

Functional and logic programming

- written exam -

Important:

1. Subjects are graded as follows: of - 1p; A – 1.5p; B - 2.5p; C - 2.5p; D - 2.5p.
2. Prolog problems will be resolved using SWI Prolog. The following are required: (1) explanation of the code and of the reasoning behind it; (2) recursive model that solves the problem, for all the predicates used; (3) specification of every predicate (parameters and their meaning, flow model, type of the predicate - deterministic/non-deterministic).
3. Lisp problems will be resolved using Common Lisp. The following are required: (1) explanation of the code and of the reasoning behind it; (2) recursive model that solves the problem, for each function used; (3) specification of every function (parameters and their meaning).

A. The following function definition in LISP is given

```
(DEFUN F(N)
  (COND
    ((= N 1) 1)
    (> (F (- N 1)) 2) (- N 2))
    (> (F (- N 1)) 1) (F (- N 1)))
    (T (- (F (- N 1)) 1))
  )
)
```

Rewrite the definition in order to avoid the repeated call **(F (- N 1))**. Do NOT redefine the function. Do NOT use SET, SETQ, SETF. Justify your answer.

B. For two lists that represent numbers digit by digit, we define the operation of rearranging in the following way: we compare the digits and form two new lists, one with the greater digits, and one with the smaller digits. For example, rearranging lists [1,4,2,7] and [8,2,9,6,1] will return [8, 2, 9, 6, 7] and [1, 4, 2, 1]. Given two lists that contain numbers and sublists of digits, write a SWI-Prolog program that returns two lists with sublists containing the result after rearranging the sublists in the two lists. One of the lists contains the sublists with greater digits and the other the sublists with smaller digits. The two input lists have the same number of sublists, but not necessarily on the same positions. For example, for the lists [1, 2, [6, 2, 4], 6, [9, 9, 1, 1], 17, 9, [5, 3, 8, 1, 9]] and [1, 2, 3, [1, 5], 7, 11, [8, 3], 7, 5, [9, 4, 2, 5], 77] the result will be [[6, 2, 5], [9, 9, 8, 3], [5, 9, 8, 2, 9]] and [[1, 4], [1, 1], [3, 4, 1, 5]].

C. Write a PROLOGO program that generates the list of arrangements of k elements from a list of integer numbers, having the given product P . Write the mathematical models and flow models for the predicates used. For example, for the list $[2, 5, 3, 4, 10]$, $k=2$ and $P=20 \Rightarrow [[2,10],[10,2],[5,4],[4,5]]$ (not necessarily in this order).

D. Given a nonlinear list, write a Lisp function to return the list with all occurrences of an element **e** removed. **A MAP function shall be used.**

Example **a)** if the list is (1 (2 A (3 A)) (A)) and **e** is A => (1 (2 (3)) NIL)

b) if the list is (1 (2 (3))) and **e** is A => (1 (2 (3)))