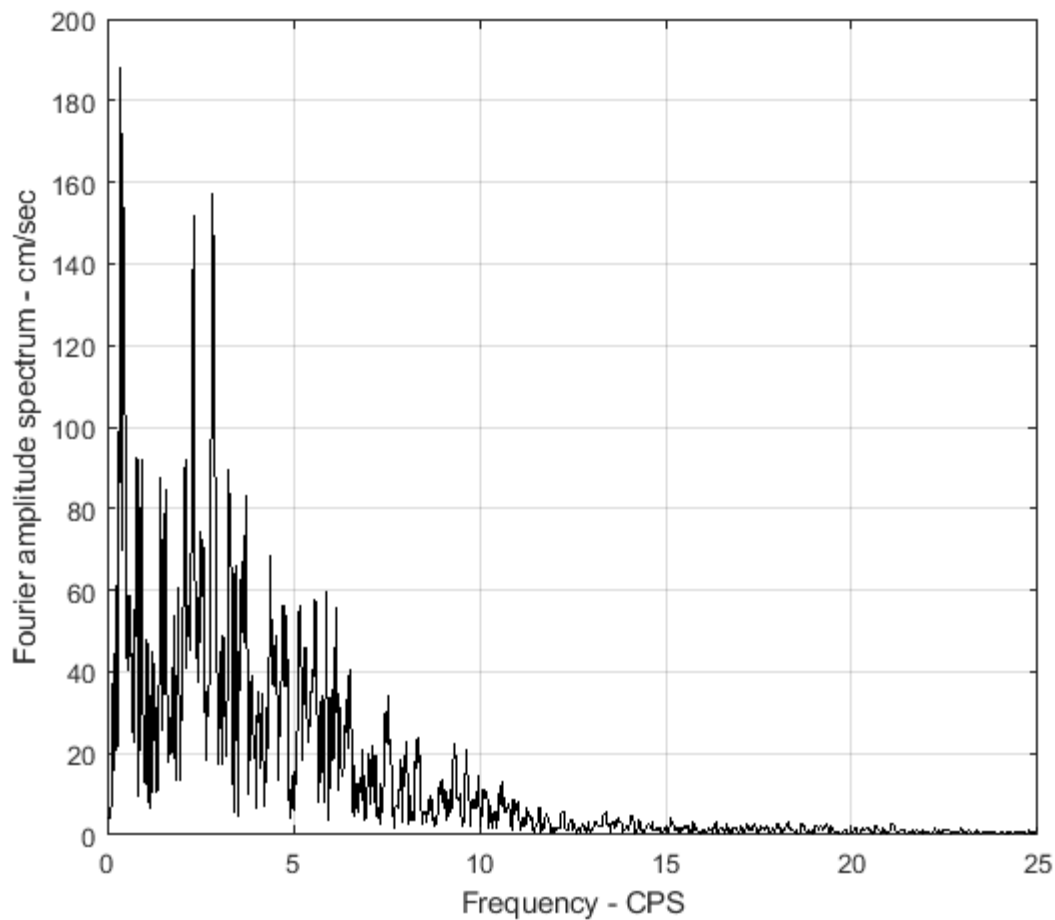
Plot the Fourier amplitude spectrum

```
% Initialize figure  
figure()  
% Plot the Fourier amplitude spectrum on page 14 of the above reference  
plot(S1.freq,S1.FAS,'k','LineWidth',1)  
% Finalize figure  
grid on
```

```

xlabel('Frequency - CPS')
ylabel('Fourier amplitude spectrum - cm/sec')
ylim([0,200])
xlim([0,25])

```

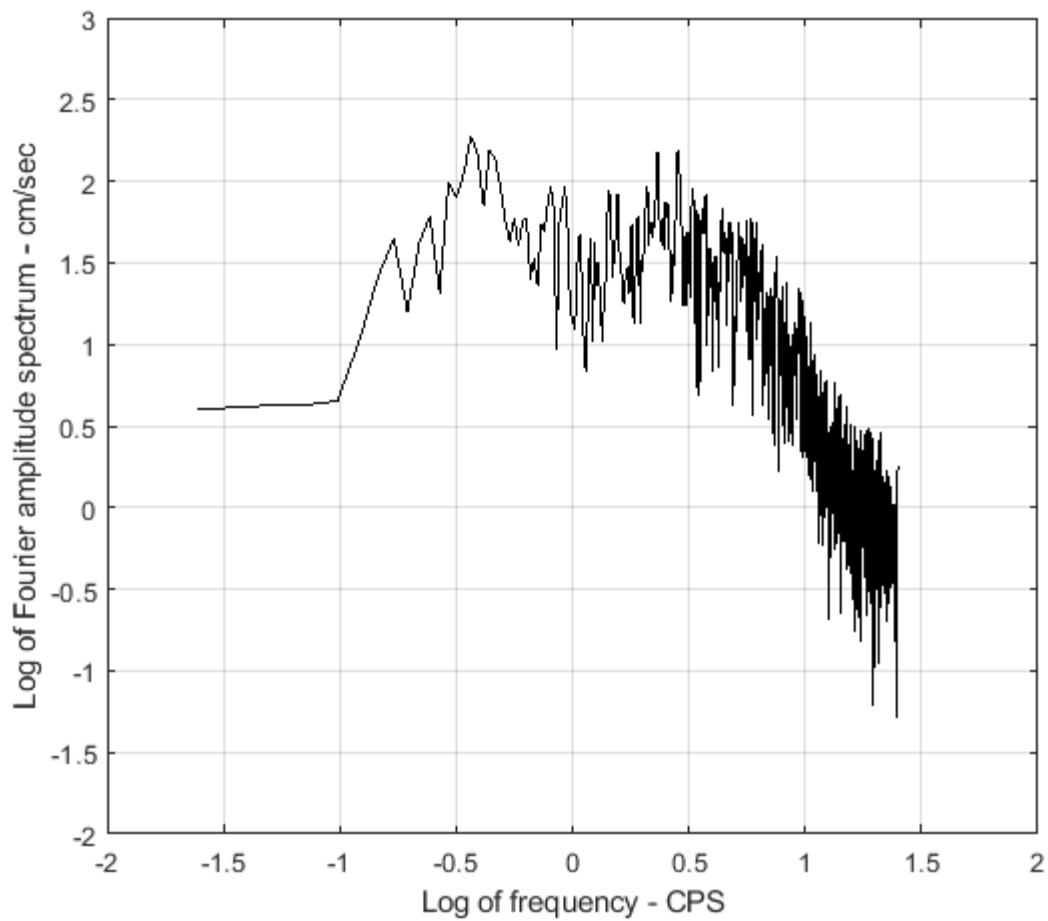


Plot the Fourier amplitude spectrum in logarithmic scale

```

% Initialize figure
figure()
% Plot the Fourier amplitude spectrum on page 15 of the above reference
plot(log10(S1.freq),log10(S1.FAS),'k','LineWidth',1)
% Finalize figure
grid on
xlabel('Log of frequency - CPS')
ylabel('Log of Fourier amplitude spectrum - cm/sec')
ylim([-2,3])
xlim([-2,2])

```



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Verify the incremental dynamic analysis of OpenSeismoMatlab

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Reference

Mashayekhi, M., Harati, M., Darzi, A., & Estekanchi, H. E. (2020). Incorporation of strong motion duration in incremental-based seismic assessments. *Engineering Structures*, 223, 111144.

Description

Incremental dynamic analysis (IDA) is performed for a non-degrading SDOF model with eigenperiod $T=1$ sec. The employed hysteretic model is a bilinear elastoplastic model used for non-degrading SDOF systems and is shown in Figure 17(a) of the above reference. An IDA analysis is performed with a ground motion the spectral acceleration of which resembles the red line of Figure 14 of the above reference, i.e. the ground motion must have $S_a(1\text{ sec})=0.382g$ (which is the Intensity Measure - IM) and the duration D_{5_75} must be roughly equal to 8.3 sec. An acceleration time history with such characteristics is shown in Figure 16(c) of the above reference. In this example, an arbitrary ground motion acceleration is loaded, which is then adjusted so that the resulting time history has $S_a(1\text{ sec})=0.382g$ and $D_{5_75}=8.3$ sec. The adjusted time history is plotted in this example and can be compared to Figure 16(c) of the above reference. Based on the above problem statement, the median response curve of Figure 18(a) of the above reference is verified.

Earthquake motion

Load earthquake data

```
egmotions={'LomaPrietaHallsValley90'};
data=load([egmotions{1}, '.dat']);
t=data(:,1);
dt=t(2)-t(1);
xgdt=data(:,2);
```

Adjust earthquake motion to have $D_{5_75}=8.3\text{sec}$

Switch

```
sw='arias';
```

Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtt,sw);
```

Duration D_5_75 of the initially loaded motion

```
S1.Td_5_75
```

```
ans =
```

```
7.759999999999999
```

S.Td_5_75 must be roughly near 8.3 sec, as required in Mashayekhi et al. (2020) We manipulate the strong shaking part of the motion which corresponds to the significant duration so that S.Td_5_75 is increased to the desired value (8.3 sec)

```
id1=find(t==S1.t_5_75(1));  
id2=find(t==S1.t_5_75(2));  
xgtt(id1:id2)=0.8*xgtt(id1:id2);
```

Calculate duration D_5_75 of adjusted earthquake motion

Switch

```
sw='arias';
```

Apply OpenSeismoMatlab

```
S2=OpenSeismoMatlab(dt,xgtt,sw);
```

Duration D_5_75 of the adjusted motion

```
S2.Td_5_75
```

```
ans =
```

```
8.359999999999999
```

Scale earthquake motion to have Sa(1 sec)=0.382g

Switch

```
sw='es';
```

Critical damping ratio


```
ksi=0.05;
```

Period where $S_a=0.382g$

```
T=1;
```

Apply OpenSeismoMatlab

```
S3=OpenSeismoMatlab(dt,xgtt,sw,T,ksi);
```

Spectral acceleration of the adjusted motion at 1 sec

```
S3.Sa
```

```
ans =  
  
1.286911370102642
```

S_a at 1 sec must be equal to $0.382g$, so we scale the entire acceleration time history up to this level

```
scaleF=0.382*9.81/S3.Sa;  
xgtt=xgtt*scaleF;
```

Calculate spectral acceleration of scaled earthquake motion

Switch

```
sw='es';
```

Critical damping ratio

```
ksi=0.05;
```

Period where $S_a=0.382g$

```
T=1;
```

Apply OpenSeismoMatlab

```
S4=OpenSeismoMatlab(dt,xgtt,sw,T,ksi);
```

Spectral acceleration of the adjusted motion at 1 sec

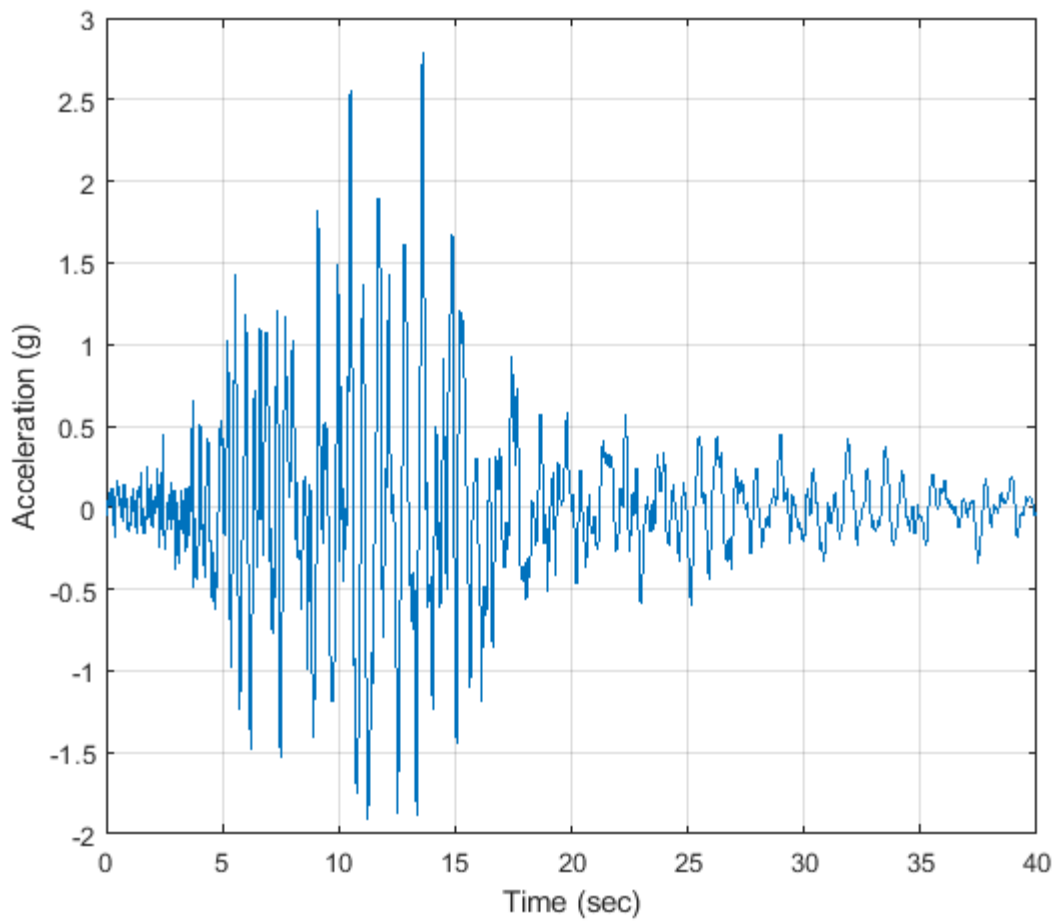
S4.Sa

ans =

3.747419999999983

Plot the acceleration time history

```
% Initialize figure
figure()
% Plot the acceleration time history of the adjusted motion
plot(t,xgtt)
% Finalize figure
grid on
xlabel('Time (sec)')
ylabel('Acceleration (g)')
```



Perform IDA analysis

Switch

```
sw='ida';
```

Eigenperiod

```
T=1;
```

Scaling factors

```
lambdaF=logspace(log10(0.001),log10(10),100);
```

Type of IDA analysis

```
IM_DM='Sa_disp';
```

Mass

```
m=1;
```

Yield displacement

```
uy = 0.082*9.81/(2*pi/T)^2;
```

Post yield stiffness factor

```
pysf=0.01;
```

Fraction of critical viscous damping

```
ksi=0.05;
```

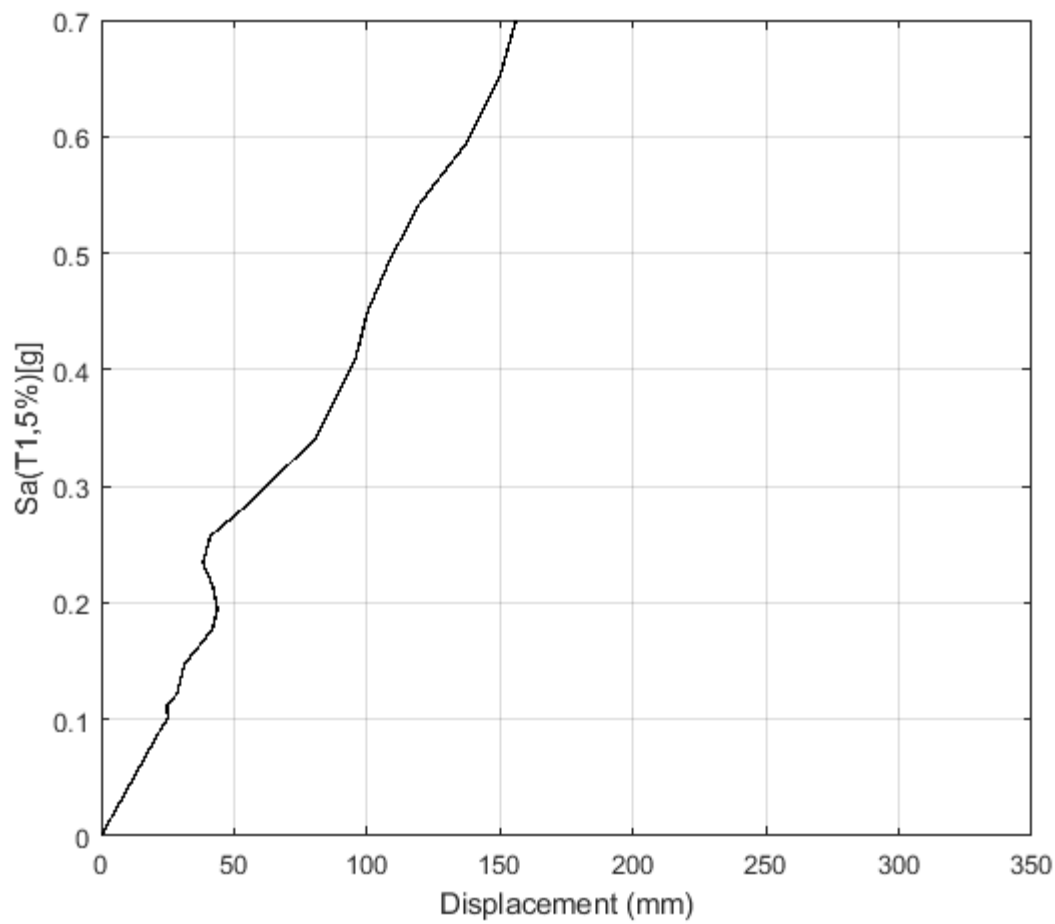
Apply OpenSeismoMatlab

```
S5=OpenSeismoMatlab(dt,xgtd,sw,T,lambdaF,IM_DM,m,uy,pysf,ksi);
```

Plot the displacement time histories

```
% Initialize figure
figure()
% Plot the response curve of the incremental dynamic analysis
plot(S5.DM*1000,S5.IM/9.81,'k','LineWidth',1)
% Finalize figure
grid on
xlabel('Displacement (mm)')
ylabel('Sa(T1,5%)[g]')
```

```
xlim([0,350])  
ylim([0,0.7])
```



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Verify the incremental dynamic analysis for multiple motions

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- [Setup parameters for IDA analysis](#)
- [Construct and plot the IDA curves in a loop](#)
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Reference

Deng, P., Pei, S., van de Lindt, J. W., Liu, H., & Zhang, C. (2017). An approach to quantify the influence of ground motion uncertainty on elastoplastic system acceleration in incremental dynamic analysis. *Advances in Structural Engineering*, 20(11), 1744-1756.

Description

Figure 4(a) of the above reference contains the IDA curves of an elastoplastic SDOF system under the Consortium of Universities for Research in Earthquake Engineering (CUREE) GM suite (Krawinkler et al., 2001), which were constructed using the maximum acceleration. In this example, an arbitrary suite of strong ground motions is selected and the maximum acceleration IDA curves are constructed similar to Figure 4(a) of the above reference. The IDA curves of this example strongly resemble those of that figure.

Earthquake motions

Load data from a suite of earthquakes

```
GM={ 'Cape Mendocino.dat';  
     'ChiChi.dat';  
     'Christchurch2011HVPS_UP.dat';  
     'Imperial Valley.dat';  
     'Imperial_Valley_El_Centro_9_EW.dat';  
     'Kobe.dat';  
     'Kocaeli.dat';  
     'San Fernando.dat';  
     'Spitak.dat'};  
n=size(GM,1);  
dt=cell(n,1);  
xgtt=cell(n,1);  
for i=1:n  
    fid=fopen(GM{i},'r');  
    text=textscan(fid,'%f %f');  
    fclose(fid);  
    t=text{1,1};  
    dt{i}=t(2)-t(1);  
    xgtt{i}=text{1,2};  
end
```

Setup parameters for IDA analysis

Switch

```
sw='ida';
```

Eigenperiod

```
T=1;
```

Scaling factors

```
lambdaF=logspace(log10(0.001),log10(10),100);
```

Type of IDA analysis

```
IM_DM= 'pgv_acc' ;
```

Mass

```
m=1;
```

Yield displacement

```
uy = 0.18*9.81/(2*pi/T)^2;
```

Post yield stiffness factor

```
pysf=0.01;
```

Fraction of critical viscous damping

```
ksi=0.05;
```

Algorithm to be used for the time integration

```
AlgID= 'U0-V0-Opt' ;
```

Set initial displacement

```
u0=0;
```

Set initial velocity

```
ut0=0;
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance for convergence

```
maxtol=0.01;
```

Maximum number of iterations per increment

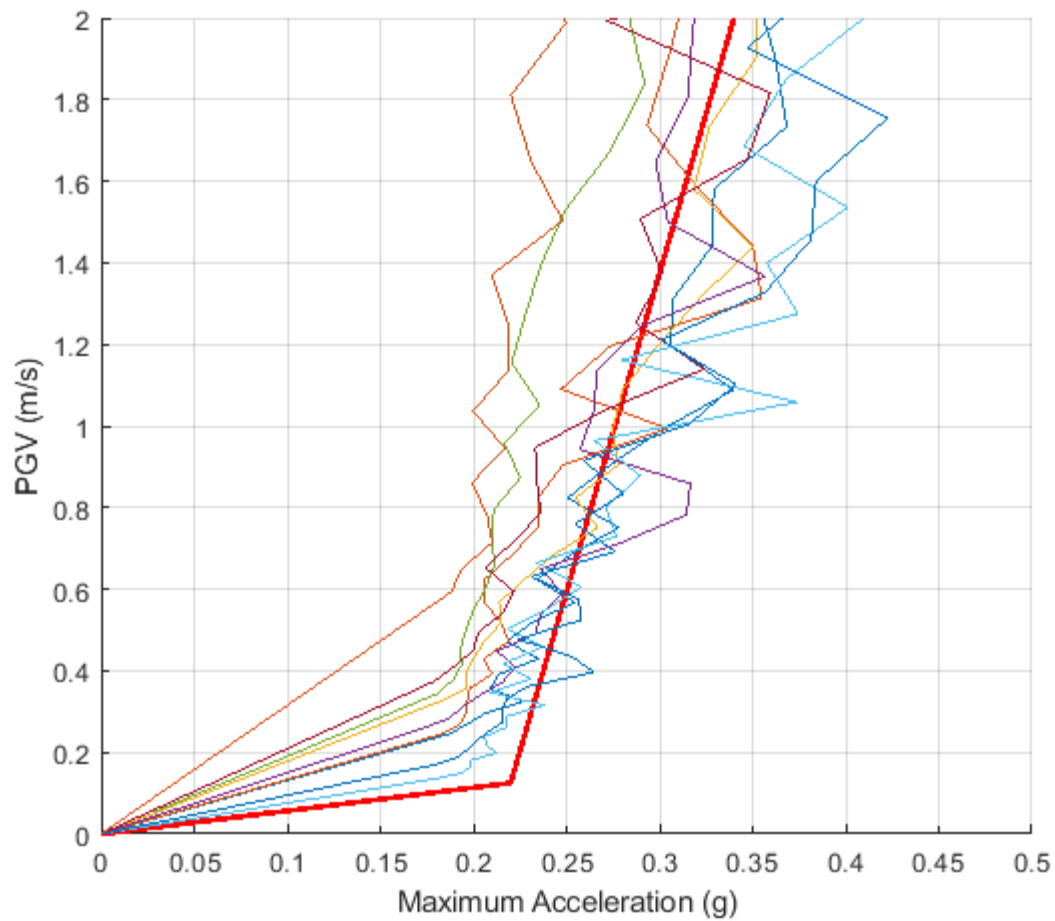
```
jmax=200;
```

Infinitesimal variation of acceleration

```
dak=eps;
```

Construct and plot the IDA curves in a loop

```
% Initialize figure
figure()
hold on
% Plot the red bold curve of Figure 4(a) of the above reference
plot([0,0.22,0.34],[0,0.125,2],'r','LineWidth',2)
for i=1:n
    % Apply OpenSeismoMatlab to calculate the ith IDA curve
    S1=OpenSeismoMatlab(dt{i},xgtt{i},sw,T,lambdAF,IM_DM,m,uy,pysf,ksi,AlgID,...
        u0,ut0,rinf,maxtol,jmax,dak);
    % Plot the ith IDA curve
    plot(S1.DM/9.81,S1.IM)
end
% Finalize figure
grid on
xlabel('Maximum Acceleration (g)')
ylabel('PGV (m/s)')
xlim([0,0.5])
ylim([0,2])
```



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Verify the incremental dynamic analysis for ductility response

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Reference

Vamvatsikos, D., & Cornell, C. A. (2002). Incremental dynamic analysis. Earthquake engineering & structural dynamics, 31(3), 491-514.

Description

The ductility response IDA curve of an elastoplastic SDOF system excited by the Loma Prieta, 1989, Halls Valley earthquake (component 090) is constructed at multiple levels of shaking, and compared to the curve shown in Figure 4(a) of the above reference. The SDOF system has $T=1$ sec and critical damping ratio 5%

Earthquake motion

Load earthquake data

```
GM='LomaPrietaHallsValley90.dat';
fid=fopen(GM,'r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtd=text{1,2};
```

Perform IDA analysis

Switch

```
sw='ida';
```

Eigenperiod

```
T=1;
```

Scaling factors

```
lambdaF=logspace(log10(0.01),log10(30),100);
```

Type of IDA analysis

```
IM_DM= 'Sa_mu' ;
```

Mass

```
m=1 ;
```

Yield displacement

```
uy=0.25 ;
```

Post yield stiffness factor

```
pysf=0.01 ;
```

Fraction of critical viscous damping

```
ksi=0.05 ;
```

Algorithm to be used for the time integration

```
AlgID= 'U0-V0-Opt' ;
```

Set initial displacement

```
u0=0 ;
```

Set initial velocity

```
ut0=0 ;
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1 ;
```

Maximum tolerance for convergence

```
maxtol=0.01 ;
```

Maximum number of iterations per increment

```
jmax=200 ;
```

Infinitesimal variation of acceleration

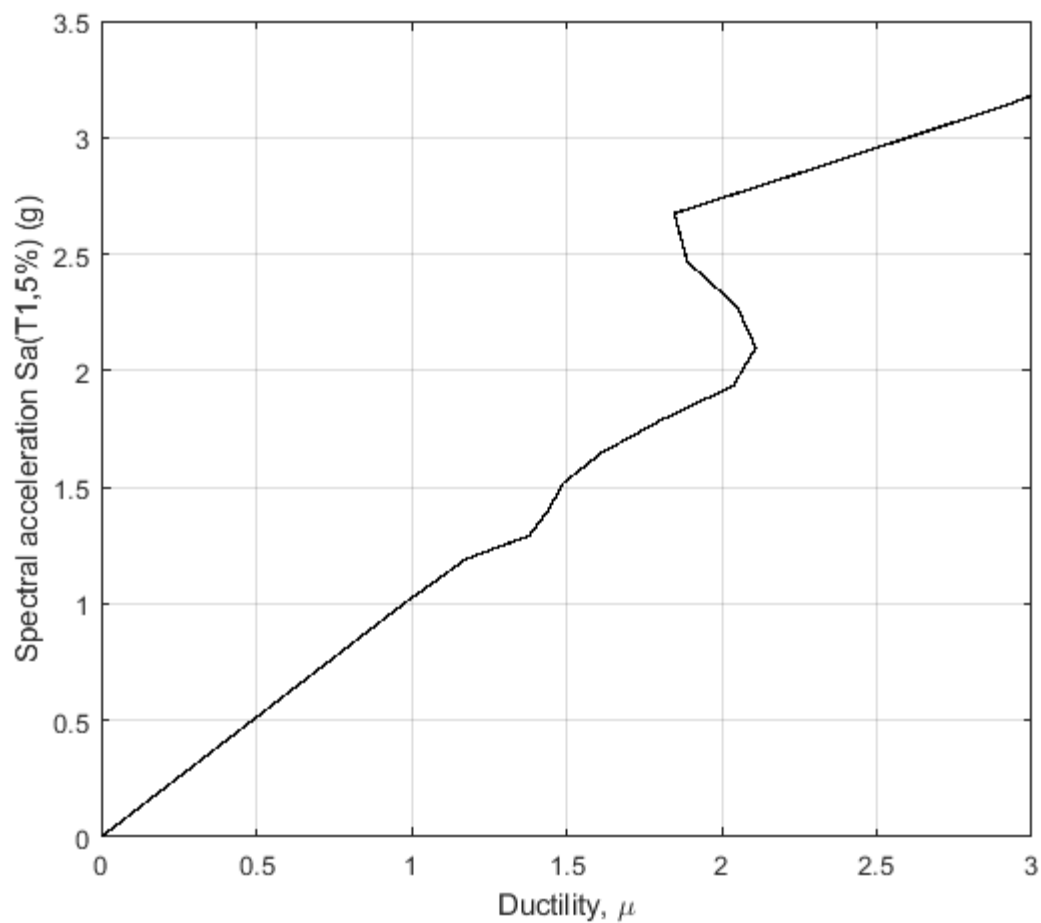
```
dak=eps;
```

Apply OpenSeismoMatlab

```
S1=OpenSeismoMatlab(dt,xgtd,sw,T,lambdaF,IM_DM,m,uy,pysf,ksi,AlgID,...  
    u0,ut0,rinf,maxtol,jmax,dak);
```

Plot the IDA curve

```
% Initialize figure  
figure()  
% Plot the IDA curve  
plot(S1.DM,S1.IM/9.81,'k','LineWidth',1)  
% Finalize figure  
grid on  
xlabel('Ductility, \mu')  
ylabel('Spectral acceleration Sa(T1,5%) (g)')  
xlim([0,3])  
ylim([0,3.5])
```



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Verify the incremental dynamic analysis for ductility response

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Reference

De Luca, F., Vamvatsikos, D., & Iervolino, I. (2011, May). Near-optimal bilinear fit of capacity curves for equivalent SDOF analysis. In Proceedings of the COMPDYN2011 Conference on Computational Methods in Structural Dynamics and Earthquake Engineering, Corfu, Greece.

Description

Figure 1(b) of the above reference presents the median IDA curves of SDOF systems with $T=0.5\text{sec}$. The actual capacity curve of the SDOF oscillator shown in Figure 1(a) of the same reference (green line), has been fitted with an elastoplastic bilinear fit according to FEMA-440 (blue line). This fitting introduces an error (bias) which appears as the blue area in Figure 1(b), which is generally conservative. In this example two arbitrary acceleration time histories are selected, then the corresponding displacement response IDA curves are plotted, based on a SDOF system with suitably selected properties, based on Figure 1(a). It is shown that both curves approximately fall into the bias (blue area) of Figure 1(b) of the above reference.

Earthquake motions

Load data from two earthquakes

```
GM={ 'Imperial Valley'; % Imperial valley 1979
     'Cape Mendocino' };
n=size(GM,1);
dt=cell(n,1);
xgtd=cell(n,1);
for i=1:n
    fid=fopen([GM{i}, '.dat'], 'r');
    text=textscan(fid, '%f %f');
    fclose(fid);
    t=text{1,1};
    dt{i}=t(2)-t(1);
    xgtd{i}=text{1,2};
end
```

Setup parameters for IDA analysis

Switch

```
sw='ida';
```

Eigenperiod

```
T=0.5;
```

Scaling factors

```
lambdaF=logspace(log10(0.01),log10(30),100);
```

Type of IDA analysis

```
IM_DM='Sa_disp';
```

Yield displacement

```
uy=0.042;
```

Initial stiffness

```
k_hi=1000/uy;
```

Mass

```
m=k_hi/(2*pi/T)^2;
```

Post yield stiffness factor

```
pysf=0.01;
```

Fraction of critical viscous damping

```
ksi=0.05;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt';
```

Set initial displacement

```
u0=0;
```

Set initial velocity

```
ut0=0;
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance for convergence

```
maxtol=0.01;
```

Maximum number of iterations per increment

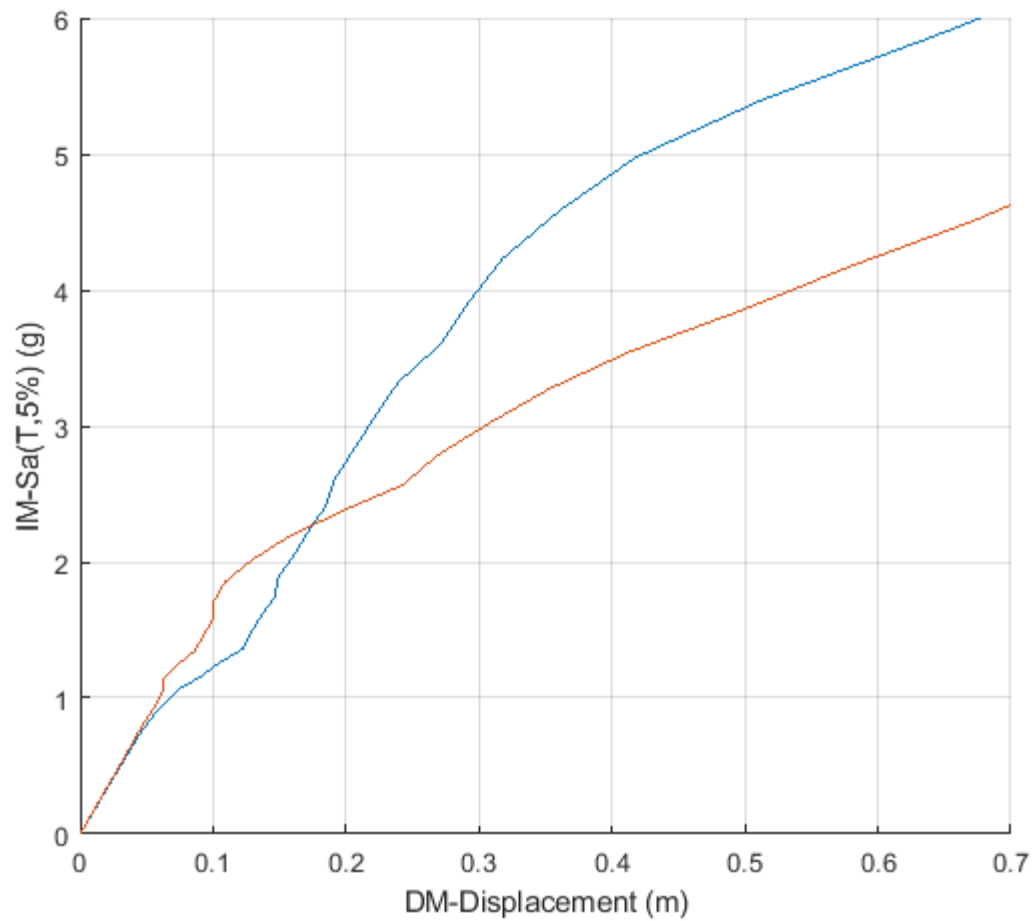
```
jmax=200;
```

Infinitesimal variation of acceleration

```
dak=eps;
```

Construct and plot the IDA curves in a loop

```
% Initialize figure
figure()
hold on
% Plot the IDA curves of Figure 1(b) of the above reference
for i=1:n
    S1=OpenSeismoMatlab(dt{i},xgtt{i},sw,T,lambaF,IM_DM,m,uy,pysf,ksi,AlgID,...
        u0,ut0,rinf,maxtol,jmax,dak);
    plot(S1.DM,S1.IM/9.81)
end
% Finalize figure
grid on
xlabel('DM-Displacement (m)')
ylabel('IM-Sa(T,5%) (g)')
xlim([0,0.7])
ylim([0,6])
```



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Verify the linear dynamic response of SDOF oscillator

Calculate the dynamic response of a linear SDOF oscillator. This example verifies Figure 6.6.1 in Chopra for $T_n=1\text{sec}$

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Reference

Chopra, A. K. (2020). Dynamics of structures, Theory and Applications to Earthquake Engineering, 5th edition. Prentice Hall.

Earthquake motion

Load earthquake data

```
dt=0.02;  
fid=fopen('elcentro.dat','r');  
text=textscan(fid,'%f %f');  
fclose(fid);  
xgtd=text{1,2};
```

Setup parameters for LIDA function

Eigenperiod

```
Tn=1;
```

Critical damping ratio

```
ksi=0.02;
```

Initial displacement

```
u0=0;
```

Initial velocity

```
ut0=0;
```

Algorithm to be used for the time integration

```
AlgID='U0-V0-Opt' ;
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Calculate dynamic response

Calculate circular eigenfrequency

```
omega=2*pi/Tn;
```

Apply LIDA

```
[u,ut,utt] = LIDA(dt,xgtt,omega,ksi,u0,ut0,AlgID,rinf);
```

Results

Maximum displacement in cm

```
D=max(abs(u))*100
```

D =

```
15.063275193038429
```

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Verify the energy time history of SDOF oscillator

Calculate the time history of the strain energy and the energy dissipated by viscous damping and yielding of a linear and a nonlinear SDOF oscillator

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Reference

Chopra, A. K. (2020). Dynamics of structures, Theory and Applications to Earthquake Engineering, 5th edition. Prentice Hall.

Description

Figure 7.9.1 of the above reference is reproduced in this example, for both the linear elastic and the elastoplastic SDOF systems. The linear system has $T_n=0.5$ sec and $\xi=5\%$, whereas the elastoplastic system has $T_n=0.5$ sec, $\xi=5\%$ and $f_y/\bar{\sigma}=0.25$.

Load earthquake data

Earthquake acceleration time history of the El Centro earthquake will be used (El Centro, 1940, El Centro Terminal Substation Building)

```
fid=fopen('elcentro.dat','r');
text=textscan(fid,'%f %f');
fclose(fid);
t=text{1,1};
dt=t(2)-t(1);
xgtd=text{1,2};
```

Setup parameters for NLIDABLKIN function for linear SDOF

Mass

```
m=1;
```

Eigenperiod

```
Tn=0.5;
```

Calculate the small-strain stiffness matrix

```
omega=2*pi/Tn;  
k_hi=m*omega^2;
```

Assign linear elastic properties

```
k_lo=k_hi;  
uy1=1e10;
```

Critical damping ratio

```
ksi=0.05;
```

Initial displacement

```
u0=0;
```

Initial velocity

```
ut0=0;
```

Algorithm to be used for the time integration

```
AlgID= 'U0-V0-Opt' ;
```

Minimum absolute value of the eigenvalues of the amplification matrix

```
rinf=1;
```

Maximum tolerance of convergence for time integration algorithm

```
maxtol=0.01;
```

Maximum number of iterations per integration time step

```
jmax=200;
```

Infinitesimal acceleration

```
dak=eps;
```

Calculate dynamic response of the linear SDOF

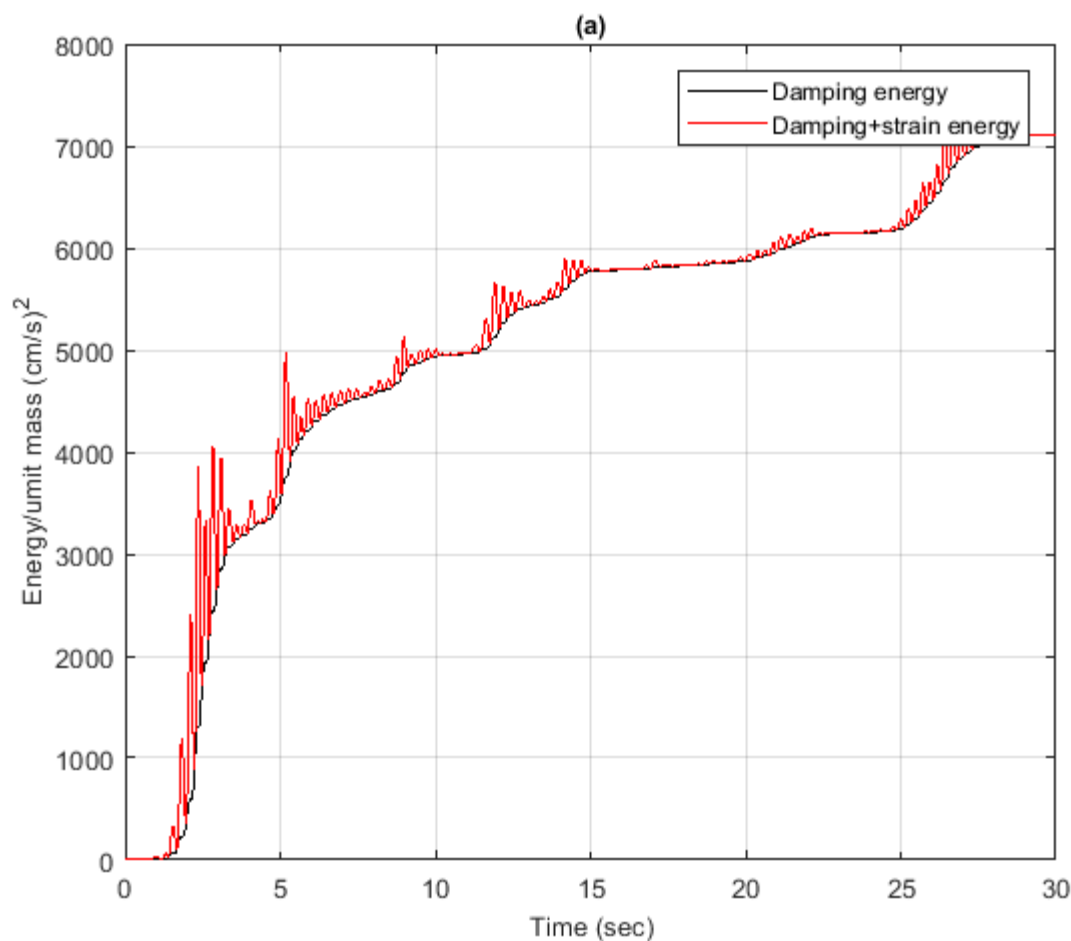
Apply NLIDABLKIN

```
[u,ut,utt,Fs,Ey,Es,Ed,jiter] = NLIDABLKIN(dt,xgtt,m,k_hi,k_lo,uy1,...  
ksi,AlgID,u0,ut0,rinf,maxtol,jmax,dak);
```

Plot the energy time history of the linear SDOF

Plot the damping energy and strain energy of the linearly elastic SDOF system. Convert from m to cm

```
figure()  
plot(t',cumsum(Ed)*1e4,'k','LineWidth',1)  
hold on  
plot(t',cumsum(Ed)*1e4+Es*1e4,'r','LineWidth',1)  
hold off  
xlim([0,30])  
ylim([0,8000])  
xlabel('Time (sec)','FontSize',10);  
ylabel('Energy/umit mass (cm/s)^2','FontSize',10);  
title('(a)','FontSize',10)  
grid on  
legend('Damping energy','Damping+strain energy')
```



Setup parameters for NLIDABLKIN function for nonlinear SDOF

The properties of the nonlinear SDOF system are identical to those of the linear SDOF system, except for the yield displacement and the

post-yield stiffness.

Post yield stiffness

```
k_lo=0.01*k_hi;
```

normalized yield strength

```
fybar=0.25;
```

Yield displacement for nonlinear response

```
uy2=fybar*max(abs(u));
```

Calculate dynamic response of the nonlinear SDOF

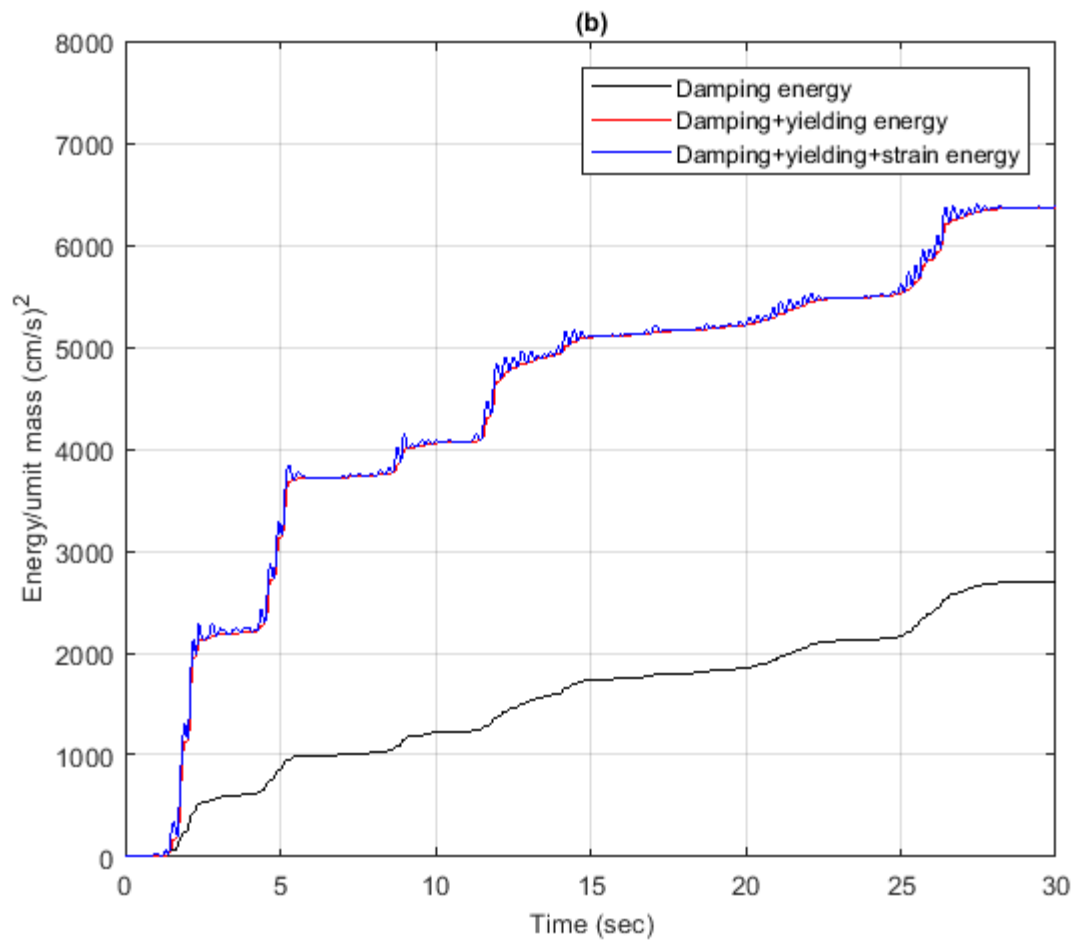
Apply NLIDABLKIN

```
[u,ut,utt,Fs,Ey,Es,Ed,jiter] = NLIDABLKIN(dt,xgtt,m,k_hi,k_lo,uy2,...  
ksi,AlgID,u0,ut0,rinf,maxtol,jmax,dak);
```

Plot the energy time history of the nonlinear SDOF

Plot the damping energy, the hysteretic energy and strain energy of the nonlinear SDOF system. Convert from m to cm.

```
figure();  
plot(t,cumsum(Ed)*1e4,'k','LineWidth',1)  
hold on  
plot(t,cumsum(Ed)*1e4+cumsum(Ey)*1e4-Es*1e4,'r','LineWidth',1)  
plot(t,cumsum(Ed)*1e4+cumsum(Ey)*1e4,'b','LineWidth',1)  
hold off  
xlim([0,30])  
ylim([0,8000])  
xlabel('Time (sec)','FontSize',10);  
ylabel('Energy/umit mass (cm/s)^2','FontSize',10);  
title('(b)','FontSize',10)  
grid on  
legend('Damping energy','Damping+yielding energy',...  
      'Damping+yielding+strain energy')
```



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