

More Relational Algebra

LECTURE 6

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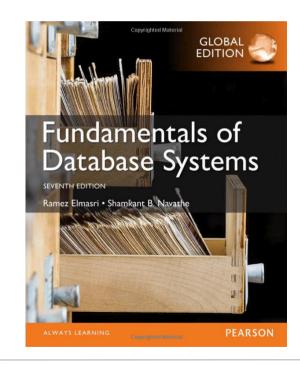


LECTURE 6

Covers ...

Parts of Chapter 8
Parts of Chapter 14 (high-level!)

Please read this up until next lecture!





What we will be covering

Aggregation
Outer Joins
Basics of Functional Dependencies
Normalization

6/1/16





 Table 8.1
 Operations of Relational Algebra

OPERATION	PURPOSE	NOTATION
SELECT	Selects all tuples that satisfy the selection condition from a relation R .	$\sigma_{< m selection\ condition>}(R)$
PROJECT	Produces a new relation with only some of the attributes of <i>R</i> , and removes duplicate tuples.	$\pi_{< ext{attribute list}>}(R)$
THETA JOIN	Produces all combinations of tuples from R_1 and R_2 that satisfy the join condition.	$R_1 \bowtie_{< \text{join condition}>} R_2$
EQUIJOIN	Produces all the combinations of tuples from R_1 and R_2 that satisfy a join condition with only equality comparisons.	$R_1\bowtie_{< \text{join condition}>} R_2$, OR $R_1\bowtie_{(< \text{join attributes 1}>)}$, $(< \text{join attributes 2}>)$ R_2
NATURAL JOIN	Same as EQUIJOIN except that the join attributes of R_2 are not included in the resulting relation; if the join attributes have the same names, they do not have to be specified at all.	$R_1^*_{< \text{join condition}>} R_2,$ OR $R_1^*_{< \text{join attributes 1}>},$ (< join attributes 2>) R_2 OR $R_1^*_{< \text{2}} R_2^*$

 Table 8.1
 Operations of Relational Algebra

OPERATION	PURPOSE	NOTATION
UNION	Produces a relation that includes all the tuples in R_1 or R_2 or both R_1 and R_2 ; R_1 and R_2 must be union compatible.	$R_1 \cup R_2$
INTERSECTION	Produces a relation that includes all the tuples in both R_1 and R_2 ; R_1 and R_2 must be union compatible.	$R_1 \cap R_2$
DIFFERENCE	Produces a relation that includes all the tuples in R_1 that are not in R_2 ; R_1 and R_2 must be union compatible.	$R_1 - R_2$
CARTESIAN PRODUCT	Produces a relation that has the attributes of R_1 and R_2 and includes as tuples all possible combinations of tuples from R_1 and R_2 .	$R_1 \times R_2$



Let's do some in-class exercises.



Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
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Ahmad	٧	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX	М	25000	987654321	4
James	Е	Borg	888665555	1937-11-10	450 Stone, Houston, TX	М	55000	NULL	1

"Find the first and last names of all employees, along with their department (number)."



Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
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James	Е	Borg	888665555	1937-11-10	450 Stone, Houston, TX	М	55000	NULL	1

"Find the first and last names of all employees, along with their department (number)."

 $\pi_{Fname,Lname,Dno}(EMPLOYEE)$



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John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
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James	Е	Borg	888665555	1937-11-10	450 Stone, Houston, TX	М	55000	NULL	1

"Find an unique set of last names of all employees born after 1959"





Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
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James	Е	Borg	888665555	1937-11-10	450 Stone, Houston, TX	М	55000	NULL	1

"Find an unique set of last names of all employees born after 1959"

$$\pi_{Lname}(\sigma_{(Bdate \geq 1960-01-01)}(EMPLOYEE))$$

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Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
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"Find the first and last names of all employees born after 1959, and store them to a relation NEWBIES(First,Last)"

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Е	Borg	888665555	1937-11-10	450 Stone, Houston, TX	М	55000	NULL	1
	B T J S K A V	B Smith T Wong J Zelaya S Wallace K Narayan A English V Jabbar	B Smith 123456789 T Wong 333445555 J Zelaya 999887777 S Wallace 987654321 K Narayan 666884444 A English 453453453 V Jabbar 987987987	B Smith 123456789 1965-01-09 T Wong 333445555 1955-12-08 J Zelaya 999887777 1968-01-19 S Wallace 987654321 1941-06-20 K Narayan 666884444 1962-09-15 A English 453453453 1972-07-31 V Jabbar 987987987 1969-03-29	B Smith 123456789 1965-01-09 731 Fondren, Houston, TX T Wong 333445555 1955-12-08 638 Voss, Houston, TX J Zelaya 999887777 1968-01-19 3321 Castle, Spring, TX S Wallace 987654321 1941-06-20 291 Berry, Bellaire, TX K Narayan 666884444 1962-09-15 975 Fire Oak, Humble, TX A English 453453453 1972-07-31 5631 Rice, Houston, TX V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX	B Smith 123456789 1965-01-09 731 Fondren, Houston, TX M T Wong 333445555 1955-12-08 638 Voss, Houston, TX M J Zelaya 999887777 1968-01-19 3321 Castle, Spring, TX F S Wallace 987654321 1941-06-20 291 Berry, Bellaire, TX F K Narayan 666884444 1962-09-15 975 Fire Oak, Humble, TX M A English 453453453 1972-07-31 5631 Rice, Houston, TX F V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M	B Smith 123456789 1965-01-09 731 Fondren, Houston, TX M 30000 T Wong 333445555 1955-12-08 638 Voss, Houston, TX M 40000 J Zelaya 999887777 1968-01-19 3321 Castle, Spring, TX F 25000 S Wallace 987654321 1941-06-20 291 Berry, Bellaire, TX F 43000 K Narayan 666884444 1962-09-15 975 Fire Oak, Humble, TX M 38000 A English 453453453 1972-07-31 5631 Rice, Houston, TX F 25000 V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M 25000	B Smith 123456789 1965-01-09 731 Fondren, Houston, TX M 30000 333445555 T Wong 333445555 1955-12-08 638 Voss, Houston, TX M 40000 888665555 J Zelaya 999887777 1968-01-19 3321 Castle, Spring, TX F 25000 987654321 S Wallace 987654321 1941-06-20 291 Berry, Bellaire, TX F 43000 888665555 K Narayan 666884444 1962-09-15 975 Fire Oak, Humble, TX M 38000 333445555 A English 453453453 1972-07-31 5631 Rice, Houston, TX F 25000 333445555 V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M 25000 987654321

$$NEWBIES \leftarrow \rho_{(First, Last)}(\pi_{Fname, Lname}(\sigma_{(Bdate \geq 1960 - 01 - 01)}(EMPLOYEE)))$$



Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
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"Find all pairs of employees with different sex."

(for simplicity it's ok if the same pairs appear multiple in the result)

"Find all pairs of employees with different sex."

_								
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В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
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$$E_1 \leftarrow EMPLOYEE$$

$$E_2 \leftarrow EMPLOYEE$$

$$\sigma_{(E1.Sex \neq E2.Sex)}(E_1 \times E_2)$$



Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
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"Find the last names of all supervisors."



"Find the last names of all supervisors."

	_								
Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
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$$EMP \leftarrow EMPLOYEE$$
 $SUP \leftarrow EMPLOYEE$

$$\pi_{(SUP.Lname)}(EMP_{\bowtie EMP.Super_ssn=SUP.Ssn}SUP)$$



Aggregation

What the operations we discussed so far cannot express are aggregations

Functions that calculate something across multiple tuples

SUM, AVERAGE, MAXIMUM, MINIMUM, COUNT





Aggregate Functional Operation F

General notation:

<grouping> $\mathscr{F}<$ functions>(R)

We'll talk in a second about what the "grouping" is about

whereas <functions> is a list of

[MIN | MAX | AVERAGE | SUM | COUNT] <attribute>

Usage Examples

FMAX Salary (EMPLOYEE)

Retrieves the maximum salary of an employee

FMIN Salary (EMPLOYEE)

Retrieves the minimum salary

FSUM Salary (EMPLOYEE)

Retrieves the sum of all salaries

FCOUNT Ssn, AVERAGE Salary (EMPLOYEE)

computes the count (number) of employees and their average salary

Result of Aggregate Queries

Aggregate queries (without grouping) are different to what we discussed so far because they essentially return **single values**

Still in form of a relation for completeness, but as a relation with a **single tuple**

FCOUNT Ssn, AVERAGE Salary (EMPLOYEE)

Count_ssn	Average_salary
8	35125

Result of Aggregate Queries

We cannot directly combine aggregate queries and normal projection

FCOUNT Ssn, Salary (EMPLOYEE)

Note that applying any operation, including projection or renaming, to the result relation is fine:

P(NR OF EMPLOYEES, MAX SAL) (FCOUNT SSN, MAX Salary (EMPLOYEE))

The Special Case of COUNT

COUNT has one special property - it generally does not matter **which** attribute in a given relation you count over. The result is always the same (the number of tuples in the relation).

Note that COUNT does **nothing clever** - it does not remove duplicates, nor does it skip NULL values.

Handling Duplicates in Aggregate Functions

Recall that relations are **not allowed to have duplicate tuples**All duplicates are removed from the results of relational operations to keep this constraint intact

However, **during processing** duplicates are fine For instance, $\mathscr{F}_{\text{AVERAGE Salary}}(\text{EMPLOYEE})$ **does not** remove duplicates before calculating the average

In practice this matters only for SUM, COUNT, and AVERAGE

Grouping

Often we don't want to aggregate over the **entire** relation, but first group the tuples by some common attribute

Example:

Find the number and average employee salary **per department**

Basic idea:

For each unique department number, find all employees that work in that department and apply aggregate functions to those

Grouping

DNO FCOUNT Ssn, AVERAGE Salary (EMPLOYEE)

This operation **groups** employees by DNO (department number) and computes the count of employees and average salary per department Result is a relation with one tuple per DNO, and two additional attributes (the count and average salary for each DNO)

Dno	Count_ssn	Average_salary
5	4	33250
4	3	31000
1	1	55000

OUTER JOINS

In NATURAL JOIN and EQUIJOIN, tuples without a matching (or related) tuple are **eliminated from the join result**Including tuples with null in the join attributes

A set of operations, called OUTER JOINS, can be used when we want to keep all the tuples, regardless of whether or not they have matching tuples in the other relation.

Regular JOINS can lead to information loss

Example:

DEPARTMENT ⋈ MGRSSN=SSN EMPLOYEE

If a department currently does not have a manager (for whatever reason) it won't show up in the result relation.

Basically always an issue when one or both of the join attributes are allowed to be NULL

Types of OUTER JOINS

LEFT OUTER JOIN (keeps every tuple in the **left** relation)

 $A \bowtie B$

RIGHT OUTER JOIN (keeps every tuple in the **right** relation)

 $A \bowtie B$

FULL OUTER JOIN (keeps every tuple in **both** relations)

 $A = \bowtie B$

Example OUTER JOIN

```
RESULT \leftarrow \pi_{\text{Fname, Minit, Lname, Dname}} ( 
 EMPLOYEE \longrightarrow EMPLOYEE.DNO=DEPARTMENT.DNUMBER DEPARTMENT )
```

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RESULT

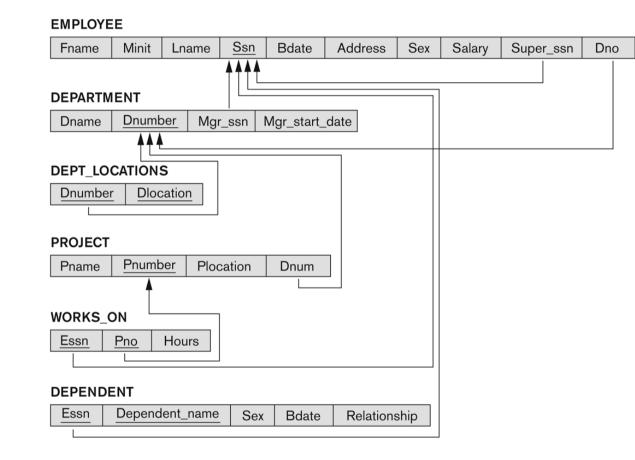
Fname	Minit	Lname	Dname
John	В	Smith	NULL
Franklin	Т	Wong	Research
Alicia	J	Zelaya	NULL
Jennifer	S	Wallace	Administration
Ramesh	K	Narayan	NULL
Joyce	Α	English	NULL
Ahmad	V	Jabbar	NULL
James	Е	Borg	Headquarters



Some more exercises.

How many projects are there at each location?

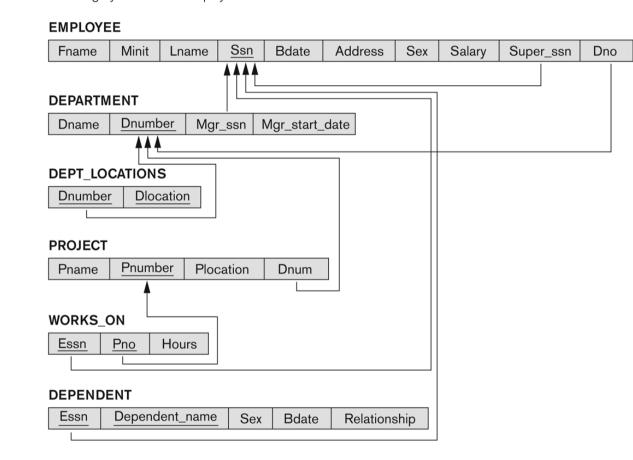
Figure 5.7Referential integrity constraints displayed on the COMPANY relational database schema.



How many projects are there at each location?

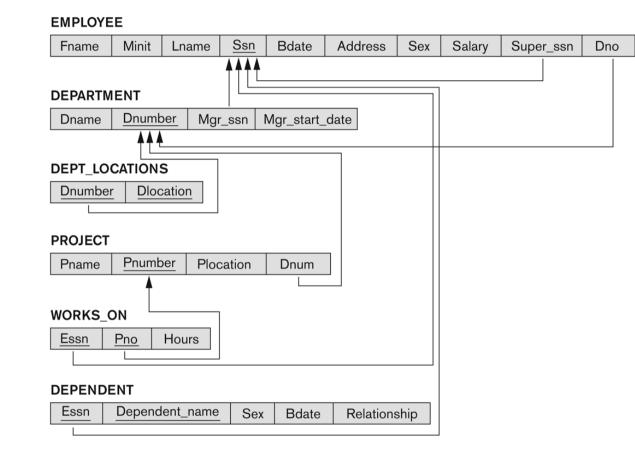
 $_{Plocation}\mathscr{F}_{COUNT\ Pnumber}\left(PROJECT\right)$

Figure 5.7Referential integrity constraints displayed on the COMPANY relational database schema.



Get a list of all projects and the employees (all info, not just the employee Id) that work on them. Projects with no employees working on them should still be listed.

Figure 5.7Referential integrity constraints displayed on the COMPANY relational database schema.



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Get a list of all projects and the employees (all info, not just the employee Id) that work on them. Projects with no employees working on them should still be listed.

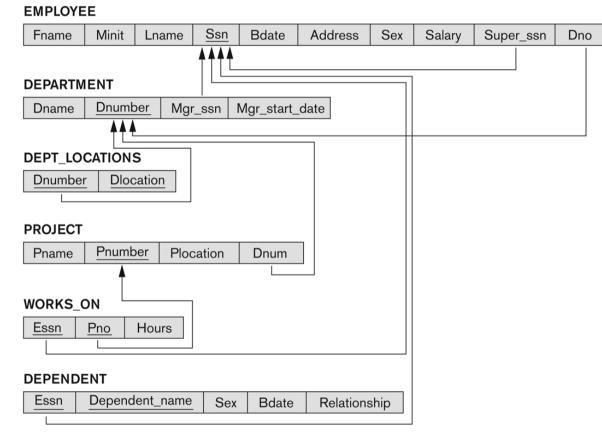
$$P \leftarrow PROJECT$$

$$PE \leftarrow WORKS_ON$$

$$E \leftarrow EMPLOYEE$$

$$P\bowtie_{(P.Pnumber=PE.Pno)} PE \bowtie_{(PE.Essn=E.Ssn)} E$$

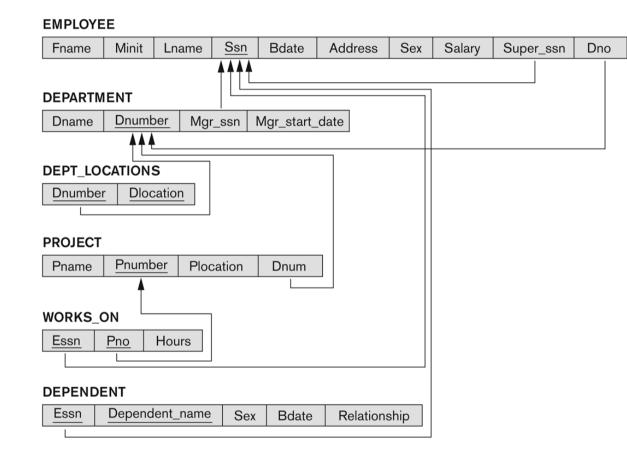
Figure 5.7Referential integrity constraints displayed on the COMPANY relational database schema.



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For each project name, find out how many employees are assigned to them. Projects without employees should not show up in the results (result should be a list of project names and employee counts).

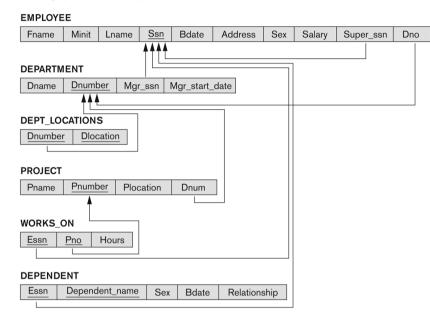
Figure 5.7Referential integrity constraints displayed on the COMPANY relational database schema.



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For each project name, find out how many employees are assigned to them. Projects without employees should not show up in the results (result should be a list of project names and employee counts).

Figure 5.7
Referential integrity constraints displayed on the COMPANY relational database schema.



 $TMP \leftarrow \rho_{(Pno,Emp_count)}(Pno\mathscr{F}_{COUNT\ Essn}\ (WORKS_ON))$ $\pi_{PROJECT.Pname,TMP.Emp_count}(TMP_{\bowtie(TMP.Pno=PROJECT.Pnumber)}PROJECT)$

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Let's take a big step back now!





What constitutes a "good" relational design?

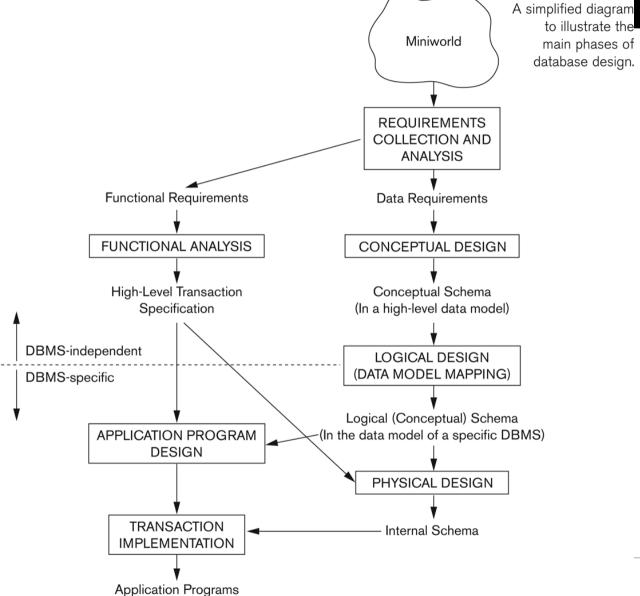


Figure 3.1



Informal criteria for "good" design

Clear semantics

Mapping to the real world

No (or at least controlled) redundancy

Avoidance of NULL values

Support for arbitrary queries

Efficiency

An example of redundancy

Example:

EMP_PROJ(Emp#, Proj#, Ename, Pname, No_hours)

(the employee and project name are **redundant**, because we could also get them via join to the employee and project relations)

Informally:

A redundancy happens if information is stored explicitly that could also be derived from some other place in the database.

On redundancy

Two problems of redundancy:

- (1) wastes space (same info is stored multiple times)
 This is nowadays not the biggest problem anymore
- (2) data can easily become **corrupted** when updating **(update anomalies)**

On redundancy

However:

There is usually a trade-off, and in some database designs developers will choose **controlled redundancy** to improve query times.

Joins, and even moreso calculations, are expensive, but projections are cheap.

Alternatively:

Using database views (a "virtual relation" where certain information is pre-calculated for faster querying)

Supporting arbitrary queries

It is possible to design a database in a way that certain queries become **technically impossible** or **deliver wrong results** (spurious tuples).

This is usually the case if the relations contain matching attributes that are not primary key / foreign key pairs.

This has a lot to do with the notion of **functional dependencies**.

Functional dependencies

Functional dependencies (FDs)

Used to specify formal measures of the **"goodness"** of relational designs

And keys are used to define **normal forms** for relations

Are constraints that are derived from the **meaning and interrelationships** of the data attributes

A set of attributes X functionally determines a set of attributes Y if the value of X determines a unique value for Y

Functional dependencies

A set of attributes X functionally determines a set of attributes Y if the value of X determines a unique value for Y

Mathematically: $X \rightarrow Y$ ("X implies Y")

Or in RA form: $t1[X]=t2[X] \rightarrow t1[Y]=t2[Y]$

Some examples

Social security number determines employee name SSN → ENAME

Project number determines project name and location PNUMBER → {PNAME, PLOCATION}

Employee ssn and project number determines the hours per week that the employee works on the project

 $\{SSN, PNUMBER\} \rightarrow HOURS$

FDs and keys

FDs are not bidirectional

SSN → ENAME, but the inverse is not true

Keys **automatically** have a FD on every attribute in the relation

If you know the key, you can determine all other attribute values

Redundancies formulated as FDs

Note that data redundancies can be formulated as (unwanted) functional dependencies:

```
EMP_PROJ(Emp#, Proj#, Ename, Pname, No_hours)

EMP_PROJ[Ename] → EMP[Ename]

EMP_PROJ[Pname] → PROJECT[Pname]
```

These are said to be **redundant FDs** as there are also the expected FDs between primary / foreign keys.

Colloquially, we can state that we need to maintain multiple pairs of FDs where one would do.

Finding FDs

We **cannot** define functional dependencies without knowing what the attributes in our data **mean**

However, given a valid database state, we can **rule out** certain FDs

TEACH

Teacher	Course	Text
Smith	Data Structures	Bartram
Smith	Data Management	Martin
Hall	Compilers	Hoffman
Brown	Data Structures	Horowitz

Normal Forms and Normalization

Normalization is the process of identifying FDs and refactoring a database schema so that (1) keys are properly identified and (2) unwanted FDs are removed.

Normal Forms:

A database is said to be in **normal form** after normalization.

Typically: 2NF, 3NF, BCNF

(there are more which we won't cover)



First Normal Form (1NF)

Disallows

Composite attributes

Multivalued attributes

Nested relations

This basically comes automatically with the RM (RM does not support models that are not in 1NF)



Second Normal Form (2NF)

Requires that every attribute that is not part of a primary key is **fully functionally dependent** on the primary key.

That is, no attribute should have a FD on only a part of a composed primary key.



Third Normal Form (3NF)

Requires that no non-key attribute has a functional dependency on another non-key attribute.

Basically:

Avoid redundancies

More on normal forms

In the book you find (much) **more formal definitions** and concrete algorithms for normalization.

Plus: more normal forms

In practice you will be fine if you follow the informal guidelines outlined earlier, most importantly:

Define relations and attributes in a way that makes domain sense

Stay aware of redundancy

Define primary keys



Key Takeaways

Remaining concepts of RA:

OUTER JOINS

Aggregate functions

Normal forms and normalization:

Functional dependencies Normal forms (1/2/3NF)

6/1/16