## Intro to scientific Python programming

Hans Petter Langtangen<sup>1,2</sup>

Simula Research Laboratory<sup>1</sup>

University of Oslo<sup>2</sup>

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# This is a very quick intro to Python programming

- variables for numbers, lists, and arrays
- while loops and for loops
- functions
- if tests
- plotting

Method: show program code through math examples

Variables, loops, lists, and arrays

2 Functions and branching

Files

## Variables, loops, lists, and arrays



Do you have access to Python?

See TKT4140 Course specific installation guidelines
Other methods:

- Mac and Windows: Anaconda
- Web browser (Wakari or SageMathCloud)

## Mathematical example

Most examples will involve this formula:

$$s = v_0 t + \frac{1}{2} a t^2 \tag{1}$$

We may view s as a function of t: s(t), and also include the parameters in the notation:  $s(t; v_0, a)$ .

## A program for evaluating a formula

### Task

Compute s for t = 0.5,  $v_0 = 2$ , and a = 0.2.

### Code

```
t = 0.5
v0 = 2
a = 0.2
s = v0*t + 0.5*a*t**2
print s
```

#### Execution

```
Terminal> python distance.py 1.025
```

## Assignment statements assign a name to an object

Rule: evaluate right-hand side object, left-hand side is a name for that object

## Formatted output with text and numbers

- Task: write out s=1.025
- Method: printf syntax

Modern alternative: format string syntax

```
print s=\{s:.2f\}, format(s=s)
```

## Programming with a while loop

- Task: write out a table of t and s(t) values (two columns), for  $t \in [0,2]$  in steps of 0.1
- Method: while loop

```
v0 = 2
a = 0.2
dt = 0.1  # Increment
t = 0  # Start value
while t <= 2:
    s = v0*t + 0.5*a*t**2
    print t, s
    t = t + dt</pre>
```

## Output of the previous program

```
Terminal> python while.py
0.0
0.1 0.201
0.2 0.404
0.3 0.609
0.4 0.816
0.5 1.025
0.6 1.236
0.7 1.449
0.8 1.664
0.9 1.881
1.0 2.1
1.1 2.321
1.2 2.544
1.3 2.769
1.4 2.996
1.5 3.225
1.6 3.456
1.7 3.689
1.8 3.924
1.9 4.161
```

## Structure of a while loop

### Note:

- the colon in the first line
- all statements in the loop must be indented
- condition is a boolean expression (e.g., t <= 2)

## Let's take a closer look at the output of our program

```
Terminal> python while.py
0 0.0
0.1 0.201
0.2 0.404
...
1.8 3.924
1.9 4.161
```

The last line contains 1.9, but the while loop should run also when t=2 since the test is  $t \le 2$ . Why is this test False?

Let's examine the program in the Python Online Tutor

Python Online Tutor: step through the program and examine variables

```
a = 0
da = 0.4
while a <= 1.2:
    print a
    a = a + da</pre>
```

(Visualize execution)

## Ooops, why is a <= 1.2 when a is 2? Round-off errors!

```
a = 0
da = 0.4
while a <= 1.2:
    print a
    a = a + da
    # Inspect all decimals in da and a
    print '%.16E, %.16E' % (da, a), a <= 1.2</pre>
```

### (Visualize execution)

# Rule: never a == b for real a and b! Always use a tolerance!

```
a = 1.2
b = 0.4 + 0.4 + 0.4
boolean_condition1 = a == b  # may be False
# This is the way to do it
tol = 1E-14
boolean_condition2 = abs(a - b) < tol  # True</pre>
```

A list collects several variables (objects) in a given sequence:

```
L = [-1, 1, 8.0]
```

A list can contain any type of objects, e.g.,

```
L = ['mydata.txt', 3.14, 10]
```

Some basic list operations:

```
>>> L = ['mydata.txt', 3.14, 10]
>>> print L[0]
mydata.txt
>>> print L[1]
3.14
>>> del L[0]  # delete the first element
>>> print L
[3.14, 10]
>>> print len(L)  # length of L
2
>>> L.append(-1)  # add -1 at the end of the list
>>> print L
[3.14, 10, -1]
```

### Store our table in two lists, one for each column

```
v0 = 2
a = 0.2
dt = 0.1 # Increment
t = 0
t values = []
s_values = []
while t \le 2:
    s = v0*t + 0.5*a*t**2
   t_values.append(t)
    s_values.append(s)
    t = t + dt
print s_values # Just take a look at a created list
# Print a nicely formatted table
i = 0
while i <= len(t values)-1:
    print '%.2f %.4f' % (t_values[i], s_values[i])
    i += 1 # Same as i = i + 1
```

### For loops

A for loop is used for visiting elements in a list, one by one:

```
>>> L = [1, 4, 8, 9]
>>> for e in L:
... print e
...
1
4
8
9
```

Demo in the Python Online Tutor:

```
list1 = [0, 0.1, 0.2]
list2 = []
for element in list1:
    p = element + 2
    list2.append(p)
print list2
```

(Visualize execution)

# For loops used traditionally an integer counter over list/array indices

```
for i in range(len(somelist)):
    # Work with somelist[i]
```

#### Note:

- range returns a list of integers
- range(a, b, s) returns the integers a, a+s, a+2\*s, ... up to but not including (!!) b
- range(b) implies a=0 and s=1
- range(len(somelist)) returns [0, 1, 2]

## Let's replace our while loop by a for loop

```
v0 = 2
a = 0.2
dt = 0.1 # Increment
t_values = []
s_values = []
n = int(round(2/dt)) + 1  # No of t values
for i in range(n):
    t = i*dt
    s = v0*t + 0.5*a*t**2
    t_values.append(t)
    s_values.append(s)
print s_values # Just take a look at a created list
# Make nicely formatted table
for t, s in zip(t_values, s_values):
    print '%.2f %.4f' % (t, s)
# Alternative
for i in range(len(t_values)):
    print '%.2f %.4f' % (t_values[i], s_values[i])
```

## Traversal of multiple lists at the same time with zip

```
for e1, e2, e3, ... in zip(list1, list2, list3, ...):
Alternative: loop over a common index for the lists

for i in range(len(list1)):
    e1 = list1[i]
    e2 = list2[i]
    ...
```

### Arrays

- List: collect a set of numbers or other objects in a single variable
- Lists are very flexible (can grow, can contain "anything")
- Array: computationally efficient and convenient list
- Arrays must have fixed length and can only contain numbers of the same type (integers, real numbers, complex numbers)
- Arrays require the numpy module

## numpy functions creates entire arrays at once

Create n + 1 uniformly distributed coordinates in [a, b]:

```
t = numpy.linspace(a, b, n+1)
```

## Let's use arrays in our previous program

```
import numpy
v0 = 2
a = 0.2
dt = 0.1  # Increment
n = int(round(2/dt)) + 1  # No of t values

t_values = numpy.linspace(0, 2, n+1)
s_values = v0*t + 0.5*a*t**2

# Make nicely formatted table
for t, s in zip(t_values, s_values):
    print '%.2f %.4f' % (t, s)
```

# Standard mathematical functions are found in the math module

```
>>> import math
>>> print math.sin(math.pi)
1.2246467991473532e-16  # Note: only approximate value

Get rid of the math prefix:

from math import sin, pi
print sin(pi)

# Or import everything from math
from math import *
print sin(pi), log(e), tanh(0.5)
```

# Use the numpy module for standard mathematical functions applied to arrays

Matlab users can do

```
from numpy import *
x = linspace(0, 1, 101)
y = exp(-x)*sin(pi*x)
```

The Python community likes

```
import numpy as np
x = np.linspace(0, 1, 101)
y = np.exp(-x)*np.sin(np.pi*x)
```

Our convention: use np prefix, but not in formulas involving math functions

```
import numpy as np
x = np.linspace(0, 1, 101)
from numpy import sin, exp, pi
y = exp(-x)*sin(pi*x)
```

### Plotting

Plotting is done with matplotlib:

```
import numpy as np
import matplotlib.pyplot as plt

v0 = 0.2
a = 2
n = 21  # No of t values for plotting

t = np.linspace(0, 2, n+1)
s = v0*t + 0.5*a*t**2

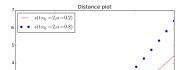
plt.plot(t, s)
plt.savefig('myplot.png')
plt.show()
```

The plotfile myplot.png looks like



## Plotting of multiple curves

```
import numpy as np
import matplotlib.pyplot as plt
v0 = 0.2
n = 21 # No of t values for plotting
t = np.linspace(0, 2, n+1)
a = 2
s0 = v0*t + 0.5*a*t**2
a = 3
s1 = v0*t + 0.5*a*t**2
plt.plot(t, s0, 'r-', # Plot s0 curve with red line
        t, s1, 'bo') # Plot s1 curve with blue circles
plt.xlabel('t')
plt.ylabel('s')
plt.title('Distance plot')
plt.legend(['$s(t; v_0=2, a=0.2)$', '$s(t; v_0=2, a=0.8)$'],
           loc='upper left')
plt.savefig('myplot.png')
plt.show()
```



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# Functions and branching



### **Functions**

- $s(t) = v_0 t + \frac{1}{2} a t^2$  is a mathematical function
- Can implement s(t) as a Python function s(t)

```
def s(t):
    return v0*t + 0.5*a*t**2

v0 = 0.2
a = 4
value = s(3)  # Call the function
```

#### Note:

- functions start with the keyword def
- statements belonging to the function must be indented
- function input is represented by arguments (separated by comma if more than one)
- function output is returned to the calling code
- v0 and a are global variables
- v0 and a must be initialized before s is called

## Functions can have multiple arguments

v0 and a as function arguments instead of global variables:

```
def s(t, v0, a):
    return v0*t + 0.5*a*t**2

value = s(3, 0.2, 4)  # Call the function

# More readable call
value = s(t=3, v0=0.2, a=4)
```

## Keyword arguments are arguments with default values

```
def s(t, v0=1, a=1):
    return v0*t + 0.5*a*t**2

value = s(3, 0.2, 4)  # specify new v0 and a
value = s(3)  # rely on v0=1 and a=1
value = s(3, a=2)  # rely on v0=1
value = s(3, v0=2)  # rely on a=1
value = s(t=3, v0=2, a=2)  # specify everything
value = s(a=2, t=3, v0=2)  # any sequence allowed
```

- Arguments without the argument name are called positional arguments
- Positional arguments must always be listed before the keyword arguments in the function and in any call
- The sequence of the keyword arguments can be arbitrary

## Vectorization speeds up the code

Scalar code (work with one number at a time):

```
def s(t, v0, a):
    return v0*t + 0.5*a*t**2

for i in range(len(t)):
    s_values[i] = s(t_values[i], v0, a)
```

Vectorized code: apply s to the entire array

```
s_values = s(t_values, v0, a)
```

How can this work?

- Array: t
- Expression: v0\*t + 0.5\*a\*t\*\*2
- r1 = v0\*t (scalar times array)
- r2 = t\*\*2 (square each element)
- r3 = 0.5\*a\*r2 (scalar times array)
- r1 + r3 (add each element)

Python functions written for scalars normally work for arrays too!

True if computations involve arithmetic operations and math functions:

```
from math import exp, sin

def f(x):
    return 2*x + x**2*exp(-x)*sin(x)

v = f(4)  # f(x) works with scalar x

# Redefine exp and sin with their vectorized versions
from numpy import exp, sin, linspace
x = linspace(0, 4, 100001)
v = f(x)  # f(x) works with array x
```

However, if tests are not allowed:

```
def f(x):
    return -1 if x < 0 else x**4*exp(-x)*sin(x)
x = linspace(0, 4, 100001)
v = f(x) # will not work</pre>
```

### Python functions can return multiple values

```
Return s(t) = v_0 t + \frac{1}{2} a t^2 and s'(t) = v_0 + a t:
 def movement(t, v0, a):
     s = v0*t + 0.5*a*t**2
     v = v0 + a*t
     return s. v
 s_value, v_value = movement(t=0.2, v0=2, a=4)
return s, v means that we return a tuple (\approx list):
 >>> def f(x):
 ... return x+1, x+2, x+3
 >>> r = f(3) # Store all three return values in one object r
 >>> print r
 (4, 5, 6)
 >>> type(r)
               # What type of object is r?
 <type 'tuple'>
 >>> print r[1]
```

Tuples are constant lists (cannot be changed)

### A more general mathematical formula

Equations from basic kinematics:

$$v = \frac{ds}{dt}, \quad s(0) = s_0$$
 $a = \frac{dv}{dt}, \quad v(0) = v_0$ 

Integrate to find v(t):

$$\int_0^t a(t)dt = \int_0^t \frac{dv}{dt}dt$$

which gives

$$v(t) = v_0 + \int_0^t a(t)dt$$

Integrate again over [0, t] to find s(t):

#### Basic if-else tests

#### An if test has the structure

#### Here,

• condition is a boolean expression with value True or False.

```
if t \le t1:

s = v0*t + 0.5*a0*t**2

else:

s = v0*t + 0.5*a0*t1**2 + a0*t1*(t-t1)
```

#### Multi-branch if tests

```
if condition1:
     <statements when condition1 is True>
 elif condition2:
     <statements when condition1 is False and condition2 is True>
 elif condition3:
     <statements when condition1 and condition 2 are False</pre>
      and condition3 is True>
 else:
     <statements when condition1/2/3 all are False>
Just if, no else:
 if condition:
     <statements when condition is True>
```

A Python function implementing the mathematical function

$$s(t) = \left\{ egin{array}{ll} s_0 + v_0 \, t + rac{1}{2} a_0 \, t^2, & t \leq t_1 \ s_0 + v_0 \, t_1 + rac{1}{2} a_0 \, t_1^2 + a_0 \, t_1 (t - t_1), & t > t_1 \end{array} 
ight.$$

reads

```
def s_func(t, v0, a0, t1):
    if t <= t1:
        s = v0*t + 0.5*a0*t**2
    else:
        s = v0*t + 0.5*a0*t1**2 + a0*t1*(t-t1)
    return s</pre>
```

## Python functions containing if will not accept array arguments

```
>>> def f(x): return x if x < 1 else 2*x
...
>>> import numpy as np
>>> x = np.linspace(0, 2, 5)
>>> f(x)
Traceback (most recent call last):
...
ValueError: The truth value of an array with more than one element is ambiguous. Use a.any() or a.all()
```

Problem: x < 1 evaluates to a boolean array, not just a boolean

## Remedy 1: Call the function with scalar arguments

```
n = 201 # No of t values for plotting
t.1 = 1.5
t = np.linspace(0, 2, n+1)
 s = np.zeros(n+1)
 for i in range(len(t)):
     s[i] = s_func(t=t[i], v0=0.2, a0=20, t1=t1)
Can now easily plot:
plt.plot(t, s, 'b-')
plt.plot([t1, t1], [0, s_func(t=t1, v0=0.2, a0=20, t1=t1)], 'r--')
plt.xlabel('t')
plt.vlabel('s')
plt.savefig('myplot.png')
plt.show()
```

## Remedy 2: Vectorize the if test with where

Functions with if tests require a complete rewrite to work with arrays.

```
s = np.where(condition, s1, s2)
```

#### Explanation:

- condition: array of boolean values
- s[i] = s1[i] if condition[i] is True
- s[i] = s2[i] if condition[i] is False

#### Our example then becomes

```
s = np.where(t \le t1, v0*t + 0.5*a0*t**2, v0*t + 0.5*a0*t1**2 + a0*t1*(t-t1))
```

Note that  $t \le t1$  with array t and scalar t1 results in a boolean array b where  $b[i] = t[i] \le t1$ .

## Remedy 3: Vectorize the if test with array indexing

- Let b be a boolean array (e.g., b = t <= t1)
- s[b] selects all elements s[i] where b[i] is True
- Can assign some array expression expr of length len(s[b]) to s[b]: s[b] = (expr)[b]

Our example can utilize this technique with b as t <= t1 and t > t1:

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Files



## File reading

Put input data in a text file:

```
v0 = 2
a = 0.2
dt = 0.1
interval = [0, 2]
```

How can we read this file into variables v0, a, dt, and interval?

#### Code for reading files with lines variable = value

```
infile = open('.input.dat', 'r')
for line in infile:
    # Typical line: variable = value
    variable, value = line.split('=')
    variable = variable.strip() # remove leading/traling blanks
    if variable == 'v0':
        v0 = float(value)
    elif variable == 'a':
        a = float(value)
    elif variable == 'dt':
        dt = float(value)
    elif variable == 'interval':
        interval = eval(value)

infile.close()
```

## Splitting lines into words is a frequent operation

```
>>> line = 'v0 = 5.3'
>>> variable, value = line.split('=')
>>> variable
'v0 '
>>> value
'5.3'
>>> variable.strip() # strip away blanks
'v0'
```

Note: must convert value to float before we can compute with the value!

## Modern Python often applies the with statement for file handling

```
with open('.input.dat', 'r') as infile:
    for line in infile:
    ...
```

No need to close the file when using with

## File writing

- We have t and s(t) values in two lists, t\_values and s\_values
- Task: write these lists as a nicely formatted table in a file

#### Code:

```
outfile = open('table1.dat', 'w')
outfile.write('# t s(t)\n') # write header
for t, s in zip(t_values, s_values):
    outfile.write('%.2f %.4f\n' % (t, s))
```

## Simplified writing of tabular data to file via numpy.savetxt

# Simplified reading of tabular data from file via numpy.savetxt

```
data = np.loadtxt('table2.dat', comments='#')
```

#### Note:

- Lines beginning with the comment character # are skipped in the reading
- data is a two-dimensional array: data[i,0] holds the t value and data[i,1] the s(t) value in the i-th row