

TITLE OF THE EXPERIMENT

The proportionality and superposition theorems.

PREREQUISITE KNOWLEDGE

- ❑ OHM's law
- ❑ Kirchhoff's current law
- ❑ Kirchhoff's voltage law
- ❑ Calculating effective resistance in series
- ❑ Calculating effective resistance in parallel
- ❑ Mesh current analysis
- ❑ Nodal voltage analysis
- ❑ Thevenin's theorem
- ❑ Norton's theorem

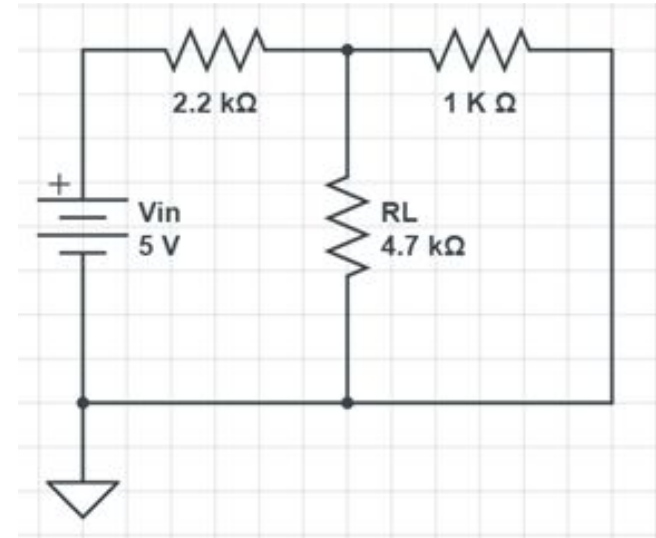
PROPORTIONALITY THEOREM - statement

The Proportionality Theorem states that the response of a circuit is proportional to the source acting on the circuit. This is also known as linearity. The proportionality constant A relates the input voltage to the output voltage as,

$$V_{\text{out}} = A \cdot V_{\text{in}}$$

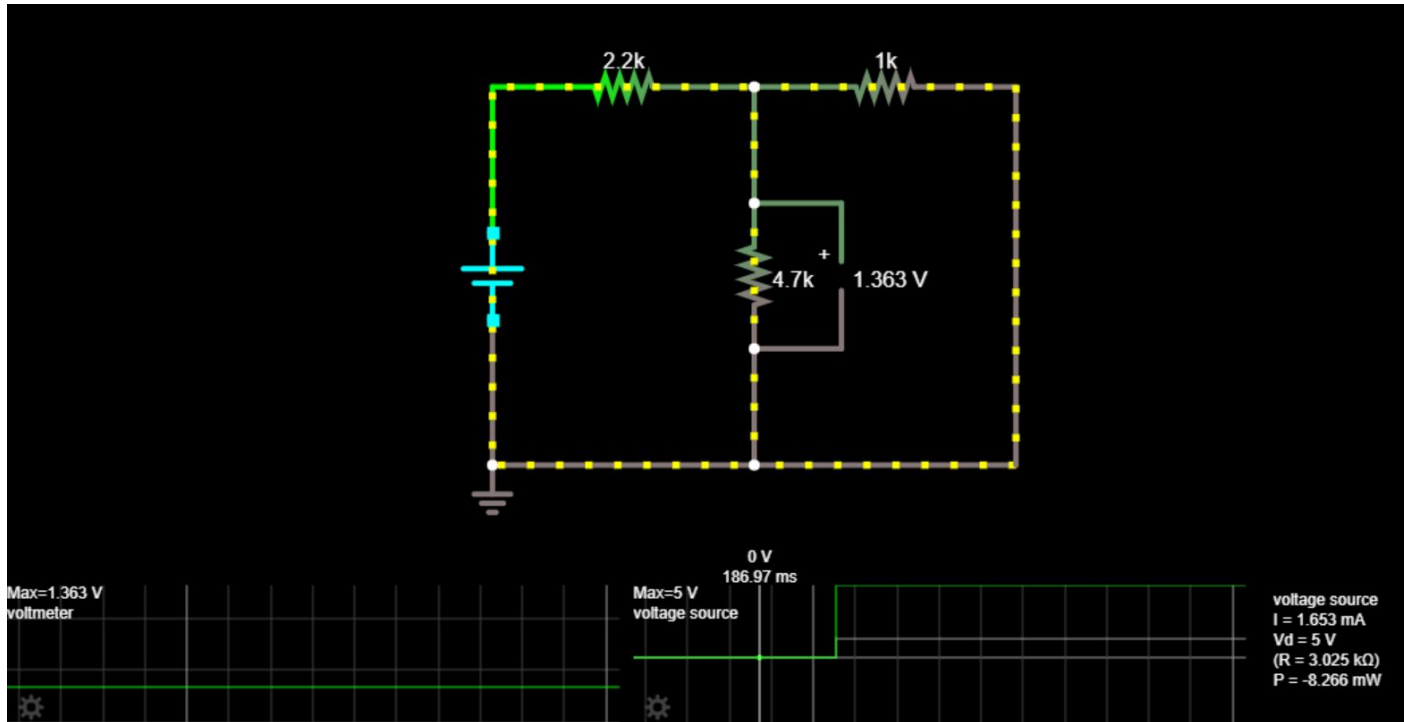
The problem statement

The proportionality factor A is sometimes referred to as the gain of a circuit. For the circuit in the given diagram, the source voltage is V_{in} . The response V_{out} is across the $4.7\text{k}\Omega$ resistor.



Circuit simulation

Link : <https://tinyurl.com/ycqfcg4v>



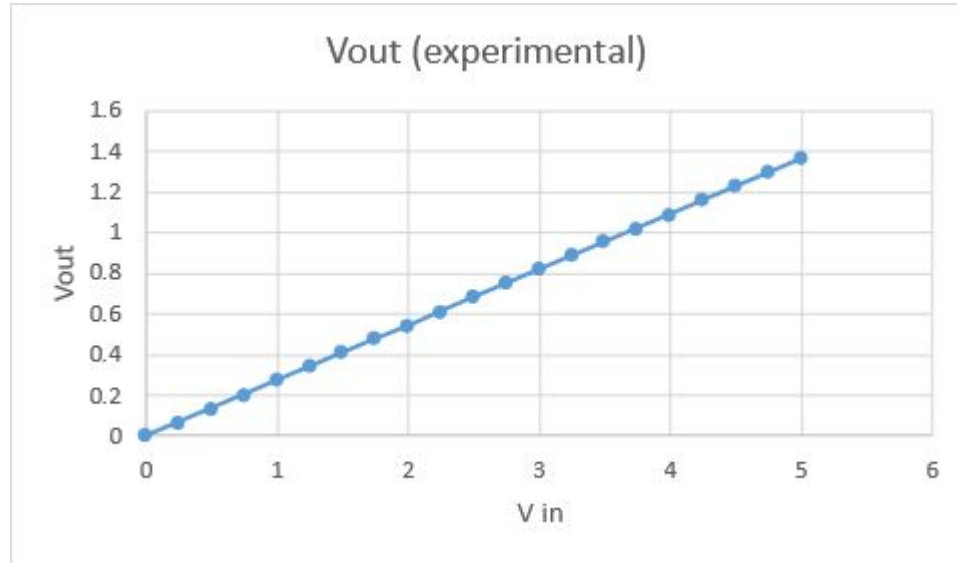
The observation table

SHEET 1 of the given link

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Proportionality Theorem- V_{out} vs V_{in} Graph

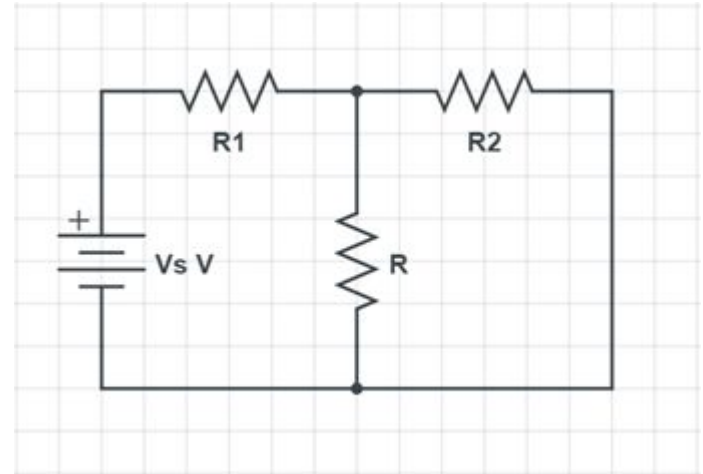
The graph we get on plotting the experimental values



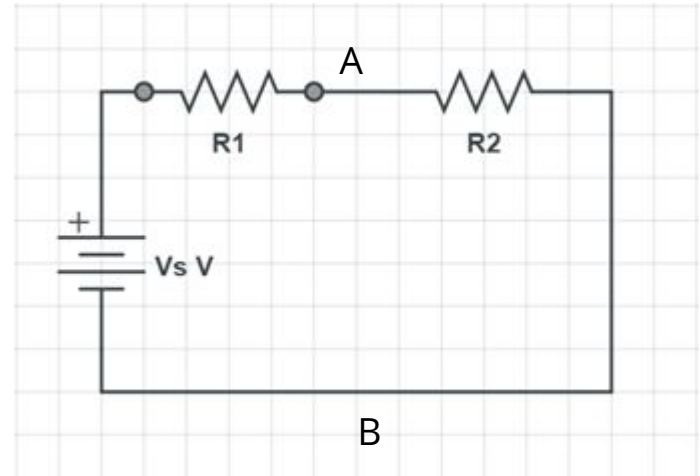
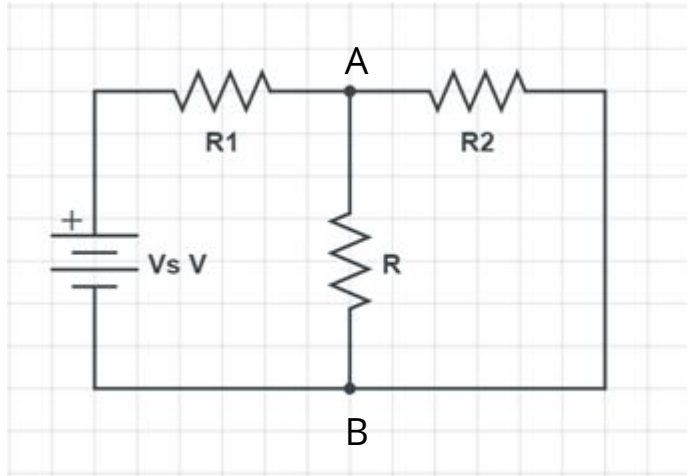
Solving the given problem statement computationally

The Thevenin's theorem states that,

Thevenin's Theorem states that it is possible to simplify any linear circuit, no matter how complex, to an equivalent circuit with just a single voltage source and series resistance connected to a load.



Using the above stated Thevenin's theorem we can simplify the above circuit as the following one,



By observation we can clearly conclude that the two resistance R_1 and R_2 are in parallel, hence the net resistance of the circuit comes out to be,

$$R_{eq} = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

To obtain the net voltage across the wire AB we need to calculate the current flowing through the circuit. For calculating it we can use OHM's law. OHM's law states that the current through a conductor between two points is directly proportional to the voltage across the two points.

From OHM's law, we can relate current with resistance as,

$$I = \frac{V}{R}$$

Here, V is the net voltage of the circuit and R is the net resistance of the circuit after removing the joint across AB, hence in the given circuit we can write the current as,

$$I = \frac{V_s}{R_1 + R_2}$$

Now for finding the voltage across AB we can use the Kirchhoff's loop rule. Kirchhoff's loop rule states that the sum of all the electric potential differences around a loop is zero.

Now on applying Kirchhoff's loop rule in the above circuit we get the following,

$$V_{\text{out}} = V_s - \left(\frac{V_s}{R_1 + R_2} \right) \cdot R_1$$

And on further simplification we get the following

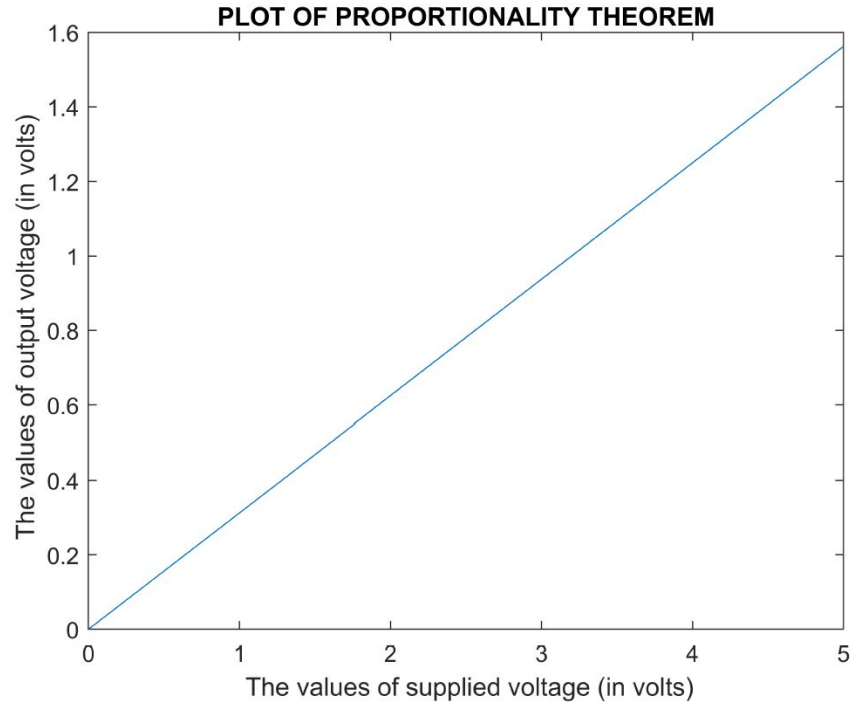
$$V_{\text{out}} = V_{\text{in}} \left(\frac{R_2}{R_1 + R_2} \right)$$

The source voltage is the input voltage that we give. Hence, $V_s = V_{\text{in}}$.

MATLAB code for computation

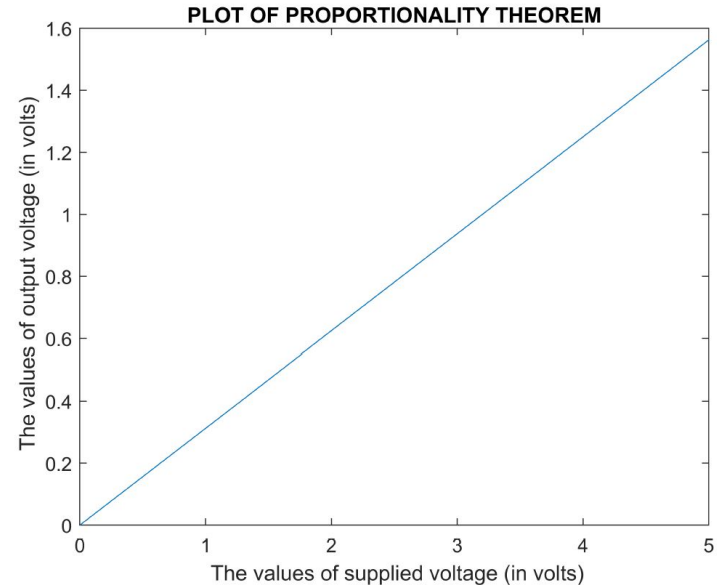
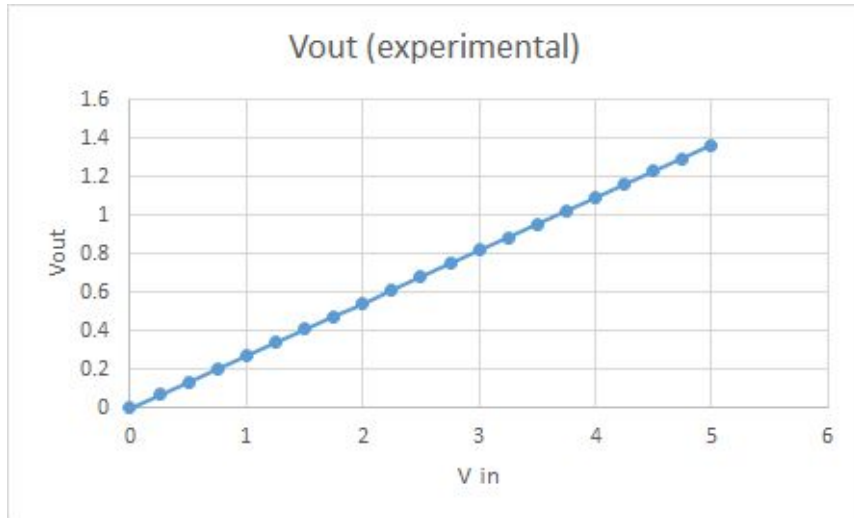
```
Vin = 0:0.25:5;  
R1=2.2;  
R2=1;  
R=R2/(R1+R2);  
Vout = Vin*R;  
plot(Vin,Vout)  
title("PLOT OF PROPORTIONALITY THEOREM")  
xlabel(" The values of supplied voltage (in volts)")  
ylabel(" The values of output voltage (in volts)")
```

Plot we get as the result



RESULT

Now on plotting a graph of the given values with V_{in} along x-axis and the experimental and computational values of V_{out} along y-axis we get the following graphs,



INFERENCE

The value A is calculated by taking the ratio of V_{out} to V_{in} or finding the slope of the above graphs i.e.,

$$V_{\text{out}} = A \cdot V_{\text{in}}$$

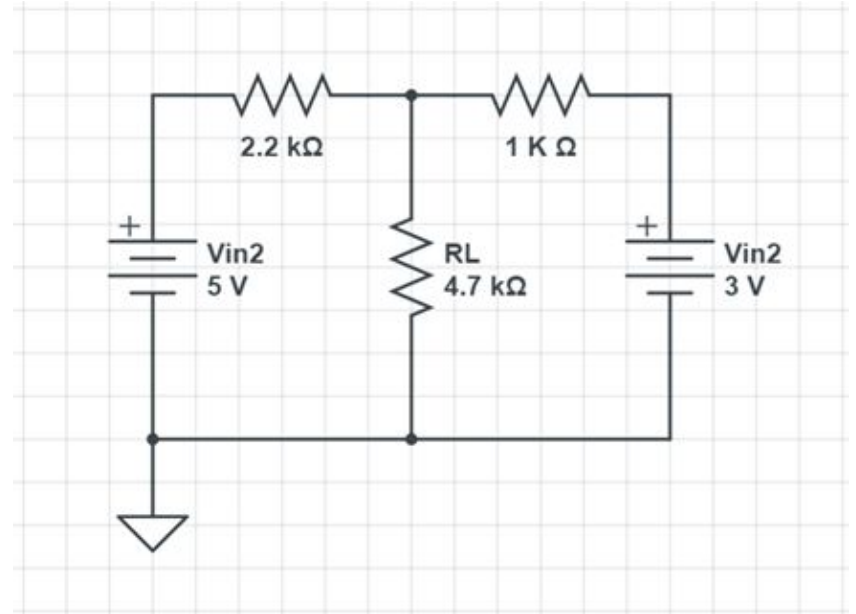
After calculating the value of A, we can observe that it is constant for any value of input voltage V_{in} . This constant A is called the gain of the circuit. Hence, the Proportionality theorem is verified for this circuit.

SUPERPOSITION THEOREM - statement

The Superposition Theorem states that the response of a linear circuit with multiple independent sources can be obtained by adding the individual responses caused by the individual sources acting alone. For an independent source acting alone, all other independent voltage sources in the circuit are replaced by short circuits and all other independent current sources are replaced by open circuits.

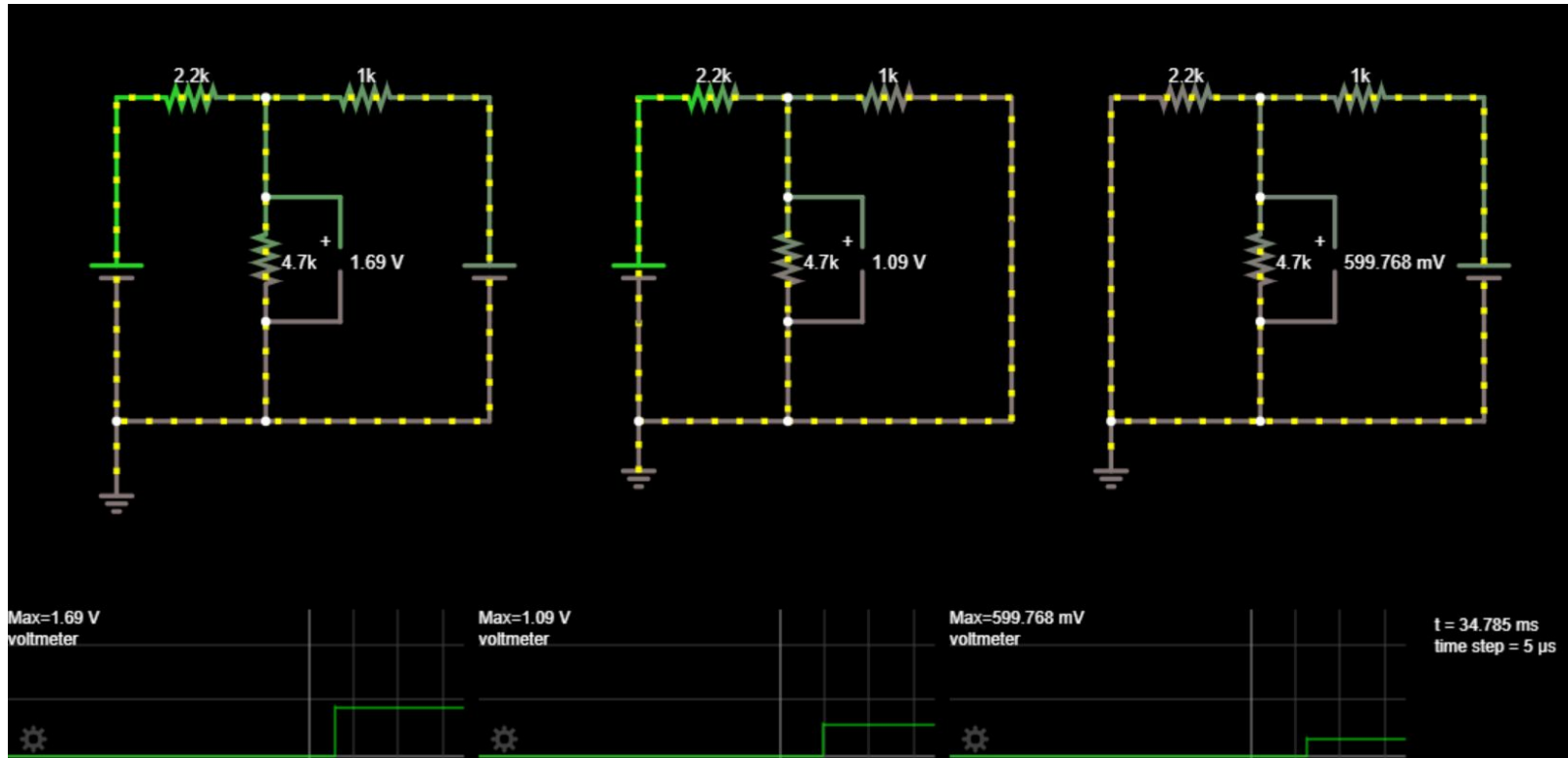
The problem statement

Check whether the given circuit obeys the principle of superposition



Circuit simulation

Link: <https://tinyurl.com/ybah4tgt>



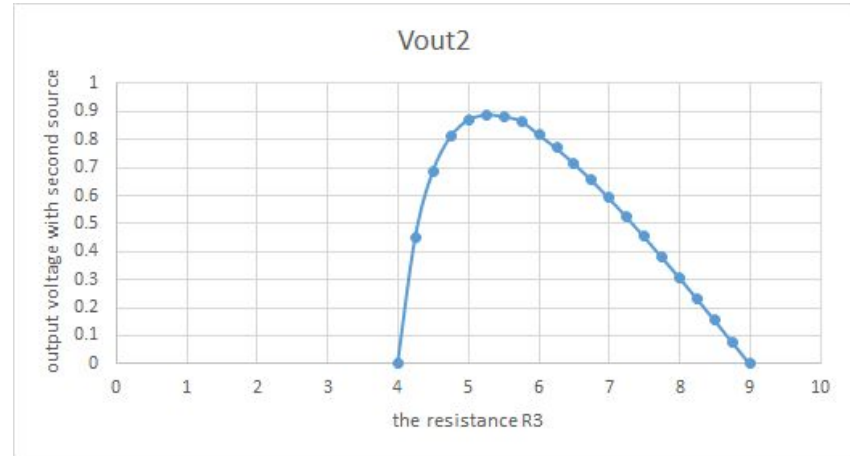
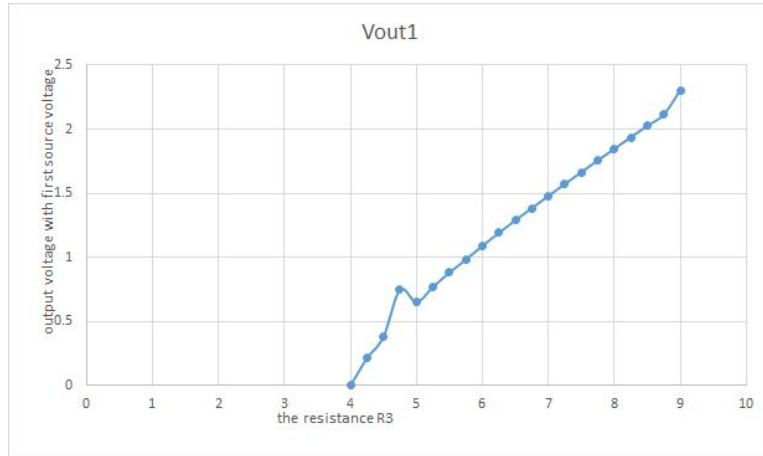
The observation table

SHEET 2 of the given link

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RESULT

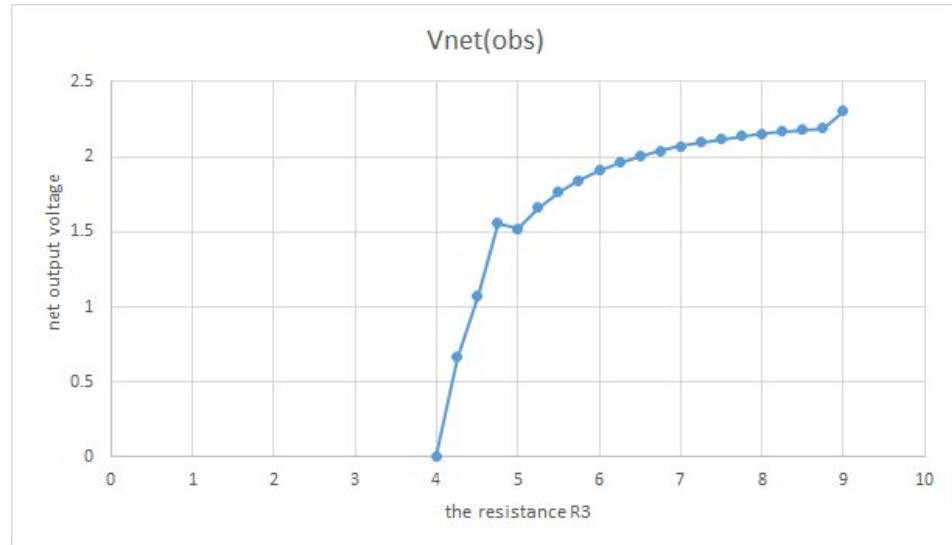
Now on plotting a graph of the given values with R_3 along x-axis and the experimental values of V_{r1} , V_{r2} along y-axis we get the following graphs.



The graph we get on plotting the experimental values.

RESULT - continued

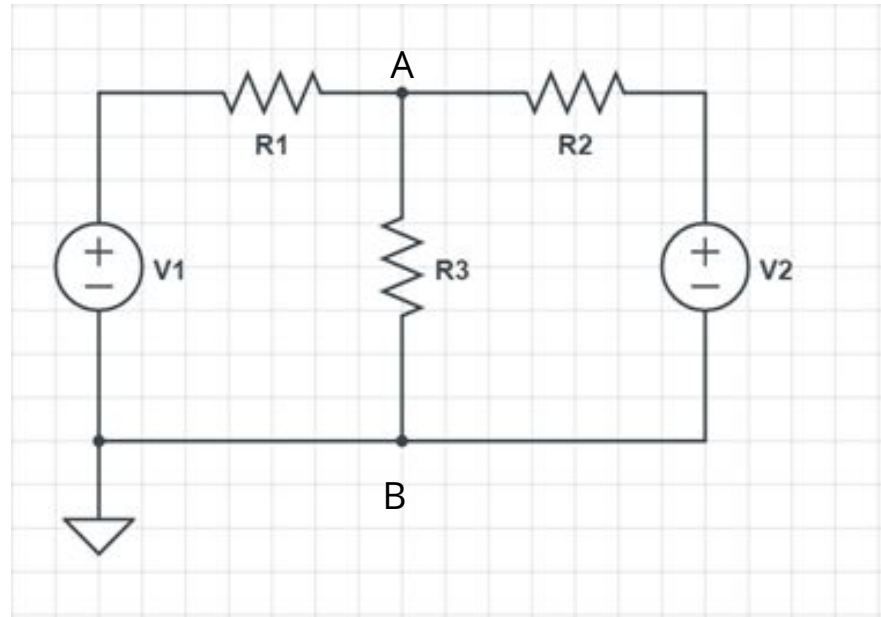
Now on plotting a graph of the given values with R_3 along x-axis and the experimental values of V_r along y-axis we get the following graph.



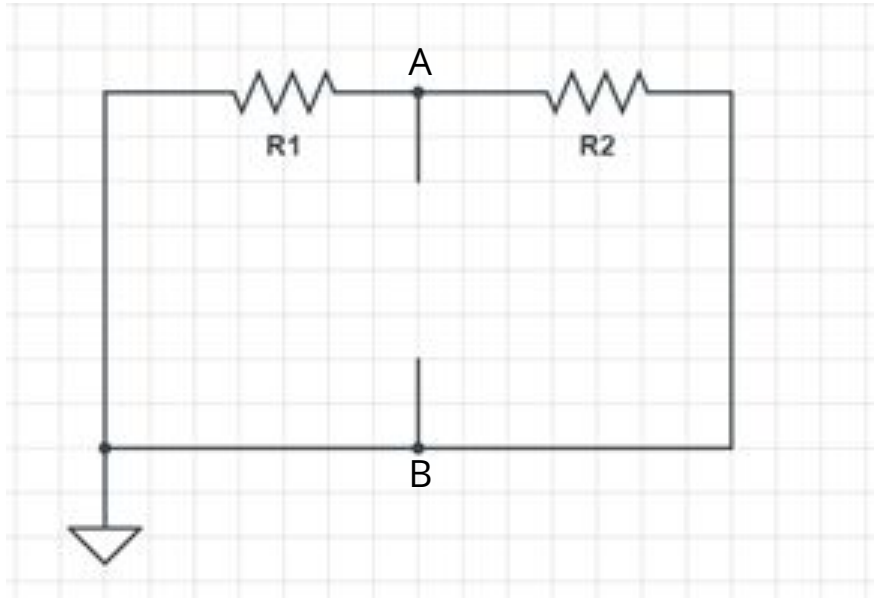
Solving the given problem statement computationally

Let us assume V_1 , V_2 as source voltage. Let $V_1 > V_2$.

Case 1 [with 2 source voltage]:

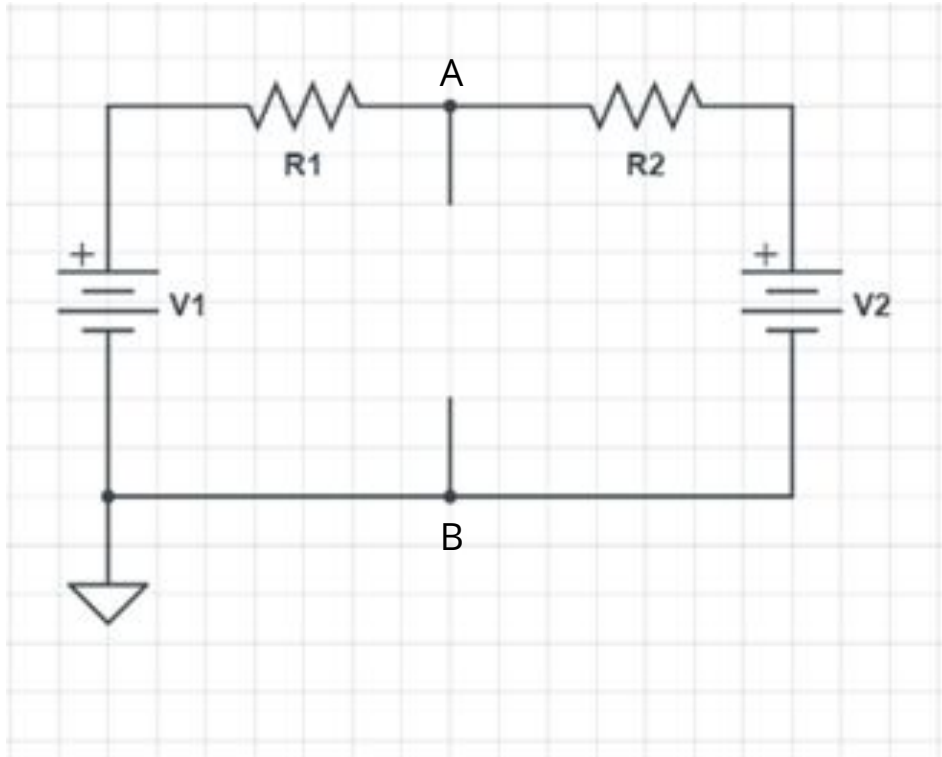


Finding the equivalent resistance, by removing the ' R_3 ' resistor. Also, by removing the voltage sources (short circuiting).



$$R_{TH} = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

Finding equivalent voltage [without ' R_3 ' resistor]



By KVL,

$$V_1 - IR_1 - IR_2 - V_2 = 0$$

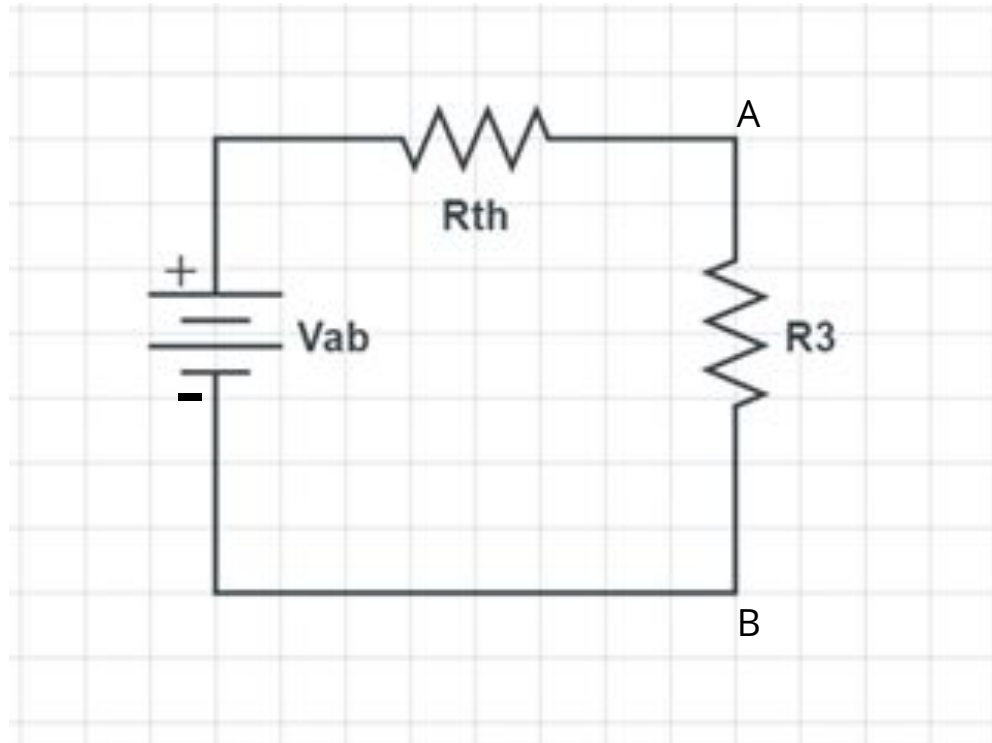
$$I = \frac{V_1 - V_2}{R_1 + R_2} ,$$

$I \rightarrow$ current flowing in the circuit.

Let V_{AB} is the equivalent voltage across A&B,

$$V_{AB} = V_1 - IR_1 = V_2 + IR_2$$

Simplified version of circuit [as per Thevenin's rule]



By applying KVL,

$$V_{AB} - I'_1 R_{TH} - I'_1 R_3 = 0$$

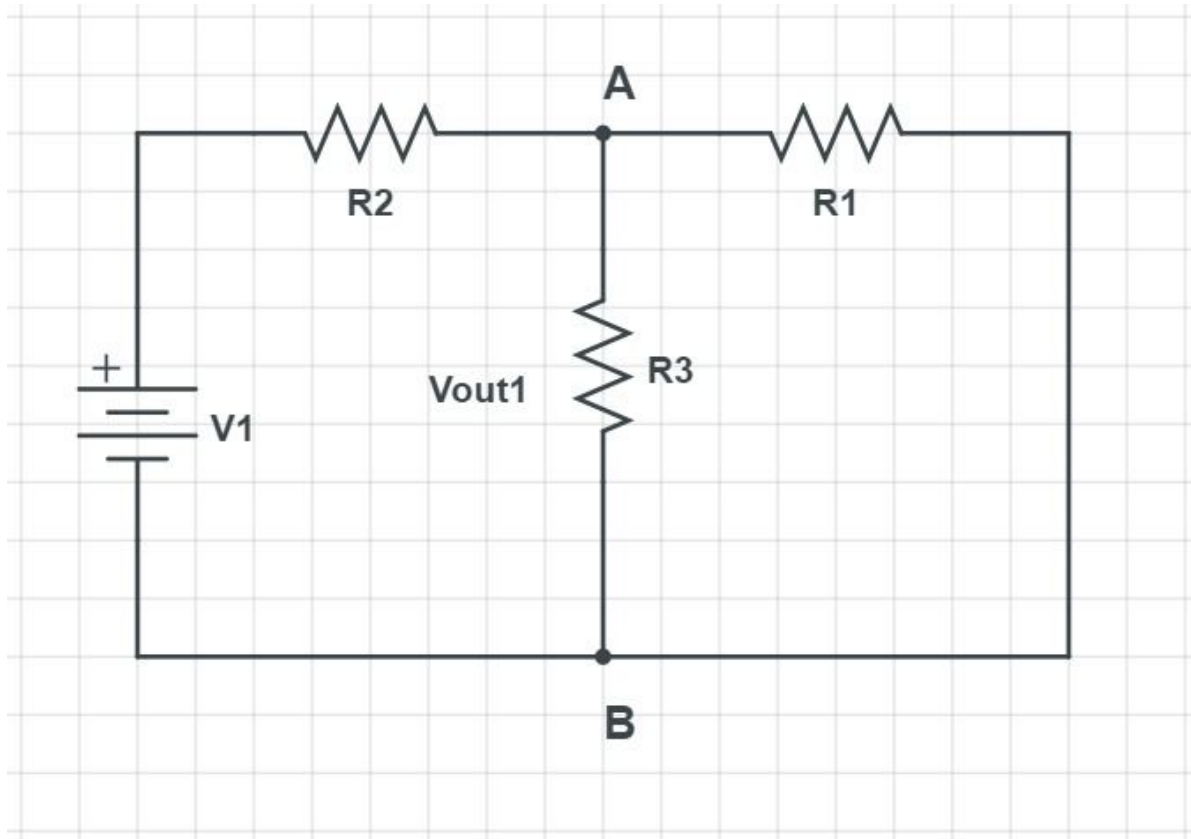
$$I'_1 = \frac{V_{AB}}{R_{TH} + R_3}$$

by ohm's law,

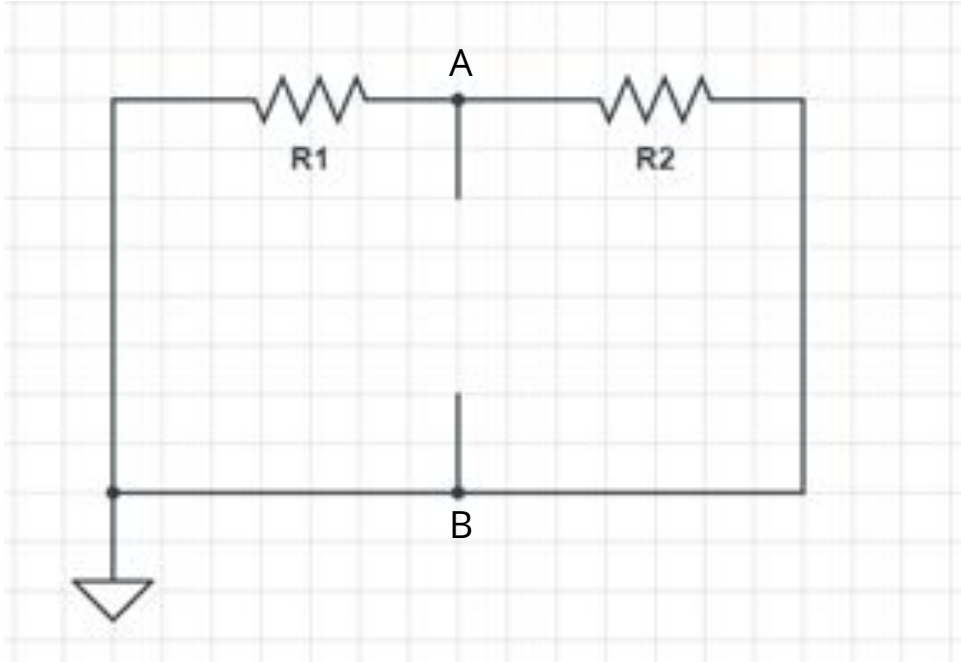
$$V_{out} = I'_1 \times R_3$$

where V_{out} is voltage across R_3

Case 2 (with source voltage V_1 and where V_2 is the short circuited)



Finding the equivalent resistance across A&B by removing ' R_3 ' resistor, [also by short circuiting source voltage]



$$R_{TH} = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

finding equivalent voltage across 'A' & 'B'

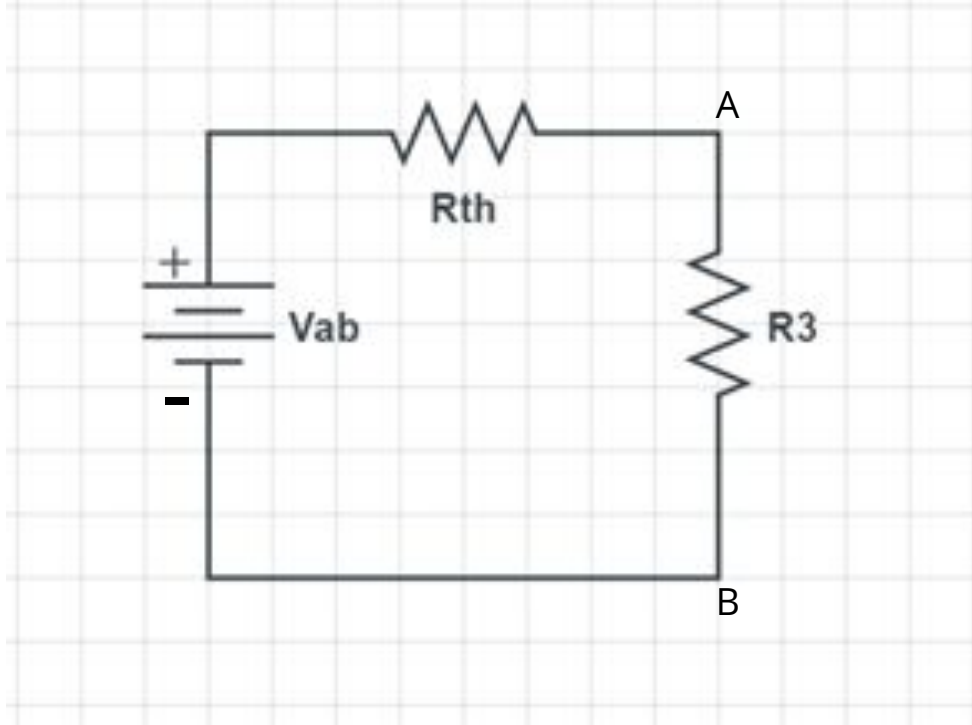
by KVL,

$$V_1 - I_2 R_1 - I_2 R_2 = 0$$

$$I_2 = \frac{V_1}{R_1 + R_2}$$

$$V_{AB} = V_1 - I_2 R_1 \quad \text{where } V_{AB} \text{ is voltage across A\&B}$$

Simplified version of the circuit, [using Thevenin's theorem]



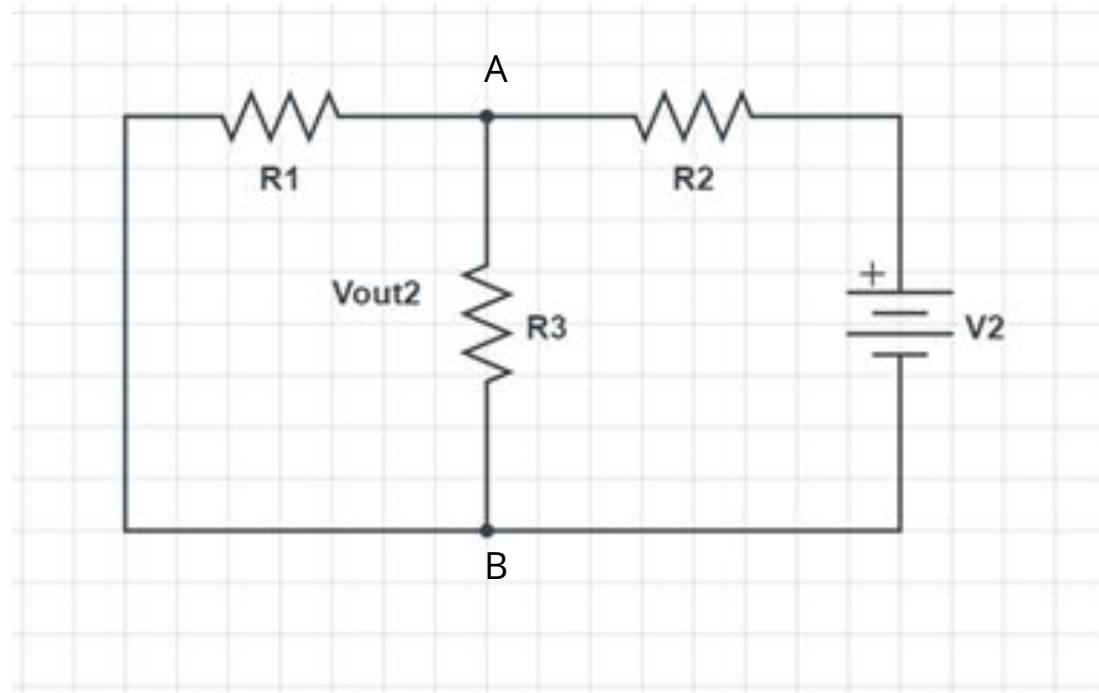
by KVL,

$$V_{AB} - I'_2 R_{TH} - I'_2 R_3 = 0$$

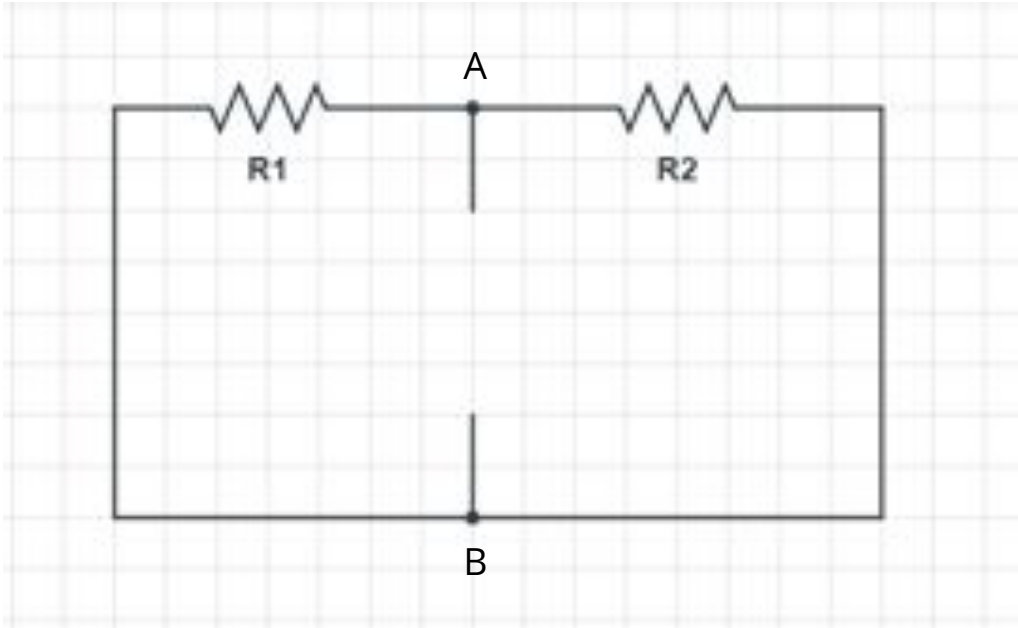
$$I'_2 = \frac{V_{AB}}{R_{TH} + R_3}$$

hence, $V_{out\ 1} = I'_2 R_3 \rightarrow$ by ohm's law

Case 3 (with source voltage V_2 , where V_1 short circuited):

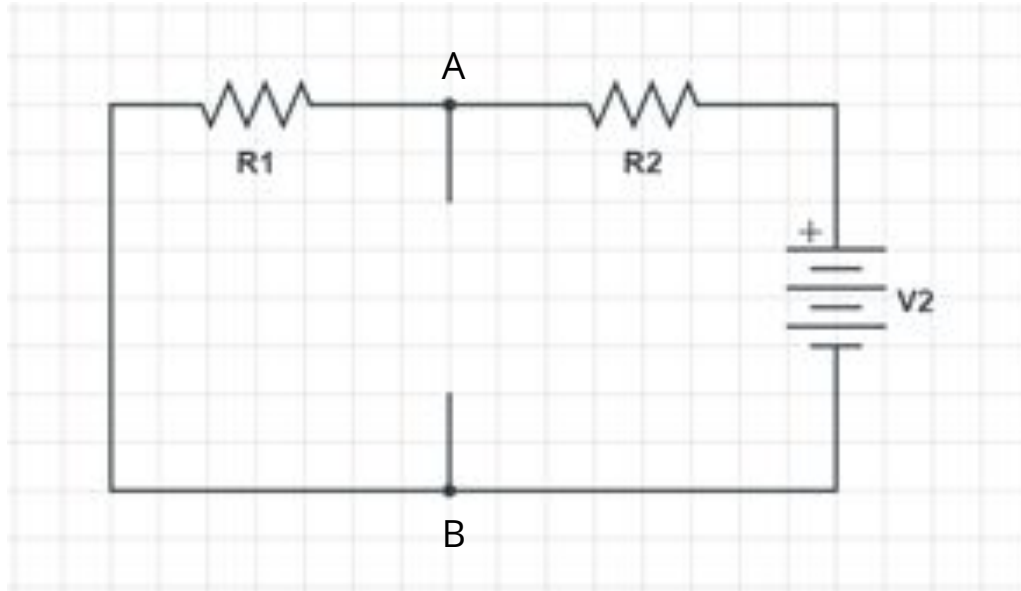


Finding the equivalent resistance across A&B by removing ' R_3 ' resistor (also by short circuiting source voltage)



$$R_{TH} = \frac{R_1 R_2}{R_1 + R_2}$$

Finding equivalent voltage across A&B



By KVL,

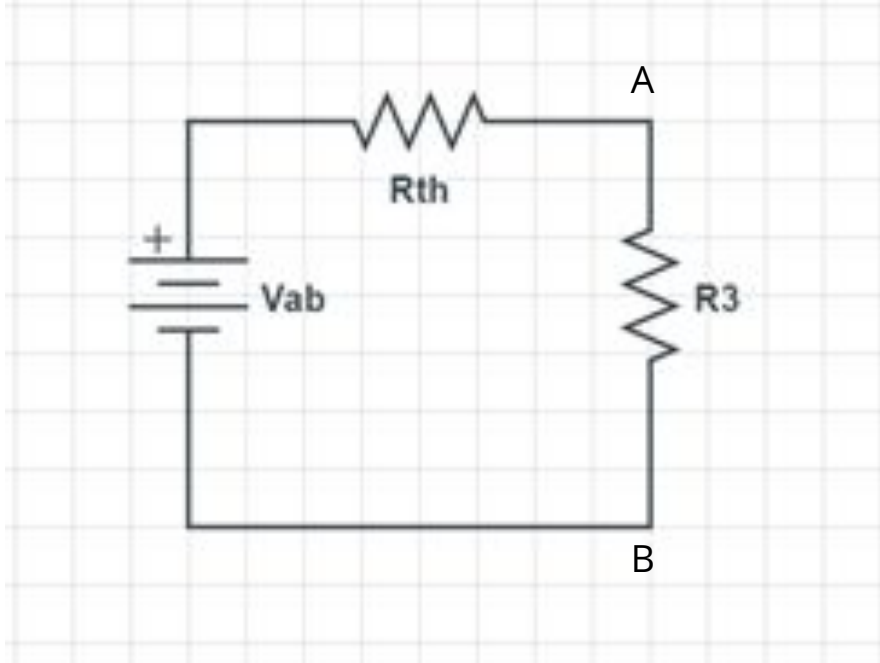
$$V_2 - I_3 R_2 - I_3 R_1 = 0$$

$$I_3 = \frac{V_2}{R_1 + R_2}$$

$$V_{AB} = V_2 - I_3 R_2$$

where V_{AB} is voltage across A&B.

Simplified version of the circuit, (using Thevenin's theorem)



by KVL,

$$V_{AB} - I'_2 R_{TH} - I'_3 R_3 = 0$$

$$I'_3 = \frac{V_{AB}}{R_1 + R_2}$$

$$\text{hence, } V_{\text{out } 2} = I'_3 R_3$$

Now, we can see that,

$$V_{\text{out}} = V_{\text{out } 1} + V_{\text{out } 2}$$

Hence, super-position theorem is proved.]

$$\text{also, } I'_1 = I'_2 + I'_3$$

$I'_1 \longrightarrow$ current flowing through R_3 when source voltages V_1 and V_2 are there.

$I'_2 \longrightarrow$ current flowing through R_3 when ' V_1 ' is there.

$I'_3 \longrightarrow$ current flowing through R_3 when ' V_2 ' is there.

MATLAB code for computation

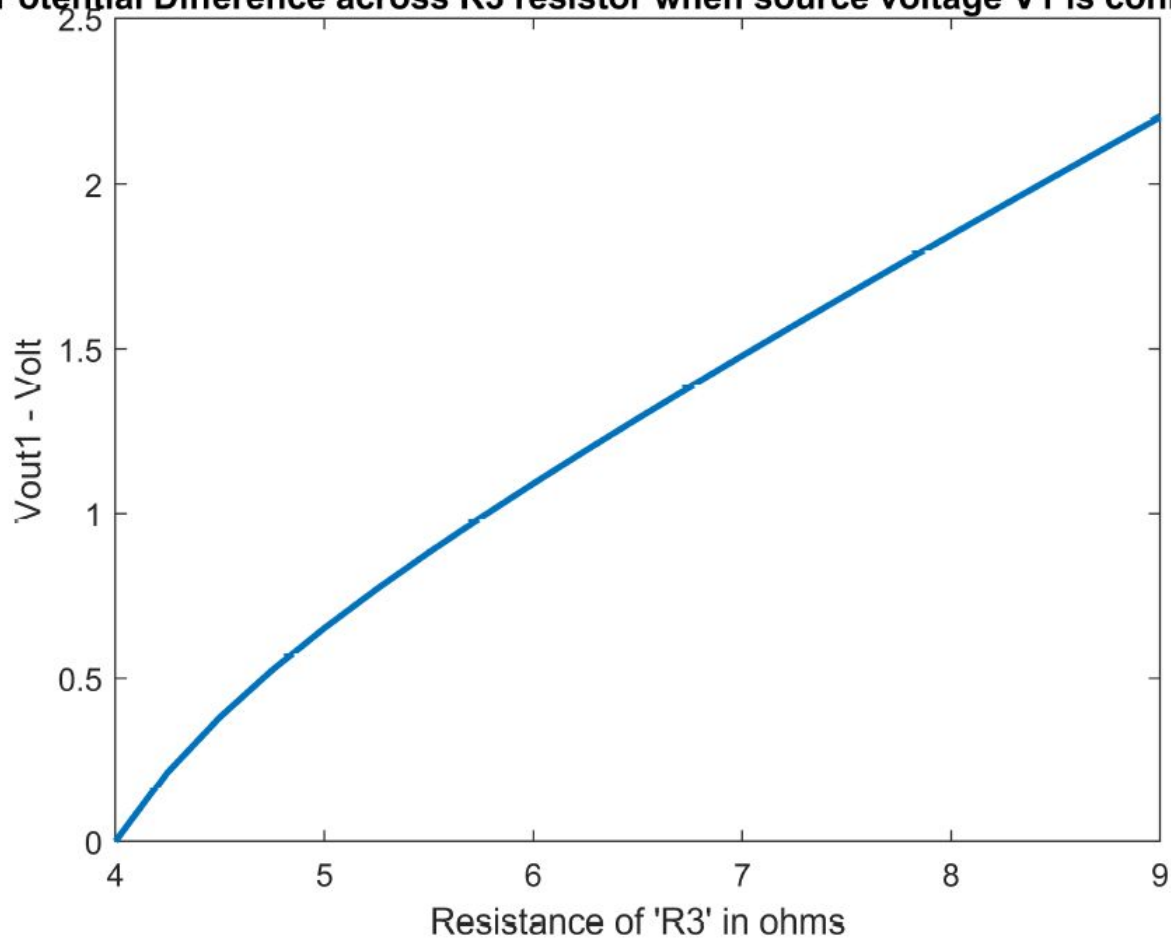
```
clc;
clear all;
close all;

% Resistance Values
R1 = 0:0.25:5;
R2 = 2:0.25:7;
R3 = 4:0.25:9;

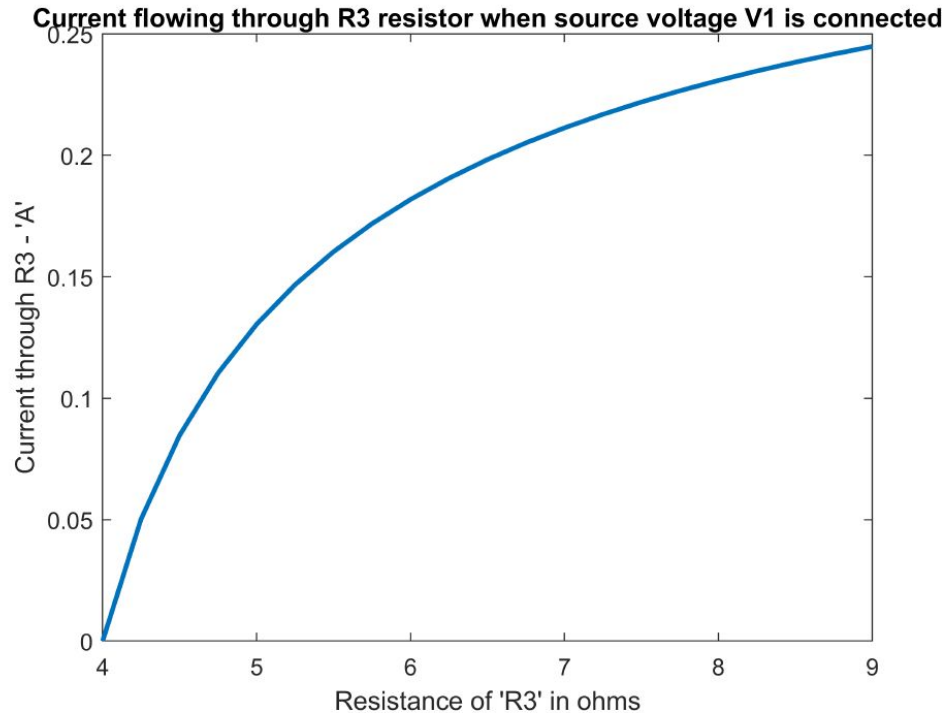
% Source Voltages
V1 = 0:0.25:5;
V2 = 5:-0.25:0;

% With source voltage V1
R_TH = R1.*R2 ./ (R1 + R2);
I2 = (V1) ./ (R1 + R2);
V_ab_1 = V1 - I2.*R1;
IR3_1 = V_ab_1 ./ (R3 + R_TH);
Vout1 = IR3_1 .* R3;
figure
plot(R3,Vout1,"LineWidth",2)
title("Potential Difference across R3 resistor when source voltage V1 is connected")
xlabel("Resistance of 'R3' in ohms")
ylabel("Vout1 - Volt")
```

Potential Difference across R3 resistor when source voltage V1 is connected

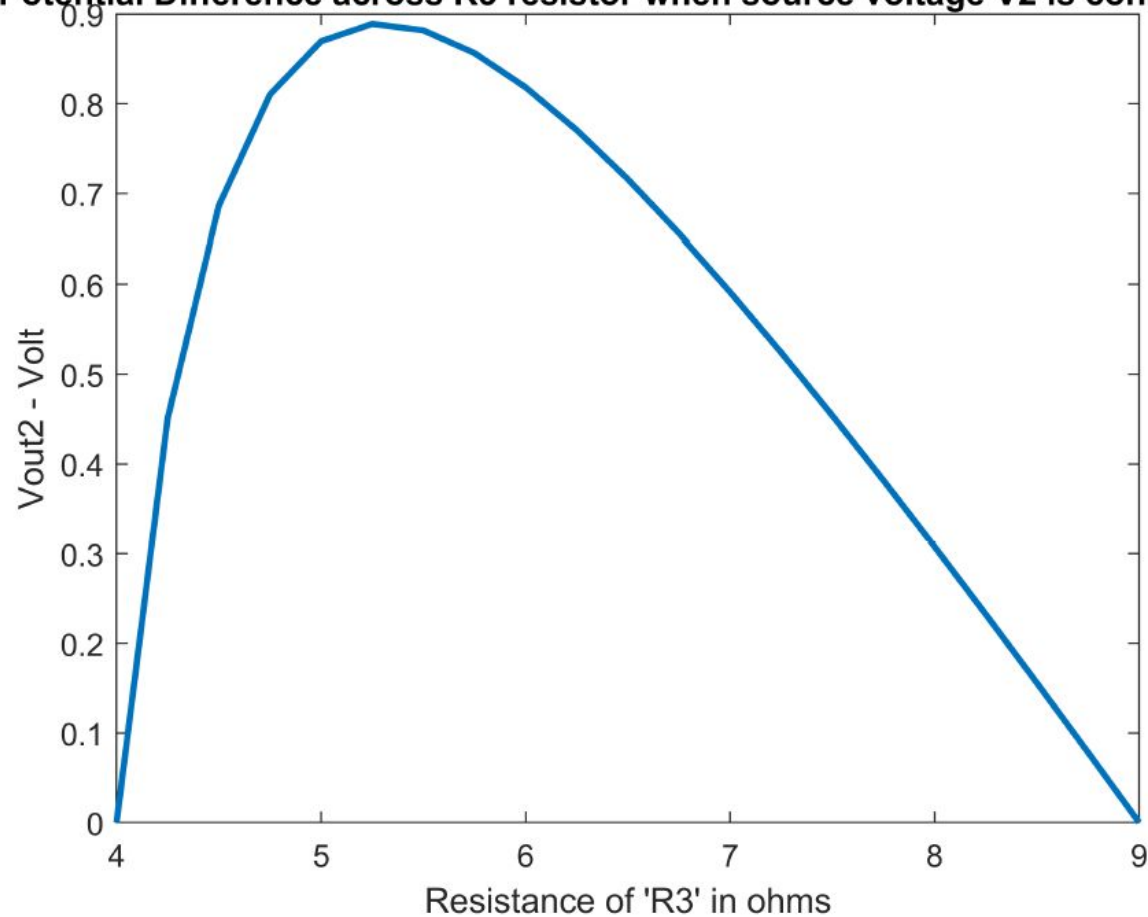


```
plot(R3,IR3_1,"LineWidth",2)
title("Current flowing through R3 resistor when source voltage V1 is connected")
xlabel("Resistance of 'R3' in ohms")
ylabel("Current through R3 - 'A'")
```

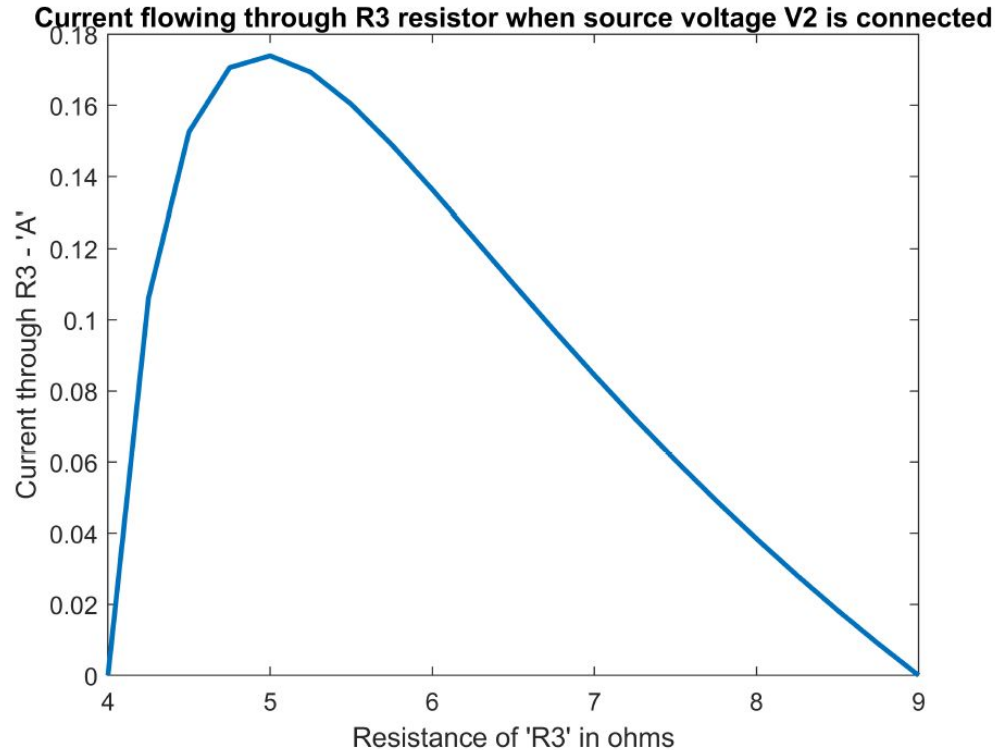


```
% With source voltage V2
R_TH = R1.*R2 ./ (R1 + R2);
I3 = (V2) ./ (R1 + R2);
V_ab_2 = V2 - I3.*R2;
IR3_2 = V_ab_2 ./ (R3 + R_TH);
Vout2 = IR3_2 .* R3;
figure
plot(R3,Vout2,"LineWidth",2)
title("Potential Difference across R3 resistor when source voltage V2 is connected")
xlabel("Resistance of 'R3' in ohms")
ylabel("Vout2 - Volt")
```

Potential Difference across R3 resistor when source voltage V2 is connected

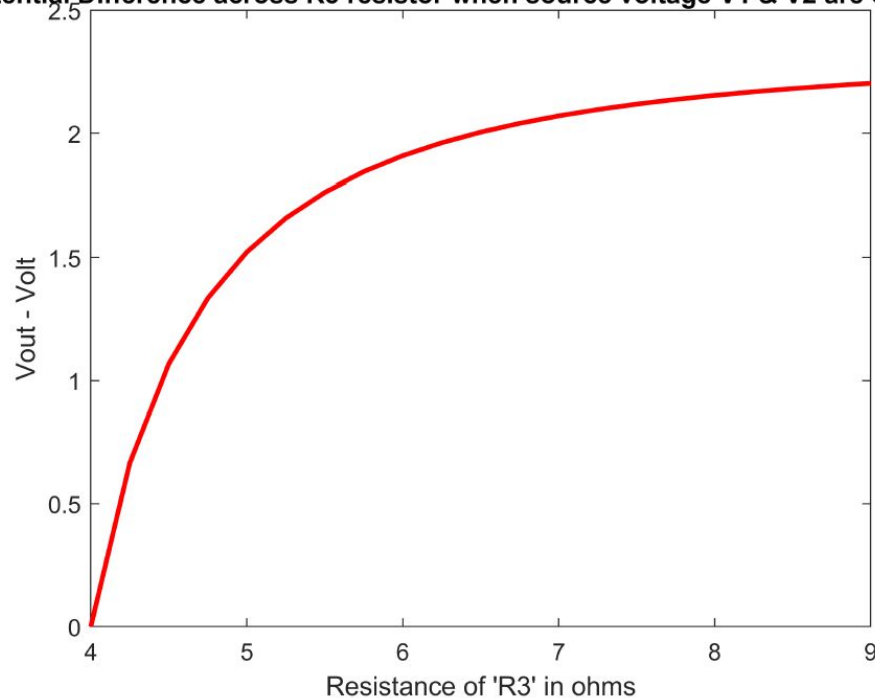



```
plot(R3,IR3_2,"LineWidth",2)
title("Current flowing through R3 resistor when source voltage V2 is connected")
xlabel("Resistance of 'R3' in ohms")
ylabel("Current through R3 - 'A'")
```

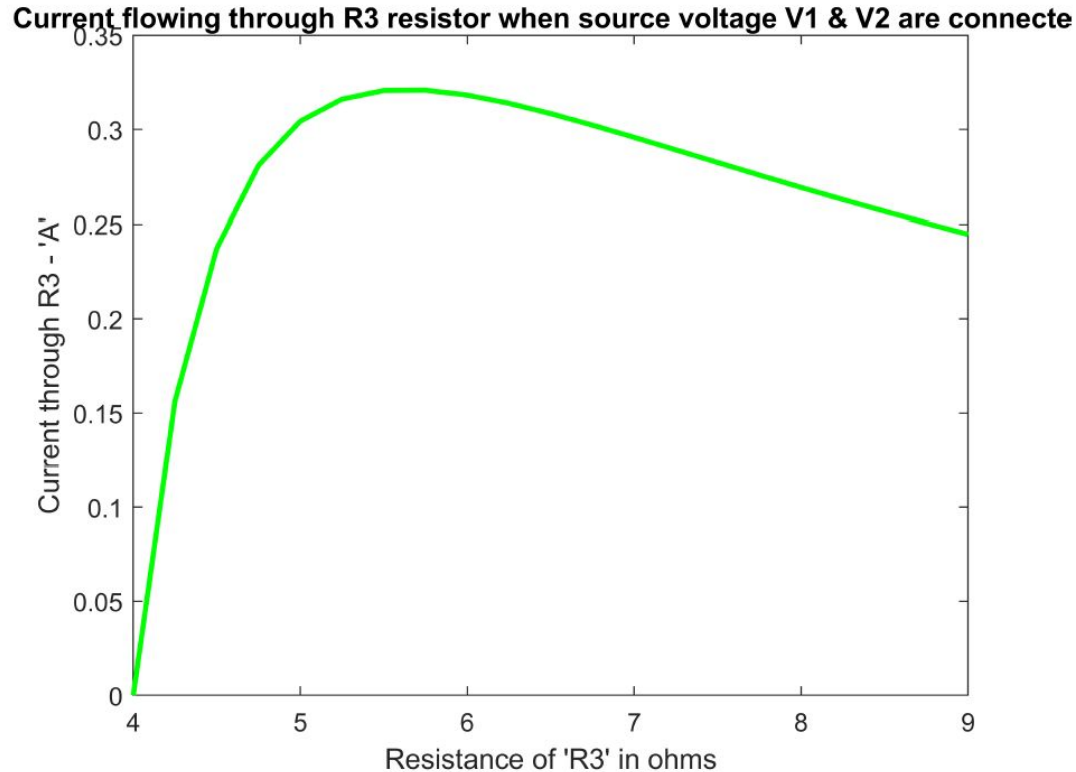


```
Vout = Vout1 + Vout2;  
IR3 = IR3_1 + IR3_2;  
plot(R3,Vout,"LineWidth",2,"Color",'r')  
title("Potential Difference across R3 resistor when source voltage V1 & V2 are connected")  
xlabel("Resistance of 'R3' in ohms")  
ylabel("Vout - Volt")
```

Potential Difference across R3 resistor when source voltage V1 & V2 are connect

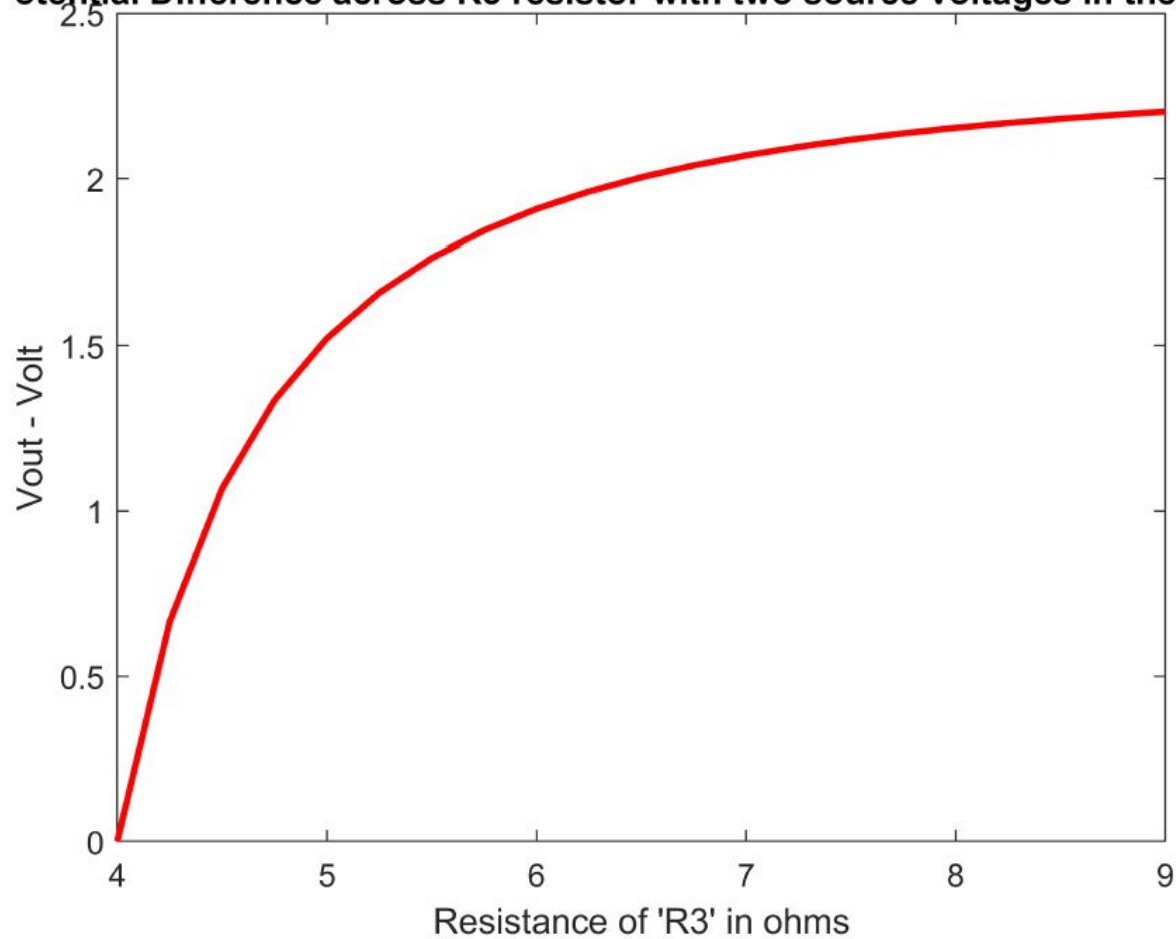


```
plot(R3,IR3,"LineWidth",2,"Color",'green')  
title("Current flowing through R3 resistor when source voltage V1 & V2 are connected")  
xlabel("Resistance of 'R3' in ohms")  
ylabel("Current through R3 - 'A'")
```

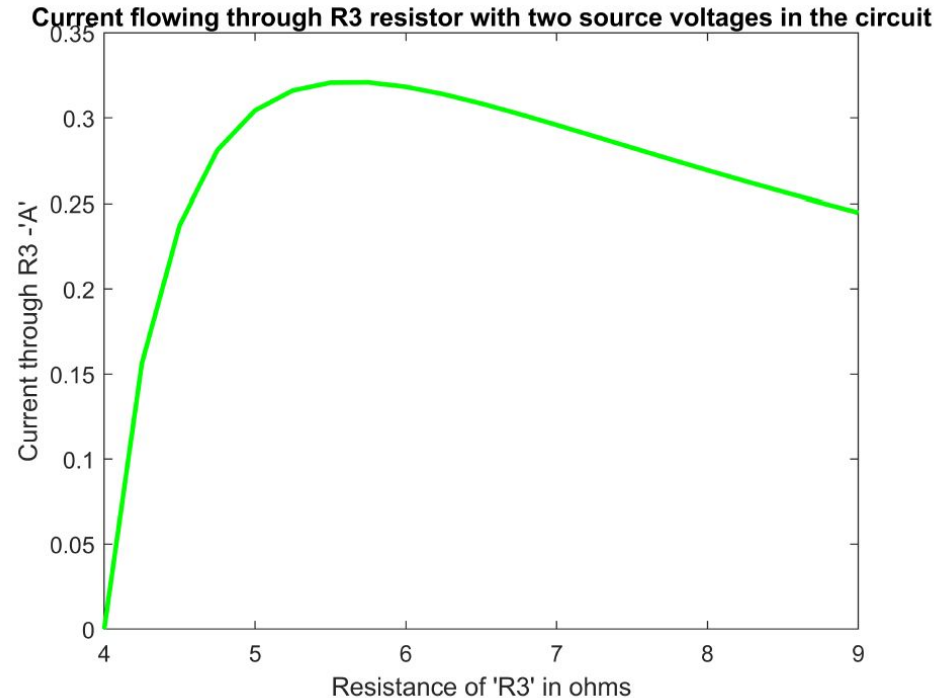


```
% With source voltageS V1 and V2
R_TH = R1.*R2 ./ (R1 + R2);
I1 = (V1 - V2) ./ (R1 + R2);
V_ab = V1 - I1.*R1;
IR3 = V_ab ./ (R3 +R_TH);
Vout = IR3 .* R3;
plot(R3,Vout,"LineWidth",2,"Color",'r')
title("Potential Difference across R3 resistor with two source voltages in the circuit")
xlabel("Resistance of 'R3' in ohms")
ylabel("Vout - Volt")
```

Potential Difference across R3 resistor with two source voltages in the circuit



```
plot(R3,IR3,"LineWidth",2,"Color",'green')  
title("Current flowing through R3 resistor with two source voltages in the circuit")  
xlabel("Resistance of 'R3' in ohms")  
ylabel("Current through R3 -'A'")
```



INFERENCE

We can observe that the sum of individual output voltages is equal to the output voltage when both source voltages (V_1 and V_2) are connected in the circuit.

- For $V_{in} = V_1$ and V_2 , we get output voltage across resistor Vr_{out} and current flowing through the circuit is I_{out} .
- For $V_{in} = V_1$, we get output voltage across resistor Vr_{out1} and current flowing through the circuit is I_{out1} .
- For $V_{in} = V_2$, we get output voltage across resistor as Vr_{out2} and current flowing through the circuit is I_{out2} .

We observe that:

$$\begin{aligned} \diamond Vr_{out} &= Vr_{out1} + Vr_{out2} \\ \diamond I_{out} &= I_{out1} + I_{out2} \end{aligned}$$

Hence, the superposition theorem is proved.

APPLICATION OF SUPERPOSITION IN RC CIRCUIT

Superposition theorem for differential equation:

Suppose $y_1(t)$ solves the differential equation, $\frac{dy}{dt} + f(t) = g_1(t)$

Suppose $y_2(t)$ solves the differential equation, $\frac{dy}{dt} + f(t) = g_2(t)$

Then $y_1 + y_2$ is a solution to $\frac{dy}{dt} + f(t) = g_1(t) + g_2(t)$

Proof:

$$y = y_1 + y_2$$

$$y' = y_1' + y_2'$$

$$y_1' + y_2' + f(t) * [y_1 + y_2] = g_1(t) + g_2(t)$$

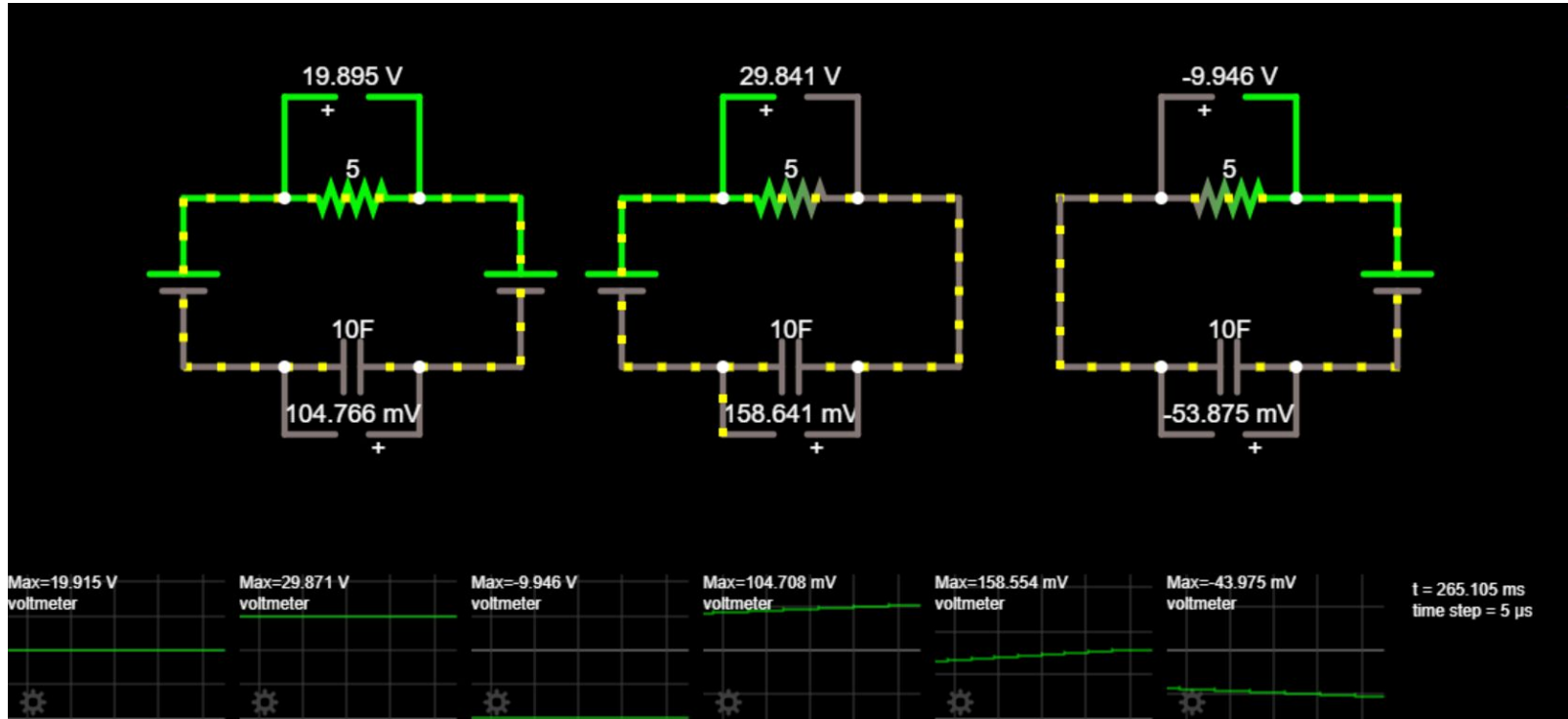
$$[y_1' + f(t) * y_1] + [y_2' + f(t) * y_2] = g_1(t) + g_2(t)$$

$$g_1(t) + g_2(t) = g_1(t) + g_2(t)$$

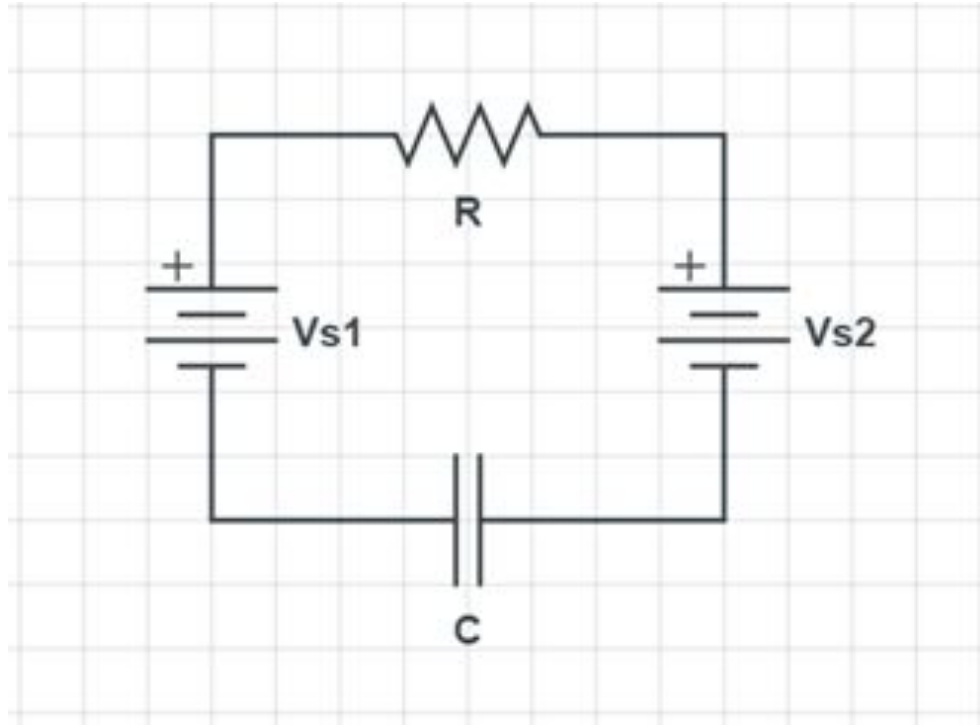
Hence Proved.

Circuit simulation - RC Circuit

Link: <https://tinyurl.com/ybm6tyey>



Proof of superposition theorem given that two source voltages are V_{s_1} and V_{s_2}



Let V_c be the voltage across the capacitor.

Let V_r be the voltage across the resistor.

Let V_{s1} be source voltage 1.

Let V_{s2} be source voltage 2.

Let R be the resistance of the resistor and C be the capacitance of the capacitor.

Let $q(t)$ be charge on capacitor,

$$q(t) = C \times V_c(t)$$

$$\frac{dq(t)}{dt} = C \times V_c'(t)$$

$$V_c'(t) = \frac{I(t)}{C} \text{ ---- (i)}$$

By Ohm's law, $I = \frac{V}{R}$

By, Kirchhoff's voltage law [Sum of voltage around any closed loop is zero],

$$V_{s1} - V_{s2} - V_r - V_c(t) = 0$$

$$\mathbf{V_r = V_{s1} - V_{s2} - V_c(t) \text{ ---- (ii)}}$$

Use (ii) in (i),

$$V_c'(t) = \frac{V_{s1} - V_{s2} - V_c(t)}{R \times C}$$

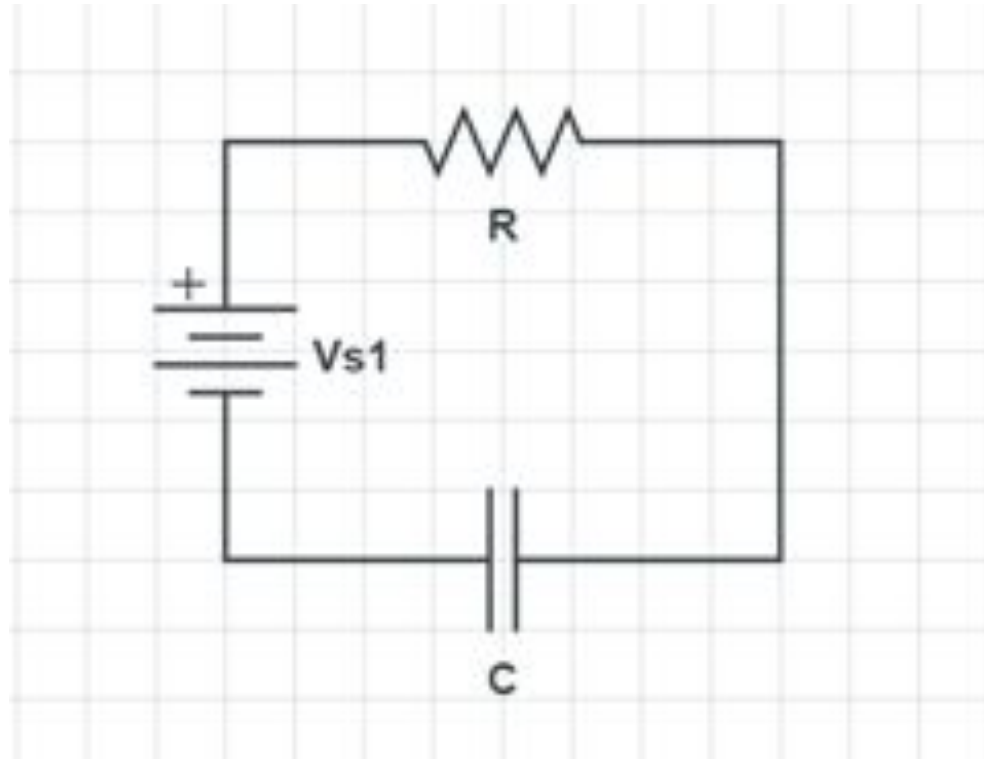
By Euler's method,

$$\mathbf{V_c(n+1) = V_c(n) + \Delta t \times \frac{V_{s1} - V_{s2} - V_c(n)}{R \times C}}$$

$$\mathbf{I = \frac{V_{s1} - V_{s2} - V_c(t)}{R}}$$

In this case, let voltage across the resistor, capacitor be V_{r_out} and V_{c_out} . Let the total current flowing in the circuit be I_out .

With source voltage V_{s1}



By, Kirchhoff's voltage law [Sum of voltage around any closed loop is zero],

$$V_{s1} - V_r - V_c(t) = 0$$

$$V_r = V_{s1} - V_c(t) \rightarrow (ii)$$

Use (ii) in (i),

$$V_c'(t) = \frac{V_{s1} - V_c(t)}{R \times C}$$

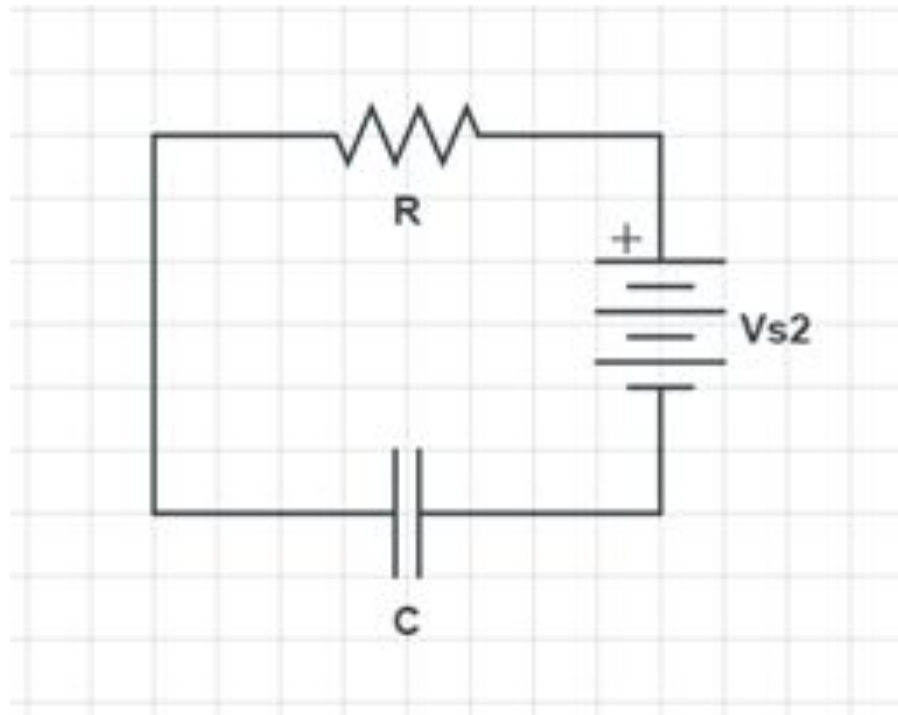
By Euler's method,

$$V_c(n+1) = V_c(n) + \Delta t \times \frac{V_{s1} - V_c(n)}{R \times C}$$

$$I_1 = \frac{V_{s1} - V_c(t)}{R}$$

In this case, let voltage across the resistor, capacitor be V_{r_out1} and V_{c_out1} . Let the total current flowing in the circuit be I_1 .

With source voltage $V_{s2'}$



By, Kirchhoff's voltage law (Sum of voltage around any closed loop is zero)

$$-V_{s2} - V_r - V_c(t) = 0$$

$$V_r = -V_{s2} - V_c(t) \rightarrow (ii)$$

Use (ii) in (i),

$$V_c'(t) = \frac{-V_{s2} - V_c(t)}{R \times C}$$

By Euler's method,

$$V_c(n+1) = V_c(n) + \Delta t \times \frac{-V_{s2} - V_c(n)}{R \times C}$$

$$I_2 = \frac{-V_{s2} - V_c(t)}{R}$$

In this case, let voltage across the resistor, capacitor be V_{r_out2} and V_{c_out2} . Let the total current flowing in the circuit be I_2 .

By super-position theorem,

$$V_{c_out} = V_{c_out1} + V_{c_out2}$$

$$V_{r_out} = V_{r_out1} + V_{r_out2}$$

$$I_{out} = I_1 + I_2$$

MATLAB code for computation

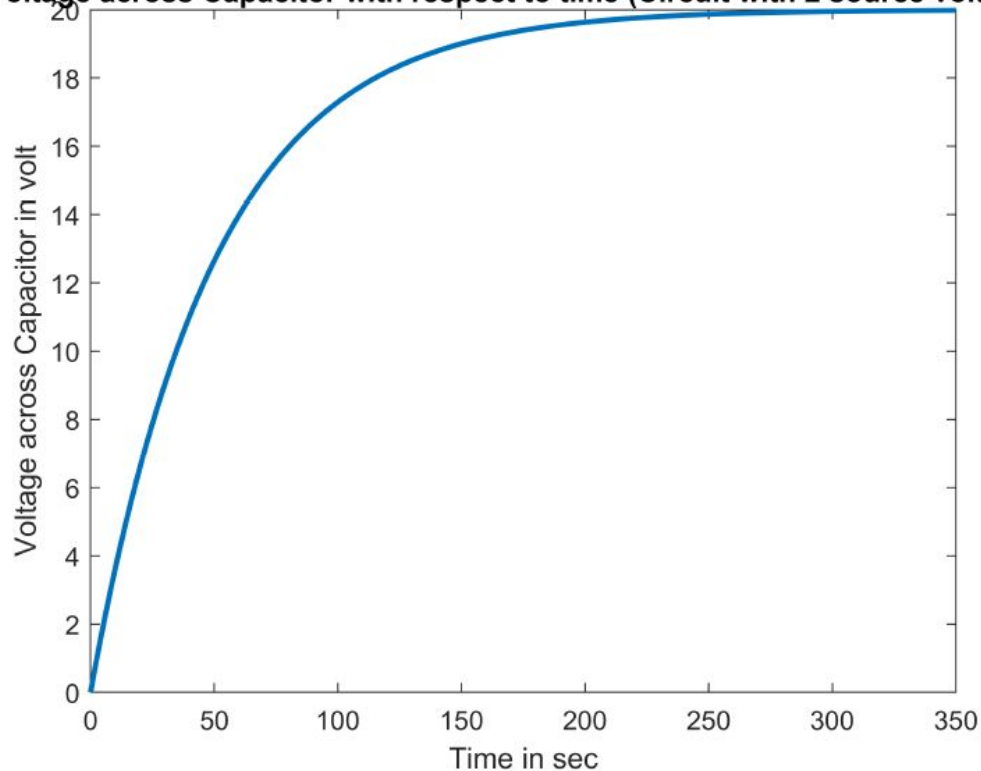
```
clc;
clear all;
close all;

R = 5;
C = 10;
time_constant = R * C;
% To get a smooth graph we here take 7 times the time constant
% Actually steady state is achieved at 5 times the time constant
T = 7 * time_constant;
dt = 0.01;
t = 0:dt:T;
Vs1 = 30;
Vs2 = 10;
Vc(1) = 0;

for n = 1:(length(t)-1)
Vc(n+1) = Vc(n) + dt*((Vs1 - Vs2 - Vc(n))*(1/(R*C)));
end
Vr = Vs1 - Vs2 - Vc;
I = (Vs1 - Vs2 - Vc) / R;
```

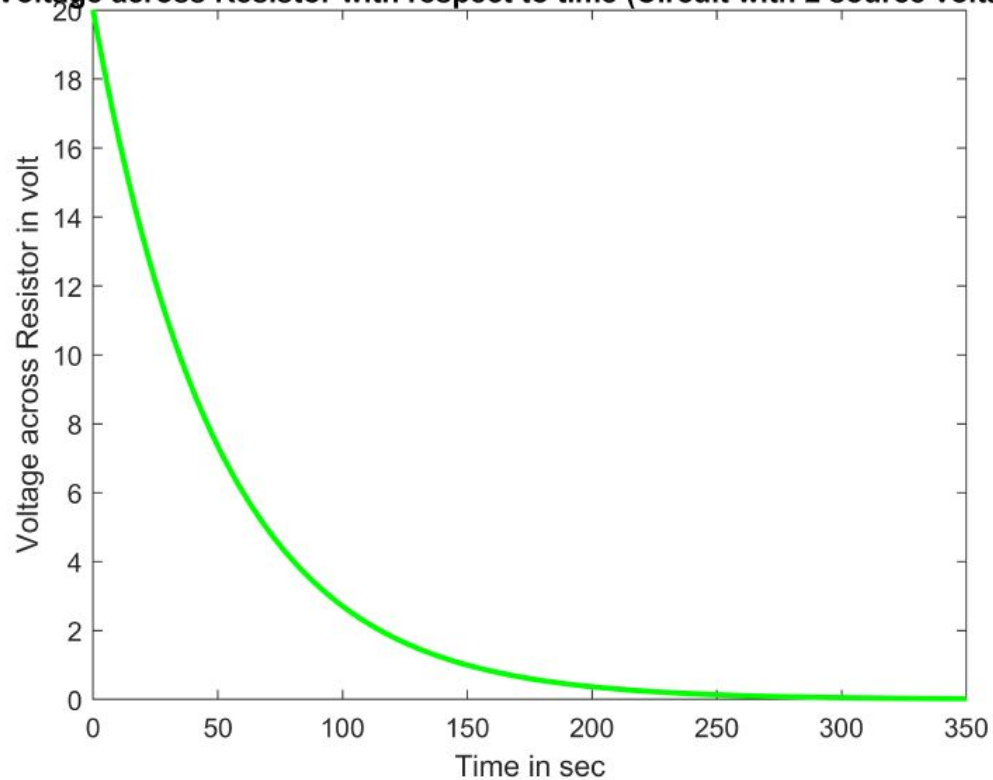
```
% Plotting the graph  
plot(t,Vc,"LineWidth",2)  
title("Voltage across Capacitor with respect to time (Circuit with 2 source voltages)")  
xlabel("Time in sec")  
ylabel("Voltage across Capacitor in volt")
```

Voltage across Capacitor with respect to time (Circuit with 2 source voltages)



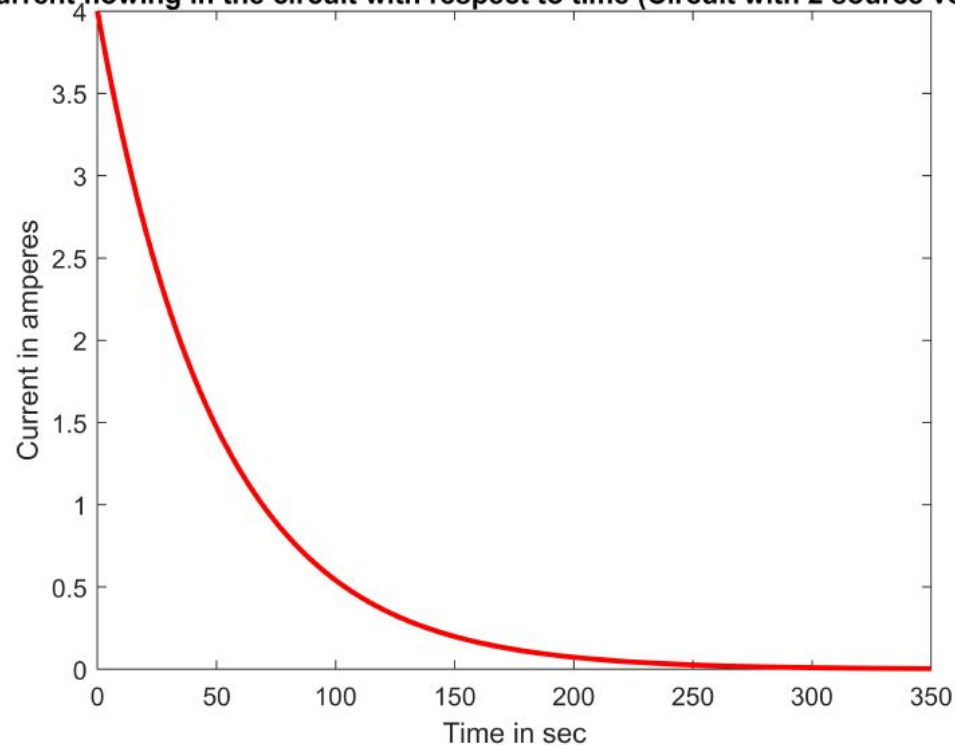
```
plot(t,Vr,"LineWidth",2,"Color",'green')  
title("Voltage across Resistor with respect to time (Circuit with 2 source voltages)")  
xlabel("Time in sec")  
ylabel("Voltage across Resistor in volt")
```

Voltage across Resistor with respect to time (Circuit with 2 source voltages)



```
plot(t,I,"LineWidth",2,"Color",'r')  
title("Current flowing in the circuit with respect to time (Circuit with 2 source voltages)")  
xlabel("Time in sec")  
ylabel("Current in amperes")
```

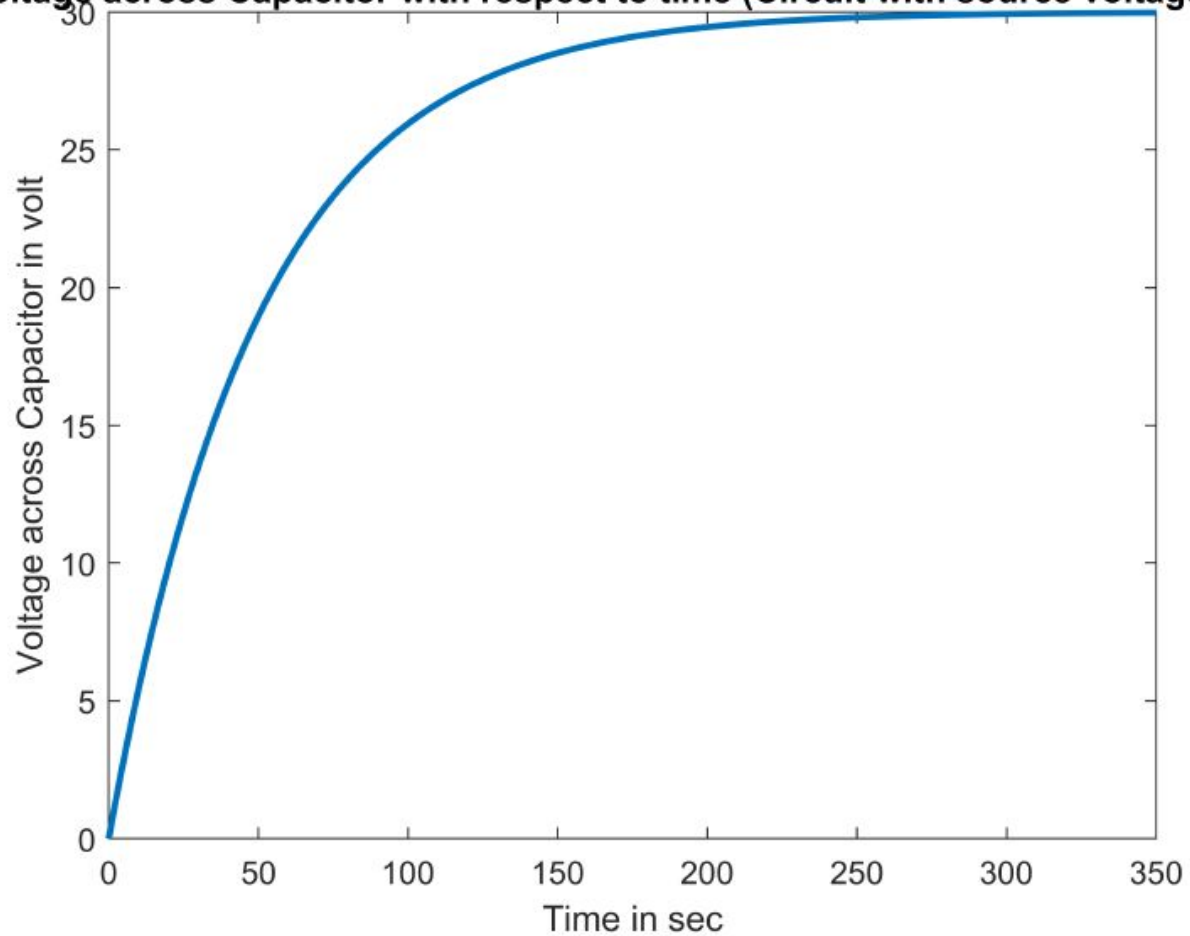
Current flowing in the circuit with respect to time (Circuit with 2 source voltage:



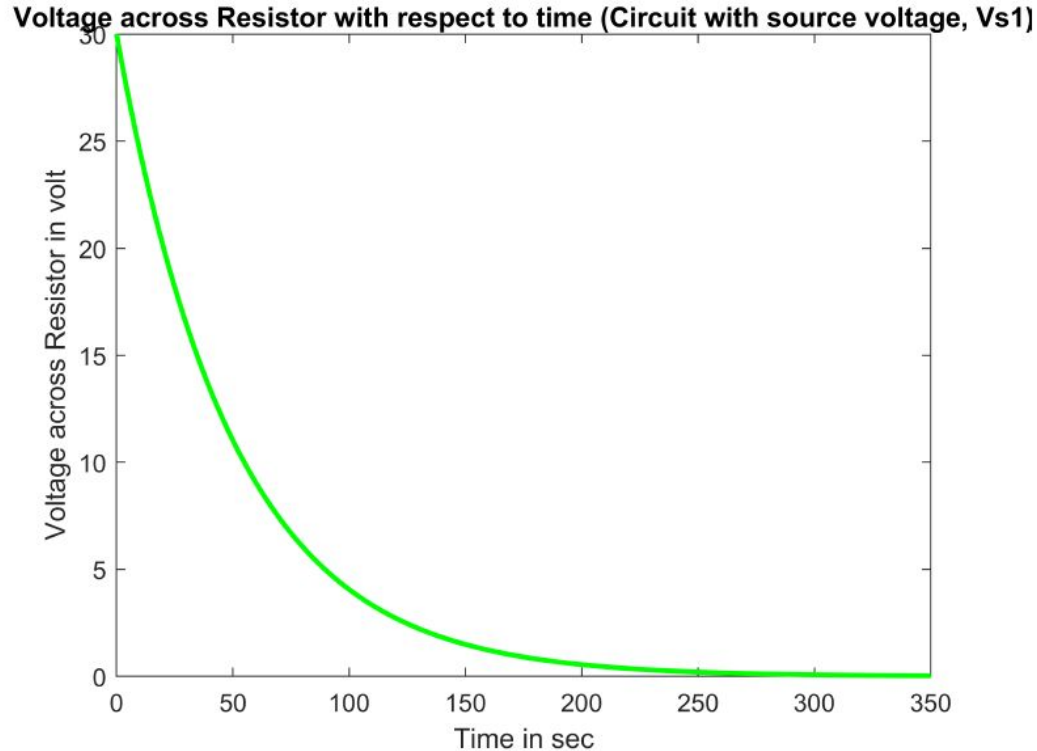
When one source voltage (Vs1) is alone connected

```
Vc_out1(1) = 0;  
for i = 1:(length(t)-1)  
    Vc_out1(i+1) = Vc_out1(i) + dt*((Vs1 - Vc_out1(i))*(1/(R*C)));  
end  
Vr_out1 = Vs1 - Vc_out1;  
I1 = (Vs1 - Vc_out1) / R;  
  
% Plotting the graph  
plot(t,Vc_out1,"LineWidth",2)  
title("Voltage across Capacitor with respect to time (Circuit with source voltage, Vs1)")  
xlabel("Time in sec")  
ylabel("Voltage across Capacitor in volt")
```

Voltage across Capacitor with respect to time (Circuit with source voltage, Vs1

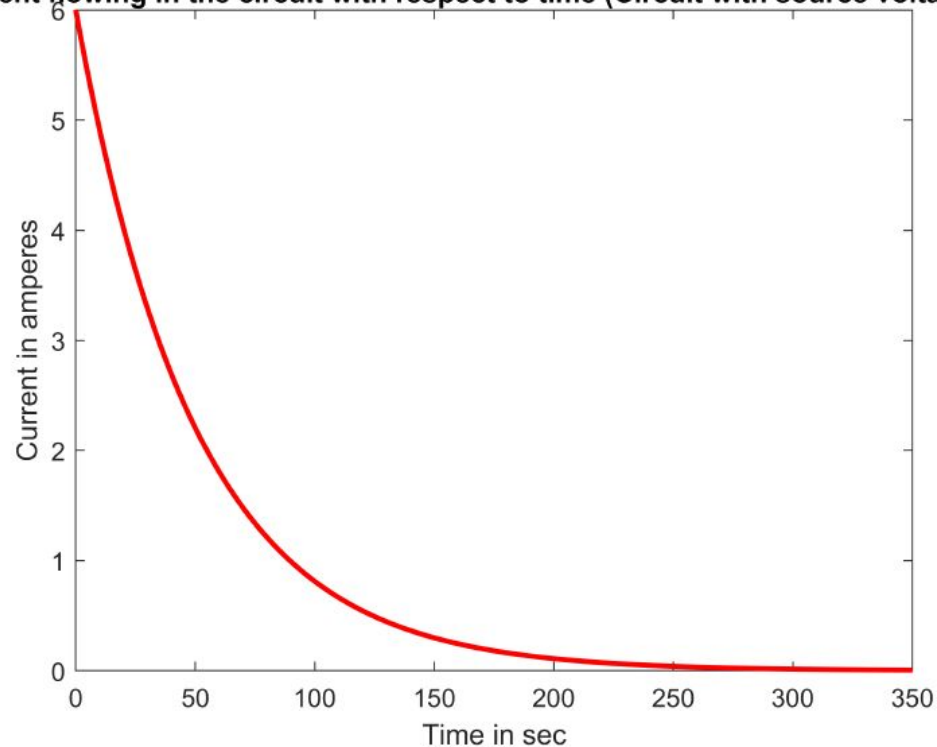



```
plot(t,Vr_out1,"LineWidth",2,"Color",'green')  
title("Voltage across Resistor with respect to time (Circuit with source voltage, Vs1)")  
xlabel("Time in sec")  
ylabel("Voltage across Resistor in volt")
```



```
plot(t,I1,"LineWidth",2,"Color",'r')  
title("Current flowing in the circuit with respect to time (Circuit with source voltage, Vs1)")  
xlabel("Time in sec")  
ylabel("Current in amperes")
```

Current flowing in the circuit with respect to time (Circuit with source voltage, Vs1)

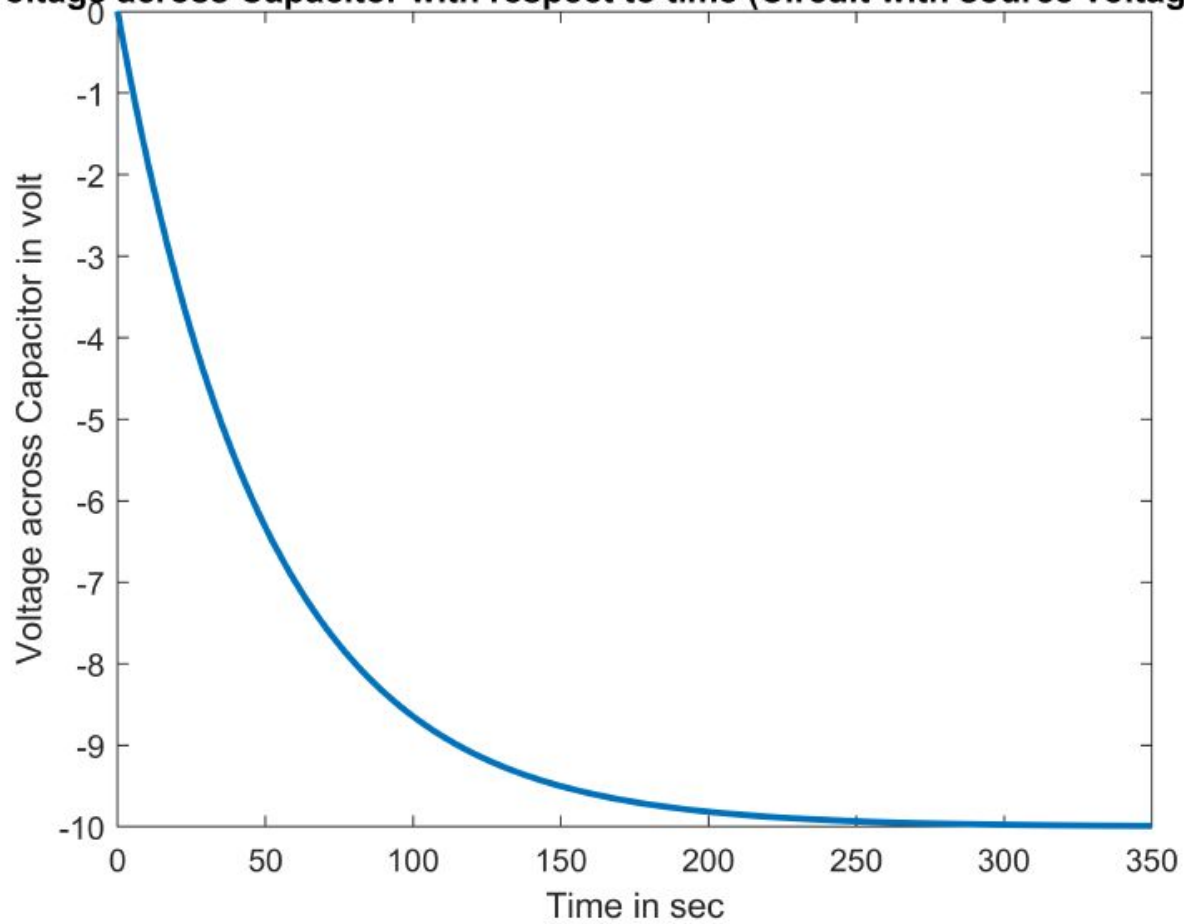


When one source voltage (V_{s2}) is alone connected

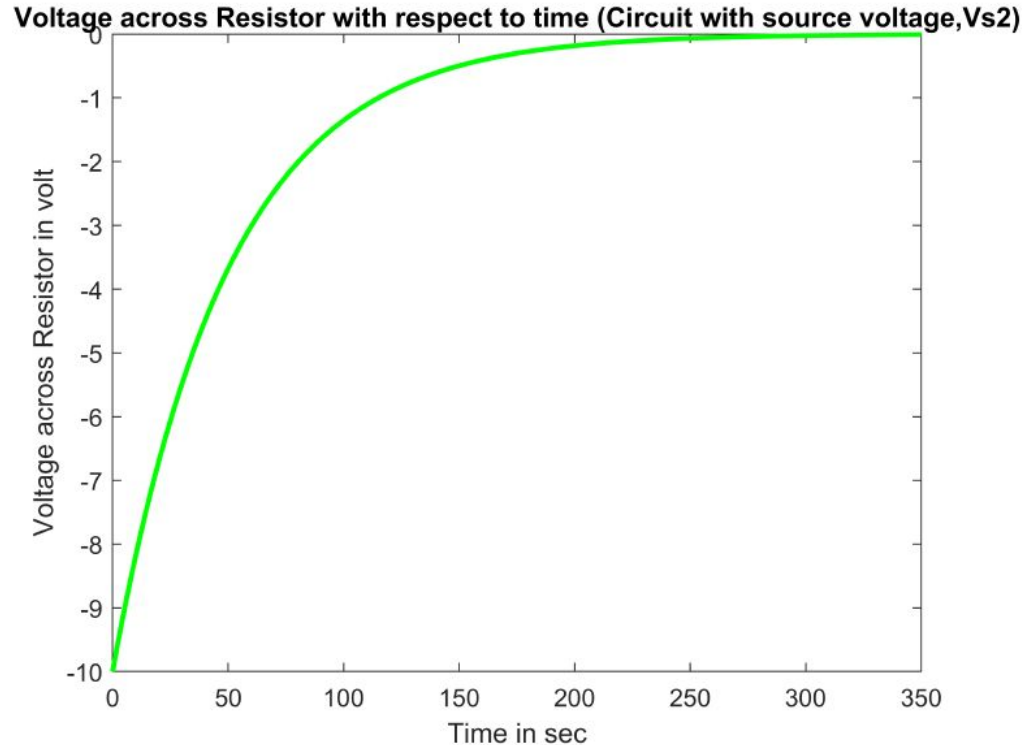
```
Vc_out2(1) = 0;
for j = 1:(length(t)-1)
    Vc_out2(j+1) = Vc_out2(j) + dt*((-Vs2 - Vc_out2(j))*(1/(R*C)));
end
Vr_out2 = -Vs2 - Vc_out2;
I2 = (-Vs2 - Vc_out2) / R;

% Plotting the graph
plot(t,Vc_out2,"LineWidth",2)
title("Voltage across Capacitor with respect to time (Circuit with source voltage,Vs2)")
xlabel("Time in sec")
ylabel("Voltage across Capacitor in volt")
```

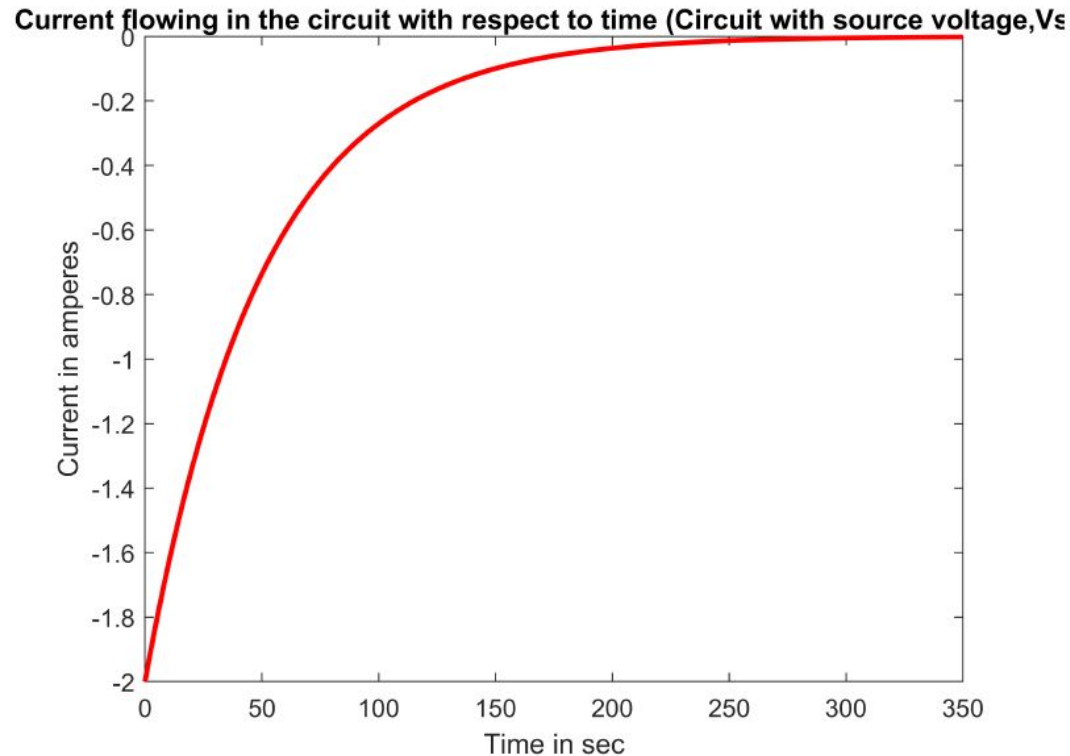
Voltage across Capacitor with respect to time (Circuit with source voltage, Vs2



```
plot(t,Vr_out2,"LineWidth",2,"Color",'green')  
title("Voltage across Resistor with respect to time (Circuit with source voltage,Vs2)")  
xlabel("Time in sec")  
ylabel("Voltage across Resistor in volt")
```



```
plot(t,I2,"LineWidth",2,"Color",'r')  
title("Current flowing in the circuit with respect to time (Circuit with source voltage,Vs2)")  
xlabel("Time in sec")  
ylabel("Current in amperes")
```



Negative voltage in a circuit is voltage that is more negative in polarity than the ground of the circuit.

A voltage source has positive or negative polarity depending on its orientation in a circuit. In the case when a voltage across an element has negative voltage, it just means the negative terminal of the voltmeter is connected to the positive side of the circuit and the positive terminal of the voltmeter is connected to the negative side of the circuit.

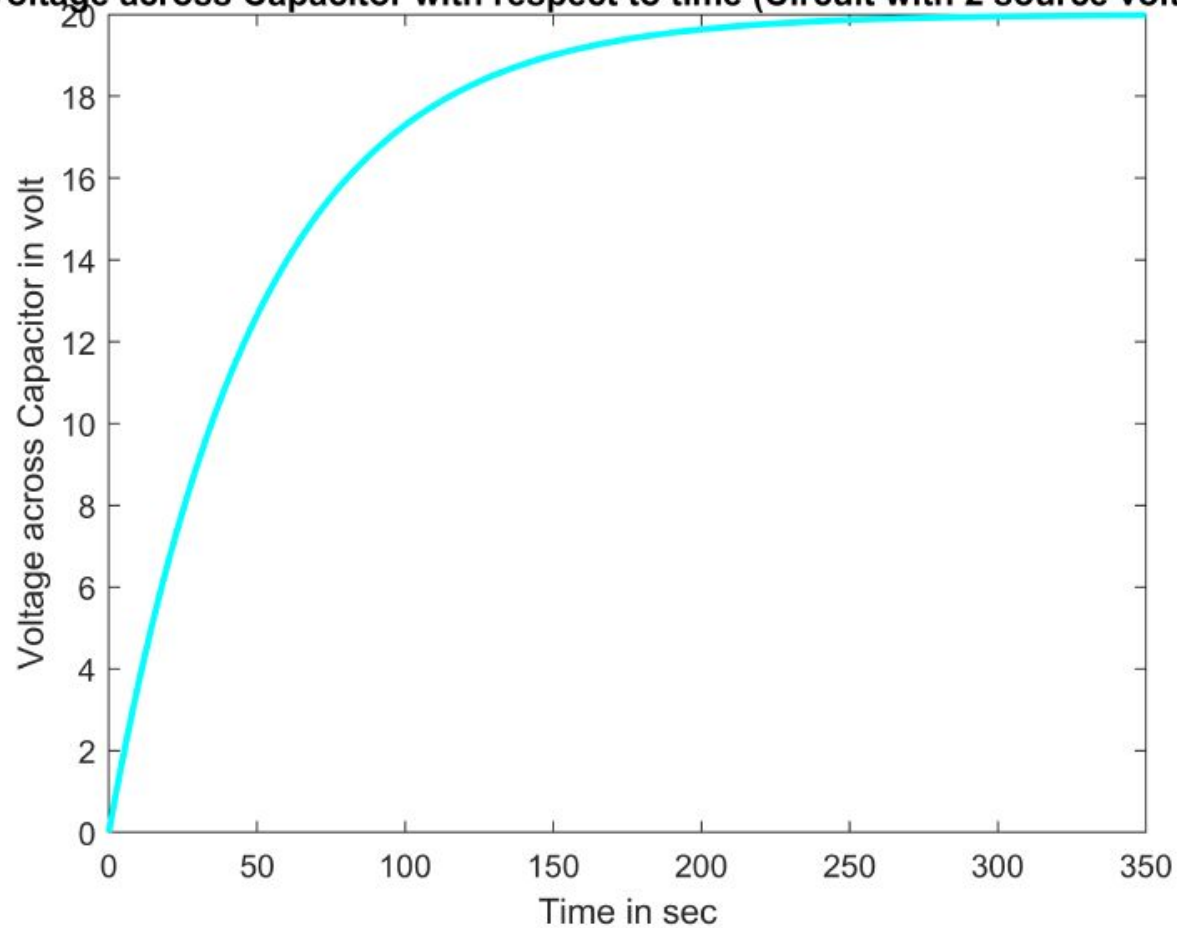
It just conveys the orientation, but do not make any effect.

The negative value of current also shows just the opposite direction of flow of current in the circuit. Negative sign tells the direction and not affect magnitude in any way.

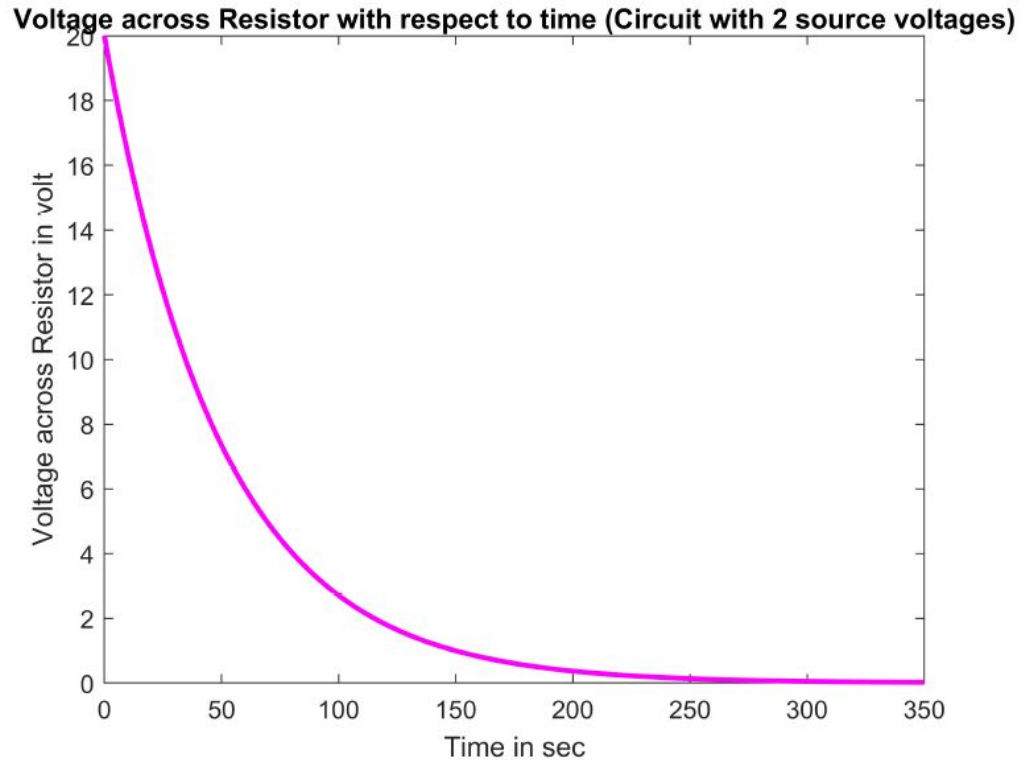
Thus, on summing both the functions, as per the super_position theorem,

```
Vc_out = Vc_out1 + Vc_out2;  
Vr_out = Vr_out1 + Vr_out2;  
I_out = I1 + I2;  
  
plot(t,Vc_out,"LineWidth",2,"Color",'c')  
title("Voltage across Capacitor with respect to time (Circuit with 2 source voltages)")  
xlabel("Time in sec")  
ylabel("Voltage across Capacitor in volt")
```

Voltage across Capacitor with respect to time (Circuit with 2 source voltages)

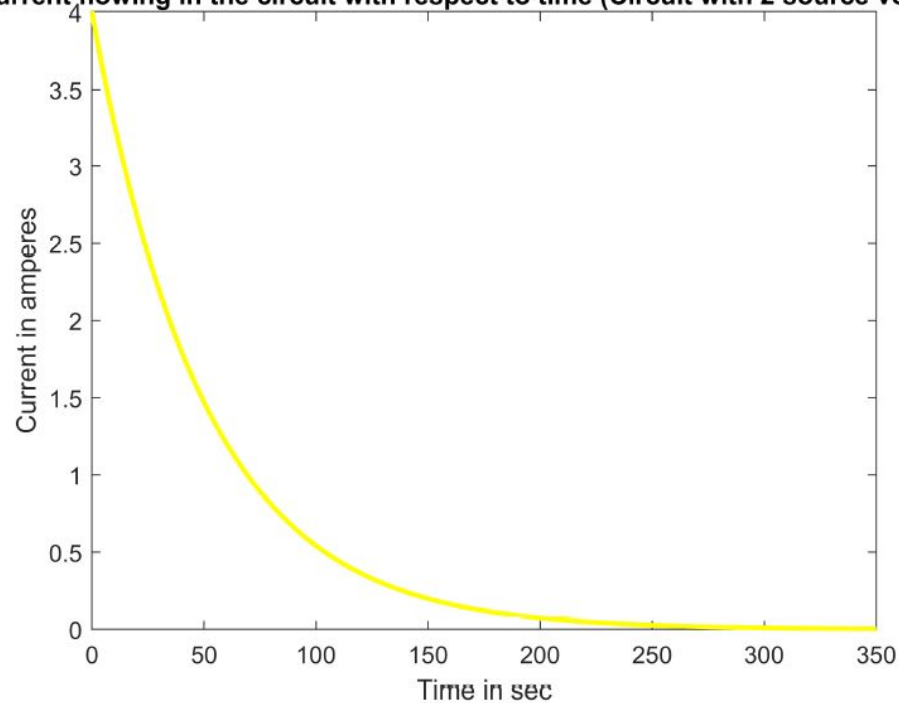



```
plot(t,Vr_out,"LineWidth",2,"Color",'m')
title("Voltage across Resistor with respect to time (Circuit with 2 source voltages)")
xlabel("Time in sec")
ylabel("Voltage across Resistor in volt")
```



```
plot(t,I_out,"LineWidth",2,"Color",'y')  
title("Current flowing in the circuit with respect to time (Circuit with 2 source voltages)")  
xlabel("Time in sec")  
ylabel("Current in amperes")
```

Current flowing in the circuit with respect to time (Circuit with 2 source voltage:



INFERENCE

We can observe that the sum of individual output voltages is equal to the output voltage when both source voltages (30 V and 10 V) are connected in the circuit.

- For $V_{in} = 30V$ and $10V$, we get output voltage across resistor and capacitor as V_{r_out} and V_{c_out} and current flowing through the circuit is I_{out} .
- For $V_{in} = 30V$, we get output voltage across resistor and capacitor as V_{r_out1} and V_{c_out1} and current flowing through the circuit is I_{out1} .
- For $V_{in} = 10V$, we get output voltage across resistor and capacitor as V_{r_out2} and V_{c_out2} and current flowing through the circuit is I_{out2} .

We observe that:

- $V_{r_out} = V_{r_out1} + V_{r_out2}$
- $V_{c_out} = V_{c_out1} + V_{c_out2}$
- $I_{out} = I_{out1} + I_{out2}$

Hence, the superposition theorem is proved.

SUMMARY OF THE ENTIRE EXPERIMENT

REFERENCES

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- <https://www.falstad.com/circuit/directions.html>
- <https://byjus.com/>

Thank you