

# **A Theory of Refinement of Cyber-Physical-Systems into Implementations**

Bachelor's Thesis of

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I declare that I have developed and written the enclosed thesis completely by myself, and have not used sources or means without declaration in the text.

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.....  
(Daniel H. Draper)



# Abstract

English abstract.



# **Zusammenfassung**

Deutsche Zusammenfassung





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# 1. Introduction

The following Bachelorthesis will try to formalize the following process: Replacing the abstract notion of the control program in a verified (by KēYmaera) Cyber-Physical-System (*CPS*) with an actual implementation through a form of Formal Refinement and being able to verify that the entire CPS still satisfies the required safety constraints, using both KēYmaera and KēY.

CPS are generally modelled as either Hybrid Automata or - Programs.(See ref. [platzerb]). Mostly, this means, that an abstract version of the discrete control program is modelled, often as a non-deterministic assignment of a control value (See app. A.1). To replace this non-deterministic assignment with an actual implementation a certain "glue" or "coupling" has to be found to translate discrete and real continuous values into each other. To explain this process we will take a look at the following:

- I:** CPS Watertank (Example taken from KēYmaera) refined.
- II:** Introduction of Formalized used in both examples.
- III:** CPS Gear-Backlash (See ref. [bla ]) refined.





## **2. Refinement of a concrete Example: CPS Controlled Watertank**

2.0.1. Finding the concrete Control Value Assignment

2.0.2. Refining the original Hybrid Automata

2.0.3. Finding the correct Program Safety Condition

2.0.4. The (simple) Java Control Program

2.0.5. Finding the glue between Java and the Hybrid Model of the system

2.0.6. Verification based on KeYmaera



## **3. Evaluation**

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### **3.1. First Section**

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### **3.2. Second Section**

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### **3.3. Third Section**

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## **4. Conclusion**

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## **A. Appendix**

### **A.1. Images**

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Placeholder

Figure A.1.: Watertank Hybrid Program and - Automata with Non-Deterministic Control  
Program Abstraction marked.