

**National Institute of Technology, Silchar**

Subject Code : CS-204, Subject: Theory of Computation

Semester: 4<sup>th</sup>. Branch: Computer Sci. & Engg.

Duration: One Hour. Total Marks: 20

*Figure in the right hand margin indicates full marks for the question.*

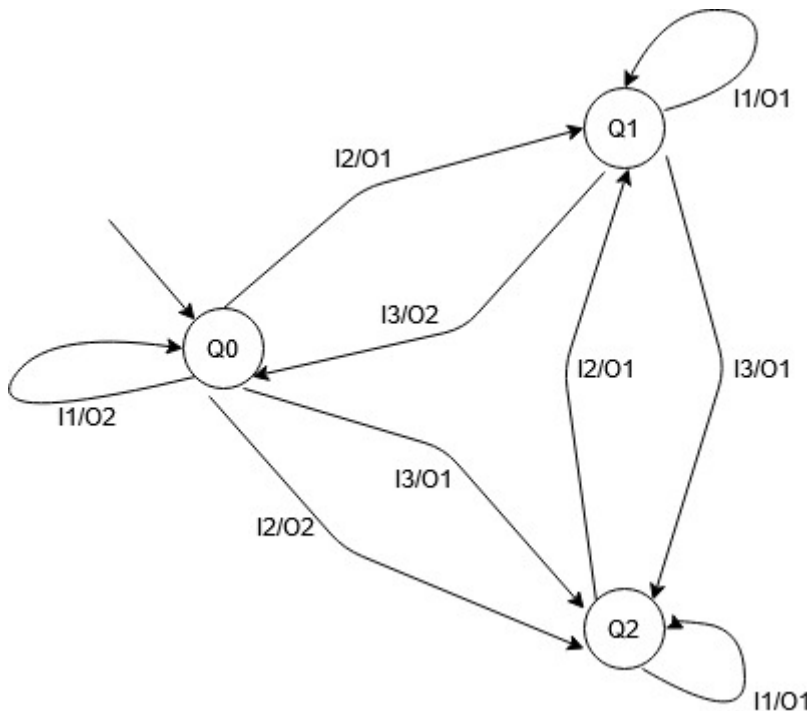
*All questions are compulsory (NO-NEGATIVE Marks for wrong Answers)*

**NOTE:**

Fill google-form and submit your response along with your name, institute email ID and scholar No. in the classwork section at Google Classroom.

- Q1.** Let  $\alpha$  be a string over some alphabet  $\Sigma$ . By  $\text{odd}(\alpha)$ , we refer to the string obtained by deleting symbols at all even positions of  $\alpha$ . That is, if  $\alpha = a_1 a_2 a_3 \dots a_n$ , then  $\text{odd}(\alpha) = a_1 a_3 a_5 \dots a_{n'}$ , where  $n'$  is  $n$  or  $n-1$  according as whether  $n$  is odd or even. For a language  $L$  in  $\Sigma^*$  define  $\text{odd}(L) = \{\text{odd}(\alpha) : \alpha \in L\}$  then:
- a) if  $L$  is regular, then  $\text{odd}(L)$  is finite and regular.
  - b) if  $L$  is regular, then  $\text{odd}(L)$  is not necessarily regular.
  - c) if  $L$  is regular, then  $\text{odd}(L)$  is in-finite and not regular.
  - d) if  $L$  is regular, then  $\text{odd}(L)$  is in-finite and regular.

**Q2.**



The above transducer is designed for testing divisibility-by-3 for multi-digit decimal numbers with three different classes of inputs:  $I1 = (0,3,6,9)$ ,  $I2 = (1,4,7)$ ,  $I3 = (2,5,8)$  and two different classes of outputs:  $O1 = 0$  and  $O2 = 1$ .

What can you say about the states Q0, Q1 and Q2.

- a) They represent start-state, carry and no-carry respectively.
- b) They represent divisibility by 3, 6 and 9 respectively.
- c) They represent zero-remainder state, one-remainder state and two-remainder state respectively.
- d) They represent input class I1, I2 and I3 respectively.

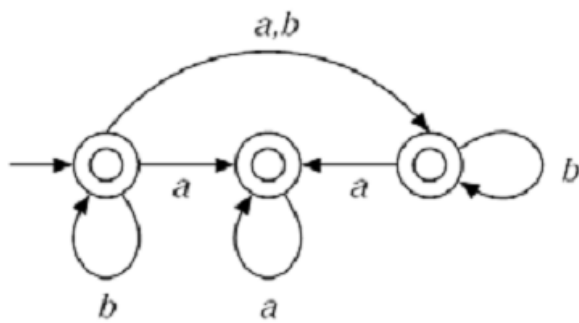
Q3. Let  $L \subseteq \Sigma^*$ , where  $\Sigma = \{a,b\}$ , which of the following is true? 4

- a)  $L = \{x : x \text{ has an equal number of a's and b's}\}$  is regular.
- b)  $L = \{a^n b^n : n \geq 1\}$  is regular.
- c)  $L = \{x : x \text{ has more number of a's than b's}\}$  is regular.
- d)  $L = \{a^m b^n : n, m \geq 1\}$  is regular.

Q4. Which of the following statement is wrong? 4

- a) Any regular language has an equivalent context-free grammar.
- b) Some non-regular language can't be generated by any context-free grammar.
- c) The intersection of context-free languages and a regular language is always context-free.
- d) All languages can be generated by context-free grammar.

Q5. Consider the following NFA (over the alphabet  $\{a,b\}$ ). Let L denote the set of all strings not accepted by this NFA. 4



The regular expression for L is :

- a)  $ab(a+b)^*$
- b)  $(a+b)b^*ab$
- c)  $aab(a+b)^*$
- d)  $b^*ab^*aa^*b(a+b)^*$

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