

DYNAMIC FORMATION CONTROL WITH HETEROGENOUS MOBILE  
ROBOTS

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# ABSTRACT

## DYNAMIC FORMATION CONTROL WITH HETEROGENOUS MOBILE ROBOTS

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Formation control in robotics is a growing topic where mainly research works are geared towards heterogenous swarm colonies under decentralized control or heterogenous colonies where some centralization is considered. In swarm works where decentralization is applied, it is nevertheless assumed that the agents are capable of getting global information about the whole swarm. Moreover in the literature, formation control is generally done for known fixed shapes that can be defined mathematically. However no dynamically changing shapes are envisaged and no shape transitions are clearly handled in those works. We attempt to bring a clear impact to the literature by focusing our thesis work on tracking and realising formation shapes under dynamically changing formation shape demands. Furthermore, in our thesis work, we focus on robot colonies composed of heterogeneous robots of different dynamics and sensory capabilities under decentralized dynamically changing formation control. These robots are able furthermore, to just possess local mutual interactions only with their closeby neighboring agents. Using communications with those neighbors, all agents are being able to acquire graph theoretically, information about the whole colony. Simulations in our work will be generated using the Gazebo environment modeling a rough territory. Hardware applications of our approach will also be developed.

Keywords: Multi Agent Systems, Formation Control, Localization, Mesh Network

# ÖZ

## HETEROJEN ROBOTLARLA DİNAMİK FORMASYON KONTROLÜ

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Formasyon kontrolü robotik alanında heterojen robot kolonilerinin merkezi yönetici birimler olmadan ya da yerel merkezi birimleri barındıran topolojilerle kontrolü konularına yönelik büyüyen bir araştırma alanıdır. Merkezi yönetim birimlerinin olmadığı robot sürüsü çalışmalarında ne yazık ki her üyenin, koloniye mensup diğer üyelerin tüm verilerine erişebildiği varsayımı yapılmaktadır. Öte yandan, literatürde formasyon kontrolü genellikle matematiksel olarak ifade edilebilen basit geometrik şekillerle yapılmaktadır. Bununla birlikte bu çalışmalarda, dinamik olarak değişen şekiller ve bu şekiller arasında formasyon geçişleri konusu yeterli olarak ele alınmamaktadır. Bu çalışma kapsamında dinamik olarak değişen şekiller için formasyon kontrolü sağlayarak literatüre katkıda bulunmayı hedefliyoruz. Öte yandan bu tez çalışmamızda, farklı dinamiklere ve sensör yetkinliklerine sahip heterojen robot kolonileri kullanarak dinamik formasyon kontrolü problemini merkezi karar verici birimlerin olmadığı bir topolojide ele alacağız. Çalışma kapsamında ele alınan kolonilerdeki tüm robotlar yalnızca kendilerine en yakın komşu üyelerle yerel etkileşimlerde bulunabileceklerdir. Komşularıyla etkileşimde bulunan üyeler, konsensus koordinat sistemi ve koloninin geri kalanı hakkında bilgi sahibi olabileceklerdir. Çalışmamız kapsamında simülasyonlar Gazebo ortamında üç boyutlu düzgün olmayan araziler modellenerek yapılacaktır. Ayrıca donanımsal gerçeklemeler içeren çalışmalar da yapılacaktır.

Anahtar Kelimeler: Çok Elemanlı Sistemler, Formasyon Kontrolü, Konumlama, Örgün Ağlar



*To my family and people who are reading this page*

## ACKNOWLEDGMENTS

TODO

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## **LIST OF ABBREVIATIONS**

ABBRV	Abbreviation
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# **CHAPTER 1**

## **INTRODUCTION**

In this thesis work, it is aimed to create a novel method for formation control of a swarm which consists of heterogenous mobile robots. The term of swarm represents a large group of locally interacting individuals with common goals[4].

Self organizing swarm researches and its applications are generally inspired by the biological systems in the nature. The behaviours of these biological systems were considered mysterious and strange for a long time, but recent researches show that individuals don't need any sophisticated knowledge or top level functionalities to produce such complex tasks[2] . These biological systems (e.g. colony of ants) have simple behaviours but they can accomplish very complicated collective tasks in the nature which are impossible with their own individual capabilities. Beni [1] describes this collaboration of members as follows:

The group of robots is not just a group. It has some special characteristics, which are found in swarms of insects, that is, decentralised control, lack of synchronisation, simple and (quasi) identical members.

It is obvious that such a collective behaviour of these swarms has more power and efficiency than the sum of the individual capabilities of the members.

General aspects of the swarm robotics systems are the simplicity of individuals, restricted sensing and communication capabilities, achieving tasks mutually, robustness and decentralized control capability[6].

Swarm robotics has been studied to produce different collective behaviors to solve

tasks such as aggregation, pattern formation, self-assembly and morphogenesis, object clustering, assembling and construction, collective search&rescue and exploration, coordinated motion, collective transportation, self-deployment, foraging and others[5]. Dorigo and Trianni[7] are studied on controllers for aggregation of coordinated motion of the identical mobile robots called swarm-bots. Hou, S.P., C.C. Cheah, and J.J.E. Slotine is focused on controlling of a swarm within a dynamically changing formation[8]. Ganesh and Lisa introduced two new strategies for collective search and exploration of fields with swarm intelligence[9]. Chaimowicz and Campos proposed a new methodology which is based on a dynamic role assignment mechanism in which the robots cooperate with each other and they demonstrate this method in a cooperative transportation task[10]. Campo and Gutierrez is studied on collective foraging task and they propose a method for path selection to optimize the profits of the swarm[11].

There are lots of studies related with different problems in swarm robotics literature as discussed briefly. In this thesis project, we are focused on dynamic pattern formation control of swarms consist of heterogeneous robots.

## **1.1 Problem Definition**

In this thesis work, the main idea is to propose a complete design solution to a dynamically changing formation system, including a local positioning system and formation control system. The swarm which is used in this formation system is assumed to be composed of heterogenous agents which have different functionalities and physical properties. The formation shape is expected to be closed contours which cannot be identified with analytical expressions and these shapes will be changing dynamically with a continuous manner.

Formation control system is heavily depend on the position data of individual agents in the environment. Since it is expected to have high number of agents in the environment due to the nature of a swarm, the agents are assumed to have simple structures with low capabilities including lack of certain types of sensors. On the other hand, for indoor applications it will not be possible to use satellite dependent positioning

systems on agents. Even if a positioning solution depending on different methods including visual feedback(by image processing), RSS(received signal strength) etc. is available for an indoor application, it is not possible to implement this solution for each single agent in the environment due to the increasing complexity and the costs by the number of agents. As a result of these constraints, it is required to implement a localization solution for the agents to provide the corrected positions in the workspace to be used by the formation control system. This localization process have to correct the position data of the agents with the determined process period and within an maximum error bound which will be determined by the requirements of the formation control problem.

Formation control system have to provide a solution to the coverage of a dynamically changing formation shape by the agents in the swarm. Desired formation shapes will not be simple geometrical shapes like circles, triangles etc. Heterogenous agents with different shapes have to cover the instant formation shape homogenously as possible as. The total displacements of the agents while travelling towards the desired formation have to be minimized. In other words, agents have to adapt the new formation shape with minimum possible movement. On the other hand, collision avoidance with the obstacles in the workspace and with the other agents has to be provided while achieving different types of formation tasks. Each agent must execute its own controller-decision making algorithms in a decentralized manner.

## **1.2 Motivation**

The formation control problem can be defined as collaboration of a group of agent to maintain a formation with a certain shape [12]. It focuses on leading the individual agents of a swarm to perform collective tasks including shape generation and formation reconfiguration while traversing a trajectory by providing collision avoidance simultaneously. These kind of tasks are achieved with a large group of small and simple robots that can cooperate with each other. Formation control of multi agent systems is an actively growing research field.

Swarms which are used in formation control systems, can be composed of homoge-

nous or heterogenous agents according to the requirements of the problem. The usage of the homogenous agents increases the total energy and the coverage of the system in the environment. This kind of a swarm has an increased redundancy and is capable of resuming the current task in case of failures of some of the agents during mission. On the other hand, a swarm composed of heterogeonus agents holds the different capabilities of the agents. This kind of a system can be used in tasks which requires different functionalities has to be performed individually or simultaneously.

In real world applications there may be need for different functionalities to achieve some specific tasks. If this is the case, one solution may be to design a sophisticated robot which includes all required capabilities for this task. In this scenario, this robot will be the single point of failure in the system and if robustness is a vital feature for this solution, some redundant robots have to be added to the system. It is clear that the design of such an advanced robot and hold its redundant backups in the system will increase the cost of the solution. In swarm robotics concept, one of the approaches related with the usage of the heterogenous agents is to gather some different types of simple mobile robots which have their own specific functionalities to achieve a collective task rather than designing an advanced robot for the solution. With this approach, the robustness of the system is increased, costs are reduced down and the reusability of the individual members of the swarm for other tasks is provided. A project named Swarmanoid which is funded by European Commission, has an objective to implement and control of a novel distributed robotic system. The system is designed with heterogeneous, dynamically connected, small autonomous robots called, foot-bots , hand-bots and eye-bots where foot-bots are responsible to transport the required materials(including other types of robots) to a specific task area and foot-bots are responsible for operations with their manipulators and eye-bots are responsible of observations and reconnaissance on the area.

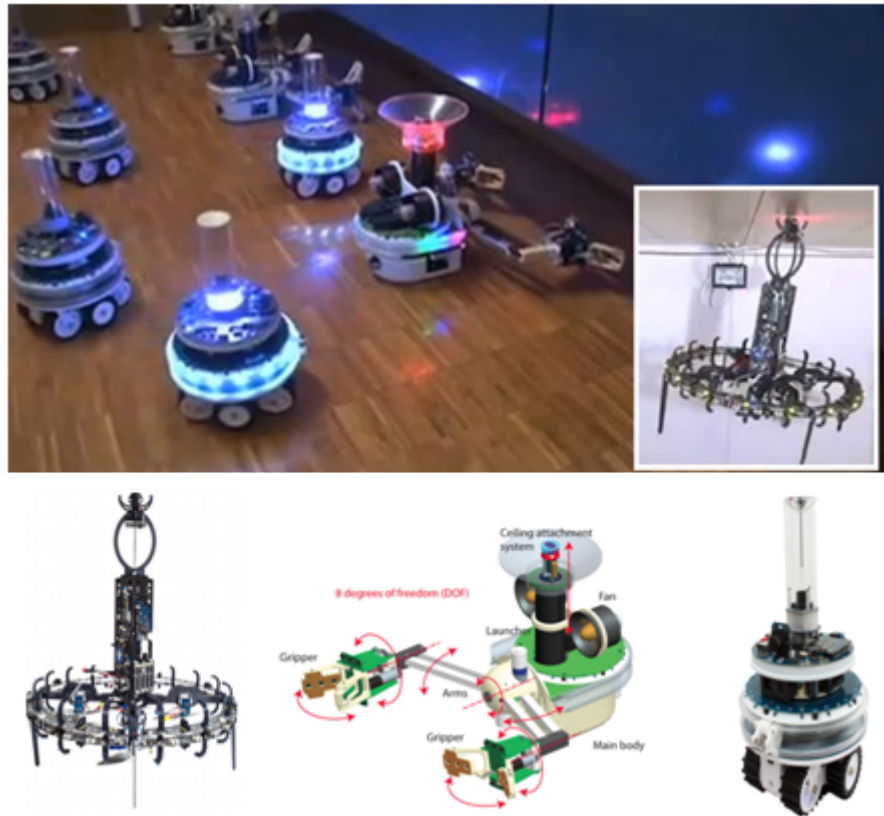


Figure 1.1: A Robot Team Consists of Eyebot, Handbot and Footbot Agents

A swarm which is composed with same type of homogenous agents can be used to increase the total impact and the energy of an individual agent. This kind of a system can be used in missions like coverage, search and reconnaissance etc. Martin and Kilberg have worked on formation control and formation tracking of microsattellites to achieve continous coverage and improved capability. They also mentioned that small formations will reduce the fuel consumption for propulsion and expand the sensing capabilities of microsattellites[15].

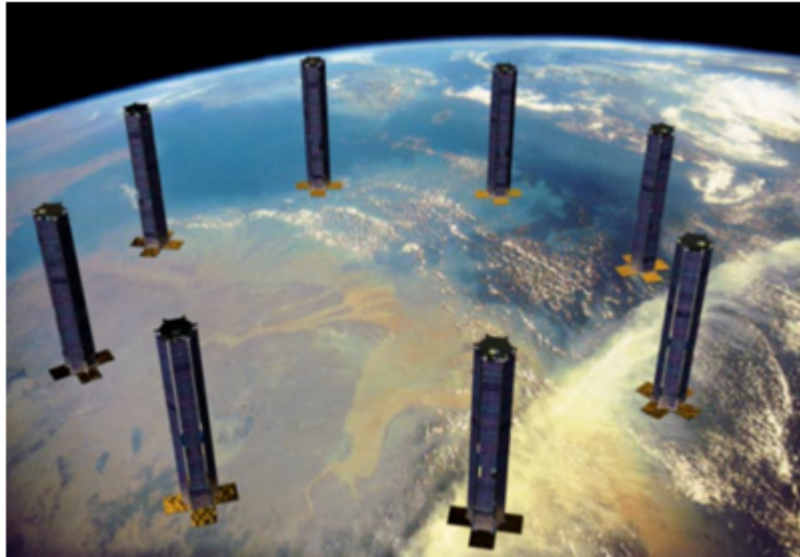


Figure 1.2: Sparse Aperture Formation of Micro Satellites

Formation control solutions has lots of usage areas such as coverage missions, security patrols and search&rescue in hazardous environments etc.[13]. For missions related with area coverage and reconnaissance, a group of autonomous vehicles may be required to keep in a specified formation [13]. Balch and Arkin presented a behaviour based formation control for multi robot teams which is implemented on a team of robotic scout vehicles manufactured for a DARPA project[14].



Figure 1.3: A Team of Four Robotic Scout Vehicles on which Formation Control Techniques Implemented

There are some hardware implementations to test the related formation control algorithms in real time applications. Since the formation control problem requires lots

of agents in a swarm, these works have a common point of providing agents with minimal costs and sensor capabilities. The Kilobot Project from Harvard university have released their agents with the name of Kilobots and they have teams which are working on different formation control problems with Kilobots.

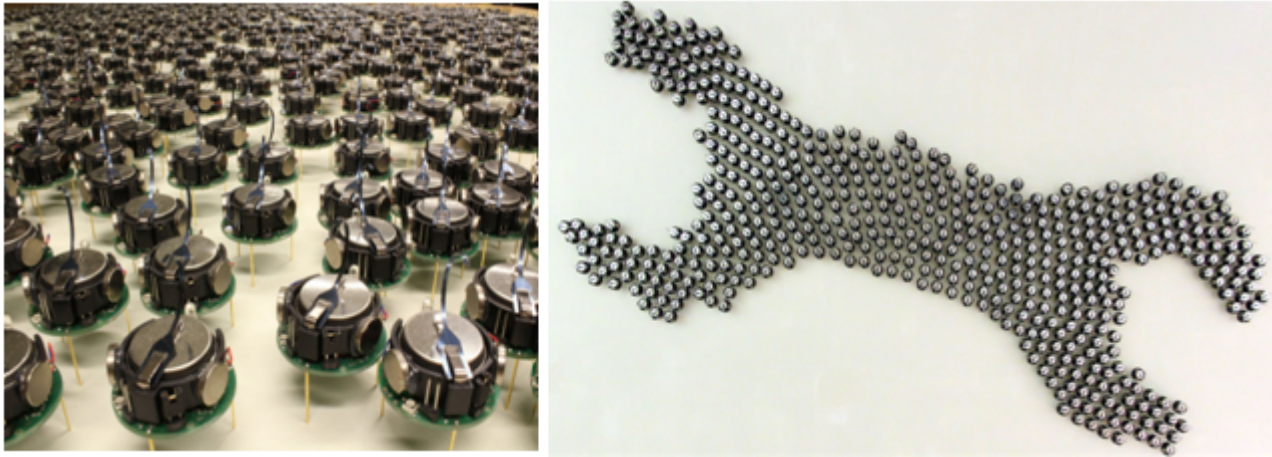


Figure 1.4: Formation Control with Kilobots

These micro robots have a great reusability for different types of formation control problems and they have biological insprations from the nature in the sense of individual simplicity and power of collective behaviors.



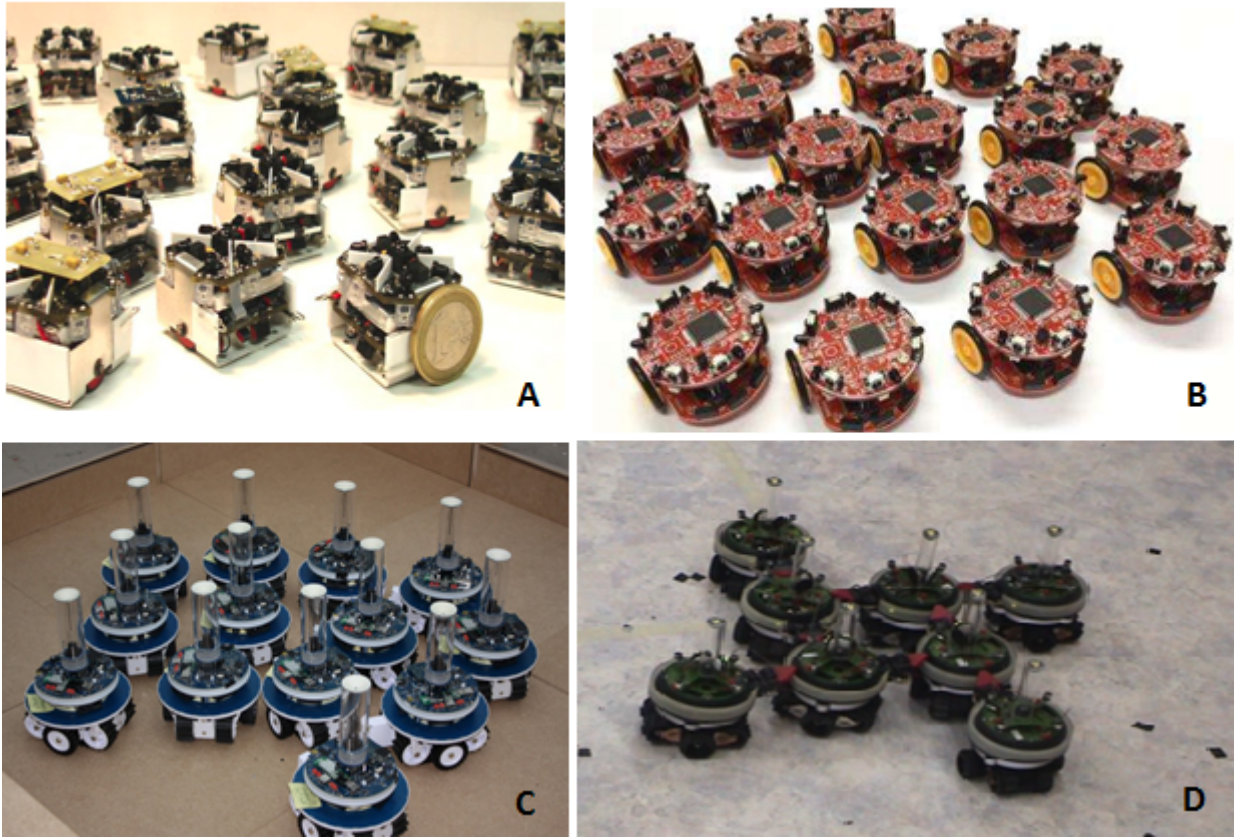


Figure 1.5: A) Swarm Robot Project from Universities of Stuttgart  
 B) Colias Project from University of Lincoln and Tsinghua University in China  
 C) Marx bot developed at EPFL  
 D) Swarm bots project conducted by European Commission

### 1.3 Objectives

In this thesis work, our aim is to provide different approaches & solutions to the requirements in formation control problem. There are mainly different types of infrastructures while providing a global solution to the formation control problem like the heterogeneity vs. homogeneity of the agents, communication structures, centralized vs. decentralized structures, swarm control strategies like behavior based and leader-following approaches or virtual structure based approaches.

In addition to choice of the formation control infrastructures, capabilities of the in-



dividual agents provide additional requirements and constraints while designing a formation control system. One of the most important characteristic of an agent in the swarm is its simplicity and limited sensor & communication capability. This approach results from the idea of achieving collective tasks with lots of simple individuals and it is based on biological inspirations in nature like colony of ants etc.

In this project the defined requirements and objectives are given as follows;

### 1.3.1 Heterogenous Robots with Different Dynamics

Agents have different dynamics from each other like different friction surfaces, geometrical structures and functionalities. They have different volumes and masses(not mass point particles) and they may collide with the other ones and the obstacles in the environment.



Figure 1.6: Heterogenous Agents with Different Physical Properties and Functionalities

### 1.3.2 Communication Infrastructure

Agents in the swarm have limited communication capabilities and can only negotiate with its local neighbors in a narrow line of sight range due to power consumption issues and their weak radio links.



Figure 1.7: Radio Links on Agents Have a Narrow LOS Range

a)Communication Topology Communication topology is a wireless mesh network in which each agent relays data for the rest of the network. The network is fully connected and has routing technique where the data is propagated along a route by transporting over the nodes(member agents of the swarm).

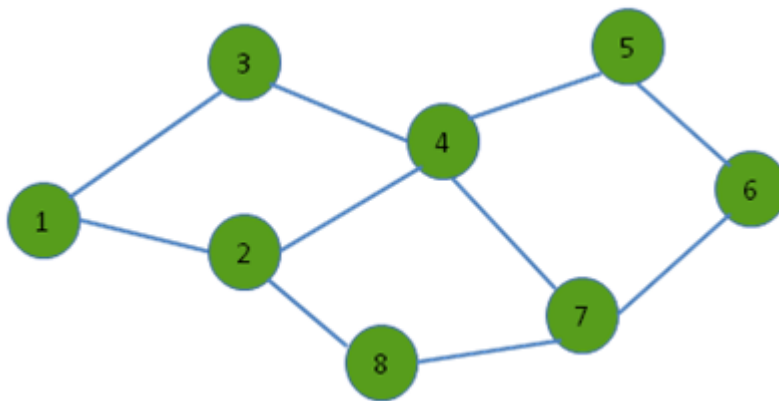


Figure 1.8: Mesh Network Between Agents

b)Communication Bandwidth Bandwidth of the communication between agents is limited and nodes can only transport most critical data like heartbeats, agent IDs, type and position etc.

### 1.3.3 Decentralized Decision Making Process

Centralized formation controller systems implement a single controller server/root node to process all the data needed to achieve the desired control objectives. This type of systems achieve superior performance and optimal decisions but they require high computational power, high communication bandwidths and are not robust due to dependence on a single controller[12]. Decentralized formation controller structures have agents which are completely autonomous and responsible their own individual decisions. In this work, a hybrid centralized/decentralized controller architecture in which there is a central manager which partitions the desired formation shapes into goal states and there are independent agents who make their own choices on these goal states to reach as unaware of the other agents' choices.

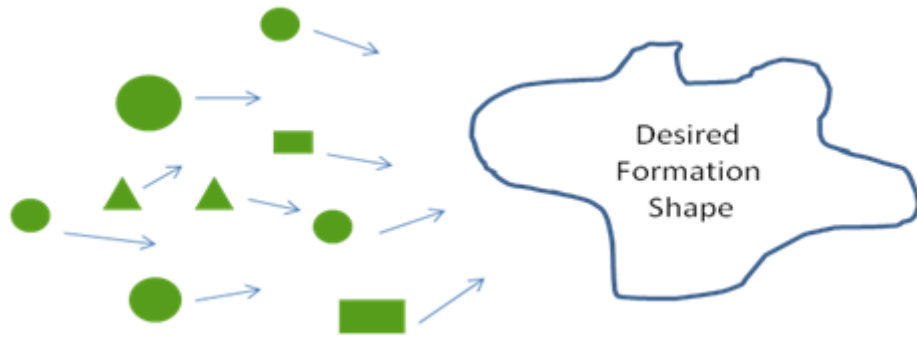


Figure 1.9: Agents make their own choices about target goal states

### 1.3.4 Complex Closed Contours

Formation shapes will be defined as closed curves with complex shapes and they cannot be identified analytically. On the other hand shapes will be changing dynamically during formation control.

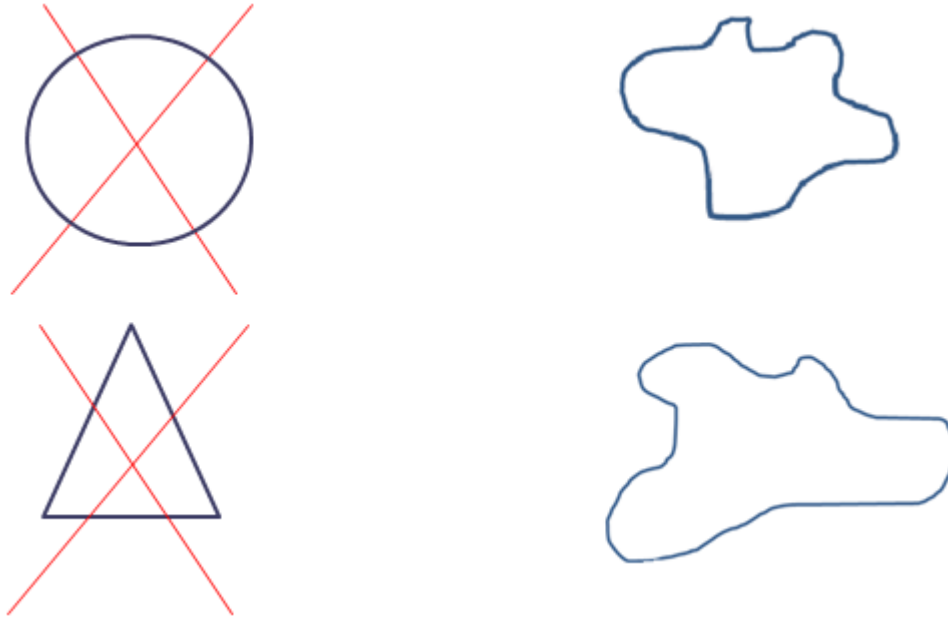


Figure 1.10: Complex and Dynamically Changing Formation Shapes

### 1.3.5 Simple Agents with Low Sensor Capabilities and Low Computing Powers

Agents in the swarm are assumed to have low sensor capabilities and weak computing power. This condition must be taken into account during the control system design, since individuals do not have a high resolution and sensitive data about their state vectors, and they cannot execute high level complex control algorithms.

## 1.4 Goals

The objectives and the assumptions about the requirements define the goals of this thesis project. The goals of the project are listed in the following section.

1. Agents have to propagate their position and velocity states with the help of inertial measurements. This process is handled with a Kalman estimator which takes the translational acceleration data as an input to the observer model. The translational acceleration data is calculated with the help of AHRS system composed by 3 axis accelerometers, gyroscopes and magnetometers.
2. Agents have to update&adjust the position data with the help of agents which have

positioning sensors(position beacons) by local trilaterations. This position data is used in the internal estimator systems as external measurements to correct the drifts caused by propagation error of translational accelerations. The ordering for this trilateration process have to be determined appropriately to minimize the error on calculated position data of agents which are far away from the position beacons.

3. Agents have to update their route tables to create a communication backbone with the mesh network topology. Since agents are assumed to have low range&bandwidth radio links, the propagation of a data between each agent in the swarm will be handled over this mesh network.

4. Agents have to determine the goal states in the desired complex formation shape to cover with the help of a central server. Desired formation shape will be partitioned into potential goal states assigned to different types of agents. Performance analysis on proposed shape partitioning methods have to be done with some different criterias.

5. Assignment of the agents to their target goal states should be handled to minimize the total displacement of the agents while travelling towards the desired formation shape.

6. Simulations should be performed to compare the efficiency of different methods proposed in this thesis work. Different types of agents have to be represented with different dynamical and physical models during simulations.

7. Hardware demonstrations should be performed to illustrate the applicability of the proposed solution in real time systems. These applications may not contain the full implementation of the proposed system, but they must demonstrate the proof of concept(POC) environment.

## **1.5 Methodology**

During the first part of the project, a local positioning system(LPS) is designed. In this system, agents which does not have position sensors propagate their position and velocity states with their inertial measurements. Due to the bias and drift errors on this solution a position update&adjust process is handled on 0.33Hz frequency

with the help of position beacons which are agents with position sensors on board in the swarm. During the update phase of the solution route tables for individual agents are determined with the help of Graph Theory based Destination-Sequenced Distance Vector Routing Protocol (DSDV) algorithms. This process provides the required information to compose the clusters around position beacons and provides rank information for the agents which are in same clusters. Position measurements are handled with local trilateration process in a turn with the rank values for every agent around each clusters after the establishment of route tables. A Kalman estimator system is designed to fuse these propagation and update phases of the solution.

On the second part of the thesis work, formation controller system is designed with two novel methods based on bubble packing methods and randomized fractals method. Desired complex formation shapes are partitioned into goal states according to the heterogeneous agents in the swarm for both of these two methods. Decision process of the agents about their target goal states to optimize the overall utility of the swarm is implemented with the help of Visibility Graphs and Hungarian algorithms. Internal velocity controllers for individual agents to reach the desired target goal states by providing obstacle avoidance, are implemented with a full state feedback method by regulating the augmented dynamical system with the gains optimized by Linear Quadratic Regulators (LQR).

## **1.6 Contribution of Thesis**

The main contributions of thesis are:

1. Designing a local positioning system(LPS) based on local trilaterations to provide a high accuracy position data to the agents which do not have a specific position sensors on their boards.
2. Implementing a wireless mesh network between agents in the swarm and design a communication infrastructure and related routing algorithms to exchange the local data globally in the network
3. Partitioning the complex formation shapes into goal states to cover the whole

formation homogenously with the different types of heterogenous agents.

4. Designing and implement the rules&algorithms for the decision process of the individual agents about the goal states to reach.

5. Designing a simulation environment to test the proposals and algorithms of this thesis work

6. Designing a simple demonstrative hardware application.

## **1.7 Outline of the Thesis**

This thesis work is organized into 5 main sections .Chapter 1 introduces the main theme and the potential areas of the usage of formation control, while specifying our motivation and the requirements&problems to meet&solve related with the topic.

Chapter 2 gives literature reviews about the related works and basic mathematical background on the methods used in this paper.

Chapter 3 introduces the methods and solutions used in two different parts of the problem; local positioning system and formation conroller system. In this chapter, routing algorithms and mathematical aspects of the trilateration process is introduced. Methods&algorithms used for formation control is discussed in details.

Chapter 4 provides simulation analysis on the local positioning system and gives mutual evaluations of the performances of different methods used in formation control system.

Chapter 5 provides and discuss the details of hardware implementations and the experimental results.

Chapter 6 concludes the thesis and defines the future works related with the thesis.





## **CHAPTER 2**

### **LITERATURE SURVEY**

This chapter focuses on the related works on local positioning systems and formation control systems.

#### **2.1 Local Positioning Systems**

Positioning systems fall in to two main branches, global positioning systems and local positioning systems. Global positioning systems(GPS) has become increasingly popular for a couple of last decades for tracking location. It is a precise system depends on satellite based positioning mainly developed for direction finding and navigation. Some of the problems encountered with the usage of GPS systems: (1) the signal from the satellites cannot penetrate to the indoor space so it doesn't perform in such areas, (2) it loses its precision in rich scattering environments such as urban areas[19]. A local positioning system can provide a position information where GPS systems are unavailable, with the usage of signaling beacons which are placed at the exactly known locations.

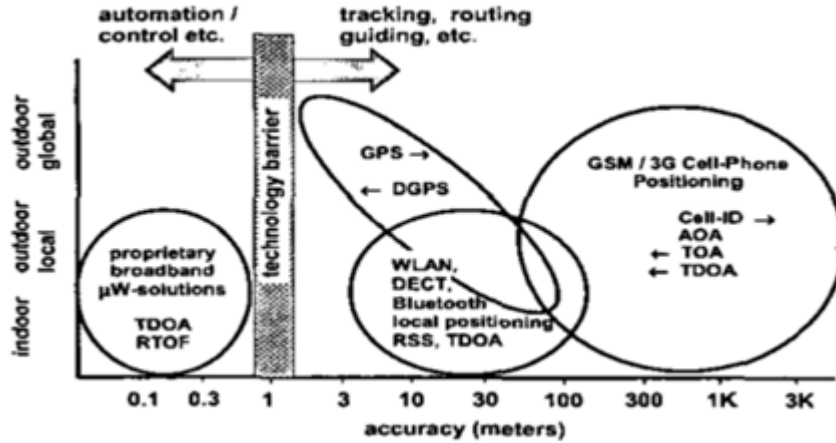


Figure 2.1: Accuracy Statistics of Different Positioning Sources

Figure xx represents an overview of current positioning systems. Global positioning systems are widely used nowadays and they provide accuracies in the range of 3-30 meters, they can operate outdoor environments with the necessity of radio signals from satellites. Differential GPS systems decrease these accuracy range below 3 meters with the help of additional local static beacons. GSM based solutions have the worst accuracy performance, but they can perform in indoor environments partially. Local positioning systems have the capability of working indoor environments and they have a wide accuracy range changing with respect to the implemented topologies and methods.

Local positioning systems has different system topologies illustrated in the Table 1[20].

Table 2.1: Local Positioning Systems with Different System Topologies

Concept	Concept Definition
Remote Positioning	Measurement from remote site to mobile device
Self Positioning	Measurement from mobile unit to usually fixed transponders(landmarks)
Indirect remote positioning	Self positioning system with data transfer of measuring result to remote site
Indirect self positioning	Remote positioning system with data transfer of measuring result to mobile unit

Two main topologies are self positioning and remote positioning systems[20]. In self positioning system a mobile device finds its own position with the help of a reference like a starting point or a beacon node with exactly known positions. On the other hand, in remote positioning systems a mobile node locates other objects positions with respect to its own position[19]. These two type of topologies can be converted to each other with the help of a communications structures integrated on the devices to share the result of position measurement and thus indirect remote positioning and indirect self positioning system topologies can be implemented.

### **2.1.1 Measurement Principles**

Angle of arrival (AOA), received signal strength(RSS) and propogation-time based systems are commonly used as three different measurement techniques used in local positioning systems.

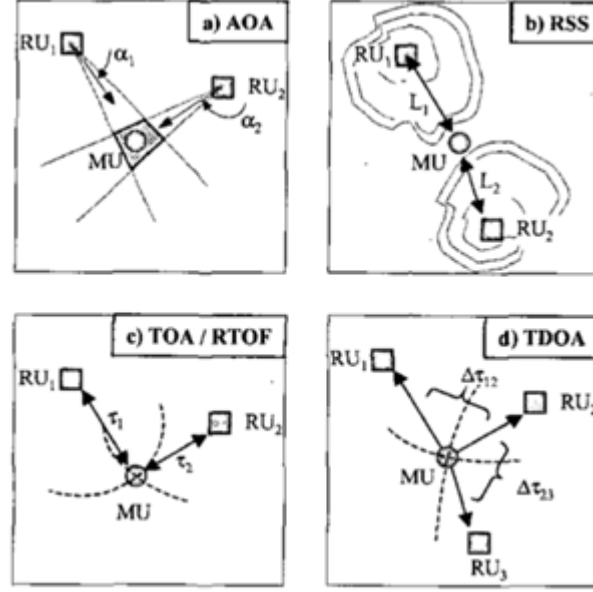


Figure 2.2: Different Measurement Principles

In Angle-of-arrival (AOA) systems use directional antennas to measure the bearing and the angle to the points located at known positions are measured. The position value of device can be calculated with the intersection of several measurement, but the accuracy is limited by shadowing and multipath reflections of radio signals.

Received signal strength(RSS) systems calculate the distance value by taking the difference of the received signal power from the transmitted power. Some advanced propagation models are required to calculate the distance from the transmission loss in the air to eliminate the multipath fading and shadowing effects[21] .

Time based systems calculates the distance between measuring unit and signal transmitter with the help of propagation time like used in the global positioning systems generally. This process requires a perfect time synchronization between the mobile and stationary units[20].

In this thesis work, we implement a self positioning system in which every agent localize itself with the help of position beacons in the swarm with exactly known positions. The distance from the agents to these beacons in the swarm are assumed to be calculated with the help of a range sensor like a ultrasonic or a lidar sensor.

### 2.1.2 Trilateration Process

Trilateration process determine the three dimensional coordinates of unknown positions with the help of distance measurement to known position [22]. It is widely used in wireless sensor network topologies and local positioning systems. In theory, it is needed to have at least four beacon nodes to calculate an unknown position in 3D, and at least three beacon nodes to calculate an unknown position in 2D environment. But these worst case numbers are generally not sufficient to estimate an unknown position with a good accuracy due to errors on range calculations and synchronization problems. Figure -xx demonstrates a simple trilateration procees in 2D environment with the help of three position beacons. Suppose a mobile device which tries to estimate its position with the local positioning systems is at the red point in the figure. If it can measure its distance to the beacons named A,B and C with exactly known positions, it will be possible to estimate the unknown position of this mobile device with the same approach used in global positioning systems.

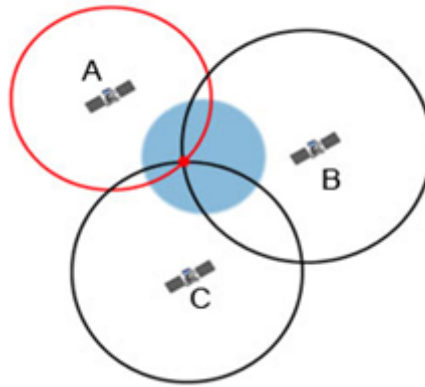


Figure 2.3: Trilateration Process

## 2.2 Formation Control Systems

Formation control problem have different subproblems like formation shape generation, formation reconfiguration and selection and formation tracking [12]. In formation shape generation agents are expected to get a formation shape which can be defined by externally or with some mathematical constraint functions[16]. One gen-

eral approach is to consider some artificial potential functions. Samitha and Pubudu have presented an artificial potential function based method by considering the problem as controlling and positioning of a swarm into a shape bounded by a simple closed contour in the complex plane while spreading members inside the contour uniformly. They provide analysis about the stability and robustness of their systems with the help of Lyapunov like functions[17].

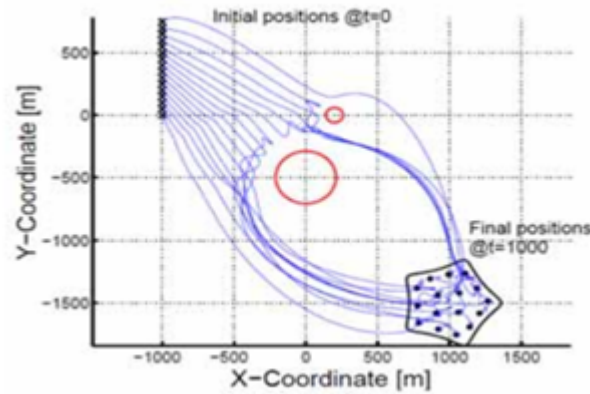


Figure 2.4: Motions and formation of the agents in presence of obstacles[17]

In some applications, it may be needed to change the formation shape or splitting and joining of the agents together due to either a change in coordinated task requirements or change in environmental conditions such as narrow corridors. This task requires formation reconfiguration and selections capabilities for the swarms. Hou and Slotine have defined a method based on global objective functions to provide formation control of a swarm. In their approach it is possible to implement scaling and rotating functions into control laws[8].

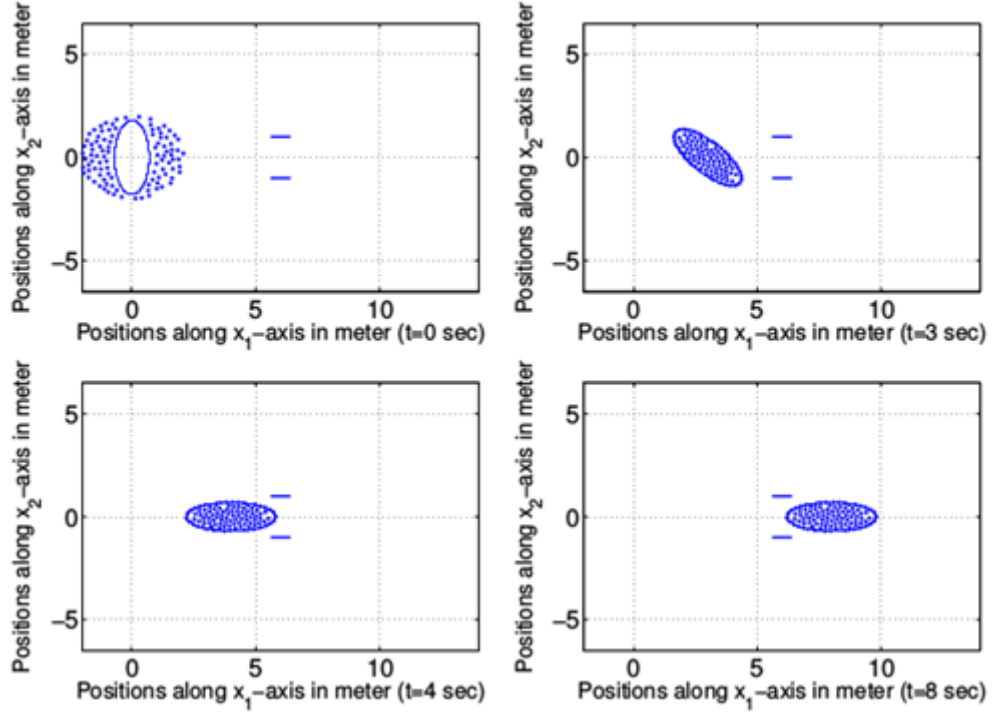


Figure 2.5: A group of 100 robots in a rotating rotating and scaling ellipse formation[8]

One of the subproblems studied in formation control is formation tracking. The main objective of this problem is to maintain a desired formation with a group of robots, while tracking or following a reference trajectory. The most general strategy to provide a solution for this problem is leader-following swarm structures. Other strategies have a basis on optimization and graph theory approaches[12]. Kumar, Fierro and Das proposed a vision based formation control framework for this problem. This framework has a leader following background [18].

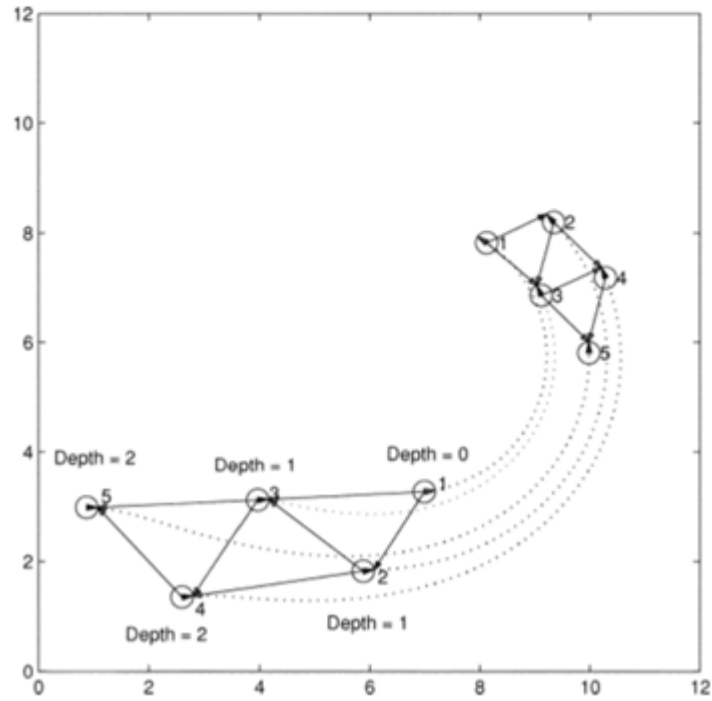
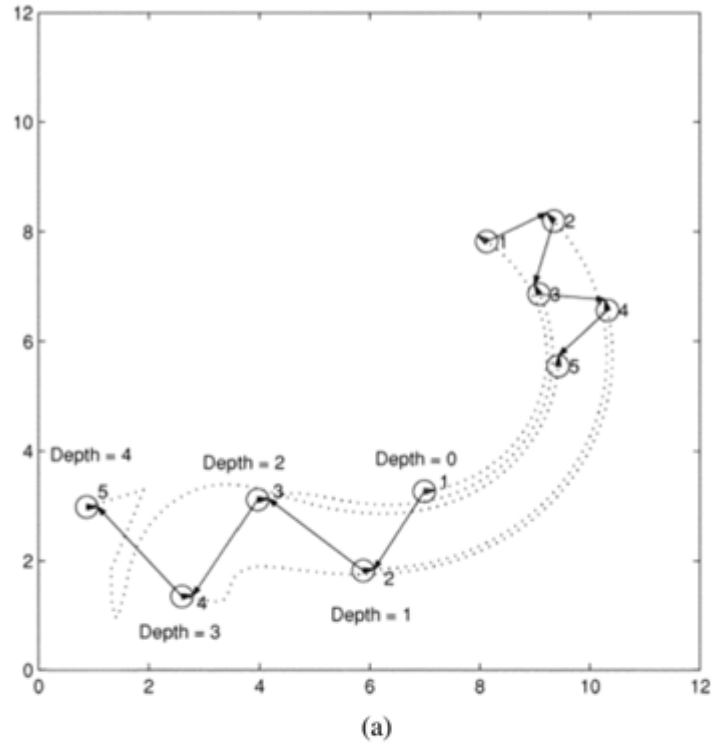


Figure 2.6: Five Robot Formation with trajectory tracking [18]

The solutions for the formation control approaches can be classified into three basic strategies as leader-following, virtual structure and behaviour based approaches[12]. In leader following strategy, some of the agents in the swarm are the leaders to manage



the rest of the swarm to achieve a desired specific task and the rest of the agents act as followers. This approach reduces the formation control problem into tracking control problem of individuals to follow the leader from a desired distance and bearing angle, thus the stability and convergence analysis of the formation can be done with the usage of single tracking controllers of members. Kumar, Fierro .. at [18] proposed a control framework in which follower agents move along a trajectory afterwards the leader agent with a desired separation  $l_{ij}$  and desired relative bearing angle  $\psi_{ij}$ . Figure -xx represents a formation control with three agents where  $R_3$  is the leader and  $R_1, R_2$  are the follower agents.

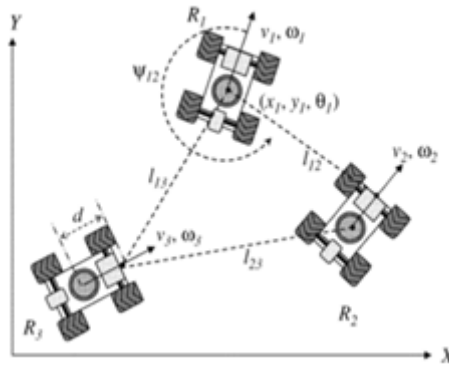


Figure 2.7: Leader-Follower Systems

In this approach it is hard to apply to gather the agents in a certain shapes. Another drawback is that, determining the separation and bearing angles for individual agents will be getting harder with the increasing number of agents in the swarm and this strategy is not fault tolerant to the absence of communication between agents.

In virtual structure approach, the formation is composed with a virtual rigid body. Formation control is applied to whole virtual structure and then the individual agent control laws are determined with inverse dynamic solutions[12]. Lewis and Tan proposed a virtual structure based method for formation control in [23] with a bidirectional flow control where robots move to stay in the virtual structure when the swarm is following a trajectory and virtual structure move to fit robots' current positions to compensate the relative errors at the end of that maneuver.

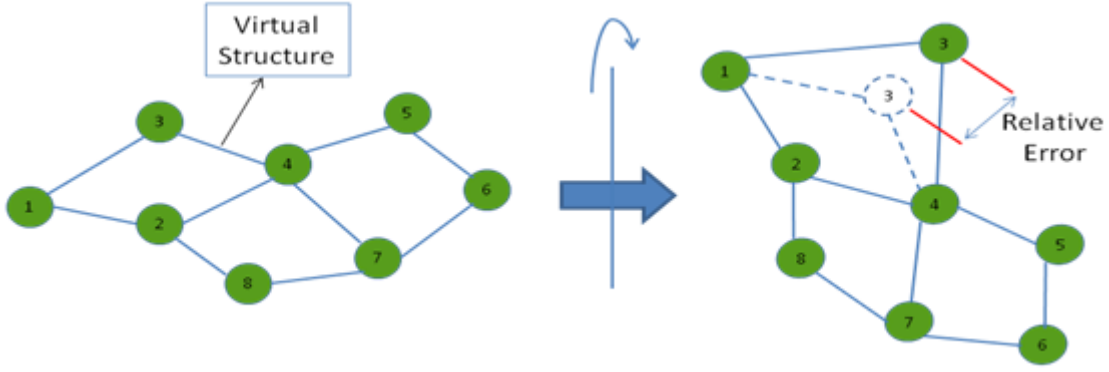


Figure 2.8: Rotational Maneuver of a Formation and Compensation of Virtual Structure

In virtual structure strategy it is easy to achieve a coordinated behavior for the group to maintain the formation during a trajectory tracking or a maneuvering, but it is not a suitable strategy to apply a formation control to achieve a certain geometrical shape with the agents in the swarm.

Behavior based strategies model every agent's behaviors to achieve specific tasks with swarm. These behaviours may be very simple like randomly walking and avoiding obstacle in the environment or they may be defined very complicated to achieve complex formation shapes with the entire swarm while optimizing the overall energy consumption depends on the implementation of the controller structures. One of the main usages of this strategy is artificial potential field based implementations. Cheng and Nagpal have introduced a robust and self-repairing formation control method for swarms in [24]. In this approach, individual control laws for the agents are composed with the artificial forces defined between the agents (to avoid collisions) and between the desired formation shape. This solution provides robustness to the agent losses in the swarm during formation control and the rest of the swarm has the ability to refill their absence in real time without changing the dynamics and the parameters of the formation controller. One of the main disadvantages of the artificial potential based approaches is that, the control forces applied to individual agents are determined instantaneously in accordance with that agent's and the other agents' positions and they cannot guarantee to optimize the total distance travelled by the agents. In this strategy the solution may converge to the steady state very slowly due to the absence of generalized

goal states for individual agents in the final state of formation.

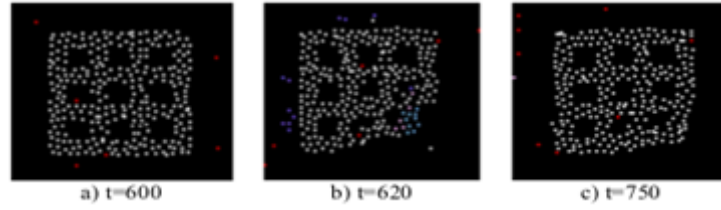


Figure 2.9: Formation Control with Artificial Forces

Another approach is to define mathematical constraints and objective functions to achieve a specific formation shape and controlling the swarm to follow a trajectory while keeping the formation. Kumar and Belta presented an abstraction method of configuration space to a manifold defined as  $A = G \times S$  where  $G$  is a Lie group representing the position and the orientation of the swarm and  $S$  represents the shape of the manifold. They provide individual control laws which can be separately handled to manipulate the lie group  $G$  to achieve formation tracking and orientation control and to manipulate the shape  $S$  to achieve different geometrical shapes. Cheah and Slotine proposed a similar method based on objective functions[8]. Common drawback for these researches, they can only implement a limited number of simple geometrical shapes because the desired formation shapes must be identified analytical to compose the related objective functions or shape manifolds.

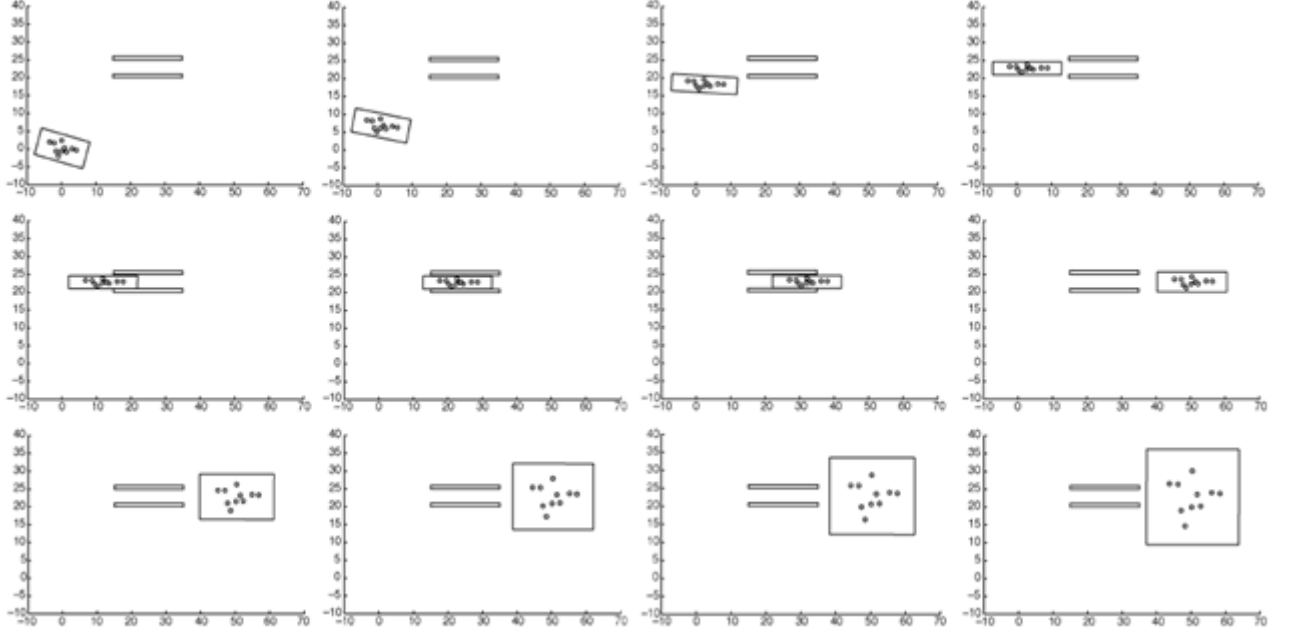


Figure 2.10: Formation Control with Objective Functions

### 2.3 Partitioning Complex Geometrical Shapes

This process is used to determine the goal states of the agents in the formation to cover the desired complex geometrical shape. There are some different solutions in the literature including fractal filling of space algorithms, bubble&circle packing algorithms and advancing front algorithms.

Fractals are self similar patterns in all scales of themselves. They are defined with simple rules and they can cover any complex shape in the nature by progressing this simple rules iteratively. This approach is widely used in mesh generating algorithms and filling space problems. Shier and Bourke [26] have introduced a randomized fractal filling of space algorithm. They proposed a fractal based method to cover a given geometrical shape with the desired shapes and they provide the proof of their algorithm is space-filling with the following statements.

$$A_i = \frac{A}{\zeta(c, N)(i + N)^c} \quad (2.1)$$

where  $\zeta(c, N)$  is the Hurwitz zeta function defined by

$$\zeta(c, N) = \sum_{i=0}^{\infty} \left( \frac{1}{(i+N)^c} \right) \quad (2.2)$$

This known to converge for  $c > 1$  and  $N > 0$ . In view of equation 2 one can write

$$\sum_{i=0}^{\infty} A_i = \sum_{i=0}^{\infty} \left( \frac{A}{\zeta(c, N)(i+N)^c} \right) \quad (2.3)$$

such that the sum of all areas  $A_i$  is the total area  $A$  to be filled, that is, if the algorithm does not halt then it is space-filling. Some of the outputs of their algorithm is given at Figure -xx

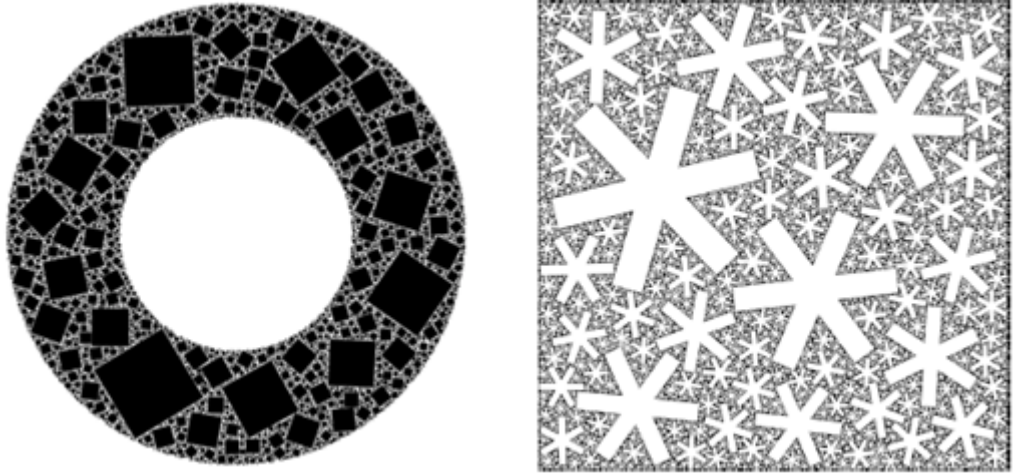


Figure 2.11: Space Filling Examples with Randomized Fractals

Bubble&Circle packing algorithms are widely used in mesh generation problems in finite element method. The main idea is that the close packing of bubbles mimics a pattern of Voroni tessellation. Corresponding to well shaped Delaunay triangles or tetrahedra which select the best topological connection for a set of nodes by avoiding small included angles[27].

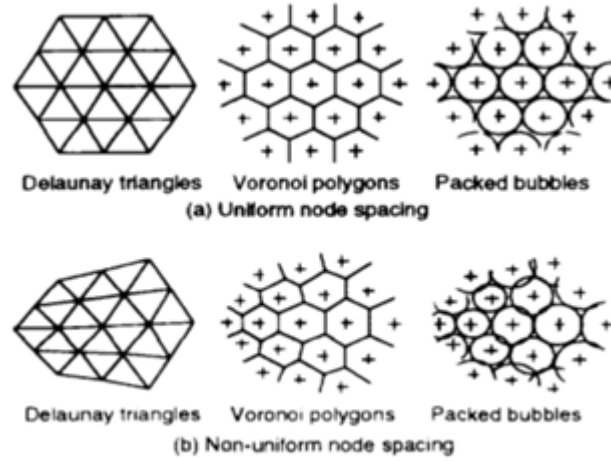


Figure 2.12: Uniform and Non-Uniform Node Spacing

Shimada and Gossard proposed a method based on interbubble forces to provide close packaging of bubbles in desired geometrical shape. This approach is very similar with the one used in formation control of swarms to achieve geometrical shapes. The related interbubble forces are described at Figure – xx.

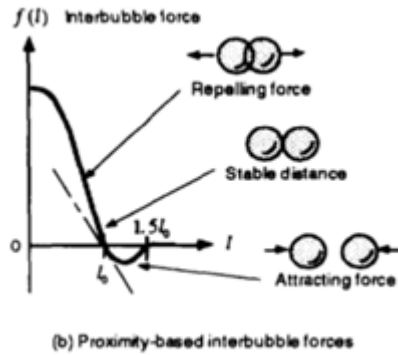


Figure 2.13: Interbubble Forces

With the help of adaptive population control by removing the excess bubble which significantly overlap their neighbors, they provide an adaptive bubble packing algorithm for mesh generation. A result with a 2D shape is given at Figure -xx

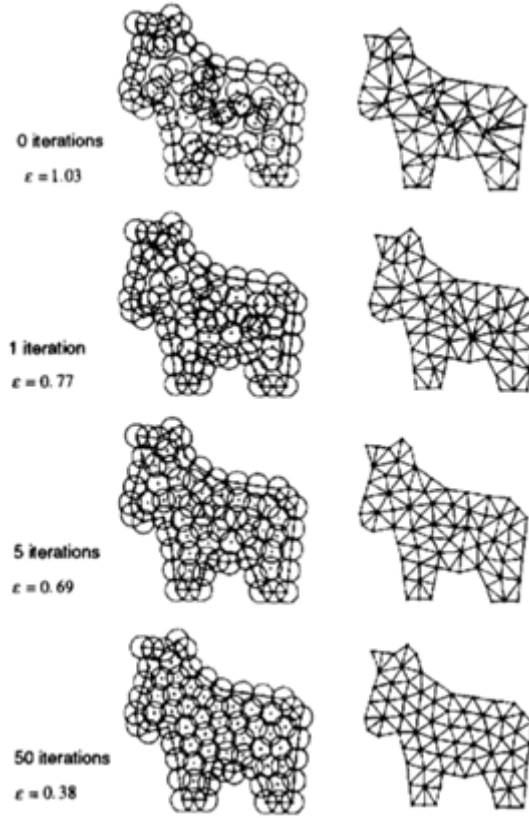


Figure 2.14: Mesh Generation with Interbubble Forces

This approach can easily be augmented for different types and number of shapes to partition a complex geometrical shape with regular sets. Basically the resultant solution will be similar to the one used in artificial potential field approach in formation control.

Advancing front methods are one of the alternatives used in mesh generation in literature. In a two dimensional advancing front method, new triangles are added into the domain from the initial front boundary and the front is propagated iteratively between the meshed and the unmeshed region. The initial front is created by the desired outer boundary of the shape and the procedure continues until the given domain is fully meshed.

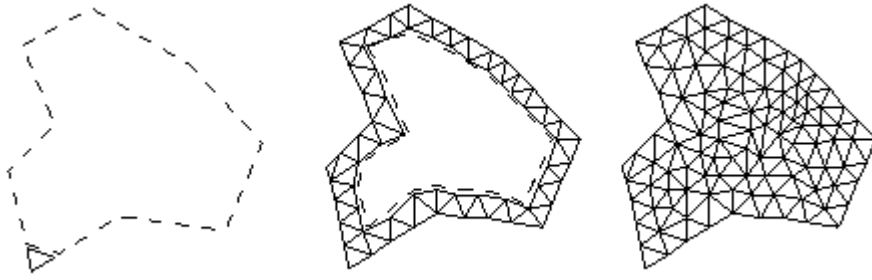


Figure 2.15: Triangulation with Advancing Front Method



## **CHAPTER 3**

### **NEXT CHAPTER**

This is another chapter. All these chapters can go into separate .tex files and you can include them with `\input{chapter1.tex}`. For only one citation [3], for multiple citations [1, 2, 4].



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## **APPENDIX A**

### **APPENDIX NAME**

Appendix content goes here.



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B.S.	B.S. Institute	B.S. Year
High School	High School Name	High School Graduating Year

### PROFESSIONAL EXPERIENCE

Year	Place	Enrollment
Duration 1	Institute/Company 1	Role/Position/Experience 1
Duration 2	Institute/Company 2	Role/Position/Experience 2

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