Functional and logic programming
- **written exam -**

Important:

1. Subjects are graded as follows: of - 1p; A – 1.5p; B - 2.5p; C - 2.5p; D - 2.5p.
2. Prolog problems will be resolved using SWI Prolog. The following are required: (1) explanation of the code and of the reasoning behind it; (2) recursive model that solves the problem, for all the predicates used; (3) specification of every predicate (parameters and their meaning, flow model, type of the predicate - deterministic/non-deterministic).
3. Lisp problems will be resolved using Common Lisp. The following are required: (1) explanation of the code and of the reasoning behind it; (2) recursive model that solves the problem, for each function used; (3) specification of every function (parameters and their meaning).

A. The following function definition in LISP is given

```
(DEFUN F(L)
        (COND
                ((NULL L) NIL)
                ((LISTP (CAR L)) (APPEND (F (CAR L)) (F (CDR L)) (CAR (F (CAR L)))))
                (T (LIST(CAR L)))
          )
 )
```

Rewrite the definition in order to avoid the double recursive call **(F (CAR L))**. Do NOT redefine the function. Do NOT use SET, SETQ, SETF. Justify your answer.

B. Given a list composed of integer numbers and sublists of integer numbers, write a SWI-Prolog program that verifies if all the elements of the list (including those in sublists) form a symmetrical sequence. For example, for the list [1, 5, [2,4], 7, 11, 25, [11, 7, 4], 2, 5, 1] the result will be true.

C. Given a list composed of integer numbers, generate in PROLOG the list of arrangements of N elements ending with an odd value and have the sum S given. Write the mathematical models and flow models for the predicates used. For example, for the list L=[2,7,4,5,3], N=2 and S=7 ⇒ [[2,5], [4,3]] (not necessarily in this order).

D. An n-ary tree is represented in Lisp as (node subtree1 subtree2 ...). Write a Lisp function to return the list of nodes on the given level **k**. The root level is assumed zero. **A MAP function shall be used.** ***Example*** for the tree (a (b (g)) (c (d (e)) (f)))
a) k=2 => (g d) **b)** k=5 => ()