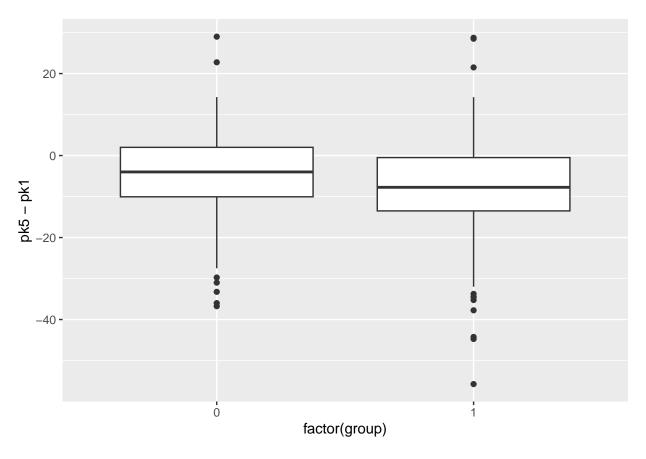
HUDM 6026 HW8

Getong Zhong(gz2338) & Ruoqiao Li(rl3288)

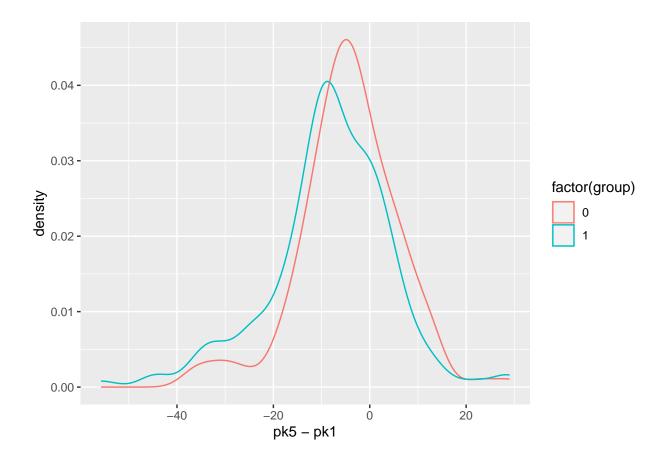
2023-03-27

1

```
data <- read.csv("D:/School/acupuncture.csv")</pre>
t.test(pk5-pk1 ~ group, data=data, val.equal = false)
##
## Welch Two Sample t-test
##
## data: pk5 - pk1 by group
## t = 2.9729, df = 297.94, p-value = 0.003191
\#\# alternative hypothesis: true difference in means between group 0 and group 1 is not equal to 0
## 95 percent confidence interval:
## 1.339278 6.584790
## sample estimates:
## mean in group 0 mean in group 1
##
        -4.367262
                      -8.329296
library(tidyverse)
## -- Attaching packages ------ tidyverse 1.3.2 --
## v ggplot2 3.4.0 v purrr 1.0.1
## v tibble 3.1.8 v stringr 1.5.0
## v tidyr
          1.2.1 v forcats 0.5.2
## v readr
          2.1.3
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
data %>% ggplot(aes(x = factor(group), y = pk5-pk1)) +
geom_boxplot()
```



```
data %>% ggplot(aes(x = pk5-pk1),) +
  geom_density(aes(color = factor(group)))
```



$\mathbf{2}$

We use mean difference between pk1 and pk5 as a non-standard test statistic.

3

```
data$diff_pk <- data$pk1 - data$pk5</pre>
pk1_diff <- data[data$group == 1, ]$diff_pk</pre>
pk5_diff <- data[data$group == 0, ]$diff_pk</pre>
observed_diff <- mean(pk1_diff) - mean(pk5_diff)</pre>
n <- 10000
permuted_diffs <- numeric(n)</pre>
sample(data$diff_pk)
     [1]
          17.00000
                      0.50000
                               26.25000
                                          25.00000
                                                       3.50000
                                                               -1.50000
                                                                           -5.50000
##
##
     [8]
          32.00000
                      5.50000
                                12.25000
                                           7.50000
                                                       8.75000
                                                                -8.75000
                                                                           -4.50000
    [15]
                      9.75000
                                 8.75000
                                                                -4.00000
##
           4.00000
                                            3.00000
                                                      2.50000
                                                                           10.25000
##
    [22]
          -3.25000 17.50000
                                 0.00000
                                           7.25000
                                                      5.00000
                                                                 4.00000
                                                                           11.75000
                                                                 2.50000
##
    [29] -28.73334
                     35.25000
                                17.50000
                                            9.75000
                                                       1.00000
                                                                            6.25000
##
    [36]
           0.50000
                      7.50000
                                 4.75000
                                            7.50000
                                                       6.50000
                                                                 0.66667
                                                                            7.00000
    [43]
          -4.00000 12.50000
                               33.25000
                                            2.50000
                                                      7.75000
                                                                 4.00000
                                                                            3.00000
##
```

```
##
    [50]
           4.75000
                      7.75000
                                -4.50000
                                           -2.00000
                                                      12.25000
                                                                  0.75000
                                                                            2.75000
##
    [57]
          13.25000
                      0.75000
                                -1.75000
                                           29.75000
                                                      -4.75000
                                                                10.50000
                                                                           14.75000
                                                      -2.50000
##
    [64] -10.50000 -12.25000 -10.00000
                                           36.00000
                                                                  3.00000
                                                                           -1.75000
    [71]
                      8.25000
                                 1.75000
                                           16.00000
                                                      -2.00000
                                                                  2.25000
##
          27.50000
                                                                           20.00000
##
    [78]
          13.75000
                      6.50000
                                12.00000
                                           27.50000
                                                     21.75000
                                                                20.75000
                                                                           -5.00000
    [85]
##
           5.75000
                     -1.50000
                                 3.50000
                                            4.00000 -12.50000
                                                                 5.50000
                                                                           18.25000
    [92]
##
          -8.75000
                      9.00000
                                 1.25000 -22.75000
                                                       2.00000
                                                                  7.25000
                                                                            5.50000
    [99]
##
           -7.50000
                     16.75000
                                 7.50000
                                           15.50000
                                                     10.00000
                                                                11.75000
                                                                            4.75000
##
   [106]
           0.50000
                      7.75000
                                 3.75000
                                           22.75000
                                                      10.25000
                                                                  2.00000
                                                                           -0.50000
##
   [113]
         -14.25000
                     13.00000
                                44.25000
                                           -2.00000
                                                      -6.75000
                                                                  1.00000
                                                                           -3.75000
   [120]
          18.00000
                      4.00000
                                11.00000
                                           11.25000
                                                       4.75000
                                                                  5.75000
                                                                           10.75000
   [127]
                                16.00000
                                            0.25000
                                                                -1.00000
##
           0.00000
                      6.50000
                                                      15.25000
                                                                           10.25000
##
   [134]
           7.25000
                      4.00000
                                17.25000
                                           34.50000
                                                      14.50000
                                                                -2.25000
                                                                           11.75000
                      0.00000
##
   [141]
           2.25000
                                 8.25000 -12.25000
                                                      -2.25000
                                                                -3.75000
                                                                           -2.75000
## [148] -14.25000
                     15.75000
                                -5.25000
                                           12.75000 -21.50000
                                                                23.00000
                                                                           -7.00000
   [155]
           15.25000
                     10.00000
                                -5.75000
                                           -1.75000
                                                      -2.00000
                                                                12.25000
                                                                           -5.00000
##
   [162]
          -5.25000
                     19.00000
                                -2.25000
                                            1.50000
                                                       9.50000
                                                                 0.00000
                                                                           -0.75000
##
   [169]
          -5.25000
                     -0.75000
                                 8.75000
                                            8.75000
                                                      14.50000
                                                                  7.75000
                                                                            0.25000
##
   [176]
                      4.50000
                                12.00000
                                            7.25000
          12.25000
                                                     20.75000
                                                                17.25000
                                                                           12.50000
##
   [183]
          -9.25000
                      6.50000
                                 3.75000
                                           11.50000
                                                      4.00000
                                                                12.25000
                                                                           10.75000
## [190]
          -6.50000
                     -8.25000
                                 7.25000
                                           13.25000
                                                      10.25000
                                                                 3.50000
                                                                            1.00000
## [197]
          31.00000
                      5.00000
                                -7.75000 -10.50000
                                                      18.00000
                                                                13.50000
                                                                            9.50000
## [204]
           3.00000
                      8.75000
                                -5.00000
                                           -0.50000
                                                       5.75000
                                                                55.75000
                                                                           18.25000
## [211]
                                                     -4.50000
           7.25000
                     -8.25000
                                25.25000
                                           -3.25000
                                                                13.00000
                                                                            8.00000
## [218]
           7.75000
                     -6.50000 -10.75000
                                           29.75000
                                                     31.25000
                                                                44.75000
                                                                            7.00000
  [225]
           6.25000
                      7.50000
                                33.75000
                                            2.50000
                                                      24.75000
                                                                10.00000
                                                                           -7.75000
   [232]
           -0.75000
                     -5.00000
                                25.50000
                                           10.25000
                                                                -7.75000
##
                                                       2.00000
                                                                           16.25000
  [239]
                                 2.00000
##
         -11.75000
                     34.50000
                                           16.00000
                                                       1.00000
                                                                 9.75000
                                                                           11.75000
## [246]
                      4.00000
                                 0.00000
                                            6.50000
                                                       0.75000
                                                                  6.50000
           1.25000
                                                                            6.00000
## [253]
           7.25000
                      9.75000
                                13.75000
                                            9.50000
                                                       1.25000
                                                                11.50000
                                                                            8.00000
## [260]
           11.25000
                      8.75000
                                11.75000
                                           13.50000 -29.00000
                                                                10.25000
                                                                           -6.50000
##
  [267]
           8.00000
                     11.25000
                                 8.00000
                                            7.25000
                                                     37.75000
                                                                 5.50000
                                                                           -2.25000
##
   [274]
           5.75000
                     -3.50000
                                -0.25000
                                           10.50000 -13.75000
                                                                24.50000
                                                                            3.00000
   [281]
##
           8.00000
                     -5.00000
                                36.75000
                                            4.75000 -28.50000
                                                                22.50000
                                                                            4.75000
   [288]
           8.75000
                     18.00000
                                10.75000
                                            1.00000
                                                       9.75000
                                                                 -2.00000
                                                                          -13.25000
##
  [295]
                     31.00000
                                14.00000 -12.75000
                                                       7.25000
                                                                  2.50000
##
          -3.25000
                                                                            3.50000
set.seed(123)
for (i in 1:n) {
  sample_dat <- sample(data$diff_pk)</pre>
  permuted_diffs[i] <- mean(sample_dat[data$group == 1]) - mean(sample_dat[data$group == 0])</pre>
}
```

P value

```
p_value <- sum(abs(permuted_diffs) >= abs(observed_diff))/n
p_value
```

[1] 0.0032