

# Linear Regression

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The goal of Linear Regression is to model a linear relationship between an independent (X) and a dependent (Y) variable. If we know the petal width can we estimate the petal length? (The iris dataset is installed as part of the base R installation and can therefore be referenced directly, as in the sample code for this section.)

First, fit a linear model.

```
model <- lm(iris$Petal.Length ~ iris$Petal.Width)
```

Summarize the model.

```
summary(model)

##
## Call:
## lm(formula = iris$Petal.Length ~ iris$Petal.Width)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.33542 -0.30347 -0.02955  0.25776  1.39453
##
## Coefficients:
##              Estimate Std. Error t value
## (Intercept)    1.08356    0.07297   14.85
## iris$Petal.Width 2.22994    0.05140   43.39
##              Pr(>|t|)
## (Intercept)    <2e-16 ***
## iris$Petal.Width <2e-16 ***
## ---
## Signif. codes:
##  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.4782 on 148 degrees of freedom
## Multiple R-squared:  0.9271, Adjusted R-squared:  0.9266
## F-statistic: 1882 on 1 and 148 DF, p-value: < 2.2e-16
```

So, our predictive equation is:

$$\text{Petal Length} = 1.08356 + 2.22994(\text{Petal Width})$$

These results tell us that:

- the intercept is significantly different than 0 ( $P < 0.05$ )
- the slope is significantly different than 0 ( $P < 0.05$ )
- the model is a good fit for the data ( $R^2 = 0.9271$ ). This means that 93% of the variation in petal length is explained by the petal width.

We can also add a linear regression line directly in the plot of the two variables:

```
# par(mar=(c(5,4,4,2)))
plot(iris$Petal.Width, iris$Petal.Length, main = "Petal Width vs. Length",
      xlab = "Petal Width", ylab = "Petal Length")
abline(model)
```

## Petal Width vs. Length

