

Evolutionary Algorithms (EA)

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Chapter 6

Grey Wolf Optimization (GWO)

6.1 Story

GWO [2] meta-heuristic approach was designed based on the group hierarchy and the hunting strategy of grey wolves in nature. Grey wolves normally live in a pack of 5-12 members with strong social hierarchy. The most dominant one, the leader is the alpha (in nature a pair of male and female). The alfa's responsibility to make decisions about hunting, sleeping, etc. The second most dominant is beta, who can be considered as an experienced, skilled member of the pack helping the alpha making decisions. The beta is subordinate to the alfa, but plays a discipliner role for the rest of the wolves. The omega is the lowest ranked wolf, he has to submit to anyone in the pack. Wolves who are not alfa, beta or omega are just called subordinates. They play the role of scouts, hunters, sentinels, caretakers. The social behaviour appears in hunting as well in a characteristic fashion. The GWO algorithm mimics the three stage hunting mechanism of grey wolves: searching for prey, encircling prey and attacking. Four types of pack members can be found in the model. There are three dominant wolves, alpha, beta and delta. They have the best fitness value. The rest of the wolves are subordinates or omega who are guided by the three dominant wolves.

Let $X = \{x_1, x_2, \dots, x_N\}$ population of wolfs, where N is the population size and $x_i \in \mathbb{R}^D$. $f : \mathbb{R}^D \rightarrow \mathbb{R}^1$ is the fitness function and $fitness_i = f(x_i)$ is the fitness value of x_i .

Three parameters are needed to be updated: a , A and C .

a is decreasing from 2 to 0 by iteration linearly:

$$a_{t+1} = 2 * (1 - \frac{t}{T}) \quad (6.1)$$

$$A = 2 * a * rand_1 - a \quad (6.2)$$

So A is a random value in the interval $[-2a, 2a]$.

$$C = 2 * rand_2 \quad (6.3)$$

Hence C is a random value in the interval $[0, 2]$.

Where $rand_i \in U(0, 1)$, where U stands for uniform distribution.

Movement of wolfs determined by the leading wolfs and through coefficient vectors in the following way: $D_\alpha = |C_1 * x_\alpha(t) - x_i(t)|$, $D_\beta = |C_2 * x_\beta(t) - x_i(t)|$, $D_\delta = |C_3 * x_\delta(t) - x_i(t)|$
 $X_1 = x_\alpha(t) - A_1 * D_\alpha$, $X_2 = x_\beta(t) - A_2 * D_\beta$, $X_3 = x_\delta(t) - A_3 * D_\delta$

$$x_i(t+1) = \frac{X_1 + X_2 + X_3}{3} \quad (6.4)$$

where $x_i(t)$ is the location of the i th wolf at iteration t , and x_α is the location of alpha. $x_\alpha : fitness_\alpha = \min_{i=1, \dots, N} f(x_i)$ (min because of minimization problem). x_β has the second best fitness value, x_δ has the third one.

Searching for prey (exploration) as other phases of hunting guided by the 3 dominant wolf. $|A| > 1$ cases oblige the agent to diverge from the prey and search for better prey (solution). Encircling the prey is also controlled by coefficient vectors A and C and the location of alpha, beta, delta. Attacking of the prey (exploitation) phase is active when $|A| < 1$. In this situation the force towards the prey is getting strong.

6.2 Pseudo code

Algorithm 1: Grey Wolf Optimizer

```
begin
  Set  $N$ : population size,  $T$ : number of iterations
  Initialize random population of wolfs  $X = \{x_1, x_2, \dots, x_N\}$ ,
  Calculate fitness values  $fitness_i$  for  $i \in \{1, 2, \dots, N\}$ 
  while  $t \leq T$  or Stopping criteria not met do
    Decrease the value of  $a$  by Equation 6.1
    Determine the three dominant wolfs  $x_{alfa}, x_{beta}, x_{delta}$ 
    for  $i \leftarrow 1$  to  $N$  do
      Update  $A$  and  $C$  parameters by Equation 6.2 and 6.3
      Update location of wolf  $x_i$  by Equation 6.4
      Check search space
      Calculate  $fitness_i = f(x_i)$ 
      if  $fitness_i < fitness_{best}$  then
         $x_{best} = x_i$ 
         $fitness_{best} = fitness_i$ 
      end
    end
    Check Stopping Criteria
     $t = t + 1$ 
  end
end
```

Chapter 7

Whale Optimization Algorithm (WOA)

7.1 Story

WOA [1] was inspired by the bubble-net attack of humpback whales. Adult humpback whales have almost the size of a school bus and their main target preys are krills and small fish herds. Whales are very intelligent mammals. They can live and hunt alone and in groups as well. Humpback whales' special hunting method is called bubble-net feeding. This can be observed when small fish herds are close to the surface. The whale dive down first around 12 meters under the herd and then start moving upward in a spiral shape by creating bubbles along the path to herd the krill herd together before the attack. This manouever was modelled as an optimization algorithm. The formalization is somewhat similar to Grey Wolf Optimizer's. But in this case the agents are driven in the exploitation phase by only one whale with the best fitness. And the exploration and exploitation

Let $X = \{x_1, x_2, \dots, x_N\}$ population of whales, where N is the population size and $x_i \in \mathbb{R}^D$. $f : \mathbb{R}^D \rightarrow \mathbb{R}^1$ is the fitness function and $fitness_i = f(x_i)$ is the fitness value of x_i .

b is a constant parameter. Generally $b = 1$. It affects the spiral encircling move.

4 parameters are needed to be updated: a , A , C and l .

a is decreasing from 2 to 0 by iteration linearly:

$$a_{t+1} = 2 * (1 - \frac{t}{T}) \quad (7.1)$$

$$A = 2 * a * rand_1 - a \quad (7.2)$$

So A is a random value in the interval $[-2a, 2a]$.

$$C = 2 * rand_2 \quad (7.3)$$

Hence C is a random value in the interval $[0, 2]$.

$$l = rand_3 \quad (7.4)$$

Where $rand_1$ and $rand_2 \in U(0, 1)$, $rand_2 \in U(-1, 1)$, and U stands for uniform distribution.

The exploration and exploitation phases are also controlled by a random mechanism. If $rand < p$ or $rand \geq p$ ($rand \in U(0, 1)$) the algorithm switches between strategies. p is a fixed parameter, generally $p = 0.5$.

The movement of whales in the population determined by the following way:

If $rand < p$ and $|A| < 1$:

$$D = |C * x_{best}(t) - x_i(t)|$$

$$x_i(t+1) = x_{best}(t) - A * D \quad (7.5)$$

If $rand < p$ and $|A| > 1$:

$$D = |C * x_{rand}(t) - x_i(t)|$$

$$x_i(t+1) = x_{rand}(t) - A * D \quad (7.6)$$

Where x_{rand} is a random member of the whale population.

If $rand \geq p$: $D = |x_{best}(t) - x_i(t)|$

$$x_i(t+1) = D * \exp(bl) * \cos(2\pi l) + x_{best}(t) \quad (7.7)$$

where $x_i(t)$ is the location of the i th wolf at iteration t , and x_{best} is the location of the whale with best fitness. $x_{best} : fitness_{best} = \min_{i=1, \dots, N} f(x_i)$ (min because of minimization problem).

Searching for prey (exploration) as other phases of hunting guided by the 3 dominant wolf. $|A| > 1$ cases oblige the agent to diverge from the prey and search for better prey (solution). Encircling the prey is also controlled by coefficient vectors A and C and the location of alpha, beta, delta. Attacking of the prey (exploitation) phase is active when $|A| < 1$. In this situation the force towards the prey is getting strong.

7.2 Pseudo code

Algorithm 2: Whale Optimization Algorithm

```

begin
  Set  $N$ : population size,  $T$ : number of iterations
  Set  $p$ : strategy switch probability,  $b$ : constant of the spiral
  Initialize random population of whales  $X = \{x_1, x_2, \dots, x_N\}$ ,
  Calculate fitness values  $fitness_i$  for  $i \in \{1, 2, \dots, N\}$ 
  while  $t \leq T$  or Stopping criteria not met do
    Decrease the value of  $a$  by Equation 7.1
    Determine the best whale  $x_{best}$ 
    for  $i \leftarrow 1$  to  $N$  do
      Update  $A$ ,  $C$  and  $l$  parameters by Equation 7.2, 7.3 and 7.4
      if  $rand < p$  then
        if  $|A| < 1$  then
          | Update location of whale  $x_i$  by Equation 7.5
        end
        else
          | Update location of whale  $x_i$  by Equation 7.6
        end
      end
    end
    else
      | Update location of whale  $x_i$  by Equation 7.7
    end
    if  $fitness_i < fitness_{best}$  then
      |  $x_{best} = x_i$ 
      |  $fitness_{best} = fitness_i$ 
    end
  end
  Check Stopping Criteria
   $t = t + 1$ 
end
end

```

Chapter 8

Flower Pollination Algorithm (FPA)

8.1 Story

8.2 Pseudo code

8.3 Flowchart

Chapter 9

Firefly Algorithm (FA)

9.1 Story

9.2 Pseudo code

9.3 Flowchart

Chapter 10

Black Hole Algorithm (BHA)

10.1 Story

BHA [3, 4] heuristic approach was introduced in 2012. The analogy is to create a random population of stars in the search space, the one with the best fitness value is considered as the black hole. The black hole gives a direction for every star's movement in all iterations. The stars are moving towards the black hole in a random way. After movement if the fitness value of a star is better than the fitness value of the black hole, then this star becomes the black hole. Furthermore another mechanism is involved to make a balance between exploration and exploitation, according to that if a star crosses the event horizon (defined distance from the black hole) then the black hole swallows it. Technically the star loose it's actual position and being redistributed randomly in the search space. Hence a new star is born to keep the population constant.

Let $X = \{x_1, x_2, \dots, x_N\}$ population of stars, where N is the population size and $x_i \in \mathbb{R}^D$. $f : \mathbb{R}^D \rightarrow \mathbb{R}^1$ is the fitness function and $fitness_i = f(x_i)$ is the fitness value of x_i .

Movement of stars towards the black hole:

$$x_i(t+1) = x_i(t) + rand * (x_{BH} - x_i(t)) \quad (10.1)$$

where $x_i(t)$ is the location of the i th star at iteration t , and x_{BH} is the black hole. $x_{BH} : fitness_{BH} = \min_{i=1, \dots, N} f(x_i)$ (min because of minimization problem).

$rand \in U(0,1)$, where U stands for uniform distribution.

Radius of the event horizon is calculated as follows:

$$EventHorizon = \frac{fitness_{BH}}{\sum_{i=1}^N fitness_i} \quad (10.2)$$

10.2 Pseudo code

Algorithm 3: Black Hole Algorithm

```
begin
  Set  $N$ : population size,  $T$ : number of iterations
  Initialize random population of stars  $X = \{x_1, x_2, \dots, x_N\}$ ,
  Calculate fitness values  $fitness_i$  for  $i \in \{1, 2, \dots, N\}$ 
  Determine the black hole  $x_{BH}$ ,
  Calculate EventHorizon by Equation 10.2
  while  $t \leq T$  or Stopping criteria not met do
    for  $i \leftarrow 1$  to  $N$  do
      Update location of star  $x_i$  by Equation 10.1
      Check search space
      Calculate  $fitness_i = f(x_i)$ 
      if  $fitness_i < fitness_{BH}$  then
         $x_{BH} = x_i$ 
         $fitness_{BH} = fitness_i$ 
        Calculate EventHorizon by Equation 10.2
      end
    else
      if  $\|x_{BH} - x_i\| < EventHorizon$  then
        Reinitialize  $x_i$  randomly within the search space
      end
    end
  end
  Check Stopping Criteria
   $t = t + 1$ 
end
```

Bibliography

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