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# MicroCash: Practical Concurrent Processing of Micropayments

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# Outline

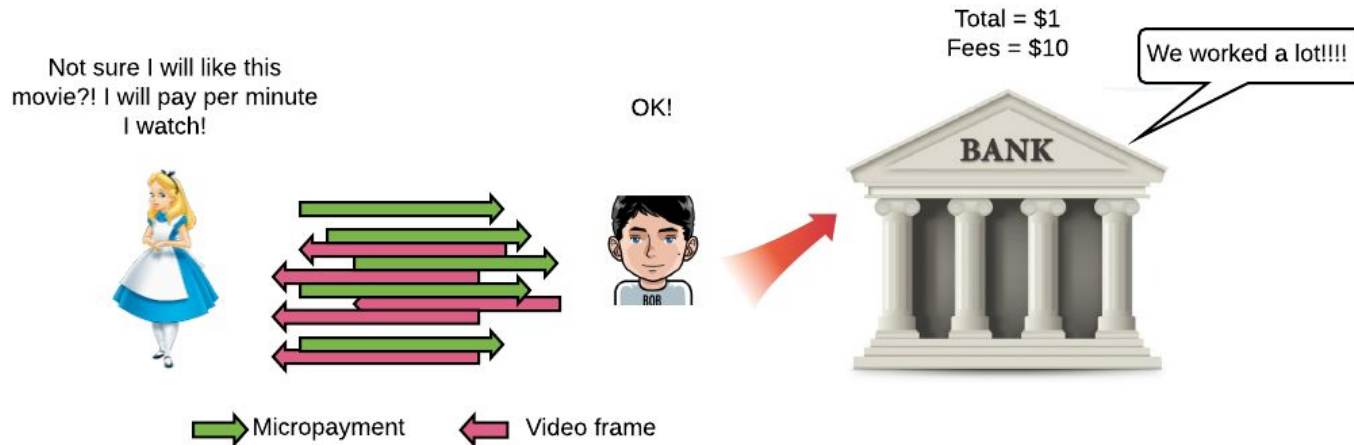
- Background.
- Motivation.
- MicroCash design.
  - Escrow setup.
  - Paying with lottery tickets.
  - Lottery protocol.
  - Claiming payments.
  - Proof of cheating and the penalty deposit.
- Security analysis.
- Performance evaluation.
- Conclusion.

# Micropayments

"MICROPAYMENTS ARE BACK, AT LEAST IN THEORY, THANKS TO P2P" \*

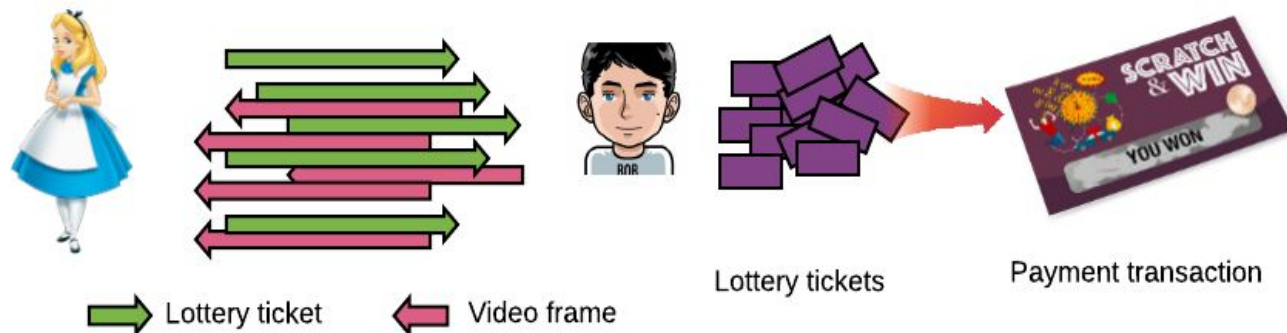


- Payments of micro values (pennies or fractions of pennies).
- Several potential applications.
  - Ad-free web surfing, online gaming, and rewarding peers in peer-assisted services.
- **Drawbacks**; high transaction fees and large log size.



# Probabilistic Micropayments

- A solution to aggregate tiny payments.
- Dated back to Rivest [Rivest, 1997] and Wheeler [Wheeler, 1996].



- Early implementations were centralized.
- Cryptocurrencies are utilized to achieve decentralization.

# Decentralized Probabilistic Micropayments

- Ingredients:
  - Trusted bank  $\Rightarrow$  Miners.
  - Bank accounts to hold payments  $\Rightarrow$  Escrows on the blockchain.
  - Distributed lottery protocol.
- Main challenges:
  - Ticket duplication (pay several parties the same lottery ticket).
  - Front running attacks.
- Prior work.
  - Only two schemes: **MICROPAY** [Pass et al., 2015] and **DAM** [Chiesa et al., 2017]

# Prior Work Limitations

- Support only **sequential** micropayments.
  - High latency, large number of escrows (more fees and larger blockchain size).
- Interactive lottery protocol.
  - Require **several rounds** of communication to exchange a lottery ticket.
- Chances of having all, or no, tickets win.
  - Psychological obstacle as a customer may pay more than expected.
- Computationally-heavy.

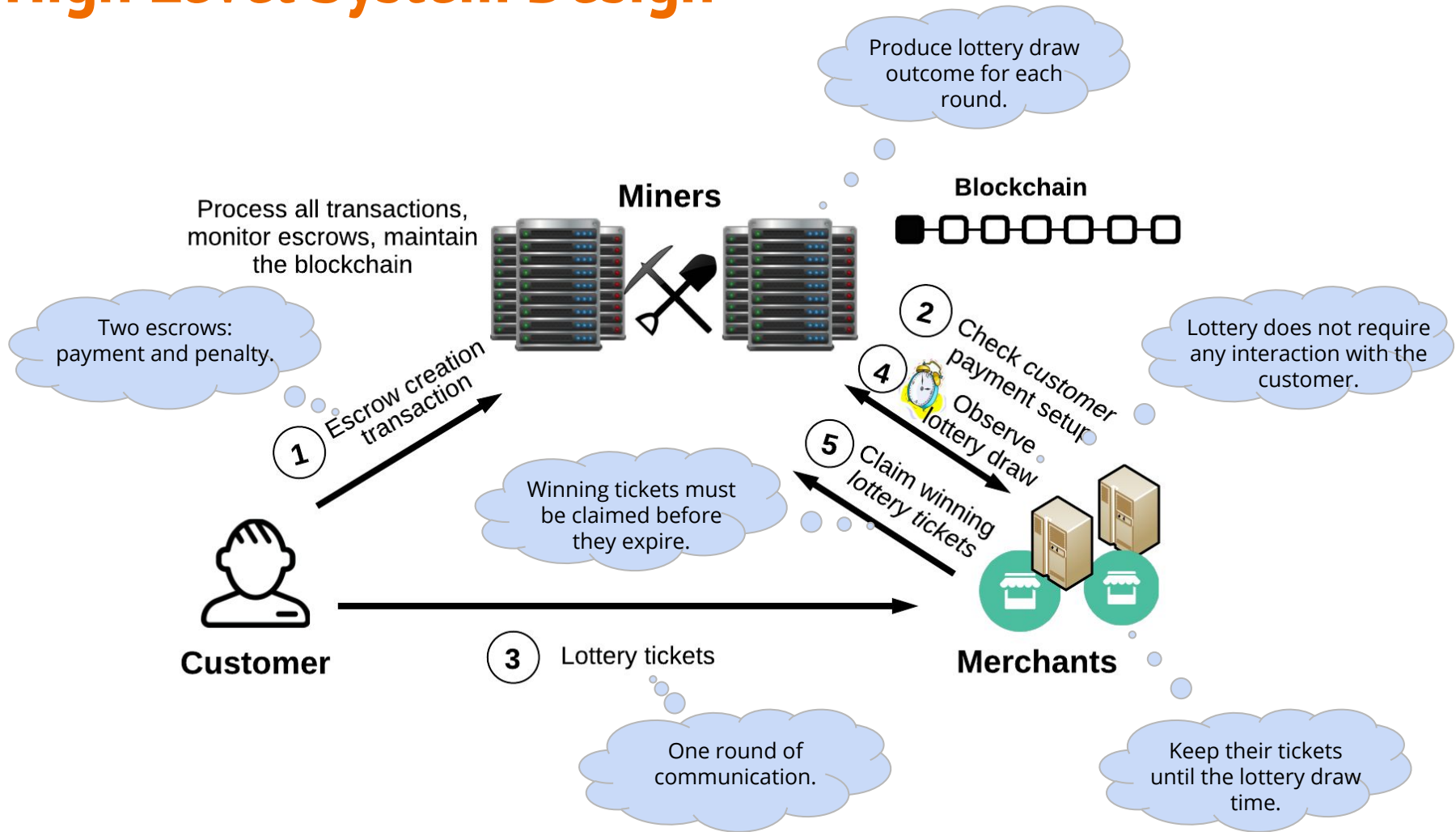


MicroCash  
addresses these  
limitations!!

# MicroCash Overview

- The ***first*** decentralized probabilistic micropayment scheme that supports **concurrent micropayments**.
- Requires ***one*** round of communication to exchange a ticket.
  - Introduces a non-interactive and lightweight lottery protocol based solely on secure hashing.
- The ***first*** to introduce a lottery protocol with ***exact win rate***.
- Reduces the amount of data to be logged on the blockchain by around **50%** (compared to sequential micropayment schemes).
- Increases ticket processing rate by **1.7 - 4.2x** (compared to MICROPAY).

# High Level System Design





# Escrows and Micropayment Concurrency

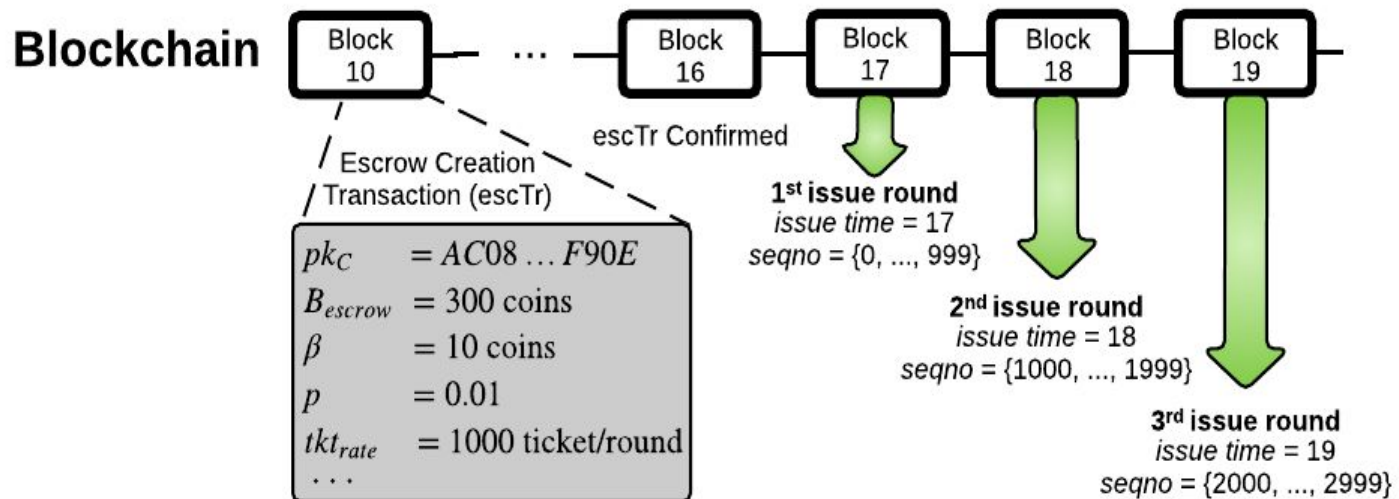
- The payment escrow balance covers all winning tickets.
  - A winning probability  $p$ , ticket issue rate  $tk_{rate}$ , lottery round length  $draw_{len}$ , and escrow lifetime  $I_{esc}$ .
  - Each lottery round there are  $p \cdot tk_{rate} \cdot draw_{len}$  winning tickets, each with value  $\beta$  coins, then the payment escrow balance is  $\beta \cdot p \cdot tk_{rate} \cdot draw_{len}$ .
- Track tickets in the system based on their sequence numbers.
- Miners control escrows in the system.
- Each escrow must identify a set of beneficiary merchants.
- A customer can create an escrow that is sufficient to pay merchants for days.

# Lottery Ticket Issuance

- Each ticket is a simple structure consist of:

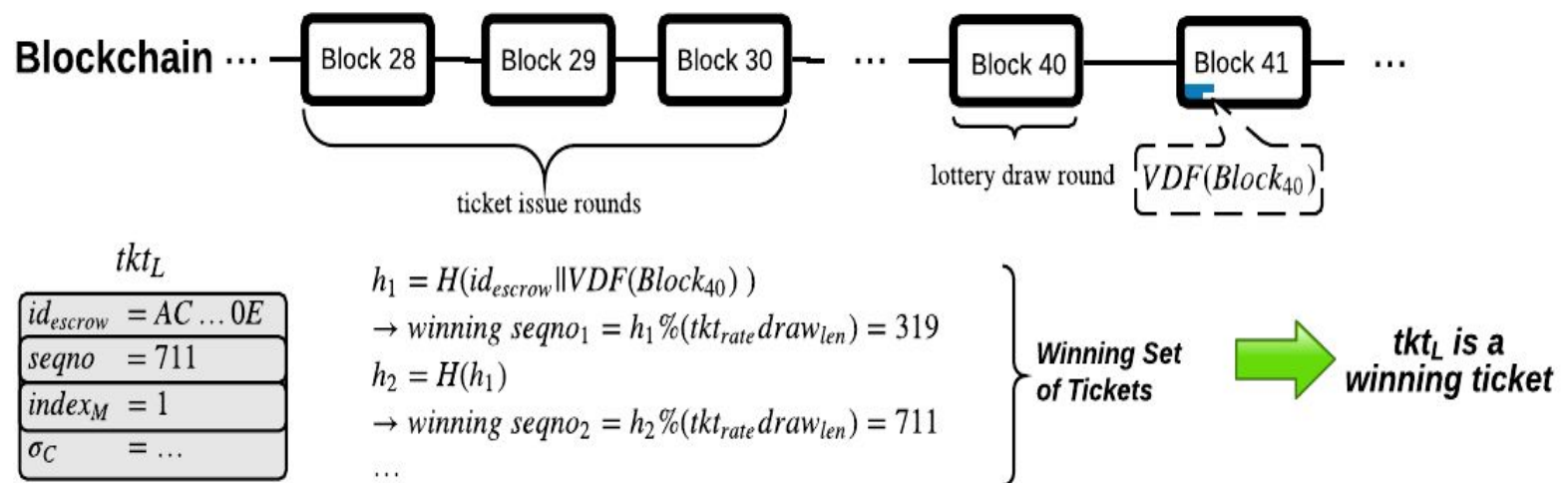
$$tkt_L = id_{esc} || index_M || seqno || \sigma_C$$

- Ticket issuance must follow a ticket issuing schedule.



# The lottery Protocol

- Lightweight, non-interactive, and supports exact win rate.
  - Based on the blockchain view and requires only secure hashing.



- Merchants claim their winning tickets through the miners within the ticket redemption period.

# Proof-of-cheating Processing

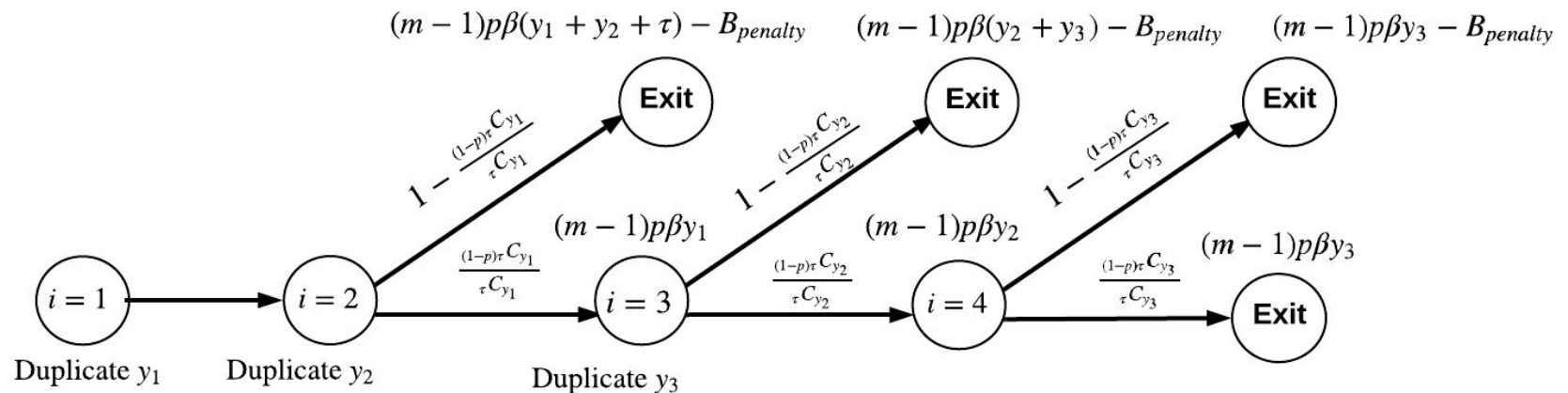
- Any party can issue a proof-of-cheating against the customer if it detects:
  - Duplicate ticket issuance.
  - Issuing more tickets with out-of-range sequence numbers.
- The miners burn the customer's penalty deposit.
  - This deposit must be large enough to make cheating unprofitable.
  - Its lower bound is derived using a game theoretic analysis of MicroCash setup.

# Penalty Deposit I

- Equals at least the additional utility gain a malicious customer obtains over an honest.
- Intuitively, it is the expected amount of payments a customer would pay for  $(m-1)$  merchants (at max ticket issuance rate) during the cheating detection period.
  - A duplicated ticket is detected after it wins the lottery and is claimed by the merchants.
  - Thus, the cheating detection period covers the lottery period and the ticket redemption period.

# Penalty Deposit II

Its lower bound is derived using a game theoretic analysis that models the system as a repeated game and tracks its evolution over time.



$$\mathbb{E}_k[u(\hat{C})] = \left(1 - \frac{(1-p)\tau C_{y1}}{\tau C_{y1}}\right) \left((m-1)p\beta \sum_{i=1}^d y_i + (m-1)p\beta r\tau - B_{\text{penalty}}\right) +$$

$$\left(\frac{(1-p)\tau C_{y1}}{\tau C_{y1}}\right) \left((m-1)p\beta y_1 + \mathbb{E}_{k-1}[u(\hat{C})]\right)$$

# Penalty Deposit III

But  $\mathbb{E}_{k-1}[u(\hat{C})] \leq 0$  and  $\mathbb{E}_k[u(\hat{C})] \leq 0$ , hence:

$$B_{penalty}(y_1, \dots, y_d) > (m-1)p\beta \left( \frac{y_1}{1 - \frac{(1-p)\tau^{C_{y_1}}}{\tau^{C_{y_1}}}} + \sum_{i=2}^d y_i + r\tau \right)$$

The above is maximized when  $y_i = (1-p)\tau$  for  $i \in \{1, \dots, d\}$ , thus:

$$B_{penalty} > (m-1)p\beta tkt_{rate} draw_{len} \left( \frac{1-p}{1-\rho^{-1}} + draw_{len} \left( (1-p)(d_{draw} - 1) + d_{redeem} \right) \right)$$

# MicroCash Security Properties

- Prevents **escrow overdraft**.
  - Front running attacks are not possible.
  - Ticket tracking prevent issuing more tickets than what can be covered.
- Prevents **escrow-withholding**.
  - An escrow will be refunded once all tickets expire.
- Prevents **manipulating the lottery** outcome.
  - Achieved by the use of VDFs and ticket issuing schedule.
- Addresses **duplicated ticket issuance**.
  - Using detect-and-punish approach.



# MicroCash Efficiency - MicroBenchmarks I

- **Ticket processing rate** (ticket / sec):

| Scheme           | ECDSA (secp256k1) | ECDSA (P-256) | EdDSA (Ed25519) |
|------------------|-------------------|---------------|-----------------|
| <b>MICROPAY</b>  |                   |               |                 |
| Customer         | 1,859             | 32,471        | 26,238          |
| Merchant         | 1,328             | 2,399         | 2,561           |
| Miner            | 1,340             | 2,448         | 2,617           |
| <b>MicroCash</b> |                   |               |                 |
| Customer         | 1,868             | 33,006        | 26,749          |
| Merchant         | 2,249             | 10,505        | 8,473           |
| Miner            | 2,241             | 10,345        | 8,368           |

Merchants and miners in MicroCash are **1.7x, 4.2x, and 3.2x** faster than in MICROPAY (for the three digital signature schemes shown above).

# MicroCash Efficiency - MicroBenchmarks II

- **Bandwidth cost (in terms of ticket size):**
  - From customer to merchant; 274 bytes (MICROPAY), 110 byte (MicroCash, around **60% reduction**).
  - From merchant to miner; 355 byte (MICROPAY), 110 bytes (MicroCash, around **70% reduction**).
- **Number of escrows:**
  - MICROPAY needs **60, 1019, and 653 escrows** to support the rates reported previously.
  - MicroCash needs only ***one escrow***.

# In Real World Applications - Online Gaming

| Metric                                    | Bitcoin   | MICROPAY    | MicroCash  |
|---|-----------|-------------|------------|
| Winning tickets / sec                     | N/A       | 0.000167    | 0.000167   |
| Escrows / sec                             | N/A       | 0.000552    | 0.000386   |
| Transactions /sec                         | 16.67     | 0.000719    | 0.000552   |
| Transaction fees / round                  | \$680     | \$0.029341  | \$0.022541 |
| Bandwidth between customers and miners    | 3,333 bps | 1.105 bps   | 1.009 bps  |
| Bandwidth between customers and merchants | N/A       | 36,533 bps  | 14,667 bps |
| Bandwidth between merchants and miners    | N/A       | 0.807 bps   | 0.523 bps  |
| Delta blockchain size / round             | 2.38 MB   | 0.000137 MB | 0.00011 MB |

- **Bitcoin:** Average transaction fee is \$0.068, and average transaction size is 250 bytes.
- **Minecraft:** 125 servers, each serving 8 players. Cost is \$12 per 8 players per month.
  - With 2% overhead percentage,  $p = 0.00001$
  - Each player pay one ticket per minute.

# In Real World Applications - P2P CDNs

| Metric                                    | Bitcoin     | MICROPAY    | MicroCash   |
|---|-------------|-------------|-------------|
| Winning tickets / sec                     | N/A         | 0.001964    | 0.001964    |
| Escrows / sec                             | N/A         | 0.001976    | 0.000012    |
| Transactions /sec                         | 128         | 0.00394     | 0.001976    |
| Transaction fees / round                  | \$5,222     | \$0.160769  | \$0.08062   |
| Bandwidth between customers and miners    | 256,000 bps | 3.95 bps    | 0.165 bps   |
| Bandwidth between customers and merchants | N/A         | 280,576 bps | 112,640 bps |
| Bandwidth between merchants and miners    | N/A         | 9.508 bps   | 6.16 bps    |
| Delta blockchain size / round             | 18.31 MB    | 0.000963 MB | 0.000452 MB |

- **CDN:** one publisher serving 1 Gpb, cost is \$0.01, each cache gets a ticket per 1 MB it serves..
  - With 2% overhead percentage,  $p = 0.000023$
  - Issues 128 tickets per second

# Conclusions

- Micropayments have a large number of potential applications.
  - Cryptocurrencies provided a template to recast centralized probabilistic micropayments into distributed ones.
- Microcash is the first distributed probabilistic micropayment scheme that supports concurrent micropayments with exact win lottery protocol.
- It is also efficient, its non-interactive lottery requires only one round of communication and relies only on secure hashing.
- Results confirm its variability to be used in large-scale distributed systems.

**Thank You!**

***Questions?***

# References

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