

PageRank (Additional Materials)

Social Networks Analysis and Graph Algorithms

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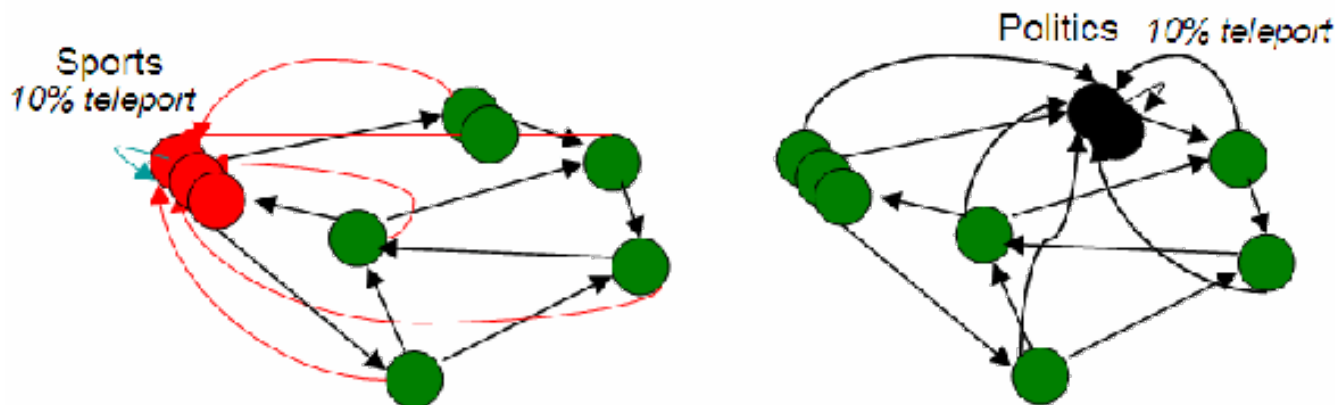
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Sources

- D. Easley and J. Kleinberg (2010): Networks, Crowds, and Markets – Chapter 14
- Fei Li's lecture on PageRank (2011)
- Evimaria Terzi's lecture on link analysis (2013)
- URLs in the footer of specific slides

Variant: **personalized** PageRank

- Modify $R(i)$ according to users' tastes
(e.g. user interested in sports vs politics)



PageRank and internal linking

- A website has a maximum amount of Page Rank that is distributed between its pages by internal links [depends on internal links]
- The maximum amount of Page Rank in a site increases as the number of pages in the site increases.
- By linking poorly, it is possible to fail to reach the site's maximum Page Rank, but it is not possible to exceed it.

PageRank Implementation

- Suppose there are n pages and m links
- Trivial implementation of PageRank requires $O(M+N)$ memory

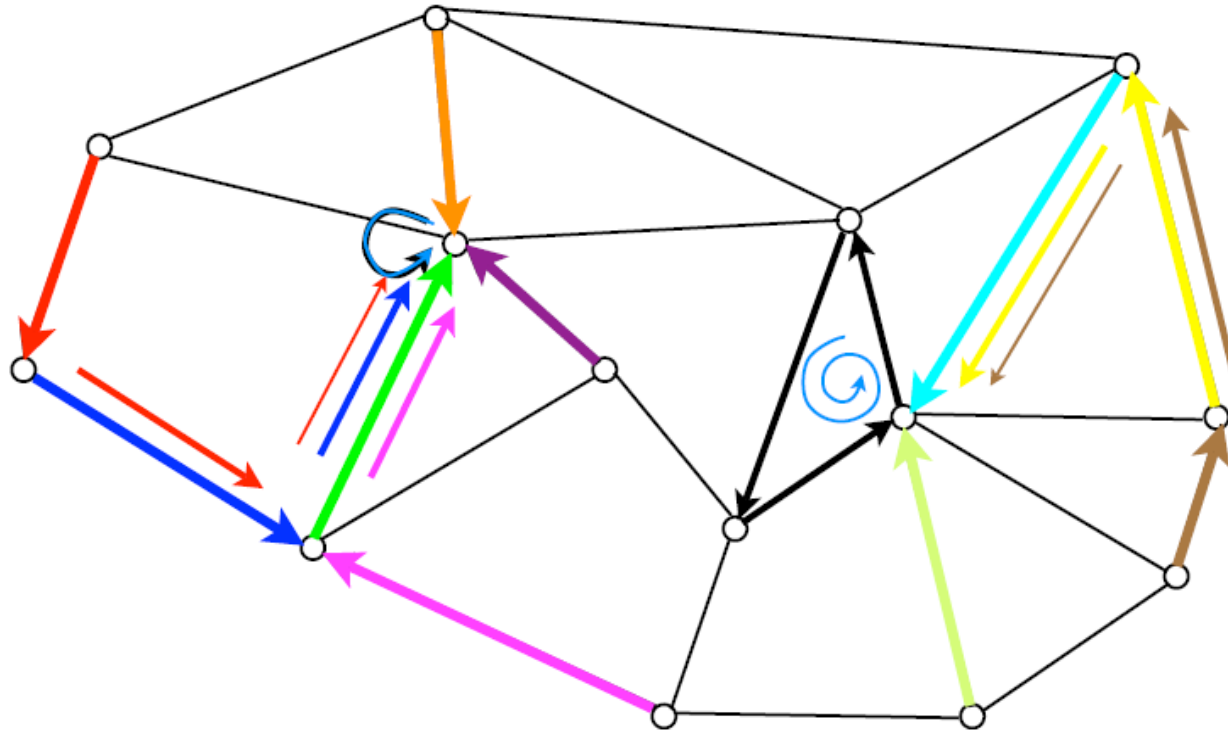
Streaming implementation requires $O(N)$ memory ... *how?*
"Streaming" means the graph is never held on memory

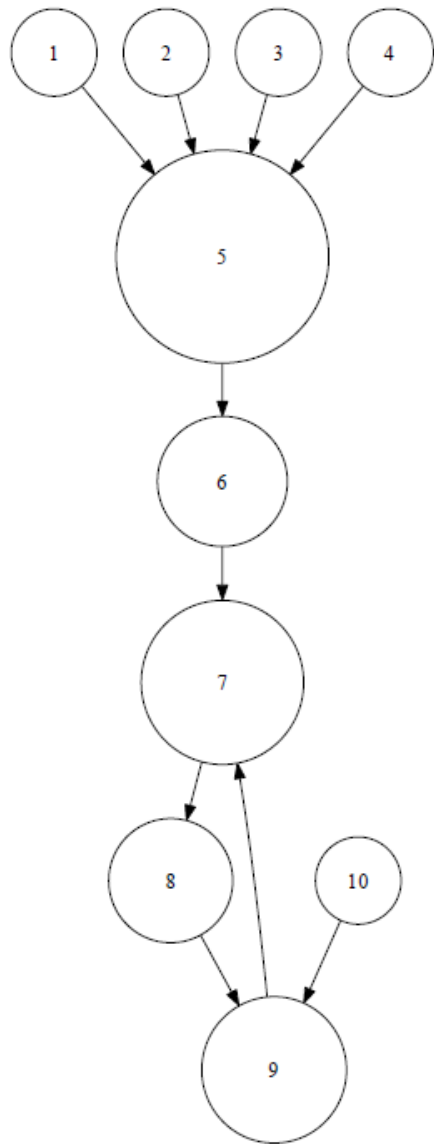
Liquid democracy

PageRank as a form of actual voting (liquid democracy)

- If $\alpha = 1$, we can implement liquid democracy
 - In liquid democracy, people chose to either vote or to delegate their vote to somebody else
- If $\alpha < 1$, we have a sort of “viscous” democracy where delegation is not total

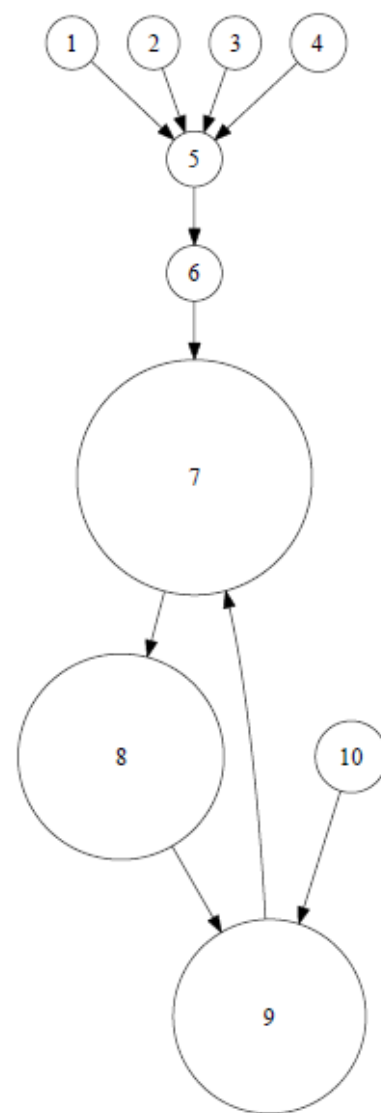
PageRank as a form of liquid democracy





These two graphs
have different alpha
(0.2 and 0.9)

Which one is
which?



Summary

Things to remember

- Personalized PageRank
- Liquid democracy example, will help you understand the role of the parameter α