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PROJECT ON: PROBABILITY DISTRIBUTION	-
AND ITS APPLICATIONS	e
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PREFACE:

The probability distributions are used to emplain many of variations observed in real life phenomenon and show how these can be described in simple numerical terms. The distribution shows the probability of an event in an experiment; the event could be testing of human memory, survival of patient of cancer of a protest, time before the next telephone call, the distance between mutations on DNA stands, the number of care passing through a certain point on road, the number of viruses that can affect a cell in cell culture and so on. The collection of more important facts about common distribution in statistical theory and practice would be useful to variety of scientific works and workers. The distribution can be discrete or continuous depending upon the random variable taken into consideration. for example, the number of objects one is able to remember in a memory test is discrete random variable whereas, the amount of rainfall measured

A discrete probability distribution is applicable to scenarios where the set of possible outcomes is discrete and the probabilities are encoded by a discrete list of probabilities of outcomes, known as probability mass function. On the other hand, continuous probability distribution is applicable to scenarios where the set of possible outcomes can take on values in continuous range. In this case, probabilities are typically described by a probability density function.

over certain period is a continuous variable.

PROBABILITY DISTRIBUTION:

various forms, such as by a probability mass function or a cumulative distribution function.

One of the most general descriptions, which applies for continuous and discrete variables, is by means of a probability function P: A > IR, whose input space A is related to the sample space, and

A probability distribution can be described in

gives a probability as its output.

The concept of probability function is made more rigorous by defining it as the element of a probability space (X, A, P).

cohere,

X is the set of possible outcomes

A is the set of all subsets ECX whose

probability can be measured.

and, P is the probability function, or probability measure, that assigns a probability to

each of these measurable subjets FEA

PROBABILITY MASS FUNCTION:

Probability mass function is the probability distribution of a discrete vandom variable, and provides the possible values and their associated probabilities. It is the function $p: \mathbb{R} \to [0,1]$ defined by $px(x_i) = p(x_i) = p(x_i)$; for $-\infty<\infty$

where. Pic 2 probability measure

Px(x) can also be simplified as p(x).

The probabilities associated with each possible values must be positive and sum up to I. For all other values, the probability needs to be 0.

≥ px (24) = 1

p(x;) >0

p(n) = 0, for all other n.

Thinking of probability as mass helps to avoid mistakes since the physical mass is conserved as is the total probability for all hypothetical outcomes x.

EXAMPLE. L:

Roll a die an infinite number of times and look at the proportion of I, the proportion of 2 and so on.

Call on the random variable that corresponds to the outcome of the dice roll. Thus, the random variable or can only take the following discrete values:

1, 2, 3, 4, 5 or 6. It is thus a discrete random

variable.

The sim of the probability mass function is to describe the probability of each possible value. In this example, it describes the probability to get a 1, the probability to get a 2 and so on. In the case of rolling the dice, the possibility to get each value is the same, i.e., P(x=1) = P(x=2) = P(x=3) = P(x=4) = P(x=5) = P(x=6)

Since there are 6 possible outcomes, they are equiprobable.

i.e., $P(n=1) = \frac{1}{6}$

$$P(n=2) = \frac{1}{6}$$

$$P(n=2) = \frac{1}{6}$$

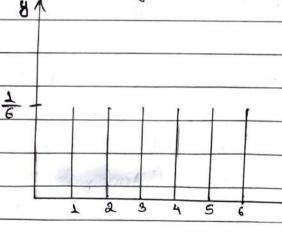
$$P(n=3) = \frac{1}{6}$$

$$P(x=5) = \frac{1}{6}$$

and,
$$P(n=6) = \frac{1}{6}$$

This distribution shows the same probability for each value, hence it is called uniform distribution.

The probability mass function for this example would look something like the figure below:



Here, the y-axis gives the probability and theo n-axis gives the outcome.

PROPERTY OF A PROBABILITY MASS FUNCTION:

A function is a probability mass function if Anen ; OSP(x) SI

i.e. for every possible value x in the range of

x, the probability that the outcome corresponds

In the continuous univariate case, the reference measure is the Lebesgue measure. The probability mass function of a discrete random variable is the density with respect to the counting measure over the sample space.

No. of Lot

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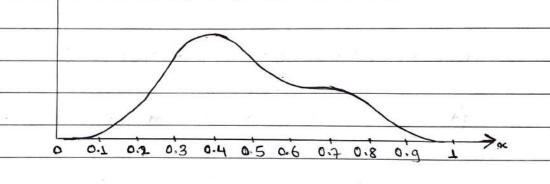
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It is not possible to define a density with reference to an arbitrary measure. Furthermore, when it does exit, the density is almost everywhere unique.

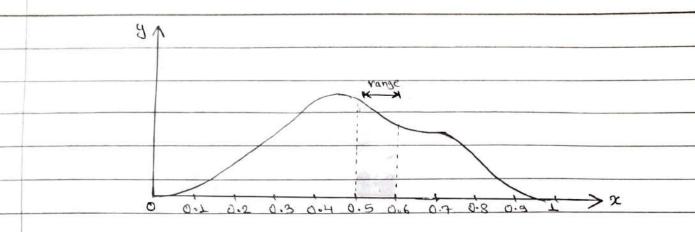
EXAMPLE. 2: Let a random variable a can take values between O and I, such that its probability density

function is as shown in the figure below:

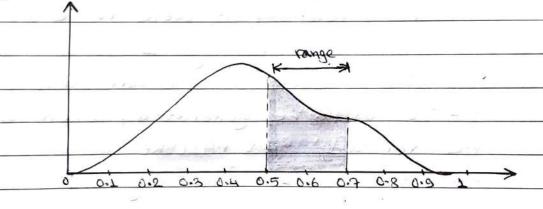


It can be seen that O seems not to be possible (i.e., probability around 0) and neither I. The graph around 0.4 means that it will get a lot of outcomes around this value.

Finding probabilities from probability density function between a certain range of values can be done by calculating the area under the curve for this range. For example, the probability of drawing & value between 0.5 and 0.6 corresponds to the following stres:



It can be seen that with an increase in the range, the probability increases as well. For instance, the range of 0.5 to 0.7 is as follows:



The probability associated with a specific range can be obtained by calculating the area under the curve

PROPERTY OF A PROBABILITY DENSITY FUNCTION:

A function is a probability density function if, $\forall x \in x ; p(x) \geq 0$

In this case, p(n) is not necessarily less than I because it doesn't correspond to the probability (the probability itself will still need to be between 0 and 1).

BINOMIAL DISTRIBUTION:

A binomial distribution can be thought of as simply the probability of a Success or FATLURE outcome in an experiment or survey that is repeated multiple times The binomial is a type of distribution that has two possible outcomes. For example, a coin toss has only two possible outcomes: heads or tails.

for example, to find the probability of getting a 1 on a die roll. If it were rolled 20 times, the probability of rolling a 1 in any throw is $\frac{1}{6}$. In 20 rolls, a binomial distribution of n=20 and $p=\frac{1}{6}$ would be generated, where Success would be 'roll a 1' and fallure would be 'roll any number except 1'. Similarly, the probability of the die landing on an even number, when the die is rolled 20 times would be given by the binomial distribution having n=20 and $p=\frac{1}{2}$.

The binomial distribution formula is:

b(n:n,P)= "Cx.P". (1-P)"-x

because the probability of rolling an even

where, b is binomial probability

P is probability of success on an individual trial

n is total number of successes

(1-P) = 0 or 9 is probability of failure on a trial. $^{n}C_{\infty}$ is combination formula = $\frac{n!}{(n-x)! x!}$ **********

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REAL LIFE EXAMPLES OF BINOMTAL DISTRIBUTION:

Basically, anything that can be thought to be either a success or a failure can be represented by a binomial distribution.

It a new drug is introduced to cure a disease, it is either a success, meaning it cures the disease, or it doesn't cure the meaning, meaning it's a

If a lottery ticket is purchased, the buyer either wing the prize or doesn't win the prize.

POTSION DISTRIBUTION:

A Poisson distribution is a tool that helps to predict the probability of certain events from happening when it is known how often the event has occurred. It gives the probability of a given number of events happening in a fixed interval of time.

The formula for Poisson probability mass function is p(x; 2) = e-2 22

n = 0, 1, 2where

I is the expected number of occurrences.

It is sometimes denoted by u and is called the event rate or rate parameter. EXAMPLE. 4:

If the average number of major storms in a city is 2 per year, what is the probability that exactly 3 storms will hit that city the next year?

Here,

Average number of storms per year, $\mu = 2$ Number of storms to hit the next year, n = 3Euler's number, e = 2.71828

So,

Placing these component values in the Poisson distribution formula,

 $P(3; 2) = (2.71828)^{-2} \cdot 2^{3}$

- 0.13584x8

0

= 0.780

i.e. the probability of 3 storms happening next year is 0.180, or 18%.

As it can probably be seen, Poisson distribution can be calculated manually, but it would taker an extraordinary amount of time unless a simple set of data is provided. The usual way to calculate a Poisson distribution in real life situations is with software like IBM SPSS.

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PRACTICAL USE OF POISSON DISTRIBUTION:

A tentbook store rents an average of 200 books every Saturday night. Using this data, one can predict the probability that more books (perhaps 300 a 400) will sell on the following Saturday nights.

Another example is the number of diners in a Certain rectaurant every day. If the average number of diner for seven days is 500, it can be predicted that the probability of a certain day having more customers.

Because of this application, Poisson distributions are used by businessmen to make forecasts about the number of customers or sales on certain days or sezions of the year. In business, overstocking will Sometimes mean losses if the goods are not sold likewise, having too few stock would still mean a lost business. By using poisson distribution, businessmen are able to estimate the time when demand is unusually higher, so they can purchase more stock Hotels and restaurants could prepare for an influe of customers, hire entra temporary workers in advance. purchase more supplies etc.

With the Poisson distribution, companies can adjust supply to demand in order to keep their business chining good profit. In addition, waste of resource is prevented.

POISSON DISTRIBUTION VS BINOMIAL DISTRIBUTION:

It can be challenging to figure out whether to we a Binomial distribution or a Poisson distribution in exam-related questions. The following two points are general guidelines to distinguish between the two:

- 1. If the question has an average probability of an event happening per unit (i.e., per unit time, cycle, event) and it has been asked to find probability of a certain number of events happening in a period of time for number of events), then the Poisson Distribution is used.
- 2. If the question has provided an exact probability of and it has been asked to find the probability of the event happening a certain number of times out of a (i.e., 10 times out of 100, or 39 times out of 3000), the Binomial Distribution formula is used.

NORMAL DISTRIBUTION:

Normal distribution, also known as Gaussian distribution, is a probability distribution that is symmetric about the mean, showing that data near the mean are more frequent in occurrence than data far from the mean. In graph form, normal distribution will appear as a bell curve.

of a distribution. The normal distribution is symmetric and has a skewness of zero. If the distribution of a data set has a skewness less than zero, or negative skewness, then the left tail of the distribution is longer than the right tail; positive skewness implies that the right tail of the distribution is longer than the left.

The Kurtosis statistic measures the thickness of the tail ends of a distribution in relation to the tails of the normal distribution. Distributions with large kurtosis exhibit tail data exceeding the tails of the normal distribution. Distributions with low kurtosis exhibit tail data that is generally less extreme than the tails of the normal distribution.

EXAMPLE. 5:

If the bottom 80% of students failed an end of semester enam, where the mean for the test was 120 and the standard deviation was 17, what was the passing score?
Here,

Z = X-M

04, X = 26+4

= 775+750

To find the value of z, we will be looking at the normal distribution curve.

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REAL LIFE APPLICATION OF NORMAL DISTRIBUTION:

- I. Height: Height of the population is the example of normal distribution. Most of the people on a specific population are of average height. The number of people taller and shorter than the average height people is almost equal, and a very small number of people are either extremely tall or extremely chort. Therefore, it follows the normal distribution.
 - Technical Stock Market: The falling and hiking in the price of the chares, the changes in the log values of Forex rates, price indices and stock prices return often from a bell shaped curve.
- 3. Income Distribution in Economy: The income of a country lies in the hands of enduring politics and government. It depends upon how they distribute the income among the rich and poor community.

 The middle-class population is higher than the rich and poor population, so, the wages of the middle-class population makes the mean in the

normal distribution curve.

4. Birth Weight: The normal birth weight of a newborn ranges from 25 to 3.5 kg. The majority of newborns have normal birthweight whereas, only a few percentage have a weight higher or lower than the normal. Hence, birth weight follows the normal distribution curve.

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