





Image Enhancement (Histogram Processing)



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Over the next few lectures we will look at image enhancement techniques working in the spatial domain:

- What is image enhancement?
- Different kinds of image enhancement
- Histogram processing
- Point processing
- Neighbourhood operations

A Note About Grey Levels

So far when we have spoken about image grey level values we have said they are in the range $[0, 255]$

- Where 0 is black and 255 is white

There is no reason why we have to use this range

- The range $[0, 255]$ stems from display technologies

For many of the image processing operations in this lecture grey levels are assumed to be given in the range $[0.0, 1.0]$

What Is Image Enhancement?

Image enhancement is the process of making images more useful

The reasons for doing this include:

- Highlighting interesting detail in images
- Removing noise from images
- Making images more visually appealing

Image Enhancement Examples



Image Enhancement Examples (cont...)

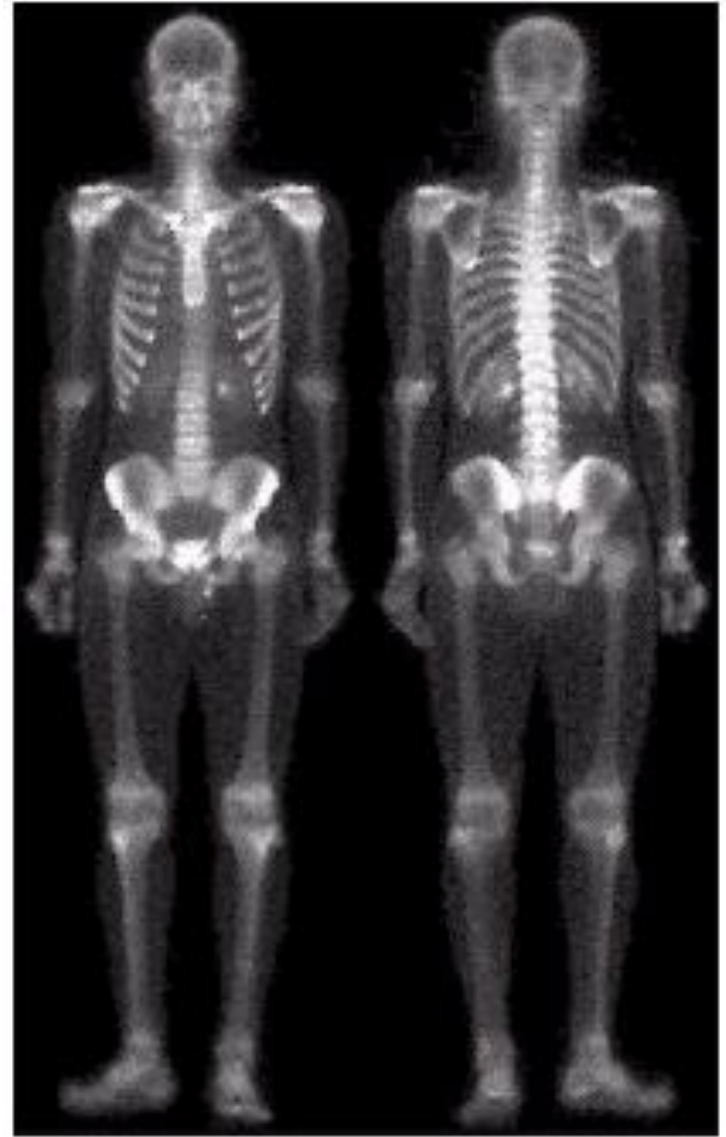
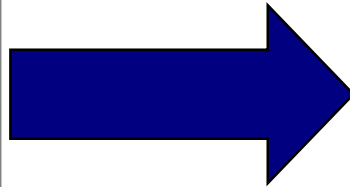
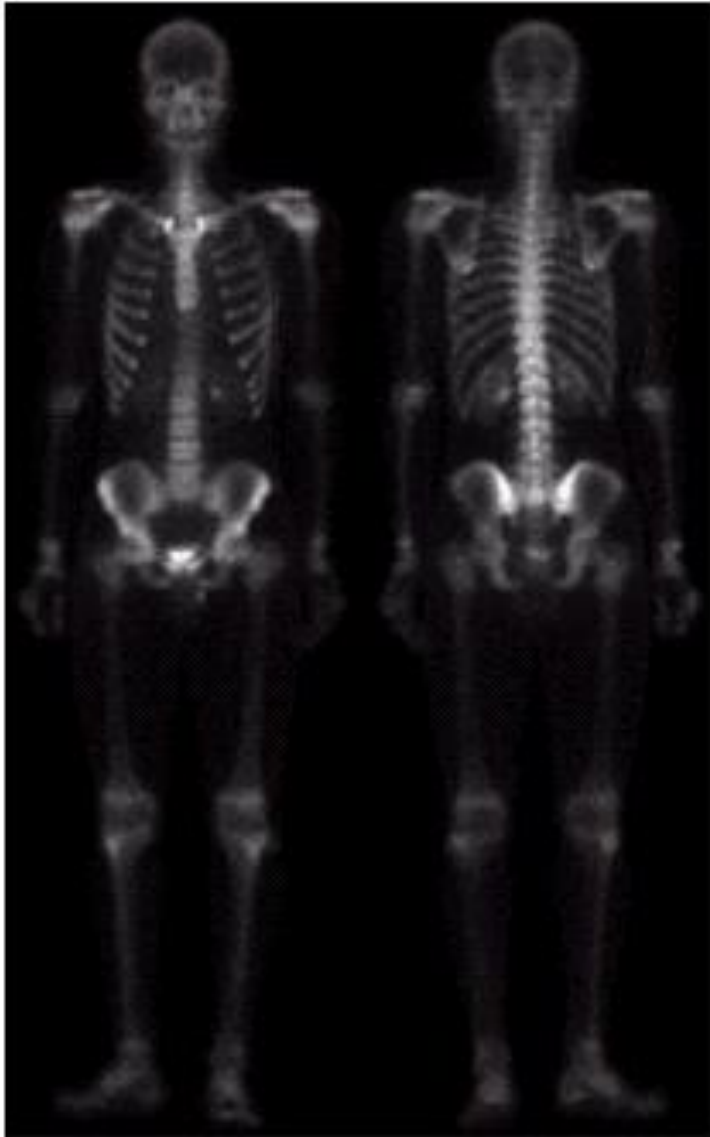


Image Enhancement Examples (cont...)

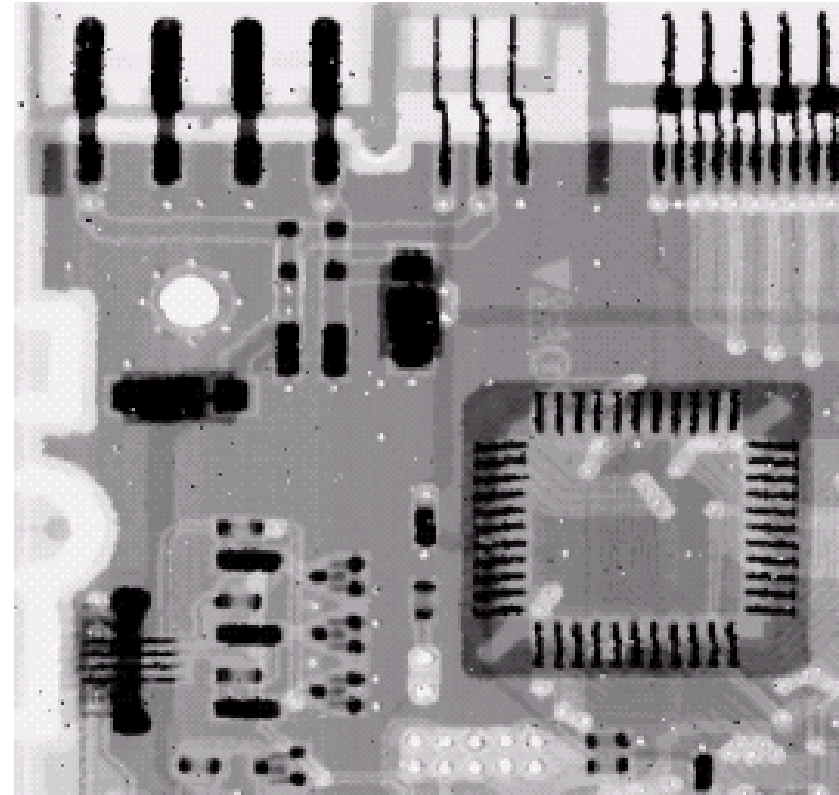
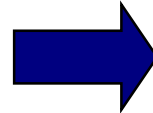
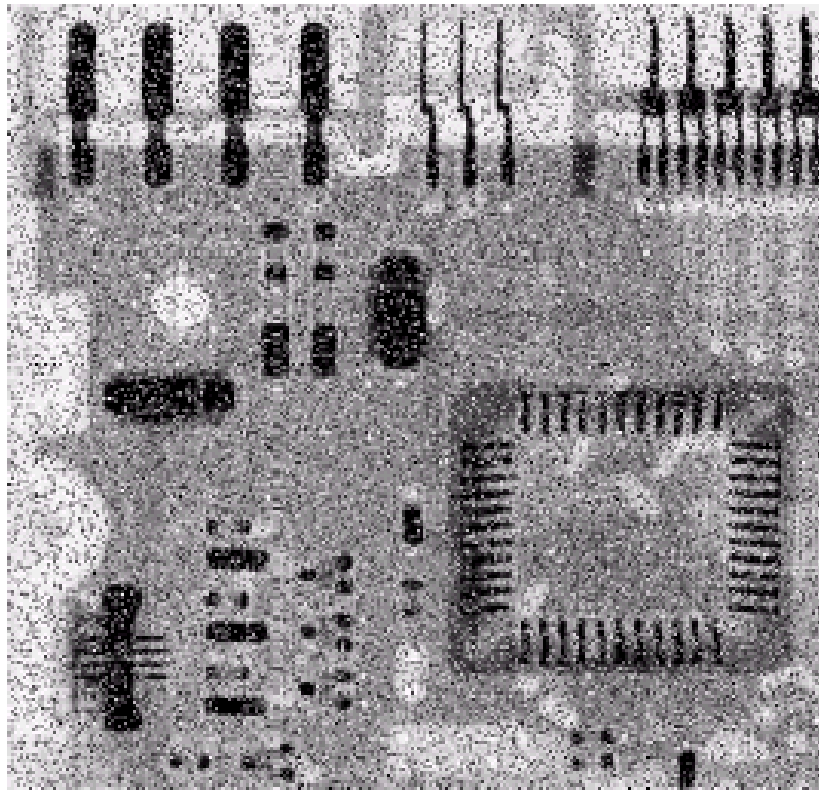


Image Enhancement Examples (cont...)



Spatial & Frequency Domains

There are two broad categories of image enhancement techniques

– Spatial domain techniques

- Direct manipulation of image pixels

– Frequency domain techniques

- Manipulation of Fourier transform or wavelet transform of an image

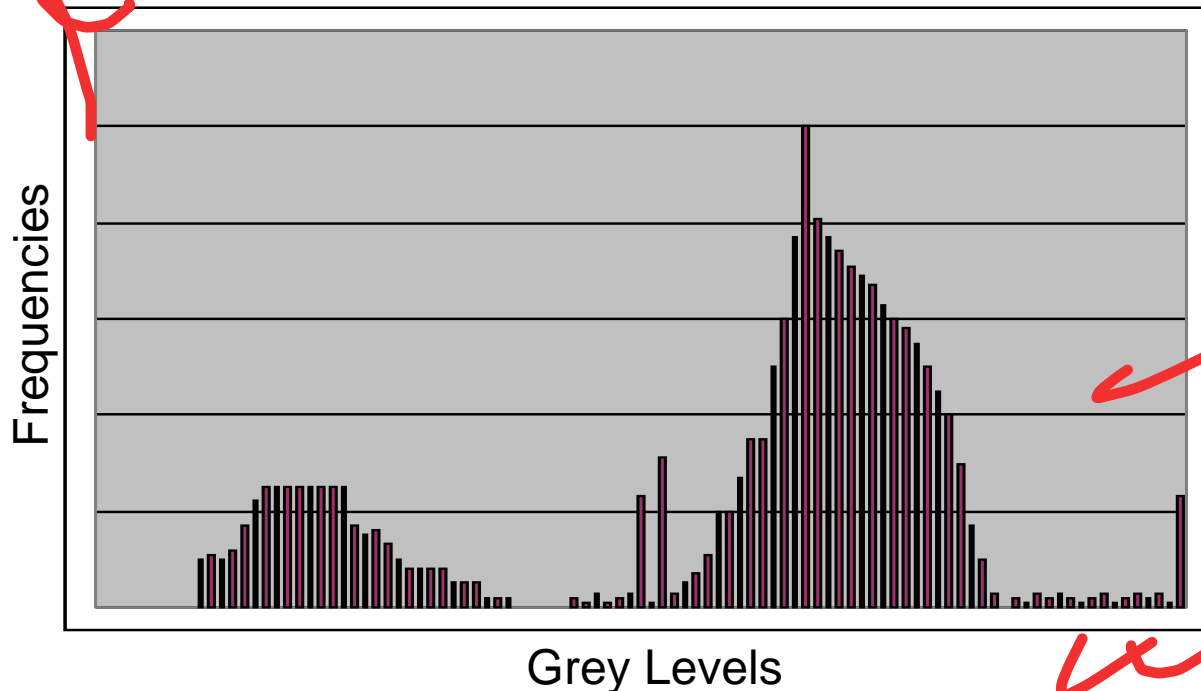
For the moment we will concentrate on techniques that operate in the spatial domain

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Image Histograms

The histogram of an image shows us the distribution of grey levels in the image

Massively useful in image processing,
especially in segmentation

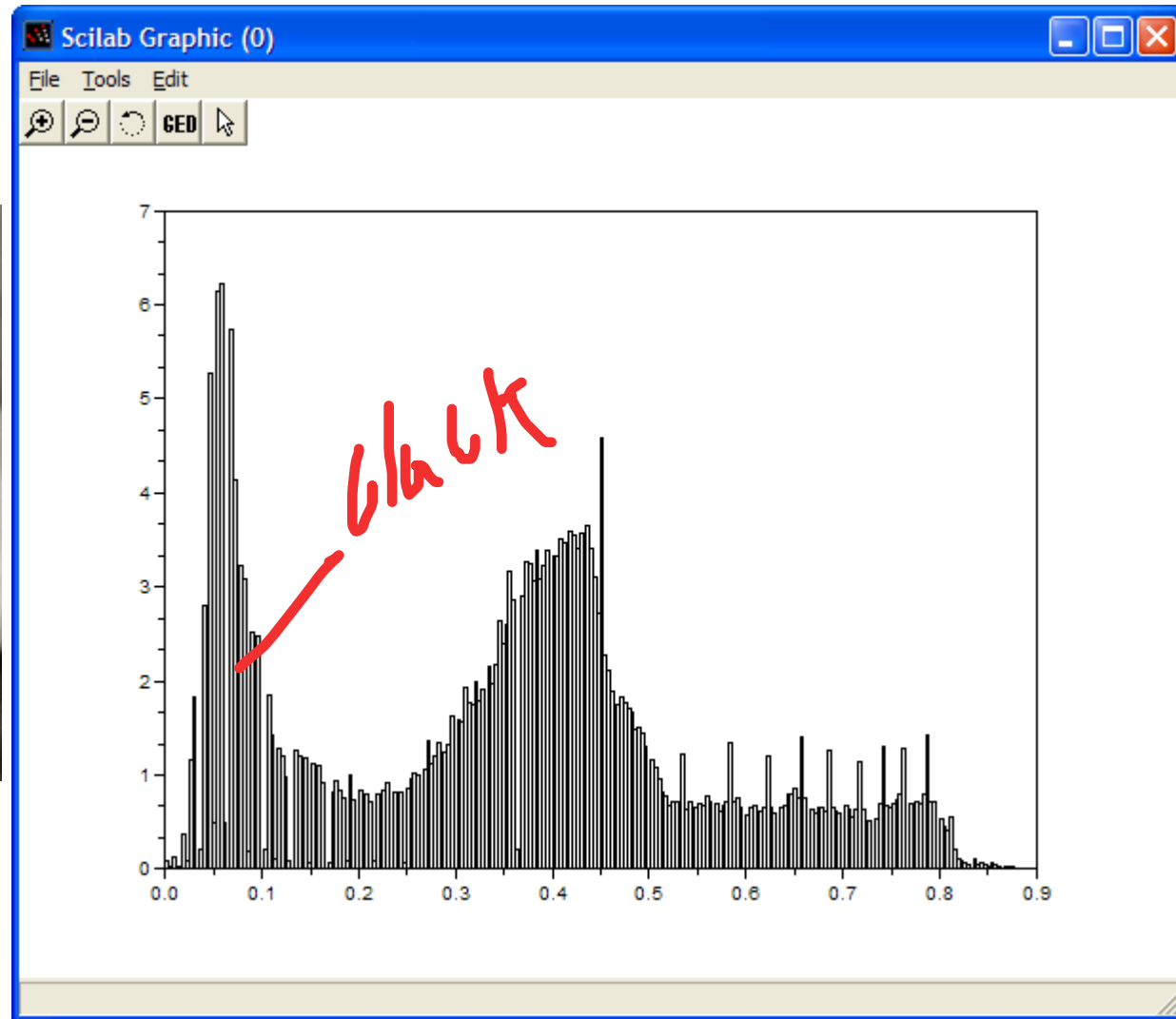


Histogram Examples

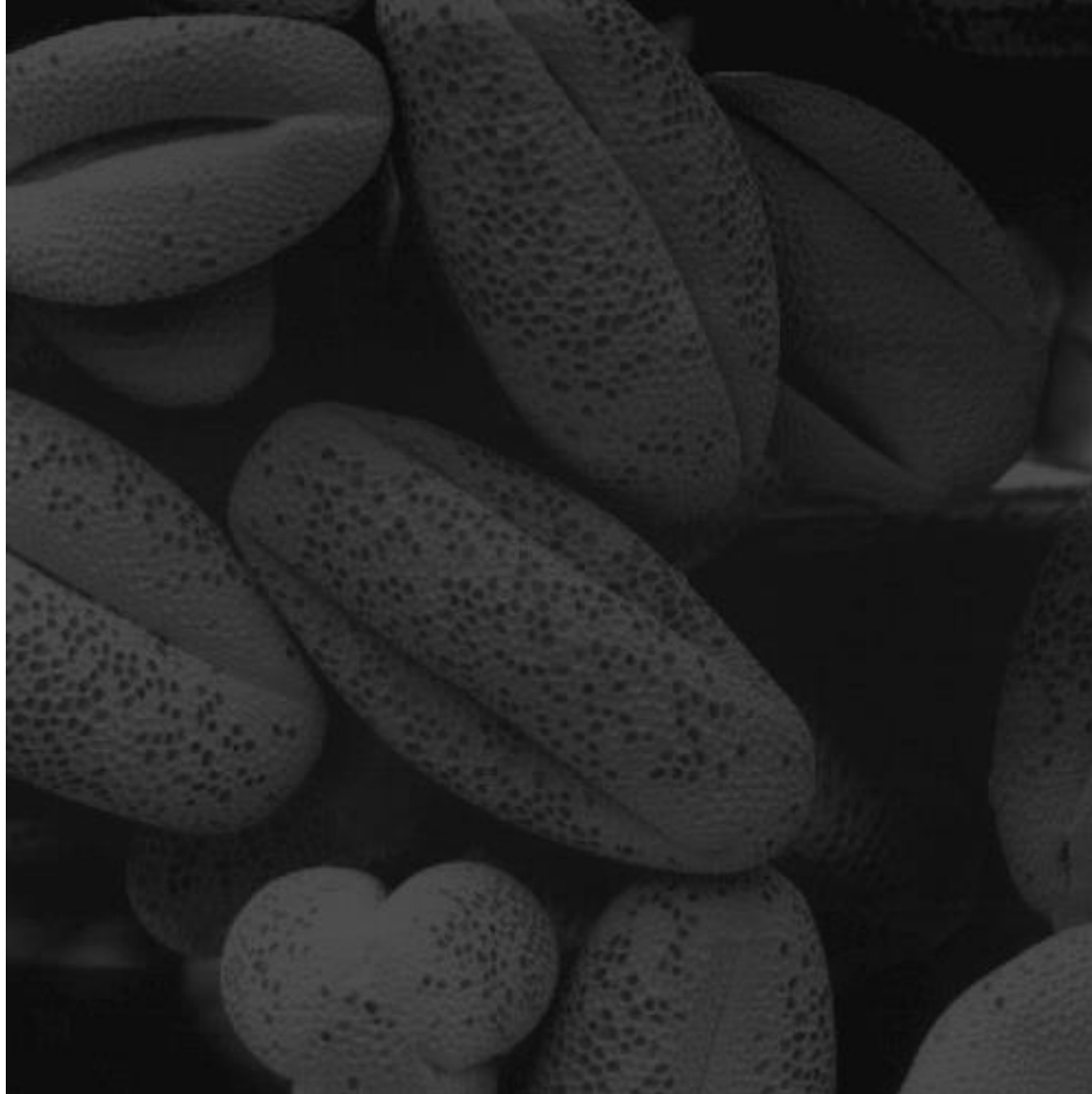


Histogram Examples (cont...)

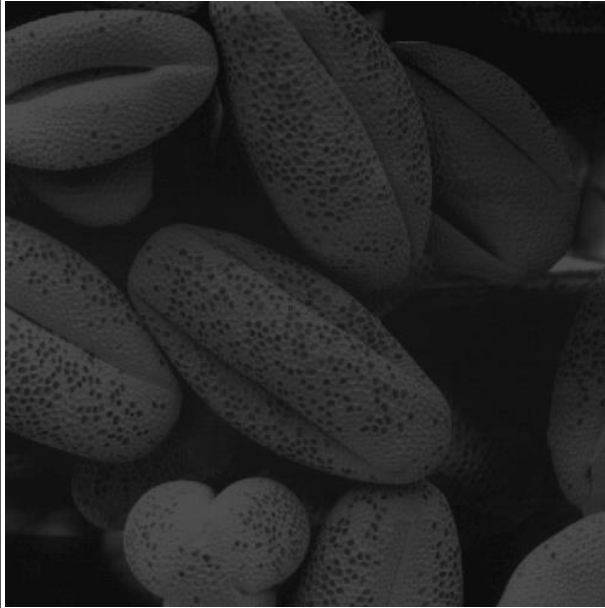
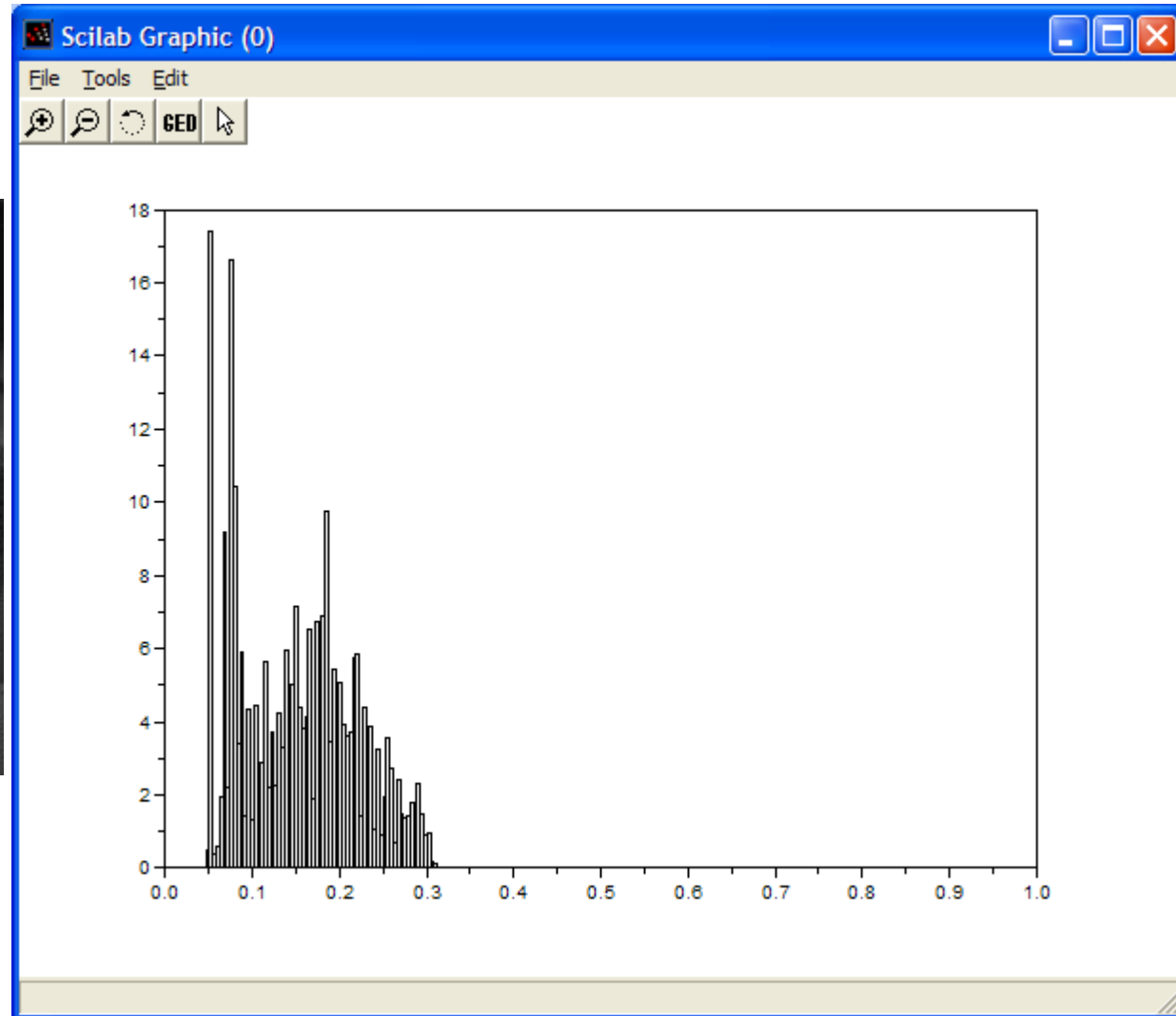
L



Histogram Examples (cont...)



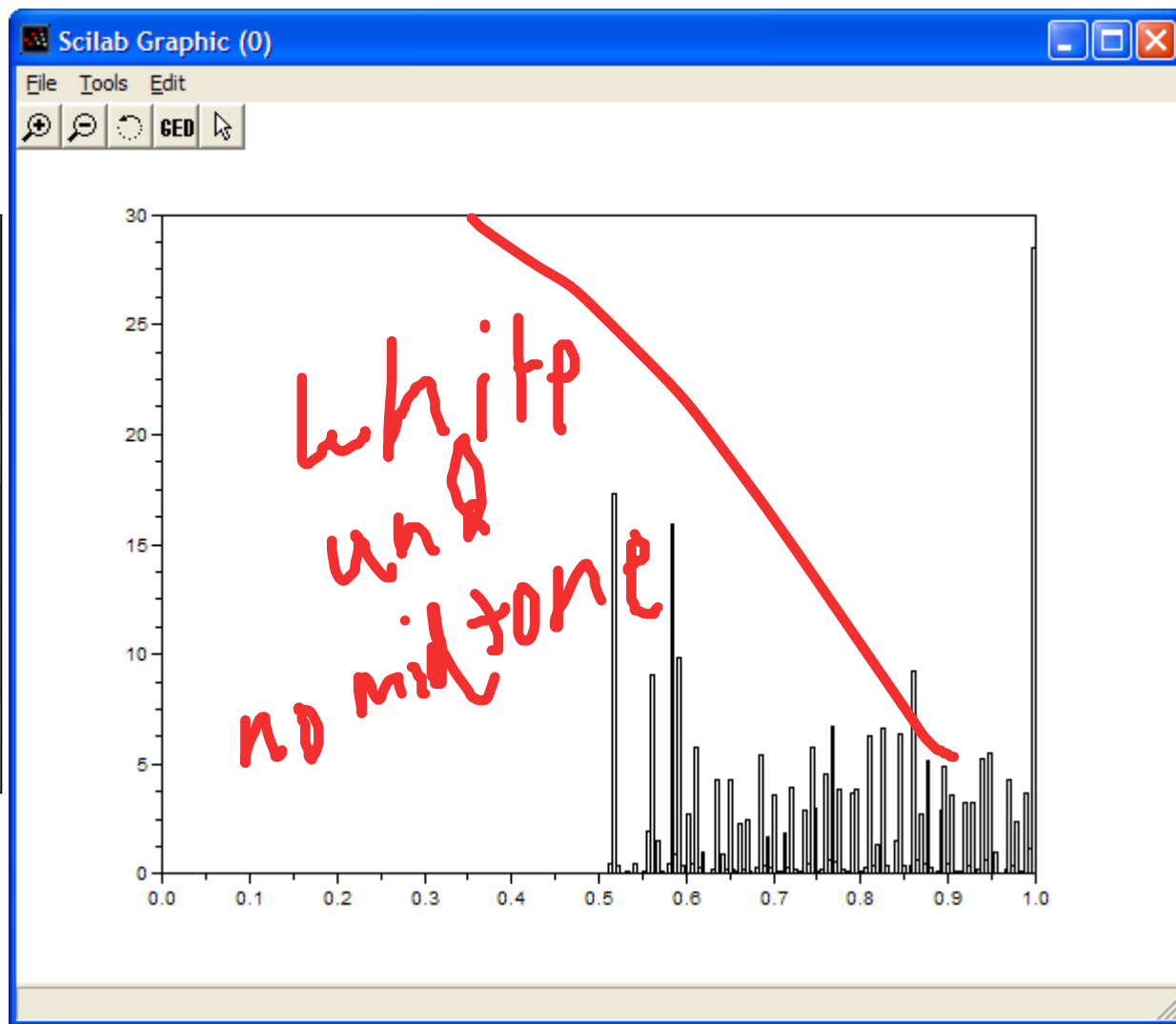
Histogram Examples (cont...)



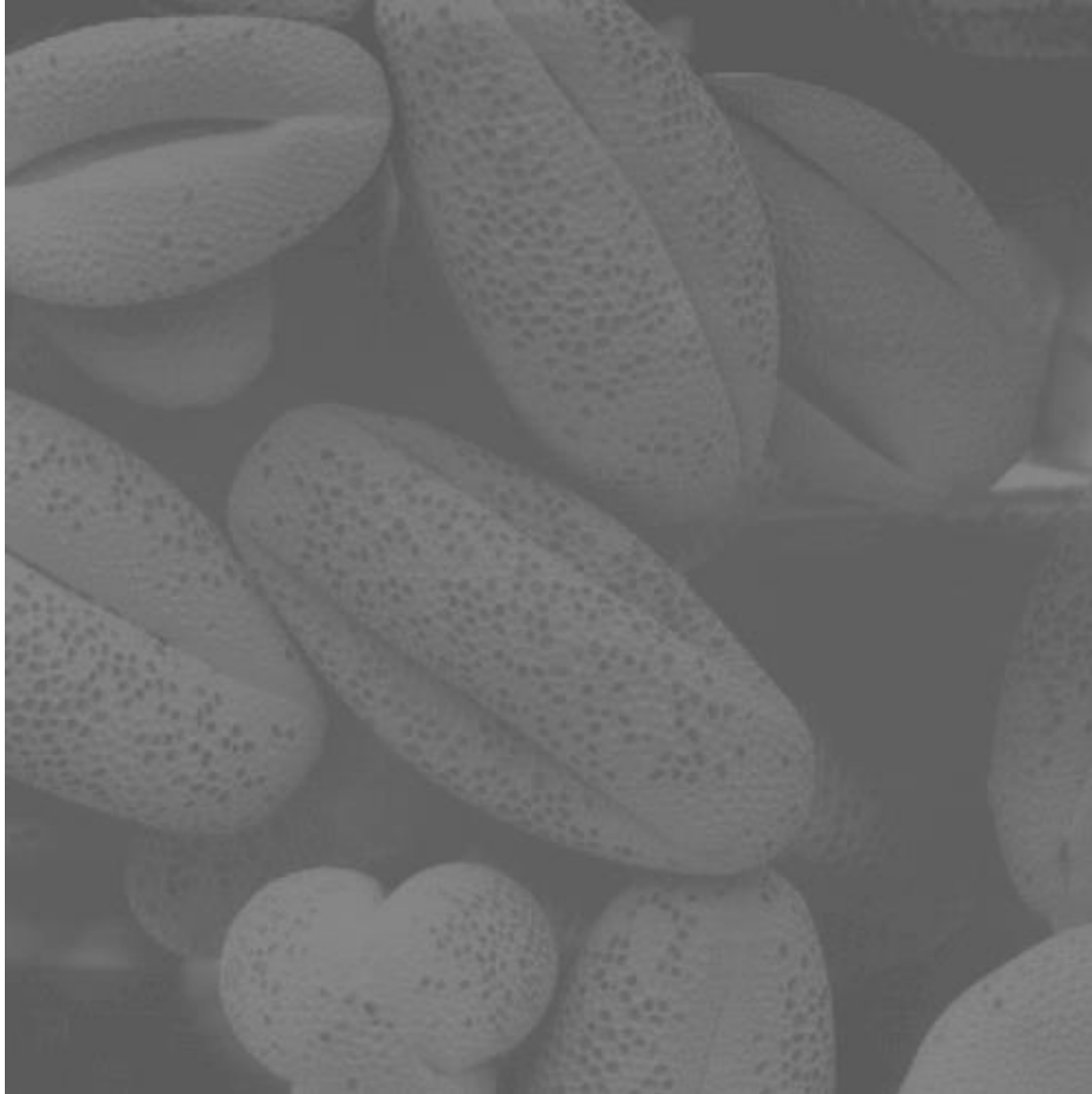
Histogram Examples (cont...)



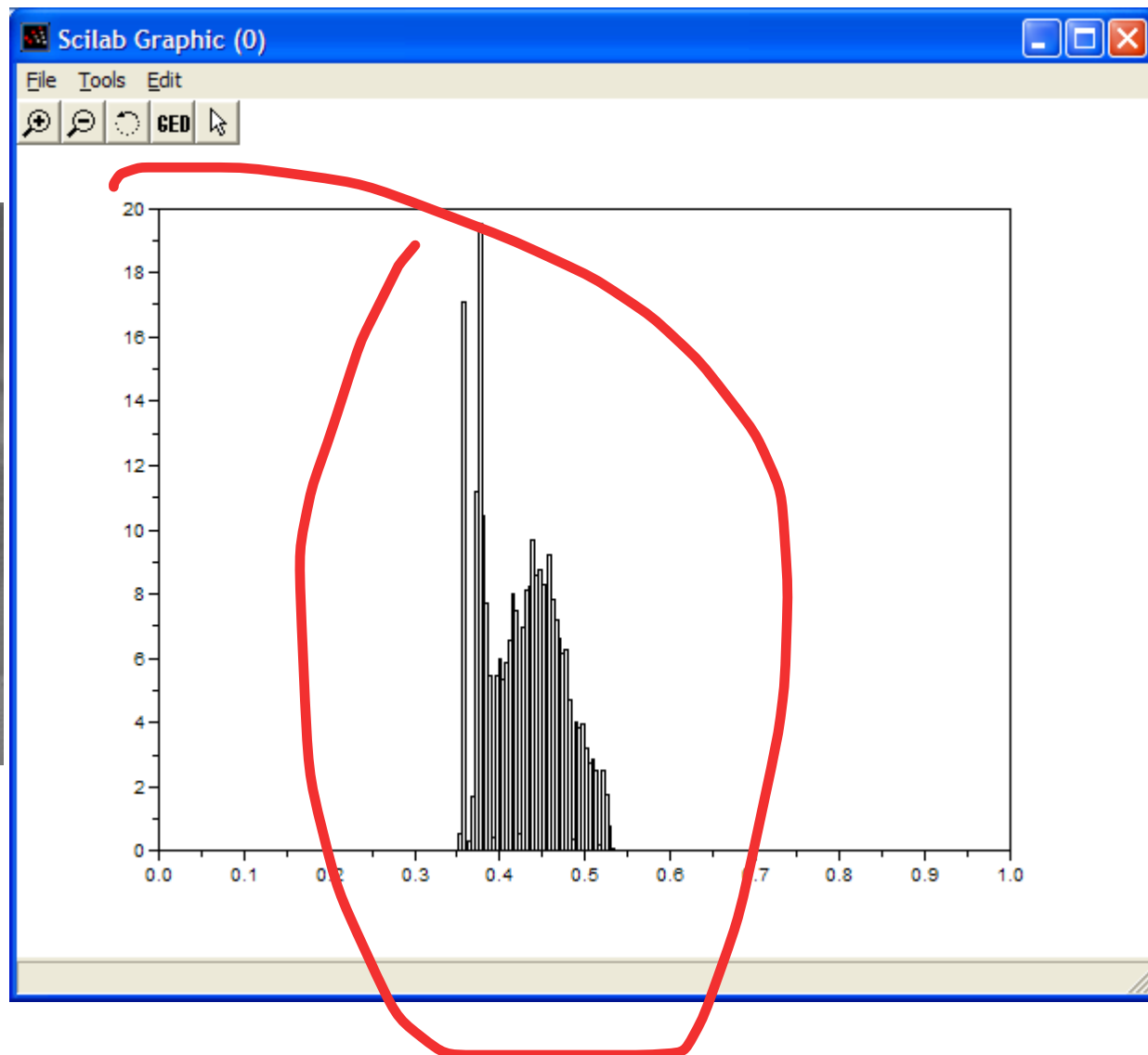
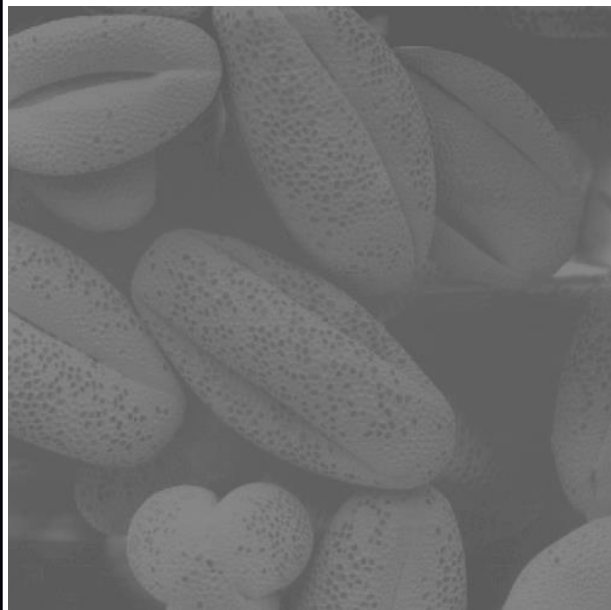
Histogram Examples (cont...)



Histogram Examples (cont...)



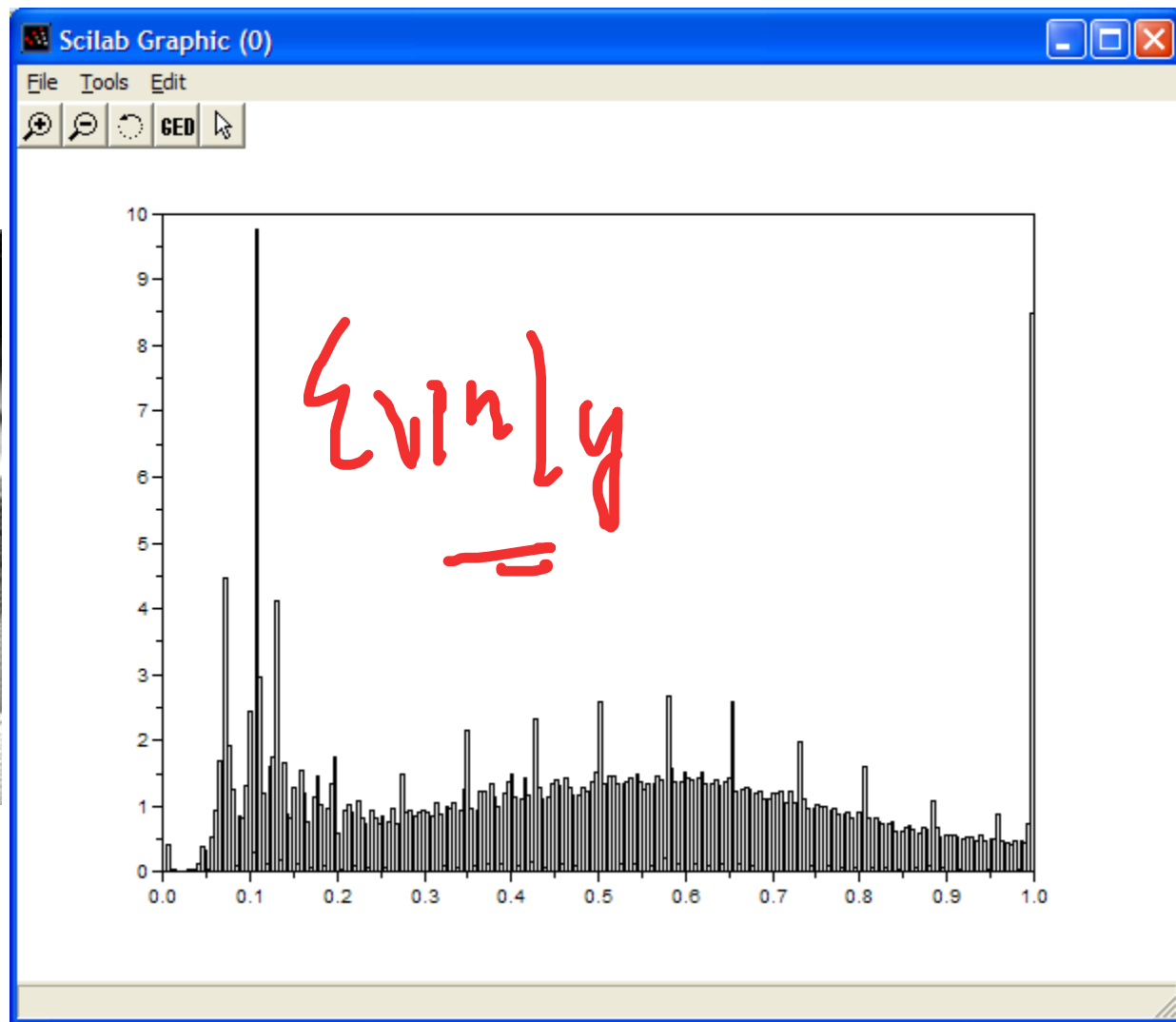
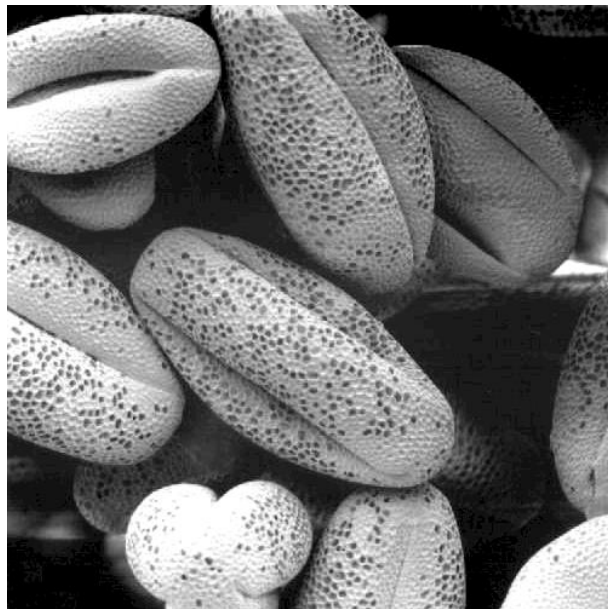
Histogram Examples (cont...)



Histogram Examples (cont...)



Histogram Examples (cont...)

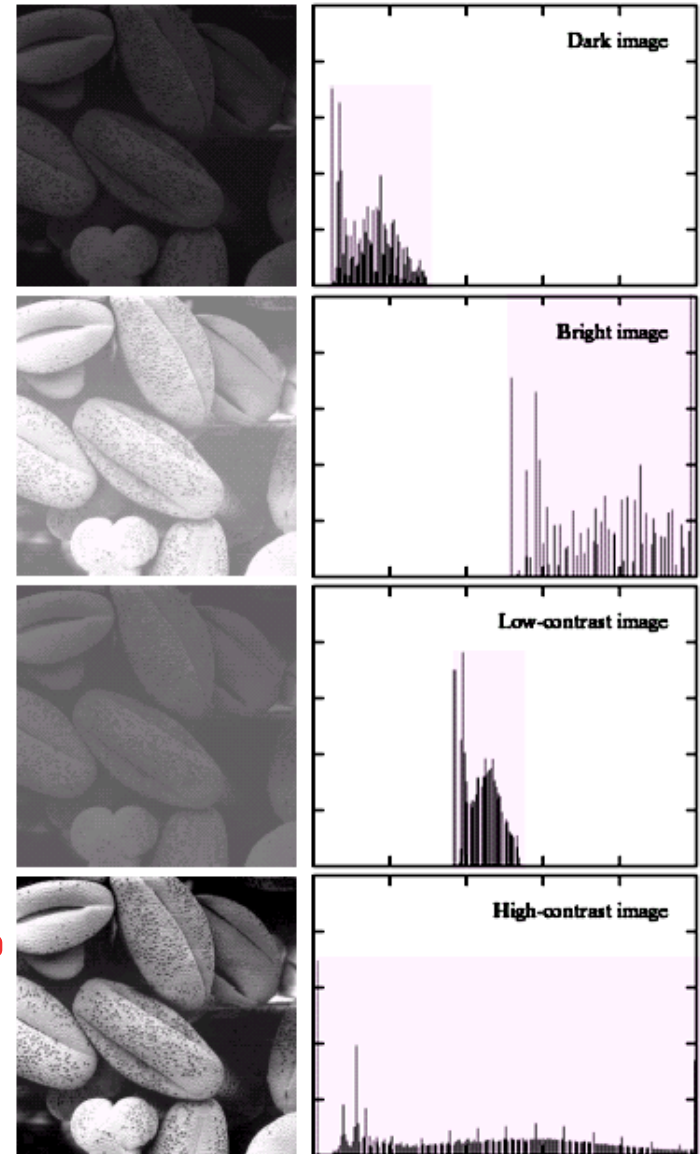


Histogram Examples (cont...)

A selection of images and
their histograms

Notice the relationships
between the images and
their histograms

Note that the high contrast
image has the most
evenly spaced histogram



Contrast Stretching

We can fix images that have poor contrast
by applying a pretty simple contrast
specification

The interesting part is how do we decide on
this transformation function?





Histogram Equalisation

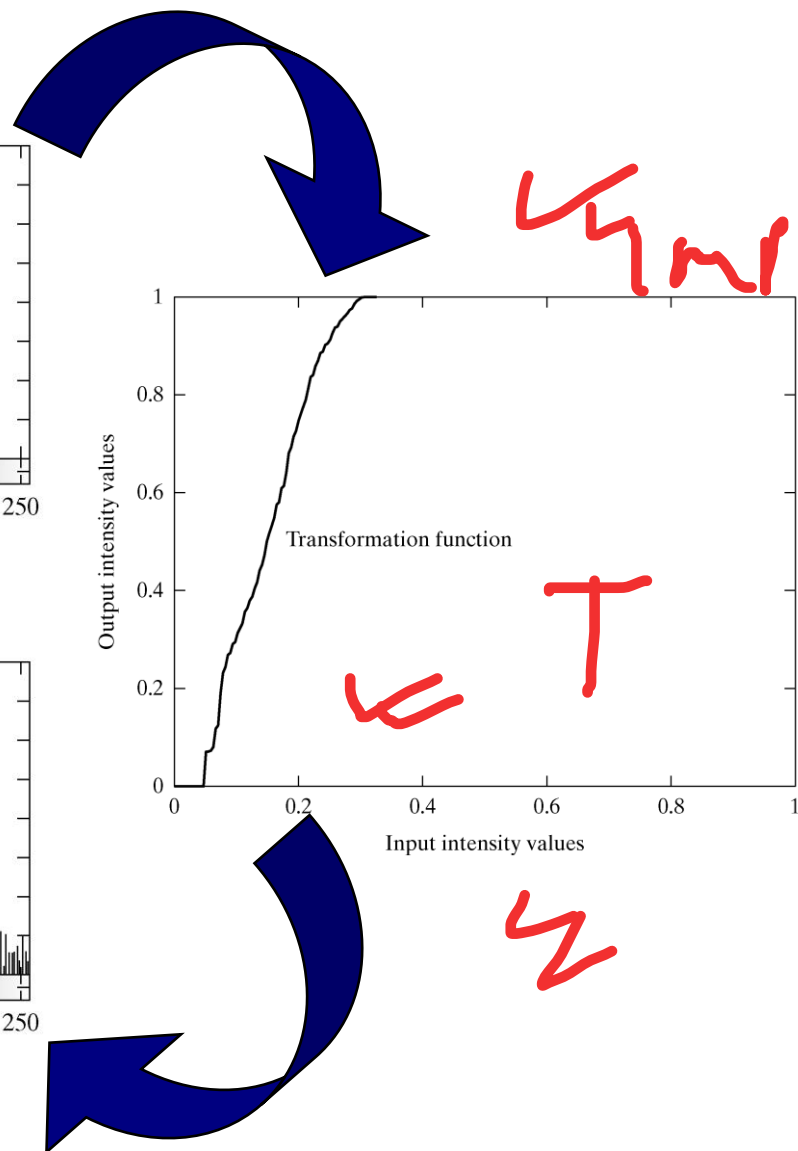
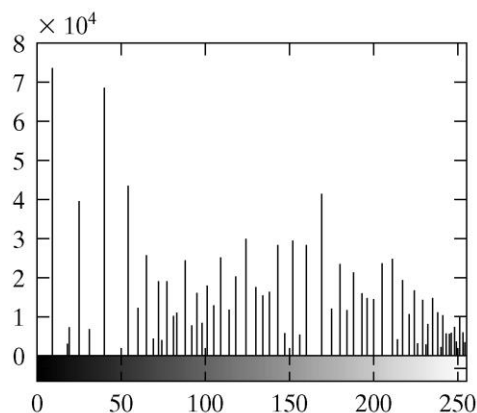
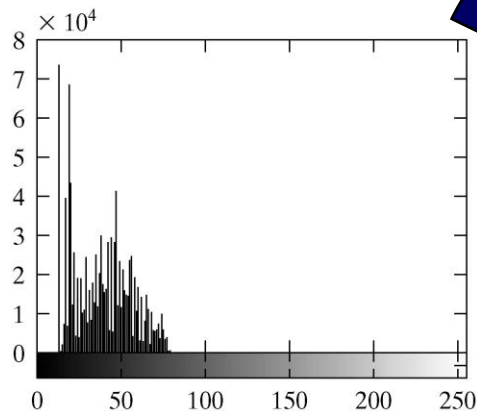
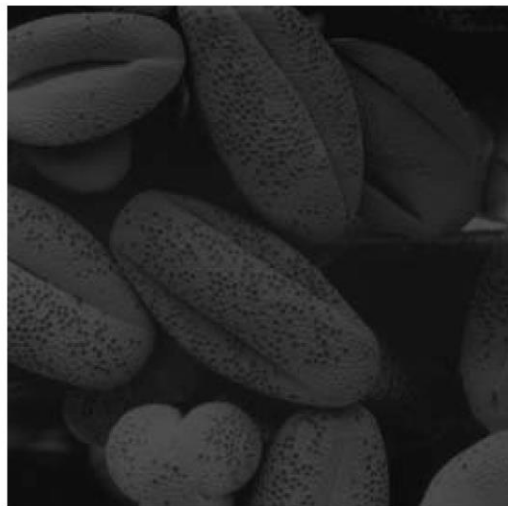
Spreading out the frequencies in an image (or equalising the image) is a simple way to improve dark or washed out images

The formula for histogram equalisation is given where

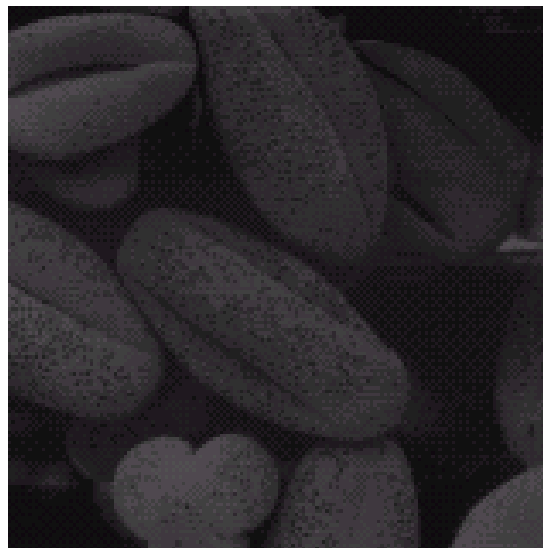
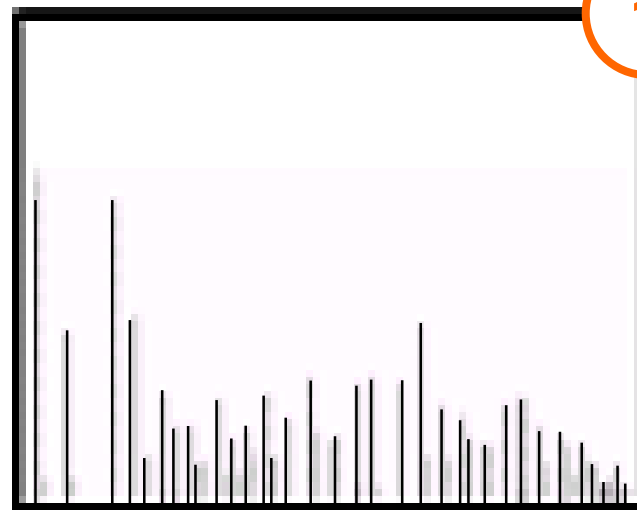
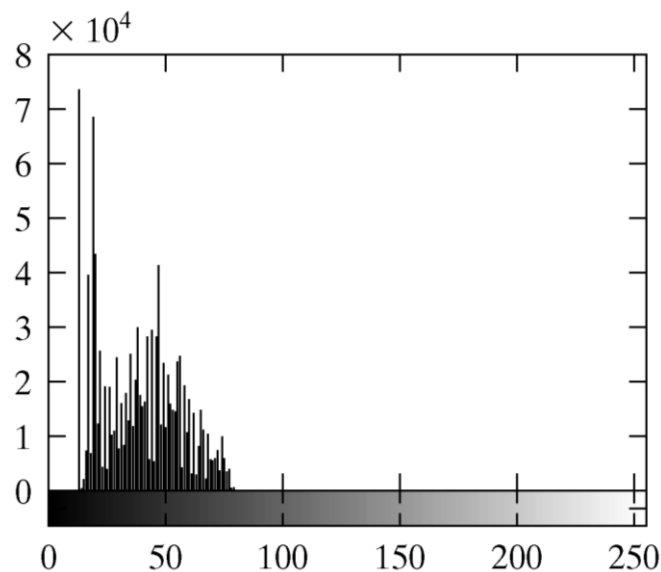
- r_k : input intensity
- s_k : processed intensity
- k : the intensity range (e.g 0.0 – 1.0)
- n_j : the frequency of intensity j
- n : the sum of all frequencies

$$\begin{aligned} s_k &= T(r_k) \\ &= \sum_{j=1}^k p_r(r_j) \\ &= \sum_{j=1}^k \frac{n_j}{n} \end{aligned}$$

Equalisation Transformation Function

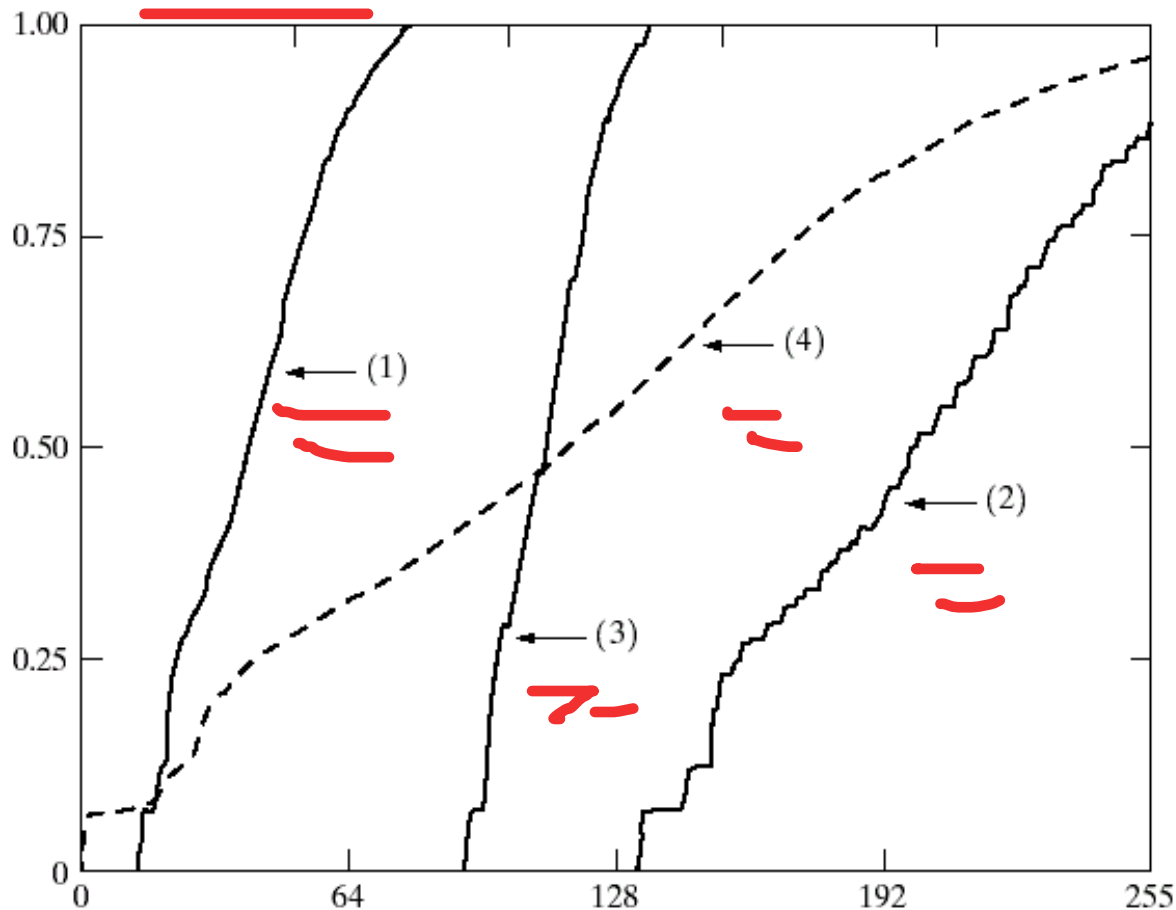


Equalisation Examples

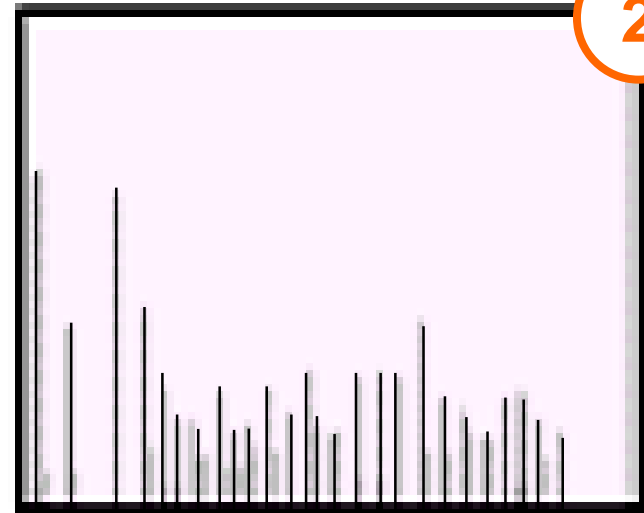
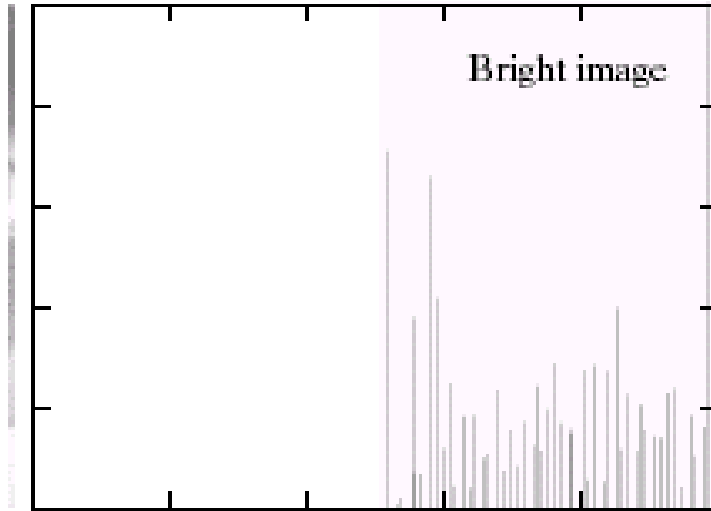


Equalisation Transformation Functions

The functions used to equalise the images in the previous example



Equalisation Examples

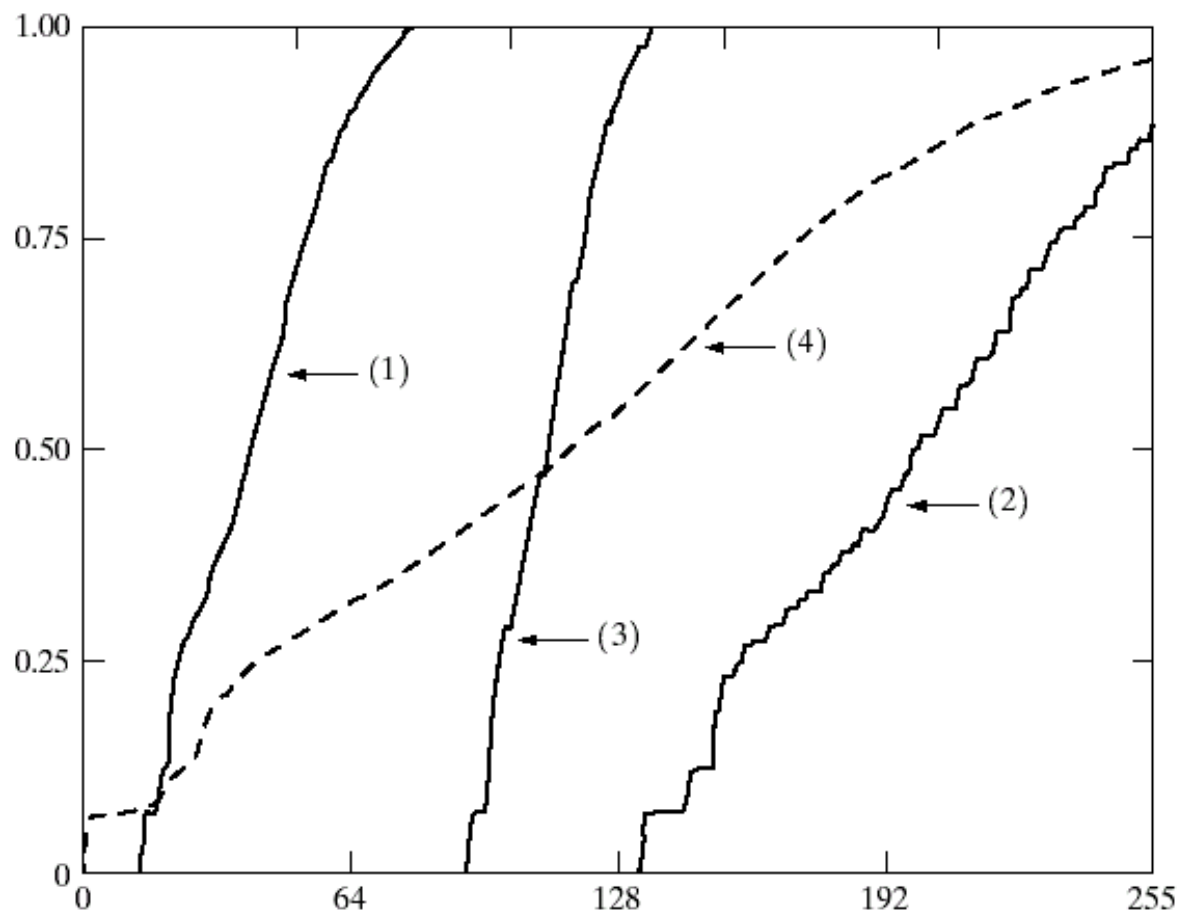


2

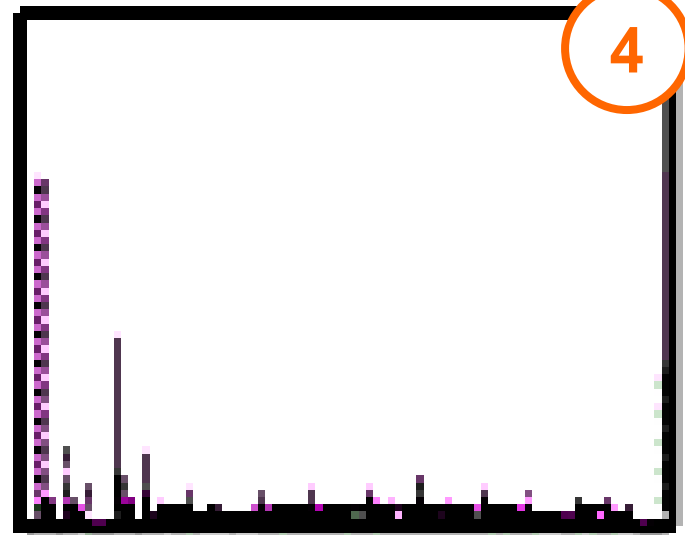
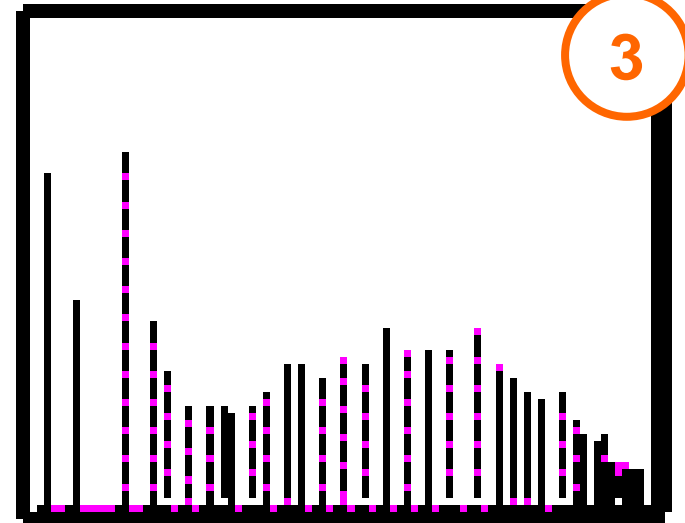
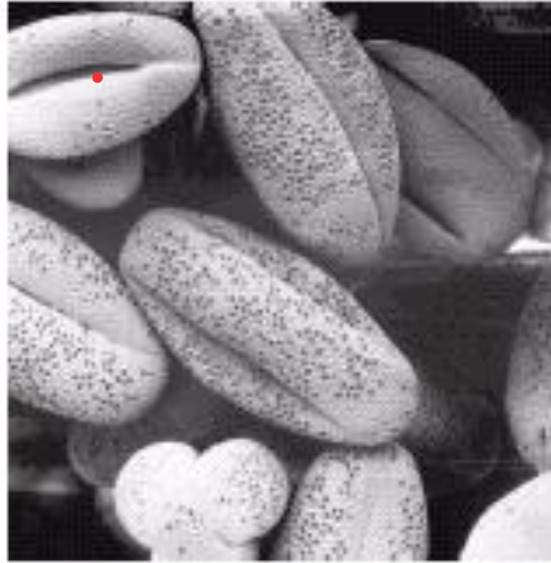
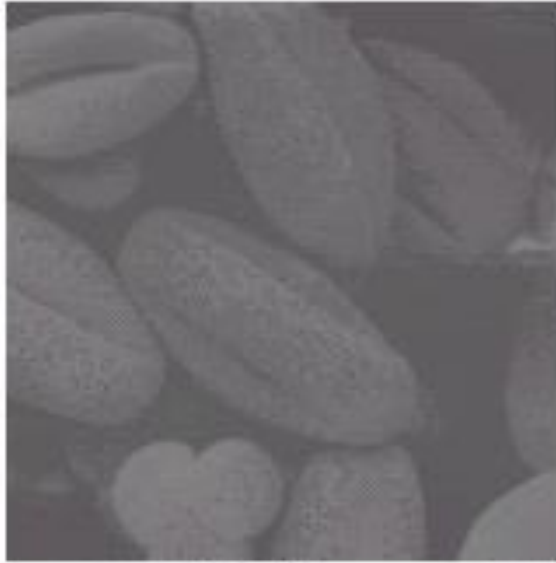


Equalisation Transformation Functions

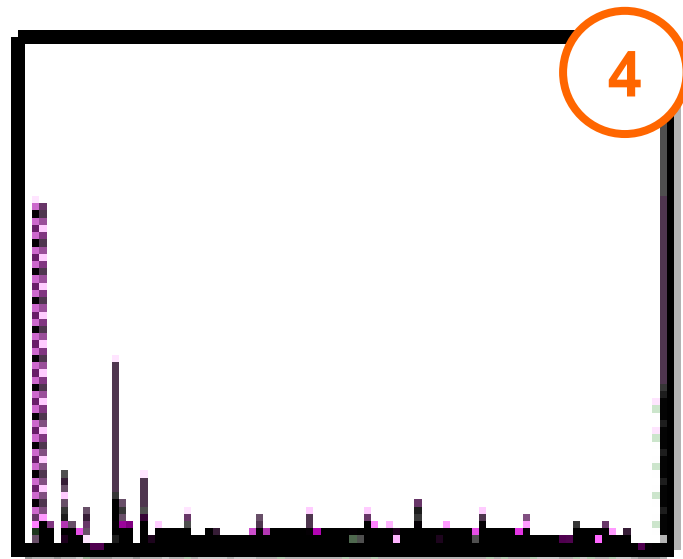
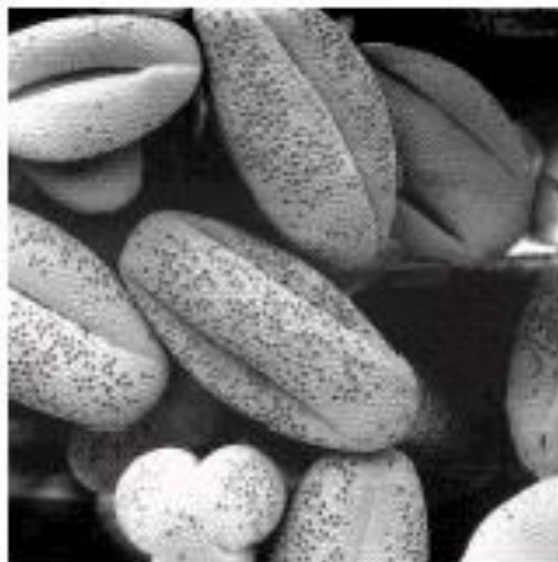
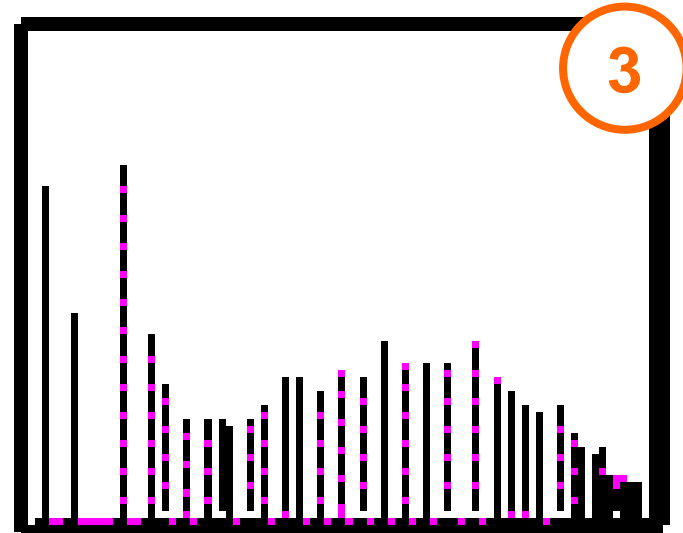
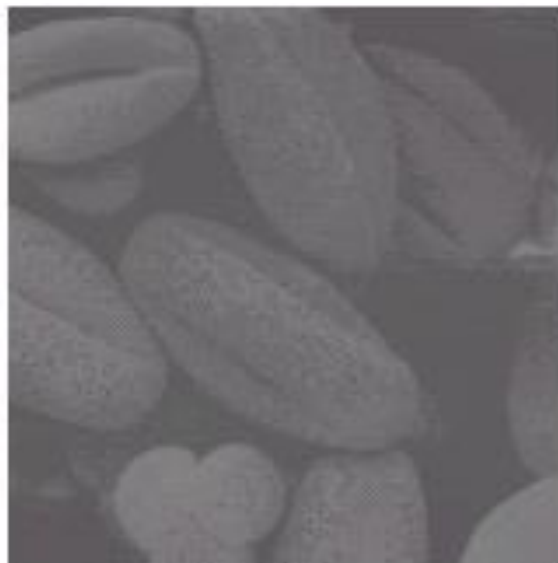
The functions used to equalise the images in the previous example



Equalisation Examples (cont...)

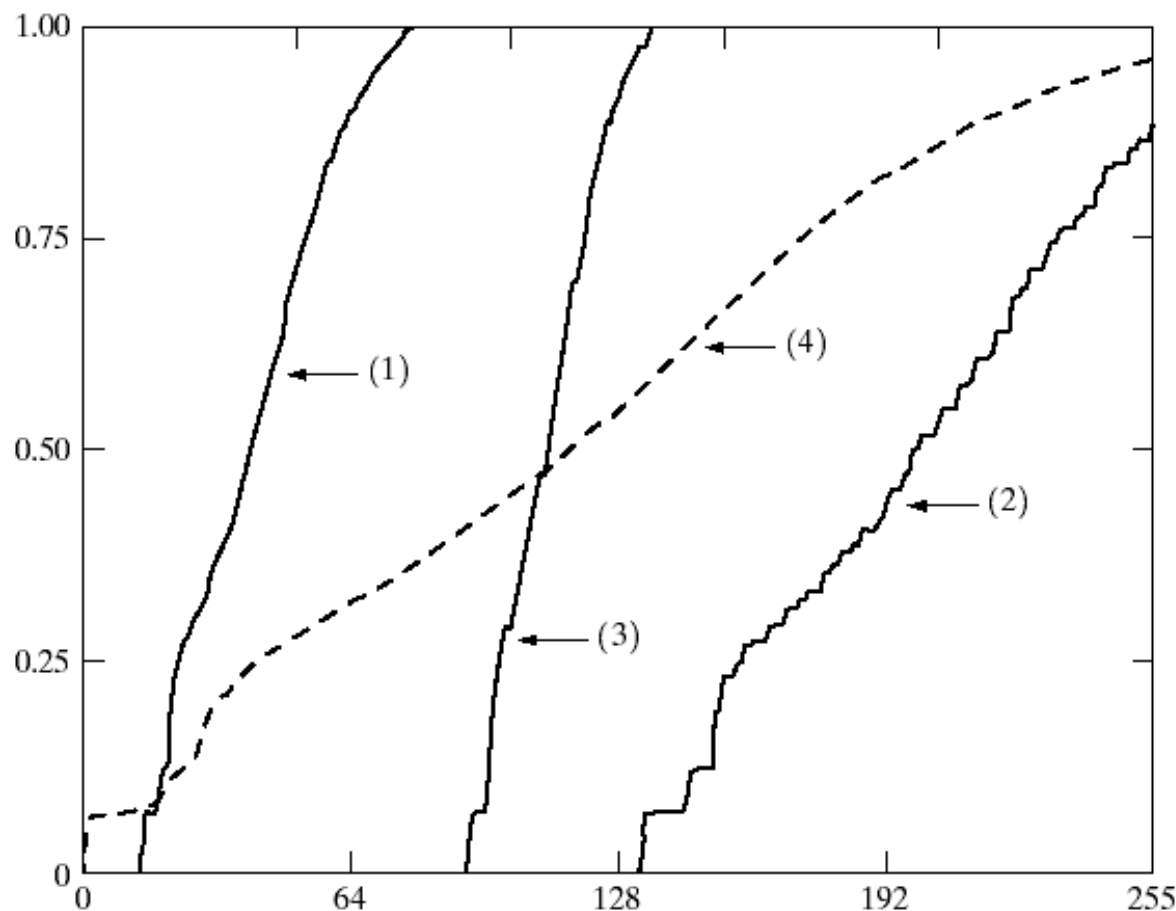


Equalisation Examples (cont...)



Equalisation Transformation Functions

The functions used to equalise the images in the previous examples



We have looked at:

- Different kinds of image enhancement
- Histograms
- Histogram equalisation

Next time we will start to look at point processing and some neighbourhood operations

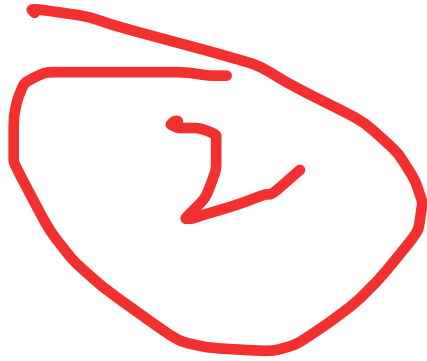


Image Enhancement (Point Processing)



• In this lecture we will look at image enhancement point processing techniques:

- What is point processing?
- Negative images
- Thresholding
- Logarithmic transformation
- Power law transforms
- Grey level slicing
- Bit plane slicing

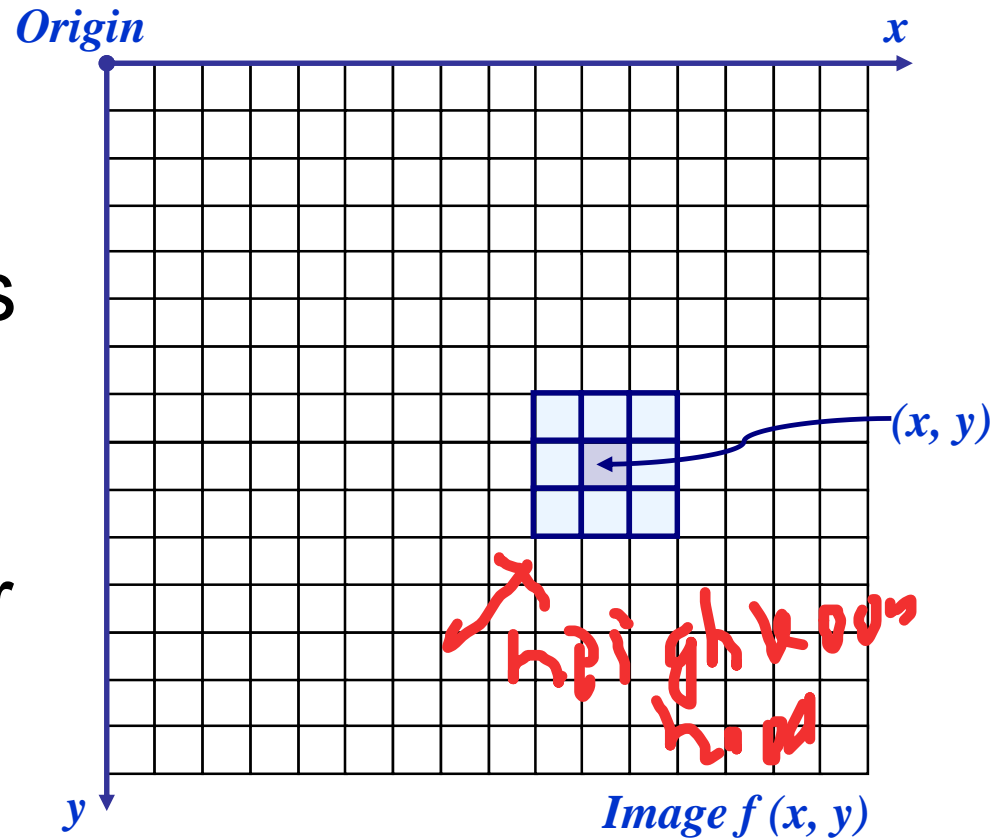
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Basic Spatial Domain Image Enhancement

- Most spatial domain enhancement operations can be reduced to the form

- $g(x, y) = T[f(x, y)]$

- where $f(x, y)$ is the input image, $g(x, y)$ is the processed image and T is some operator defined over some neighbourhood of (x, y)



- The simplest spatial domain operations occur when the neighbourhood is simply the pixel itself

- In this case T is referred to as a *grey level transformation function* or a *point processing operation*

- Point processing operations take the form

$$s = T(r)$$

- where s refers to the processed image pixel value and r refers to the original image pixel value

Point Processing Example: Negative Images

- Negative images are useful for enhancing white or grey detail embedded in dark regions of an image

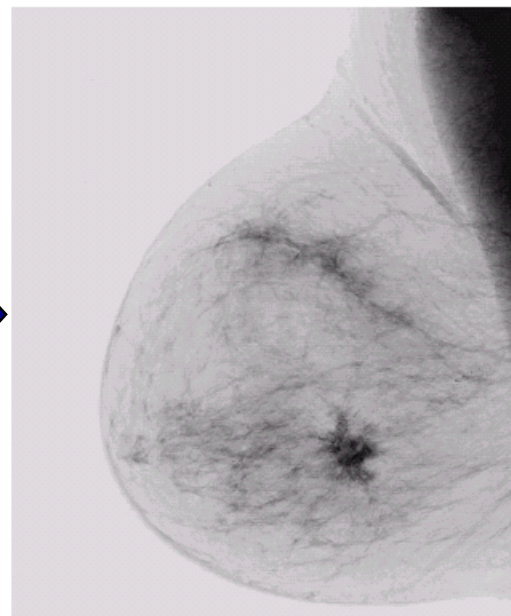
- Note how much clearer the tissue is in the negative image of the mammogram below

Original
Image

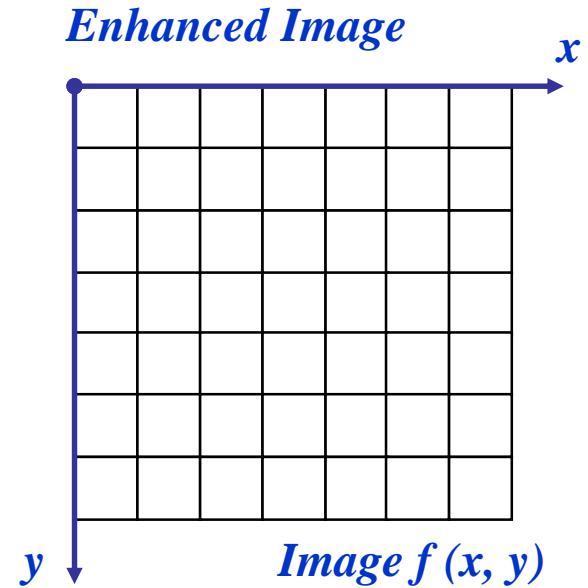
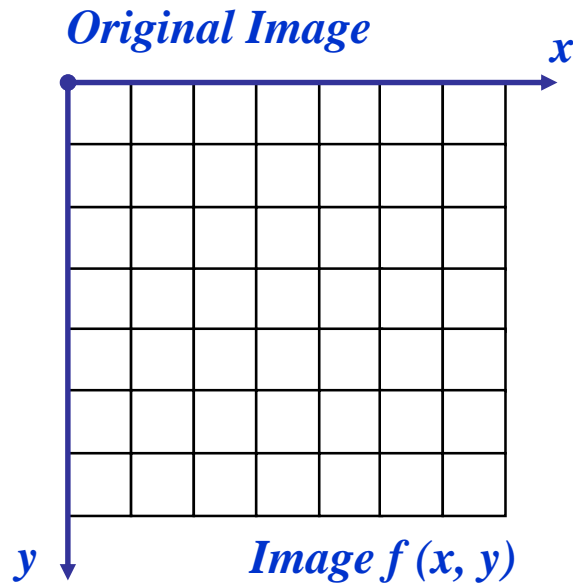


$$s = 1.0 - r$$

Negative
Image



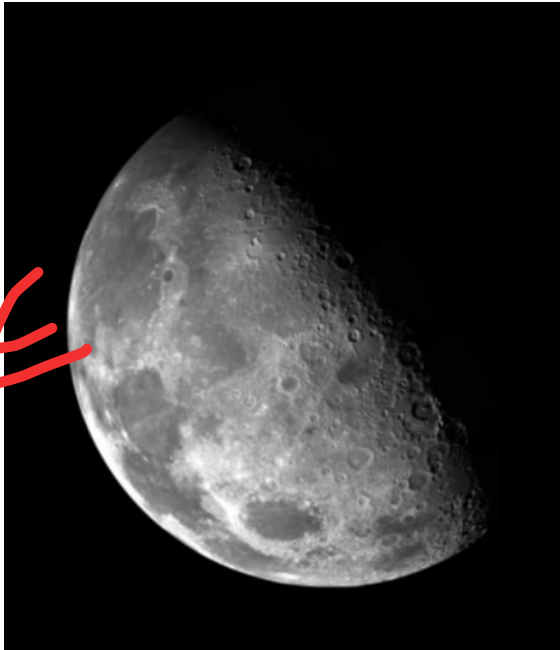
Point Processing Example: Negative Images (cont...)



$$s = \text{intensity}_{\max} - r$$

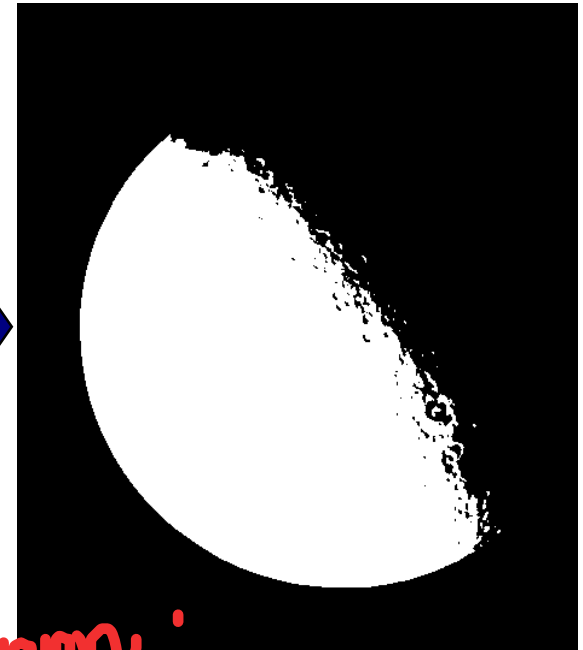
Point Processing Example: Thresholding

- Thresholding transformations are particularly useful for segmentation in which we want to isolate an object of interest from a background



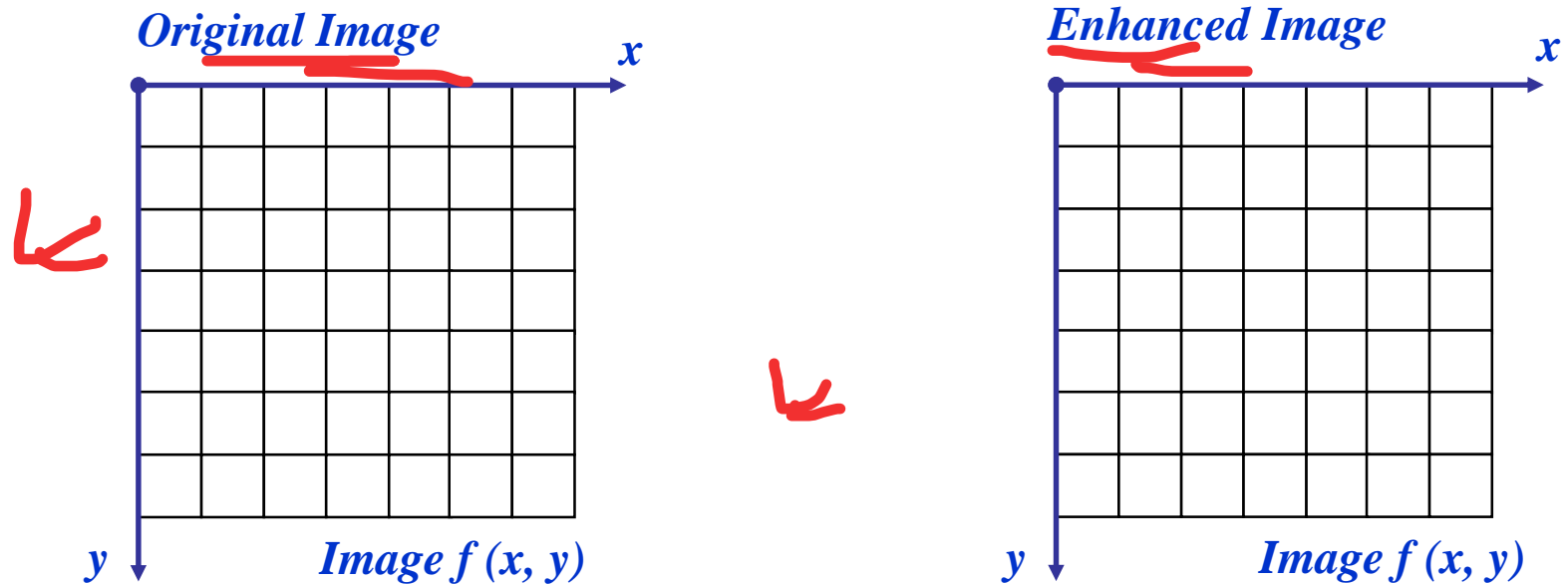
map

$$s = \begin{cases} 1.0 & r > \text{threshold} \\ 0.0 & r \leq \text{threshold} \end{cases}$$



isolating moon

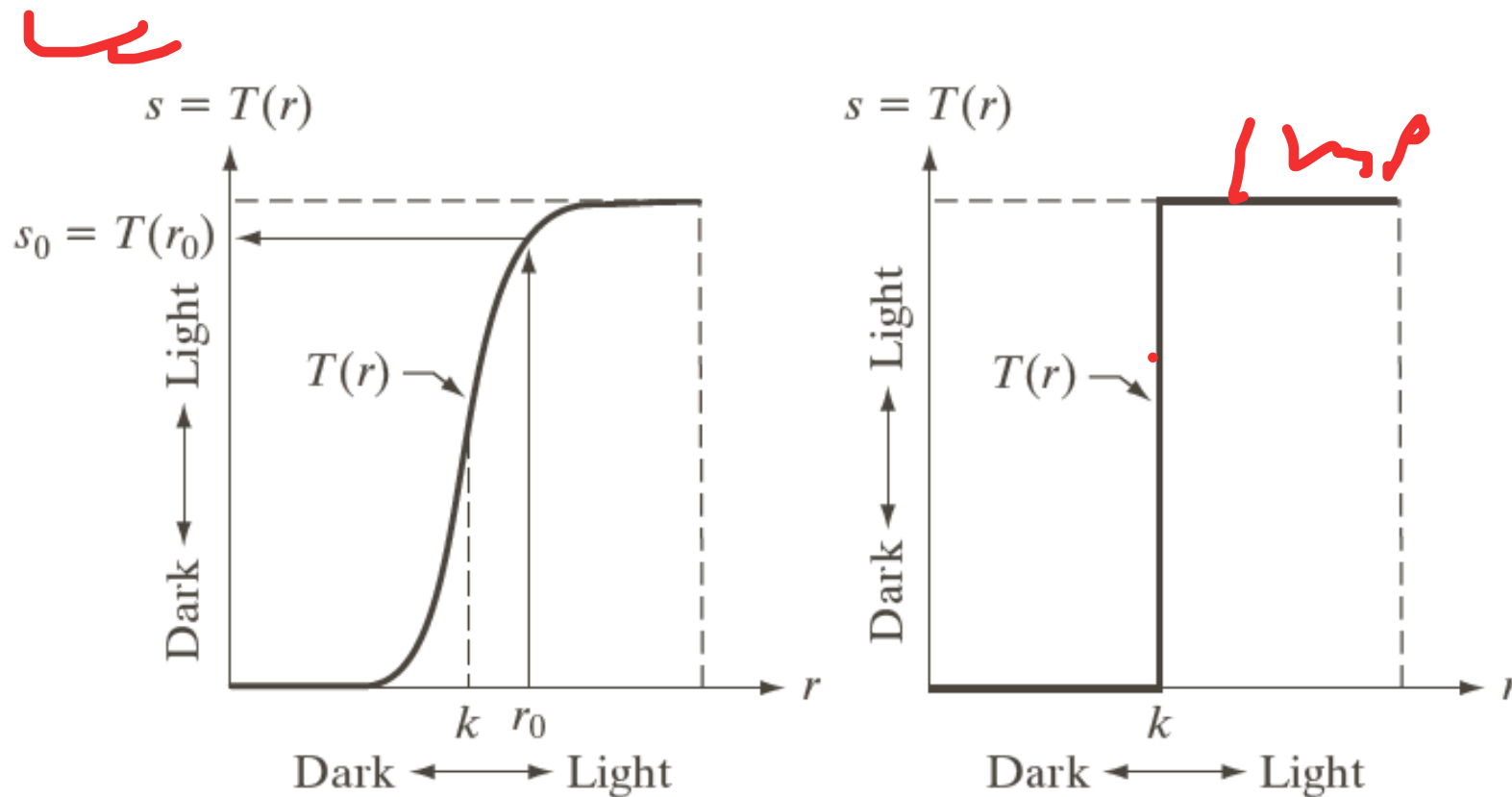
Point Processing Example: Thresholding (cont...)



$$s = \begin{cases} 1.0 & r > \text{threshold} \\ 0.0 & r \leq \text{threshold} \end{cases}$$

we have to find "profit"

Intensity Transformations



Basic Grey Level Transformations

- There are many different kinds of grey level transformations

- Three of the most common are shown here

- Linear

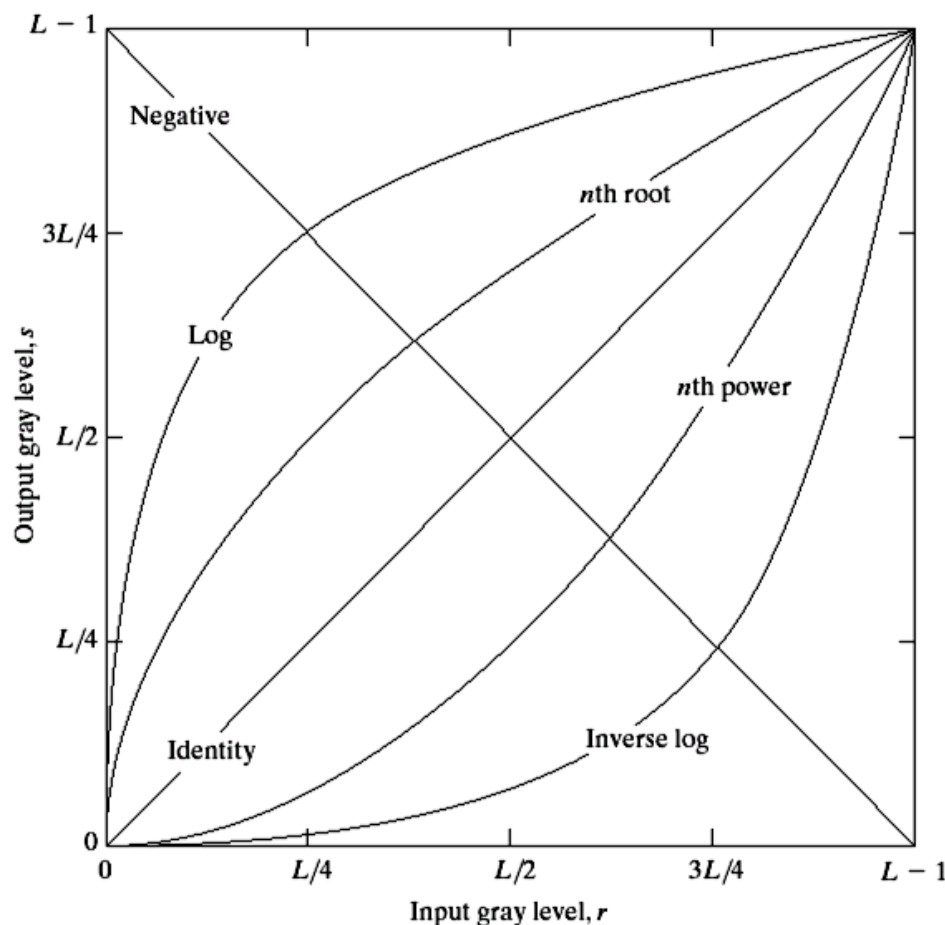
- Negative/Identity

- Logarithmic

- Log/Inverse log

- Power law

- n^{th} power/ n^{th} root



Logarithmic Transformations

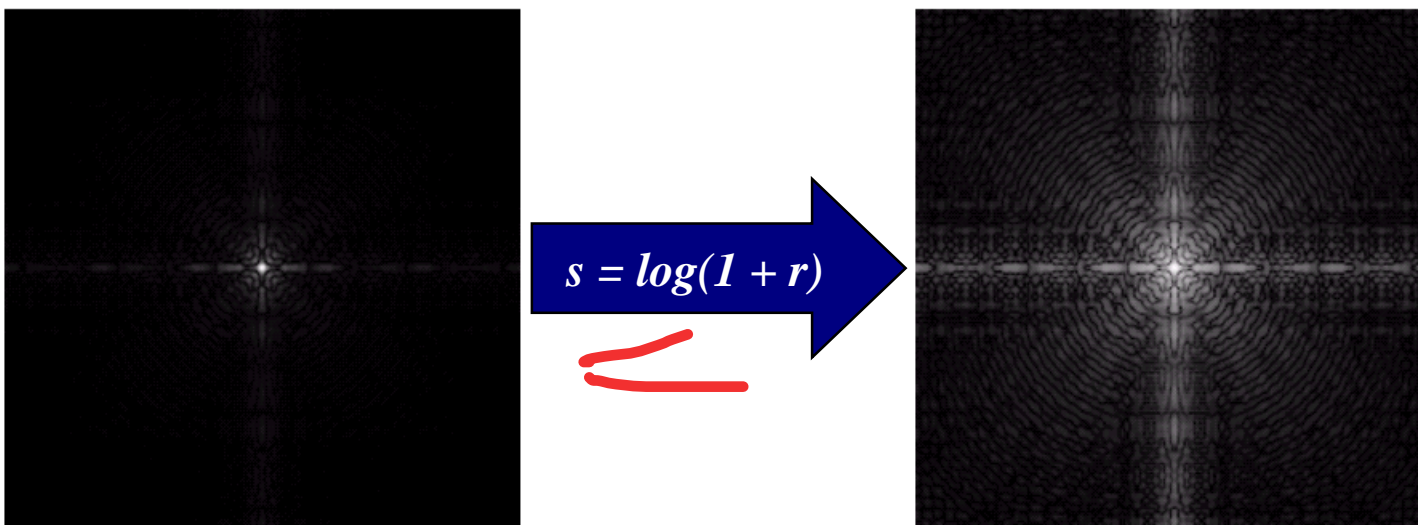
- ~~The~~ general form of the log transformation is

$$s = c * \log(1 + r)$$

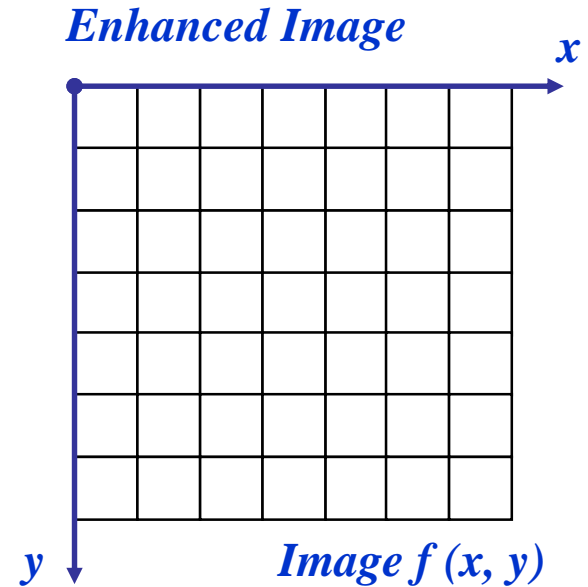
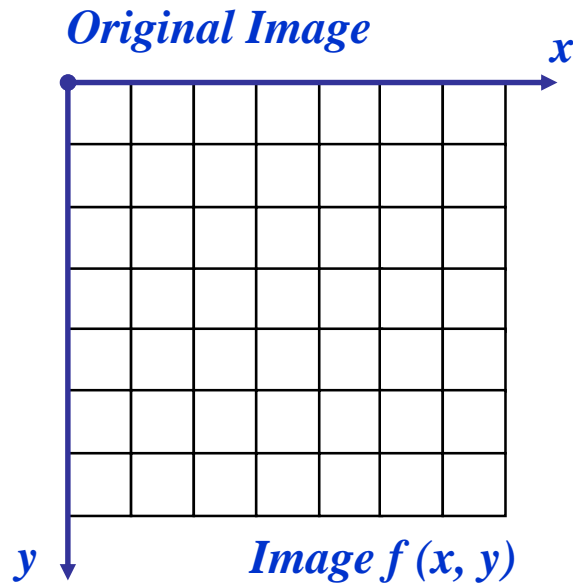
- The log transformation maps a narrow range of low input grey level values into a wider range of output values
- The inverse log transformation performs the opposite transformation

Logarithmic Transformations (cont...)

- Log functions are particularly useful when the input grey level values may have an extremely large range of values
- In the following example the Fourier transform of an image is put through a log transform to reveal more detail



Logarithmic Transformations (cont...)



$$s = \log(1 + r)$$

We usually set c to 1

Grey levels must be in the range ~~[0.0, 1.0]~~

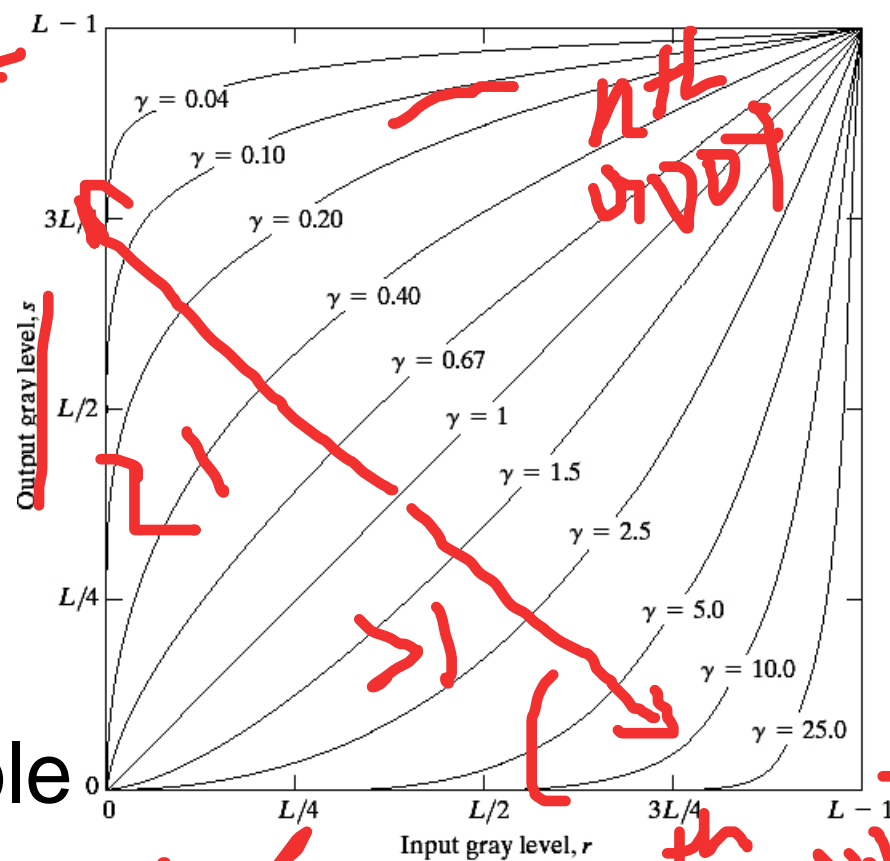
Power Law Transformations

• Power law transformations have the following form

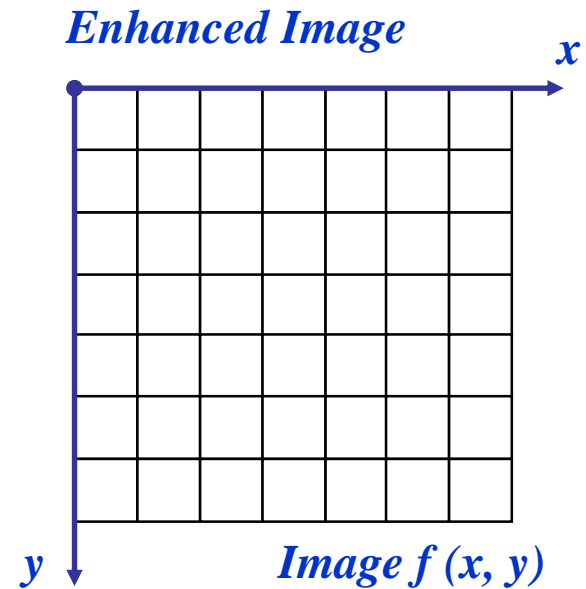
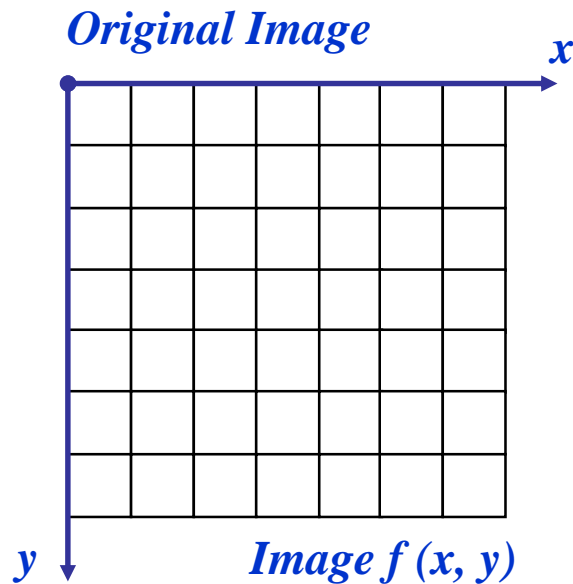
$$s = c * r^\gamma$$

• Map a narrow range of dark input values into a wider range of output values or vice versa

• Varying γ gives a whole family of curves



Power Law Transformations (cont...)



$$s = r^\gamma$$

- We usually ~~set c to 1~~
- Grey levels must be ~~in~~ in the range $[0.0, 1.0]$



Power Law Example



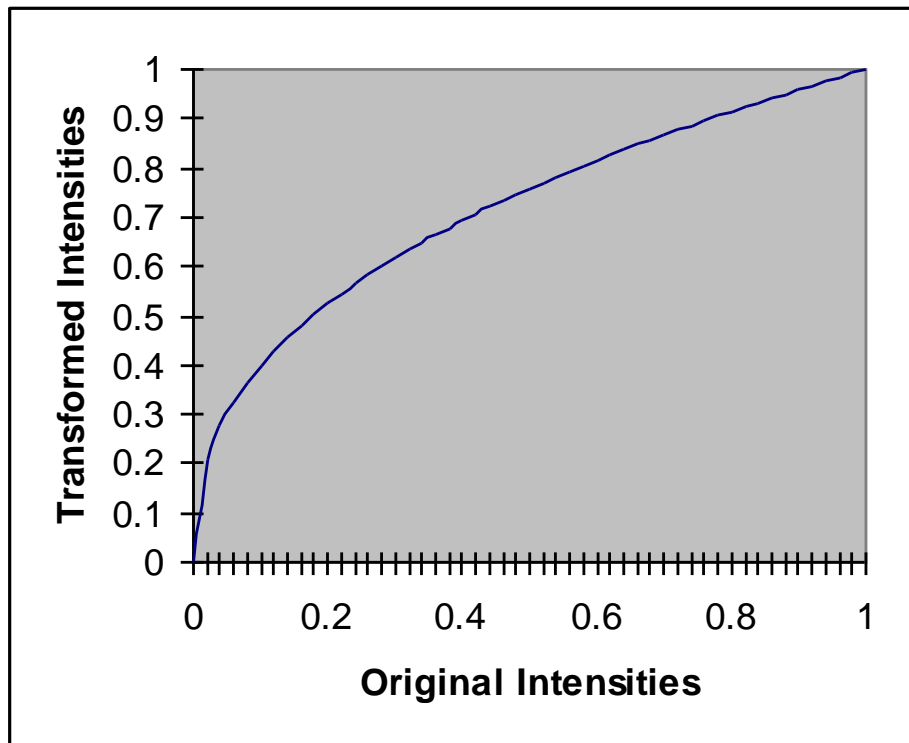
Power Law Example (cont...)

$$\gamma = 0.6$$



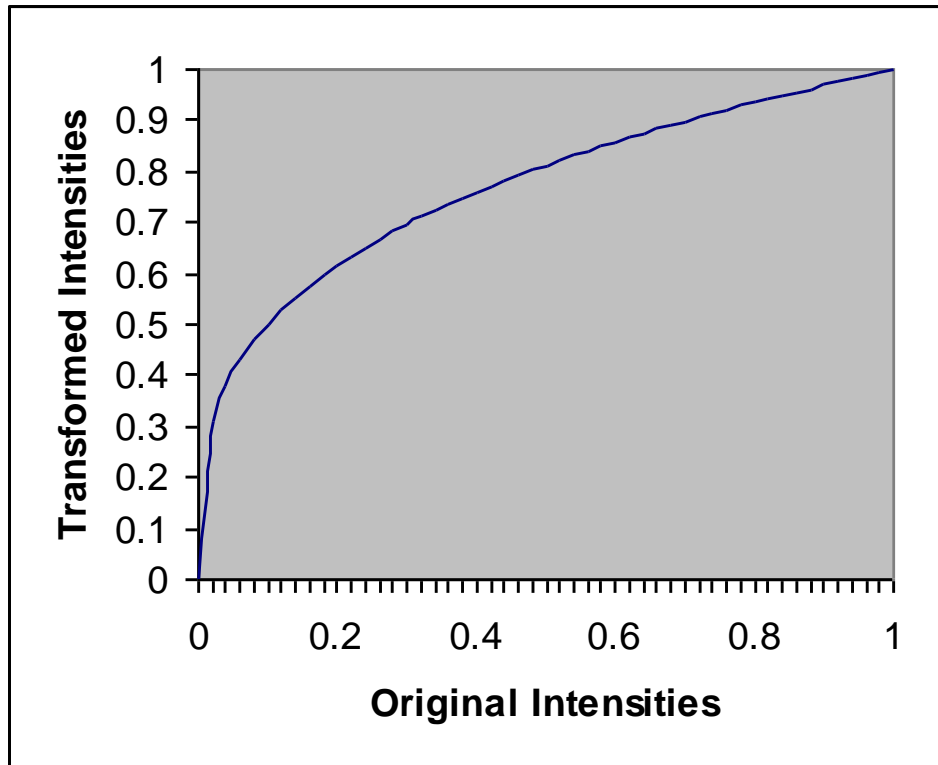
Power Law Example (cont...)

$$\gamma = 0.4$$



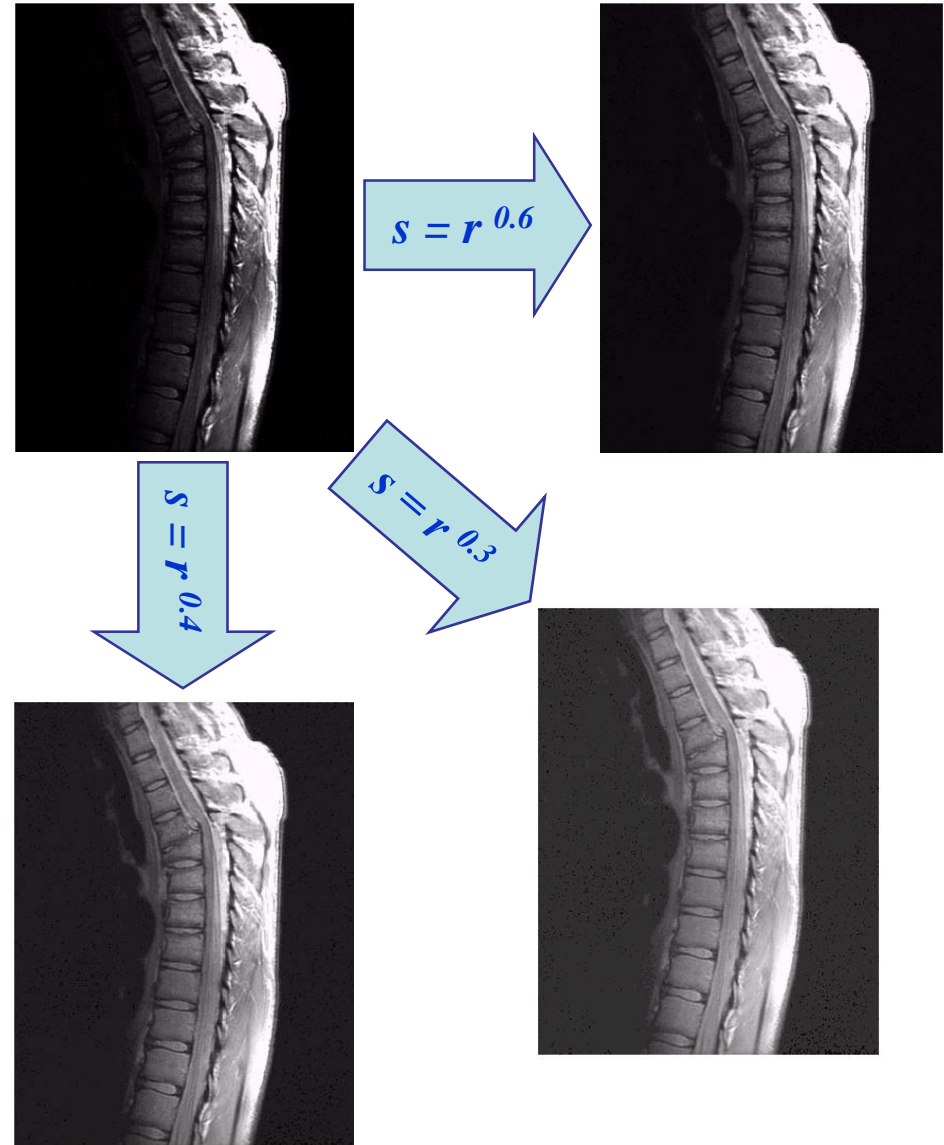
Power Law Example (cont...)

$$\gamma = 0.3$$



Power Law Example (cont...)

- The images to the right show a magnetic resonance (MR) image of a fractured human spine
- Different curves highlight different detail



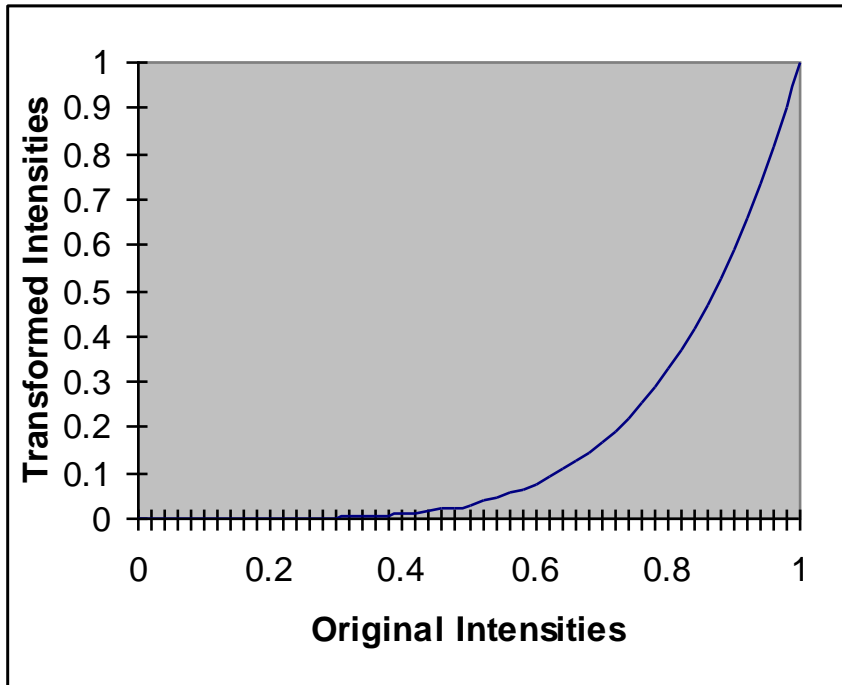
Power Law Example



Power Law Example (cont...)

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$$\gamma = 5.0$$

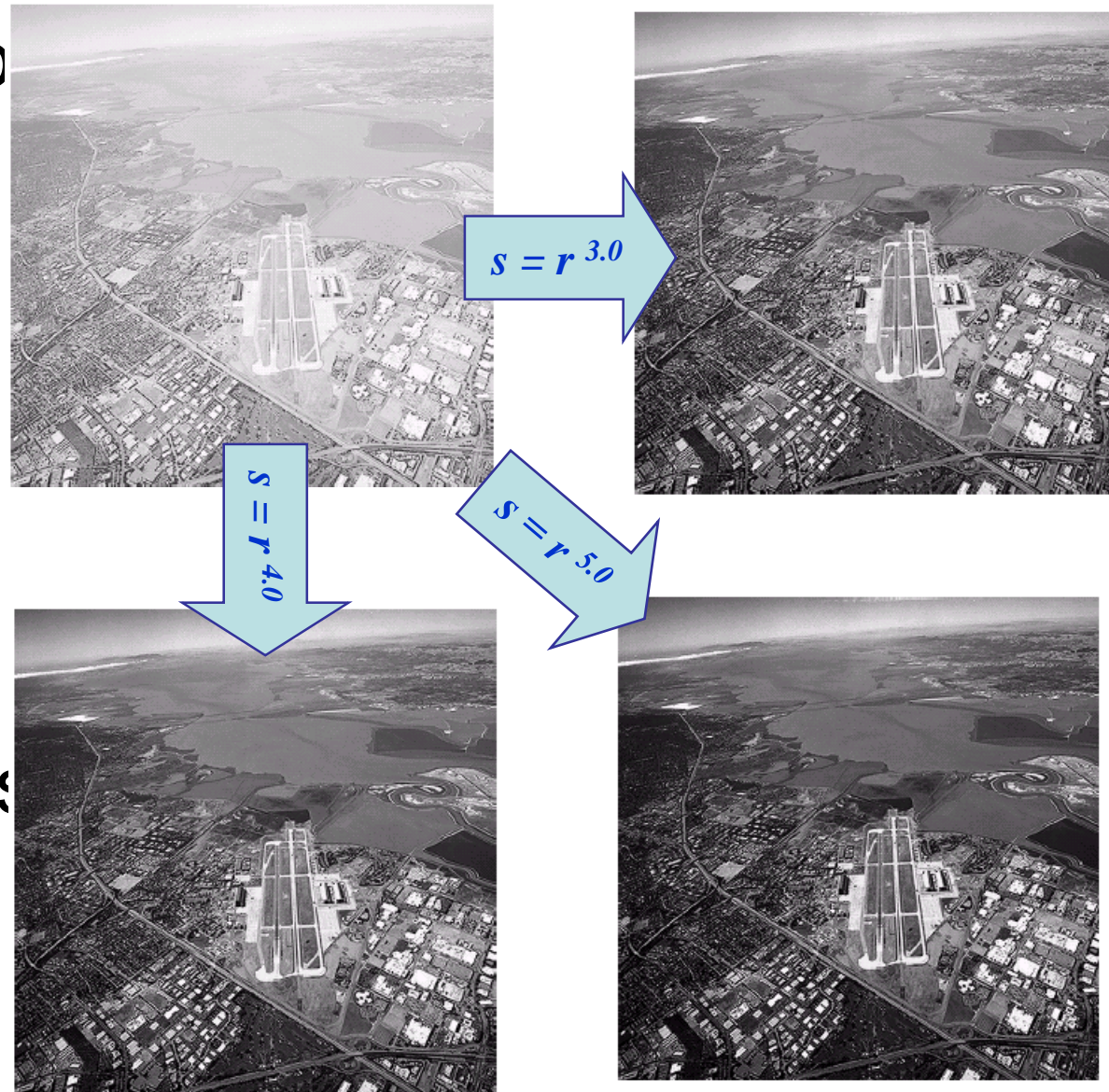


Power Law Transformations (cont...)

- An aerial photo of a runway is shown

- This time power law transforms are used to darken the image

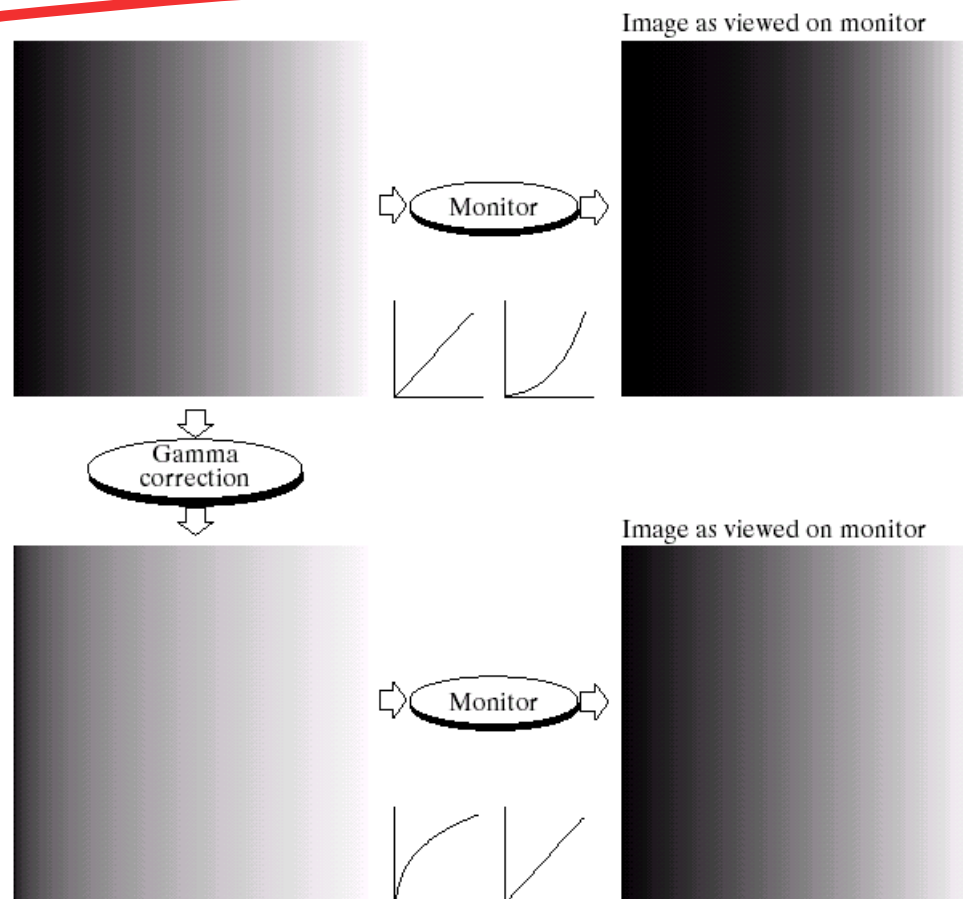
- Different curves highlight different detail



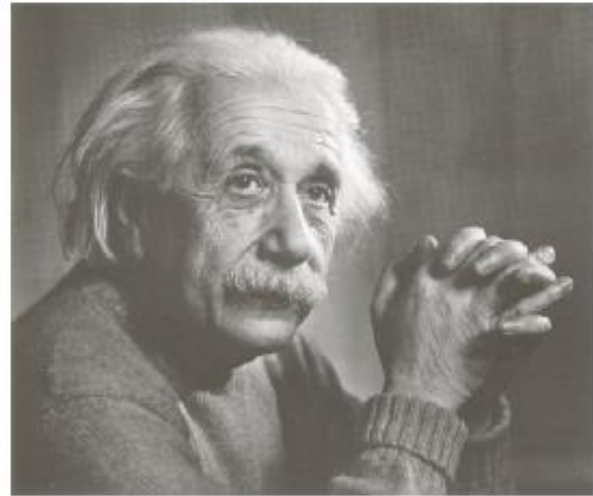
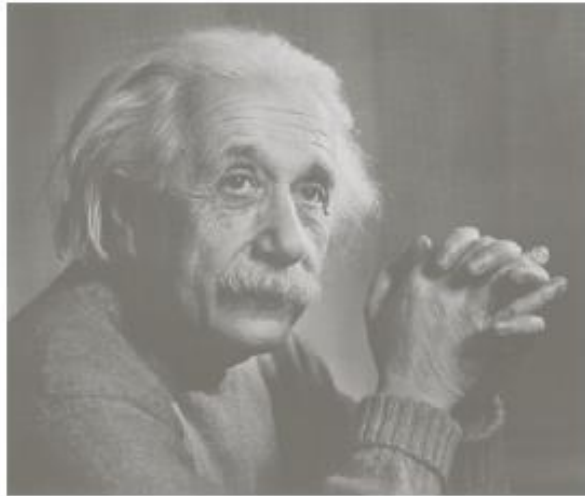
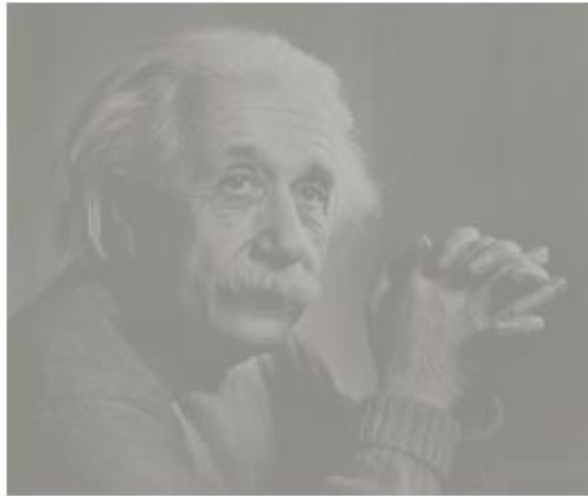


Gamma Correction

- Many of you might be familiar with gamma correction of computer monitors
- Problem is that display devices do not respond linearly to different intensities
- Can be corrected using a log transform



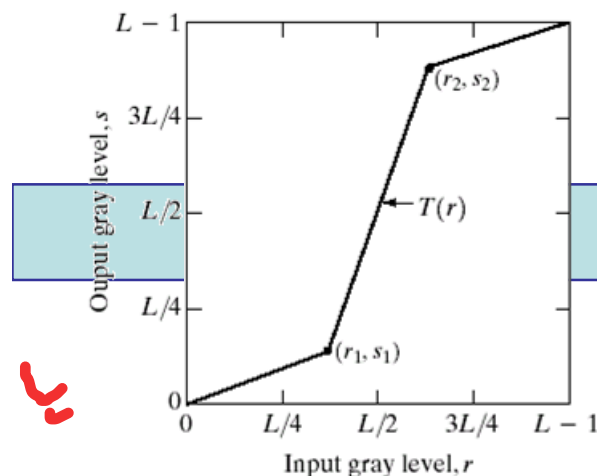
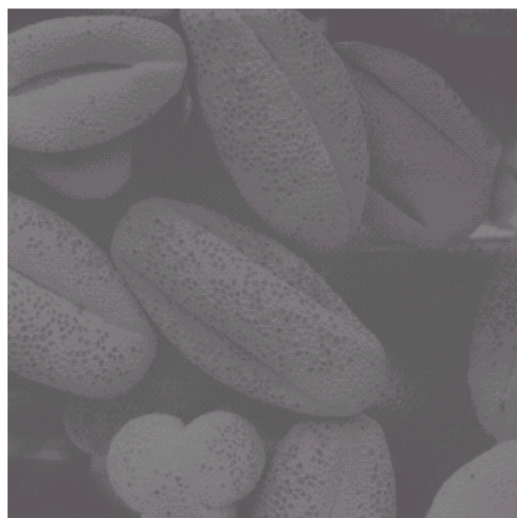
More Contrast Issues



✓

Piecewise Linear Transformation Functions

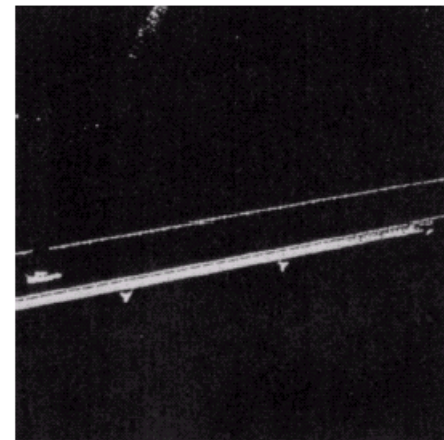
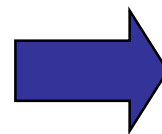
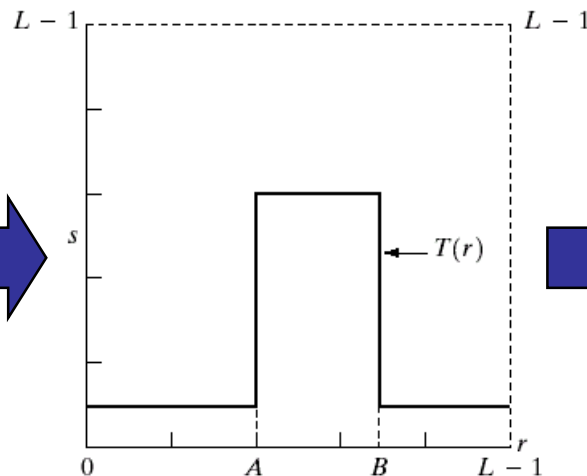
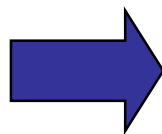
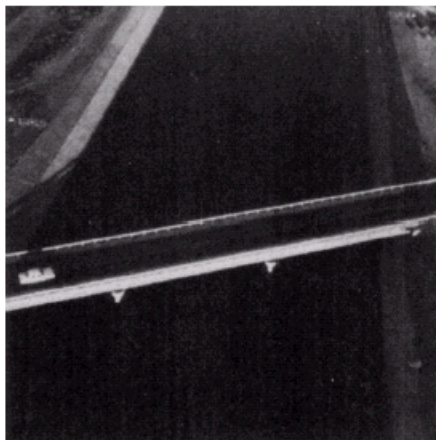
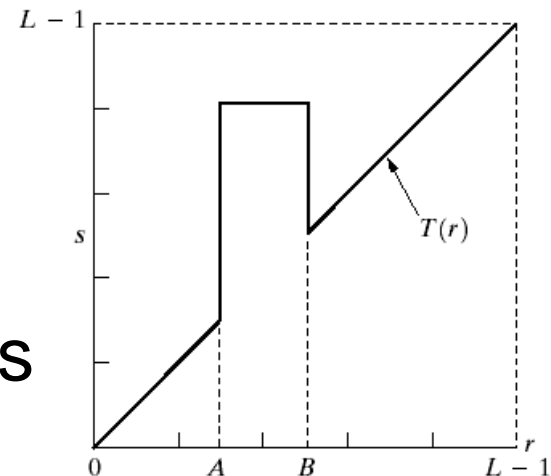
- Rather than using a well defined mathematical function we can use arbitrary user-defined transforms
- The images below show a contrast stretching linear transform to add contrast to a poor quality image



Gray Level Slicing

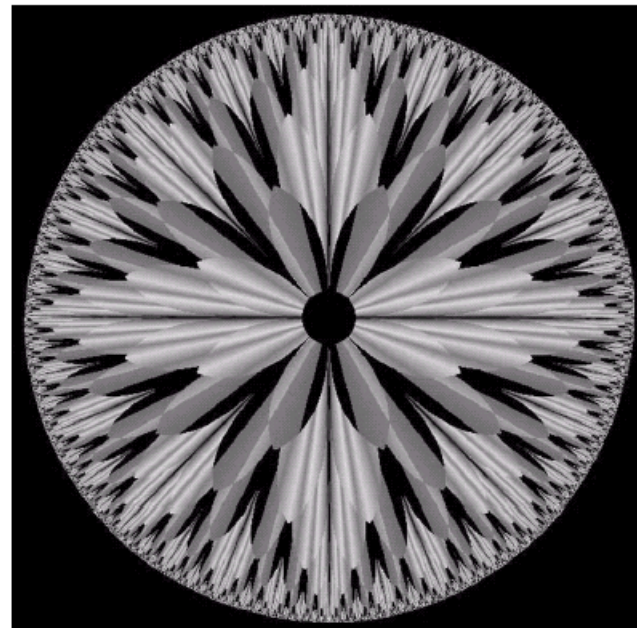
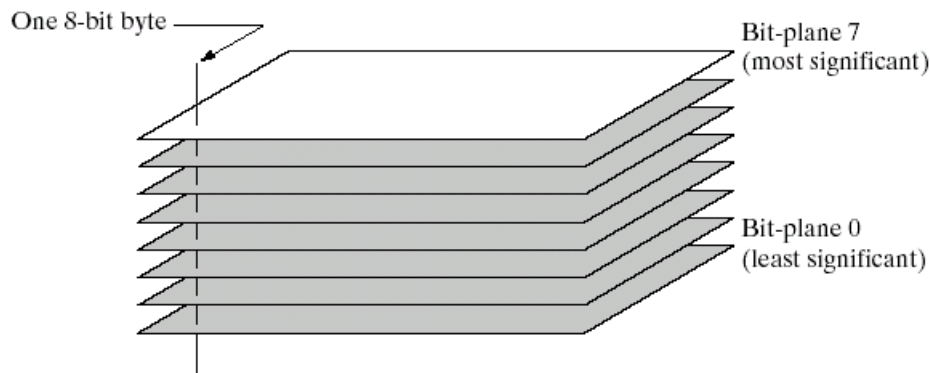
- Highlights a specific range of grey levels

- Similar to thresholding
- Other levels can be suppressed or maintained
- Useful for highlighting features in an image



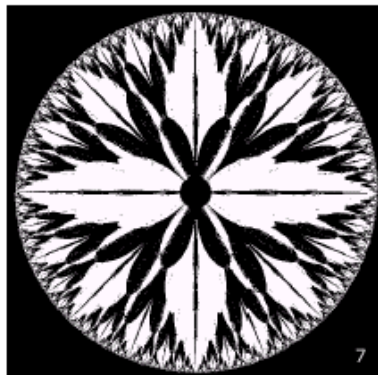
Bit Plane Slicing

- Often by isolating particular bits of the pixel values in an image we can highlight interesting aspects of that image
 - Higher-order bits usually contain most of the significant visual information
 - Lower-order bits contain subtle details

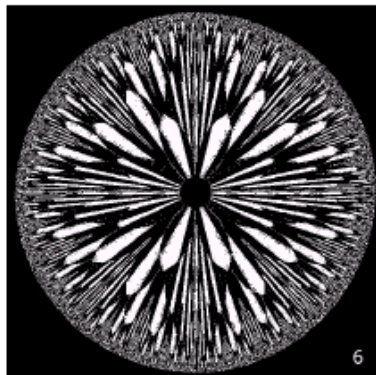


Bit Plane Slicing (cont...)

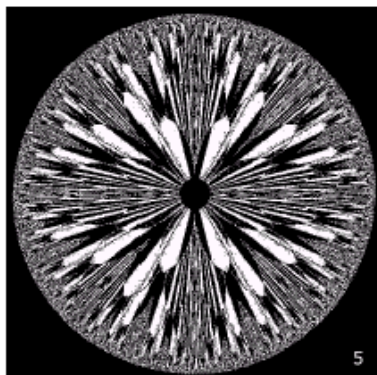
[10000000]



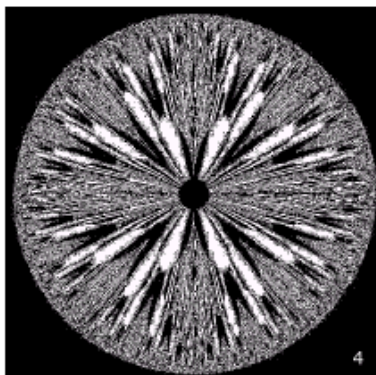
[01000000]



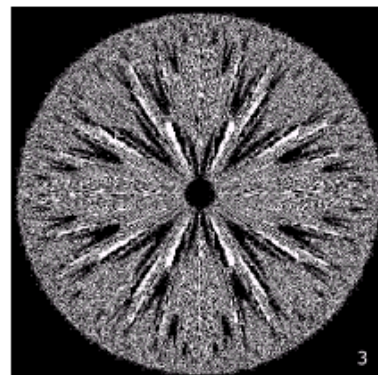
[00100000]



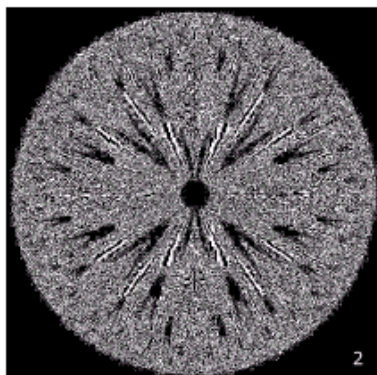
[00001000]



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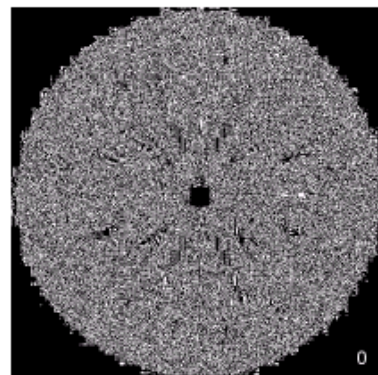
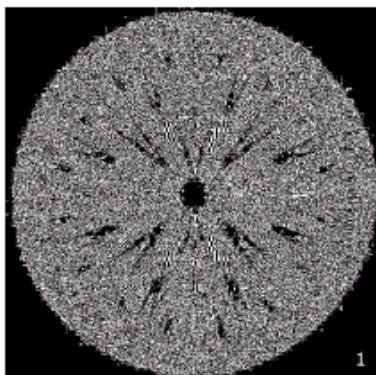


[00000100]



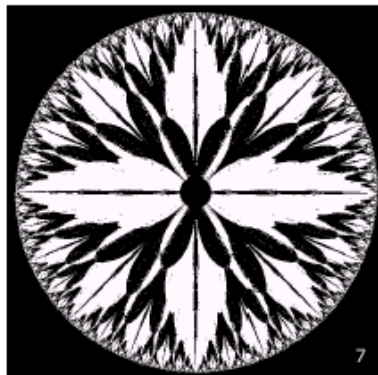
[00000001]

—
—

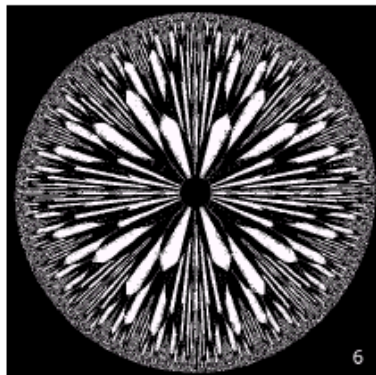


Bit Plane Slicing (cont...)

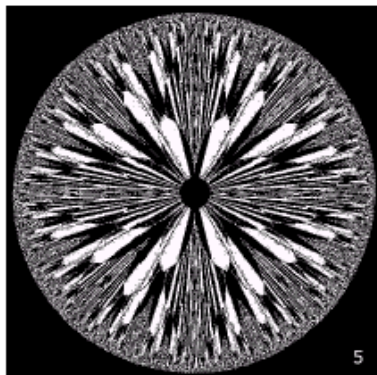
[10000000]



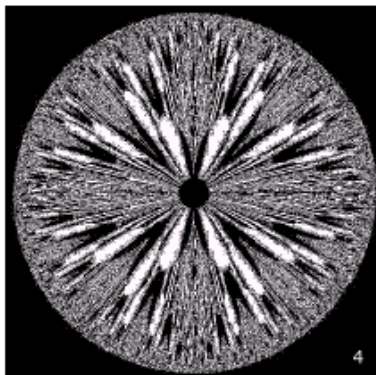
[01000000]



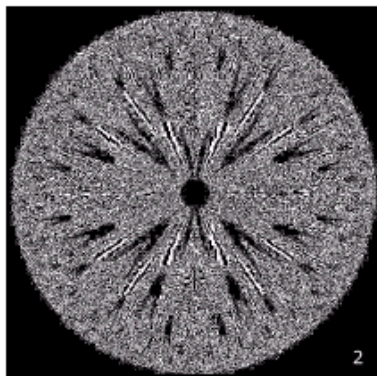
[00100000]



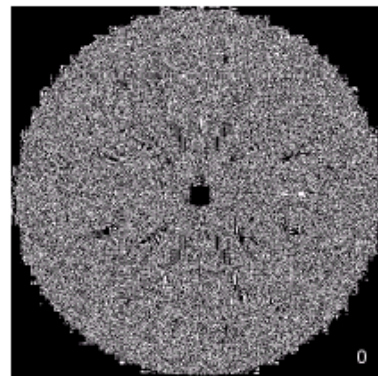
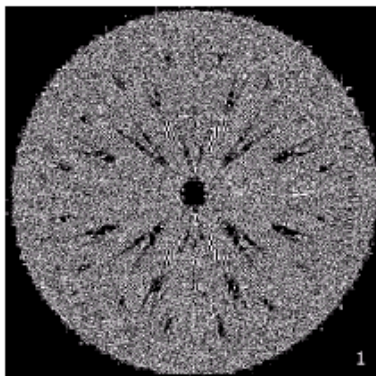
[00001000]



[00000100]



[00000001]



Bit Plane Slicing (cont...)



a	b	c
d	e	f
g	h	i

FIGURE 3.14 (a) An 8-bit gray-scale image of size 500×1192 pixels. (b) through (i) Bit planes 1 through 8, with bit plane 1 corresponding to the least significant bit. Each bit plane is a binary image.

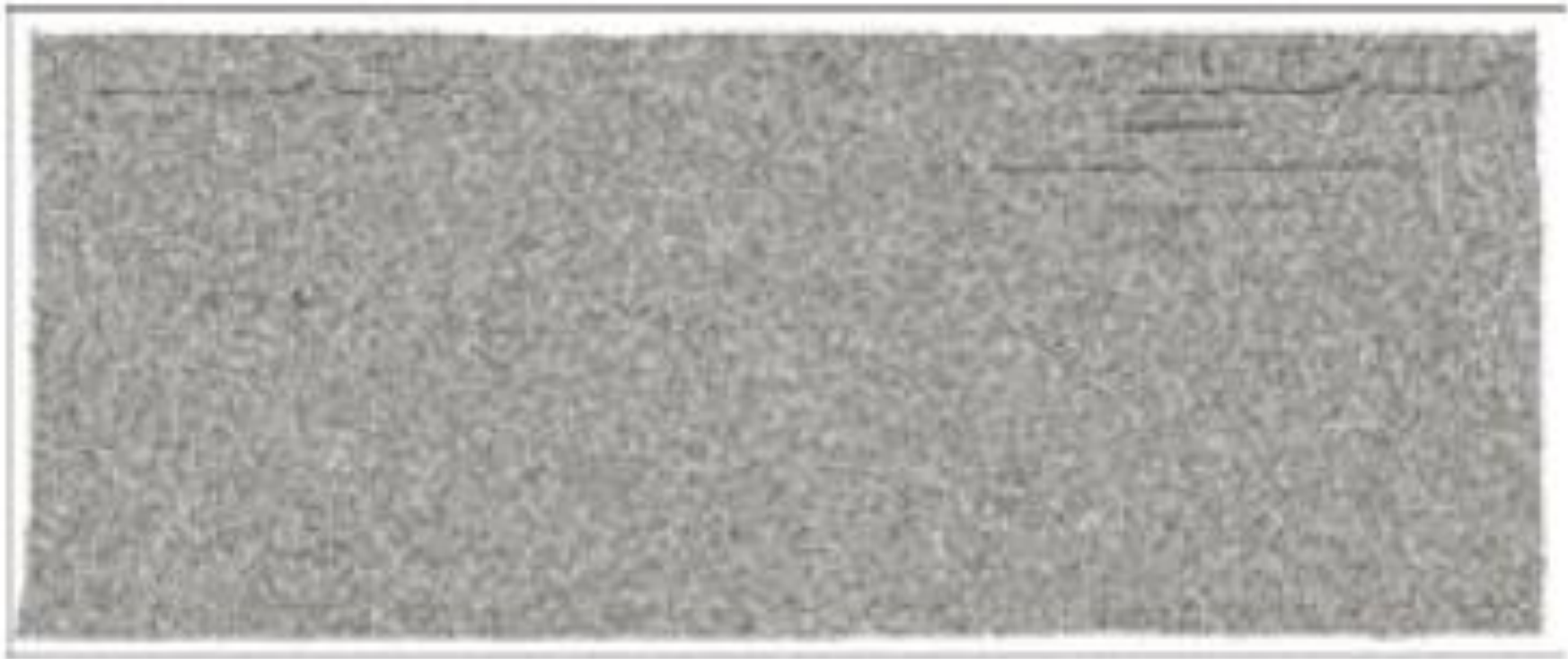
Bit Plane Slicing (cont...)



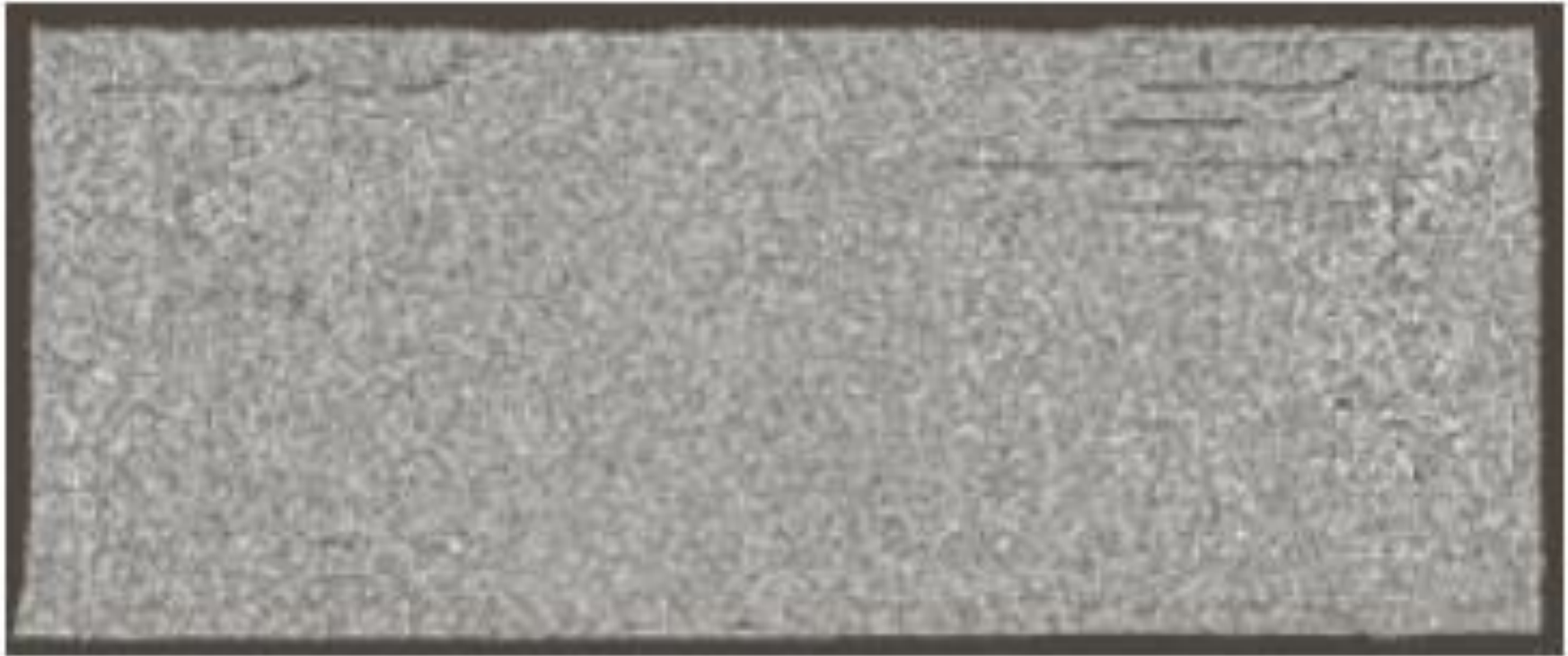
Bit Plane Slicing (cont...)



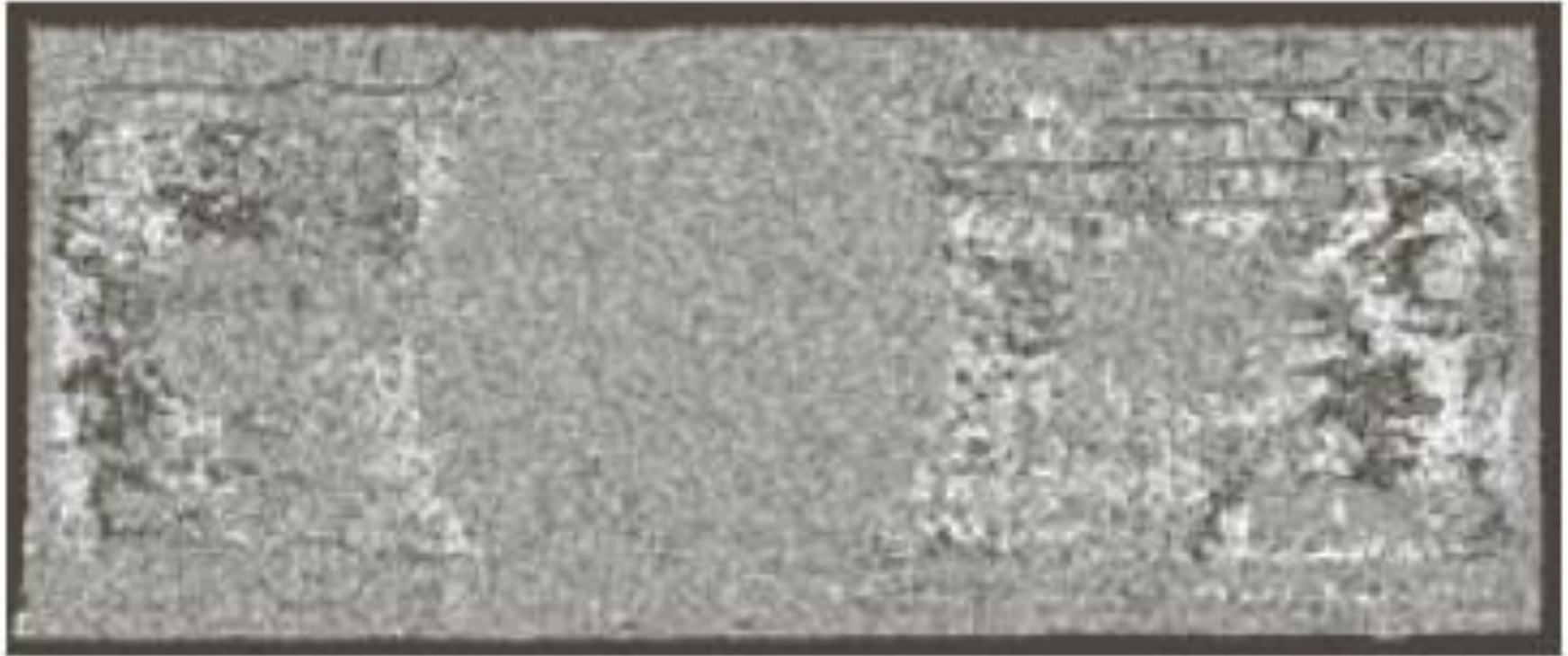
Bit Plane Slicing (cont...)



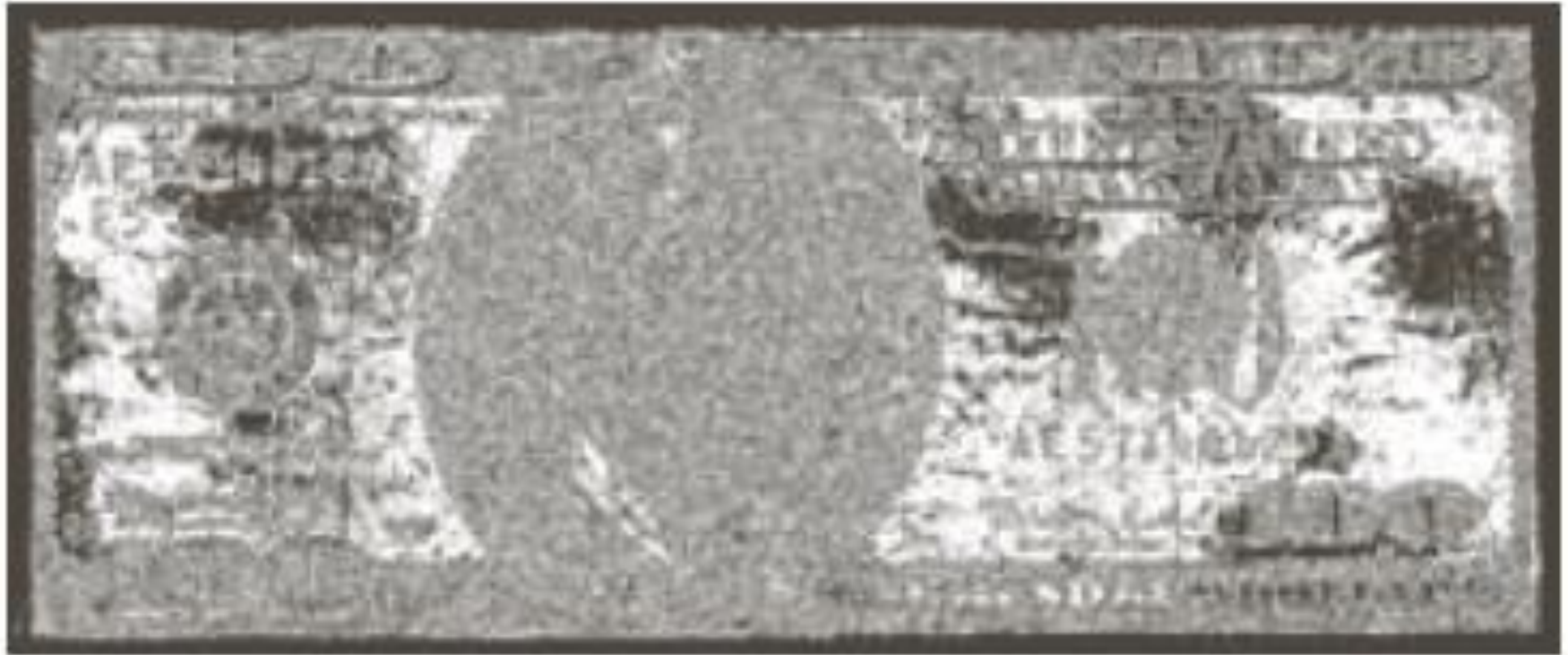
Bit Plane Slicing (cont...)



Bit Plane Slicing (cont...)



Bit Plane Slicing (cont...)



Bit Plane Slicing (cont...)



Bit Plane Slicing (cont...)



Bit Plane Slicing (cont...)



Bit Plane Slicing (cont...)



Reconstructed image
using only bit planes 8
and 7



Reconstructed image
using only bit planes 8, 7
and 6



Reconstructed image
using only bit planes 7, 6
and 5

- We have looked at different kinds of point processing image enhancement
- Next time we will start to look at neighbourhood operations – in particular *filtering* and *convolution*