

Prof. Dr. Peer Küppers

Summer School 2021

Bias-Variance-Tradeoff



Use Case

■ Simulated Webshop

<https://pk-bigdata.appspot.com>

■ Business Context

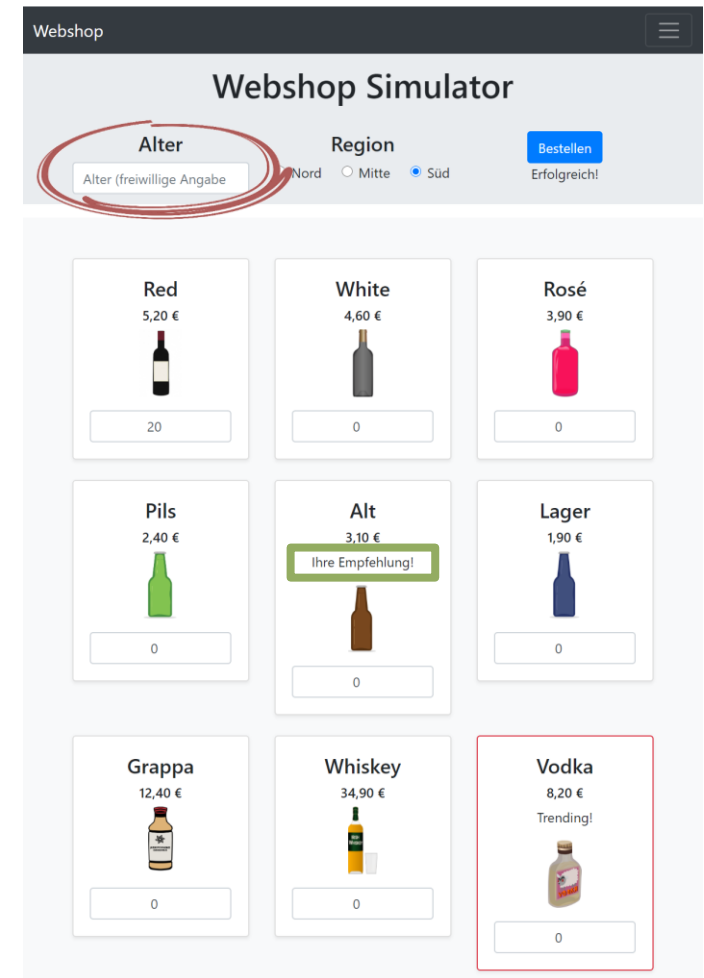
- “Personalized recommendations increase turnover.”

→ Machine learning-based personalized recommendation

■ Problem

- Personalization requires knowledge about the age group of a customer

→ Not all users provide their age.



Use Case

■ Task

- Age (group) missing? → **predict it!**

■ Approach

based on ...

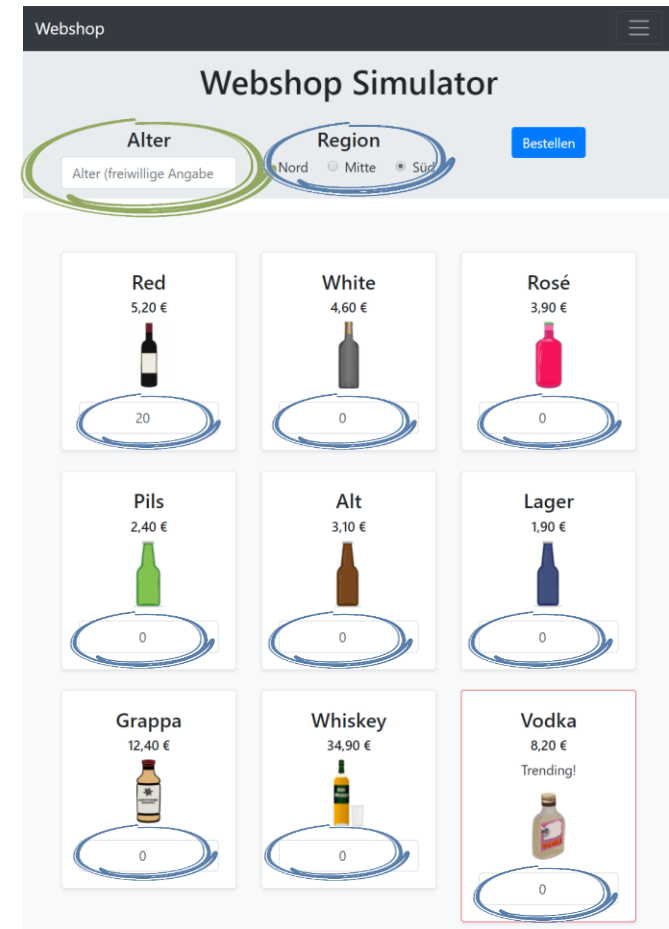
- Region
- Order date
- Contents in the shopping cart

Features

predict ...

- Age group

Target

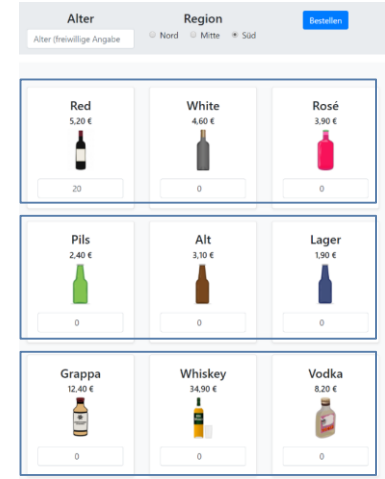


Use Case: Data Understanding

Product group 1: wine

Product group 2: beer

Product group 3: spirits



weekday	region	sum_sales_pg1	sum_sales_pg2	sum_sales_pg3	age_group
Sunday	Middle	99.0	0.0	0.0	18-29
Wednesday	North	8.1	91.9	0.0	18-29
Friday	South	68.8	19.3	0.0	18-29
Thursday	South	65.5	13.9	15.7	30-49
Friday	Middle	51.6	3.8	34.6	50-

Features

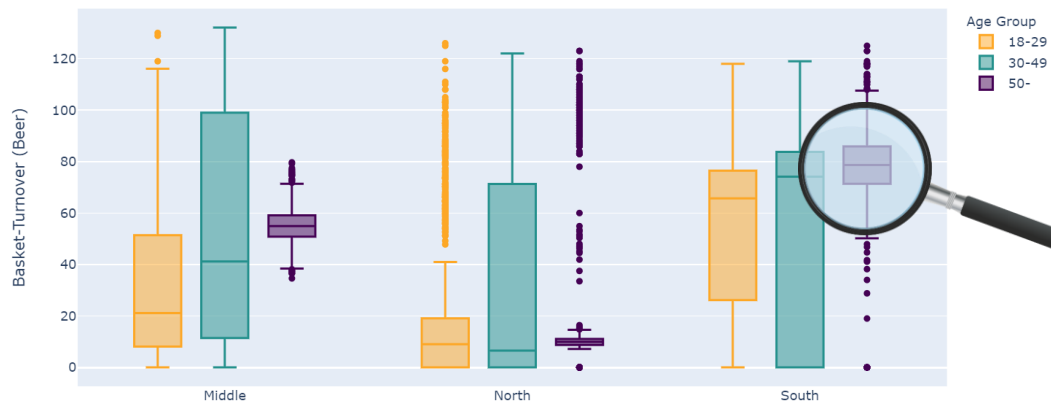
Target

] One shopping cart



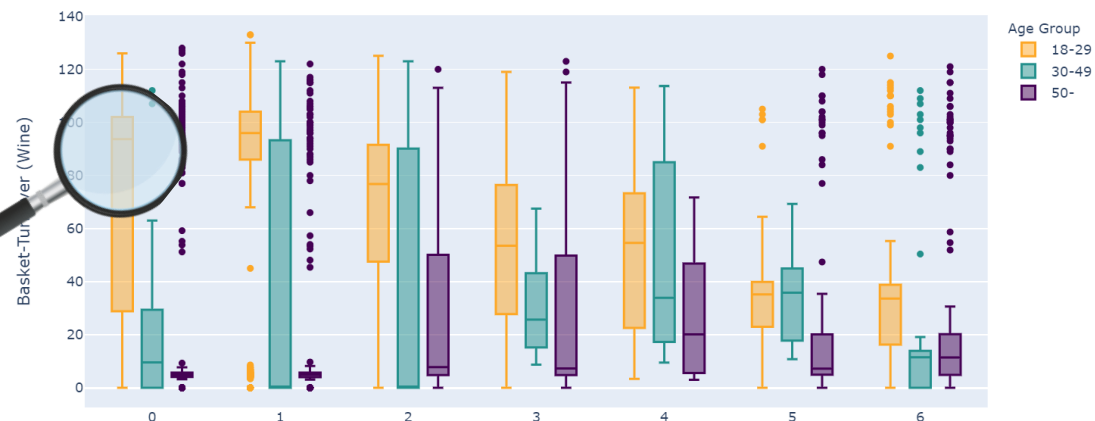
■ Patterns in the data, e.g.

Basket-Turnover (Beer) per Region and Age-Group(=Target)



Older customers tend to buy more beer in the south compared to the other regions.

Basket-Turnover (Wine) per Weekday and Age-Group(=Target)



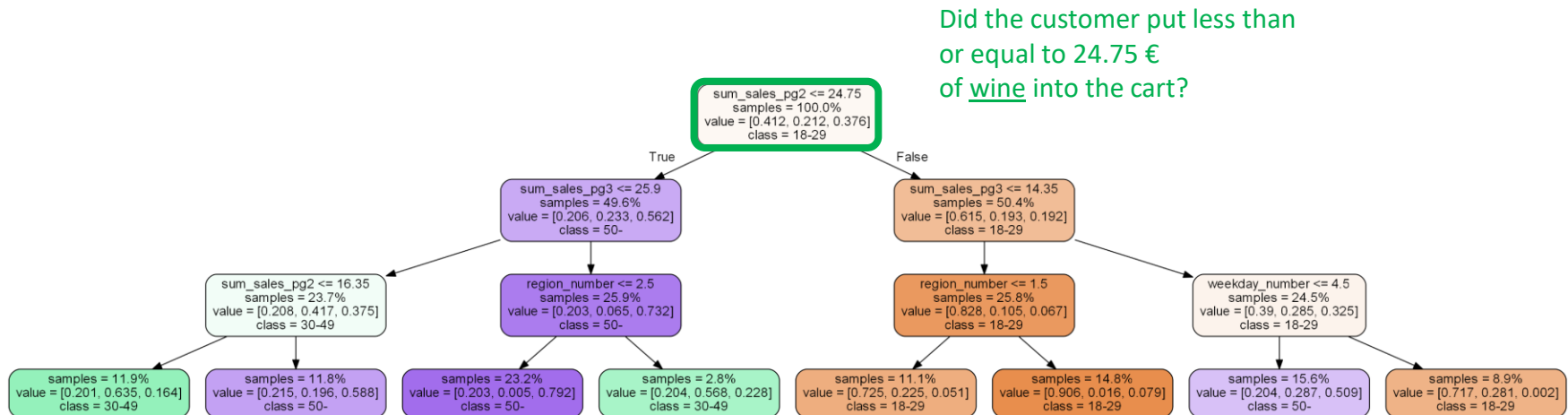
Younger customers seem to fill up their wine stocks at the beginning of the week.

Use Case: Current Solution

■ Patterns identified by machine learning

■ Current solution: Decision Tree

- Example: Customer from the “South” (region 3) buys 50€ wine and 8€ spirits.
- What is the predicted age group?

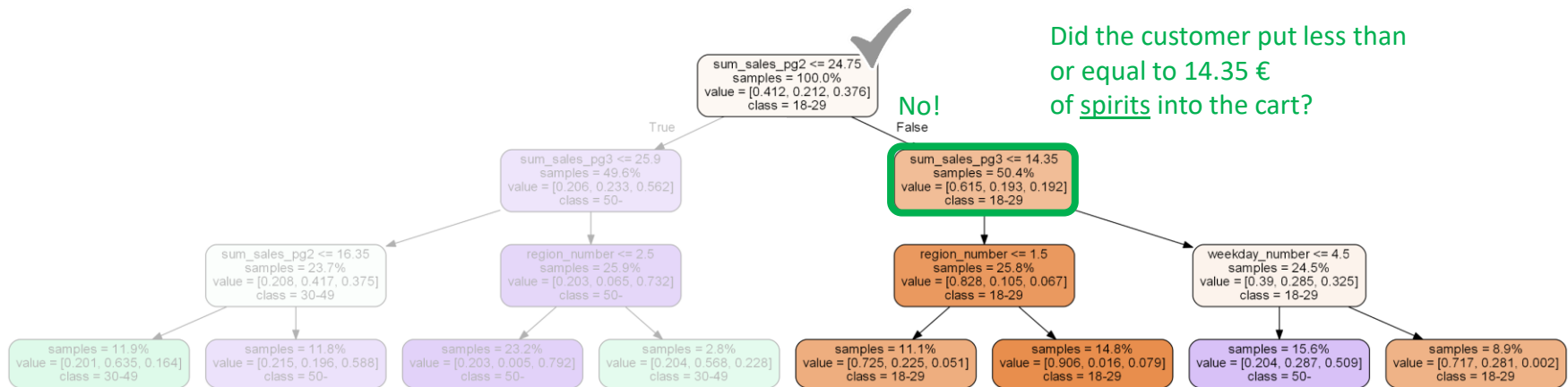


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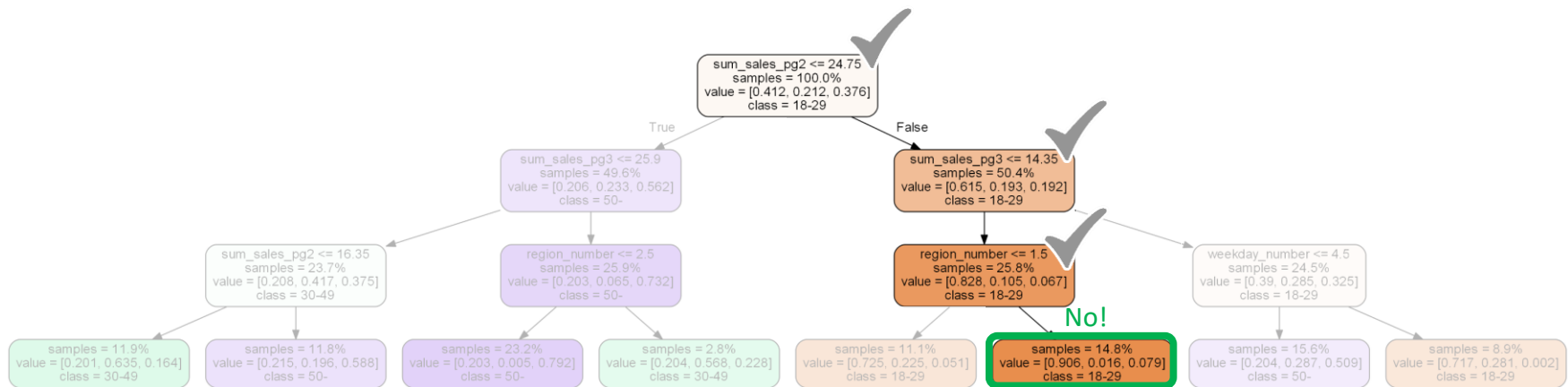


Use Case: Current Solution

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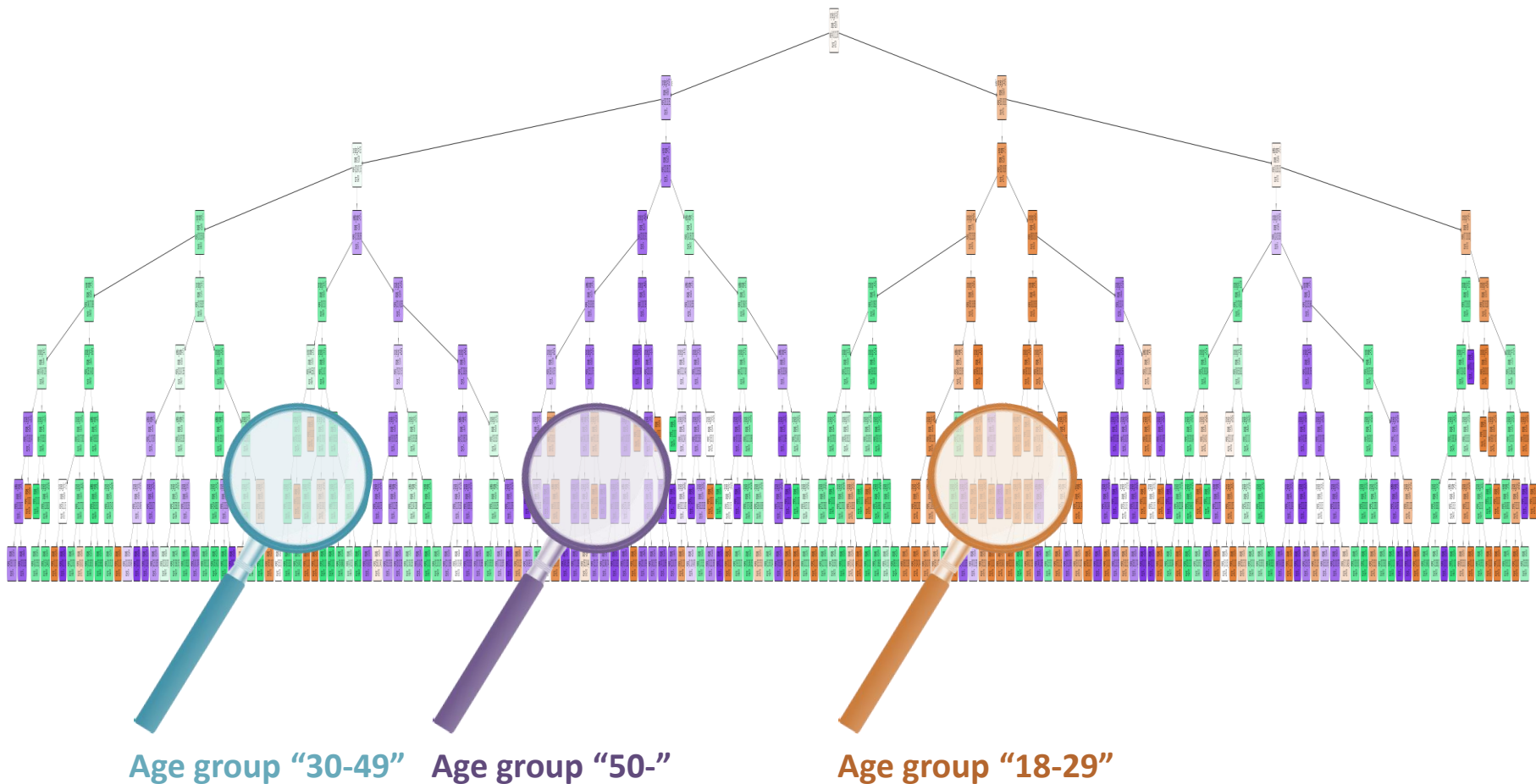
- Example: Customer from the “South” (region 3) buys 50€ wine and 8€ spirits.
- **What is the predicted age group? 18-29**



Predict age group “18-29”

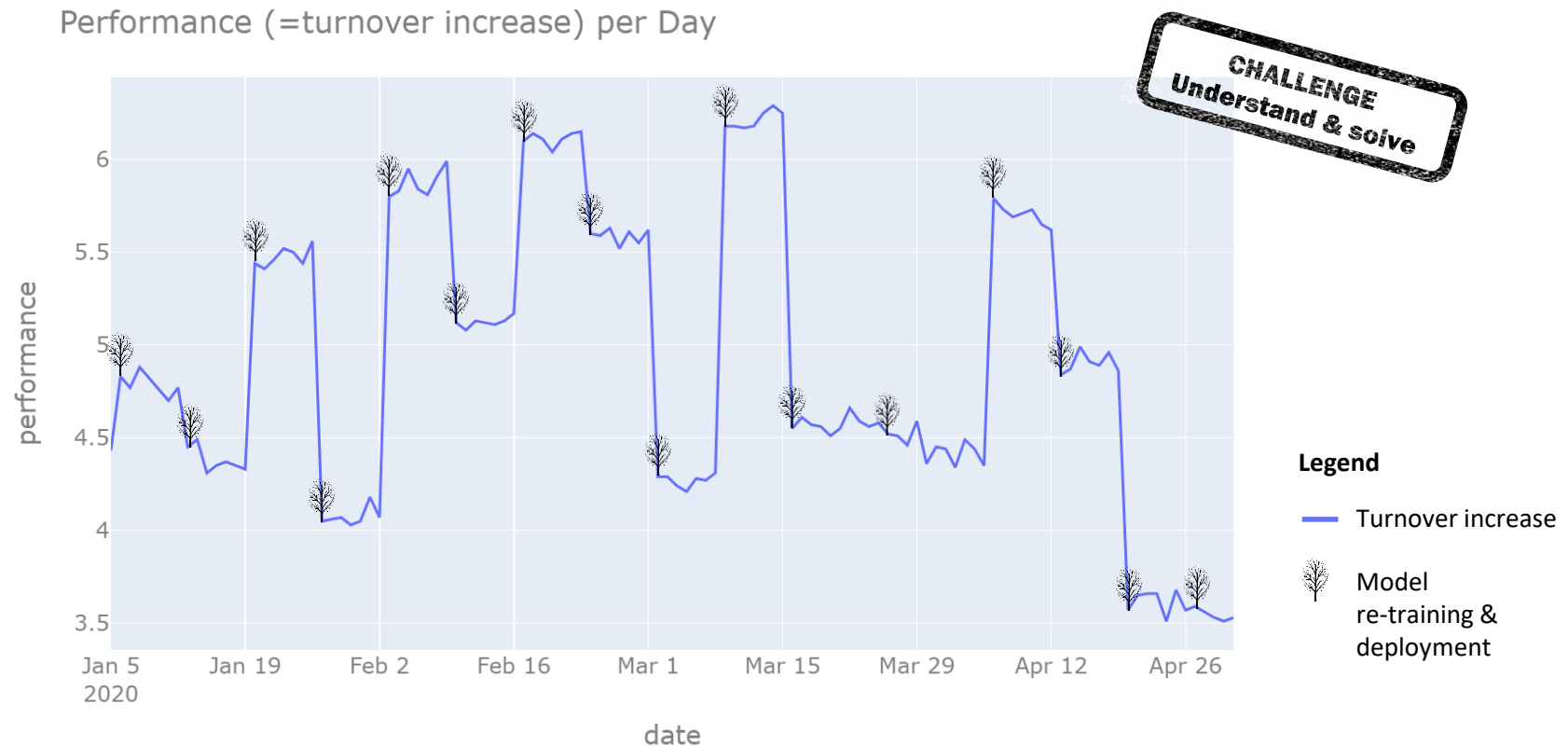
Use Case: Initial Solution

- Initial solution: Decision Tree
 - It is capable of identifying the patterns in the data.



Use Case: The Challenge

- Our model achieves an accuracy of ~80%
 - This should lead to ~5.00 % increase in turnover.
- Result:



Goals

- Present the central challenge in machine learning: the “**Bias-Variance Tradeoff**”
- See its effects in an exemplary use case.
- Learn about the idea to design more **effective** machine learning solutions with ensemble methods.

Agenda

- **Use Case & Goals**
- ☐ **Bias-Variance Tradeoff**
- ☐ **Reducing Variance with Ensemble Methods**
- ☐ **Summary & Outlook**

- **Fundamental challenge in machine learning**

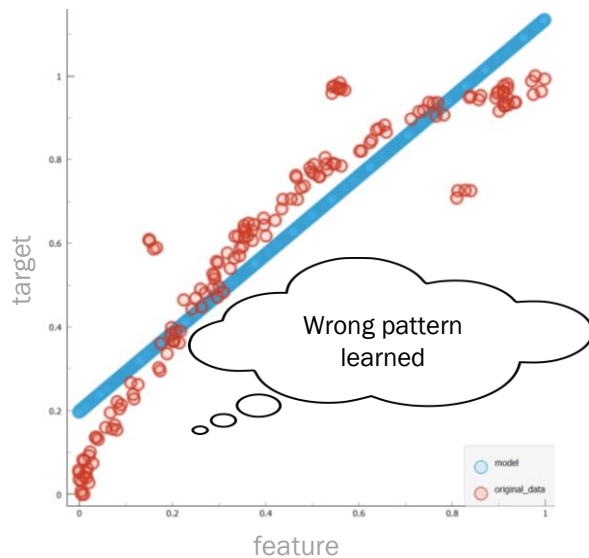
How can a model

- (a) catch the **right patterns** in historical data
- (b) work well on new data (i.e. **generalize**)?

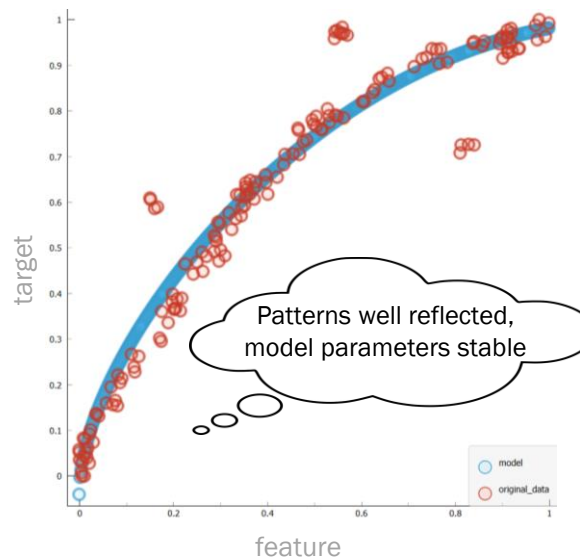
Bias-Variance Tradeoff

■ Fundamental challenge in machine learning

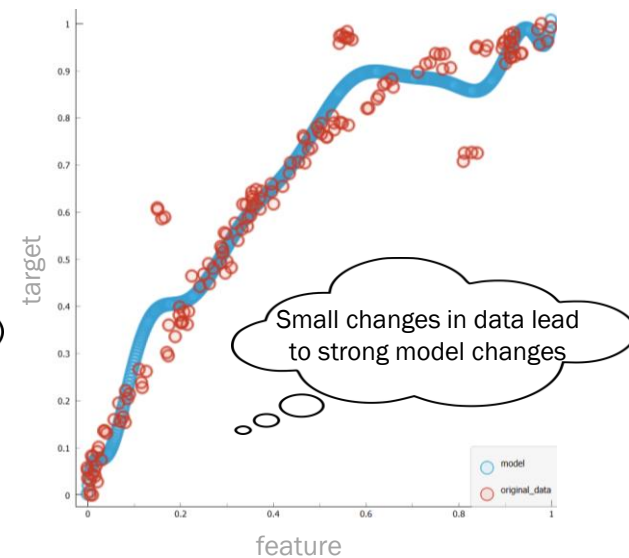
Linear model
(degree 1)



Linear model
(degree 2)



Linear model
(degree 14)



model complexity

**UNDERFITTING
= HIGH BIAS**



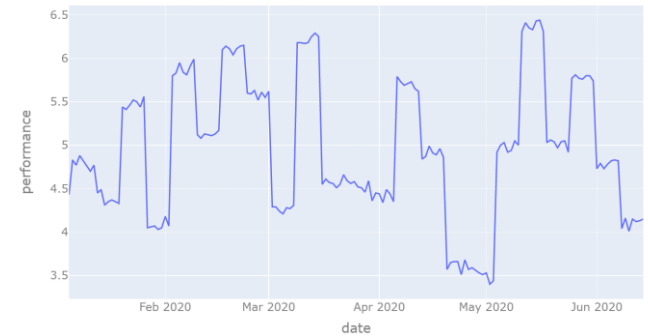
Bias-Variance Tradeoff



**OVERFITTING
= HIGH VARIANCE**

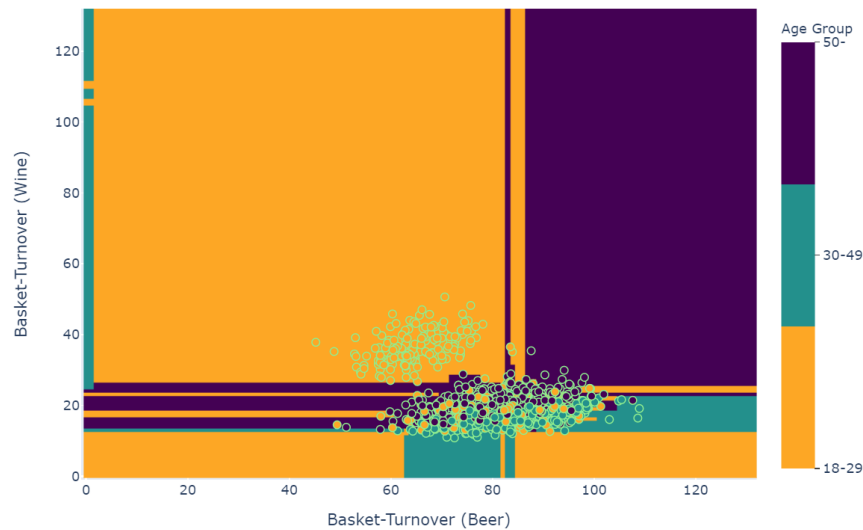
Use Case: Variance in Current Solution

- Probably, the model has a high variance
 - How does variance look like in classification?
 - Let's take a look at the decision boundaries.



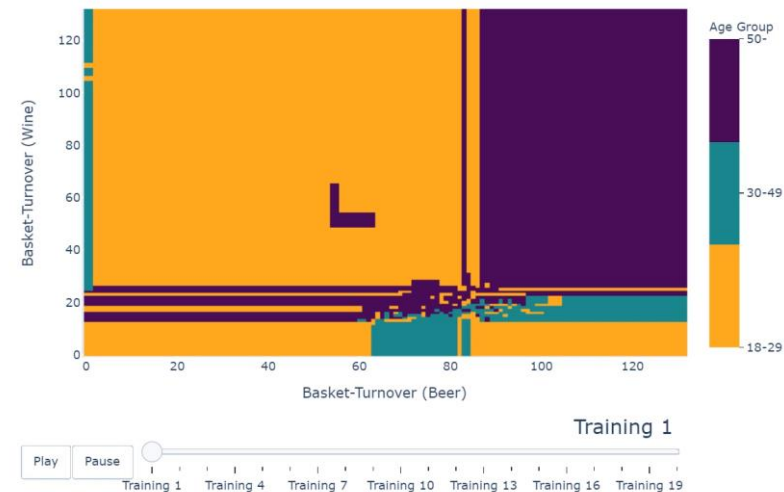
Fix values of 3 features, then a scatterplot is possible, e.g.:

Decision Regions (DecisionTreeClassifier)



Train model multiple times and watch decision boundary

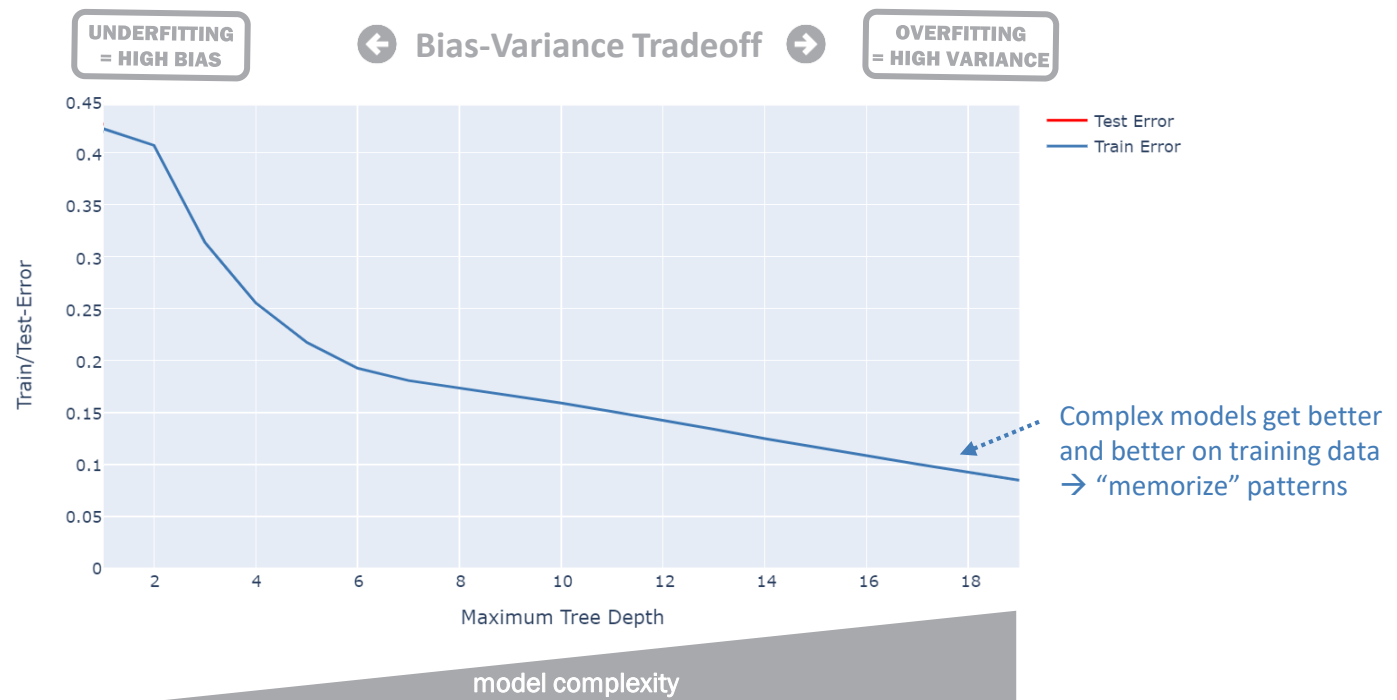
Decision Regions (DecisionTreeClassifier)



Bias-Variance Tradeoff

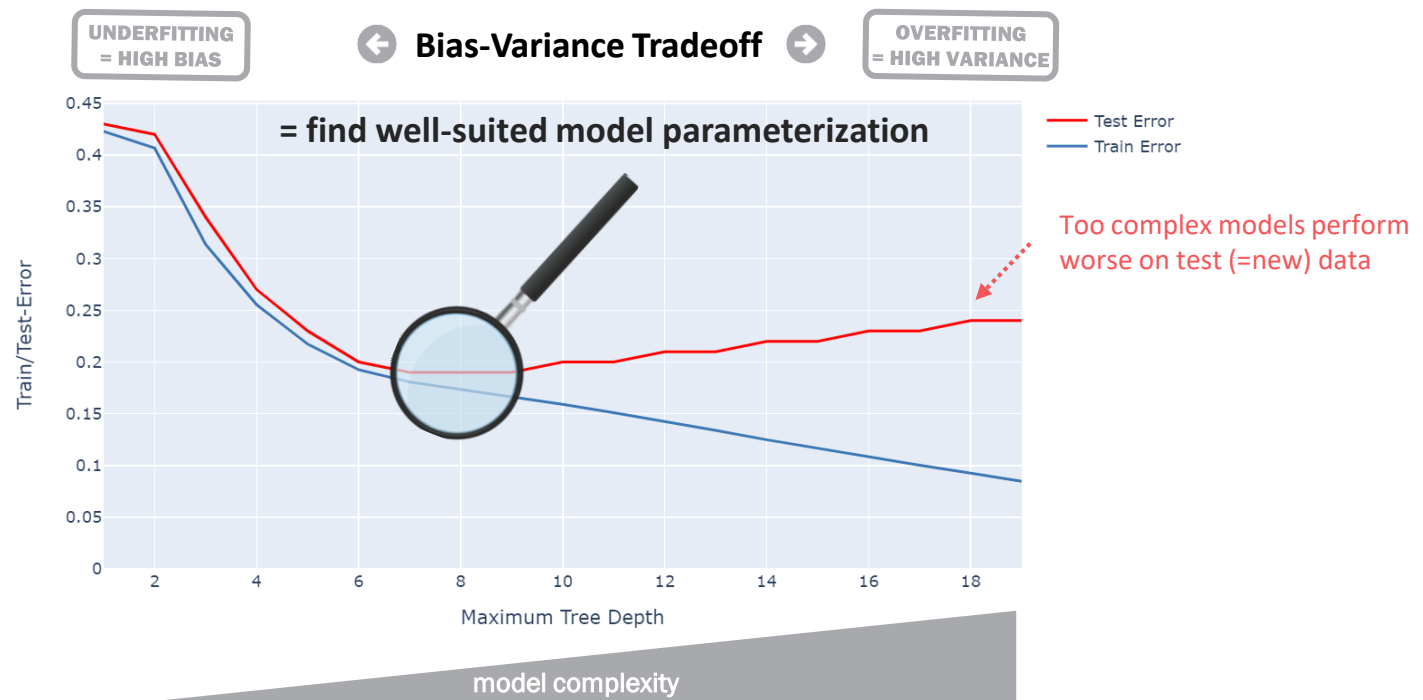
■ Approaching the Bias-Variance Tradeoff numerically

- Vary model parameters & measure train-test-error



Bias-Variance Tradeoff

- Approaching the Bias-Variance Tradeoff numerically
 - Vary model parameters & measure train-test-error



Over- and Underfitting

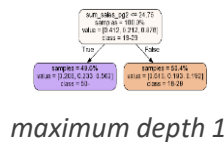
- There is a **fundamental challenge** in machine learning

How should a model be parameterized to work well in its use case?

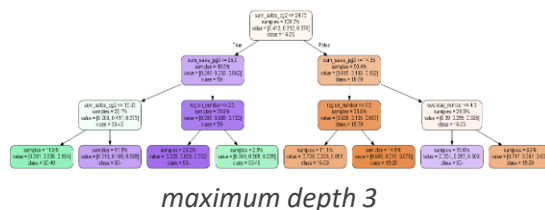
UNDERFITTING

The model is (potentially) ...

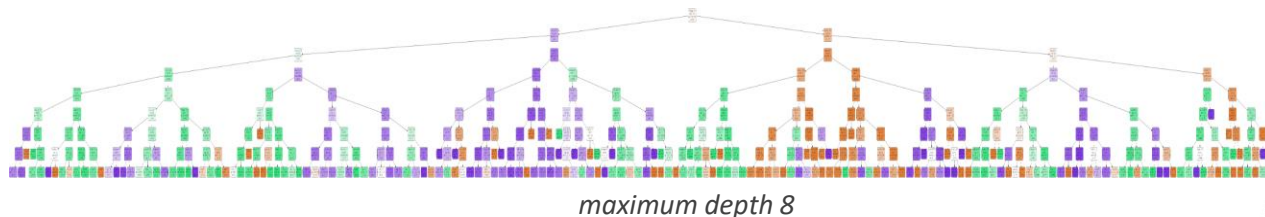
... too simple



... reasonable



... too complex



Model complexity

OVERFITTING

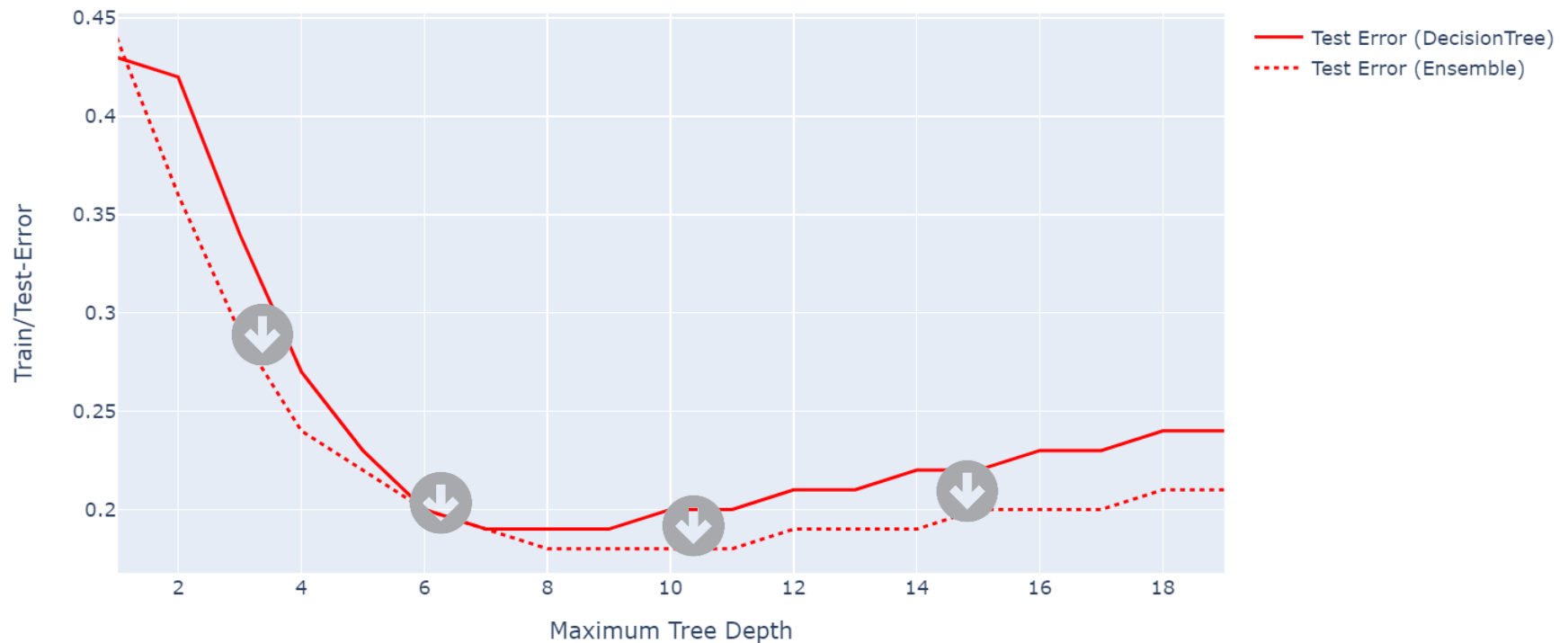
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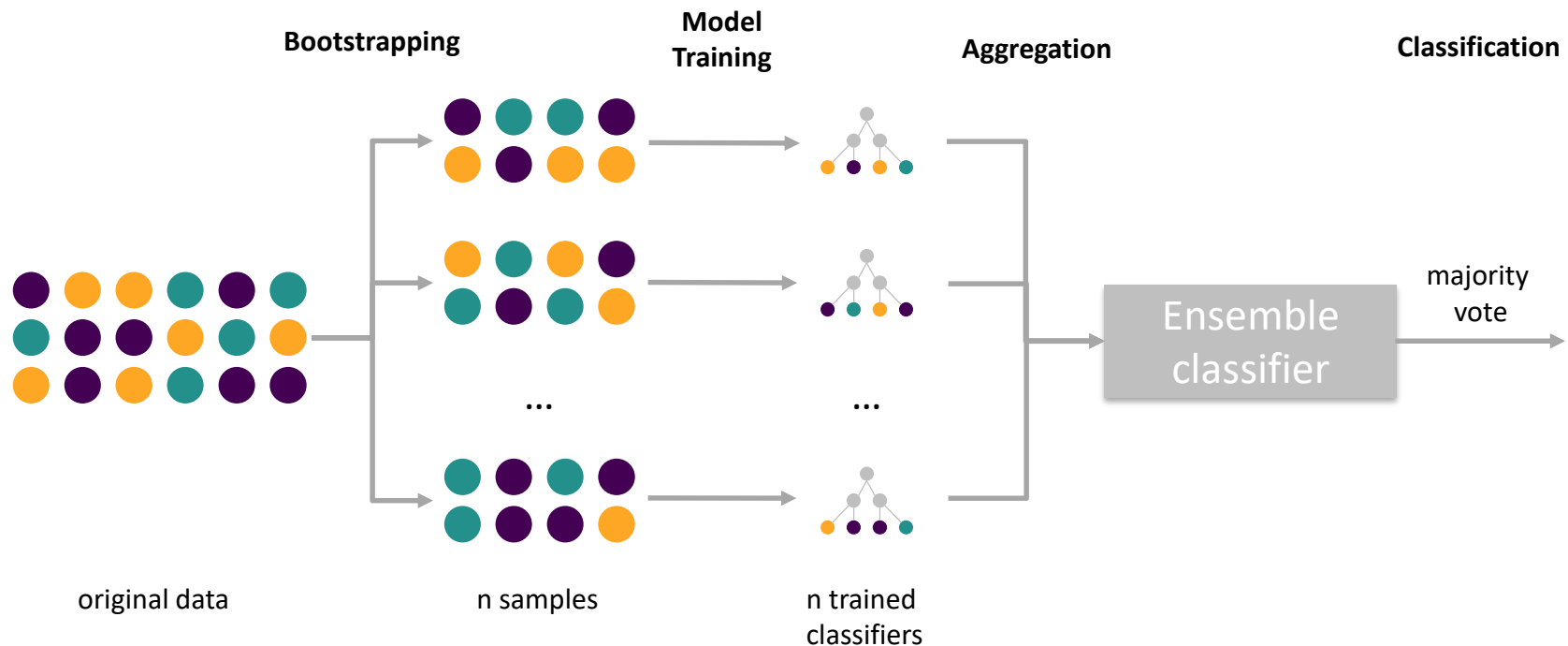
Reduce Variance with Ensemble Methods

■ Idea: combine predictions of multiple models

- Goal: improve model performance



■ Example: Bagging

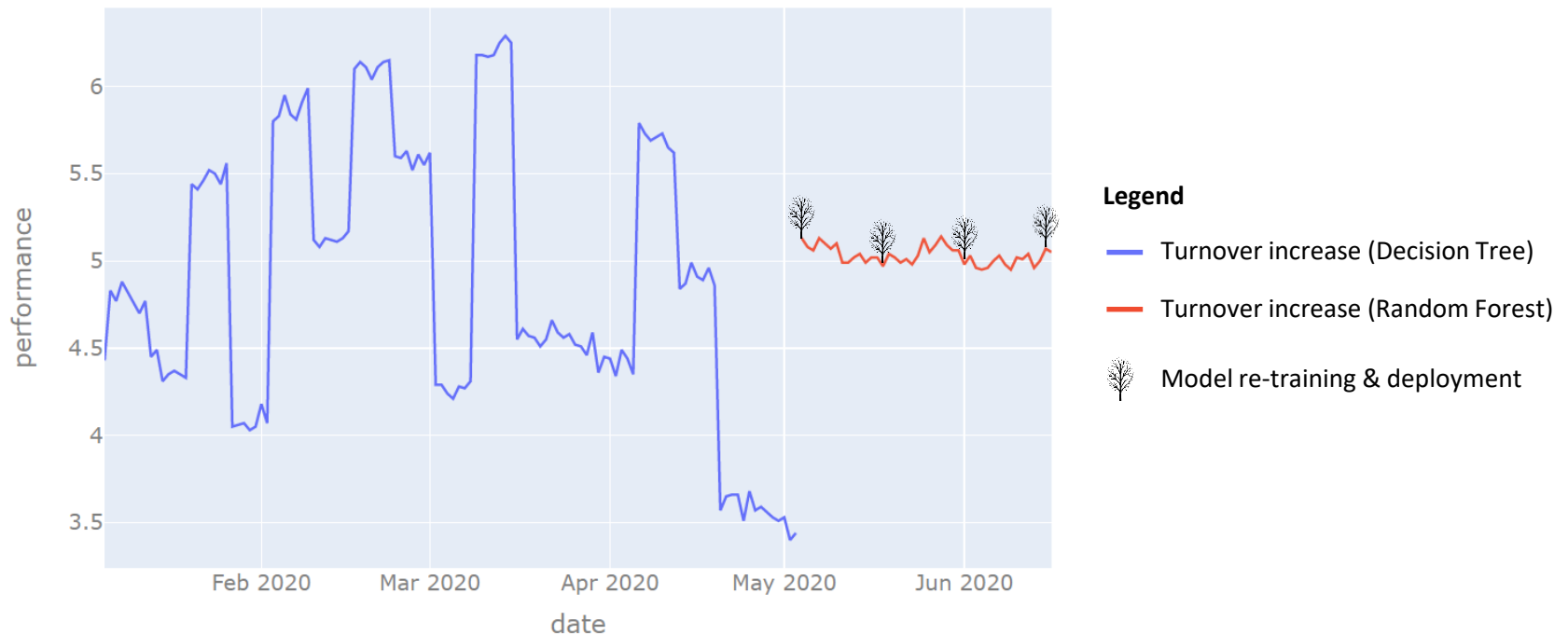


How do such models perform regarding the bias-variance tradeoff?

Use Case: The Improvement

- Our model now achieves an accuracy of ~82%
 - This leads to ~5.15 % increase in turnover.
 - Our tests show improved performance and less variance → **more effective model.**

Performance (=turnover increase) per Day

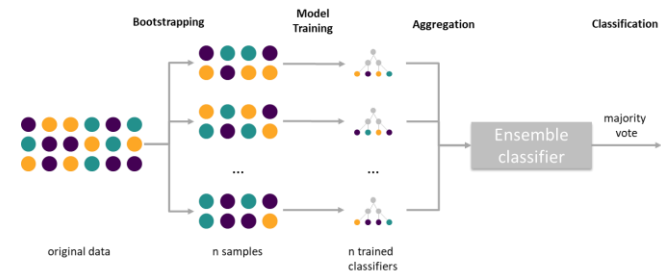
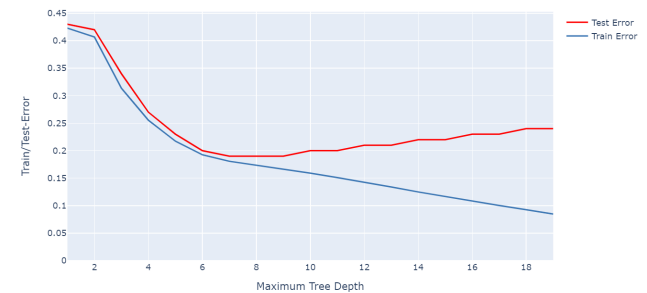


Agenda

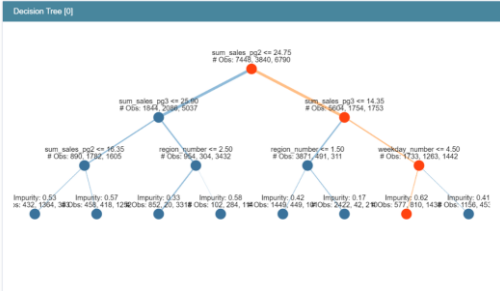
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Summary & Outlook

- Effects of overfitting in a predictive application
- Methods for evaluating bias vs. variance
- Ensemble methods to improve model performance



- Wick et al. (2020)



- Cf. Microsoft (2020)



References

Fortmann-Roe, Scott (2012). “Understanding the Bias-Variance Tradeoff.” Accessed June 04, 2020. <http://scott.fortmann-roe.com/docs/BiasVariance.html>.

Microsoft (2020). “Fit Interpretable Models. Explain Blackbox Machine Learning.” Accessed June 08, 2020. <https://github.com/interpretml/interpret>.

Wick, Felix, Ulrich Kerzel, and Michael Feindt (2020). *Cyclic Boosting - an Explainable Supervised Machine Learning Algorithm*.

Zhou, Zhi-Hua (2012). *Ensemble Methods: Foundations and Algorithms*. Chapman & Hall / CRC Machine Learning & Pattern Recognition. Hoboken: CRC Press.
<http://search.ebscohost.com/login.aspx?direct=true&scope=site&db=nlebk&db=nlabk&AN=465619>.

Thank you!

