

# Digital Image Processing

 Morphological Image Processing

Once segmentation is complete, morphological operations can be used to remove imperfections in the segmented image and provide information on the form and structure of the image

In this lecture we will consider

- What is morphology?
- Simple morphological operations
- Compound operations
- Morphological algorithms

✓✓ Throughout all of the following slides whether 0 and 1 refer to white or black is a little interchangeable

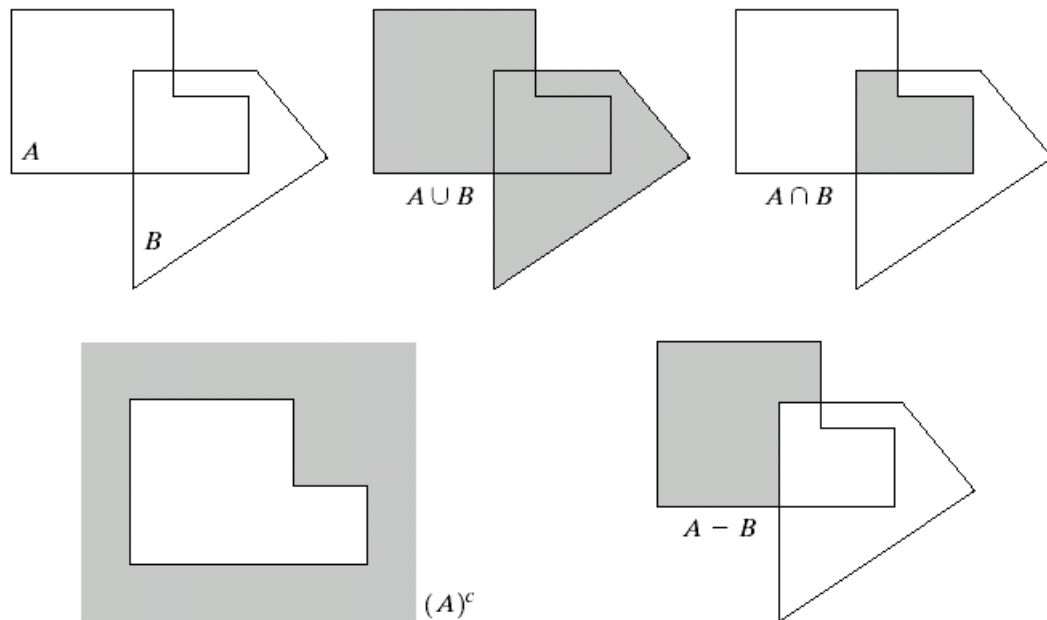
All of the discussion that follows assumes segmentation has already taken place and that images are made up of 0s for background pixels and 1s for object pixels

After this it doesn't matter if 0 is black, white, yellow, green.....

# What Is Morphology?

Morphological image processing (or *morphology*) describes a range of image processing techniques that deal with the shape (or morphology) of features in an image

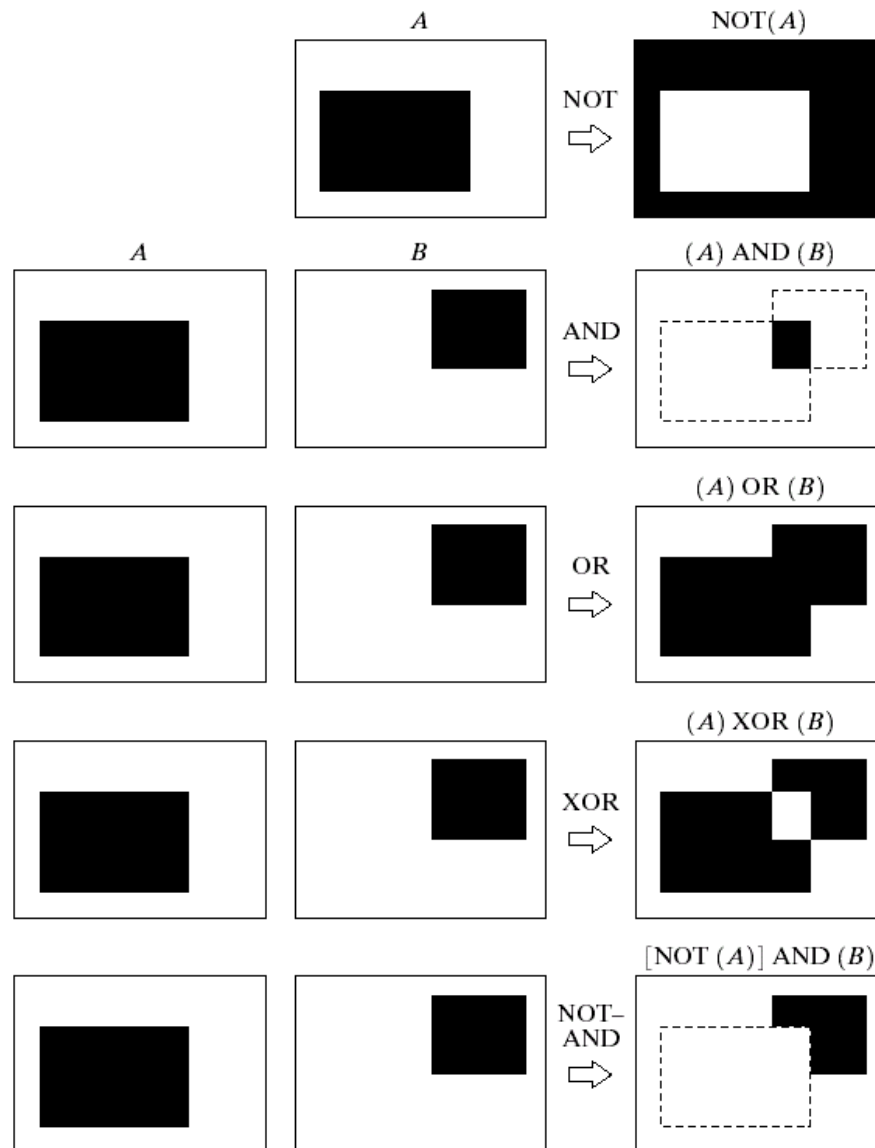
Morphological operations are typically applied to remove imperfections introduced during segmentation, and so typically operate on bi-level images



a	b	c
d	e	

**FIGURE 9.1**

(a) Two sets  $A$  and  $B$ . (b) The union of  $A$  and  $B$ . (c) The intersection of  $A$  and  $B$ . (d) The complement of  $A$ . (e) The difference between  $A$  and  $B$ .



**FIGURE 9.3** Some logic operations between binary images. Black represents binary 1s and white binary 0s in this example.

# Quick Example

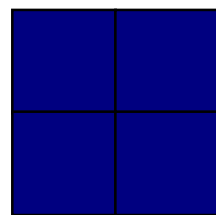
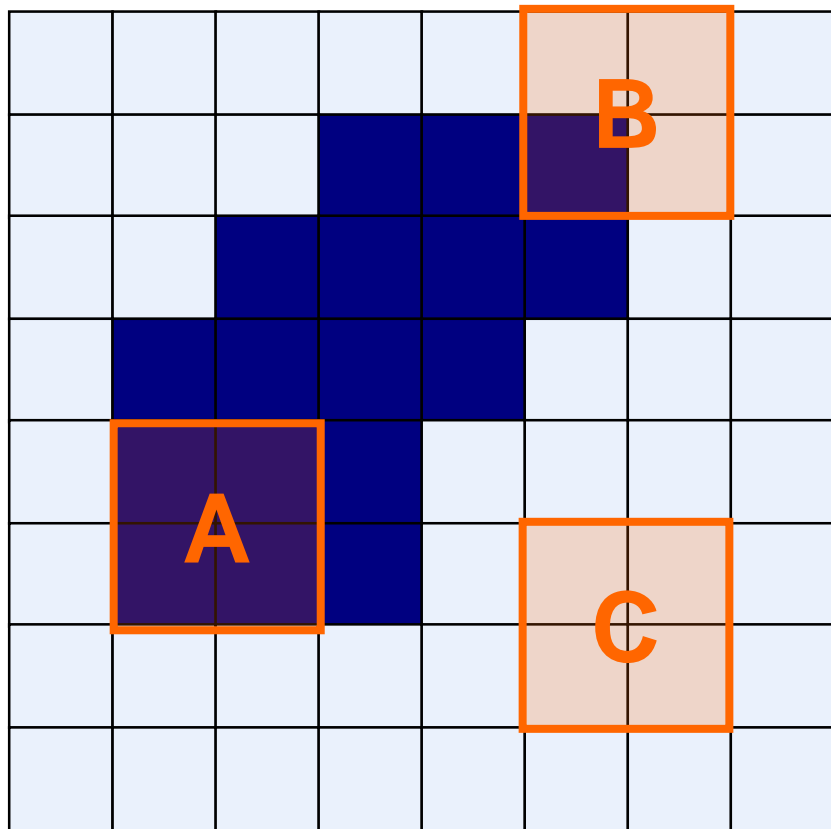


Image after segmentation



Image after segmentation and  
morphological processing

# Structuring Elements, Hits & Fits



Structuring Element

**Fit:** All on pixels in the structuring element cover on pixels in the image

**Hit:** Any on pixel in the structuring element covers an on pixel in the image

All morphological processing operations are based on these simple ideas



# Structuring Elements

✓ Structuring elements can be any size and make any shape

✓ However, for simplicity we will use rectangular structuring elements with their origin at the middle pixel

1	1	1
1	<b>1</b>	1
1	1	1

0	1	0
1	<b>1</b>	1
0	1	0

0	0	1	0	0
0	1	1	1	0
1	1	<b>1</b>	1	1
0	1	1	1	0
0	0	1	0	0

# Fitting & Hitting

0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	0	0	0	0	0	0	0
0	0	1	<b>B</b>	1	1	1	0	<b>C</b>	0	0	0
0	1	1	1	1	1	1	1	0	0	0	0
0	1	1	1	1	1	1	1	0	0	0	0
0	0	1	1	1	1	1	1	0	0	0	0
0	0	1	1	1	1	1	1	1	1	0	0
0	0	1	1	1	1	1	<b>A</b>	1	1	1	0
0	0	0	0	0	1	1	1	1	1	1	0
0	0	0	0	0	0	0	0	0	0	0	0

1	1	1
1	1	1
1	1	1

Structuring  
Element 1

0	1	0
1	1	1
0	1	0

Structuring  
Element 2

# Fundamental Operations

Fundamentally morphological image processing is very like spatial filtering

The structuring element is moved across every pixel in the original image to give a pixel in a new processed image

The value of this new pixel depends on the operation performed

There are two basic morphological operations: **erosion** and **dilation**

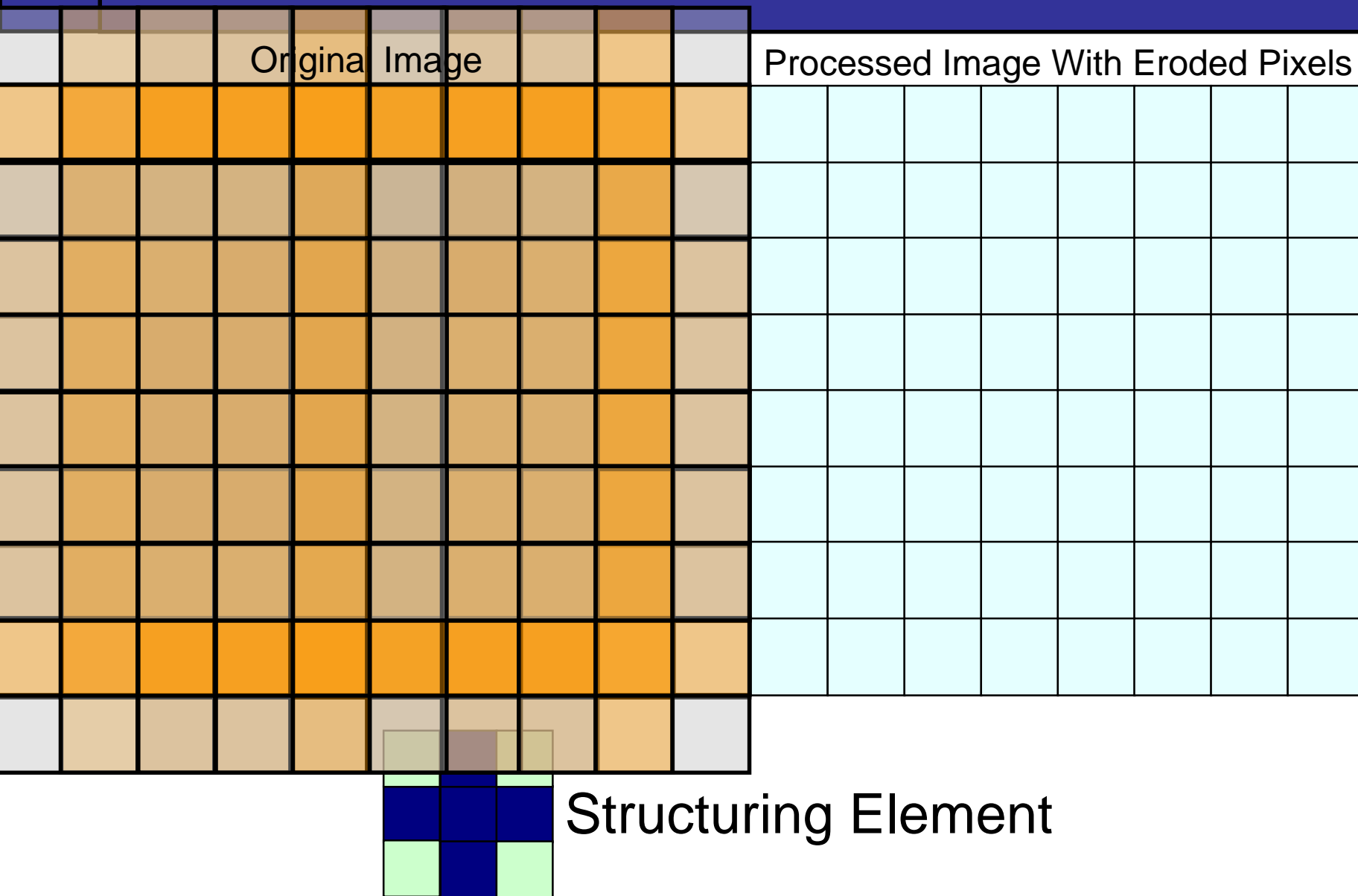
✓ Erosion of image  $f$  by structuring element  $s$  is given by  $f \ominus s$

The structuring element  $s$  is positioned with its origin at  $(x, y)$  and the new pixel value is determined using the rule:

$$g(x, y) = \begin{cases} 1 & \text{if } s \text{ fits } f \\ 0 & \text{otherwise} \end{cases}$$

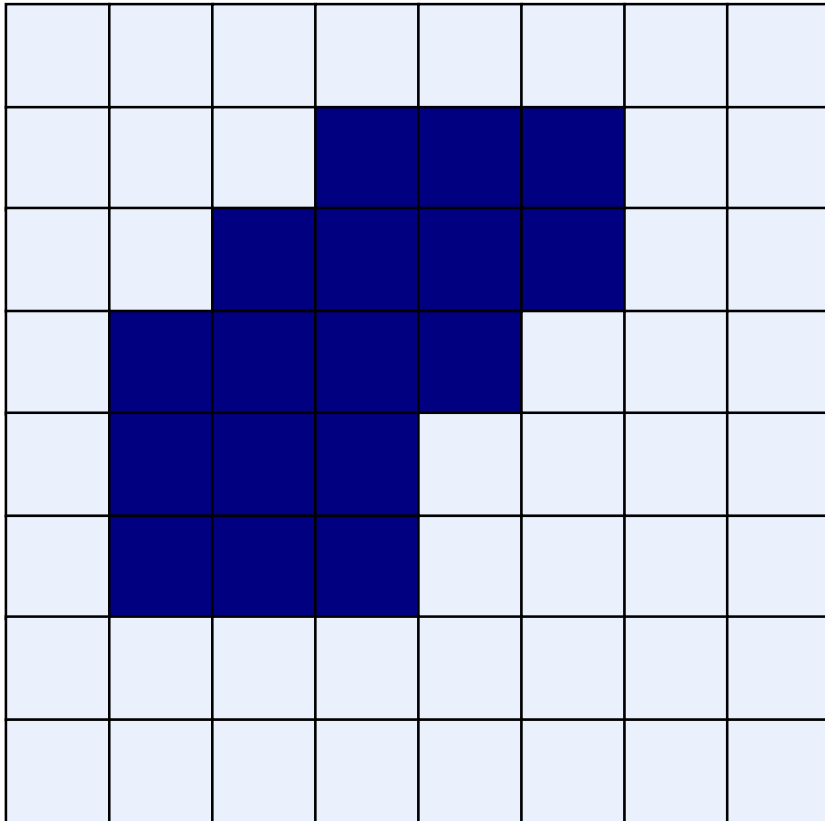
✓  
min A

# Erosion Example

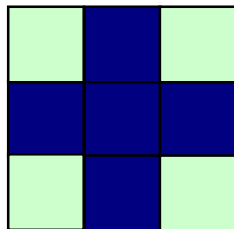
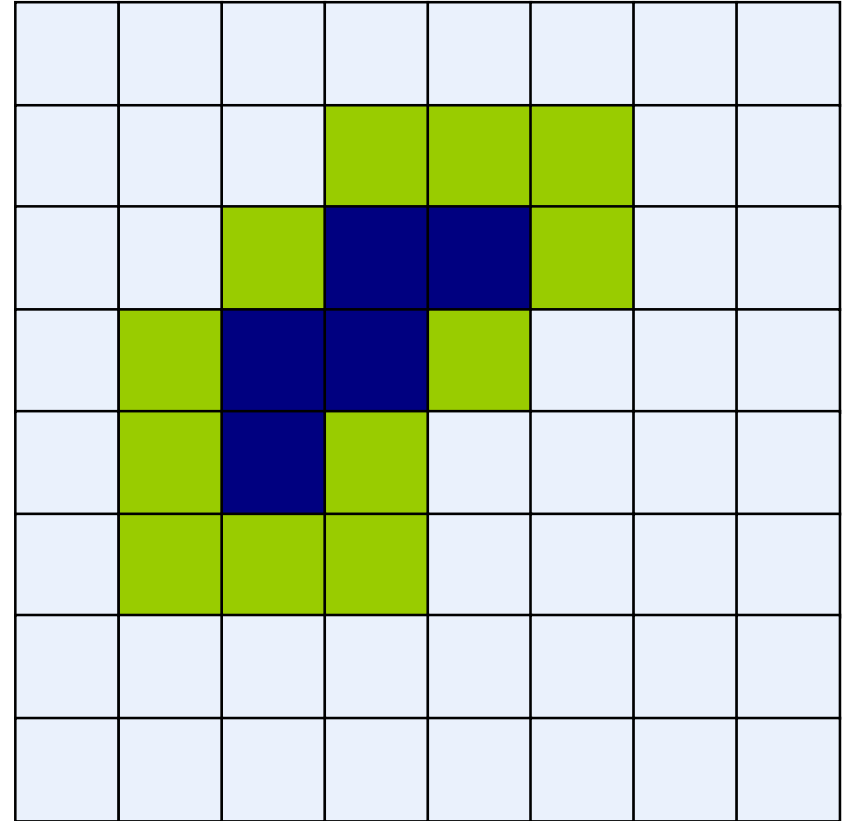


# Erosion Example

Original Image



Processed Image

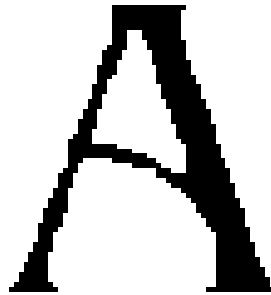


Structuring Element

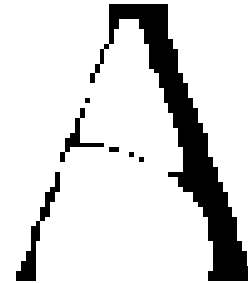
# Erosion Example 1



Original image



Erosion by 3\*3  
square structuring  
element

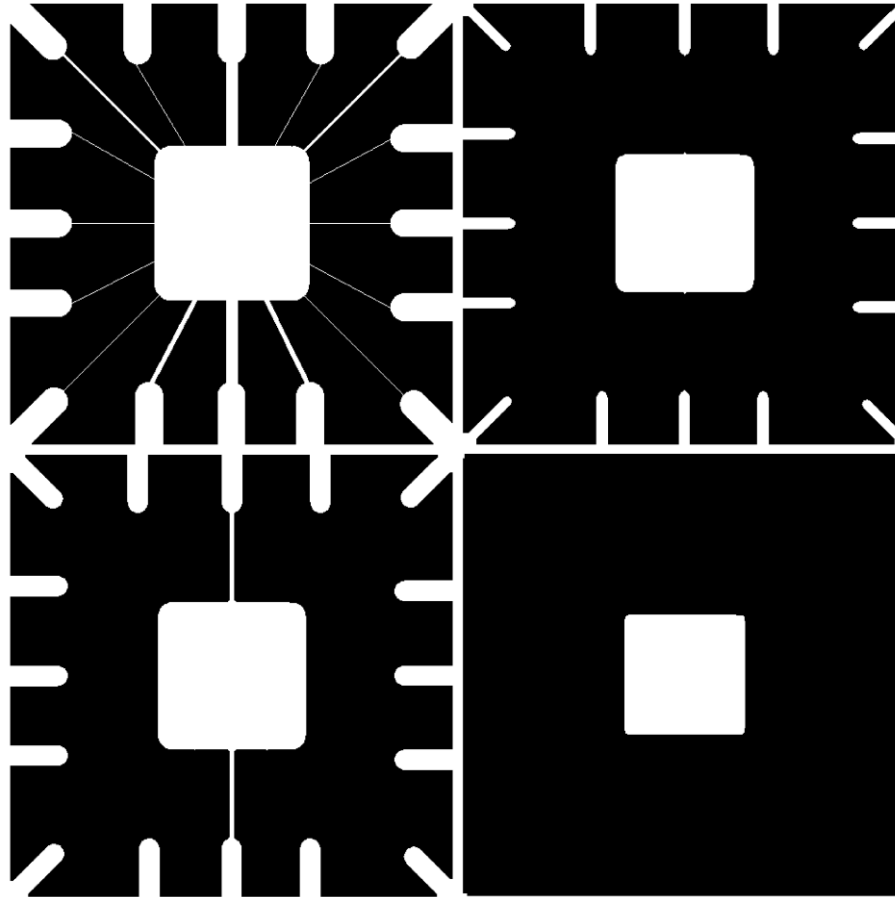


Erosion by 5\*5  
square structuring  
element

**Watch out:** In these examples a 1 refers to a black pixel!

# Erosion Example 2

Original  
image



After erosion  
with a disc of  
radius 10

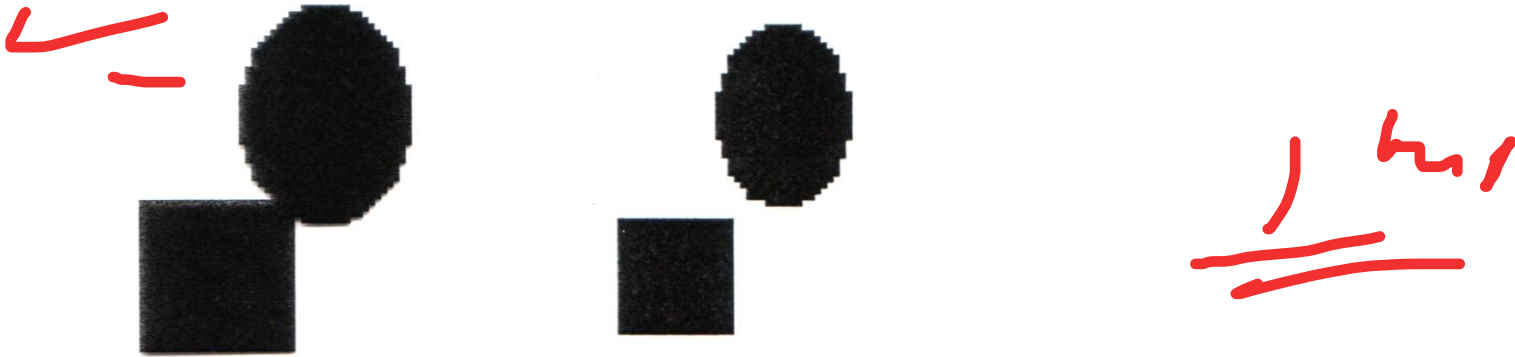
After erosion  
with a disc of  
radius 5

After erosion  
with a disc of  
radius 20

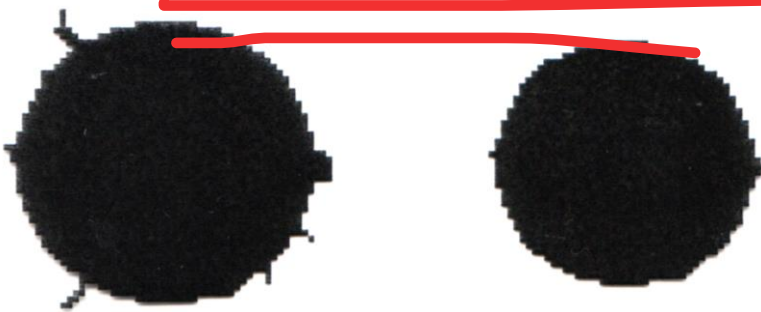


# What Is Erosion For?

Erosion can split apart joined objects



Erosion can strip away extrusions



**Watch out:** Erosion shrinks objects

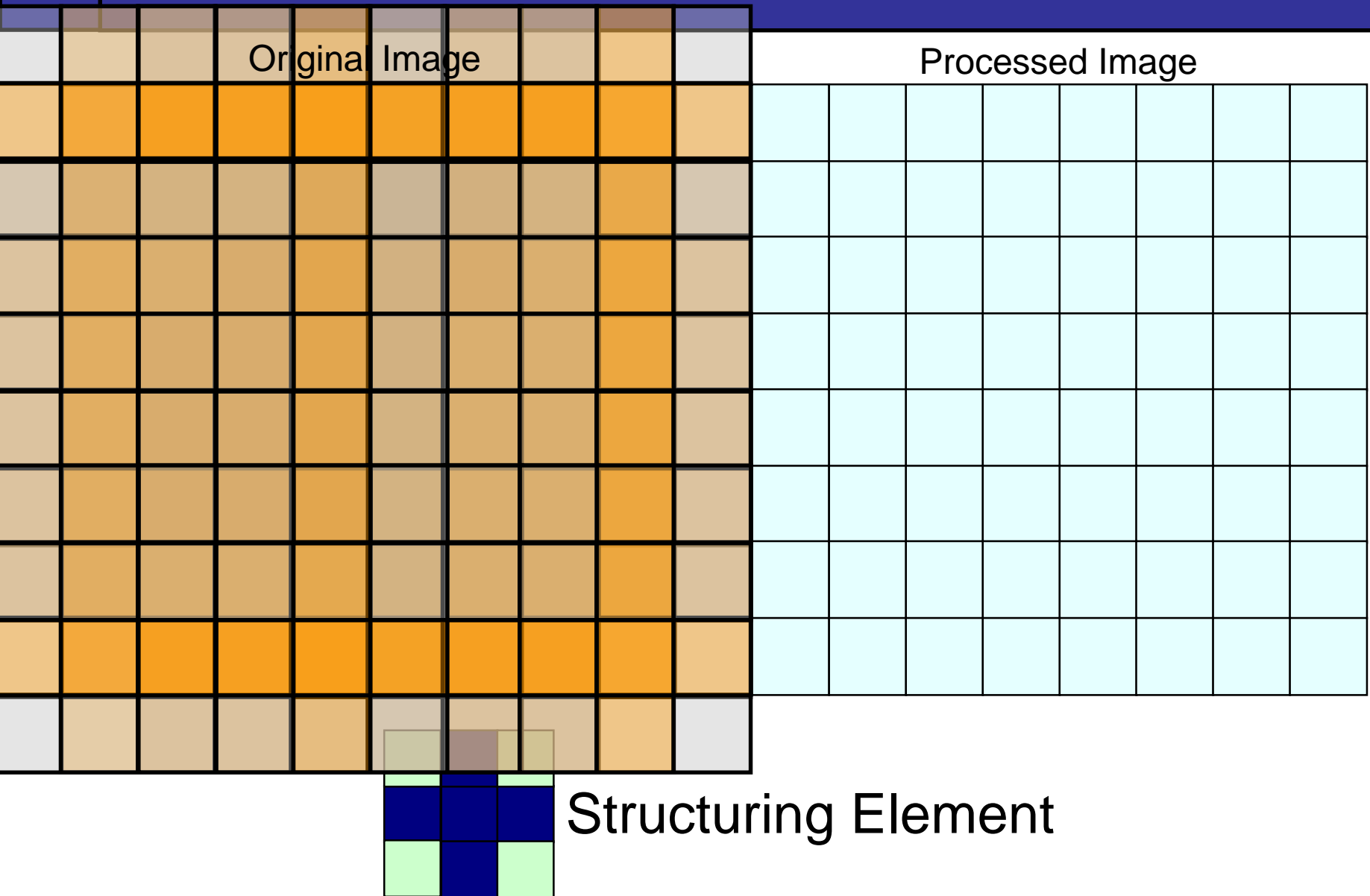
↖ Dilation of image  $f$  by structuring element  $s$  is given by  $f \oplus s$

The structuring element  $s$  is positioned with its origin at  $(x, y)$  and the new pixel value is determined using the rule:

$$g(x, y) = \begin{cases} 1 & \text{if } s \text{ hits } f \\ 0 & \text{otherwise} \end{cases}$$

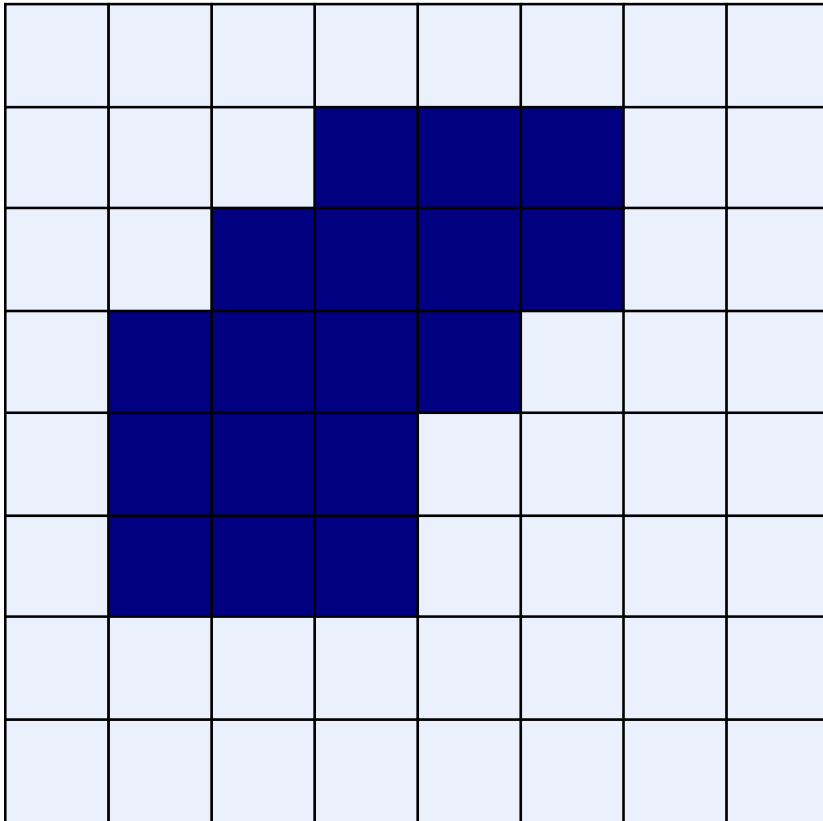
↖

# Dilation Example

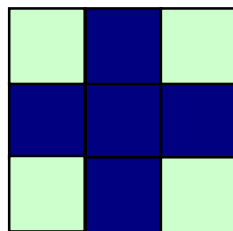
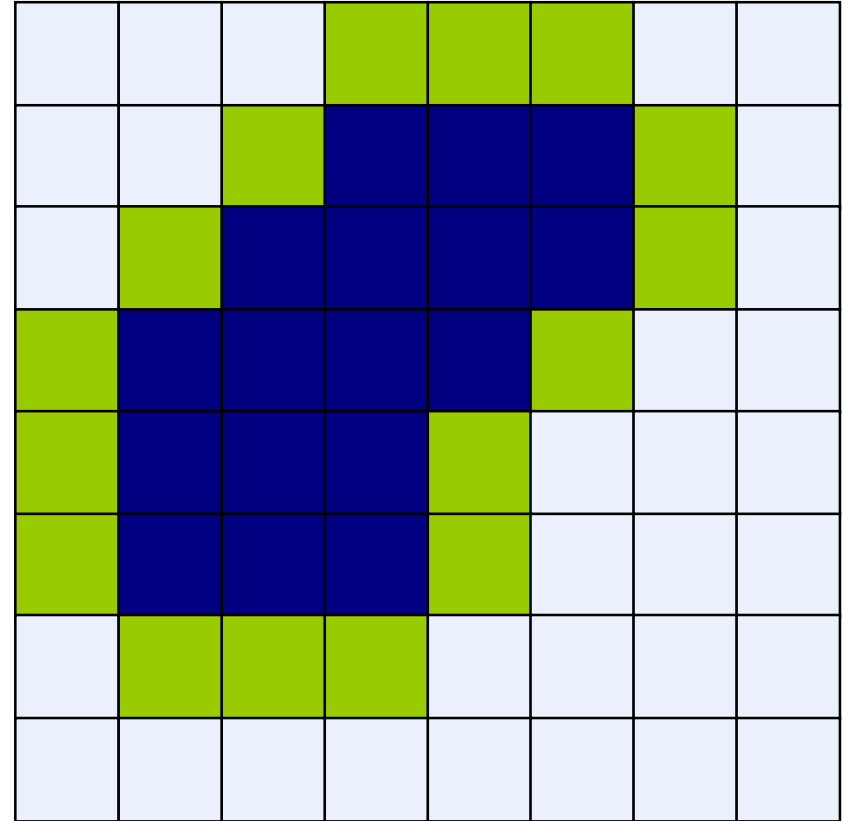


# Dilation Example

Original Image



Processed Image With Dilated Pixels



Structuring Element

# Dilation Example 1



Original image



Dilation by 3\*3  
square structuring  
element



Dilation by 5\*5  
square structuring  
element

**Watch out:** In these examples a 1 refers to a black pixel!

# Dilation Example 2

Original image

Historically, certain computer programs were written using only two digits rather than four to define the applicable year. Accordingly, the company's software may recognize a date using "00" as 1900 rather than the year 2000.



After dilation

Historically, certain computer programs were written using only two digits rather than four to define the applicable year. Accordingly, the company's software may recognize a date using "00" as 1900 rather than the year 2000.



0	1	0
1	1	1
0	1	0

Structuring element

# What Is Dilation For?

Dilation can repair breaks



Dilation can repair intrusions



Watch out: Dilation enlarges objects

# Compound Operations

More interesting morphological operations can be performed by performing combinations of erosions and dilations

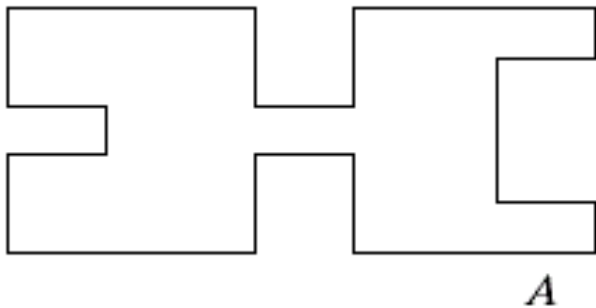
The most widely used of these *compound operations* are:

- Opening
- Closing

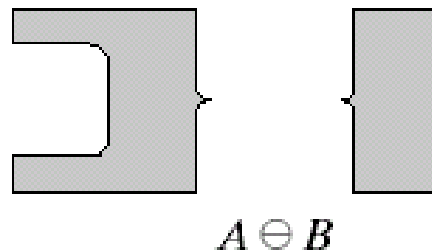


The opening of image  $f$  by structuring element  $s$ , denoted  $f \circ s$  is simply an erosion followed by a dilation

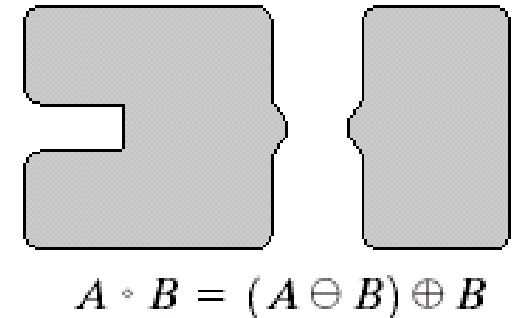
$$f \circ s = (f \ominus s) \oplus s$$



Original shape



After erosion



After dilation  
(opening)

Note a disc shaped structuring element is used

# Opening Example

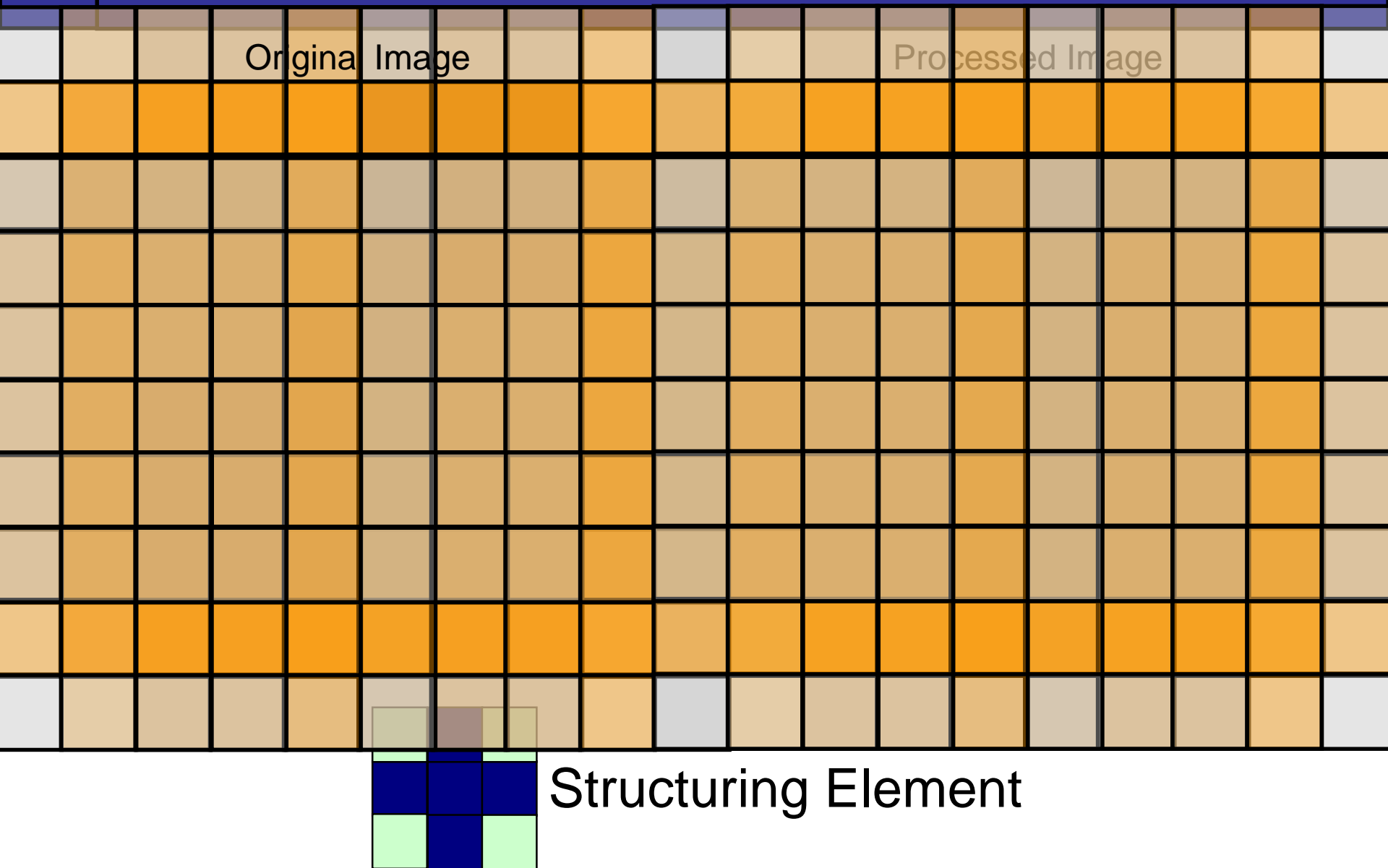
Original  
Image



Image  
After  
Opening

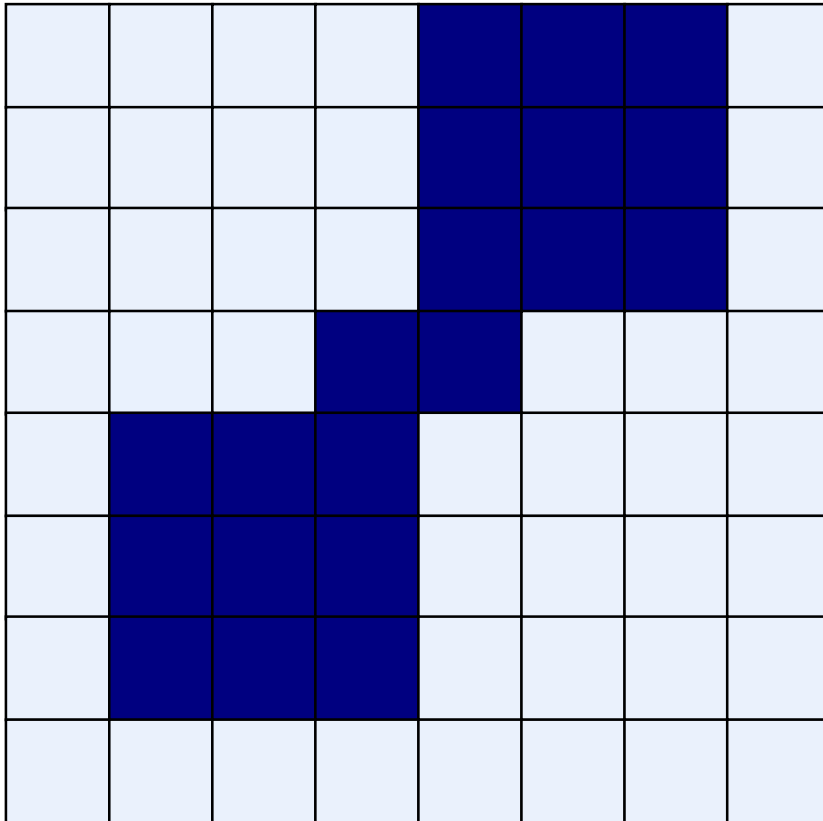


## Opening Example

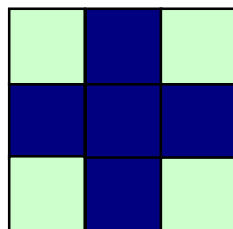
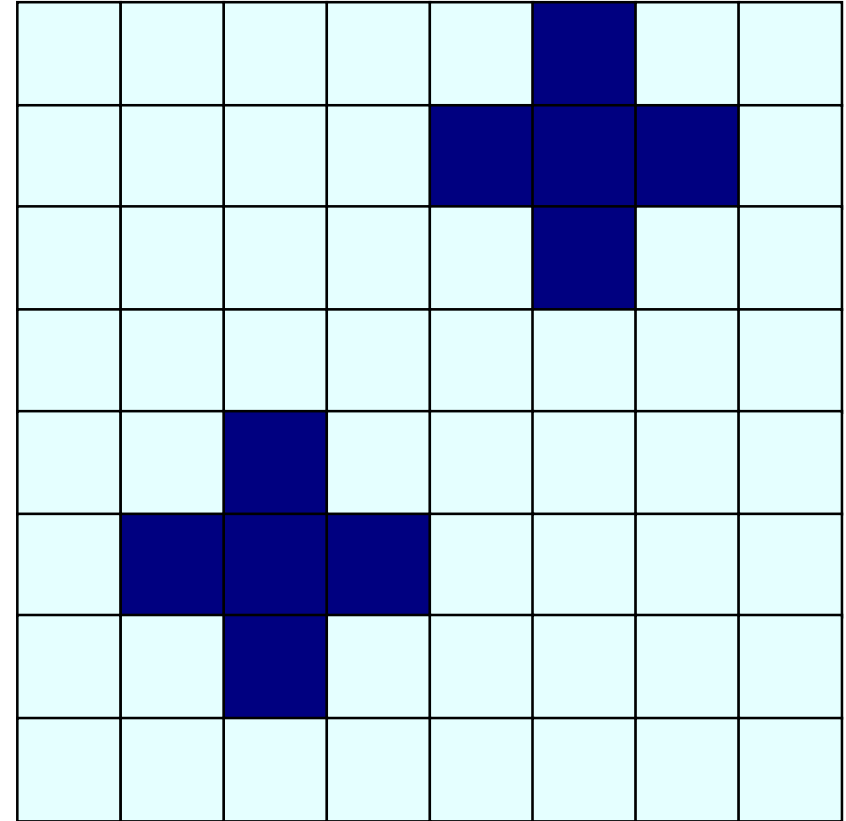


# Opening Example

Original Image



Processed Image

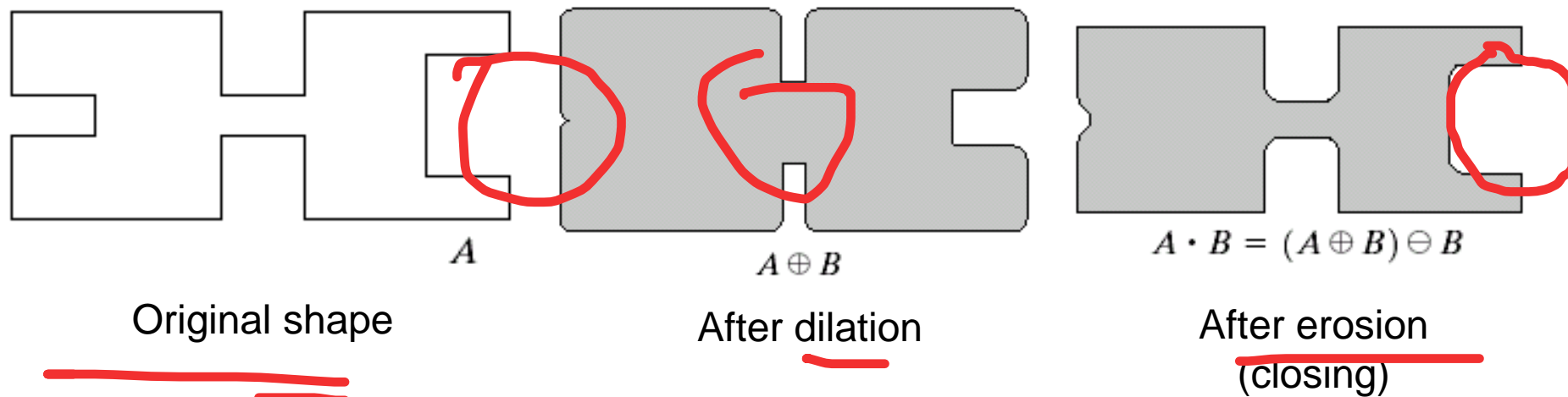


Structuring Element

*Handwritten red marks:*  
A large checkmark and some scribbles.

The closing of image  $f$  by structuring element  $s$ , denoted  $f \cdot s$  is simply a dilation followed by an erosion

$$f \cdot s = (f \oplus s) \ominus s$$



Note a disc shaped structuring element is used

# Closing Example

Original  
Image

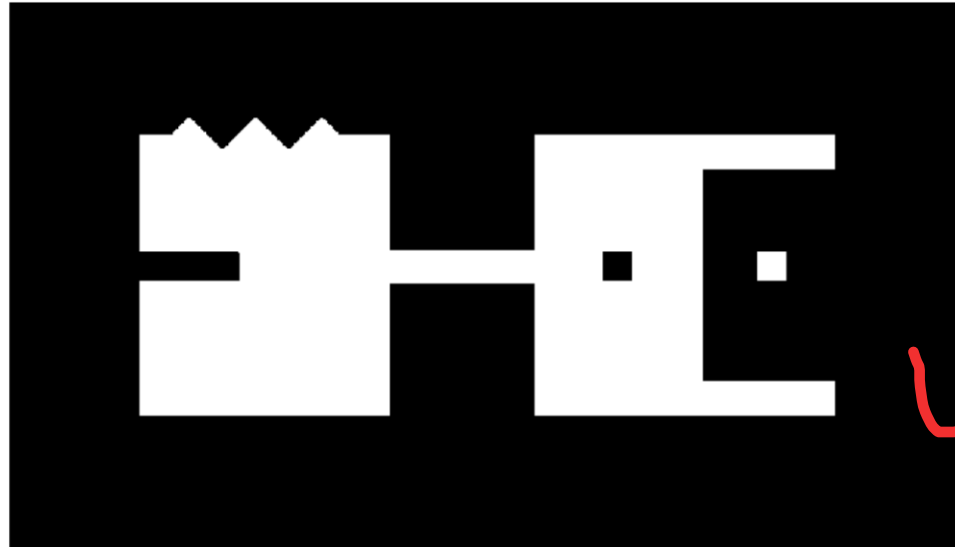
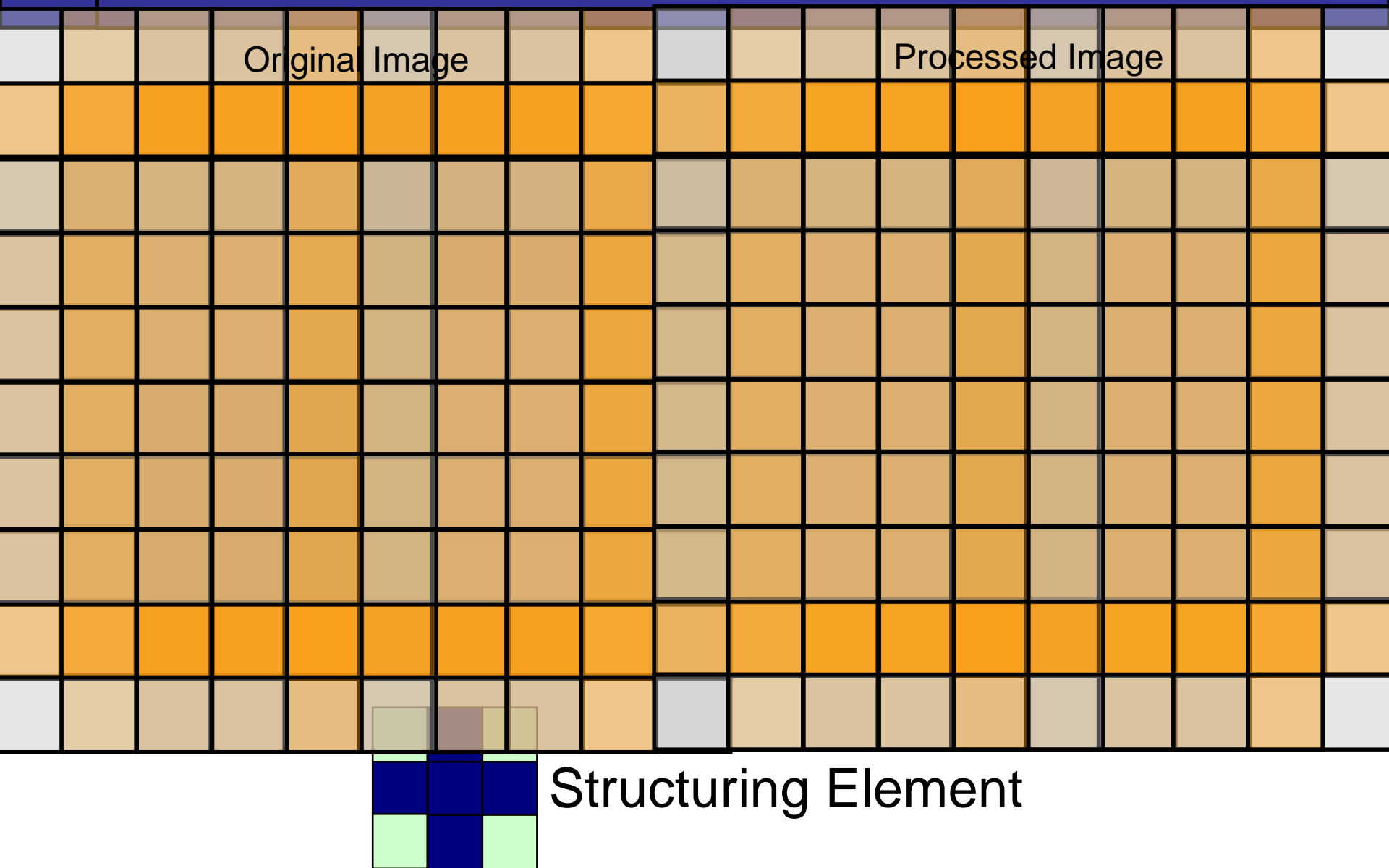


Image  
After  
Closing

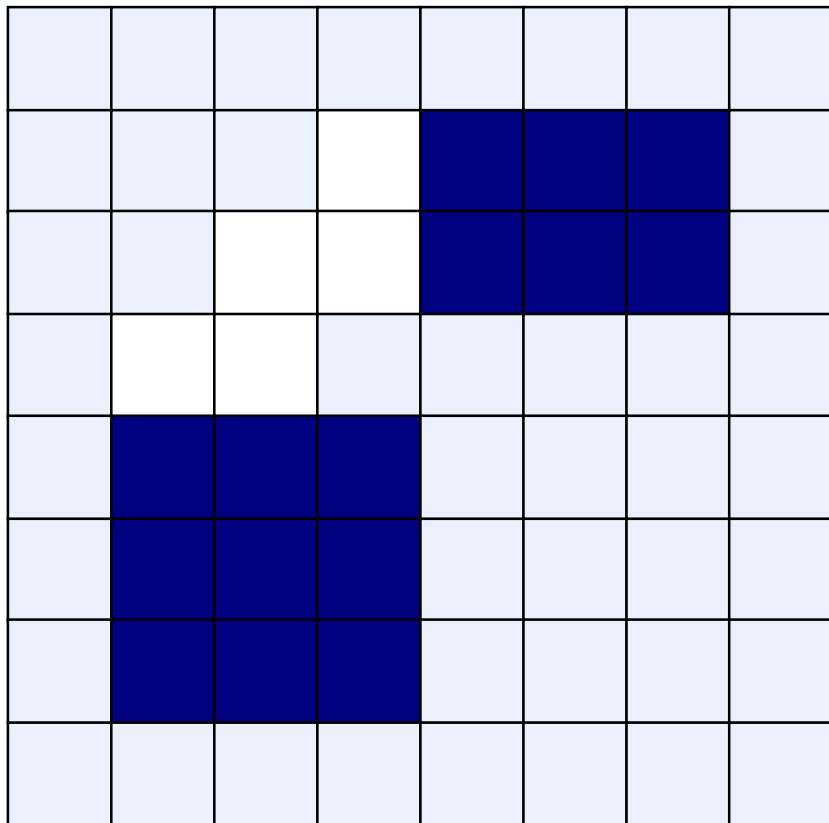


# Closing Example

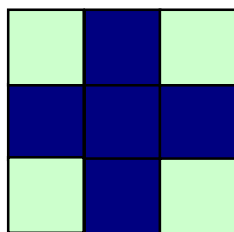
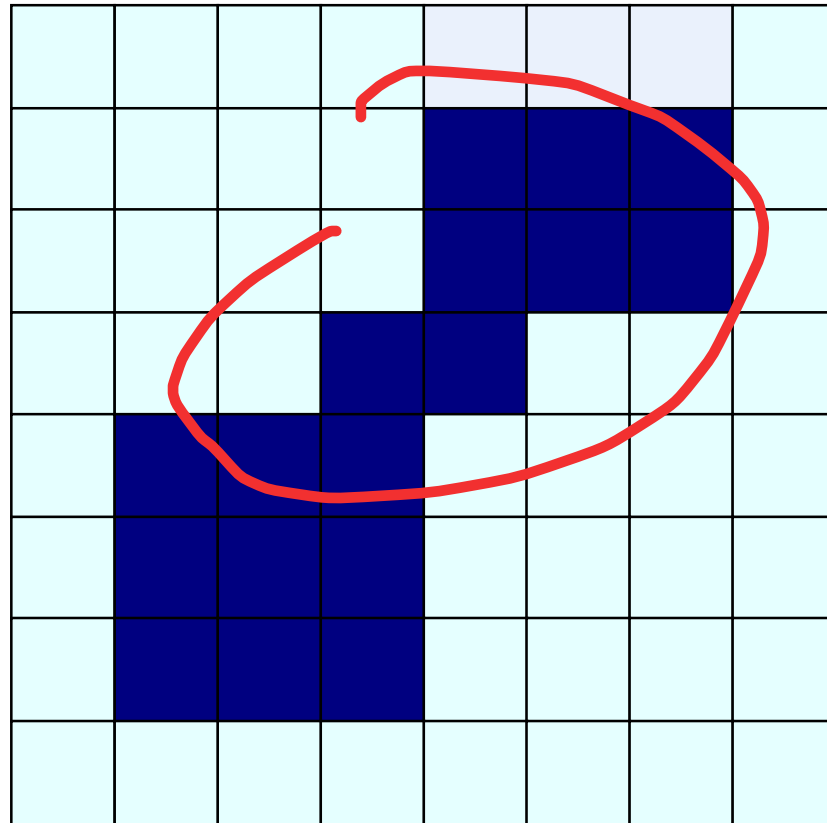


# Closing Example

Original Image



Processed Image

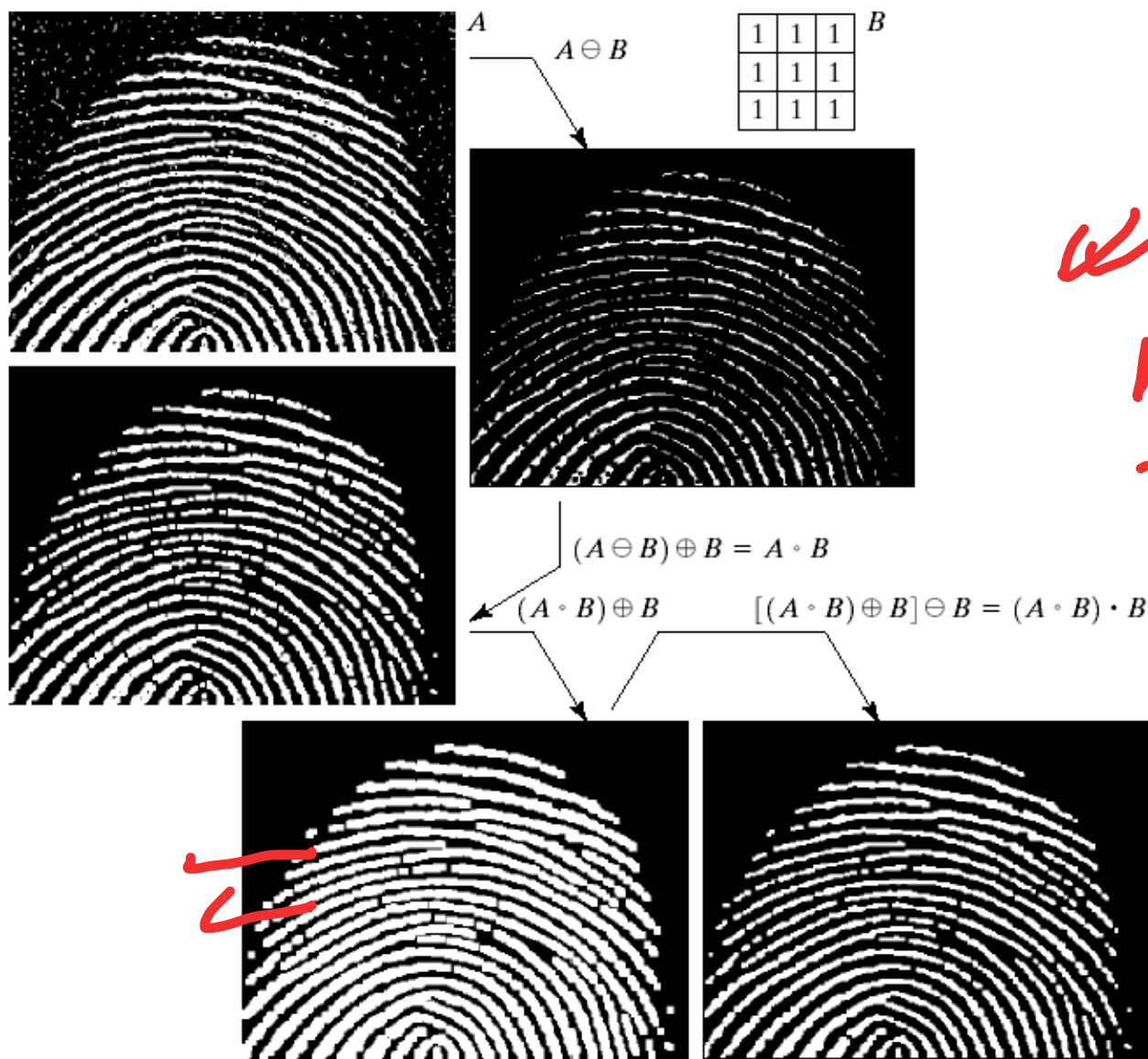


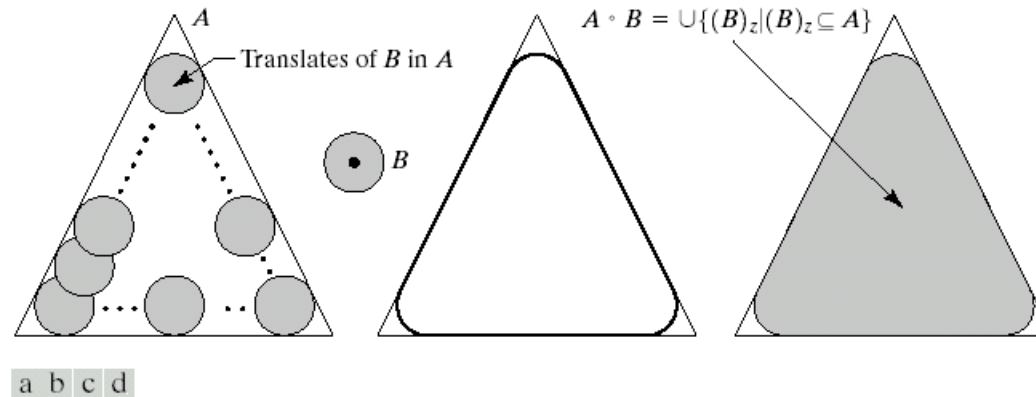
Structuring Element



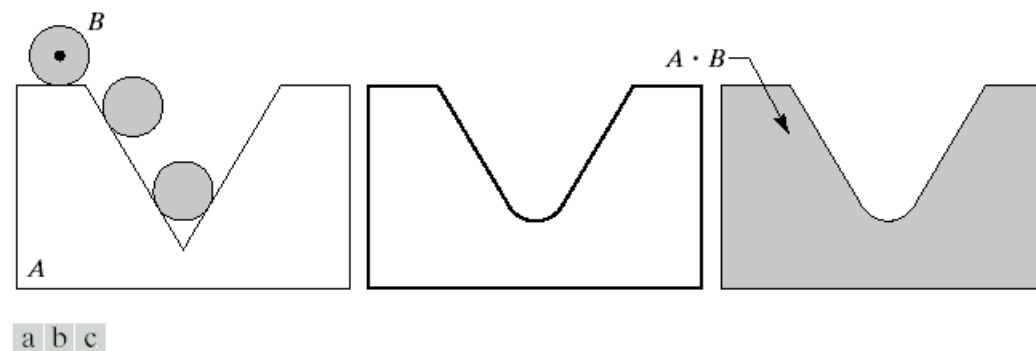


# Morphological Processing Example





**FIGURE 9.8** (a) Structuring element  $B$  "rolling" along the inner boundary of  $A$  (the dot indicates the origin of  $B$ ). (c) The heavy line is the outer boundary of the opening. (d) Complete opening (shaded).

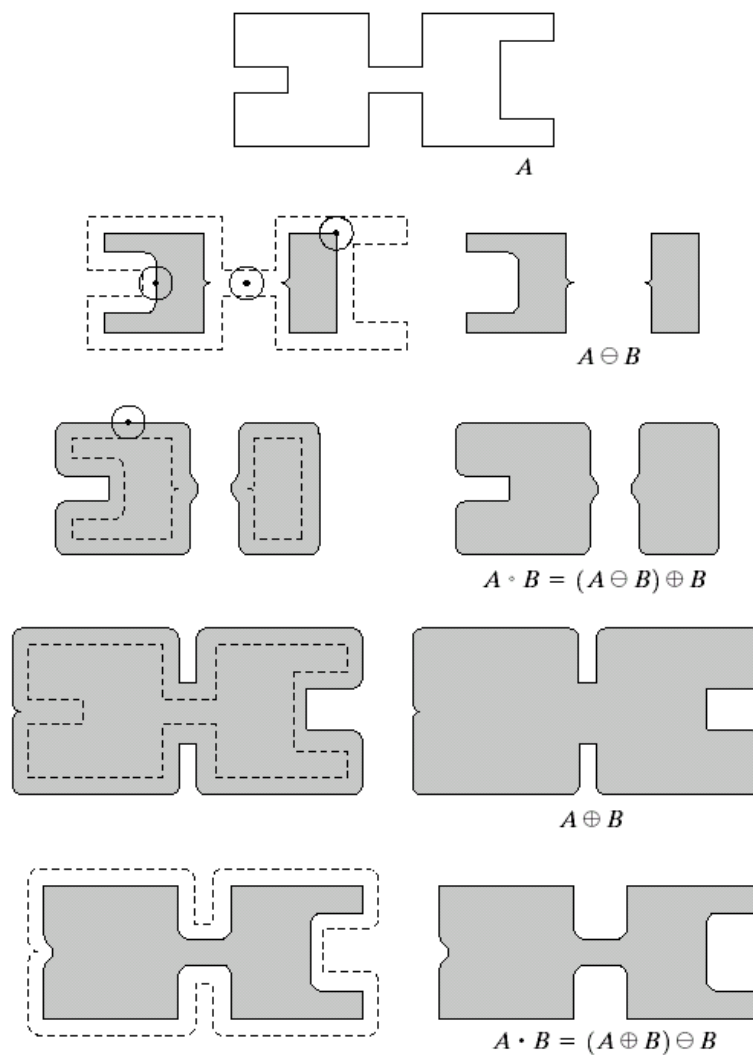


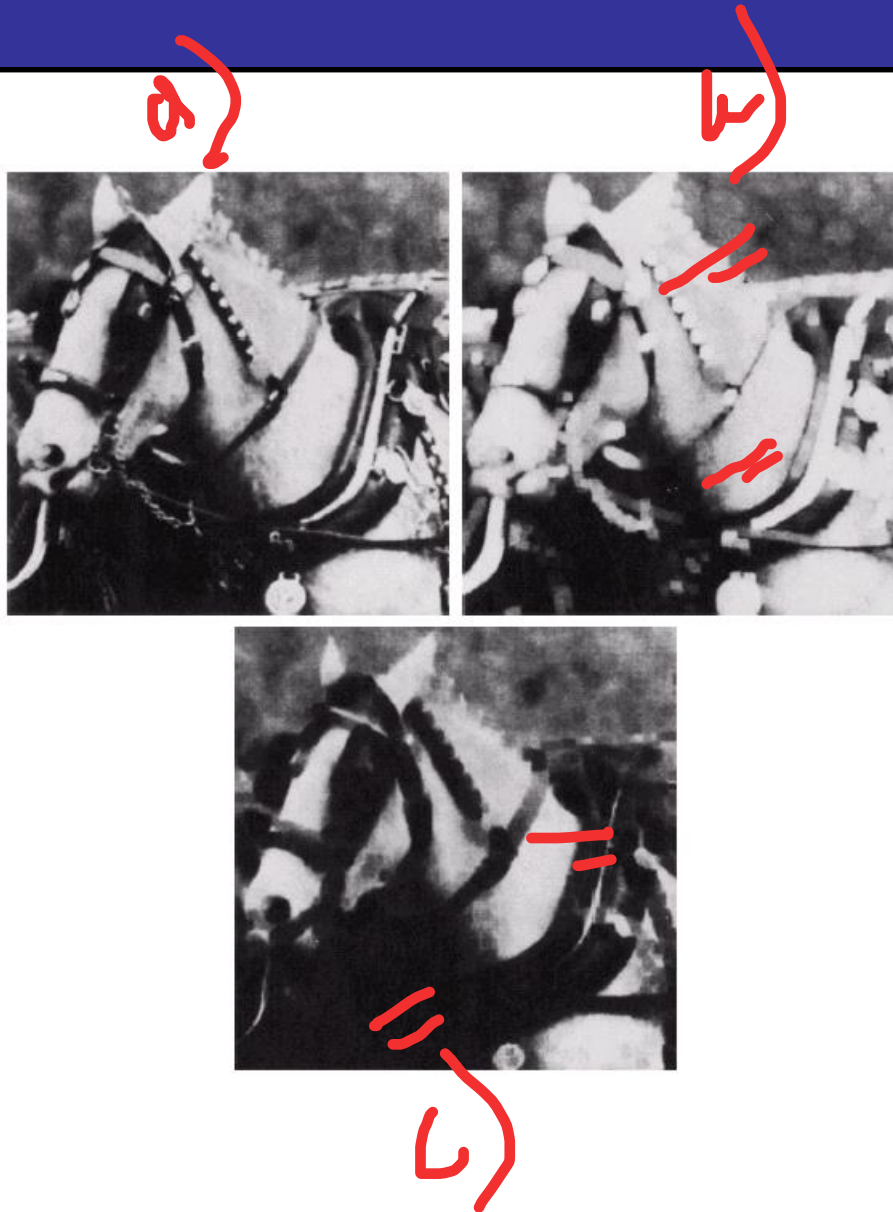
**FIGURE 9.9** (a) Structuring element  $B$  "rolling" on the outer boundary of set  $A$ . (b) Heavy line is the outer boundary of the closing. (c) Complete closing (shaded).

a
b c
d e
f g
h i

**FIGURE 9.10**

Morphological opening and closing. The structuring element is the small circle shown in various positions in (b). The dark dot is the center of the structuring element.

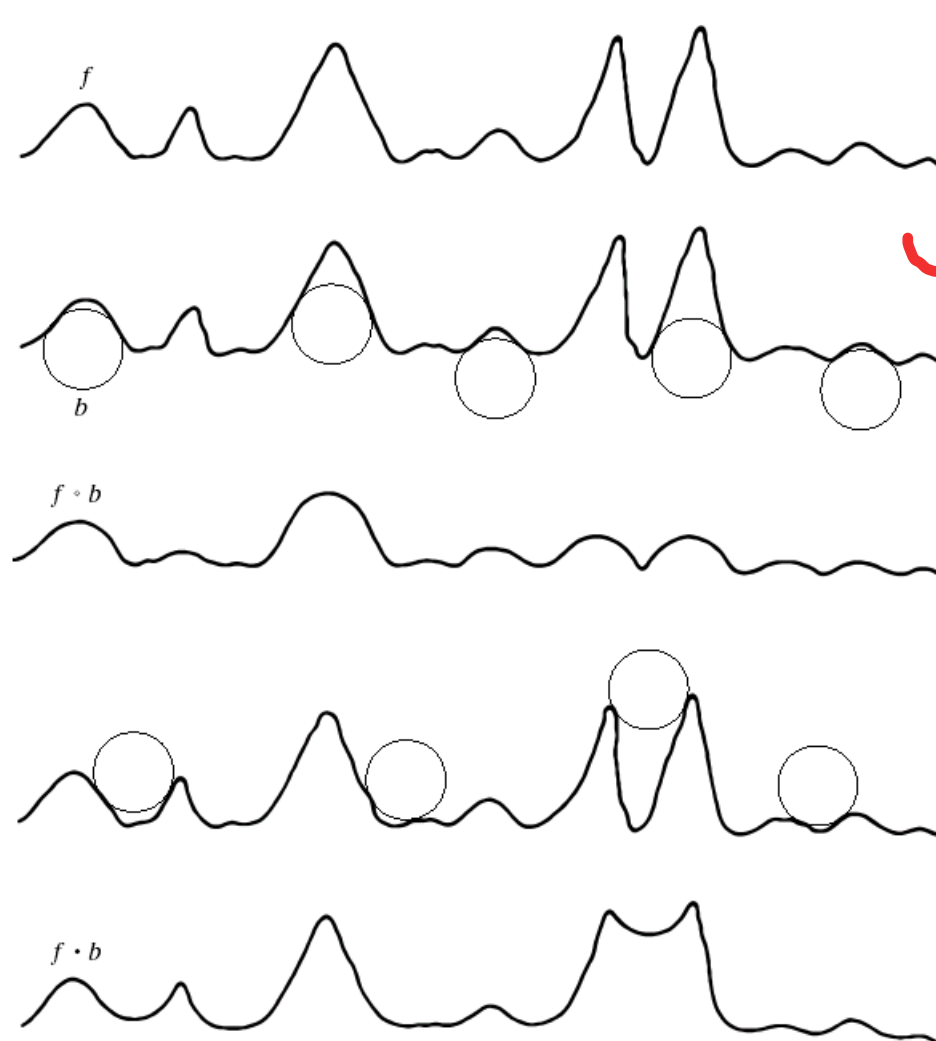




a b  
c

**FIGURE 9.29**  
(a) Original image. (b) Result of dilation.  
(c) Result of erosion.  
(Courtesy of Mr. A. Morris, Leica Cambridge, Ltd.)





a  
b  
c  
d  
e

**FIGURE 9.30**

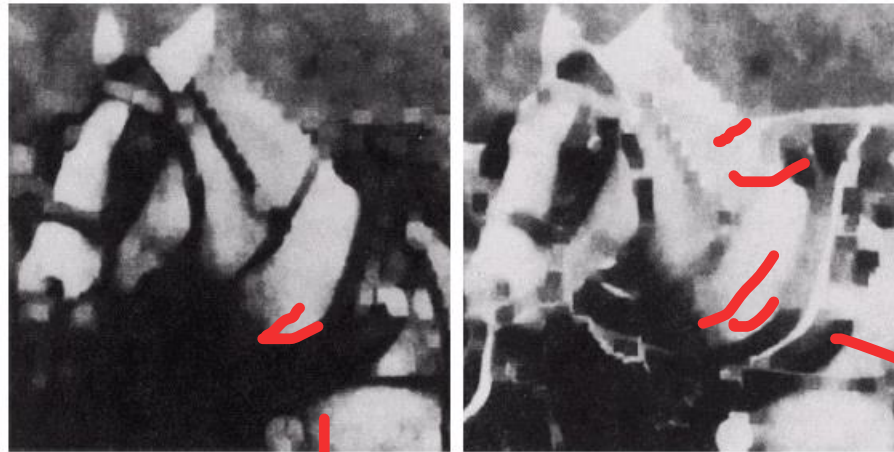
(a) A gray-scale scan line.

(b) Positions of rolling ball for opening.

(c) Result of opening.

(d) Positions of rolling ball for closing.

(e) Result of closing.



**FIGURE 9.31** (a) Opening and (b) closing of Fig. 9.29(a). (Courtesy of Mr. A. Morris, Leica Cambridge, Ltd.)

not so prominent

more prominent

# Morphological Algorithms

Using the simple technique we have looked at so far we can begin to consider some more interesting morphological algorithms

~~We~~ will look at:

- Boundary extraction
- Region filling

There are lots of others as well though:

- Extraction of connected components
- Thinning/thickening
- Skeletonisation

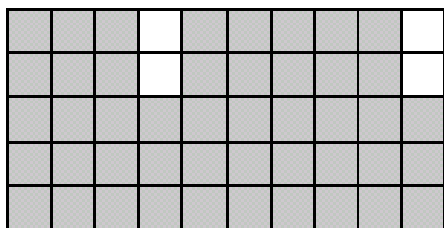
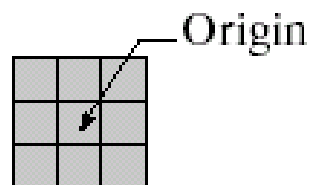
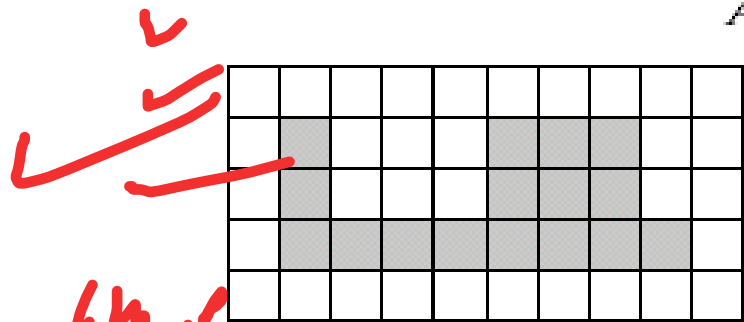
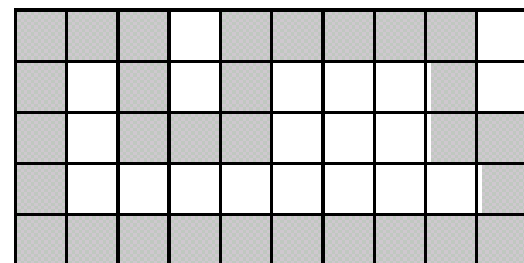
①

# Boundary Extraction

Extracting the boundary (or outline) of an object is often extremely useful

The boundary can be given simply as

$$\beta(A) = A - (A \ominus B)$$

*A**B**A ⊖ B**β(A)*



# Boundary Extraction Example

A simple image and the result of performing  
boundary extraction using a square  $3 \times 3$   
structuring element

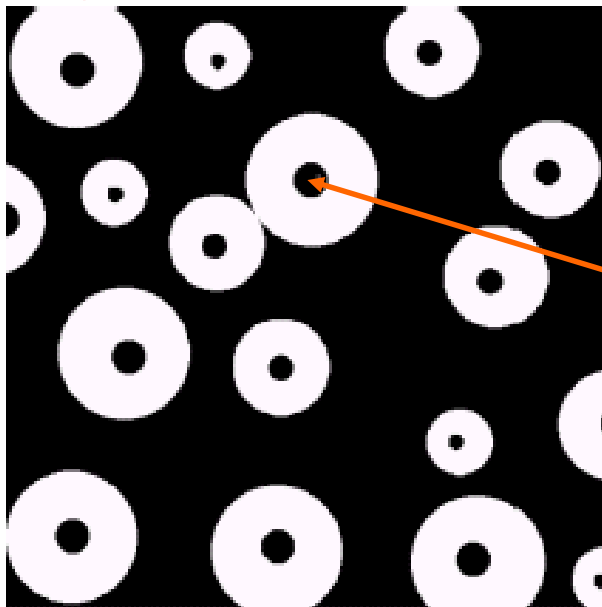


Original Image



Extracted Boundary

Given a pixel inside a boundary, *region filling* attempts to fill that boundary with object pixels (1s)



Given a point inside here, can we fill the whole circle?

The key equation for region filling is

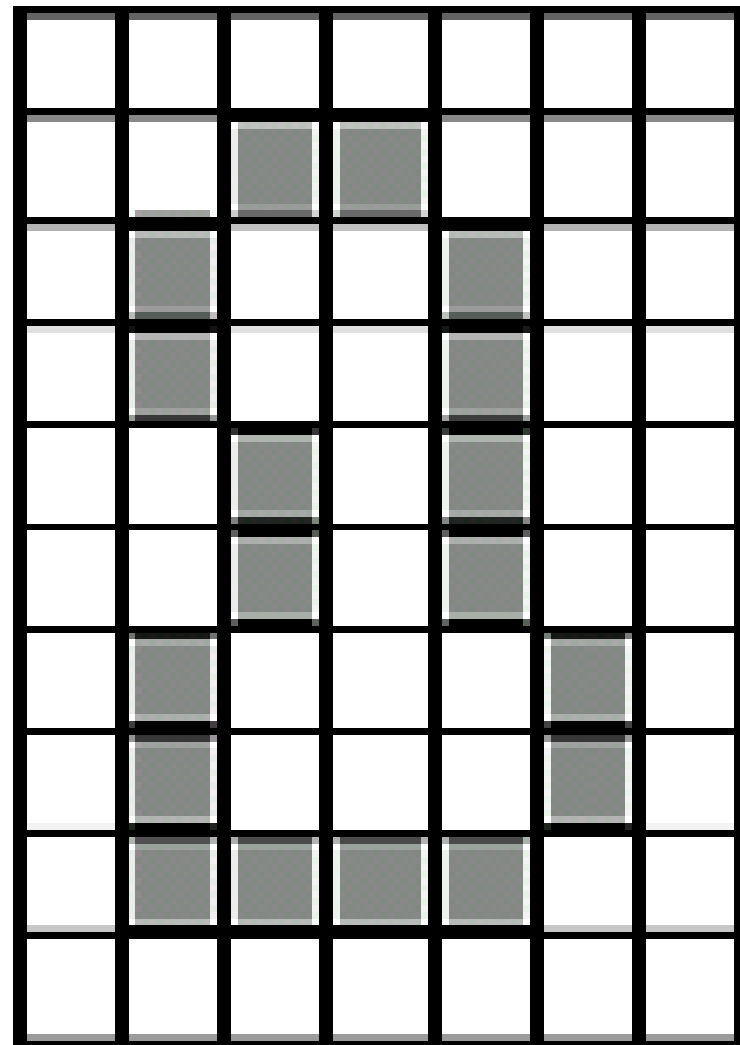
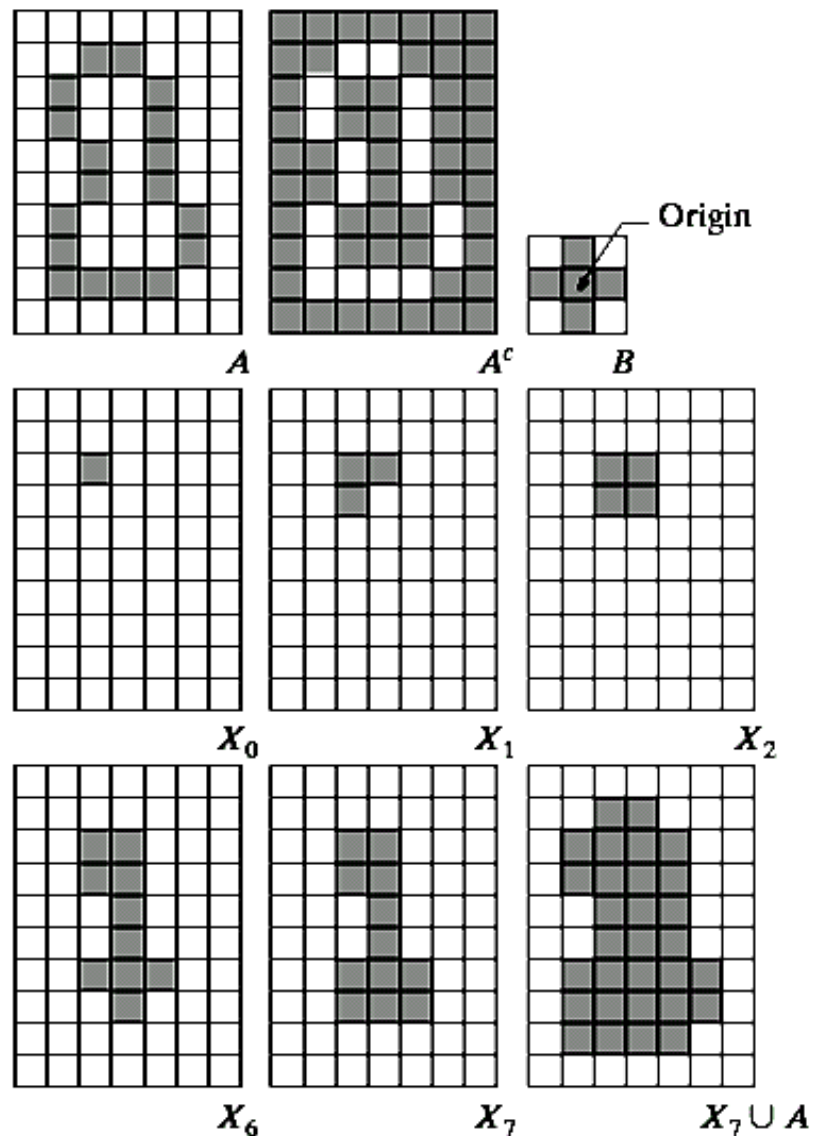
$$X_k = (X_{k-1} \oplus B) \cap A^c \quad k = 1, 2, 3, \dots$$

Where  $X_0$  is simply the starting point inside the boundary,  $B$  is a simple structuring element and  $A^c$  is the complement of  $A$

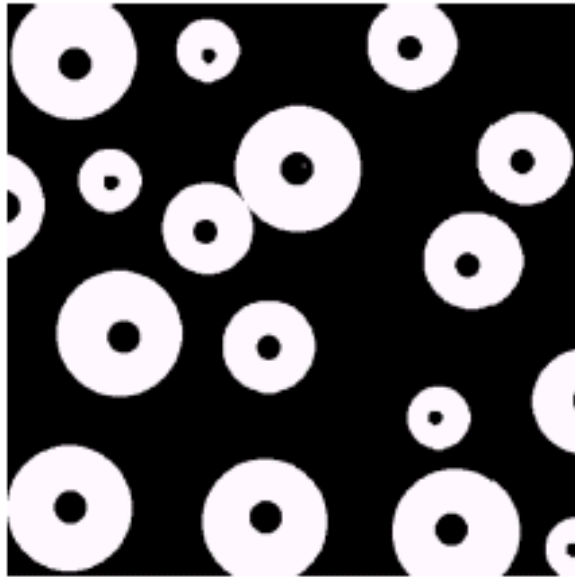
This equation is applied repeatedly until  $X_k$  is equal to  $X_{k-1}$

Finally the result is unioned with the original boundary

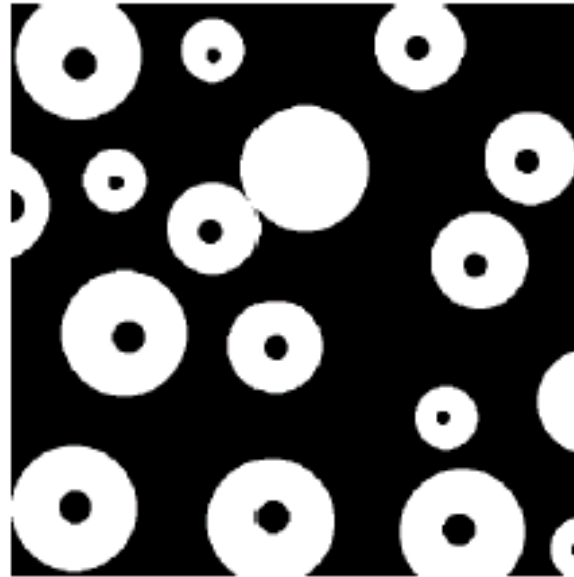
# Region Filling Step By Step



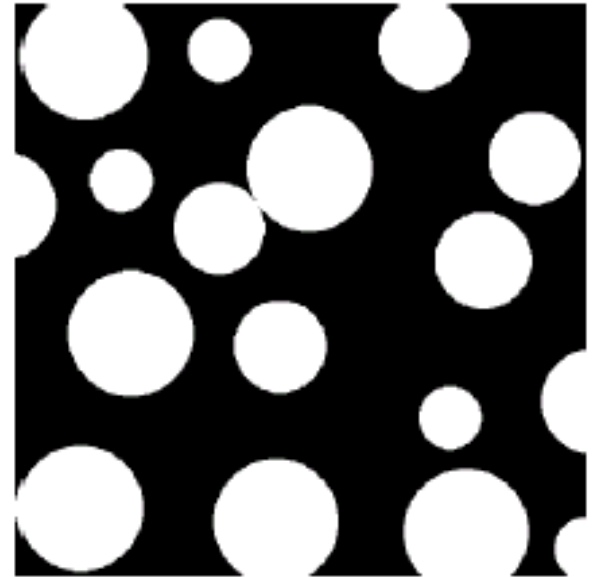
# Region Filling Example



Original Image



One Region  
Filled



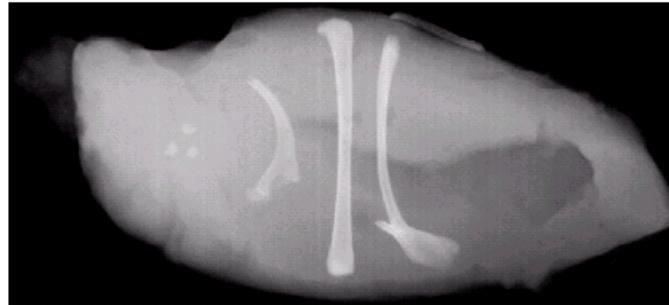
All Regions  
Filled

a  
b  
c d**FIGURE 9.18**

(a) X-ray image of chicken filet with bone fragments.

(b) Thresholded image. (c) Image eroded with a  $5 \times 5$  structuring element of 1's.

(d) Number of pixels in the connected components of (c). (Image courtesy of NTB Elektronische Geraete GmbH, Diepholz, Germany, [www.ntbxbay.com](http://www.ntbxbay.com).)



Connected component	No. of pixels in connected comp
01	11
02	9
03	9
04	39
05	133
06	1
07	1
08	743
09	7
10	11
11	11
12	9
13	9
14	674
15	85

~~The purpose of morphological processing is primarily to remove imperfections added during segmentation~~

~~The basic operations are *erosion* and *dilation*~~

~~Using the basic operations we can perform *opening* and *closing*~~

~~More advanced morphological operation can then be implemented using combinations of all of these~~

# Region Filling Step By Step

