## Saint-Venant equations: fluid dynamics

Tsunami Travel Times

Tide Gage
DART
Earthquake

120° 150° 180° 210° 240° 270° 200°





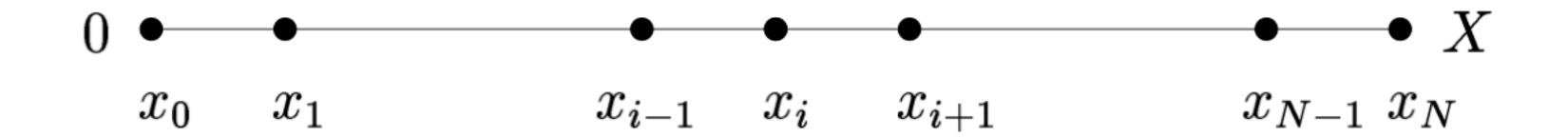


<u>youtube</u>

## Finite difference methods

Principle: derivatives in the partial differential equation are approximated by linear combinations of function values at the grid points

1D: 
$$\Omega = (0, X), \quad u_i \approx u(x_i), \quad i = 0, 1, ..., N$$
  
grid points  $x_i = i\Delta x$  mesh size  $\Delta x = \frac{X}{N}$ 



First-order derivatives

$$\frac{\partial u}{\partial x}(\bar{x}) = \lim_{\Delta x \to 0} \frac{u(\bar{x} + \Delta x) - u(\bar{x})}{\Delta x} = \lim_{\Delta x \to 0} \frac{u(\bar{x}) - u(\bar{x} - \Delta x)}{\Delta x}$$
$$= \lim_{\Delta x \to 0} \frac{u(\bar{x} + \Delta x) - u(\bar{x} - \Delta x)}{2\Delta x} \quad \text{(by definition)}$$