

Validation with Zheng

Case 1

$$V_p = 10 \text{ kV}, \quad Q_{\text{couple}} = 0.179 \text{ mJ/cm} = 0.0179 \text{ J/m}$$

$$L = 3.88 \text{ mm}$$

$$S = 61.8 \text{ } \mu\text{m}, \quad \eta = 0.35, \quad F = 10 \text{ kHz}, \quad \tau_n = 350 \text{ ns}$$

→ estimated electrode width, $w \approx 8 \text{ cm}$

$$\begin{aligned} \text{Power: } W &= Q_n \cdot F = \eta \cdot w \cdot Q_{\text{couple}} \cdot F = \\ &= 0.35 \cdot 0.08 \cdot 0.0179 \cdot 10^4 \Rightarrow \\ &\Rightarrow \boxed{W = 5.012 \text{ Watt}} \end{aligned}$$

$$\text{Fr Options value: } \dot{w}_n^{\text{max}} = 3 \cdot \dot{w}_n \text{ (in W/m}^3\text{)}$$

$$\dot{w}_n = \frac{Q_{\text{couple}} \cdot \eta}{A \cdot \tau_n} = \frac{0.0179 \cdot 0.35}{\frac{1}{2} \cdot 3.88 \cdot 61.8 \cdot 10^{-6} \cdot 350 \cdot 10^{-9}} \Rightarrow$$

$$\Rightarrow \dot{w}_n = 1.493 \cdot 10^{11} \text{ W/m}^3 \Rightarrow$$

$$\Rightarrow \boxed{\dot{w}_n^{\text{max}} = 4.479 \cdot 10^{11} \text{ W/m}^3}$$

Case 2

$$V_p = 20 \text{ kV}, Q_{\text{couple}} = 1.396 \text{ mJ/cm} = 0.1396 \text{ J/m}$$

$$L = 6.88 \text{ mm} \quad \eta = 0.35 \quad F = 10 \text{ kHz}$$

$$S = 62.7 \text{ } \mu\text{m} \quad \tau_n = 350 \text{ ns} \quad \Delta T_{\text{max}} = 407.7 \text{ K}$$

electrode width $w = 8 \text{ cm}$

Power: $W = Q_n \cdot f = \eta \cdot w \cdot Q_{\text{couple}} \cdot f =$

$$= 0.35 \cdot 0.08 \cdot 0.1396 \cdot 10^4 \Rightarrow$$

$$\Rightarrow \boxed{W = 39.088 \text{ Watt}}$$

Options value: $\dot{w}_n^{\text{max}} = 3 \dot{w}_n$

$$\dot{w}_n = \frac{Q_{\text{couple}} \cdot \eta}{A \cdot \tau_n} = \frac{0.1396 \cdot 0.35}{\frac{1}{2} \cdot 6.88 \cdot 62.7 \cdot 10^{-9} \cdot 350 \cdot 10^{-9}} \Rightarrow$$

$$\Rightarrow \dot{w}_n = 6.47 \cdot 10^{11} \text{ W/m}^3 \Rightarrow$$

$$= \boxed{\dot{w}_n^{\text{max}} = 1.9417 \cdot 10^{12} \text{ W/m}^3}$$

Case 3

$$V_p = 30 \text{ kV}, Q_{\text{couple}} = 4.654 \text{ mJ/cm} = 0.4654 \text{ J/m}$$

$$L = 9.99 \text{ mm} \quad \eta = 0.35 \quad F = 10 \text{ kHz}$$

$$J = 65.6 \text{ km} \quad \tau_h = 350 \text{ ns} \quad \Delta T_{\text{max}} = 894.8 \text{ K}$$

electrode with $w \approx 8 \text{ cm}$

Power: $W = Q_h \cdot f = \eta \cdot w \cdot Q_{\text{couple}} \cdot f$
 $= 0.35 \cdot 0.08 \cdot 0.4654 \cdot 10^4 \Rightarrow$
 $\Rightarrow W = 130.312 \text{ Watt}$

FrOptions: $\dot{w}_h^{\text{max}} = 3 \cdot \dot{w}_h$

$$\dot{w}_h = \frac{Q_{\text{couple}} \cdot \eta}{A \cdot \tau_h} = \frac{0.4654 \cdot 0.35}{\frac{1}{2} 9.99 \cdot 65.6 \cdot 10^9 \cdot 350 \cdot 10^{-9}} \Rightarrow$$

$$\Rightarrow \dot{w}_h = 1.412 \cdot 10^2 \text{ W/m}^3 \Rightarrow$$

$$\Rightarrow \dot{w}_h^{\text{max}} = 4.261 \cdot 10^2 \text{ W/m}^3$$

Case 4

$$N_p = 40 \text{ kV}, Q_{\text{couple}} = 10.89 \text{ mJ/cm} = 1.089 \text{ J/m}$$

$$L = 13.08 \text{ mm} \quad \eta = 0.35 \quad F = 10 \text{ kHz}$$

$$\delta = 68.0 \text{ } \mu\text{m} \quad \tau = 350 \quad \Delta T_{\text{max}} = 1542.7 \text{ K}$$

electrode width $w \approx 8 \text{ cm}$

• Power: $W = Q_n F = \eta w Q_{\text{couple}} F =$
 $= 0.35 \cdot 0.08 \cdot 1.089 \cdot 10^4 =$
 $\Rightarrow \boxed{W = 304.92 \text{ Watts}}$

• Fr Options: $\dot{w}_h^{\text{max}} = 3 \cdot \dot{w}_h$

$$\dot{w}_h = \frac{Q_{\text{couple}} \cdot \eta}{\Delta \cdot \tau_h} = \frac{1.089 \cdot 0.35}{\frac{1}{2} 13.08 \cdot 68.0 \cdot 10^{-6} \cdot 350 \cdot 10^{-3}}$$

$$\Rightarrow \dot{w}_h = 2.44686 \cdot 10^2 \text{ W/m}^3 \Rightarrow$$

$$\Rightarrow \boxed{\dot{w}_h^{\text{max}} = 7.34 \cdot 10^{12} \text{ W/m}^3}$$

Case 5

$$V_p = 50 \text{ kV}, Q_{\text{couple}} = 20.965 \text{ mJ/cm} = 2.0965 \text{ J/m}$$
$$L = 16.13 \text{ mm} \quad \eta = 0.35 \quad f = 10 \text{ kHz}$$
$$S = 70.3 \mu\text{m} \quad \tau_n = 350 \text{ ns} \quad \Delta T_{\text{max}} = 2329.5 \text{ K}$$

electrode width $w \approx 8 \text{ cm}$

Power: $W = Q_n f = \eta \cdot w \cdot Q_{\text{couple}} \cdot f =$

$$= 0.35 \cdot 0.08 \cdot 2.0965 \cdot 10^4 =$$
$$\Rightarrow \boxed{W = 587.02 \text{ Watt}}$$

Options: $\dot{W}_n^{\text{max}} = 3 \cdot \dot{W}_n$

$$\dot{W}_n = \frac{Q_{\text{couple}} \cdot \eta}{A \cdot \tau_n} = \frac{2.0965 \cdot 0.35}{\frac{1}{2} 16.13 \cdot 70.3 \cdot 10^{-9} \cdot 350 \cdot 10^{-9}} \Rightarrow$$
$$\rightarrow \dot{W}_n = 3.69773 \cdot 10^{12} \text{ W/m}^3 \Rightarrow$$
$$\Rightarrow \boxed{\dot{W}_n^{\text{max}} = 1.1093 \cdot 10^{13} \text{ W/m}^3}$$