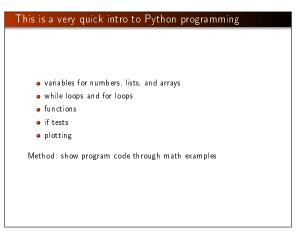
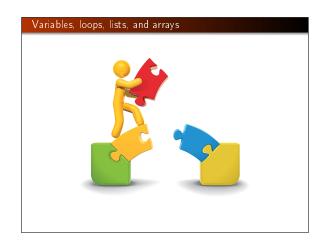
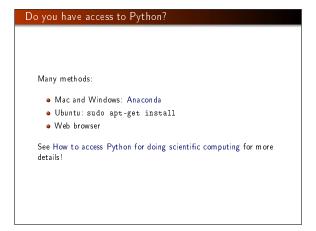
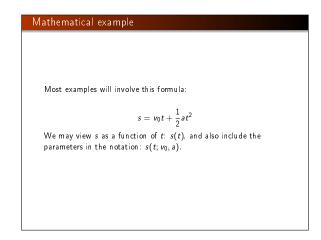
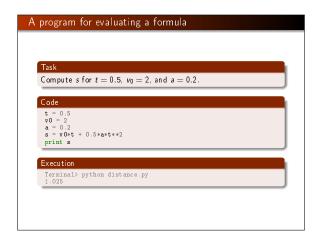
# Intro to scientific Python programming Hans Petter Langtangen<sup>1,2</sup> Simula Research Laboratory<sup>1</sup> University of Oslo<sup>2</sup> Jan 9, 2015











## Assignment statements assign a name to an object t = 0.5 v0 = 2 a = 0.2 s = v0\*t + 0.5\*a\*t\*\*2 Rule: evaluate right-hand side object, left-hand side is a name for that object

```
    Task: write out s=1.025
    Method: printf syntax
    print 's="%g' % s  # g: compact notation print 's="% 21' % s  # f: decimal notation, .2f: 2 decimals
    Modern alternative: format string syntax
    print 's={s:.2f}' .format(s=s)
```

```
Programming with a while loop

• Task: write out a table of t and s(t) values (two columns), for t ∈ [0,2] in steps of 0.1

• Method: while loop

v0 = 2
a = 0.2
dt = 0.1 # Increment
t = 0 # Start value
while t <= 2:
s = v0+t + 0.5*a*t**2
print t, s
t = t + dt
```

```
Output of the previous program

Terminal> python while.py
0 0.0
0.1 0.201
0.2 0.404
0.3 0.609
0.4 0.816
0.5 1.025
0.6 1.236
0.7 1.449
0.8 1.664
0.9 1.881
1.0 2.1
1.1 2.321
1.1 2.321
1.2 2.544
1.3 2.769
1.4 2.996
1.5 3.255
1.6 3.456
1.7 3.689
1.8 3.924
1.9 4.161
```

```
The Python Online Tutor can help you understand the program flow

Python Online Tutor lets you step through the program and examine variables.

a = 1
da = 0.5
while a <= 3:
print a
a = a + da

(Visualize execution)
```

```
Lists

A list collects several variables (objects) in a given sequence:

L = [-1, 1, 8.0]

A list can contain any type of objects, e.g.,

L = ['mydata.txt', 3.14, 10]

Some basic list operations:

>>> L = ['mydata.txt', 3.14, 10]

>>> print L[0]

mydata.txt
>>> print L[1]

3.14

>>> del L[0]  # delete the first element
>>> print L

[3.14, 10]

>>> print L

[3.14, 10]

>>> print L

[3.14, 10]

| Add -1 at the end of the list
| Call, 13, 14, 10, -1]
```

```
v0 = 2
a = 0.2
dt = 0.1  # Increment
t = 0
t_values = []
s_values = []
while t <= 2:
    s = v0*t + 0.5*a*t**2
    t_values append(t)
    s_values append(s)
    t = t + dt
print s_values # Just take a look at a created list

# Print a nicely formatted table
i = 0
while i <= len(t_values)-1:
    print '%.2f %, 4f' % (t_values[i], s_values[i])
    i += 1  # Same as i = i + 1</pre>
```

```
For loops

A for loop is used for visiting elements in a list, one by one:

>>> L = [1, 4, 8, 9]
>>> for e in L:
... print e

1
4
8
9

Demo in the Python Online Tutor:

list1 = [0, 0.1, 0.2]
list2 = []
for element in somelist:
    p = element + 2
    list2 append(p)
    print list2

(Visualize execution)
```

```
For loops used traditionally an integer counter over list/array indices

for i in range(len(somelist)):
    # Work with somelist[i]

Note:

• range returns a list of integers
• range(a, b, s) returns the integers a, a+s, a+2*s, ...
    up to but not including (!!) b
• range(b) implies a=0 and s=1
• range(len(somelist)) returns [0, 1, 2]
```

```
Let's replace our while loop by a for loop

v0 = 2
a = 0.2
dt = 0.1  # Increment
t_values = []
s_values = []
n = int(round(2/dt)) + 1  # No of t values
for i in range(n):
t = i*dt
s = v0*t + 0.5*a*t**2
t_values.append(t)
s_values.append(t)
s_values = spend(s)
print s_values  # Just take a look at a created list
# Make nicely formatted table
for t, s in zipt(t_values, s_values):
    print '%.2f  %.4f' % (t, s)

# Alternative
for i in range(len(t_values)):
    print '%.2f  %.4f' % (t_values[i], s_values[i])
```

```
Traversal of multiple lists at the same time with zip

for e1, e2, e3, ... in zip(list1, list2, list3, ...):

Alternative: loop over a common index for the lists

for i in range(len(list1)):
    e1 = list1[i]
    e2 = list2[i]
    ...
```

## 

```
numpy functions creates entire arrays at once

>>> c = numpy.log(a)  # Take ln of all elements in a
>>> print c
[ 0. 1.38629436 2.30258509]

Create n + 1 uniformly distributed coordinates in [a, b]:
t = numpy.linspace(a, b, n+1)
```

```
import numpy
v0 = 2
a = 0.2
dt = 0.1 # Increment
n = int(round(2/dt)) + 1 # No of t values

t.values = numpy.linspace(0, 2, n+1)
s_values = v0+t + 0.5**a*t**2
# Make nicely formatted table
for t, s in zip(t_values, s_values):
    print '%.2f %.4f' % (t, s)
```

```
Standard mathematical functions are found in the math module

>>> import math
>>> print math sin(math.pi)
1.2246467991473532e-16  # Note: only approximate value

Get rid of the math prefix:

from math import sin, pi
print sin(pi)

# Or import everything from math
from math import *
print sin(pi), log(e), tanh(0.5)
```

```
Use the numpy module for standard mathematical functions applied to arrays

Matlab users can do

from numpy import *

The Python community likes

import numpy as np
print np.sin(np.pi)

Our convention: use np prefix, but not in formulas involving math functions

import numpy as np
from numpy import sin, exp
t = np.linepace(0, 4, 1001)
p = exp(-t)*sin(2*t)
```

```
Plotting is done with matplotlib:

import numpy as np
import matplotlib.pyplot as plt

v0 = 0.2
a = 2
n = 21 # No of t values for plotting

t = np.linspace(0, 2, n+1)
s = v0*t + 0.5*a*t**2

plt.plot(t, s)
plt.savefig('myplot.png')
plt.show()

The plotfile myplot.png looks like
```

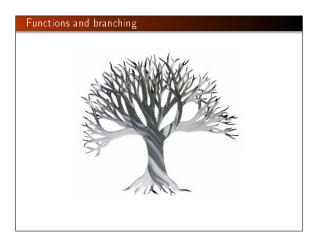
```
Plotting of multiple curves

import numpy as np
import matplotlib.pyplot as plt

v0 = 0.2
a = 2
n = 21  # No of t values for plotting

t = np.linspace(0, 2, n+1)
s = v0*t + 0.5*a*t**2

plt.plot(t, s)
plt.savefig('myplot.png')
plt.show()
```



### Functions

- $s(t) = v_0 t + \frac{1}{2} a t^2$  is a mathematical function
- Can implement s(t) as a Python function s(t)

```
def s(t):
    return v0*t + 0.5*a*t**2
v0 = 0.2
a = 4
value = s(3)  # Call the function
```

### Note:

- functions start with the keyword def
- statements belonging to the function must be indented
- function input is represented by arguments (separated by comma if more than one)
- function output is returned to the calling code
- v0 and a are global variables
- $\bullet$  v0 and a must be initialzed before s is called

### Functions can have multiple arguments

vO and a as function arguments instead of global variables:

```
def s(t, v0, a):
    return v0*t + 0.5*a*t**2
value = s(3, 0.2, 4)  # Call the function
# Hore readable call
value = s(t*3, v0*=0.2, a*4)
```

### Keyword arguments are arguments with default values

```
def s(t, v0=1, a=1):
    return v0*t + 0.5*a*t**2

value = s(3, 0.2, 4)  # specify new v0 and a
value = s(3, a=2)  # rely on v0=1 and a=1
value = s(3, a=2)  # rely on v0=1
value = s(3, v0=2)  # rely on a=1
value = s(t=3, v0=2, a=2)  # specify everything
value = s(t=3, v0=2, a=2)  # any sequence allowed
```

- Arguments without the argument name are called positional arguments
- Positional arguments mustalways be listed before the keyword arguments in the function and in any call
- The sequence of the keyword arguments can be arbitrary

### Vectorization speeds up the code

```
Scalar code (work with one number at a time):

def s(t, v0, a):
    return v0*t + 0.5*a*t**2

for i in range(len(t)):
    s_values[i] = s(t_values[i], v0, a)
```

 $\label{prop:condition} Vectorized\ code:\ \ \mbox{apply s to the entire array}$ 

```
s_values = s(t_values, v0, a)
```

How can this work?

- Array: t
- Expression: v0\*t + 0.5\*a\*t\*\*2
- r1 = v0\*t (scalar times array)
- r2 = t\*\*2 (square each element)
- r3 = 0.5\*a\*r2 (scalar times array)r1 + r3 (add each element)

## Python functions written for scalars normally work for arrays too!

True if computations involve arithmetic operations and math functions:

```
from math import exp, sin

def f(x):
    return 2*x + x**2*exp(-x)*sin(x)

v = f(4)  # f(x) works with scalar x

# Redefine exp and sin with their vectorized versions from numpy import exp, sin, linspace x = linspace(0, 4, 100001)

v = f(x)  # f(x) works with array x
```

However, if tests are not allowed:

```
def f(x):
    return -1 if x < 0 else x**4*exp(-x)*sin(x)
x = linspace(0, 4, 100001)
y = f(x) # will not work</pre>
```

### Python functions can return multiple values

### A more general mathematical formula

Equations from basic kinematics:

$$v = \frac{ds}{dt}, \quad s(0) = s_0$$
$$a = \frac{dv}{dt}, \quad v(0) = v_0$$

Integrate to find v(t):

$$\int_0^t a(t)dt = \int_0^t \frac{dv}{dt}dt$$

which gives

$$v(t) = v_0 + \int_0^t a(t)dt$$

Integrate again over [0, t] to find s(t):

### Basic if-else tests

An if test has the structure

```
if condition:
     <statements when condition is True>
else:
           <statements when condition is False>
```

Tuples are constant lists (cannot be changed)

Here,

• condition is a boolean expression with value True or False.

```
 \begin{array}{lll} \mbox{if } t <= t1: \\ \mbox{s} = v0*t + 0.5*a0*t**2 \\ \mbox{else:} \\ \mbox{s} = v0*t + 0.5*a0*t1**2 + a0*t1*(t-t1) \\ \end{array}
```

### Multi-branch if tests

### Implementation of a piecewisely defined function with if

A Python function implementing the mathematical function (??)

## Python functions containing if will not accept array arguments

```
>>> def f(x): return x if x < 1 else 2*x
...
>>> import numpy as np
>>> x = np.linspace(0, 2, 5)
>>> f(x)
Traceback (most recent call last):
...
ValueError: The truth value of an array with more than one element is ambiguous. Use a.any() or a.all()
```

Problem: x < 1 evaluates to a boolean array, not just a boolean

### Remedy 1: Call the function with scalar arguments

```
n = 201  # No of t values for plotting
t1 = 1.5

t = np.linspace(0, 2, n+1)
s = np.zeros(n+1)
for i in range(len(t));
    s[i] = s_func(t=t[i], v0=0.2, a0=20, t1=t1)

Can now easily plot:
plt.plot(t, s, 'b-')
plt.plot([t1, t1], [0, s_func(t=t1, v0=0.2, a0=20, t1=t1)], 'r--')
plt.ylabel('t')
plt.ylabel('t')
plt.ylabel('s')
plt.savefig('myplot.png')
plt.show()
```

### Remedy 2: Vectorize the if test with where

Functions with if tests require a complete rewrite to work with arrays.

```
s = np.where(condition, s1, s2)
```

### Explanation:

- condition: array of boolean values
- s[i] = s1[i] if condition[i] is True
- s[i] = s2[i] if condition[i] is False

Our example then becomes

Note that t <= t1 with array t and scalar t1 results in a boolean array b where b[i] = t[i] <= t1.

### • Let b be a boolean array (e.g., b = t <= t1)

- s[b] selects all elements s[i] where b[i] is True
- Can assign some array expression expr of length len(s[b]) to s[b]: s[b] = (expr)[b]

Our example can utilize this technique with b as t <= t1 and t > t1:

### Classes

- All objects in Python are made from a class
- You don't need to know about classes to use Python
- But class programming is powerful
- Class = functions + variables packed together
- A class is a logical unit in a program
- A large program as a combination of appropriate units

ans Petter Langtangen

### A very simple class

- One variable: a
- One function: dump for printing a

```
class Trivial:
    def __init__(self, a):
        self.a = a

    def dump(self):
        print self.a
```

Class terminology: Functions are called *methods* and variables are called *attributes*.

### How can we use this class?

First, make an instance (object) of the class:

```
t = Trivial(a=4)
t.dump()
```

### Note:

- The syntax Trivial(a=4) actually means Trivial.\_\_init\_\_(t, 4)
- self is an argument in \_\_init\_\_ and dump, but not used in the calls
- \_\_init\_\_ is called constructor and is used to construct an object (instance) if the class

### The self argument is a difficult thing for newcomers..

It takes time and experience to understand the self argument in class methods!

- self must always be the first argument
- self is never used in calls
- self is used to access attributes and methods inside methods

We refer to a more comprehensive text on classes for better explanation of self.

self is confusing in the beginning, but later it greatly helps the understanding of how classes work!

### A class for representing a mathematical function

Function with one independent variable t and two parameters  $v_0$  and a:

$$s(t; v_0, a) = v_0 t + \frac{1}{2} a t^2$$

Class representation of this function:

- v0 and a are variables (data)
- A method to evaluate s(t), but just function of t

### Usage:

```
s = Distance(v0=2, a=0.5) # create instance v = s(t=0.2) # compute formula
```

### The class code

```
class Distance:
    def __init__(self, v0, a):
        self.v0 = v0
        self.v0 = v0
        self.a = a

    def __call__(self, t):
        v0, a = self.v0, self.a  # make local variables
        return v0+t + 0.5*a*t**2

s = Distance(v0=2, a=0.5)  # create instance
    v = s(t=0.2)  # actually s.__call__(t=0.2)
```

### Class implementation of $f(x, y, z; p_1, p_2, ..., p_n)$

- The *n* parameters  $p_1, p_2, \ldots, p_n$  are attributes
- \_\_call\_\_(self, x, y, z) is used to compute f(x, y, z)

```
class F:
    def __init__(self, p1, p2, ...):
        self.p1 = p1
        self.p2 = p2
        ...

    def __call__(self, x, y, z):
        # return formula involving x, y, z and self.p1, self.p2 ...

f = F(p1=..., p2=..., ...)  # create instance with parameters
print f(i, 4, -1)  # evaluate f(x, y, z) function
```