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CS590 Homework Assignment  
12: Application Exercises

Due Date: April 17, 2022

### **Problem 14.7.18:**

Consider stations as Vertex in graph and channels as edges. Assign 1 weight to all edges that are not compromised. Assign large weight like 10000 to all compromised channels. Apply single source shortest path algorithm to the graph (Dijkstra's algorithm below).

Algorithm->

->Create a set that keeps track of vertices included in shortest path tree, i.e., whose minimum distance from source is calculated and finalized. Initially, this set is empty.

-> Assign a distance value to all vertices in the input graph. Initialize all distance values as INFINITE. Assign distance value as 0 for the source vertex so that it is picked first.

->While set doesn't include all vertices  
.... Pick a vertex u which is not there in set and has minimum distance value.  
.... Include u to set.

.... Relax all adjacent unvisited vertices. Update distance value of all adjacent vertices of  $u$ . To update the distance values, iterate through all adjacent vertices. For every adjacent vertex  $v$ , if sum of distance value of  $u$  (from source) and weight of edge  $u-v$ , is less than the distance value of  $v$ , then update the distance value of  $v$ .

Time complexity  $\rightarrow O(n^2)$  for adjacency matrix.  
Time complexity can be reduced to  $O(m + n \log n)$  using Fibonacci Heap implementation of Dijkstra's algorithm.