

統計學與實習上
第四次作業

1. 資料集 iris 為 R 語言內建之資料集，其中包含了 150 株鳶尾花的外表性狀調查資料，請使用此資料完成以下題目。(by R) (1 points)

a. 請分別計算出花瓣 (petal) 長度的樣本平均數與標準差。在假定花瓣長度為常態分佈時，以此樣本平均和標準差計算隨機採樣一株鳶尾花，其花瓣長度介於 2 至 5 公分的機率（機率值請四捨五入至小數點第二位）。(0.2 points)

b. 使用此組資料計算出實際長度介於 2 至 5 公分的樣本數佔總樣本數的比例（機率值請四捨五入至小數點第二位）。(0.3 points)

c. 請比較 b, c 小題的結果，基於你的觀察說明兩者結果間之一致/不一致性來源為何，可適度使用統計圖表、統計值做輔助說明。(0.5 points)

2. (Text, p.264) A population consists of the following five values: 2, 2, 4, 4, and 8. (by hand)

a. List all samples of size 2, and compute the mean of each sample. (0.2points)

b. Compute the mean of the distribution of sample means and the population mean. Compare the two values. (0.2points)

c. Compare the dispersion in the population with that of the sample means. (0.3points)

3. Beer bottles are filled so that they contain an average of 330ml of beer in each bottle. Suppose that the amount of beer in a bottle is normally distributed with a standard deviation of 4ml. (by hand)

a. What is the probability that a randomly selected bottle will have less than 325ml of beer? (0.4points)

b. What is the probability that a randomly selected 6-pack of bottle will have less than 325ml of beer? (0.4points)

c. What is the probability that a randomly selected 12-pack of bottle will have less than 325ml of beer? (0.4points)

d. Comment on the sample size and the corresponding probabilities. (0.5points)

4. A small hair salon averages about 30 customers on weekdays with a standard deviation of 6. It is safe to assume that the underlying distribution is normal. In an attempt to increase the number of weekday customers, the manager offers a \$2 discount on 5 consecutive weekdays. She reports that her strategy has worked since the sample mean of customers during the 5 weekday period jumps to 35. (by hand)

a. How unusual would it be to get a sample average of 35 or more customers if the manager has not offered the discount? (0.5points)

b. Do you feel confident that the manager's discount strategy has worked? Explain. (0.5points)

5. 假設某次 TOEIC 考試台灣考生成績呈常態分配，平均 $\mu = 580$ ，標準差 $\sigma = 140$ 。(by hand)

- a.若某校研究所甄試入學將 TOEIC 成績高於 600 者列為審核加分的標準，假設有 49 位學生報名甄試該研究所，且所有參加甄試學生皆有 TOEIC 成績，且其成績也呈現常態分配，請問有多少甄試學生能夠獲得加分？(0.3points)
- b.承上題，若假設要以 TOEIC 成績先節選前 33%的學生作為二階段口試的門檻，則應該如何指定該標準？(0.3points)