Algoritmi di ottimizzazione

Agent Scheduling Problem

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1 Agent Scheduling Problem

This isn't the classic Traveling Salesman Problem with Time Windows because there are more constraints to respect. Those constraints are:

30 minutes for lunch between 12:00 AM and 2:00 PM;

Limited working time (8 hours);

Limited waiting and traveling time;

Minimum time to spent in office (1 hour);

Importing libraries

```
[1]: import gurobipy as gb
from gurobipy import GRB

import math
import matplotlib.pyplot as plt
import networkx as nx
import numpy as np
import pandas as pd
```

Define file with clients data

```
[2]: FILE = "./TEST_SETS/test_1.txt"
```

Define costant parameters

```
[3]: # Default params
     SUPPORTED_FORMAT = ['NUM', 'X', 'Y', 'DEMAND', 'READYTIME', 'DUEDATE', 'SERVICE']
     # Macros for time values conversions
     MINUTES = 60
     HOURS = 3600
     OFFSET_TIMES = 8*HOURS
     COLUMNS_OPS = {'NUM': lambda x: float(x),
                    'X': lambda x: float(x),
                    'Y': lambda x: float(x),
                    'DEMAND': lambda x: 1,
                    'READYTIME': lambda x: float(x),
                    'DUEDATE': lambda x: float(x),
                    'SERVICE': lambda x: float(x)
     # Agents count
     AGENTS = 10
     # Multiplier for distance cost
     TIME_PER_DISTANCE = 1
```

```
# Agent Working day start and end
WORKING_TIME_RANGE = (0, 8*HOURS)

# Agent Lunch break time range, lasting
LUNCH_BREAK_RANGE = (12*HOURS-OFFSET_TIMES, 13.5*HOURS-OFFSET_TIMES)
LUNCH_BREAK_TIME = 30*MINUTES

# Agents office parameters
OFFICE_NUM = 0
OFFICE_X = .0
OFFICE_Y = .0
OFFICE_Y = .0
OFFICE_READYTIME = WORKING_TIME_RANGE[0]
OFFICE_DUEDATE = WORKING_TIME_RANGE[1]
OFFICE_SERVICE = 1*HOURS
```

Read clients data

```
[4]: def read_input_tsptw(filename):
         """ Function used to convert input file to usable data.
             :params filename: File to convert,
             :return: A dict with nodes parameters,
                      A distance matrix between nodes,
                      Nodes coordinates.
         # Dict sed for locations parameters
         data_dict = dict()
         # List of node positions for plots
         nodes_x = list()
         nodes_y = list()
         # Add office to data for matrix distance calculation.
         data_dict.update({OFFICE_NUM: {'X': OFFICE_X,
                                         'Y': OFFICE_Y,
                                         'DEMAND': AGENTS,
                                         'READYTIME': OFFICE_READYTIME,
                                         'DUEDATE': OFFICE_DUEDATE,
                                         'SERVICE': OFFICE_SERVICE,}})
         # Add office to nodes
         nodes_x.append(OFFICE_X)
         nodes_y.append(OFFICE_Y)
         # Open file and read lines
         with open(filename, "r") as file:
             # Initialize columns in empty dict
```

```
columns = file.readline().replace("#","").split()
        if columns != SUPPORTED_FORMAT:
            print("ERROR! Format not supported.")
            return
        # For each data line
        for line in file.readlines():
            node_dict = {k: COLUMNS_OPS[k](val) for k, val in zip(columns, line.
 →split())}
            # Get. i.d.
            node_id = node_dict.pop('NUM')
            # Insert new node in data dict
            data_dict.update({int(node_id): node_dict})
            # Get nodes positions
            nodes_x.append(float(line.split()[columns.index('X')]))
            nodes_y.append(float(line.split()[columns.index('Y')]))
    # Get distance matrix
    distance_matrix = compute_distance_matrix(nodes_x, nodes_y)
    return (data_dict, distance_matrix, dict(enumerate(zip(nodes_x, nodes_y))))
def compute_distance_matrix(nodes_x, nodes_y):
    """ Function used to compute the euclidean distance matrix.
        :param nodes_x: List of nodes x coordinates,
        :param nodes_y: List of nodes y coordinates,
        :return: Distance matrix between nodes."""
    # Get clients count and initialize distance matrix
    clients = len(nodes_x)
    distance_matrix = [[None for i in range(clients)] for j in range(clients)]
    for i in range(clients):
        # Set cost of trip between same agent and himself as null
        distance_matrix[i][i] = 0
        for j in range(clients):
            # Compute distance matrix calculating euclidean distance between_
 →each node
            dist = compute_dist(nodes_x[i], nodes_x[j], nodes_y[i], nodes_y[j])
            distance_matrix[i][j] = dist
            distance_matrix[j][i] = dist
    return distance_matrix
def compute_dist(xi, xj, yi, yj):
    """ Function used to compute euclidean distance.
        :param xi: x coordinate of first node,
        :param xj: x coordinate of second node,
```

```
[5]: # Getting locations parameters
data_dict, distance_matrix, positions = read_input_tsptw(FILE)
```

```
[6]: # DEBUG RESTRICTIONS
     CLIENTS = len(data_dict)
     data_dict = {k: v for k,v in data_dict.items() if k < CLIENTS}</pre>
     distance_matrix = [dm[:CLIENTS] for dm in distance_matrix[:CLIENTS]]
     # ADD FITTICIOUS LOCATION
     # This location is used to have a complete loop in Agent trips without |
      \rightarrow interfering
     # with trips costs. Having a complete loop simplify the job of creating a trip.
     # To not interfer with costs it's distance to all other locations is 0.
     distance_matrix = [dm + [0,] for dm in distance_matrix]
     distance_matrix = distance_matrix + [[0]*(CLIENTS+1)]
     # Add location data
     #remove office from data_dict
     del data_dict[0]
     # POSITIONS SETS FOR CLEANER MODEL
     agent_list = list(range(AGENTS))
     #-----
     clients_list = list(range(CLIENTS))
     meets_duedates = [(i, data_dict[i]['READYTIME']) for i in data_dict.keys()]
```

Definiamo una funzione che dato un percorso, definito come lista, ne restituisce il costo. Un percorso è una successione di azioni tra {'office', 'meet', 'wait', 'travel', 'lunch'} ai quali sono associati un tempo di inizio e una posizione.

Il costo del percorso è calcolato dai tempi di wait e di travel, che si punta a minimizzare.

```
[7]: def path_cost(path):
    """ Function used to compute the cost of an agent schedule.
    :param path: a schedule that contains tuples of actions that an agent_
    →does
    :return: the computed cost
    """

p = path.copy()
p.append(('end', WORKING_TIME_RANGE[1], -1)) #useful for the last work_
    →computation
cost = 0
```

```
for i in range(len(p)-1):
    time_range = p[i+1][1] - p[i][1]
    if time_range < 0:
        raise Exception("Error in the schedule " + str(path) + ": a time is_\(\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\tilte{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\texi{\text{\text{\texi{\text{\text{\text{\text{\tex
```

2 Primal master problem

We define the master problem: we provide a set of feasible schedules (each schedule has exactly one lunch and all the action times are in increasing order), and the master model chooses some schedules respecting the following constraints: 1. every agents has only one schedule assigned. 2. every meet is in only one schedule among those selected.

A binary variable x in the set $\{0,1\}$ is assigned to each schedule.

```
[8]: def pmp(schedules):
         """ This function defines an integer programming model that uses a binary \Box
      \rightarrow variable
             for each possible schedule.
             :param schedules: the possible schedules
             :return: a gurobi model to optimize
         #Constants
         scheds_list = list(range(len(schedules)))
         meets_list = list(range(len(meets_duedates)))
         positions = [m[0] for m in meets_duedates]
         # Create model
         mod = gb.Model("TSPTW")
         #Vars
         x = mod.addVars({(a,s): 0 for a in schedules.keys()
                                for s in range(len(schedules[a])) },
                    name="x",
                    vtype=GRB.BINARY)
         #Constrs
         oneschedperagent = mod.addConstrs((gb.quicksum(x[a,s] for s in_
      →range(len(schedules[a]))) == 1 for a in agent_list),
                                            name='one_sched_per_agent')
         meetsconstr = mod.addConstrs((gb.quicksum(x[a,s]
                                                     for a in agent_list
                                                     for s in range(len(schedules[a]))
```

3 Useful functions for the model

```
[9]: def swap(agents_paths):
         """ This function generates lists of paths for agents, swapping nodes in a_{\sqcup}
      \rightarrow first assignment of paths to agents.
              An agent path is a list of integers that represents the meets sequence \Box
      \rightarrow that an agent must follow.
             For each generated path is also generated a variant of length +1 and -1.
              :param agents_paths: a dict that associate each agent to a path
              :return: more agents paths
          11 11 11
         lens = { i : len(agents_paths[i]) for i in range(len(agents_paths))}
         #init lens_reduced
         lens_reduced = {}
         counter = 0
         accumulate = True
         for i in agents_paths.keys():
             dim = len(agents_paths[i])
             if dim > 0:
                  lens_reduced[i] = dim-1
                  counter = counter+1
             elif accumulate:
                  lens_reduced[i] = counter
                  accumulate = False
             else:
                  lens_reduced[i] = 0
         #init lens_increased
         lens_increased = {}
         budget = sum(len(agents_paths[i]) for i in agents_paths.keys())
         end = False
         for i in agents_paths.keys():
             dim = len(agents_paths[i])
```

```
if budget >= dim+1:
            lens_increased[i] = dim+1
            budget = budget-dim-1
        elif not end:
            lens_increased[i] = budget
            budget = 0
            end = True
        else:
            lens_increased[i] = 0
    nodes = \Pi
    all_lens = [lens, lens_reduced, lens_increased]
    for i in range(len(agents_paths)):
        nodes = nodes + agents_paths[i]
    all_paths = []
    #swap
    for i in range(len(nodes)-1):
        for j in range(i+1, len(nodes)):
            new_nodes = nodes.copy()
            (new_nodes[i], new_nodes[j]) = (new_nodes[j], new_nodes[i])
            counter = 0
            for 1 in all_lens:
                for k in range(len(agents_paths)):
                    new_path = []
                    new_path = new_path + new_nodes[counter:counter+l[k]]
                    counter = counter + 1[k]
                    agents_paths[k] = new_path
                all_paths.append(agents_paths.copy())
                counter = 0
    return all_paths
def schedules_from_mod(mod):
    """ Gets the agent schedules from an optimized model
        :param mod: the optimized gurobi model
        :return: dict that associate each agent to a schedule
    .....
    1 = []
    for v in mod.getVars():
        if v.x == 1:
            s = str(v.varName)
            s = s[1:len(s)]
            split = s.split(',')
            cmd = 'l.append(scheds'+split[0]+']['+split[1]+')'
            exec(cmd)
    scheds = {i: l[i] for i in range(len(1))}
    return scheds
```

```
def optimize_time_windows(sched):
    \hookrightarrow office.
        :param sched: the schedule to optimize.
   sched.append(('end', WORKING_TIME_RANGE[1], -1)) #useful for compute lastu
 →wait range
   waits = [w for w in sched if w[0] == 'wait']
   waits.reverse()
   #save office indexes in the schedule
   indexes = []
   for i, s in enumerate(sched):
       if s[0] == 'office':
           indexes.append(i)
   if len(indexes) in [0,1] and not sched[-2][0] == 'wait' and not sched[0][0]
 →== 'wait': #no slices to optimzie
       return
   #must optimize a series of slices. A slice contains one or more wait actions.
   slices = ∏
   for i in range(len(indexes)-1):
       slices.append(sched[indexes[i]:indexes[i+1]+1])
   if len(indexes) > 0 and 'wait' in [w[0] for w in sched[indexes[-1]:
 →len(sched)]:
       slices.append(sched[indexes[-1]:len(sched)]) #if a wait is in the last_
   elif 'wait' in [w[0] for w in sched[0:len(sched)]]:
       slices.append(sched)
   #optimize office-office slice or first/last slice if it contains 'wait'
   for s in slices:
       waits = [w for w in s if w[0] == 'wait']
       waits.reverse()
       for w in waits: #waits are in reverse order(reverse()). The optimization_{\sqcup}
 →is done staring from last 'wait'
           for i, work in enumerate(s):
               if w == work:
                   #cerco l'indice del meet precedente a questo wait
                   j = i
                   while not s[j][0] == 'meet':
                       if i == 0:
                           break
```

```
j = j-1
                    _{\mathtt{min}} = 0
                    if s[j][0] == 'meet':
                        wait_time = s[i+1][1] - s[i][1]
                        meet_time = data_dict[s[j][2]]['DUEDATE'] -__
\rightarrowdata_dict[s[j][2]]['READYTIME']
                        if 'lunch' in [w[0] for w in s[j:i+1]]:#lunch is between_\sqcup
\rightarrowmeet and wait
                            lunch_index = -1 #qet lunch index
                            for 1, w in enumerate(s):
                                 if w[0] == 'lunch':
                                     lunch_index = 1
                            lunch_time = LUNCH_BREAK_RANGE[1] - s[lunch_index][1]
                            _min = min(wait_time, meet_time, lunch_time)
                        else:
                             _min = min(wait_time, meet_time)
                    elif s[j][0] == 'office': #no meet, office time is extended_
\rightarrow with wait_time
                        if 'lunch' in [w[0] for w in s[j:i+1]]:# se c'è il_{\sqcup}
→pranzo in mezzo
                            lunch_index = -1 #get lunch index
                            for 1, w in enumerate(s):
                                 if w[0] == 'lunch':
                                     lunch_index = 1
                            lunch_time = LUNCH_BREAK_RANGE[1] - s[lunch_index][1]
                            _min = min(wait_time, lunch_time)
                        else:
                            wait_time = s[i+1][1] - s[i][1]
                            _min = wait_time
                        j = j+1 #the first is office, there's no meet moving but
→ the next work will start later
                    for k in range(j,i+1):
                        newval = list(s[k])
                        newval[1] = newval[1] + _min
                        s[k] = tuple(newval)
                    break
   #rebuild schedule from slices
   newsched = []
   for s in slices:
       newsched = newsched + s[0:len(s)-1]
   #if the optimized schedule starts with 'wait' must check that there is u
→enough time for office work
   if newsched[0][0] == 'wait':
```

```
diff = newsched[1][1] - newsched[0][1]
        if diff >= OFFICE_SERVICE +
 →distance_matrix[0][sched[1][2]]*TIME_PER_DISTANCE:
            start_travel = newsched[1][1] -___
 →distance_matrix[0] [newsched[1][2]]*TIME_PER_DISTANCE
            newsched.pop(0)
            newsched.insert(0, ('travel', start_travel, -1))
            newsched.insert(0, ('office', 0.0, 0))
    sched = newsched
def path_to_schedule(path):
    """ Gets a schedule starting from a path (a list of meet nodes associated to_\sqcup
 \rightarrow an agent).
        Between each node is valued if there an agent has enough time to come_
 \rightarrow back in office.
        :param path: an agent path expressed as a list of meets.
    sched = []
    if not path:
            sched.append(('office', 0.0, 0))
            sched.append(('lunch', LUNCH_BREAK_RANGE[0], -1))
            sched.append(('office', LUNCH_BREAK_RANGE[0]+LUNCH_BREAK_TIME, 0))
    else:
        lunch_done = False
        lunch_shift = False
        meet_hour = data_dict[path[0]]['READYTIME']
        meet_end = meet_hour + data_dict[path[0]]['SERVICE']
        if OFFICE_SERVICE + distance_matrix[0][path[0]]*TIME_PER_DISTANCE <=_
 →meet_hour:
            start_travel = meet_hour -u
 →distance_matrix[0][path[0]]*TIME_PER_DISTANCE
            sched.append(('office', 0.0, 0))
            if meet_hour >= LUNCH_BREAK_RANGE[0] + LUNCH_BREAK_TIME and_
 -meet_hour <= LUNCH_BREAK_RANGE[1] + LUNCH_BREAK_TIME and not lunch_done:</pre>
                sched.append(('travel', start_travel - LUNCH_BREAK_TIME, -1))
                sched.append(('lunch', meet_hour - LUNCH_BREAK_TIME, -1))
                lunch_done = True
            else:
                sched.append(('travel', start_travel, -1))
            sched.append(('meet', meet_hour, path[0]))
        else:
            sched.append(('wait', 0.0, -1))
            sched.append(('meet', meet_hour, path[0]))
        if meet_end >= LUNCH_BREAK_RANGE[0] and meet_end <= LUNCH_BREAK_RANGE[1]_
 →and not lunch_done:
```

```
sched.append(('lunch', meet_end, -1)) # in this case next meet will_
⇒start an half hour later
           lunch_done = True
       #iter 0 to n-1 taking i and i+1 node to add works between two meets.
       for j in range(len(path)-1):
           prev = path[j]
           _{next} = path[j+1]
           shift = 0.0
           if lunch_shift:
               shift = LUNCH_BREAK_TIME
               lunch_shift = False
           end_prev_meet = data_dict[prev]['READYTIME'] +__
→data_dict[prev]['SERVICE'] + shift
           start_next_meet = data_dict[_next]['READYTIME']
           end_next_meet = start_next_meet + data_dict[_next]['SERVICE']
           diff = start_next_meet - end_prev_meet
           if ((start_next_meet >= LUNCH_BREAK_RANGE[0] + LUNCH_BREAK_TIME #èu
→ora di pranzo
               and start_next_meet <= LUNCH_BREAK_RANGE[1] + LUNCH_BREAK_TIME)__
\hookrightarrowor
               (end_next_meet >= LUNCH_BREAK_RANGE[0] and end_next_meet <=___</pre>
→LUNCH_BREAK_RANGE[1])) and not lunch_done:
               #Check if lunch must be done before the meet
               if start_next_meet >= LUNCH_BREAK_RANGE[0] + LUNCH_BREAK_TIME_
→and start_next_meet <= LUNCH_BREAK_RANGE[1] + LUNCH_BREAK_TIME and not_
→lunch_done: #check prima del meet
                   #if there is enough time to come back in office
                   if OFFICE_SERVICE +
→distance_matrix[0][prev]*TIME_PER_DISTANCE +
distance_matrix[0][_next]*TIME_PER_DISTANCE + LUNCH_BREAK_TIME <= diff:</pre>
                       in_office = end_prev_meet +_
→distance_matrix[0][prev]*TIME_PER_DISTANCE
                       start_travel_to_meet = start_next_meet -u
→distance_matrix[0][_next]*TIME_PER_DISTANCE - LUNCH_BREAK_TIME #pranzo_
→all'arrivo
                       sched.append(('travel', end_prev_meet, -1))
                       sched.append(('office', in_office, 0))
                       sched.append(('travel', start_travel_to_meet, -1))
                       sched.append(('lunch', start_next_meet -_
→LUNCH_BREAK_TIME, -1))
                       sched.append(('meet', start_next_meet, _next))
                       lunch_done = True
                   else:
```

```
#per l'inizializzazione si è tenuto conto che wait sia
→maggiore di LUNCH_BREAK_TIME (SOLO INIT)
                       travel_arrive = end_prev_meet +_
→distance_matrix[prev] [_next] *TIME_PER_DISTANCE
                       lunch_diff = start_next_meet - travel_arrive
                       if lunch_diff >= LUNCH_BREAK_TIME:
                            sched.append(('travel', end_prev_meet, -1))
                           sched.append(('lunch', travel_arrive, -1))
                           sched.append(('wait', travel_arrive +
→LUNCH_BREAK_TIME, -1))
                           sched.append(('meet', start_next_meet, _next))
                           lunch_done = True
                       else: #it's lunch time but there's no time to come back
\rightarrow in office
                           sched.append(('travel', end_prev_meet, -1))
                           sched.append(('wait', travel_arrive, -1))
                           sched.append(('meet', start_next_meet, _next))
               #Check if lunch can be done after the meet
               if end_next_meet >= LUNCH_BREAK_RANGE[0] and end_next_meet <=_
→LUNCH_BREAK_RANGE[1] and not lunch_done: #end meet check
                   if OFFICE_SERVICE +
→distance_matrix[0][prev]*TIME_PER_DISTANCE +
→distance_matrix[0][_next]*TIME_PER_DISTANCE <= diff:</pre>
                       in_office = end_prev_meet +
→distance_matrix[0][prev]*TIME_PER_DISTANCE
                       start_travel_to_meet = start_next_meet -_
→distance_matrix[0][_next]*TIME_PER_DISTANCE
                       sched.append(('travel', end_prev_meet, -1))
                       sched.append(('office', in_office, 0))
                       sched.append(('travel', start_travel_to_meet, -1))
                       sched.append(('meet', start_next_meet, _next))
                       sched.append(('lunch', end_next_meet, -1)) #prossima_
\rightarrow iterazione end_prev_meet swifta
                       lunch_done = True
                       lunch_shift = True
                   else: #no time to come back in office
                       travel_arrive = end_prev_meet +
→distance_matrix[prev] [_next]*TIME_PER_DISTANCE
                       if _next == path[-1]: #if _next+1 == len(path) corner_
\hookrightarrow case
                           sched.append(('travel', end_prev_meet, -1))
                           sched.append(('wait', travel_arrive, -1))
                           sched.append(('meet', start_next_meet, _next))
                           sched.append(('lunch', end_next_meet, -1))
                           lunch_shift = True
                           lunch_done = True
```

```
else:
                           lunch_diff = data_dict[path[j+2]]['READYTIME'] -__
→end_next_meet
                           if lunch_diff >= LUNCH_BREAK_TIME: #check diff
                                sched.append(('travel', end_prev_meet, -1))
                               sched.append(('wait', travel_arrive, -1))
                               sched.append(('meet', start_next_meet, _next))
                               sched.append(('lunch', end_next_meet, -1))
                               lunch_shift = True
                               lunch_done = True
                           else: #it's lunch time there's no time
                               sched.append(('travel', end_prev_meet, -1))
                               sched.append(('wait', travel_arrive, -1))
                               sched.append(('meet', start_next_meet, _next))
           else: #it's not lunch time
               if OFFICE_SERVICE + distance_matrix[0][prev]*TIME_PER_DISTANCE +
→distance_matrix[0][_next]*TIME_PER_DISTANCE <= diff: #enough time to come back_
\rightarrow in office
                   in_office = end_prev_meet +
→distance_matrix[0][prev]*TIME_PER_DISTANCE
                   start_travel_to_meet = start_next_meet -_
→distance_matrix[0][_next]*TIME_PER_DISTANCE
                   sched.append(('travel', end_prev_meet, -1))
                   sched.append(('office', in_office, 0))
                   sched.append(('travel', start_travel_to_meet, -1))
                   sched.append(('meet', start_next_meet, _next))
               else:
                   #travel -> wait -> meet
                   waiting = end_prev_meet +
→distance_matrix[prev] [_next]*TIME_PER_DISTANCE
                   sched.append(('travel', end_prev_meet, -1))
                   sched.append(('wait', waiting, -1))
                   sched.append(('meet', start_next_meet, _next))
       last = path[len(path)-1]
       shift = 0.0
       if lunch_shift:
           shift = LUNCH_BREAK_TIME
           lunch_shift = False
       last_meet_end = data_dict[last]['READYTIME'] +__
→data_dict[last]['SERVICE'] + shift
       office_arriving = last_meet_end +
→distance_matrix[0][last]*TIME_PER_DISTANCE
       if WORKING_TIME_RANGE[1] - office_arriving >= OFFICE_SERVICE:
           sched.append(('travel', last_meet_end, -1))
```

```
sched.append(('office', office_arriving, 0))
        else:
            sched.append(('wait', last_meet_end, -1)) #end of the day
    #check lunch num
    lunch_num = len([m for m in sched if m[0] == 'lunch'])
    if lunch_num > 1:
        raise Exception('Error, more than one lunch in the schedule: ' +u
 →str(path) + ' --- ' + str(sched))
    elif lunch_num == 0:#if lunch is not in the schedule, must try to get it \sqcup
 \rightarrow during office time
        sched.append(('end', WORKING_TIME_RANGE[1], -1))
        for i in range(len(sched)-1):
            r1=sched[i][1]
            r2=sched[i+1][1]
            if sched[i][0] == 'office':
                if (r1 <= LUNCH_BREAK_RANGE[0] and r2 >= LUNCH_BREAK_RANGE[0] + |
 →LUNCH_BREAK_TIME):
                    sched.insert(i+1, ('lunch', LUNCH_BREAK_RANGE[0], -1))
                    sched.insert(i+2, ('office', LUNCH_BREAK_RANGE[0] +__
 →LUNCH_BREAK_TIME, 0))
                    break
                elif r1 >= LUNCH_BREAK_RANGE[0] and r2 <= LUNCH_BREAK_RANGE[1]
 →and r2-r1 >= LUNCH_BREAK_TIME:
                    sched.insert(i+1, ('lunch', r1, -1))
                    sched.insert(i+2, ('office', r1 + LUNCH_BREAK_TIME, -1))
                    del(a[i])
                    break
                elif r1 <= LUNCH_BREAK_RANGE[1] and r2 >= LUNCH_BREAK_RANGE[1] +__
 →LUNCH_BREAK_TIME:
                    sched.insert(i+1, ('lunch', LUNCH_BREAK_RANGE[1], -1))
                    sched.insert(i+2, ('office', LUNCH_BREAK_RANGE[1] +__
 →LUNCH_BREAK_TIME, 0))
                    break
        del(sched[-1]) #remove end
    return sched
def paths_to_schedule():
    """ Transforms agent path into schedules.
        :return: a dict agent-schdule
    scheds = {a: [] for a in agent_list}
    for i in agent_list:
        scheds[i].append(path_to_schedule(agents_paths[i]))
    return scheds
```

```
def is_sched_feasible(schedule):
    """ Checks if a scheudule is feasible, looking if each value is more than \Box
 \hookrightarrow the previous.
        :return: True if the schedule is feasible, False otherwise.
    time = 0.0
    for work in schedule:
        if time > work[1]:
            return False
        time = work[1]
    return True
def all_schedule_comb(agents_paths):
    """ Makes the nodes swap and gets new schedules from the combinations.
        :param agents_paths: agent-path dict
    scheds = paths_to_schedule()
    all_combinations = swap(agents_paths)
    for comb in all_combinations: #all_combination is a list of dicts
        for key in comb.keys():
            sched = path_to_schedule(comb[key])
            if is_sched_feasible(sched) and sched not in scheds[key]:
                scheds[key].append(sched)
    return scheds
```

4 Initialization

Must be provided an initial solution to give for the first iteration. We use a greedy algorithm that for each agent he tries to attempt as many meets as possible choosing to all the remaining meets.

```
[10]:
    Greedy init: each agent takes all the meets he can do.
    '''
    agents_paths = {a:[] for a in agent_list}
    uncovered_meets = meets_duedates.copy()
    uncovered_meets.sort(key=lambda x: x[1])
    for i in range(len(agents_paths)):
        lunch_done = False
        if uncovered_meets:
            next_meet = uncovered_meets.pop(0)
            freeat = next_meet[1] + data_dict[next_meet[0]]['SERVICE']
            if next_meet[1] <= LUNCH_BREAK_RANGE[0] and freeat >=_u
            LUNCH_BREAK_RANGE[1]:
            raise Exception("Error, a meet takes all the lunch time range.")
            agents_paths[i].append(next_meet[0])
```

```
if next_meet[1] >= LUNCH_BREAK_RANGE[0] + LUNCH_BREAK_TIME and_
-next_meet[1] <= LUNCH_BREAK_RANGE[1] + LUNCH_BREAK_TIME: #lunch already done</pre>
           lunch_done = True
      elif freeat >= LUNCH_BREAK_RANGE[0] and freeat <= LUNCH_BREAK_RANGE[1]:
→#it's lunch time, freeat is moved an half hour later
           freeat = freeat + LUNCH_BREAK_TIME
           lunch_done = True
      to_remove = []
      for m in uncovered_meets:
           if m[1] <= LUNCH_BREAK_RANGE[0] and m[1] +__
→data_dict[m[0]]['SERVICE'] >= LUNCH_BREAK_RANGE[1]:
               raise Exception("Error, a meet takes all the lunch time range.")
           if freeat +
→distance_matrix[agents_paths[i][-1]][m[0]]*TIME_PER_DISTANCE <= m[1]:</pre>
               freeat = m[1] + data_dict[m[0]]['SERVICE']
               agents_paths[i].append(m[0])
               to_remove.append(m)
               if m[1] >= LUNCH_BREAK_RANGE[0] + LUNCH_BREAK_TIME and m[1] <=_1
→LUNCH_BREAK_RANGE[1] + LUNCH_BREAK_TIME and not lunch_done:
                   lunch_done = True
               if freeat >= LUNCH_BREAK_RANGE[0] and freeat <=_u
→LUNCH_BREAK_RANGE[1] and not lunch_done:
                   freeat = freeat + LUNCH_BREAK_TIME
                   lunch_done = True
      for m in to_remove:
           uncovered_meets.remove(m)
```

5 Model optimization

We iterate between master and slave problem until the cost convergence. The slave model swaps all paths nodes for all agents and generates feasible schedules. The master model chooses a subset of these schedules and starting from these reapplies the swap.

```
[11]: #initial cost
last_cost = 0
scheds = paths_to_schedule()

for key in scheds.keys():
    for s in scheds[key]:
        optimize_time_windows(s)

for key in scheds.keys():
    last_cost = last_cost + path_cost(scheds[key][0])
print("Initial cost: " + str(last_cost))
```

```
while (True):
    scheds = all_schedule_comb(agents_paths)
    for key in scheds.keys():
        for s in scheds[key]:
            optimize_time_windows(s)
    mod = pmp(scheds)
    mod.optimize()
    scheds = schedules_from_mod(mod)
    agents_paths = {i: [w[2] for w in scheds[i] if w[0] == 'meet'] for i in_
 →range(len(scheds))}#update agents_paths
    cost = 0
    for key in scheds.keys():
        cost = cost + path_cost(scheds[key])
    \rightarrowstr(cost)+"\n")
    if (last_cost <= cost):</pre>
        break
    else:
        last_cost = cost
Initial cost: 35606.0
Using license file C:\Users\gabriele\gurobi.lic
Academic license - for non-commercial use only
Gurobi Optimizer version 9.0.3 build v9.0.3rc0 (win64)
Optimize a model with 20 rows, 41 columns and 122 nonzeros
Model fingerprint: 0x12c159e0
Variable types: 0 continuous, 41 integer (41 binary)
Coefficient statistics:
 Matrix range
                [1e+00, 1e+00]
 Objective range [6e+02, 2e+04]
 Bounds range
                  [1e+00, 1e+00]
 RHS range
                  [1e+00, 1e+00]
Found heuristic solution: objective 34886.000000
Presolve removed 20 rows and 41 columns
Presolve time: 0.00s
Presolve: All rows and columns removed
Explored O nodes (O simplex iterations) in 0.01 seconds
Thread count was 1 (of 8 available processors)
Solution count 2: 33155
Optimal solution found (tolerance 1.00e-04)
Best objective 3.315500000000e+04, best bound 3.315500000000e+04, gap 0.0000%
```

Prev cost: 35606.0, cost: 33155.0 Gurobi Optimizer version 9.0.3 build v9.0.3rc0 (win64) Optimize a model with 20 rows, 41 columns and 122 nonzeros Model fingerprint: 0x4a17b2c2 Variable types: 0 continuous, 41 integer (41 binary) Coefficient statistics: [1e+00, 1e+00] Matrix range Objective range [6e+02, 2e+04] Bounds range [1e+00, 1e+00] [1e+00, 1e+00] RHS range Found heuristic solution: objective 32435.000000 Presolve removed 20 rows and 41 columns Presolve time: 0.00s Presolve: All rows and columns removed Explored O nodes (O simplex iterations) in 0.01 seconds Thread count was 1 (of 8 available processors) Solution count 1: 32435 Optimal solution found (tolerance 1.00e-04) Best objective 3.243500000000e+04, best bound 3.243500000000e+04, gap 0.0000% ______ Prev cost: 33155.0, cost: 32435.0 Gurobi Optimizer version 9.0.3 build v9.0.3rc0 (win64) Optimize a model with 20 rows, 41 columns and 122 nonzeros Model fingerprint: 0x4415c595 Variable types: 0 continuous, 41 integer (41 binary) Coefficient statistics: Matrix range [1e+00, 1e+00] Objective range [6e+02, 2e+04] Bounds range [1e+00, 1e+00] RHS range [1e+00, 1e+00] Found heuristic solution: objective 33155.000000 Presolve removed 20 rows and 41 columns Presolve time: 0.00s Presolve: All rows and columns removed Explored O nodes (O simplex iterations) in 0.01 seconds Thread count was 1 (of 8 available processors) Solution count 2: 32435 Optimal solution found (tolerance 1.00e-04)

Best objective 3.243500000000e+04, best bound 3.243500000000e+04, gap 0.0000%

Prev cost: 32435.0, cost: 32435.0

```
[12]: # Enlarge printable size
      pd.set_option('display.max_columns', 10)
      pd.set_option('display.width', 1000)
      # For each agent visit list
      for a in scheds.keys():
          agent_trip_desc = list()
          sched = scheds[a]
          last_meet_or_office = None
          lunch = False
          wait = 0.0
          for s in sched:
              if s[0] == 'meet' or s[0] == 'office':
                  pos_desc = {"POSITION": s[2] if s[2] else 'OFFICE',
                              "COST TO REACH":
       →distance_matrix[last_meet_or_office][s[2]]*TIME_PER_DISTANCE if
       →last_meet_or_office else 0.,
                               "REACHED AT": s[1],
                               "SERVICE TIME": data_dict[s[2]]['SERVICE'] if s[2] else_
       43600.0,
                               #"REAL S. TIME": c[prev, v\_mod, a].X,
                              "LEAVING TIME": s[1] + data_dict[s[2]]['SERVICE'] if___
       \rightarrows[2] else 3600.0,
                              "LUNCH_BEFORE": lunch,
                              "WAIT_BEFORE": wait
                  last_meet_or_office = s[2]
                  lunch = False
                  wait = 0.0
                  agent_trip_desc.append(pos_desc)
              if s[0] == 'lunch':
                  lunch = True
              if s[0] == 'wait':
                  for i, s2 in enumerate(sched):
                      if s == s2:
                          wait = sched[i+1][1] - s[1]
          # Print agent stats
          print(f"\nAgent {a+1}")
          print(pd.DataFrame(agent_trip_desc))
```

Agent 1 POSITION	COST TO REACH	REACHED AT	SERVICE TIME	LEAVING TIME	LUNCH_BEFORE
WAIT_BEFORE 0 8 3600.0	0.0	3600.0	2400.0	6000.0	False
1 2 2192.0	208.0	8400.0	2400.0	10800.0	False
2 9 1570.0	630.0	13000.0	2400.0	15400.0	False
3 OFFICE 0.0	845.0	18045.0	3600.0	3600.0	True
4 1 0.0	0.0	24800.0	2400.0	27200.0	False
Agent 2					
POSITION WAIT_BEFORE	COST TO REACH	REACHED AT	SERVICE TIME	LEAVING TIME	LUNCH_BEFORE
0 7 4700.0	0.0	4700.0	2400.0	7100.0	False
1 5	381.0	11900.0	2400.0	14300.0	False
4419.0 2 10 2133.0	367.0	16800.0	2400.0	19200.0	False
3 4	614.0	23400.0	2400.0	25800.0	True
1786.0					
Agent 3 POSITION WAIT_BEFORE	COST TO REACH	REACHED AT	SERVICE TIME	LEAVING TIME	LUNCH_BEFORE
O OFFICE	0.0	0.0	3600.0	3600.0	False
0.0 1 6 0.0	0.0	7100.0	2400.0	9500.0	False
2 3	573.0	10600.0	2400.0	13000.0	False
527.0 3 OFFICE 0.0	918.0	13918.0	3600.0	3600.0	False
4 OFFICE	0.0	16200.0	3600.0	3600.0	True
	COST TO REACH	REACHED AT	SERVICE TIME	LEAVING TIME	LUNCH_BEFORE
WAIT_BEFORE O OFFICE	0.0	0.0	3600.0	3600.0	False
0.0 1 OFFICE 0.0	0.0	16200.0	3600.0	3600.0	True

Agent 5 POSITION	COST TO I	REACH	REACHED AT	SERVICE TIME	LEAVING TIME	LUNCH_BEFORE
WAIT_BEFORE O OFFICE		0.0	0.0	3600.0	3600.0	False
0.0 1 OFFICE 0.0		0.0	16200.0	3600.0	3600.0	True
Agent 6 POSITION WAIT_BEFORE	COST TO I	REACH	REACHED AT	SERVICE TIME	LEAVING TIME	LUNCH_BEFORE
0 OFFICE 0.0		0.0	0.0	3600.0	3600.0	False
1 OFFICE		0.0	16200.0	3600.0	3600.0	True
Agent 7 POSITION WAIT_BEFORE	COST TO I	REACH	REACHED AT	SERVICE TIME	LEAVING TIME	LUNCH_BEFORE
0 OFFICE 0.0		0.0	0.0	3600.0	3600.0	False
1 OFFICE 0.0		0.0	16200.0	3600.0	3600.0	True
Agent 8 POSITION WAIT BEFORE	COST TO I	REACH	REACHED AT	SERVICE TIME	LEAVING TIME	LUNCH_BEFORE
POSITION WAIT_BEFORE O OFFICE		REACH 0.0	REACHED AT	SERVICE TIME 3600.0	LEAVING TIME 3600.0	LUNCH_BEFORE False
POSITION WAIT_BEFORE						
POSITION WAIT_BEFORE 0 OFFICE 0.0 1 OFFICE 0.0 Agent 9 POSITION	COST TO I	0.0	0.0	3600.0	3600.0 3600.0	False True
POSITION WAIT_BEFORE 0 OFFICE 0.0 1 OFFICE 0.0 Agent 9 POSITION WAIT_BEFORE 0 OFFICE	COST TO I	0.0	0.0	3600.0 3600.0	3600.0 3600.0	False True
POSITION WAIT_BEFORE 0 OFFICE 0.0 1 OFFICE 0.0 Agent 9 POSITION WAIT_BEFORE	COST TO I	0.0 0.0 REACH	0.0 16200.0 REACHED AT	3600.0 3600.0 SERVICE TIME	3600.0 3600.0 LEAVING TIME	False True LUNCH_BEFORE
POSITION WAIT_BEFORE 0 OFFICE 0.0 1 OFFICE 0.0 Agent 9 POSITION WAIT_BEFORE 0 OFFICE 0.0 1 OFFICE 0.0 Agent 10 POSITION	COST TO I	0.0 0.0 REACH 0.0	0.0 16200.0 REACHED AT 0.0 16200.0	3600.0 3600.0 SERVICE TIME 3600.0	3600.0 3600.0 LEAVING TIME 3600.0 3600.0	False True LUNCH_BEFORE False True
POSITION WAIT_BEFORE 0 OFFICE 0.0 1 OFFICE 0.0 Agent 9 POSITION WAIT_BEFORE 0 OFFICE 0.0 1 OFFICE 0.0 Agent 10	COST TO I	0.0 0.0 REACH 0.0	0.0 16200.0 REACHED AT 0.0 16200.0	3600.0 3600.0 SERVICE TIME 3600.0 3600.0	3600.0 3600.0 LEAVING TIME 3600.0 3600.0	False True LUNCH_BEFORE False True

[13]: print(scheds)

{0: [('wait', 0.0, -1), ('meet', 3600.0, 8), ('travel', 6000.0, -1), ('wait', 6208.0, -1), ('meet', 8400.0, 2), ('travel', 10800.0, -1), ('wait', 11430.0, -1), ('meet', 13000.0, 9), ('lunch', 15400.0, -1), ('travel', 17200.0, -1), ('office', 18045.0, 0), ('travel', 24305.0, -1), ('meet', 24800.0, 1), ('wait', 27200.0, -1), ('end', 28800, -1)], 1: [('wait', 0.0, -1), ('meet', 4700.0, 7), ('travel', 7100.0, -1), ('wait', 7481.0, -1), ('meet', 11900.0, 5), ('travel', 14300.0, -1), ('wait', 14667.0, -1), ('meet', 16800.0, 10), ('lunch', 19200.0, -1), ('travel', 21000.0, -1), ('wait', 21614.0, -1), ('meet', 23400.0, 4), ('wait', 25800.0, -1), ('end', 28800, -1)], 2: [('office', 0.0, 0), ('travel', 5223.0, -1), ('meet', 7100.0, 6), ('travel', 9500.0, -1), ('wait', 10073.0, -1), ('meet', 10600.0, 3), ('travel', 13000.0, -1), ('office', 13918.0, 0), ('lunch', 14400, -1), ('office', 16200, 0), ('end', 28800, -1)], 3: [('office', 0.0, 0), ('lunch', 14400, -1), ('office', 16200, 0), ('end', 28800, -1)], 4: [('office', 0.0, 0), ('lunch', 14400, -1), ('office', 16200, 0), ('end', 28800, -1)], 5: [('office', 0.0, 0), ('lunch', 14400, -1), ('office', 16200, 0), ('end', 28800, -1)], 6: [('office', 0.0, 0), ('lunch', 14400, -1), ('office', 16200, 0), ('end', 28800, -1)], 7: [('office', 0.0, 0), ('lunch', 14400, -1), ('office', 16200, 0), ('end', 28800, -1)], 8: [('office', 0.0, 0), ('lunch', 14400, -1), ('office', 16200, 0), ('end', 28800, -1)], 9: [('office', 0.0, 0), ('lunch', 14400, -1), ('office', 16200, 0), ('end', 28800, -1)]}

[]: