

$$8.2) b) \mu = 15 \quad \sigma = 4.824 (?)$$

$$P(20 \leq X \leq 20) \stackrel{!}{=} 0.7$$

$$P\left(\underbrace{\frac{10-15}{\sigma}}_{y_{70}} \leq \underbrace{X}_{y} \leq \underbrace{\frac{20-15}{\sigma}}_{y_{70}}\right) \stackrel{!}{=} 0.7$$

$$y_{70} - y_{30} = 0.7$$

$$N\left(\frac{5}{\sigma}\right) - 1 - N\left(\frac{5}{\sigma}\right) \stackrel{!}{=} 0.7$$

$$2 N\left(\frac{5}{\sigma}\right) \stackrel{!}{=} 1.7$$

$$N\left(\frac{5}{\sigma}\right) \stackrel{!}{=} 0.85$$

$$N(1.04) = 0.8508$$

$$\Rightarrow \frac{5}{\sigma} = 1.04 \Rightarrow \underline{\underline{\sigma = 4.8077}}$$

$$a) \mu = 30 \quad \sigma = 4$$

$$P(X \leq 34.32) = N\left(\frac{34.32 - 30}{4}\right) = 0.8599 = 85.99\%$$

$$8.3) a) \sigma^2 = 72.43 \quad \sigma = 8.511$$

$$P(X > 166) = 0.95 \Rightarrow P(X \leq 166) = 0.05$$

~~normal distribution~~

$$F(x) = \underbrace{\frac{1}{\sigma \sqrt{2\pi}}}_A \int_{-\infty}^x e^{-\frac{(t-\mu)^2}{\underbrace{2\sigma^2}_B}} dt$$

$$\frac{F(x)}{A} = 1.066296 = \int_0^{166} e^{-\frac{(t-\mu)^2}{B}} dt$$

$$8.4) a) L(\lambda) = f(x_1; \lambda) \cdot f(x_2; \lambda) \cdot \dots \cdot f(x_n; \lambda)$$

$$= \underbrace{\lambda e^{-\lambda x_1}}_{f-11, x \geq 0} \cdot \lambda e^{-\lambda x_2} \cdot \dots \cdot \lambda e^{-\lambda x_n} \quad \left. \vphantom{\lambda e^{-\lambda x_1}} \right\} \log$$

$$\log L(\lambda) = \frac{\lambda^n}{e^{\sum_{i=1}^n (\lambda x_i)}}$$

$$b) \log L(\lambda) = \frac{\lambda^n}{e^{\sum_{i=1}^n (\lambda x_i)}}$$

$$\log_{\lambda} L(\lambda) = \lambda^{n-1} \cdot e^{-\sum_{i=1}^n (\lambda x_i)} \cdot \left(n - \lambda \cdot \sum_{i=1}^n x_i \right) \stackrel{!}{=} 0$$

$$\log L(\lambda) = n \ln(\lambda) - \lambda \sum_{i=1}^n x_i$$