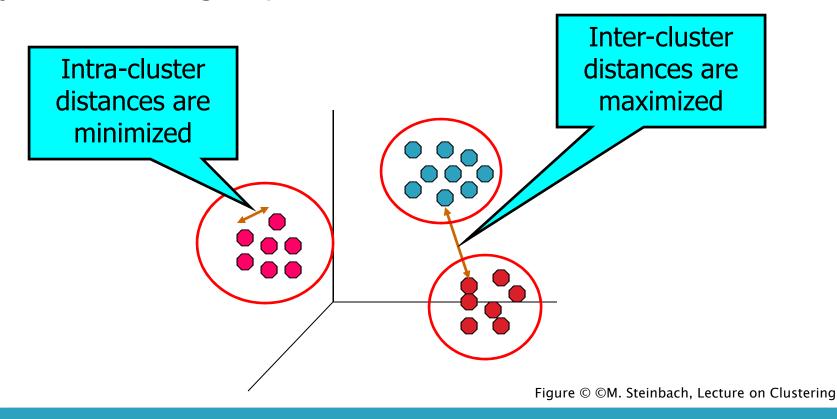
# Cluster Analysis (Part A)

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## Cluster Analysis

Cluster analysis or clustering: Finding groups of objects such that the objects in a group will be similar (or related) to one another and different from (or unrelated to) the objects in other groups.



#### **Applications**

- Document clustering (news, ...)
- Sentiment analysis (customer reviews, ...)
- Gene expression clustering
- Clustering of patients based on phenotypic and genotypic factors for efficient disease diagnosis
- Market Segmentation
- Anomaly detection
- Fraud detection
- Finding groups of driver behaviors based upon patterns of automobile motions (normal, drunken, sleepy, rush hour driving, etc.)

**...** 

#### Major Clustering Approaches

- Partitioning-based approach
  - Construct various partitions and then evaluate them by some criterion, e.g., minimizing the sum of square errors.
  - Typical methods: k-means, k-medoids, CLARA, CLARANS
- Density-based approach
  - Based on connectivity and density functions
  - Typical methods: DBSACN, OPTICS, DenClue
- Hierarchical approach
  - Create a hierarchical decomposition of the set of data (or objects) using some criterion
  - o Typical methods: Agnes, Diana, BIRCH, CURE, CAMELEON
- Model-based approach
  - A model is hypothesized for each of the clusters and tries to find the best fit of that model to each other
  - Typical methods: EM, SOM

#### Major Clustering Approaches (cont.)

- Grid-based approach
  - Based on a multiple-level granularity structure
  - Typical methods: STING, CLIQUE, WaveCluster
- Frequent Pattern-based approach
  - Based on the analysis of frequent patterns
  - Typical methods: p-Cluster
- Support Vector approach
  - Based on the idea of mapping data points into higher dimensional feature space via a kernel function.
  - Typical methods: SVC, Kernel K-means
- Graph Theoretic approach
  - Typical methods: Spectral Clustering

## Partitioning-based Approach

Construct various partitions and then evaluate them by some criterion, e.g., minimizing the sum of square errors.

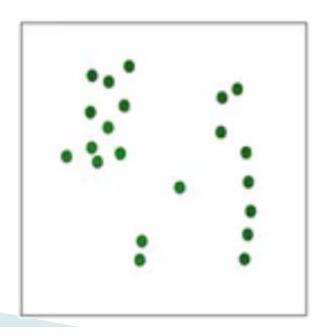
Example: K-means

# K-means Clustering

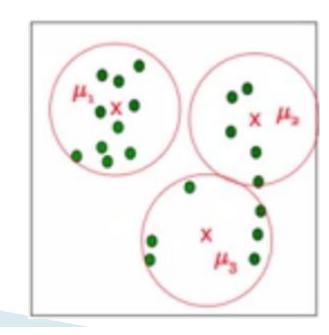
- Assume K clusters
- Iterate between two following steps:
  - Updating the assignment of data to clusters
  - Updating the cluster's summarization

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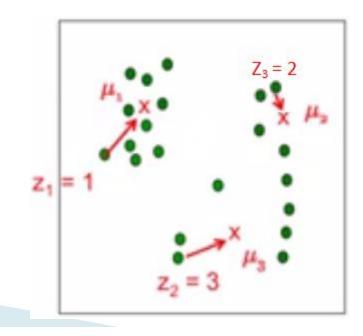
sklearn.cluster.KMeans



- Assume K clusters
- Iterate between two following steps
  - A. Updating the assignment of data to clusters
  - B. Updating the cluster's summarization
- $\square$  Each cluster C is described by a centroid  $\mu_c$



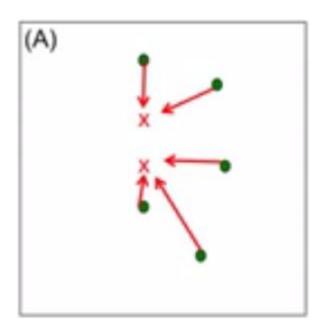
- Assume K clusters
- Iterate between two following steps:
  - A. Updating the assignment of data to clusters
  - B. Updating the cluster's summarization
- □ Assignment of  $i_{th}$  example:  $z_i \in 1...K$



Iterate until convergence

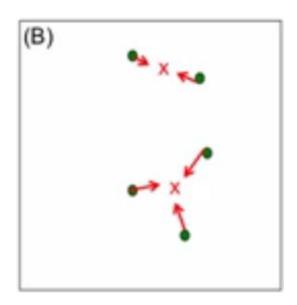
A. For each data, find the closest centroid:

$$z_i = \underset{c}{\operatorname{argmin}} ||x_i - \mu_c||^2, \forall i$$



- Iterate until convergence
  - B. Set each cluster to the mean of all assigned data:

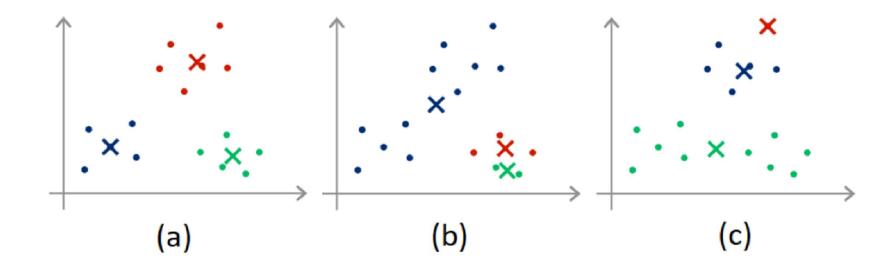
$$\forall c$$
,  $\mu_c = 1/m_c \sum_{i \in S_c} x_i$   $S_c = \{i: z_i = c\}, m_c = |S_c|$ 



<u>Demo</u>

#### **K-means Properties**

Poor initialization may lead to poor clustering



- Solution?
  - Multiple Initializations → randomness
  - K-means++, Intelligent K-means

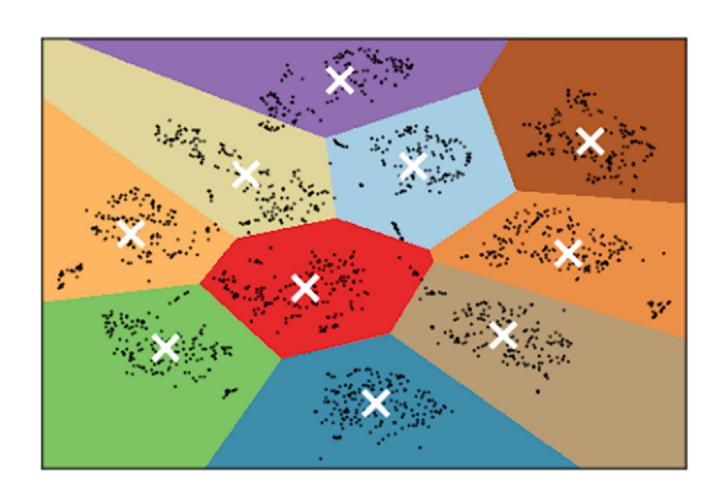
#### K-means Properties (cont.)

- Distance metrics
  - $oldsymbol{l}_1$  norm (Manhattan distance)
  - o *l*<sub>2</sub> norm (Euclidean distance)
  - Cosine similarity
- Centroids
  - Mean
  - Median → Outliers?
  - Medoid
    - Most commonly used on data when a mean or centroid cannot be defined, such as graphs.

#### K-means Properties (cont.)

- Instance-based
- □ Time complexity: O(tkm)
- Non-parametric
- Linearly separable data

# K-means: Linear Separable



## Sum of Square Error

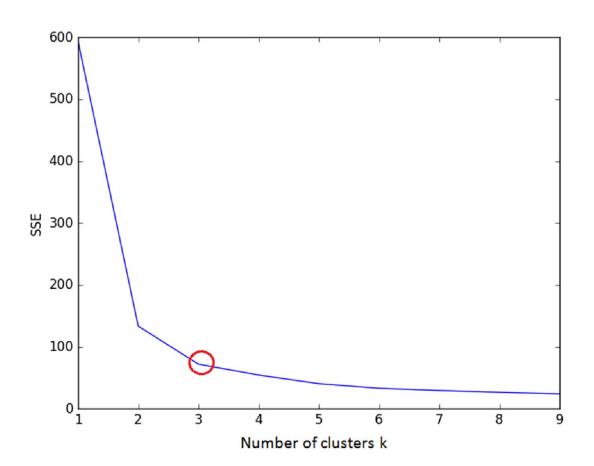
Sum of Square Error (SSE)

$$SSE = \sum_{k} \sum_{\boldsymbol{x_i} \in C_k} ||\boldsymbol{x_i} - C_k||^2$$

Goal: minimizing within-cluster distance

# Optimal number of Clusters

#### Elbow method

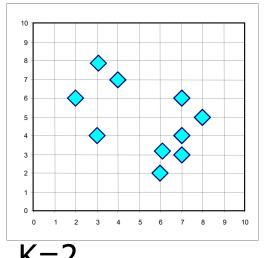


#### K-means Variations

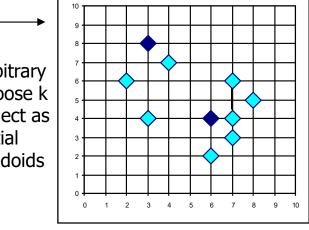
- K-medoids/PAM (Partitioning Around Medoids)
- CLARA (Clustering Large Applications)
- CLARANS (A Clustering Algorithm based on Randomized Search)

# **PAM Algorithm**

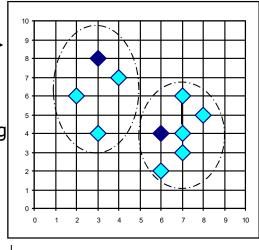




**Arbitrary** choose k object as initial medoids



Assign each remaining object to nearest medoids



K=2

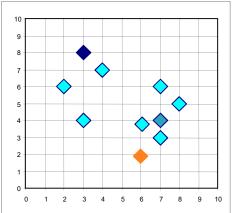
Total Cost = 26

Randomly select a nonmedoid object, O<sub>ramdom</sub>

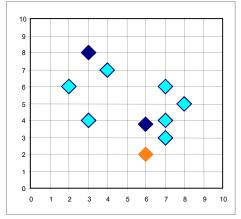
Do loop **Until** no

change

Swapping O and O<sub>ramdom</sub> If quality is improved.



Compute total cost of swapping

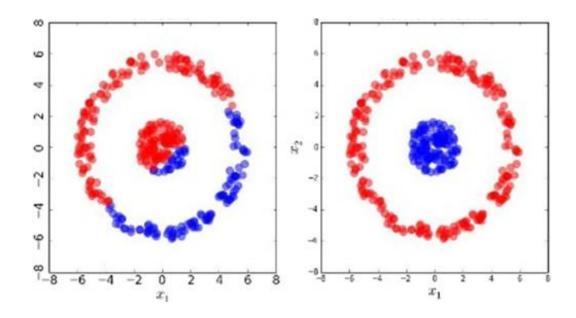


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# K-means Variations (cont.)

Fuzzy C-means

■ Kernel K-means



# **Further Reading**

- Mean Shift Clustering
- Clustering Categorical Data
  - ROCK (robust clustering algorithm for categorical attributes)
  - Sudipto Guha, Rajeev Rastogi, Kyuseok Shim, ICDE'99

#### References

□ Jiawei Han, Micheline Kamber and Jian Pei, Data Mining: Concepts and Techniques, 3<sup>rd</sup> edition, 2006.