

$\|x\|_2 = \|y\|_2 = 1$, Encontrar Q Householder $\text{tg } Qx = y$

$$Q = I - \frac{2}{\|v\|_2^2} v v^t. \quad \text{Usamos } v = x - y$$

$$Qx = \left(I - \frac{2}{\|x-y\|_2^2} (x-y)(x-y)^t \right) x = x - \frac{2}{\|x-y\|_2^2} (x-y)(x-y)^t x =$$

$$\begin{aligned} x &= \frac{(x+y)}{2} + \frac{(x-y)}{2} \\ (x-y)^t (x+y) &= \|x\|_2^2 + x^t y \\ &\quad - y^t x - \|y\|_2^2 \\ &= 0 \end{aligned}$$

$$\begin{aligned} &= x - \frac{2}{\|x-y\|_2^2} (x-y) \left[\frac{(x-y)^t (x+y)}{2} \right] - \frac{2}{\|x-y\|_2^2} (x-y) \left[\frac{(x-y)^t (x-y)}{2} \right] = \\ &= x - (x-y) = y \end{aligned}$$