

# Case study on centrality

## Social Networks Analysis and Graph Algorithms

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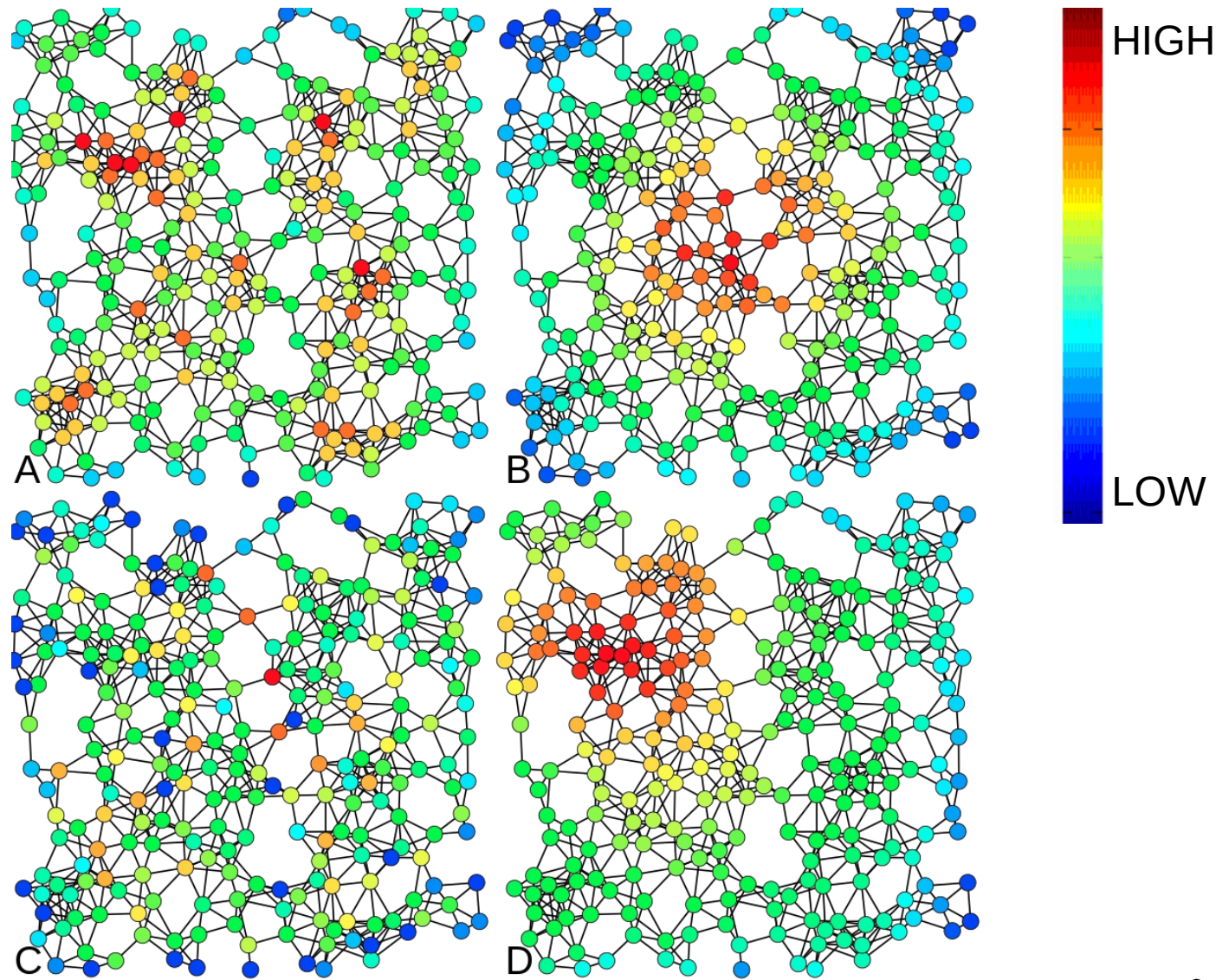
Universitat  
Pompeu Fabra  
*Barcelona*

A: Degree

B: Closeness

C: Betweenness

D. PageRank



# Wealth and political power



- The dataset contains 116 families
- **Gross wealth in Florins** (1 florin ~ 3.5g of gold)
  - Leonardo da Vinci was paid ~100 florin per year (~1 painting), until he worked with the king of France, who paid ~400 florin per year
  - Michelangelo Buonarroti got paid ~200-450 florins per sculpture
  - A palace would cost thousands of florins
- **Priorates** is the cumulative number of seats in the city council along many years

# Florentine families

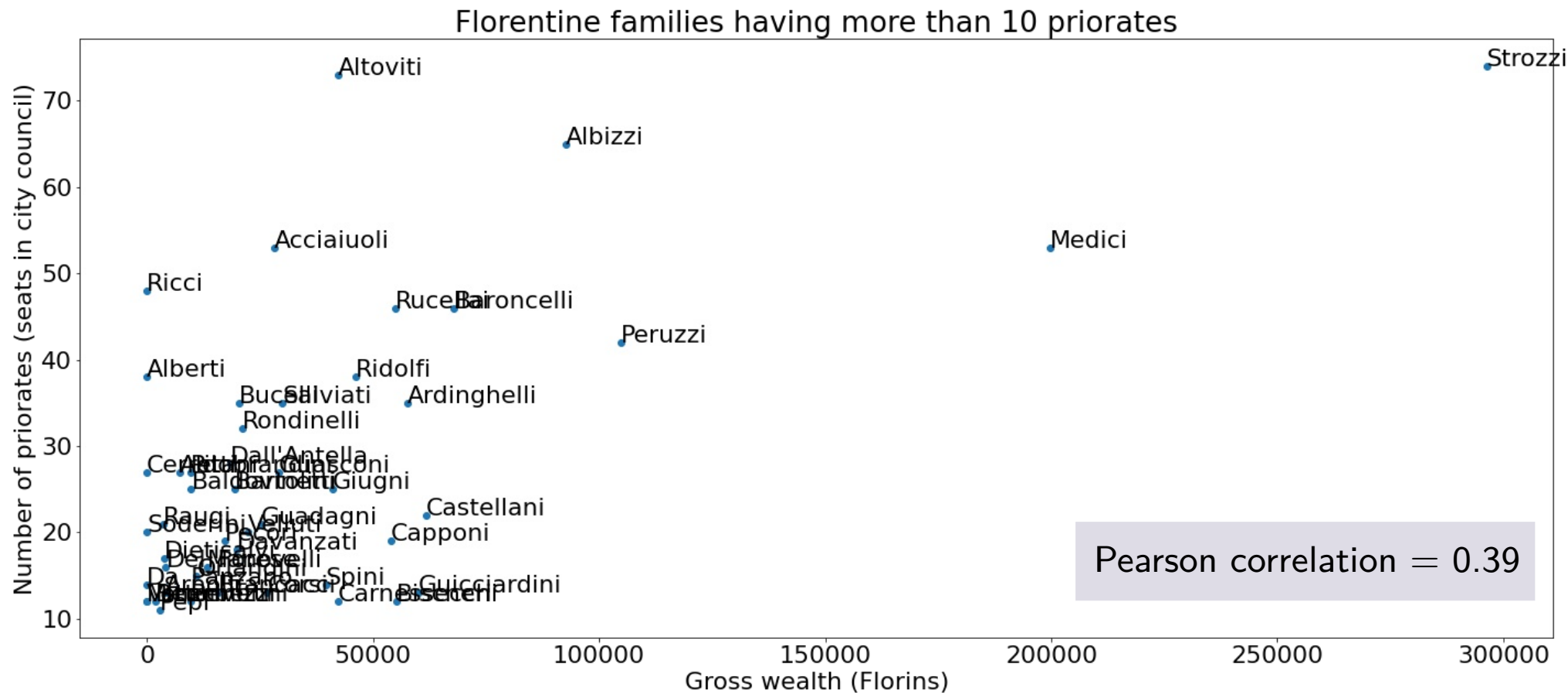
- **Noble families in Florence** around 1430
- **Power struggle** between two factions led by the Medici and the Strozzi
- The relatively newcomer Medici became, for a while, the wealthiest family in Europe ... they had their own bank!
- Dataset collected by John Padgett from historical documents



# Wealth and political power (cont.)

```
plt.scatter(  
    families[families.Npriors > MIN_PRIORS].Gwealth,  
    families[families.Npriors > MIN_PRIORS].Npriors)  
  
families.Gwealth.corr(  
    families.Npriors, method='pearson'))
```

# Wealth and political power (cont.)



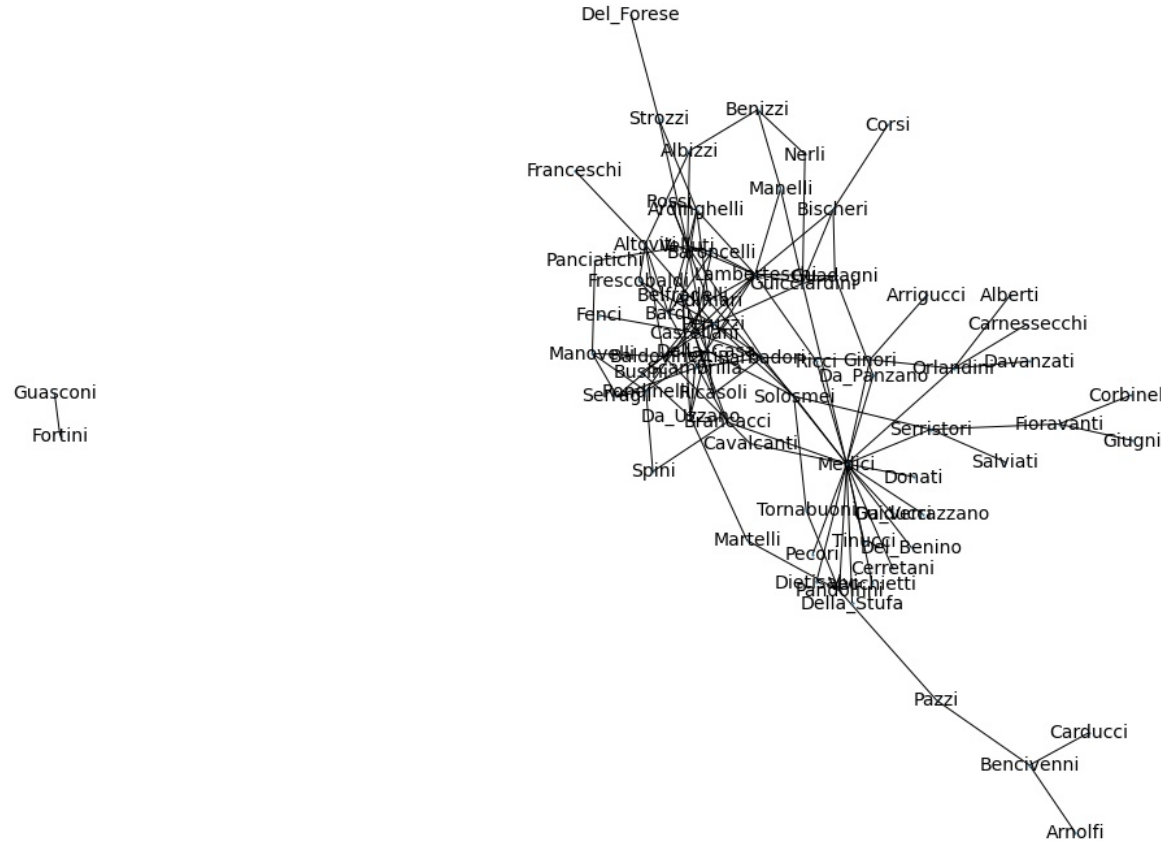


# Credit graph



# Credit graph

- 72 nodes
- 125 edges
- Credit given by one family to a member of the other
- Reciprocal in this dataset  
⇒ Undirected

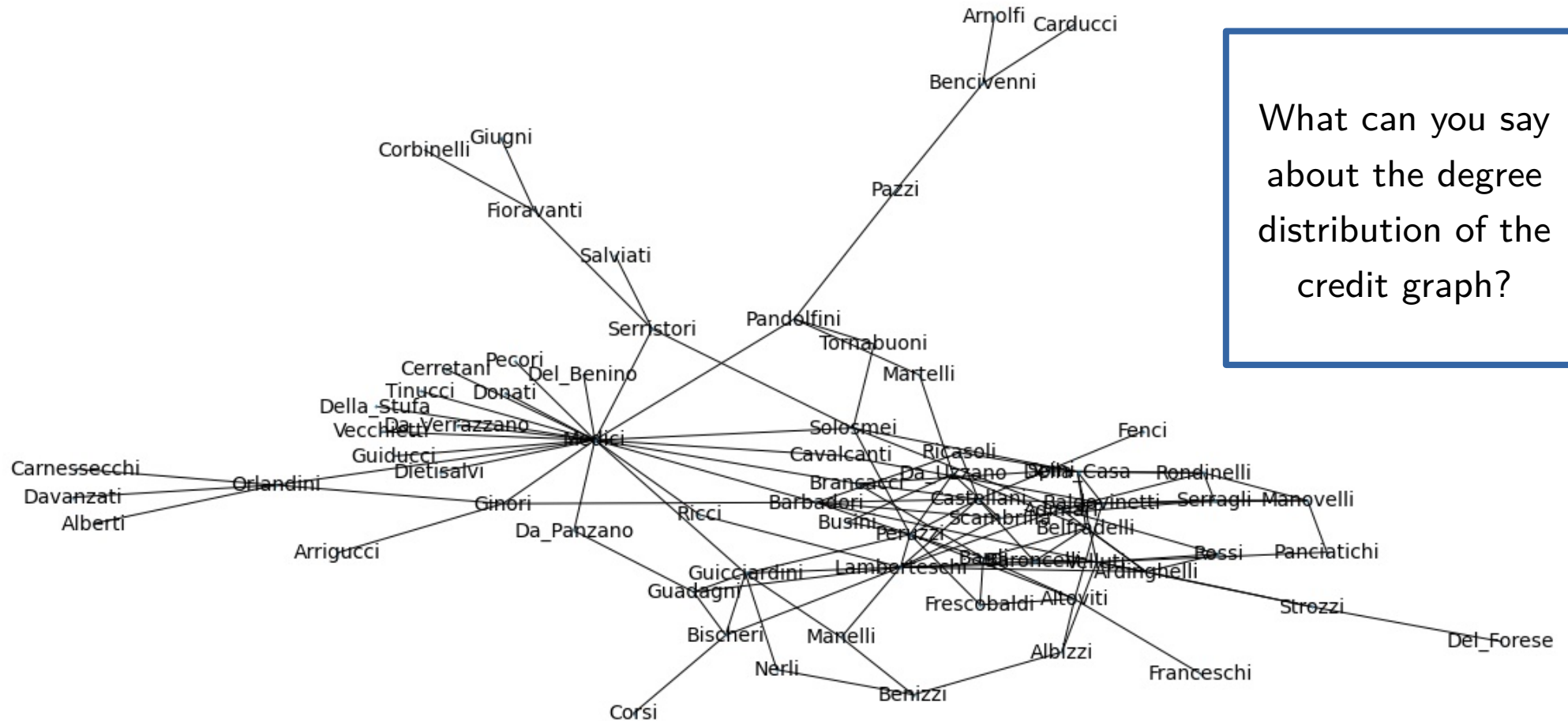




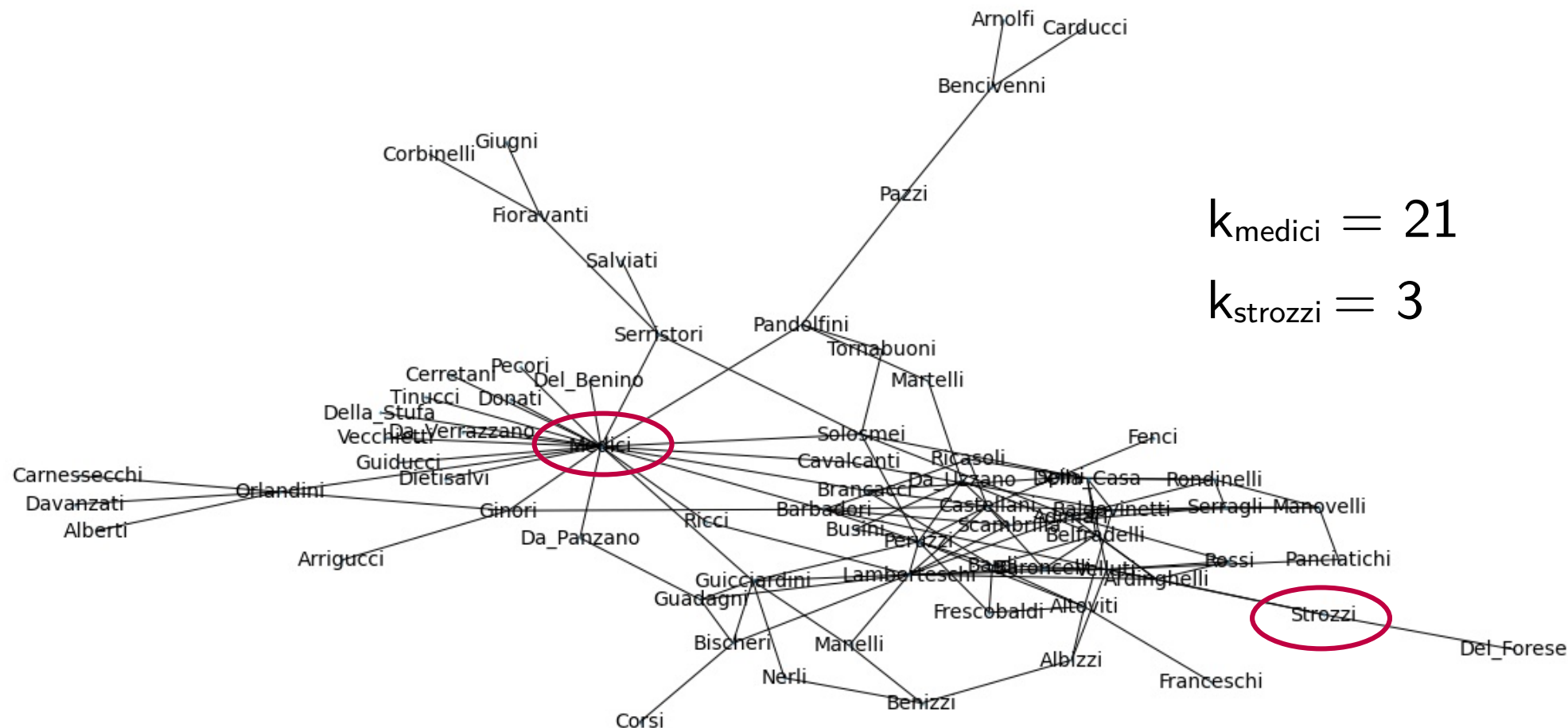
# Credit graph in NetworkX

```
credits_list = pd.read_csv(INPUT_CREDIT,  
    usecols=['FamilyA', 'FamilyB'])  
  
credits = nx.from_pandas_edgelist(credits_list,  
    "FamilyA", "FamilyB")  
  
...  
  
credits_components = sorted(  
    nx.connected_components(credits), key=len, reverse=True)  
  
credits_gcc = credits.subgraph(credits_components[0])
```

# Credit - giant connected component (70 nodes, 97%)



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# Closeness computation

```
c_closeness = pd.DataFrame.from_dict(  
    nx.closeness centrality(credits_gcc),  
    orient='index', columns=['c_closeness'])  
families = families.join(c_closeness, how='inner')
```

# Closeness, betweenness, eigencentrality

## Closeness

- Peruzzi 0.39
- Medici 0.48
- Strozzi 0.28

## Betweenness

- Peruzzi 0.11
- Medici 0.53
- Strozzi 0.03

## Eigencentrality

- Peruzzi 0.30
- Medici 0.31
- Strozzi 0.07

What can you say about the correlations of this with wealth/power?



# Computing and visualizing correlations

```
corr = families.corr()  
  
corr  
    .style.background_gradient(cmap='Reds')  
    .format(precision=2)
```

# Correlations

	Gwealth	Npriors	c_degree	c_closeness	c_betweenness	c_eigencentrality
Gwealth	1.00	0.39	0.42	0.21	0.40	0.34
Npriors	0.39	1.00	0.27	0.04	0.20	0.19
c_degree	0.42	0.27	1.00	0.67	0.84	0.88
c_closeness	0.21	0.04	0.67	1.00	0.59	0.79
c_betweenness	0.40	0.20	0.84	0.59	1.00	0.59
c_eigencentrality	0.34	0.19	0.88	0.79	0.59	1.00

Do you see the block structure in this matrix? What does it mean?

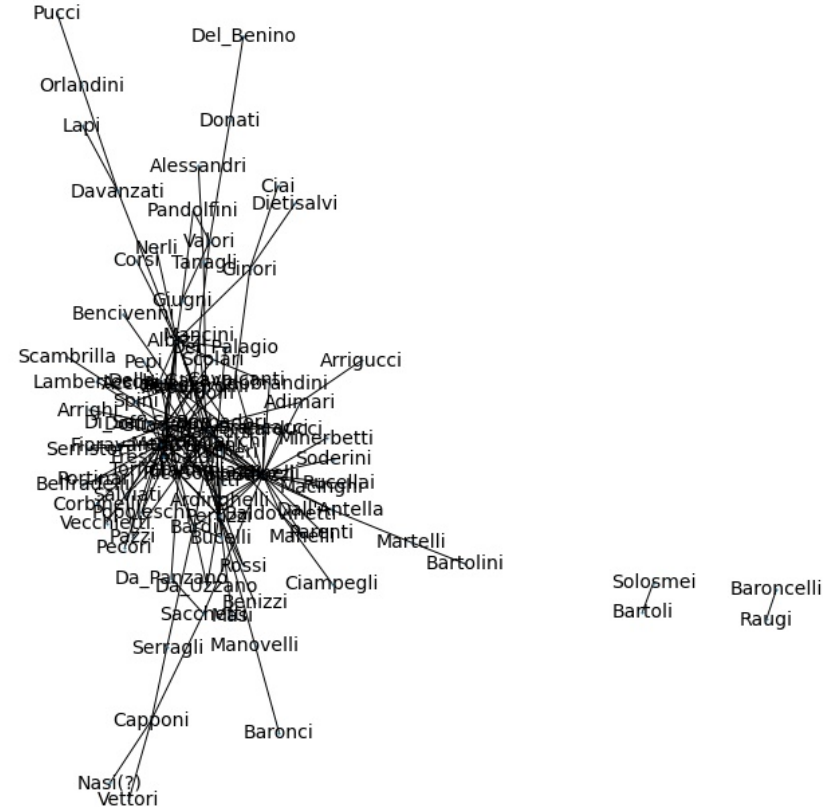
# Marriages graph



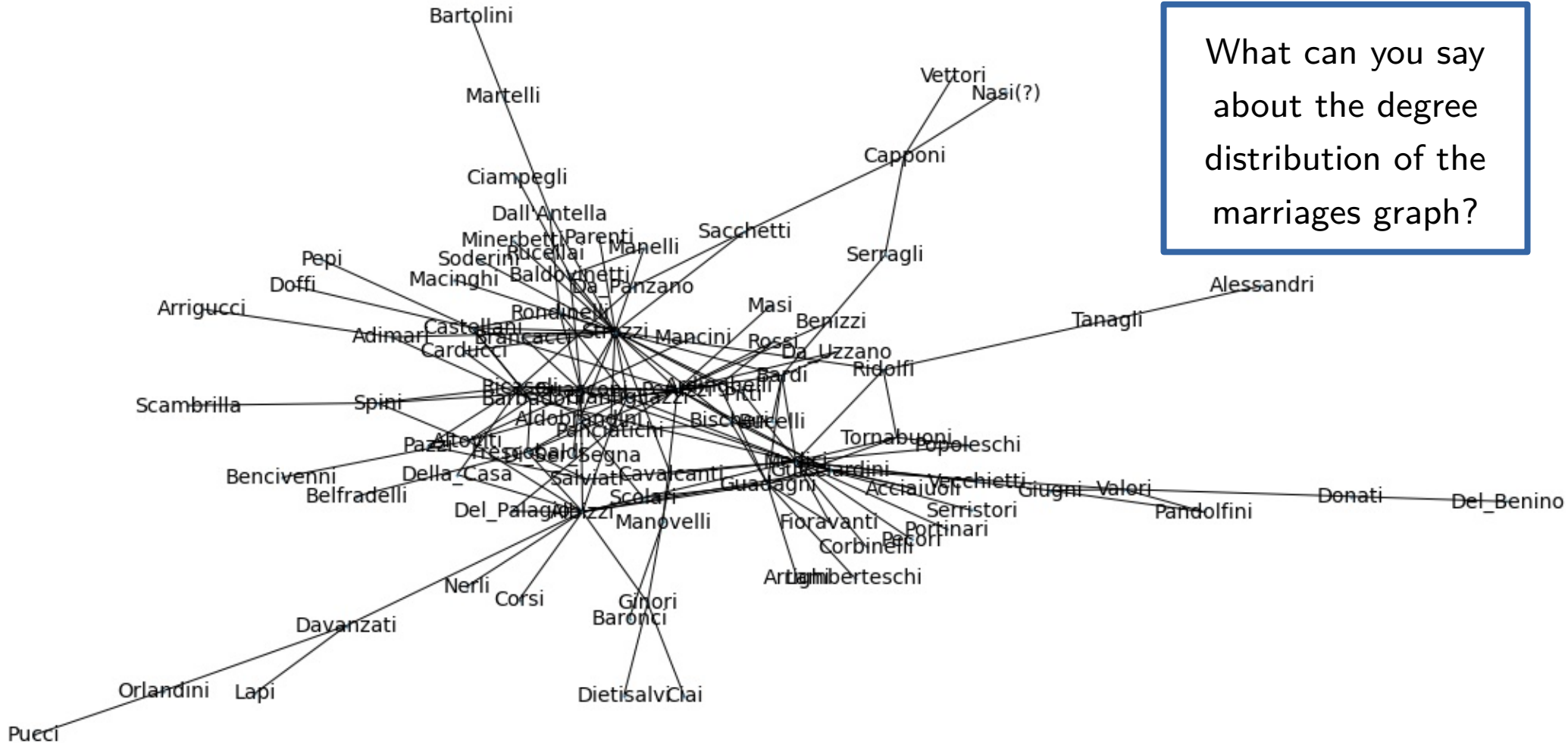
# Marriages graph

- 96 nodes
- 157 edges
- Marriages between families

Federighi  
Dello\_Scarfa



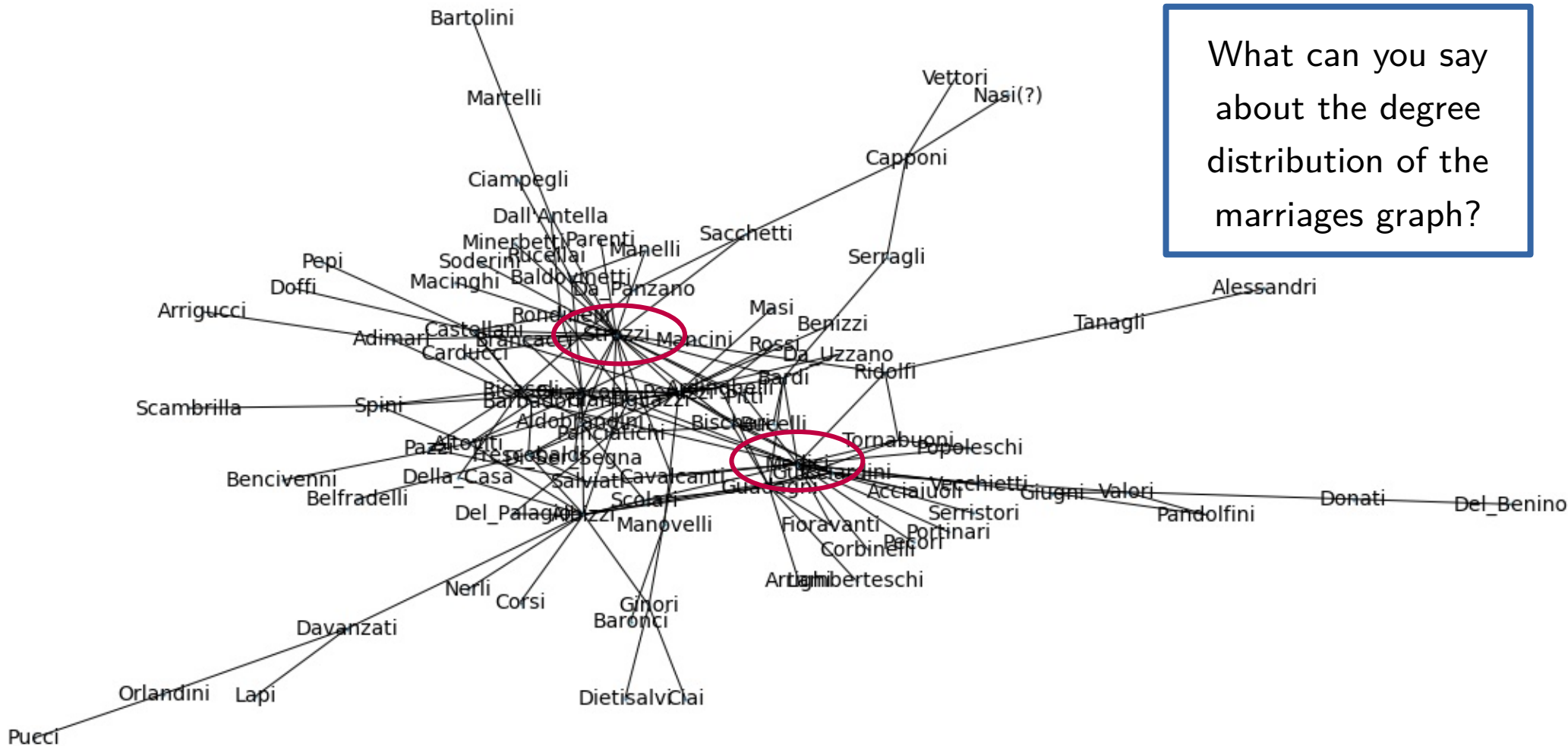
# Marriages - giant connected component (90 nodes, 94%)





## Marriages - giant connected component (90 nodes, 94%)

What can you say about the degree distribution of the marriages graph?



# Closeness, betweenness, eigencentrality

## Closeness

- Peruzzi 0.42
- Medici 0.44
- Strozzi 0.46

## Betweenness

- Peruzzi 0.15
- Medici 0.26
- Strozzi 0.35

## Eigencentrality

- Peruzzi 0.32
- Medici 0.27
- Strozzi 0.40

What can you say about the correlations of this with wealth/power?

# Correlations

	Gwealth	Npriors	m_degree	m_closeness	m_betweenness	m_eigencentrality	c_degree	c_closeness	c_betweenness	c_eigencentrality
Gwealth	1.00	0.44	0.79	0.67	0.77	0.76	0.39	0.22	0.40	0.33
Npriors	0.44	1.00	0.69	0.53	0.71	0.63	0.31	0.03	0.24	0.19
m_degree	0.79	0.69	1.00	0.77	0.95	0.93	0.48	0.30	0.45	0.42
m_closeness	0.67	0.53	0.77	1.00	0.66	0.90	0.42	0.27	0.29	0.44
m_betweenness	0.77	0.71	0.95	0.66	1.00	0.81	0.43	0.25	0.45	0.33
m_eigencentrality	0.76	0.63	0.93	0.90	0.81	1.00	0.45	0.29	0.32	0.46
c_degree	0.39	0.31	0.48	0.42	0.43	0.45	1.00	0.70	0.84	0.87
c_closeness	0.22	0.03	0.30	0.27	0.25	0.29	0.70	1.00	0.61	0.81
c_betweenness	0.40	0.24	0.45	0.29	0.45	0.32	0.84	0.61	1.00	0.57
c_eigencentrality	0.33	0.19	0.42	0.44	0.33	0.46	0.87	0.81	0.57	1.00

Do you see the block structure in this matrix? What does it mean?  
What is a good predictor of wealth/power?

# Summary

# Things to remember

- The analysis of social networks requires defining suitable graphs
- There is usually a step in which one compares this with domain-specific metrics