

UG Mid Sem Examination, 2021

Branch: CSE

Sch. Id.: 1912160

Subject: Theory of Computation

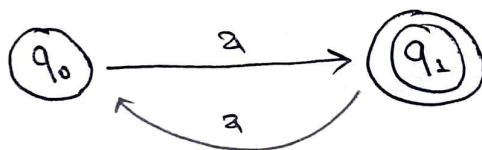
Subject Code: CS204

Semester: IVthDate: 9th March, 2021Q.10Soln:-
Ans(d)Given, α is string over alphabet Σ

$$\text{odd}(\alpha) = a_1, a_3, a_5, \dots$$

Strings formed = $a, aza, azaaz, \dots$

Constructing DFA,

If L is regular, $\text{odd}(L)$ is regular, it is clear.for language L in Σ^* ,

$$\text{odd}(\alpha) : \alpha \in L$$

$$\Sigma^*, n = 0, 1, 2, \dots$$

for odd, $n = 1, 3, 5, \dots$ \therefore The progression / string formation can go upto infinity. $\therefore \text{Odd}(L)$ is infinite (even if L was irregular).

This gives us the conclusion,

 $\text{odd}(L)$ is infinite and also regular when L is regular.

Q. 4.

Soln:-Ans:-

"All languages can be generated by context-free grammar." This statement is false.

It is known that all regular languages can be generated by context free grammar, however not all non-regular languages can be generated by context free grammar, this is because non-regular languages cannot be generated by regular expressions.

Q. 3.

Soln:-Ans (d)

Given, $L \subseteq \Sigma^*$

Alphabets $\Sigma = \{a, b\}$

By hit and trial, we come to think,

$L = \{a^m b^n : n, m \geq 1\}$ is regular.

Proof:-

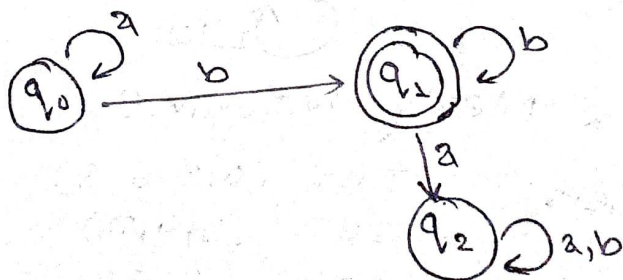
Clearly the language is infinite.

Also, it is a possibility $m=n$, $m>n$, $n>m$.

Possible string formations = $ab, aab, aabb, \dots$

meaning b must be followed after a .

DFA:



Hence, it is regular.

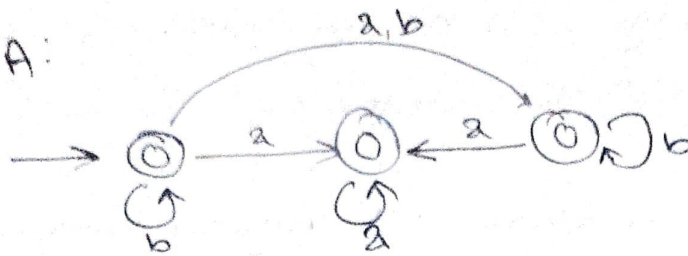
$\therefore L = \{a^m b^n : n, m \geq 1\}$ is regular.

Q.5.

Soln:-

Ans (d)

NFA:

for, $b^* ab^* aa^* b (a+b)^*$ for $n=1$,

String formed = babaaba, babaabb

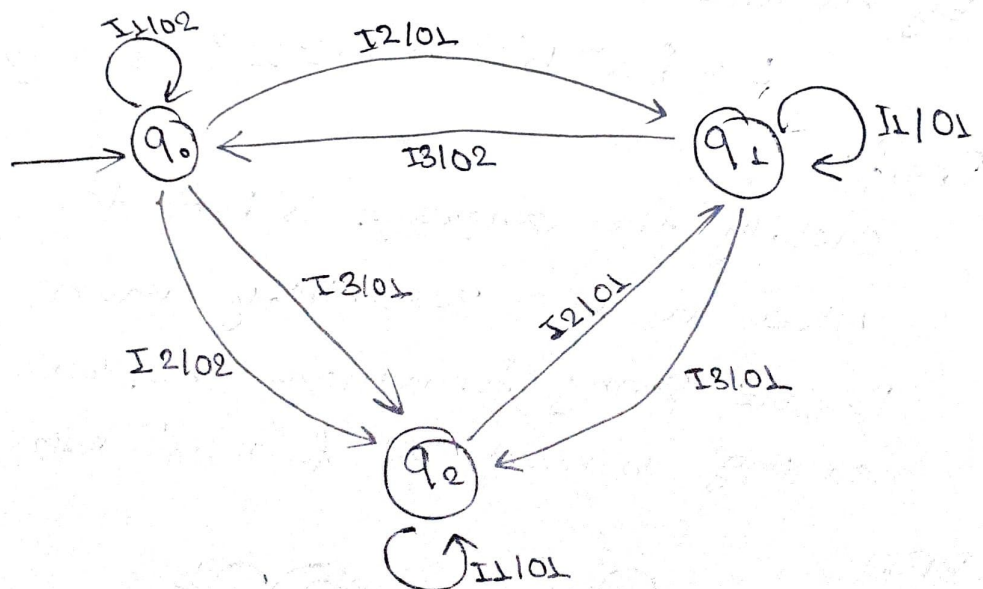
both strings are accepted by the NFA when ran through it.

When the similar process is run for other string with varied values of n , NFA is not satisfied.

Q.2.

Soln:-

Ans (c)



This is a Mealy Machine.

Inputs Sets:

 $I1 = (0, 3, 6, 9)$ $I2 = (1, 4, 7)$ $I3 = (2, 5, 8)$

Output sets:

 $O1 = 0$ $O2 = 1$

$$M_e = \{ Q, \Sigma, \Delta, \delta, q_0 \}$$

$$Q = \{ q_0, q_1, q_2 \}$$

$$\Sigma = \{ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 \}$$

Transition table, δ ,

	$I1 \text{ (rem 0)}$	$I2 \text{ (rem 1)}$	$I3 \text{ (rem 2)}$
$\rightarrow q_0^*$	q_0	q_1	q_2
q_1	q_1	q_2	q_0
q_2	q_2	q_0	q_1

Final state = q_0

From transition table, we have,

They represent zero-remainder state,
one-remainder state and
two-remainders state.