

# The SIR Model

## A Brief Demonstration of $\text{\LaTeX}$ Through An Introduction to Disease Modelling

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# Introduction

- The purpose of this presentation is to demonstrate briefly the use of  $\text{\LaTeX}$
- We go through the basics of the SIR Model as an example
  - this is very relevant to the field of public health
  - includes mathematics: this is where  $\text{\LaTeX}$  can demonstrate its full glory
  - Only a basic introduction
- We will also include comparisons with Microsoft Office
- This is not a full tutorial on using  $\text{\LaTeX}$

# What is L<sup>A</sup>T<sub>E</sub>X?



- Pronounced as ‘lay-tech’
- A free software for document preparation
- Released almost 40 years ago in 1984
- Built on top of T<sub>E</sub>X (initial release in 1978)
- Used for typesetting documents, particularly with technical content
- Widely used in academia and other communities for the production of highly professional documents

# What is the SIR Model?

- S: susceptible; I: infectious; R: recovered (sometimes called removed)
- Proposed by Kermack and McKendrick in 1927 (Kermack & McKendrick, [1927](#))
- A compartmental model
- Population assigned to different ‘compartments’: SIR
- Model infectious diseases mathematically

# A Quick Detour

Before we go any further, we have already demonstrated a few capabilities of L<sup>A</sup>T<sub>E</sub>X!

Let's have a look in detail...

# The Beamer Class

This presentation is typeset using the Beamer class in L<sup>A</sup>T<sub>E</sub>X. Hopefully it is evident by now, it is a powerful class to make good-looking presentations. You can specify in the beginning of the document by

```
1 \documentclass{beamer}
```

There are many more classes within L<sup>A</sup>T<sub>E</sub>X that you can use for various purposes. The default class is the Article class for making general documents. There are also classes for books and letters, for example.

# Title Page

With L<sup>A</sup>T<sub>E</sub>X, minimum effort is required to format the title page as you do not have to worry much about formatting. As a simple example:

```
1 \documentclass{beamer}
2 \title{An Elegant Presentation}
3 \author{John Smith}
4 \institute{University of Glasgow}
5 \date{\today}
```

You can then use the command `\titlepage` in the next frame to make it your title page, without having to worry much about formatting unless you have more specific requirements.

# NRS Data

We make use of postcode district and sector data from the National Records of Scotland ([NRS](#)).

- Shape files
- Contain geometries of districts and sectors
- Read in as `DataFrames` into PYTHON with `Pandas`
- Convert to `GeoDataFrames` with `GeoPandas`



# NRS Data

	OBJECTID	District	Shape_Leng	Shape_Area	geometry
0	1	AB10	17466.667741	4.591592e+06	POLYGON ((394256.974 806666.497, 394264.000 80...
1	2	AB11	26086.506732	5.396370e+06	MULTIPOLYGON (((393211.114 805537.072, 393207....
2	3	AB12	73839.045489	7.299857e+07	MULTIPOLYGON (((396494.604 802552.201, 396491....
3	4	AB13	15847.217768	8.770372e+06	POLYGON ((386014.000 803318.000, 385991.953 80...
4	5	AB14	27250.316419	1.754676e+07	POLYGON ((383220.204 804258.703, 383230.799 80...

**Figure 1:** A segment of **DataFrame** containing district information. Similarly for sector data, with a column representing postcode sectors.

# GP Data

- For this example we make use of a few GPs from Lanarkshire (with some modifications):
  - Nalagatla Medical Practice
  - The Craigallian Avenue Practice
  - The Stonelaw Practice
  - Ardoch Medical Practice

# Hypothetical GP

- For the purpose of testing, we also create two hypothetical practices, namely Hypothetical One and Hypothetical Two respectively
  - They cover areas defined by a combination of districts and sectors

# Data Wrangling

Steps are taken to make sure that the data are presented consistently:

- Separate the comma separated areas of the GPs into individual rows
- Distinguish and separate districts and sectors into different columns

# Data Wrangling

Practice Code	Practice Name	Areas
⋮ 66667	⋮ Hypothetical Two	⋮ G68,G74 4

Table 1: An example of how the dataset would look like **before** data wrangling.

# Data Wrangling

Practice Code	Practice Name	District	Sector
60073	Nalagatla Medical Practice	NaN	G33 6
⋮	⋮	⋮	⋮
60092	The Stonelaw Practice	G76	NaN
66667	Hypothetical Two	NaN	G74 4
66667	Hypothetical Two	G68	NaN

**Table 2:** An example of how the dataset would look like **after** data wrangling.

# Joining the Data

Now that we have our GP (hyposplit) and NRS data (sectors and districts), we merge them together. First merge sector data:

```
1 # Firstly merge with sector data to get their
2 # geometries and remove irrelevant rows
3 merged = pd.merge(hyposplit, sectors, on="Sector", how="
   outer")
4 merged = merged.head(39)
```

# Joining the Data

Then we merge our district data:

```
1 # Now merge with district data for their geometries
2 # Again we keep only rows with our GP data
3 merged = pd.merge(merged,districts,on="District",how="
    outer")
4 merged = merged.head(39)
```



# Convert to GeoDataFrame

For a DataFrame DF, we can easily convert it to a GeoDataFrame GDF with

```
1 import geopandas as gpd
2 GDF = gpd.GeoDataFrame(DF, crs="EPSG:4326")
```

where EPSG:4326 refers to the current coordinate system (latitude and longitude) based on the Earth's centre of mass.

# Undissolved Boundaries

- First plot the initial results in Matplotlib as a sanity check
- Some boundaries may not be visible due to overlapping
- Notice the boundaries are ‘undissolved’ - we can still see different levels (sectors and districts) of geographies

Glasgow NW GP Boundaries Undissolved

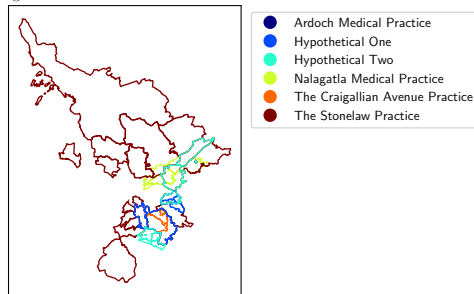


Figure 2: Undissolved Glasgow NW GP boundaries.

# Merging Geographies

- We are interested in the overall boundaries of the GPs
- Need to merge the individual postcode districts and sectors of a GP
- We can dissolve the boundaries and merge the geographies

For undissolved `GeoDataFrame` `uGDF`, we can simply dissolve the geographies by grouping and merging the `Practice Code` column:

```
1 dissolved = uGDF.dissolve(by="Practice Code")
```

# Dissolved Boundaries

We plot the final results again as a sanity check:

Glasgow NW GP Boundaries Dissolved

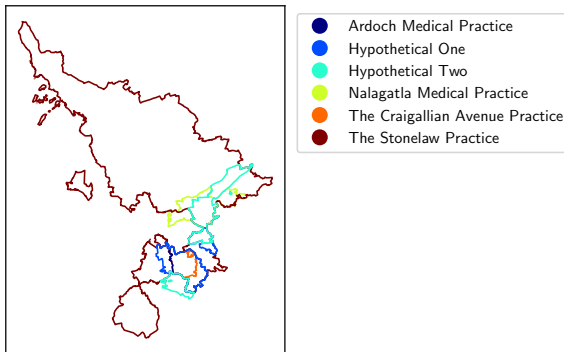


Figure 3: Dissolved Glasgow NW GP boundaries.

# Summary

- **Pandas** and **GeoPandas** in **PYTHON** provide simple methods to deal with shape files
- Can apply to other scenarios where we have to deal with a hierarchy of geography
- It takes only a few lines of codes in **PYTHON** for this task so it is relatively simple
- This is however only possible when we are provided with numerical description (e.g. in postcode sectors/districts) of the GP boundaries
  - if we are given a description by words, we will probably have to define the boundaries manually on **ArcGIS**
- Naturally, this task can also be done in **ArcGIS**

# References

Kermack, W. O., & McKendrick, A. G. 1927, [Proceedings of the Royal Society of London Series A](#), 115, 700