

# GraphGAN: Graph Representation Learning with Generative Adversarial Nets

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# About Me

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- ❑ Full-time intern at Microsoft Research Asia

## ❑ Advisor

- ❑ Prof. Minyi Guo (SJTU)
- ❑ Dr. Xing Xie and Dr. Baining Guo (MSRA)

## ❑ Research interests

- ❑ Recommender systems [TCSS 2017] [RecSys 2017] [CIKM 2017] [WWW 2018]
- ❑ Graph representation learning [WSDM 2018] [AAAI 2018a]
- ❑ Machine learning applications [ICDCS 2017] [TPDS 2018] [AAAI 2018b]

## ❑ Homepage: <https://hwwang55.github.io>



# Outline

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## ❑ Introduction to graph representation learning

- ❑ Definition and application
- ❑ Taxonomy
- ❑ Representative work

## ❑ GraphGAN [AAAI 2018]

## ❑ GRL application

- ❑ Recommender systems [WWW 2018]
- ❑ Sentiment prediction [WSDM 2018]

1. A Comprehensive Survey of Graph Embedding: Problems, Techniques and Applications, TKDE 2017
2. <https://github.com/thunlp/NRLPapers>
3. [https://hwwang55.github.io/files/a\\_literature\\_review\\_on\\_rs\\_and\\_nrl.pdf](https://hwwang55.github.io/files/a_literature_review_on_rs_and_nrl.pdf) (in Chinese)

# Outline

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## ☐ Introduction to graph representation learning

- ☐ Definition and application
- ☐ Taxonomy
- ☐ Representative work

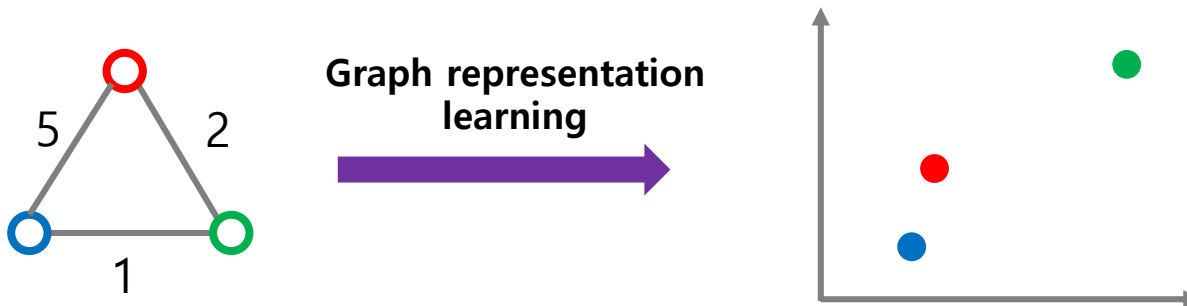
## ☐ GraphGAN [AAAI 2018]

## ☐ GRL application

- ☐ Recommender systems [WWW 2018]
- ☐ Sentiment prediction [WSDM 2018]

# Definition

- ❑ **Graph representation learning** tries to embed each node of a graph into a low-dimensional vector space, which preserves the structural similarities or distances among the nodes in the original graph
- ❑ Also known as **network embedding** / **graph embedding** / **network representation learning**



# Application

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❑ **Graph representation learning** can benefit a wide range of real-world applications:

- ❑ Link prediction (Gao, Denoyer, and Gallinari, CIKM 2011)
- ❑ Node classification (Tang, Aggarwal, and Liu, SDM 2016)
- ❑ Recommendation (Yu et al., WSDM 2014)
- ❑ Visualization (Maaten and Hinton, JMLR 2008)
- ❑ Knowledge graph representation (Lin et al., AAAI 2015)
- ❑ Clustering (Tian et al., AAAI 2014)
- ❑ Text embedding (Tang, Qu, and Mei, KDD 2015)
- ❑ Social network analysis (Liu et al., IJCAI 2016)

# Taxonomy (1/3)

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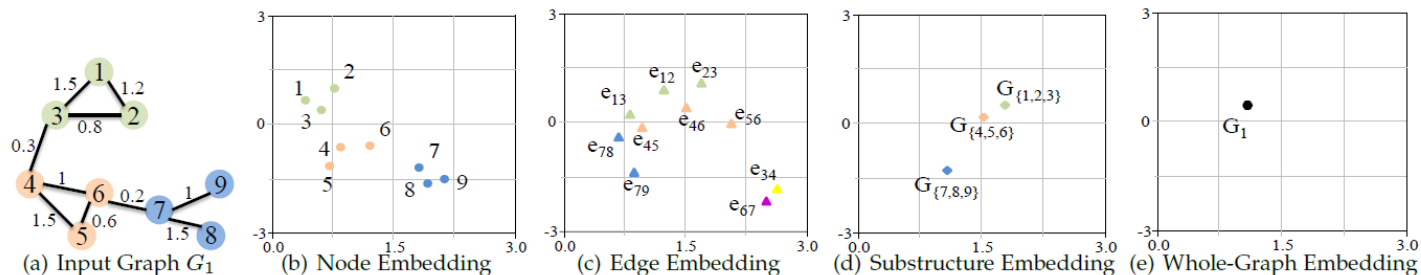
## Input

- ☐ Homogeneous graph (e.g., citation network)
  - ☐ Weighted / Unweighted
  - ☐ Directed / Undirected
  - ☐ Signed / Unsigned
- ☐ Heterogeneous graph
  - ☐ Multimedia network
  - ☐ Knowledge graph
- ☐ Graph with side information
  - ☐ Node/edge label (categorical)
  - ☐ Node/edge attribute (discrete or continuous)
  - ☐ Node feature (e.g., texts)
- ☐ Graph transformed from non-relational data
  - ☐ Manifold learning

# Taxonomy (2/3)

## Output

- ❑ Node embedding (the most common case)
- ❑ Edge embedding
  - ❑ Relations in knowledge graph
  - ❑ Link prediction
- ❑ Sub-graph embedding
  - ❑ Substructure embedding
  - ❑ Community embedding
- ❑ Whole-graph embedding
  - ❑ Multiple small graphs, e.g., molecule, protein





# Taxonomy (3/3)

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## Method

- ❑ Matrix factorization
  - ❑ SVD
  - ❑ Spectral Analysis
- ❑ Random walk
- ❑ Deep learning
  - ❑ Auto-encoder
  - ❑ Convolutional neural network
- ❑ Self-defined loss
  - ❑ Maximizing edge reconstruction probability
  - ❑ Minimizing distance-based loss
  - ❑ Minimizing margin-based ranking loss

# Representative Work

long long ago

PCA

LDA

MDS

not long ago

Isomap  
Science, 2000

LLE  
Science, 2000

LE  
NIPS, 2001

recent 5 years

GraRep  
CIKM, 2015

Word2vec  
NIPS, 2013

GraphEncoder  
AAAI, 2014

LINE  
WWW, 2015

HOPE  
KDD, 2016

DeepWalk  
KDD, 2014

HNE  
KDD, 2015

TransR  
AAAI, 2015

LANE  
WSDM, 2017

Node2vec  
KDD, 2016

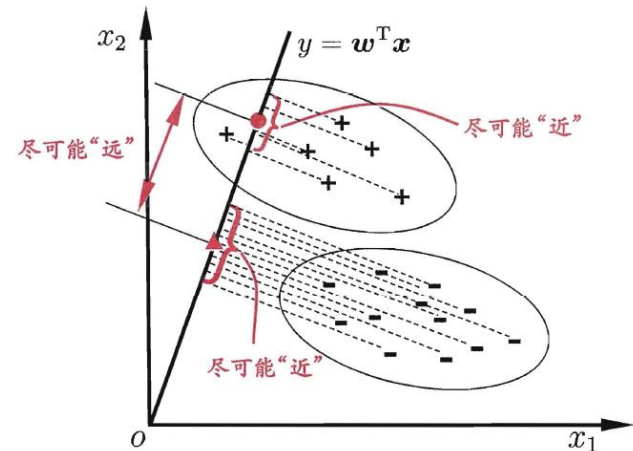
SDNE  
KDD, 2016

APP  
AAAI, 2017

# Linear Discriminant Analysis

- ❑ Suppose binary classification
- ❑  $D = \{(x_i, y_i)\}$ ,  $\mu_i$ : mean of data of the  $i$ -th class,  $\Sigma_i$ : covariance matrix of data of the  $i$ -th class
- ❑ Make projected covariance matrix as small as possible, while make projected distance between the mean of two classes as large as possible
- ❑ maximize

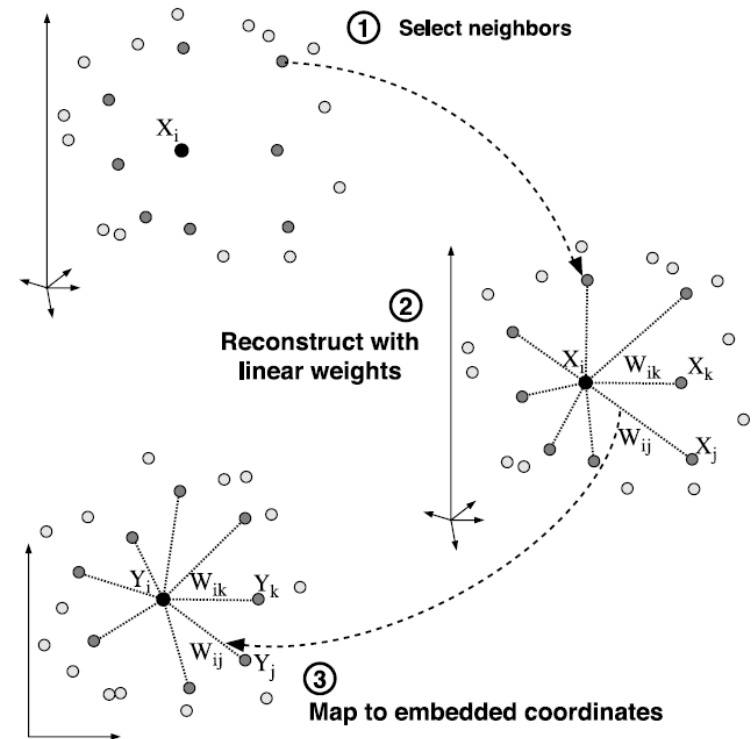
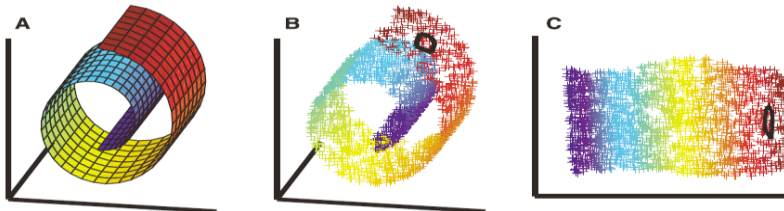
$$\begin{aligned} J &= \frac{\|w^T \mu_0 - w^T \mu_1\|_2^2}{w^T \Sigma_0 w + w^T \Sigma_1 w} \\ &= \frac{w^T (\mu_0 - \mu_1) (\mu_0 - \mu_1)^T w}{w^T (\Sigma_0 + \Sigma_1) w} \end{aligned}$$



# Locally Linear Embedding

## Introduction

- ❑ An unsupervised learning algorithm that computes low-dimensional, **neighborhood-preserving** embeddings of high-dimensional inputs
- ❑ LLE keeps linear dependency between local instances



# Word2vec

## ❑ Skip-Gram Model

- ❑ Find word representations that are useful for **predicting the surrounding words** in a sentence
- ❑ Maximizing

$$\frac{1}{T} \sum_{t=1}^T \sum_{-c \leq j \leq c, j \neq 0} \log p(w_{t+j} | w_t)$$

where

$$p(w_O | w_I) = \frac{\exp(v'_{w_O}{}^\top v_{w_I})}{\sum_{w=1}^W \exp(v'_w{}^\top v_{w_I})}$$

- ❑ Negative sampling:

$$\log \sigma(v'_{w_O}{}^\top v_{w_I}) + \sum_{i=1}^k \mathbb{E}_{w_i \sim P_n(w)} \left[ \log \sigma(-v'_{w_i}{}^\top v_{w_I}) \right]$$

# DeepWalk / Node2vec

## ❑ DeepWalk: Random walk + Word2vec

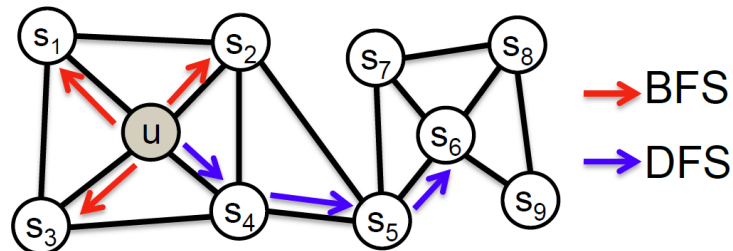
- ❑ Sample the next node to be visited **uniformly** from the neighbors of current node

$$\underset{\Phi}{\text{minimize}} \quad -\log \Pr \left( \{v_{i-w}, \dots, v_{i+w}\} \setminus v_i \mid \Phi(v_i) \right)$$

- ❑ Hierarchical softmax

## ❑ Node2vec: Biased random walk + Word2vec

- ❑ Sample the next node to be visited **with bias** from the neighbors of current node



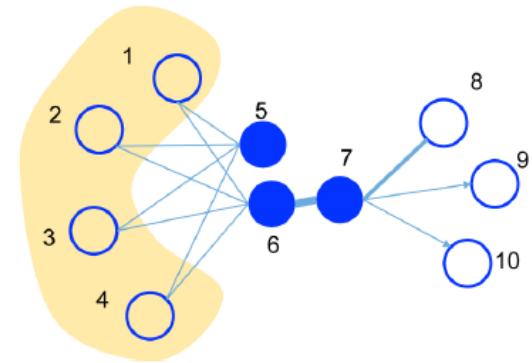
## First-order proximity

$$O_1 = d(\hat{p}_1(\cdot, \cdot), p_1(\cdot, \cdot))$$

$$p_1(v_i, v_j) = \frac{1}{1 + \exp(-\vec{u}_i^T \cdot \vec{u}_j)}$$

$$\hat{p}_1(i, j) = \frac{w_{ij}}{W}$$

$$O_1 = - \sum_{(i,j) \in E} w_{ij} \log p_1(v_i, v_j)$$



## Second-order proximity

$$O_2 = \sum_{i \in V} \lambda_i d(\hat{p}_2(\cdot | v_i), p_2(\cdot | v_i))$$

$$p_2(v_j | v_i) = \frac{\exp(\vec{u}'_j{}^T \cdot \vec{u}_i)}{\sum_{k=1}^{|V|} \exp(\vec{u}'_k{}^T \cdot \vec{u}_i)}$$

$$\hat{p}_2(v_j | v_i) = \frac{w_{ij}}{d_i}$$

$$O_2 = - \sum_{(i,j) \in E} w_{ij} \log p_2(v_j | v_i)$$

# TransX

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- ❑ Embed **knowledge graph** into a continuous vector space while preserving structural information
- ❑ TransE (NIPS 13):
  - ❑ Ensures  $\mathbf{h} + \mathbf{r} \approx \mathbf{t}$  when  $(h, r, t)$  holds
- ❑ TransH (AAAI 14):
  - ❑ Ensures  $\mathbf{h}_{\perp} + \mathbf{r} \approx \mathbf{t}_{\perp}$  when  $(h, r, t)$  holds, where  $\mathbf{h}_{\perp} = \mathbf{h} - \mathbf{w}_r^T \mathbf{h} \mathbf{w}_r$  and  $\mathbf{t}_{\perp} = \mathbf{t} - \mathbf{w}_r^T \mathbf{t} \mathbf{w}_r$
- ❑ TransR (AAAI 15):
  - ❑ Score function:  $f_r(h, t) = \|\mathbf{h} \mathbf{M}_r + \mathbf{r} - \mathbf{t} \mathbf{M}_r\|_2^2$ , where  $\mathbf{M}_r$  is the projection matrix for relation  $r$ .



# SDNE

## Reconstruction loss term

$$\begin{aligned}\mathcal{L}_{2nd} &= \sum_{i=1}^n \|(\hat{\mathbf{x}}_i - \mathbf{x}_i) \odot \mathbf{b}_i\|_2^2 \\ &= \|(\hat{X} - X) \odot B\|_F^2\end{aligned}$$

## Proximity loss term

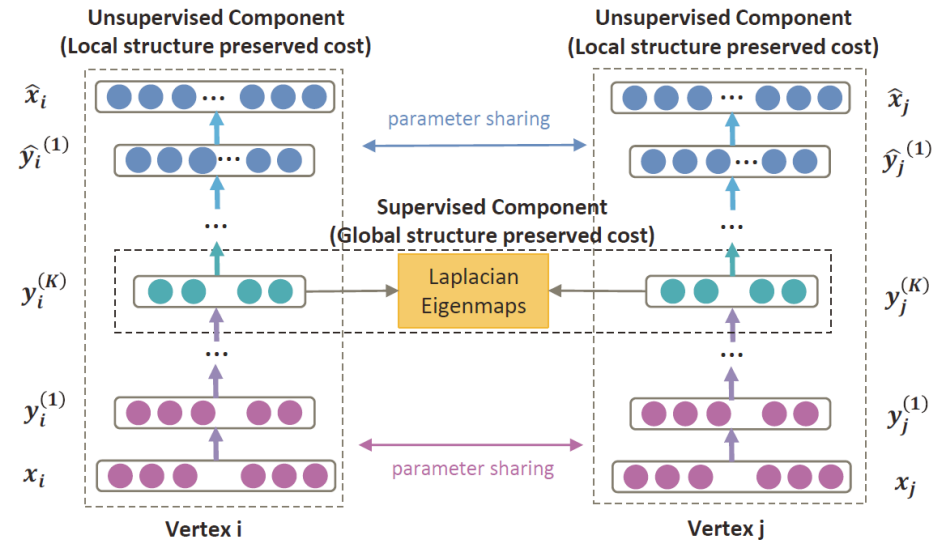
$$\begin{aligned}\mathcal{L}_{1st} &= \sum_{i,j=1}^n s_{i,j} \|\mathbf{y}_i^{(K)} - \mathbf{y}_j^{(K)}\|_2^2 \\ &= \sum_{i,j=1}^n s_{i,j} \|\mathbf{y}_i - \mathbf{y}_j\|_2^2\end{aligned}$$

## Regularization term

$$\mathcal{L}_{reg} = \frac{1}{2} \sum_{k=1}^K (\|\mathbf{W}^{(k)}\|_F^2 + \|\hat{\mathbf{W}}^{(k)}\|_F^2)$$

## Loss function

$$\mathcal{L}_{mix} = \mathcal{L}_{2nd} + \alpha \mathcal{L}_{1st} + \nu \mathcal{L}_{reg}$$



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## ☐ **GraphGAN** [AAAI 2018]

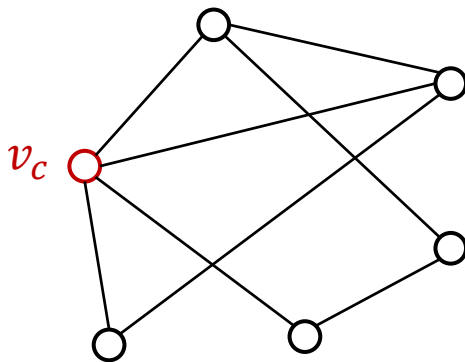
## ☐ GRL application

- ☐ Recommender systems [WWW 2018]
- ☐ Sentiment prediction [WSDM 2018]

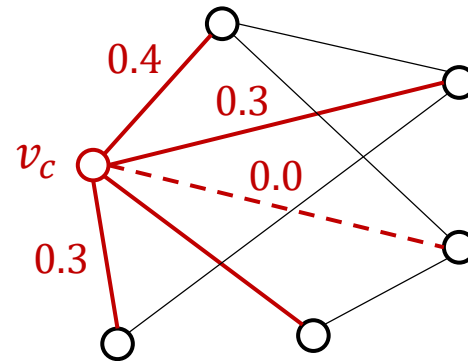
# Motivation (1/3)

## Generative Model

- Generative graph representation learning model assumes an **underlying true connectivity distribution**  $p_{true}(v|v_c)$  for each vertex  $v_c$ 
  - Similar to GMM and LDA
  - The edges can be viewed as observed samples generated by  $p_{true}(v|v_c)$
  - Vertex embeddings are learned by maximizing the likelihood of edges
  - E.g., DeepWalk (KDD 2014) and node2vec (KDD 2016)



*Original graph*

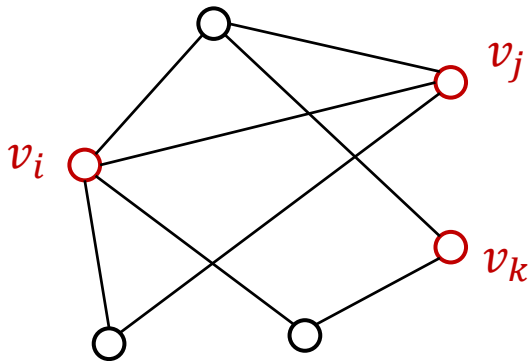


$p_{true}(v|v_c)$

# Motivation (2/3)

## Discriminative Model

- ❑ Discriminative graph representation learning model aim to learn a **classifier** for predicting the existence of edges directly
  - ❑ Consider two vertices  $v_i$  and  $v_j$  jointly as features
  - ❑ Predict the probability of an edge existing between them, i.e.,  $p(\text{edge}|v_i, v_j)$
  - ❑ E.g., SDNE (KDD 2016) and PPNE (DASFAA, 2017)



$$p(\text{edge}|v_i, v_j) = 0.8$$

$$p(\text{edge}|v_i, v_k) = 0.3$$

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# Motivation (3/3)

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## G + D ?

- ❑ Generative and discriminative models are two sides of the same coin
- ❑ LINE (WWW 2015) has tried to combine these two objectives
- ❑ Generative adversarial nets (GAN) have received a great deal of attention
  - ❑ GAN designs a game-theoretical minimax game to combine G and D
  - ❑ GAN achieves success in various applications:
    - ❑ image generation (Denton et al., NIPS 2015)
    - ❑ sequence generation (Yu et al., AACL 2017)
    - ❑ dialogue generation (Li et al., arXiv 2017)
    - ❑ information retrieval (Wang et al., SIGIR 2017)
    - ❑ domain adaption (Zhang, Barzilay, and Jaakkola, arXiv 2017)
- ❑ We propose **GraphGAN**, a framework that unifies generative and discriminative thinking for graph representation learning

# The Minimax Game

- ❑  $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ ,  $\mathcal{V} = \{v_1, \dots, v_V\}$ ,  $\mathcal{E} = \{e_{ij}\}_{i,j=1}^V$
- ❑  $\mathcal{N}(v_c)$ : set of neighbors of  $v_c$
- ❑  $p_{true}(v_c)$ : underlying true connectivity distribution for  $v_c$
- ❑ The objective of GraphGAN is to learn the following two models:
  - ❑  $G(v|v_c; \theta_G)$  which tries to approximate  $p_{true}(v_c)$
  - ❑  $D(v, v_c; \theta_D)$  which aims to discriminate the connectivity for the vertex pair  $(v, v_c)$
- ❑ The two-player minimax game:

$$\min_{\theta_G} \max_{\theta_D} V(G, D) = \sum_{c=1}^V \left( \mathbb{E}_{v \sim p_{true}(\cdot|v_c)} [\log D(v, v_c; \theta_D)] + \mathbb{E}_{v \sim G(\cdot|v_c; \theta_G)} [\log (1 - D(v, v_c; \theta_D))] \right) \quad (1)$$

# Implementation & Optimization of D

$$\min_{\theta_G} \max_{\theta_D} V(G, D) = \sum_{c=1}^V \left( \mathbb{E}_{v \sim p_{\text{true}}(\cdot | v_c)} [\log D(v, v_c; \theta_D)] + \mathbb{E}_{v \sim G(\cdot | v_c; \theta_G)} [\log (1 - D(v, v_c; \theta_D))] \right) \quad (1)$$

□ Implementation of D:

$$D(v, v_c; \theta_D) = \sigma(\mathbf{d}_v^\top \mathbf{d}_{v_c}) = \frac{1}{1 + \exp(-\mathbf{d}_v^\top \mathbf{d}_{v_c})}, \quad (2)$$

where  $\mathbf{d}_v, \mathbf{d}_{v_c} \in \mathbb{R}^k$  are the  $k$ -dimensional vectors of  $v$  and  $v_c$  for D

□ Gradient of  $V(G, D)$  w.r.t  $\theta_D$ :

$$\nabla_{\theta_D} V(G, D) = \begin{cases} \nabla_{\mathbf{d}_v, \mathbf{d}_{v_c}} \log D(v, v_c; \theta_D), & \text{if } v \sim p_{\text{true}}; \\ \nabla_{\mathbf{d}_v, \mathbf{d}_{v_c}} (1 - \log D(v, v_c; \theta_D)), & \text{if } v \sim G. \end{cases} \quad (3)$$

# Optimization of G

$$\min_{\theta_G} \max_{\theta_D} V(G, D) = \sum_{c=1}^V \left( \mathbb{E}_{v \sim p_{\text{true}}(\cdot|v_c)} [\log D(v, v_c; \theta_D)] + \mathbb{E}_{v \sim G(\cdot|v_c; \theta_G)} [\log (1 - D(v, v_c; \theta_D))] \right) \quad (1)$$

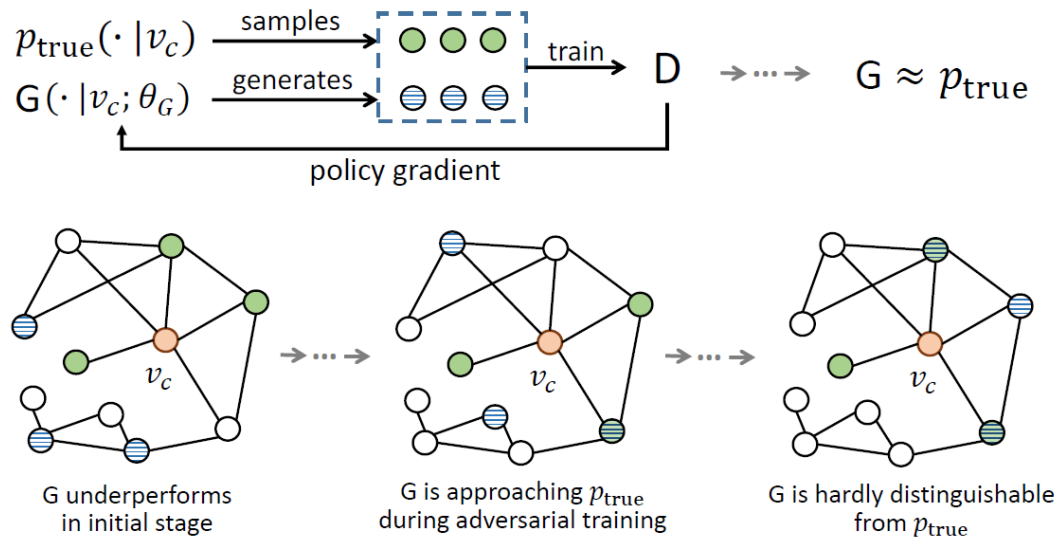
□ Gradient of  $V(G, D)$  w.r.t  $\theta_G$  (policy gradient):

$$\begin{aligned} & \nabla_{\theta_G} V(G, D) \\ &= \nabla_{\theta_G} \sum_{c=1}^V \mathbb{E}_{v \sim G(\cdot|v_c; \theta_G)} [\log (1 - D(v, v_c; \theta_D))] \\ &= \sum_{c=1}^V \sum_{i=1}^N \nabla_{\theta_G} G(v_i|v_c; \theta_G) \log (1 - D(v_i, v_c; \theta_D)) \\ &= \sum_{c=1}^V \sum_{i=1}^N G(v_i|v_c; \theta_G) \nabla_{\theta_G} \log G(v_i|v_c; \theta_G) \log (1 - D(v_i, v_c; \theta_D)) \\ &= \sum_{c=1}^V \mathbb{E}_{v \sim G(\cdot|v_c; \theta_G)} [\nabla_{\theta_G} \log G(v|v_c; \theta_G) \log (1 - D(v, v_c; \theta_D))] \end{aligned} \quad (4)$$



# GraphGAN Framework

$$\min_{\theta_G} \max_{\theta_D} V(G, D) = \sum_{c=1}^V \left( \mathbb{E}_{v \sim p_{\text{true}}(\cdot | v_c)} [\log D(v, v_c; \theta_D)] + \mathbb{E}_{v \sim G(\cdot | v_c; \theta_G)} [\log (1 - D(v, v_c; \theta_D))] \right) \quad (1)$$



# Implementation of G

## ❑ Softmax?

- ❑ Computationally inefficient
- ❑ Graph-structure-unaware

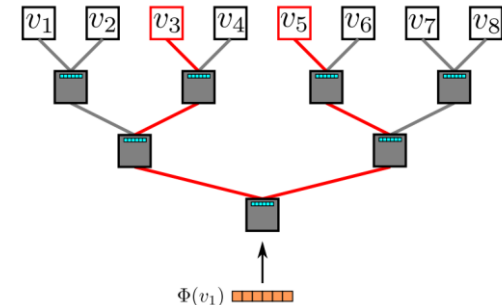
$$G(v|v_c; \theta_G) = \frac{\exp(\mathbf{g}_v^\top \mathbf{g}_{v_c})}{\sum_{v \neq v_c} \exp(\mathbf{g}_v^\top \mathbf{g}_{v_c})}$$

where  $\mathbf{g}_v, \mathbf{g}_{v_c} \in \mathbb{R}^k$  are the  $k$ -dimensional vectors of  $v$  and  $v_c$  for  $G$

## ❑ Hierarchical softmax?

- ❑ Graph-structure-unaware

$$p(w|w_I) = \prod_{j=1}^{L(w)-1} \sigma \left( \mathbb{I}[n(w, j+1) = \text{ch}(n(w, j))] \cdot v'_{n(w, j)}^\top v_{w_I} \right)$$



## ❑ Negative sampling?

- ❑ Not a valid probability distribution
- ❑ graph-structure-unaware

$$\log \sigma(v'_{w_O}^\top v_{w_I}) + \sum_{i=1}^k \mathbb{E}_{w_i \sim P_n(w)} \left[ \log \sigma(-v'_{w_i}^\top v_{w_I}) \right]$$

# Graph Softmax (1/5)

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## Objectives

- ❑ The design of graph softmax should satisfy the following three properties:
  - ❑ **Normalized:** The generator should produce a valid probability distribution, i.e.,  
$$\sum_{v \neq v_c} G(v|v_c; \theta_G) = 1$$
  - ❑ **Graph-structure-aware:** The generator should take advantage of the structural information of a graph
  - ❑ **Computationally efficient:** The computation of  $G(v|v_c; \theta_G)$  should only involve a small number of vertices in the graph

# Graph Softmax (2/5)

## Design

❑ **Breadth First Search (BFS)** on  $\mathcal{G}$  from every vertex  $v_c$

❑ **BFS-tree**  $T_c$  rooted at  $v_c$

❑ For a given vertex  $v$  and one of its neighbors  $v_i \in \mathcal{N}_c(v)$ , the **relevance probability** of  $v_i$  given  $v$  as

$$p_c(v_i|v) = \frac{\exp(\mathbf{g}_{v_i}^\top \mathbf{g}_v)}{\sum_{v_j \in \mathcal{N}_c(v)} \exp(\mathbf{g}_{v_j}^\top \mathbf{g}_v)}, \quad (6)$$

where  $\mathcal{N}_c(v)$  is the set of neighbors of  $v$  in  $T_c$

❑ **Graph softmax**

$$G(v|v_c; \theta_G) \triangleq \left( \prod_{j=1}^m p_c(v_{r_j}|v_{r_{j-1}}) \right) \cdot p_c(v_{r_m}|v_{r_{m-1}}), \quad (7)$$

given the unique path from  $v_c$  to  $v$  in tree  $T_c$ :  $P_{v_c \rightarrow v} = (v_{r_0}, v_1, \dots, v_{r_m})$ , where  $v_{r_0} = v_c$  and  $v_{r_m} = v$

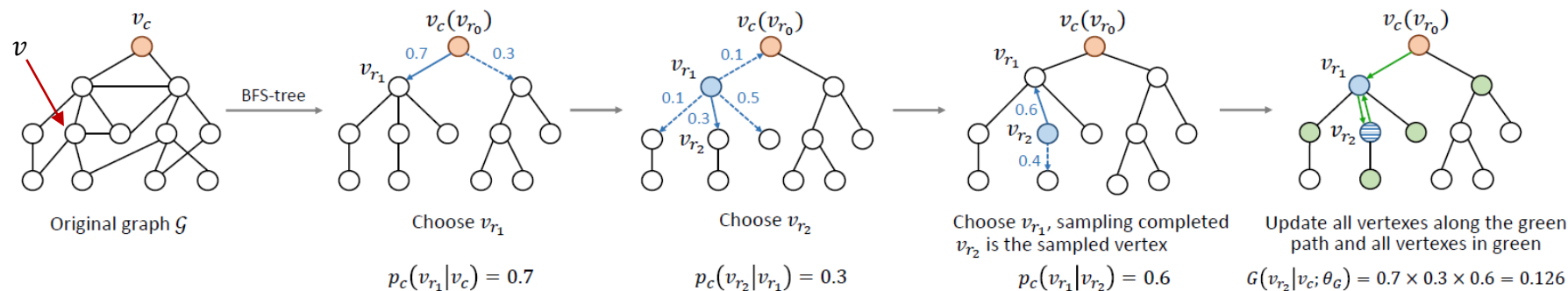
# Graph Softmax (3/5)

## Design

### Graph softmax

$$G(v|v_c; \theta_G) \triangleq \left( \prod_{j=1}^m p_c(v_{r_j}|v_{r_{j-1}}) \right) \cdot p_c(v_{r_m-1}|v_{r_m}), \quad (7)$$

given the unique path from  $v_c$  to  $v$  in tree  $T_c$ :  $P_{v_c \rightarrow v} = (v_{r_0}, v_1, \dots, v_{r_m})$ , where  $v_{r_0} = v_c$  and  $v_{r_m} = v$



# Graph Softmax (4/5)

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## Properties

- $\sum_{v \neq v_c} G(v|v_c; \theta_G) = 1$  in graph softmax
- In graph softmax,  $G(v|v_c; \theta_G)$  decreases exponentially with the increase of the shortest distance between  $v$  and  $v_c$  in original graph  $\mathcal{G}$
- In graph softmax, calculation of  $G(v|v_c; \theta_G)$  depends on  $O(d \log V)$  vertices, where  $d$  is average degree of vertices and  $V$  is the number of vertices in graph  $\mathcal{G}$

# Graph Softmax (5/5)

## Generating Strategy

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### Algorithm 1 Online generating strategy for the generator

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**Input:** BFS-tree  $T_c$ , representation vectors  $\{\mathbf{g}_i\}_{i \in \mathcal{V}}$

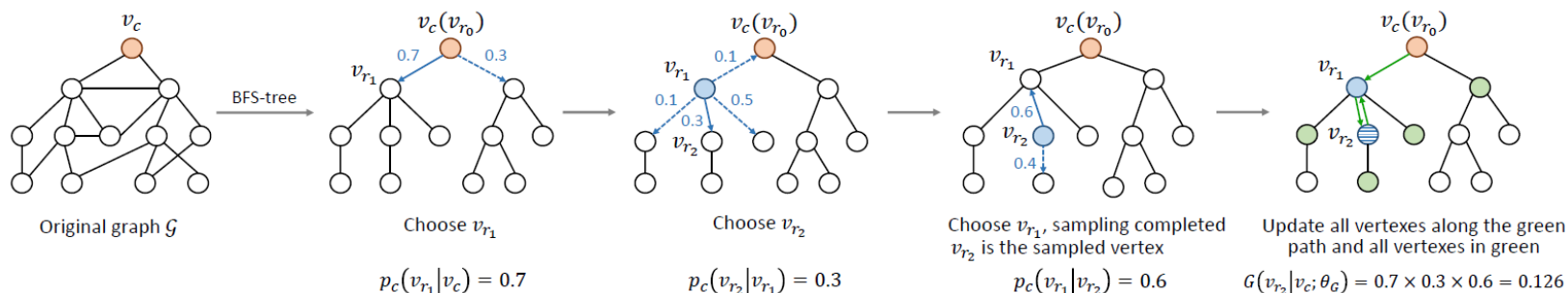
**Output:** generated sample  $v_{gen}$

```

1:  $v_{pre} \leftarrow v_c, v_{cur} \leftarrow v_c$ ;
2: while true do
3:   Randomly select  $v_i$  proportionally to  $p_c(v_i|v_{cur})$  in Eq.
   (6);
4:   if  $v_i = v_{pre}$  then
5:      $v_{gen} \leftarrow v_{cur}$ ;
6:     return  $v_{gen}$ 
7:   else
8:      $v_{pre} \leftarrow v_{cur}, v_{cur} \leftarrow v_i$ ;
9:   end if
10: end while

```

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# GraphGAN Algorithm

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**Algorithm 2** GraphGAN framework

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**Input:** dimension of embedding  $k$ , size of generating samples  $s$ , size of discriminating samples  $t$

**Output:** generator  $G(v|v_c; \theta_G)$ , discriminator  $D(v, v_c; \theta_D)$

- 1: Initialize and pre-train  $G(v|v_c; \theta_G)$  and  $D(v, v_c; \theta_D)$ ;
  - 2: Construct BFS-tree  $T_c$  for all  $v_c \in \mathcal{V}$ ;
  - 3: **while** GraphGAN not converge **do**
  - 4:   **for** G-steps **do**
  - 5:      $G(v|v_c; \theta_G)$  generates  $s$  vertices for each vertex  $v_c$  according to Algorithm 1;
  - 6:     Update  $\theta_G$  according to Eq. (4), (6) and (7);
  - 7:   **end for**
  - 8:   **for** D-steps **do**
  - 9:     Sample  $t$  positive vertices from ground truth and  $t$  negative vertices from  $G(v|v_c; \theta_G)$  for each vertex  $v_c$ ;
  - 10:     Update  $\theta_D$  according to Eq. (2) and (3);
  - 11:   **end for**
  - 12: **end while**
  - 13: **return**  $G(v|v_c; \theta_G)$  and  $D(v, v_c; \theta_D)$
-



# Experiments (1/3)

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## Datasets

- ❑ arXiv-AstroPh: 18,772 vertices and 198,110 edges
- ❑ arXiv-GrQc: 5,242 vertices and 14,496 edges
- ❑ BlogCatalog: 10,312 vertices, 333,982 edges and 39 labels
- ❑ Wikipedia: 4,777 vertices, 184,812 edges and 40 labels
- ❑ MovieLens-1M: 6,040 users and 3,706 movies

## Baselines

- ❑ DeepWalk (KDD 2014)
- ❑ LINE (WWW 2015)
- ❑ Node2vec (KDD 2016)
- ❑ Struc2vec (KDD 2017)

# Experiments (2/3)

## Link Prediction

### □ Learning curves

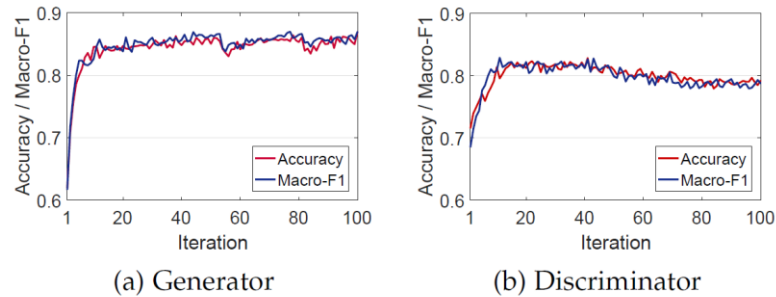


Fig. 4: Learning curves of the generator and the discriminator of GraphGAN on arXiv-GrQc in link prediction.

### □ Results

TABLE 1: Accuracy and Macro-F1 on arXiv-AstroPh and arXiv-GrQc in link prediction.

Model	arXiv-AstroPh		arXiv-GrQc	
	Accuracy	Macro-F1	Accuracy	Macro-F1
DeepWalk	0.841	0.839	0.803	0.812
LINE	0.820	0.814	0.764	0.761
Node2vec	0.845	0.854	0.844	0.842
Struc2vec	0.821	0.810	0.780	0.776
GraphGAN	<b>0.855</b>	<b>0.859</b>	<b>0.849</b>	<b>0.853</b>

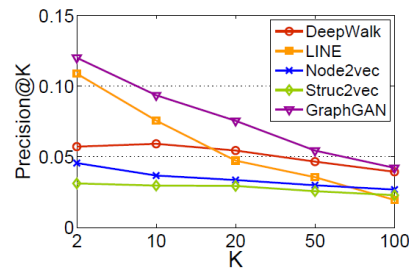
# Experiments (3/3)

## Node Classification

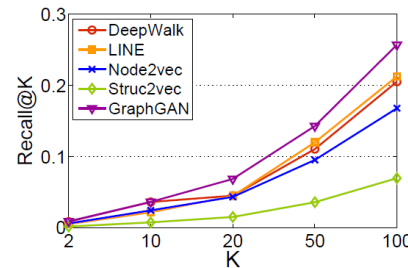
TABLE 2: Accuracy and Macro-F1 on BlogCatalog and Wikipedia in node classification.

Model	BlogCatalog		Wikipedia	
	Accuracy	Macro-F1	Accuracy	Macro-F1
DeepWalk	0.225	0.214	0.194	0.183
LINE	0.205	0.192	0.175	0.164
Node2vec	0.215	0.206	0.191	0.179
Struc2vec	0.228	0.216	0.211	0.190
GraphGAN	<b>0.232</b>	<b>0.221</b>	<b>0.213</b>	<b>0.194</b>

## Recommendation



(a) Precision@K



(b) Recall@K

Fig. 5: Precision@K and Recall@K on MovieLens-1M in recommendation.

# Summary

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- ❑ We propose **GraphGAN**, a novel framework that unifies generative and discriminative thinking for graph representation learning
  - ❑ Generator  $G(v|v_c)$  tries to fit  $p_{true}(v|v_c)$  as much as possible
  - ❑ Discriminator  $D(v, v_c)$  tries to tell whether an edge exists between  $v$  and  $v_c$
  
- ❑ G and D act as two players in a **minimax game**:
  - ❑ G tries to produce the most indistinguishable “fake” vertices under guidance provided by D
  - ❑ D tries to draw a clear line between the ground truth and “counterfeits” to avoid being fooled by G
  
- ❑ We propose **graph softmax** as the implementation of G
  - ❑ Graph softmax overcomes the limitations of softmax and hierarchical softmax
  - ❑ Graph softmax satisfies the properties of **normalization**, **graph structure awareness** and **computational efficiency**

# Outline

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## ❑ Introduction to graph representation learning

- ❑ Definition and application
- ❑ Taxonomy
- ❑ Representative work

## ❑ GraphGAN [AAAI 2018]

## ❑ GRL application

- ❑ Recommender systems [WWW 2018]
- ❑ Sentiment prediction [WSDM 2018]

# DKN (WWW 2018)

## ❑ DKN: Deep Knowledge-Aware Network for News Recommendation

- ❑ Learning knowledge graph representations by TransX
- ❑ A CNN framework for combining word embedding and entity embedding
- ❑ Attention-based CTR prediction

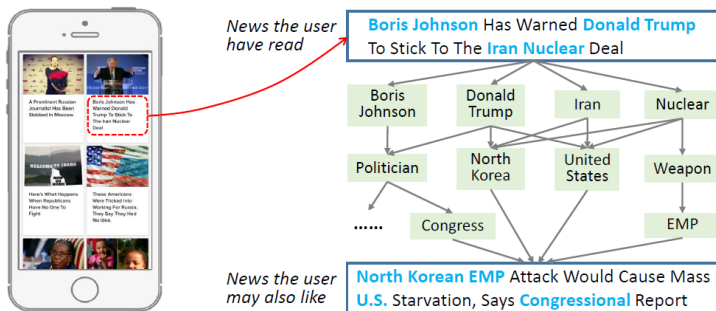


Fig. 1: Knowledge graph in news recommendation

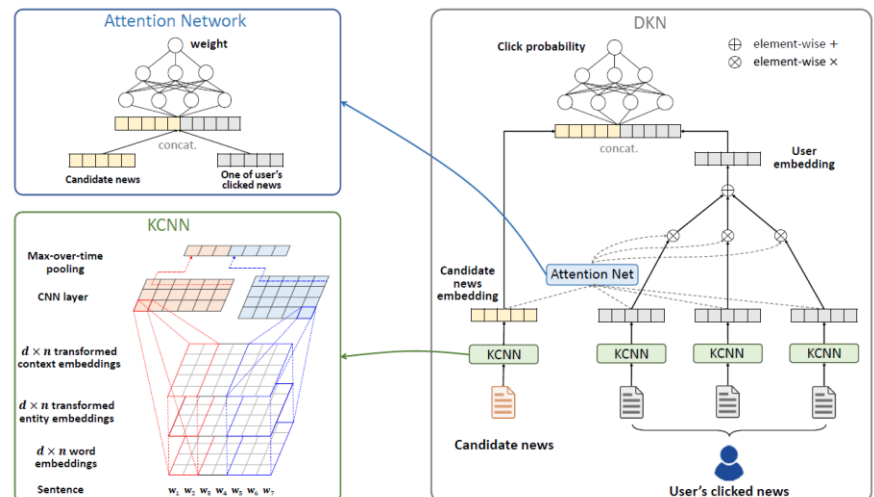


Fig. 2: DKN framework

# SHINE (WSDM 2018)

## SHINE: Signed Heterogeneous Information Network Embedding for Sentiment Link Prediction

- Sign: positive/negative sentiment link
- Heterogeneity: sentiment network, social network, knowledge graph
- Auto-encoder based framework

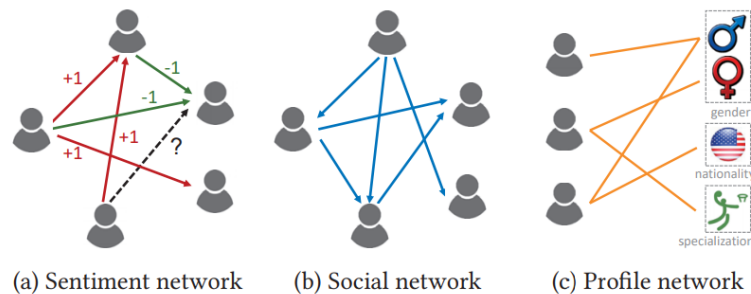


Fig. 1: Signed heterogeneous networks in sentiment prediction

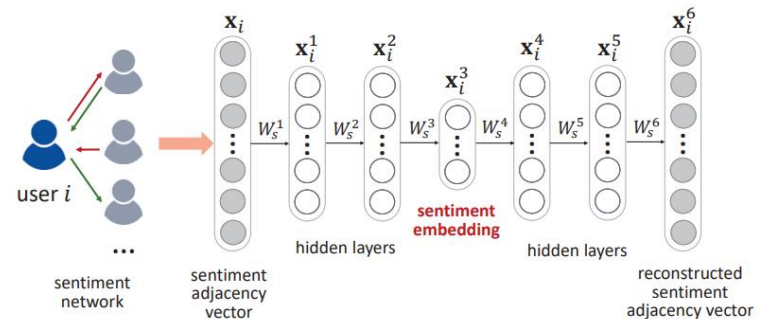


Fig. 2: Auto-encoder for sentiment network representation learning

# SHINE (WSDM 2018)

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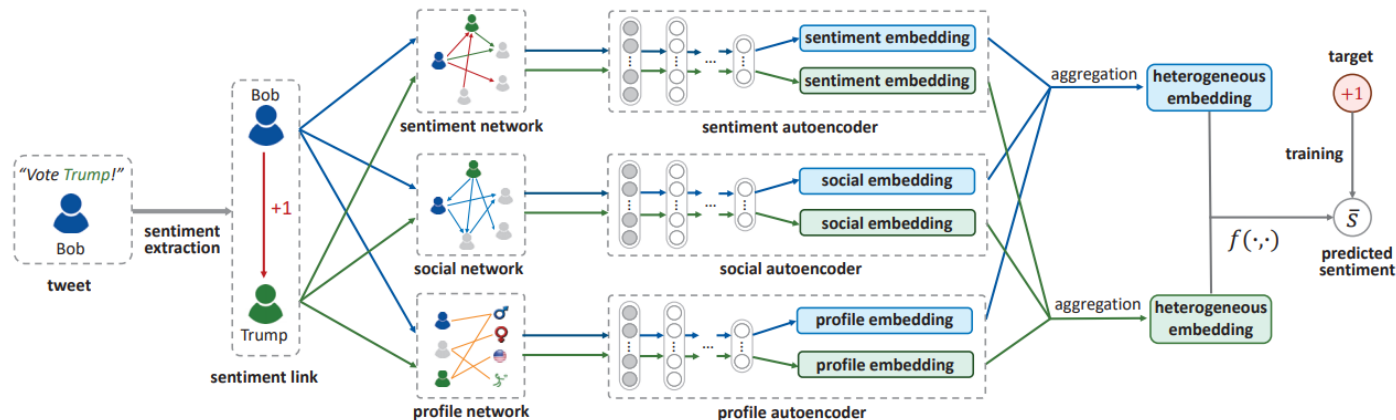


Fig. 3: SHINE framework



# Thanks!

Visit <https://hwwang55.github.io> for full papers, slides, code and more information