

Ausgang

i) Minimierung nach west corner

existiert eine feasible solution

$$x_{11} = 25, x_{12} = 11, x_{22} = 29, x_{13} = 1,$$

$$x_{32} = 29, x_{42} = 13$$

$$Z = 25 \cdot 600 + 11 \cdot 320 + 29 \cdot 350 + 50 + 29 \cdot 480 + 13 \cdot 1000 \text{ element}$$

$$= 56040$$

ii) Existiert eine feasible solution zu (i)

$$u_1 = 0, u_1 + v_1 = 600 \Rightarrow v_1 = 600 \quad w_{12} = u_1 + v_2 - c_{12} = 630 - 400 = 230$$

$$u_2 + v_1 = 320 \Rightarrow u_2 = -280 \quad w_{13} = u_1 + v_3 - c_{13} = 660 - 700 < 0$$

$$u_2 + v_2 = 350 \Rightarrow v_2 = 630 \quad w_{23} = u_2 + v_3 - c_{23} = -280 + 660 - 300 = 80$$

$$u_3 + v_2 = 450 \Rightarrow u_3 = -180 \quad w_{31} = u_3 + v_1 - c_{31} = -180 + 600 - 480 < 0$$

$$u_3 + v_3 = 480 \Rightarrow v_3 = 660 \quad w_{41} = u_1 + v_1 - c_{41} = 340 + 600 - 1000 < 0$$

$$u_4 + v_3 = 1000 \Rightarrow u_4 = 340$$

- Diagonale zu (1,2) ja ein enter variable für  $\theta = 25$

	1	3	9	
1	600	25	700	$u_1 = 0, u_1 + v_2 = 400 \Rightarrow v_2 = 400 \quad w_{11} = u_1 + v_1 - c_{11} = 370 - 600 < 0$
2	320	4	350	$u_2 + v_2 = 350 \Rightarrow u_2 = -50 \quad w_{13} = u_1 + v_3 - c_{13} = 430 - 700 < 0$
3	500	1	29	$u_2 + v_1 = 320 \Rightarrow v_1 = 370 \quad w_{23} = u_2 + v_3 - c_{23} = -50 + 430 - 300 = 80$
4	1000	-	13	$u_3 + v_2 = 450 \Rightarrow u_3 = 50 \quad w_{31} = u_3 + v_1 - c_{31} = 50 + 370 - 500 < 0$
				$u_3 + v_3 = 480 \Rightarrow v_3 = 430 \quad w_{41} = u_1 + v_1 - c_{41} = 570 + 370 - 1000 < 0$
				$u_4 + v_3 = 1000 \Rightarrow u_4 = 570$

- Diagonale zu (2,3) ja ein enter variable für  $\theta = 4$

	1	3	9	
1	600	25	700	$u_1 = 0, u_1 + v_2 = 400 \Rightarrow v_2 = 400 \quad w_{11} = u_1 + v_1 - c_{11} = 450 - 600 < 0$
2	320	4	350	$u_3 + v_2 = 450 \Rightarrow u_3 = 50 \quad w_{13} = u_1 + v_3 - c_{13} = 430 - 700 < 0$
3	500	5	25	$u_2 + v_3 = 480 \Rightarrow v_3 = 430 \quad w_{23} = u_2 + v_2 - c_{23} = -130 + 400 - 350 < 0$
4	1000	-	13	$u_2 + v_1 = 320 \Rightarrow v_1 = 450 \quad w_{31} = u_3 + v_1 - c_{31} = 50 + 450 - 500 = 0$
				$u_4 + v_1 = 1000 \Rightarrow u_4 = 570$

- Dua) jeopt 70 (4,1) jna enter variable für  $\delta = 13$  ( $\min\{13, 36\}$ )

	1	3	2	
1	600	900	700	
2	23	320	350	17
3	500	450	480	25
4	13	1000	-	1000

$$U_1 = 0, \quad U_1 + V_2 = 400 \Rightarrow V_2 = 400$$

$$U_3 + V_2 = 450 \Rightarrow U_3 = 50$$

$$U_3 + V_3 = 480 \Rightarrow V_3 = 430$$

$$U_2 + V_3 = 300 \Rightarrow U_2 = -130$$

$$U_2 + V_1 = 320 \Rightarrow V_1 = 450$$

$$U_1 + V_1 = 1000 \Rightarrow U_1 = 550$$

$$W_{11} = U_1 + V_1 - C_{11} = 450 - 600 < 0$$

$$W_{13} = U_1 + V_3 - C_{13} = 450 - 700 < 0$$

$$W_{22} = U_2 + V_2 - C_{22} = -130 + 400 - 350 < 0$$

$$W_{31} = U_3 + V_1 - C_{31} = 50 + 450 - 500 > 0$$

$$W_{43} = U_4 + V_3 - C_{43} = 550 + 430 - 1000 < 0$$

: pu optimal

$$Z = 25 \cdot 400 + 23 \cdot 320 + 17 \cdot 300 + 5 \cdot 450 + 25 \cdot 480 + 13 \cdot 1000 = 49.710$$

(iii)	1	2	3	S
1	600	700	1400	250
2	36	4300	350	4040
3	500	1480	450	30250
4	1000	1000	-	130
d	36	5225	305	
	0	25		

Exope  $P_i \rightarrow 70$  row penalty

row i equivalent to  $P_i = 70$

col penalty row i equivalent

$P_1$	$P'_1$	max: 180
1. $600 - 400 = 200$	$500 - 320 = 180$	min surplus 1: 320
2. $320 - 300 = 20$	$480 - 300 = 180$	$\Delta p_a x_{21} = 36$
3. $480 - 450 = 30$	$400 - 350 = 50$	
4. $1000 - 1000 = 0$		

$P_2$	$P'_2$	max: 1000
1. $700 - 400 = 300$	$480 - 300 = 180$	min surplus 2: 1000
2. $350 - 300 = 50$	$400 - 350 = 50$	$\Delta p_a x_{22} = 13$
3. $480 - 450 = 30$		
4. $1000$		

$P_3$	$P'_3$	max: 300	$P_4$	$P'_4$	max: 180
1. $300$	$-$	min surplus 3: 400	$-$	$-$	min surplus 4: 300
2. $50$	$180$	$\Delta p_a x_{13} = 25$	$50$	$180$	$\Delta p_a x_{42} = 9$
3. $30$	$50$		$30$	$100$	
4. $-$			$-$		

$P_5$	$P'_5$	max 30
$-$	$-$	min surplus 5: 450
$-$	$-$	$\Delta p_a x_{33} = 5$ and $x_{32} = 25$
$30$	$-$	
$-$	$-$	

$$Z = 36 \cdot 320 + 4 \cdot 300 + 95 \cdot 400 + 25 \cdot 480 + 5 \cdot 450 + 13 \cdot 1000 = 49970$$

	1	2	3	Supply
1	1600	1700	1400	250
2	5	320	300	405
3	25	1500	1480	30
	30	35	25	
	25			

0 minimaus opiv zw. aufzun.

$P_1$	$P_1'$	Durchgabe zu: (1,3)	$P_2$	$P_2'$	Durchgabe zu: (2,2)
200	180	bis zu 1800 no:	-	-	
90	180	bis zu 1800 no: (1,3)	90	180	
30	50		20	180	

$P_3$	$P_3'$
-	-

$$Z_2 = 25 \cdot 400 + 5 \cdot 320 + 35 \cdot 300 + 25 \cdot 500 = 34.600$$

Aber für zw. aufzun. geht zu 1(iii) Example  $\Delta Z = Z - Z_2 =$

$$= 49.970 - 34.600$$

$$= 15.370$$

## Asuman 2

- a)  $x_{ij}$  n posörnra berfinas na  
fırzaferen ars zo Sıvıçisimpi i  
omv neploxiı Sıvıçis j

	1	2	3	S
1	120	180	-	6
2	300	100	80	5
3	200	250	120	8
D	4	8	7	

Neploxisi:

→ H posörnra berfinas na fırzaferen ars uđde Sıvıçisimpi or uđde neploxi Se da  
omv na unirbaicu omv nıçpısa Sıvıçisimpi zo Sıvıçisimpi.

$$x_{11} + x_{12} \leq 6$$

$$x_{21} + x_{22} + x_{23} \leq 5$$

$$x_{31} + x_{32} + x_{33} \leq 8$$

→ n posörnra berfinas uđde neploxi Se da omv na fırzaferen na nıçpısa  
fırzaferen na neploxisi

$$x_{11} + x_{21} + x_{31} \leq 4$$

$$x_{21} + x_{22} + x_{23} \leq 8$$

$$x_{31} + x_{32} \leq 7$$

→ Ol posörnras arsler Se da omv aqvnıçılık

$$x_{ij} \geq 0$$

$$\min Z = 12 \cdot x_{11} + 18 \cdot x_{12} + 30 \cdot x_{21} + 10 \cdot x_{22} + 8 \cdot x_{23} + 20 \cdot x_{31} + 25 \cdot x_{32} + 18 \cdot x_{33}$$

b) (i)	1	2	3		$(1,1) : \min \{4,6\} = 4$
1	4 <small>12</small>	9 <small>18</small>	-	6 <small>0</small>	$(1,2) : \min \{2,8\} = 2$
2	30 <small>5</small>	5 <small>10</small>	18	5 <small>0</small>	$(2,2) : \min \{5,6\} = 5$
3	20 <small>1</small>	1 <small>25</small>	7 <small>12</small>	8 <small>0</small>	$(3,2) : \min \{1,3\} = 1$
	4 <small>0</small>	8 <small>0</small>	7 <small>0</small>		$(3,3) : \min \{7,7\} = 7$

$$Z = 243$$

(ii) Eşanıç as feasible solution zo (i)

BV

$$U_1 = 0, U_1 + V_1 = 12 \Rightarrow V_1 = 12$$

$$U_1 + V_2 = 13 \Rightarrow V_2 = 13$$

$$U_2 + V_2 = 10 \Rightarrow U_2 = -3,$$

$$U_3 + V_3 = 25 \Rightarrow U_3 = 7, U_3 + V_3 = 12 \Rightarrow V_3 = 5$$

NBV

$$W_{21} = U_2 + V_1 - C_{21} = -90$$

$$W_{23} = U_2 + V_3 - C_{23} = -11$$

$$W_{31} = U_3 + V_1 - C_{31} = -1$$

0) a aqvnıçılık

üpa n dia

5) van optimal

$$Z = 243.$$

(iii)	1	2	3	5
1	4 <sup>12</sup>	2 <sup>18</sup>	-	6 <sup>2</sup>
2	<sup>30</sup>	5 <sup>10</sup>	<sup>18</sup>	5
3	<sup>20</sup>	1 <sup>25</sup>	7 <sup>12</sup>	8 <sup>1</sup>
D	40	8	70	

Exaple za penalty ju za rows uan za cols

row1	col1	
1	6	8
2	2	8
3	8	4

Dijagonale  $\rightarrow$  max ans row minima (8)  
 Faušun exa 3 da Sijagonale  $\rightarrow$  row 3  
 $\rightarrow$  row 3 bispunkt  $\rightarrow$  udi (2)  $\rightarrow$  16 psp  
 uan (7,3) uan bispunkt  $\rightarrow$  min {7,8} = 7. Izvijekite te  
 upoznato rješenje.

row2	col2	
1.	6	8
2.	2	8
3.	5	-

Dijagonale  $\rightarrow$  udi (1,1) uan bispunkt  $\rightarrow$   
 min {4,6} = 4

row 3	col 3	
1.	3	-
2.	1	10
3.	1	-

Tupa Sijagonale  $\rightarrow$  sljedeci uan (10)  
 bispunkt s12 (2,2) : min {5,3} = 5  
 bispunkt s12 (1,2) : min {2,3} = 2  
 uan rijek s12 (3,2) : min {1,1} = 1

$$Z = 4 \cdot 12 + 2 \cdot 18 + 5 \cdot 10 + 1 \cdot 25 + 7 \cdot 12 = 243$$

Asuman 3

		I	II	III	
	A	20	16	24	10
a)	B	15	18	12	15
ans		6	9	10	

$$\min Z = 20x_{11} + 16x_{12} + 24x_{13} + 15x_{21} + 18x_{22} + 12x_{23}$$

Prayogishki:  $x_{11} + x_{12} + x_{13} \leq 10$

$$x_{21} + x_{22} + x_{23} \leq 15$$

$$x_{11} + x_{21} \leq 6$$

$$x_{12} + x_{22} \leq 9$$

$$x_{13} + x_{23} \leq 10$$

$$x_{ij} \geq 0$$

$$u_A = 0, u_A + v_1 = 20 \Rightarrow v_1 = 20, v_2 = 16, v_3 = 24$$

$$u_B + v_1 = 15 \Rightarrow u_B = -5$$

$$w_{AB} = u_A + v_3 - c_{A3} = 24 - 24 = 0$$

$$w_{B2} = u_B + v_2 - c_{B2} = -5 + 16 - 13 = -2 < 0$$

	I	II	III	
A	1 <del>20</del>	9 <del>16</del>	- <del>24</del>	10
B	5 <del>15</del>	- <del>13</del>	10 <del>12</del>	5 <del>0</del>

X<sub>21</sub> eivai optimal

- b) Fia vo napapravu n lichen zo (a) optimal du npernu va lichen zo  
Prayogishki ans zo (a)

Theta xpusiforshikha zo reduced cost jya in x<sub>21</sub> ans na lichen zo (a)

$$1. \text{ Exporte } Z = 20x_{A1} + 16x_{AII} + 24x_{AIII} + 15x_{B1} + 18x_{BII} + 12x_{BIII} = 359$$

2. Augjante zo transportation cost ans zo B zo 1 lichen llyups mass. (1)

$$Z = 20x_{A1} + 16x_{AII} + 24x_{AIII} + 16x_{B2} + 18x_{BII} + 12x_{BIII} = 364$$

$$3. \text{ reduced cost } x_{21} = \Delta Z - Ax_{21} = 364 - 359 - 1 \cdot 5 = -1$$

4. To reduced cost jya zo x<sub>21</sub> eivai apravu. Ans sukaiva su n lichen

Sei eine optimale Rute von  $A \rightarrow$  ans zu 15 i

Apä exakte ou in apxim für Juch eine optimal Rute von  
transportation costs ans zu B or I. Minizipra ist 15

	I	II	III	Supply
A	6 $\frac{20}{}$	4 $\frac{16}{}$	2 $\frac{24}{}$	$10 \cancel{x} 0$
B	$\frac{15}{}$	5 $\frac{18}{}$	10 $\frac{12}{}$	$15 \cancel{x} 0$
C	$\frac{18}{}$	-	2 $\frac{16}{}$	$5 \cancel{x} 3$
Demand	6	$\cancel{9} 5$	$\cancel{12} 2$	0

Optimaler wert von Juch für ein feldes North West Corner

$$u_1 = 0, u_1 + v_1 = 20 \Rightarrow v_1 = 20, u_1 + v_2 = 16 \Rightarrow v_2 = 16$$

$$u_2 = 0, u_2 + v_2 = 13 \Rightarrow u_2 = 13 - 16 \Rightarrow u_2 = 2, u_2 + v_3 = 12 \Rightarrow v_3 = 10$$

$$u_3, u_3 + v_3 = 16 \Rightarrow u_3 = 6$$

$$w_{13} = u_1 + v_3 - c_{13} = 10 - 24 < 0 \quad \text{Apä Sei}$$

$$w_{21} = u_2 + v_1 - c_{21} = 2 + 20 - 15 = 7 > 0 \quad \left\{ \begin{array}{l} \text{etral optimal} \\ \dots \end{array} \right.$$

$$w_{31} = u_3 + v_1 - c_{31} = 6 + 20 - 13 = 3 > 0$$

Kivautet Vogel:

	I	II	III		row1	col1	Diagonale zu $v_1$ :
A	1 $\frac{20}{}$	9 $\frac{16}{}$	2 $\frac{24}{}$	$10 \cancel{x} 0$	4	3	(1,2) war biefalte
B	3 $\frac{15}{}$	5 $\frac{18}{}$	12 $\frac{12}{}$	$15 \cancel{x} 0$	3	2	$\min\{9, 10\} = 9$
C	2 $\frac{18}{}$	-	2 $\frac{16}{}$	$5 \cancel{x} 3$	2	4	
Demand	6	$\cancel{9} 5$	$\cancel{12} 2$	0			

row2	col2	Diagonale zu	row3	col3	Diagonale zu
4	3	$v_1$ : (1,1) war	-	3	$v_2$ : (2,3) war biefalte
3	-	biefalte $\min\{1, 6\} = 1$	3	-	$\min\{12, 15\} = 12$
2	4		2	4	

Zwischenfuß (c) optimale Zerlegung der vorgelegten Menge. Einheitsvektor  $\bar{v}$  ist optimal in Zerosumme.

$$u_1 = 0, \quad u_1 + v_1 = 20 \Rightarrow v_1 = 20$$

$$w_{13} = u_1 + v_3 - c_{13} = 17 - 24 < 0$$

$$u_1 + v_2 = 16 \Rightarrow v_2 = 16$$

$$w_{22} = u_2 + v_2 - c_{22} = -5 + 16 - 13 < 0$$

$$u_2 + v_1 = 15 \Rightarrow u_2 = -5$$

$$w_{33} = u_3 + v_3 - c_{33} = -2 + 17 - 16 < 0$$

$$u_2 + v_3 = 12 \Rightarrow v_3 = 12 + 5 = 17$$

$$u_3 + v_1 = 18 \Rightarrow u_3 = -2$$

Apa in Zerosumme nicht optimal

Exkope

$$Z = 20 + 9 \cdot 16 + 3 \cdot 15 + 12 \cdot 12 + 2 \cdot 18 = 389$$

Für jene zu (a) Exkope

$$Z_A = 20 + 9 \cdot 16 + 5 \cdot 15 + 10 \cdot 12 = 359$$

Apa öxi in Zerosumme (a) Sehr ungünstige Bedingungen

## Άσκηση 4

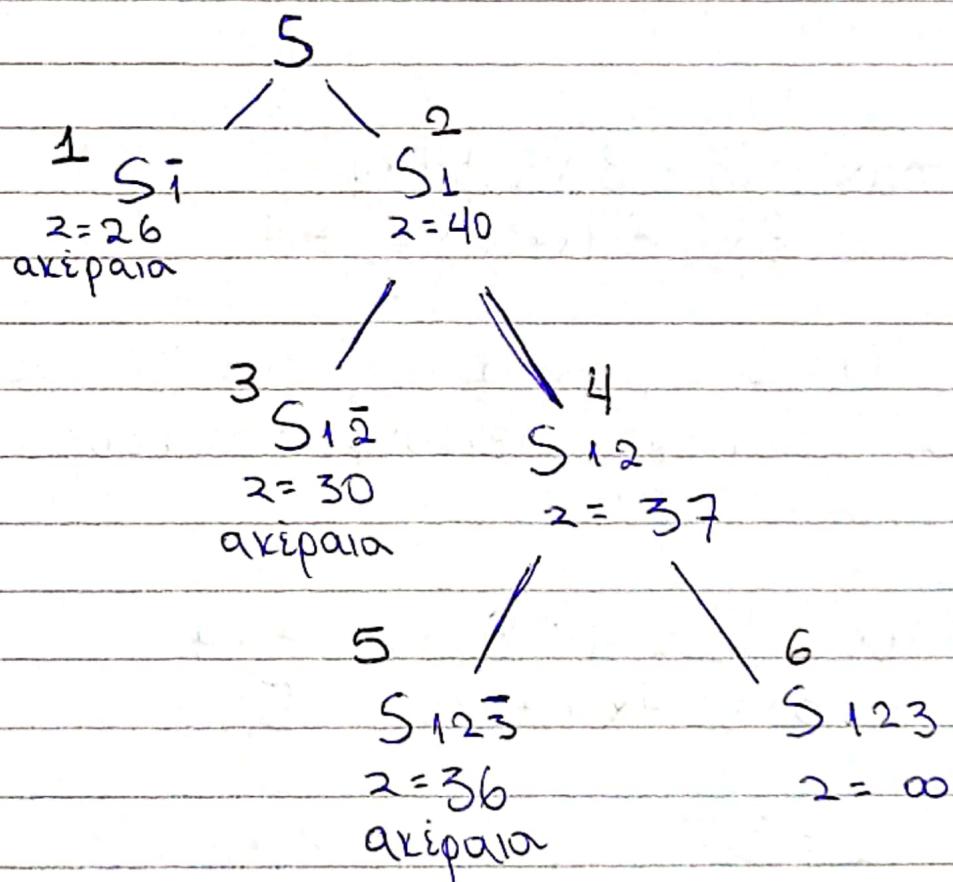
$$\text{maximize } z = 18x_1 + 14x_2 + 8x_3 + 4x_4$$

$$\text{subject to } 18x_1 + 14x_2 + 8x_3 + 4x_4 + x_5 \leq 37$$

$$x_i \in \{0, 1\}$$

### a) Depth First Search

Ανάλυση του δέντρου αναζήτησης. (οι αριθμοί δειχνούν τη σειρά της αναζήσεως κόπωση)



Για να υπολογισούνται οι συνεχείς δύσεις χαλαρώνουνται τους αριθμητικούς  $x_i \in \{0, 1\}$  σε  $x_i \in [0, 1]$ .

$$S_7 : \max 14x_2 + 8x_3 + 4x_4$$

$$14x_2 + 8x_3 + 4x_4 + x_5 \leq 37$$

$$x_2 = 1, x_3 = 1, x_4 = 1, x_5 = 1, z = 26$$

ακέραια λύση

$\Rightarrow$  δεν ενεργούνται τα κόπτο παραπάνω.

$$S_1 : \max 14x_2 + 8x_3 + 4x_4$$

$$14x_2 + 8x_3 + 4x_4 + x_5 \leq 19$$

$$x_2 = 1, x_3 = \frac{5}{8}, z = 40$$

$$S_{12} : \max 18 + 8x_3 + 4x_4$$

$$8x_3 + 4x_4 + x_5 \leq 19$$

$$x_3 = 1, x_4 = 1, x_5 = 1, z = 30 \text{ ακέραια λύση}$$

δεν ενεργούνται τα κόπτο αδιό.

$$S_{12} : \max 18 + 14 + 8x_3 + 4x_4$$

$$8x_3 + 4x_4 + x_5 \leq 5$$

$$x_3 = \frac{5}{8}, z = 37, 37 > \text{ανί ψηλιαστη}$$

ακέραια λύση αρι

ενεργούνται τα κόπτο

$$S_{12\bar{3}} : \max 18 + 14 + 4x_4 \\ 4x_4 + x_5 \leq 5$$

$x_4 = 1, x_5 = 1, z = 36 \rightarrow$  ακέραια άνω  
σεν επεκτείνουμε το κύρβο

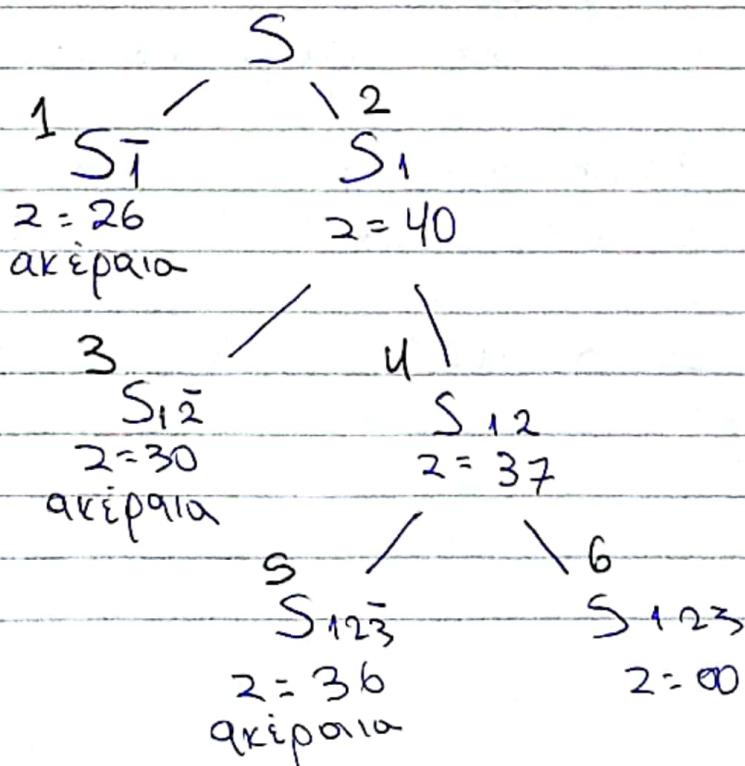
$$S_{123} : \max 18 + 14 + 8 + 4x_4 \\ 4x_4 + x_5 \leq -3$$

σεν παραγόμει ως αποριούς,  $z = 00$   
σεν επεκτείνουμε το κύρβο

Τετράκα η βέλτιστη ακέραια άνω είναι  
 $\eta : x_1 = 1, x_2 = 1, x_3 = 0, x_4 = 1, x_5 = 1$   
π.χ.  $z = 36$

### β) Breadth First Search

Δέντρο αρχής:



Si  $\max 14x_2 + 8x_3 + 4x_4$   
 $14x_2 + 8x_3 + 4x_4 + x_5 \leq 37$   
 $x_2 = 1, x_3 = 1, x_4 = 1, x_5 = 1, z = 26$   
 akrepatai zivn  
 Sev ta enekterivapti zo kópbo žawi

S<sub>1</sub>:  $\max 14x_2 + 8x_3 + 4x_4$   
 $14x_2 + 8x_3 + 4x_4 + x_5 \leq 19$   
 $x_2 = 1, x_3 = \frac{5}{8}, z = 40$

S<sub>12</sub>:  $\max 18 + 8x_3 + 4x_4$   
 $8x_3 + 4x_4 + x_5 \leq 19$   
 $x_3 = 1, x_4 = 1, x_5 = 1, z = 30$  akrepatai zivn

S<sub>12</sub>:  $\max 18 + 14 + 8x_3 + 4x_4$   
 $8x_3 + 4x_4 + x_5 \leq 5$   
 $x_3 = \frac{5}{8}, z = 37$

S<sub>123</sub>:  $\max 18 + 14 + 4x_4$   
 $4x_4 + x_5 \leq 5$   
 $x_4 = 1, x_5 = 1, z = 36$  akrepatai zivn

S<sub>123</sub>:  $\max 18 + 14 + 8 + 4x_4$   
 $4x_4 + x_5 \leq -3$   $z = \infty$

(ε)ika n βέτυση akrepatai zivn eivdu  
 n  $z = 36$  pε:

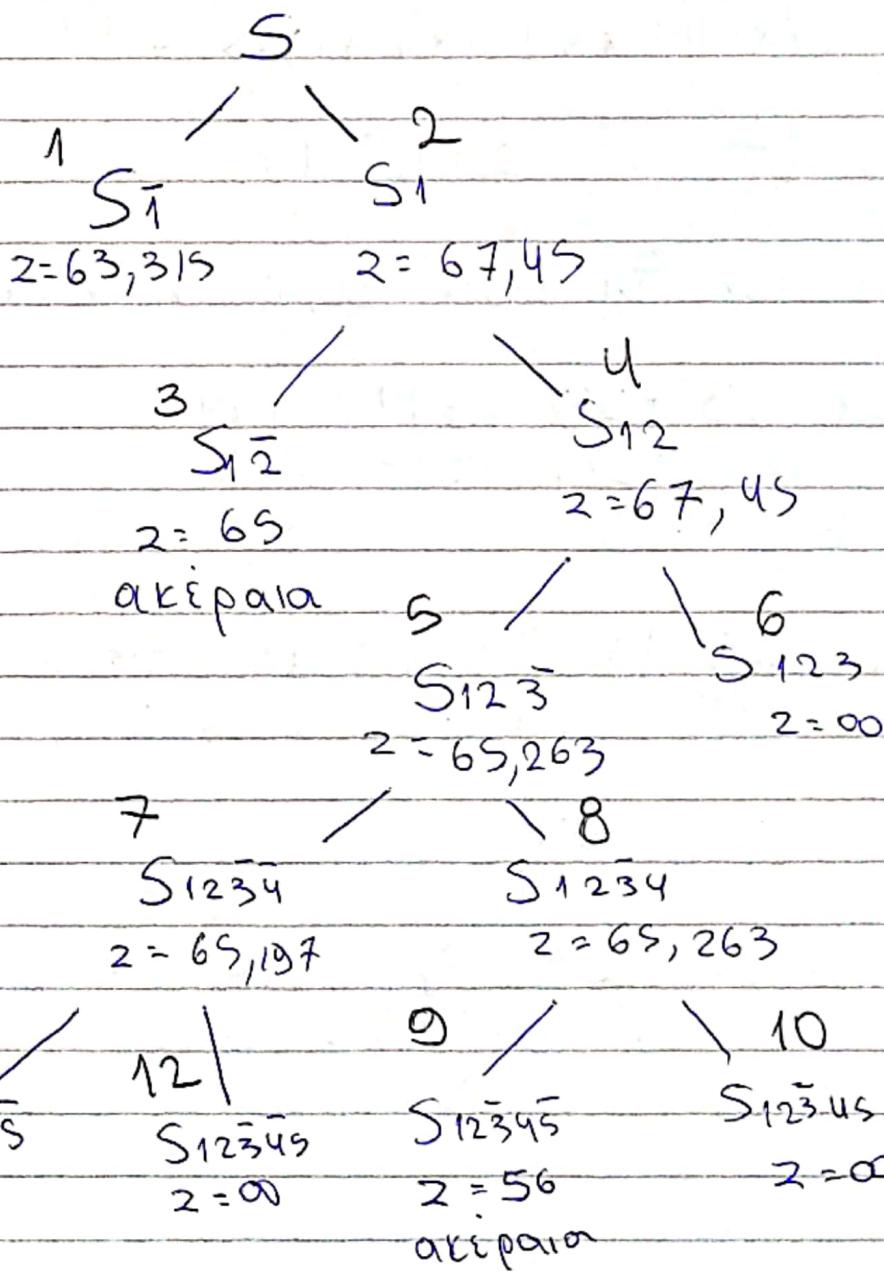
$x_1 = 1, x_2 = 1, x_3 = 0, x_4 = 1, x_5 = 1$

## Aσχνον 5

maximize  $Z = 23x_1 + 19x_2 + 28x_3 + 14x_4 + 44x_5$   
 subject to  $8x_1 + 7x_2 + 11x_3 + 6x_4 + 19x_5 \leq 25$   
 $x_i \in \{0, 1\}$

### a) Best First Search

Ανάδυση δέντρου αναζήτησης



Για να υπολογίσουμε τις συνεχείς λύσεις  
 χαλαρώνουμε τους ορισμένους προβολές  $x_i \in \{0, 1\}$   
 σε  $x_i \in [0, 1]$ .

$$S_1: \max 19x_2 + 28x_3 + 14x_4 + 44x_5 \\ 7x_2 + 11x_3 + 6x_4 + 19x_5 \leq 25$$

$$x_2 = 1, x_3 = 1, x_4 = 1, x_5 = \frac{1}{19}, z = 63,315$$

$$S_1: \max 23 + 19x_2 + 28x_3 + 14x_4 + 44x_5 \\ 7x_2 + 11x_3 + 6x_4 + 19x_5 \leq 17$$

$$x_2 = 1, x_3 = \frac{10}{11}, z = 67,45$$

Επεκτείνουμε τον  $S_1$  που είναι ο βέτας.

$$S_{12}: \max 23 + 28x_3 + 14x_4 + 44x_5 \\ 11x_3 + 6x_4 + 19x_5 \leq 17$$

$$x_3 = 1, x_4 = 1, x_5 = 0, z = 65$$

$$S_{12}: \max 23 + 19 + 28x_3 + 14x_4 + 44x_5 \\ 11x_3 + 6x_4 + 19x_5 \leq 10$$

$$x_3 = \frac{10}{11} \quad z = 67,45$$

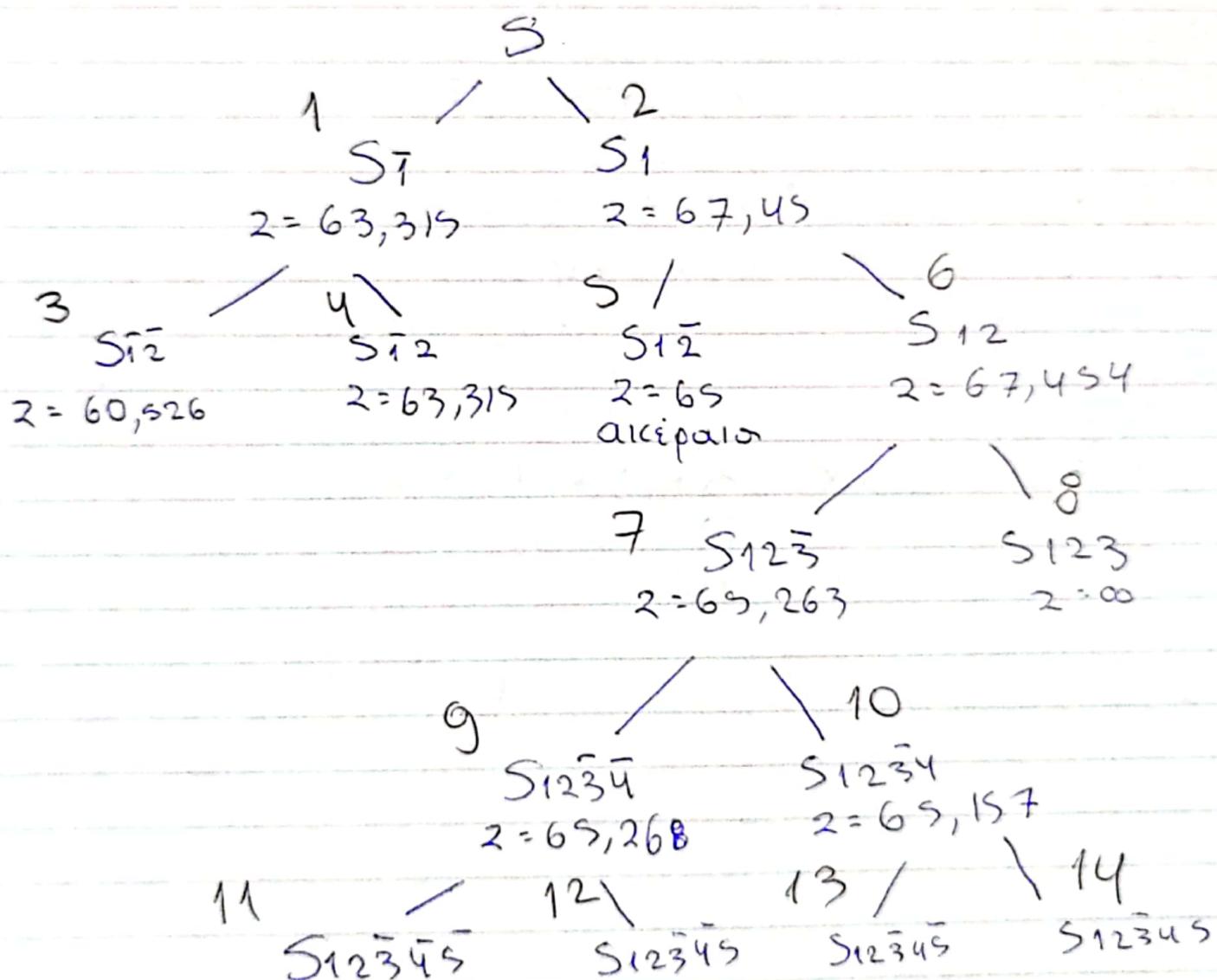
$$S_{123}: \max 23 + 19 + 14x_4 + 44x_5 \\ 6x_4 + 19x_5 \leq 10$$

$$x_4 = 1, x_5 = 4/19, z = 65,263$$

zadika max  $z = 6S$  kou

$$x_1=1, x_2=0, x_3=1, x_4=1, x_5=0$$

### B) Breadth First Search



$$S_{123}: \max 23 + 19 + 28 + 14x_4 + 44x_5 \\ 6x_4 + 19x_5 \leq -1 \\ z = \infty$$

$$S_{123\bar{4}}: \max 23 + 19 + 44x_5 \\ 19x_5 \leq 10$$

$$x_5 = \frac{10}{19}, \quad z = 65,197$$

$$S_{12\bar{3}4}: \max 23 + 19 + 14 + 44x_5 \\ 19x_5 \leq 4 \\ x_5 = \frac{4}{19}, \quad z = 65,263$$

$$S_{12\bar{3}45}: \max 23 + 19 + 14 + 44 \\ 19 \leq 4 \quad \text{δεν } 10x_5 \\ z = \infty$$

$$S_{12\bar{3}4\bar{5}}: \max 23 + 19 + 14$$

$$z = 56$$

$$S_{12\bar{3}\bar{4}5}: \max 23 + 19 + 44 \\ \text{δεν } 10x_4 + 19x_5 \leq 4 \\ z = \infty$$

$$S_{12\bar{3}\bar{4}\bar{5}}: \max 23 + 19 \\ 0 \leq 10 \\ z = 42$$

Δεν επεκτείνεται στη γιανή έχει μικρότερο  
z από τη βέλτιστη συλλογή των.

$$S_1: \max z = 19x_2 + 28x_3 + 14x_4 + 44x_5$$

$$7x_2 + 11x_3 + 6x_4 + 19x_5 \leq 25$$

$$x_2=1, x_3=1, x_4=1, x_5=\frac{1}{19}, z=63,315$$

$$S_1: \max z = 23 + 10x_2 + 28x_3 + 14x_4 + 44x_5$$

$$7x_2 + 11x_3 + 6x_4 + 19x_5 \leq 17$$

$$x_2=1, x_3=\frac{10}{11}, z=67,45$$

$$S_{12}: \max z: 19 + 28x_3 + 14x_4 + 44x_5$$

$$11x_3 + 6x_4 + 19x_5 \leq 18$$

$$x_3=1, x_4=1, x_5=\frac{1}{19}, z=63,315$$

$$S_{12}: \max z: 28x_3 + 14x_4 + 44x_5$$

$$11x_3 + 6x_4 + 19x_5 \leq 25$$

$$x_3=1, x_4=1, x_5=\frac{8}{19}, z=60,526$$

$$S_{12}: \max z: 23 + 28x_3 + 14x_4 + 44x_5$$

$$11x_3 + 6x_4 + 19x_5 \leq 17$$

$$x_3=1, x_4=1, x_5=0, z=65$$

$$S_{12}: \max z = 23 + 10 + 28x_3 + 14x_4 + 44x_5$$

$$11x_3 + 6x_4 + 19x_5 \leq 10$$

$$x_3=\frac{10}{11}, z=67,454$$

$$S_{1\bar{2}\bar{3}}: \max z = 23 + 14x_4 + 44x_5$$
$$6x_4 + 19x_5 \leq 17$$

$$x_4 = 1, x_5 = \frac{11}{19}, z = 62,473$$

$$S_{1\bar{2}3}: \max z = 23 + 28 + 14x_4 + 44x_5$$
$$6x_4 + 19x_5 \leq 6$$

$$x_4 = 1, z = 65$$

$$S_{12\bar{3}}: \max z = 23 + 19 + 14x_4 + 44x_5$$
$$6x_4 + 19x_5 \leq 10$$

$$x_4 = 1, x_5 = \frac{4}{19}, z = 65,263$$

$$S_{123}: \max z = 23 + 19 + 28 + 14x_4 + 44x_5$$
$$6x_4 + 19x_5 \leq 1, z = \infty$$

$$S_{12\bar{3}4}: \max z = 23 + 19 + 14 + 44x_5$$
$$19x_5 \leq 4$$
$$x_5 = \frac{4}{19}, z = 65,263$$

$$S_{12\bar{3}\bar{4}}: \max z = 23 + 19 + 44x_5$$
$$19x_5 \leq 10$$
$$x_5 = \frac{10}{19}, z = 65,157$$

$$S_{12\bar{3}4\bar{5}}: \max z = 23 + 19 \\ 8 + 7 \leq 25$$

$$z = 42$$

$$S_{12\bar{3}\bar{4}5}: \max z = 23 + 19 + 44 \\ 8 + 7 + 19 \leq 25 \\ 34 \leq 25 \quad \text{Sehr loxig}$$

$$z = \infty$$

$$S_{12\bar{3}4\bar{5}}: \max z = 23 + 19 + 14 \\ 8 + 7 + 6 \leq 25 \\ z = 56$$

$$S_{12\bar{3}4\bar{5}} \quad \max z = 23 + 19 + 14 + 44 \\ 8 + 7 + 6 + 19 \leq 25 \quad \text{Sehr loxig} \\ z = \infty$$

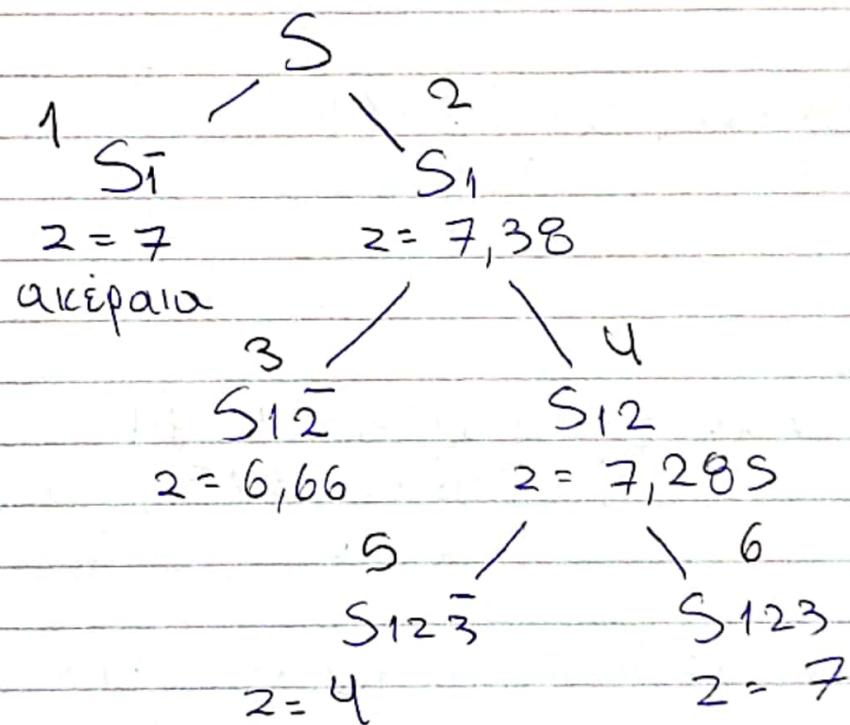
Tekika n βελτιωτη λυση ειναι  
 $n \quad z = 65 \quad \mu\varepsilon$

$$x_1 = 1, x_2 = 0, x_3 = 1, x_4 = 1, x_5 = 0$$

Aσκνσν 6

maximize  $Z = 2x_1 - x_2 + 5x_3 - 2x_4 + 4x_5$   
subject to  $3x_1 - 2x_2 + 7x_3 - 5x_4 + 4x_5 \leq 6$   
 $x_1 - x_2 + 2x_3 - 4x_4 + 2x_5 \leq 0$

Best First Search:



$S_1$ :  $\max Z = -x_2 + 5x_3 - 2x_4 + 4x_5$   
 $-2x_2 + 7x_3 - 5x_4 + 4x_5 \leq 6$   
 $-x_2 + 2x_3 - 4x_4 + 2x_5 \leq 0$

$x_2 = 0, x_3 = 1, x_4 = 1, x_5 = 1, Z = 7$

$$S_1: \max z = 2 - x_2 + 5x_3 - 2x_4 + 4x_5$$

$$-2x_2 + 7x_3 - 5x_4 + 4x_5 \leq 3$$

$$-x_2 + 2x_3 - 4x_4 + 2x_5 \leq -1$$

$$x_1=1, x_2=1, x_3=\frac{6}{7}, x_4=1, x_5=1, z=7,28$$

$$S_{1\bar{2}}: \max z = 2 + 5x_3 - 2x_4 + 4x_5$$

$$7x_3 - 5x_4 + 4x_5 \leq 3$$

$$2x_3 - 4x_4 + 2x_5 \leq -1$$

$$x_3 = \frac{2}{3}, x_4 = 1, x_5 = \frac{5}{6} \quad z = 6,666$$

$$S_{12}: \max z = 1 + 5x_3 - 2x_4 + 4x_5$$

$$7x_3 - 5x_4 + 4x_5 \leq 5$$

$$2x_3 - 4x_4 + 2x_5 \leq 0$$

$$x_3 = \frac{6}{7}, x_4 = 1, x_5 = 1, z = 7,285$$

$$S_{12\bar{3}}: \max z = 1 - 2x_4 + 4x_5$$

$$-5x_4 + 4x_5 \leq 5$$

$$-4x_4 + 2x_5 \leq 0$$

$$x_4 = \frac{1}{2}, x_5 = 1 \quad z = 4$$

$$S_{123}: \max z = 6 - 2x_4 + 4x_5$$
$$-5x_4 + 4x_5 \leq -2$$
$$-4x_4 + 2x_5 \leq -2$$

$$x_4 = 1, x_5 = \frac{3}{4}, z = 7$$

Apoj  $\max z = 7$  p.e

$$x_1 = 0, x_2 = 0, x_3 = 1, x_4 = 1, x_5 = 1$$