

## Assignment 9 (Programming)

Use methods 1-4 to estimate the probability that we hire exactly twice:

1. Output  $\frac{1}{n} \sum_{i=2}^n \frac{1}{i-1}$  ;
2. Generate 10,000 random arrays of ranks, check  $s$  : the number of arrays where we hire exactly twice, and output the probability:  $\frac{s}{10,000}$  ;
3. Generate 1,000,000 random arrays of ranks, check  $s$  : the number of arrays where we hire exactly twice, and output the probability:  $\frac{s}{1,000,000}$  ;
4. Enumerate all the  $n!$  permutations of the arrays of ranks, check  $s$  - the number of arrays where we hire exactly twice, and output the probability:  $\frac{s}{n!}$ .

Compare the results you get from method 1, 2, 3, and 4 for  $n=6$ , 8, and 10 in terms of the probability.

For  $n=6$ , output all the cases (arrays of ranks) that we hire exactly twice.

For  $n = 30, 50, 100$ , compare the results you get from method 1, 2, and 3 in terms of the probability.