

# Decision Trees and Random Forests

**Dr. Debdoot Sheet**

Assistant Professor

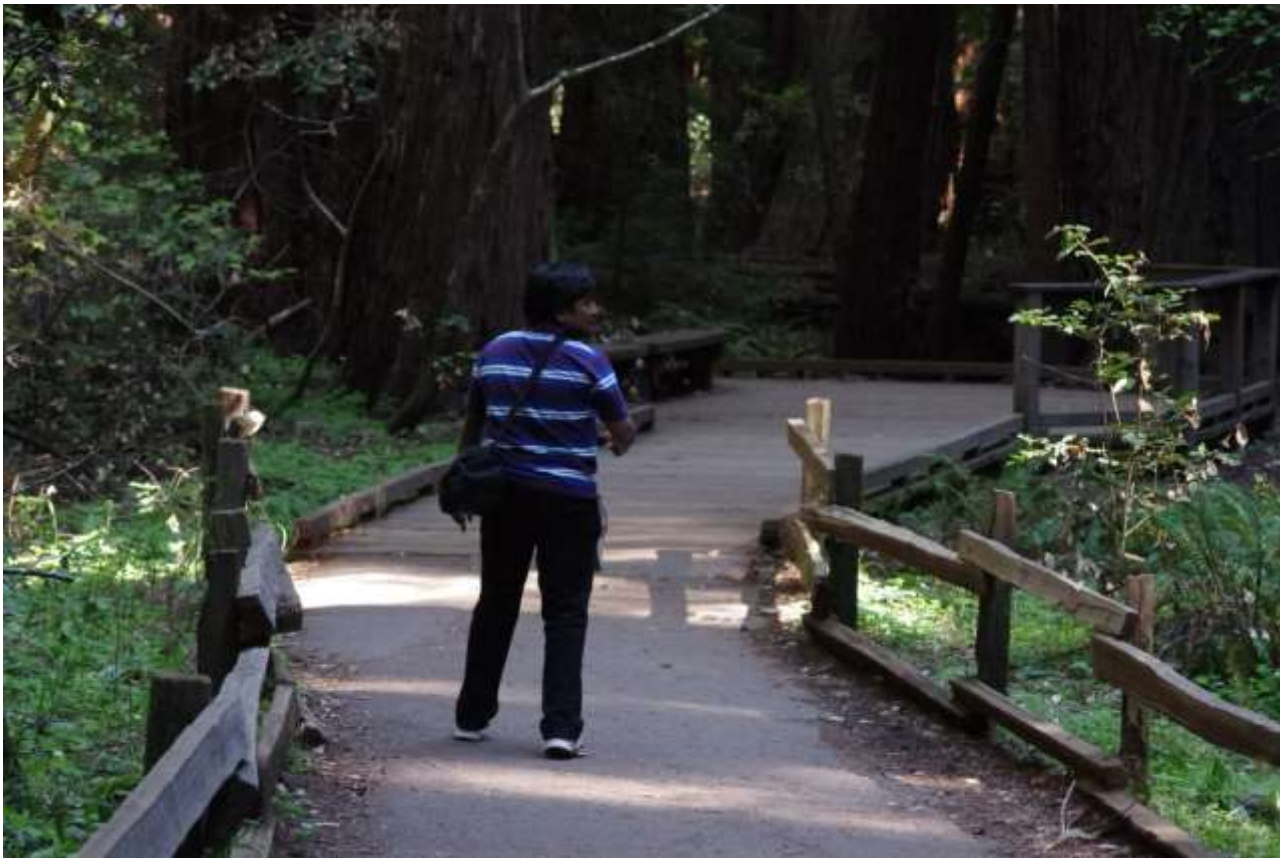
Department of Electrical Engineering  
Indian Institute of Technology Kharagpur

[www.facweb.iitkgp.ernet.in/~debdoot/](http://www.facweb.iitkgp.ernet.in/~debdoot/)



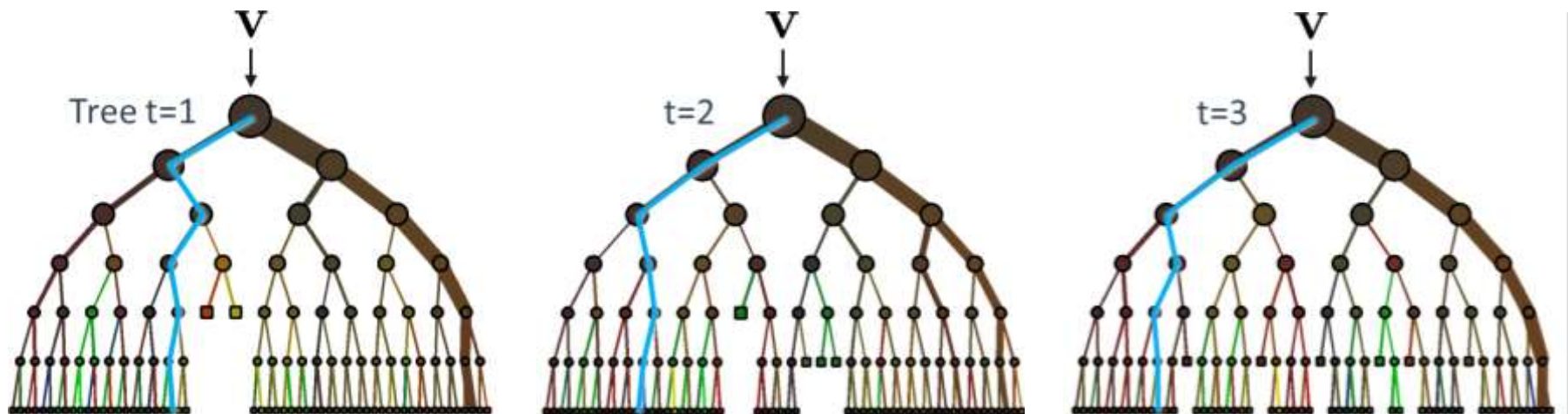


# NOT ABOUT WALKING IN A FOREST





# IS ALL ABOUT





# Overview

- Historical Perspective
- Decision Tree
- Random Forest
- Application Scenarios
- Computational Complexity
- Variable Importance
- What's hot about them in ML Research?



# Historical Perspective

## Decision Trees

- L. Breiman, J. Friedman, C. J. Stone, and R. A. Olshen, *Classification and Regression Trees*. Chapman and Hall/CRC (SIAM), **1984**.
- J. R. Quinlan, *C4.5: Programs for Machine Learning*. **1993**.

## Random Forests

- Y. Amit and D. Geman., "Shape quantization and recognition with randomized trees," *Neural Computation*, vol. 9, pp. 1545–1588, **1997**.
- T. K. Ho, "The random subspace method for constructing decision forests," *IEEE T-PAMI*, vol. 20, no. 8, pp. 832–844, **1998**.
- L. Breiman, "Random forests," *Machine Learning*, vol. 45, no. 1, pp. 5–32, **2001**.







# DECISION TREE





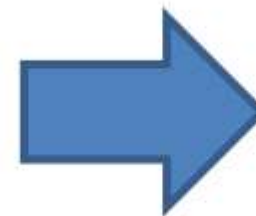
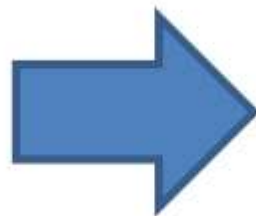
# Problem Statement

			
Queen	Princess	Soldier	Worker

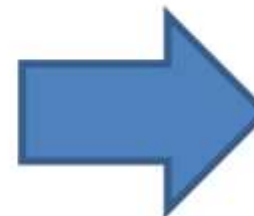
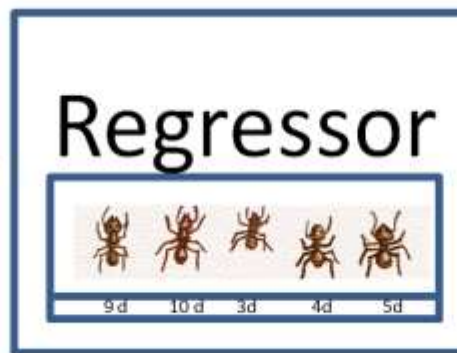
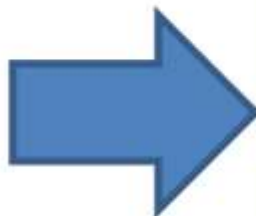
*Formica rufa* (Red wood ant)



# Classification vs. Regression



Worker

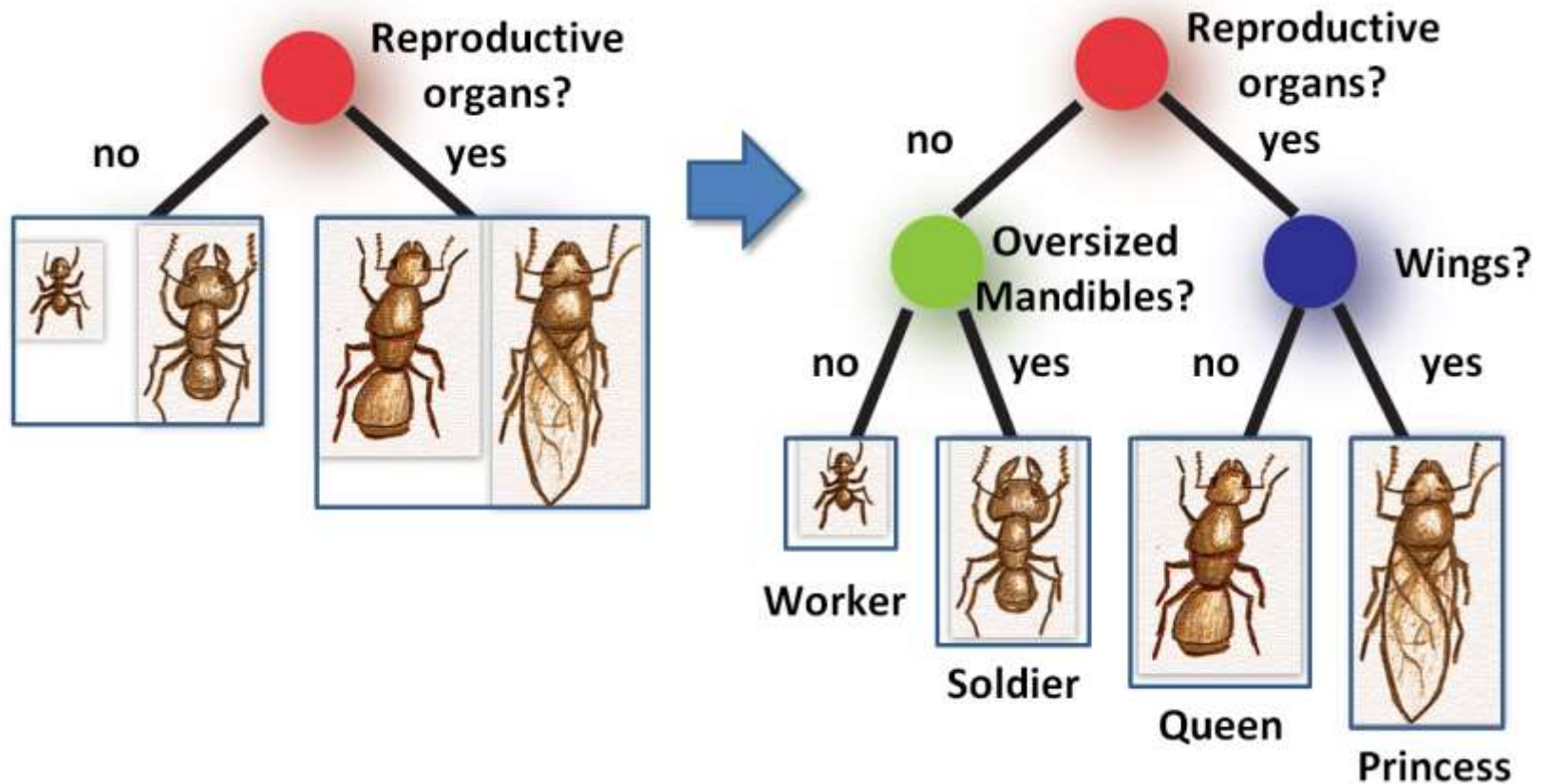


6 days





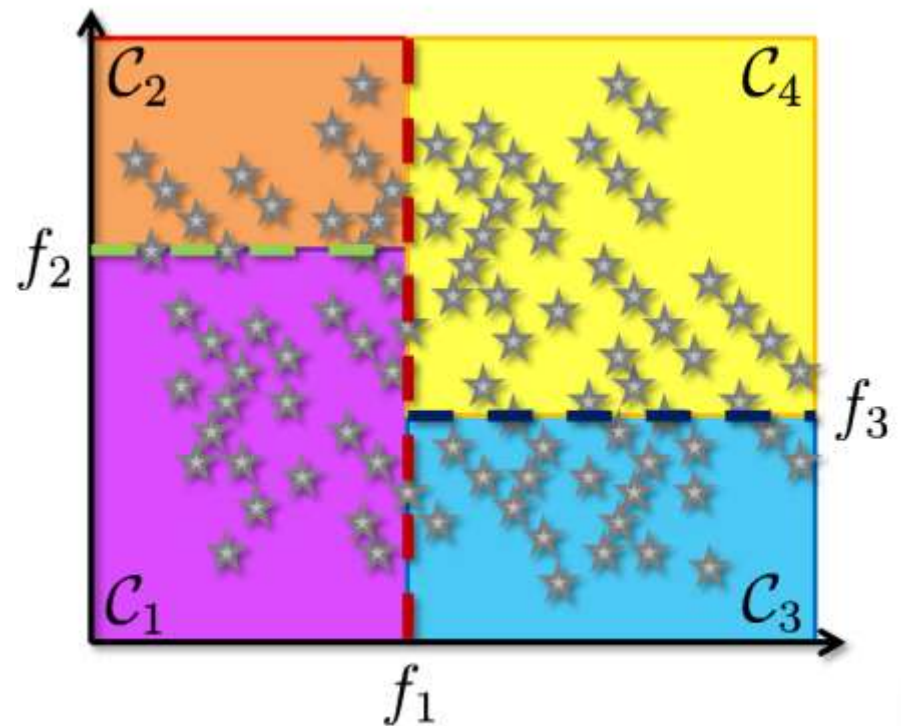
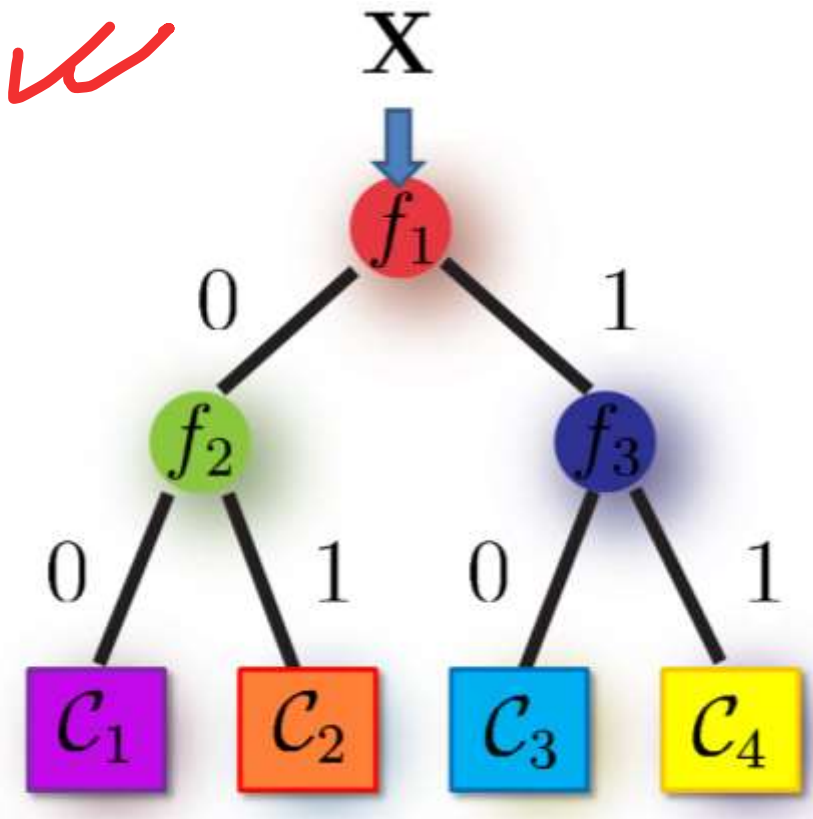
# Decision Tree





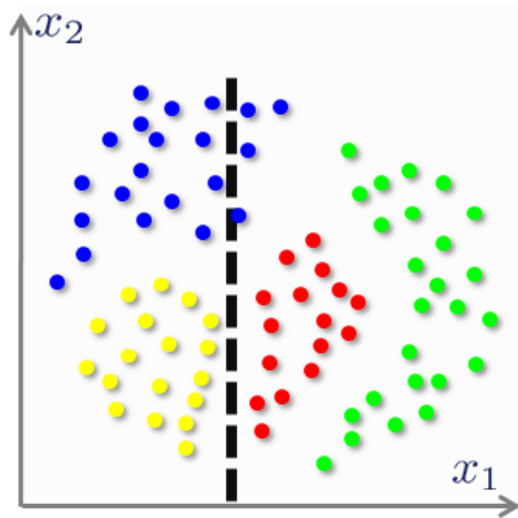
4-CLASS

# Forming a Decision Tree



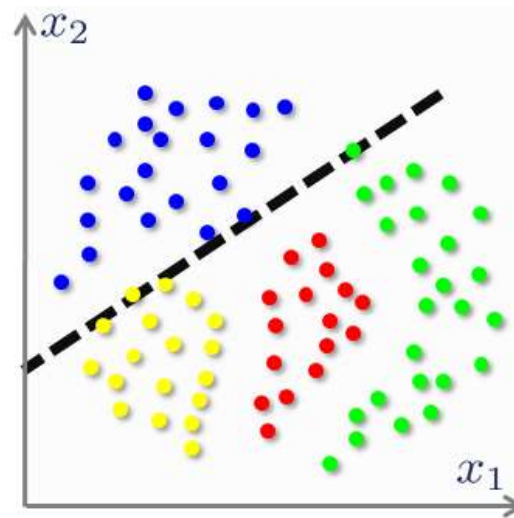


# Step 1: Split Function at Node



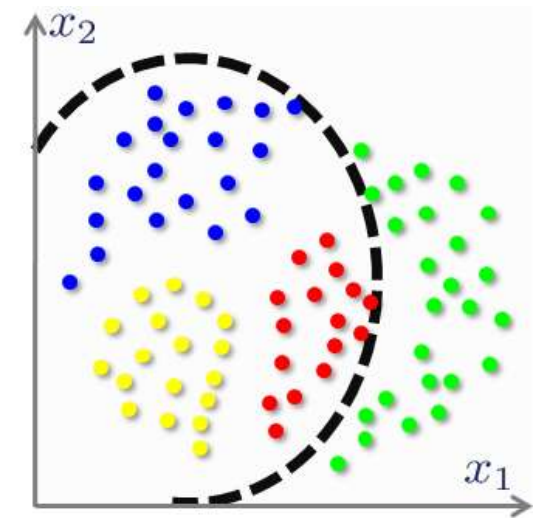
(a)

~~Axis aligned split~~



(b)

~~Oblique split~~

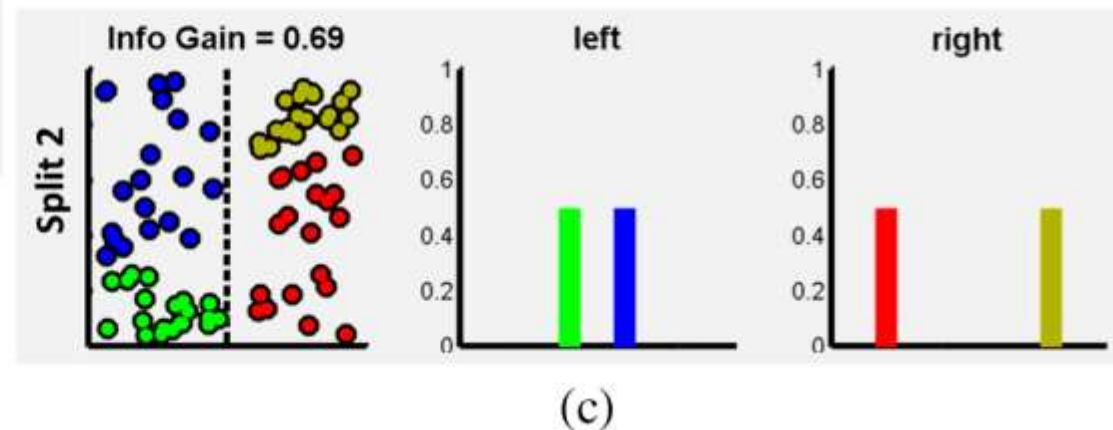
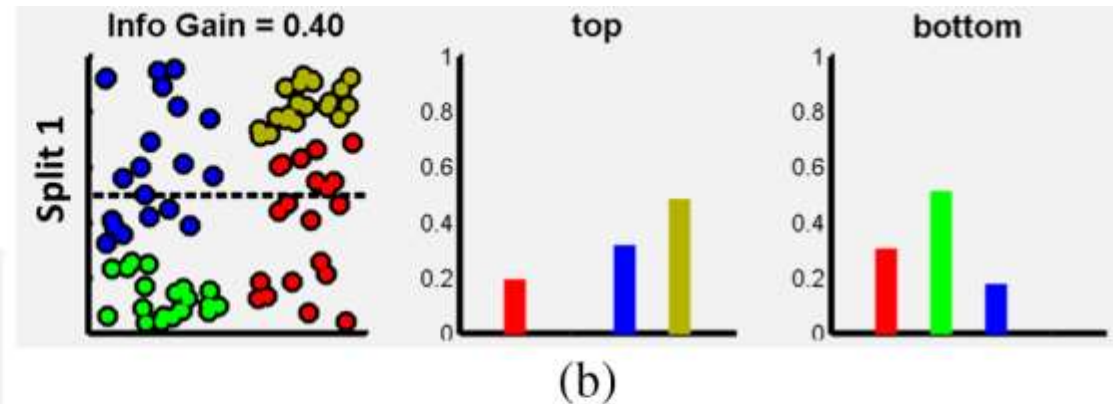
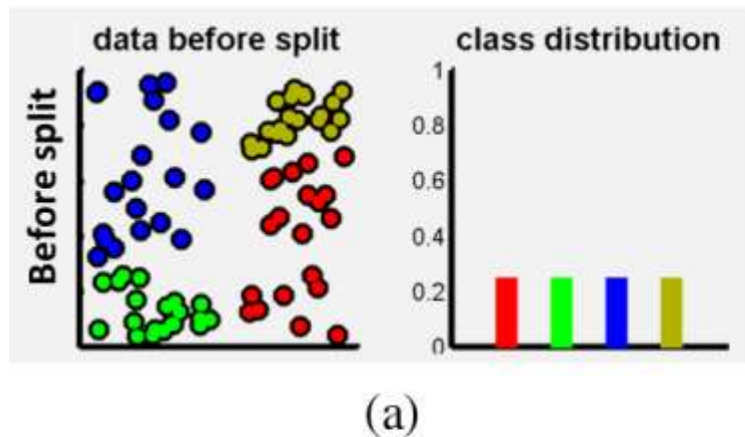


(c)

~~Polynomial split~~



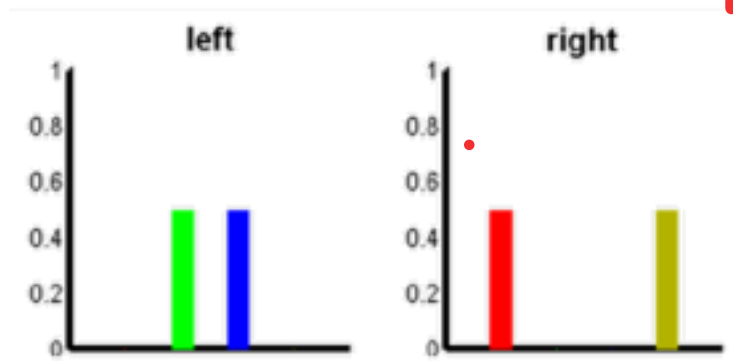
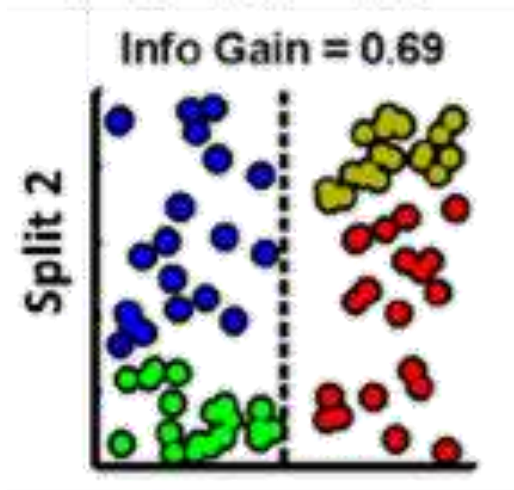
# Step 2: Assessing Purity of Split







# Cost function for Split Purity



1 hr  
Entropy of class distribution

$$H(S) = - \sum_{c \in C} p(c) \log(p(c)).$$

4 hr  
Information Gain

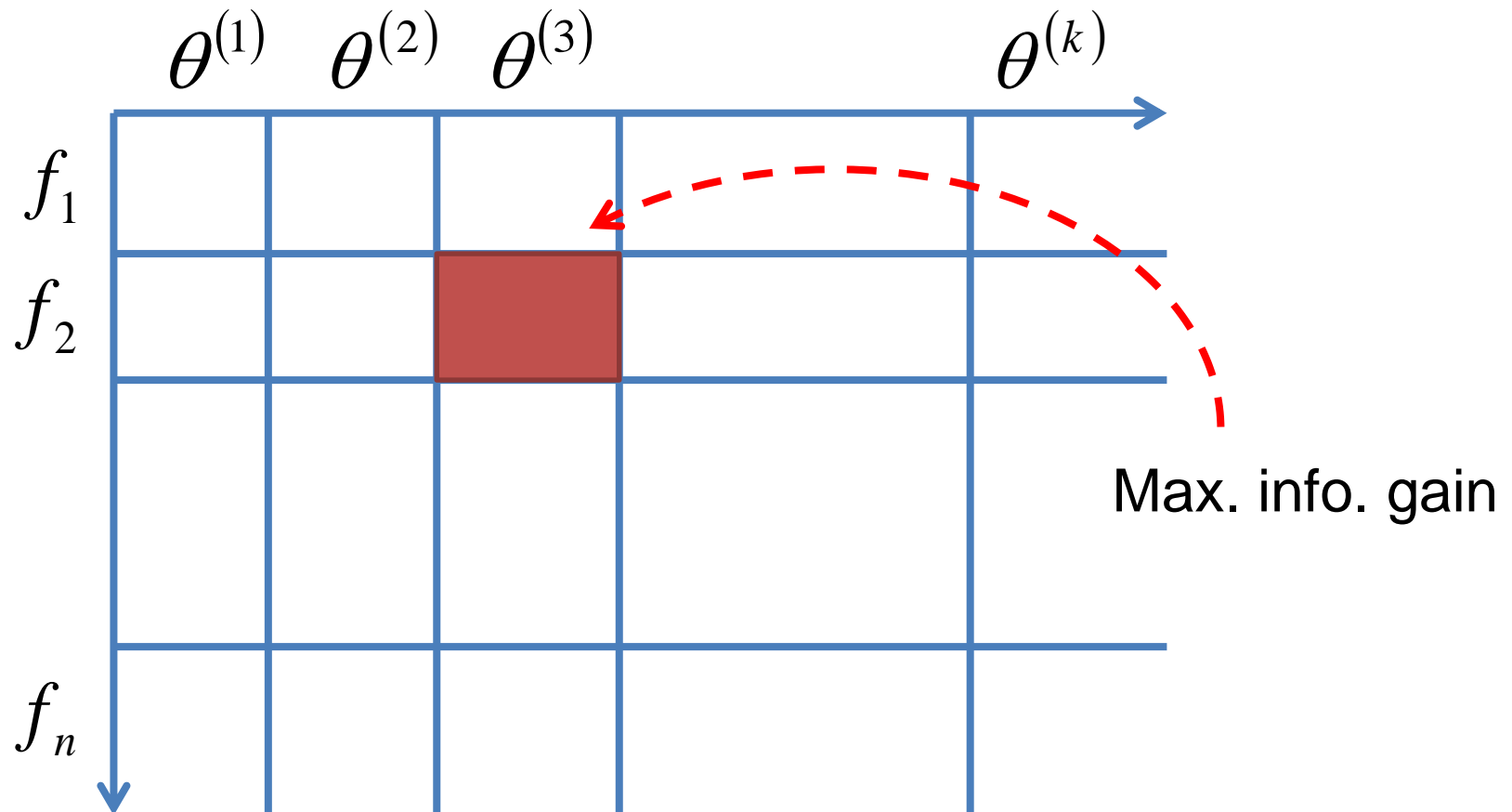
$$I = H(S) - \sum_{i \in \{L, R\}} \frac{|S^i|}{|S|} H(S^i).$$

1 hr



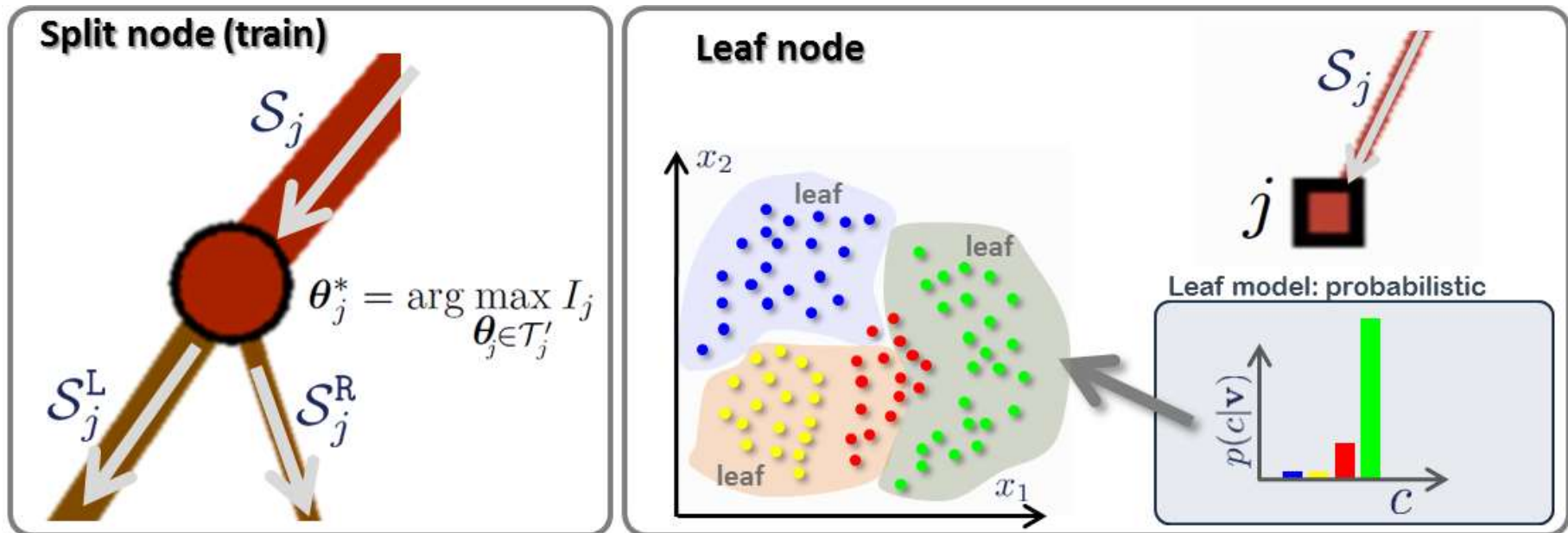


## Step 3: Selecting Optimum Split



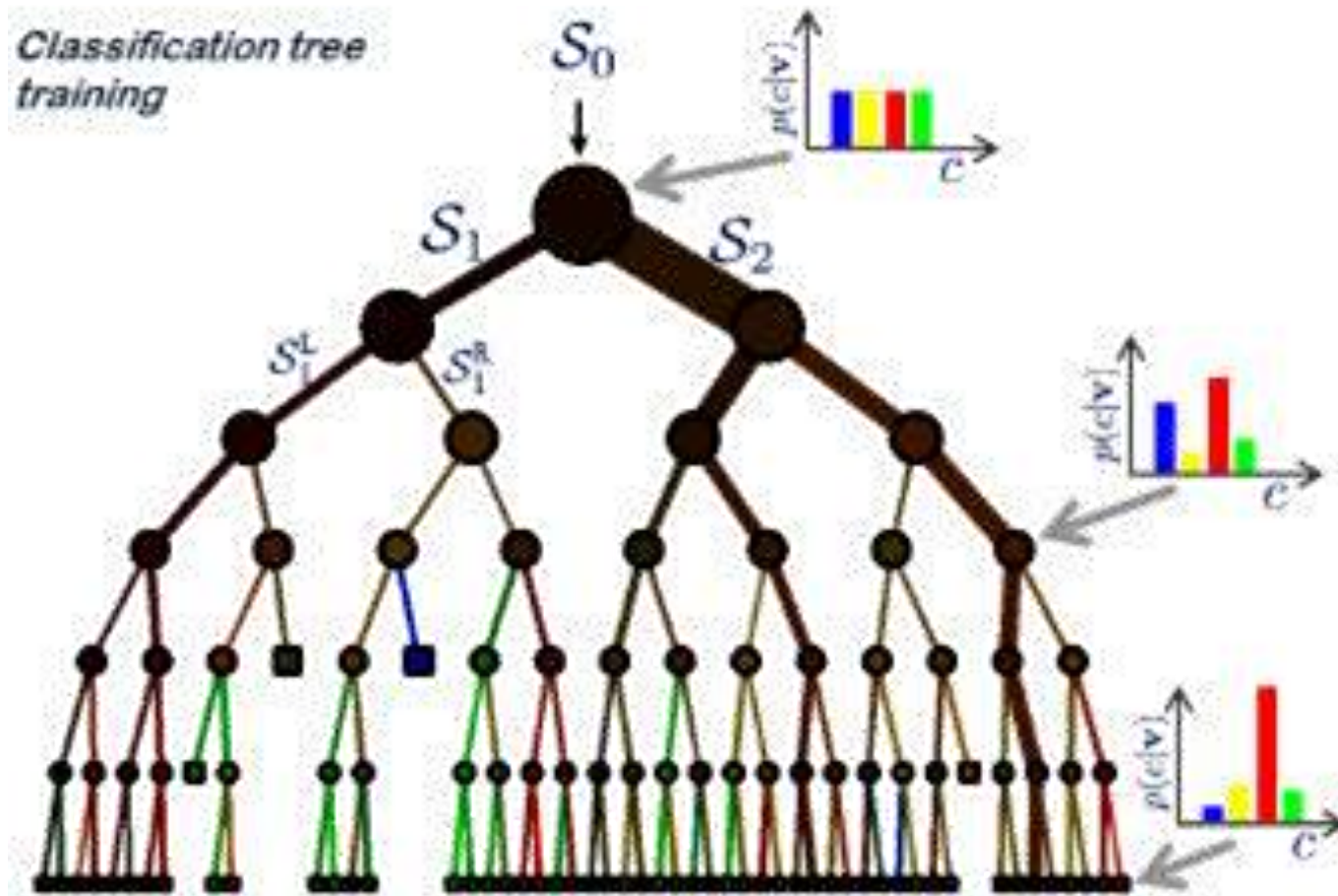


## Step 4: Stopping Criteria



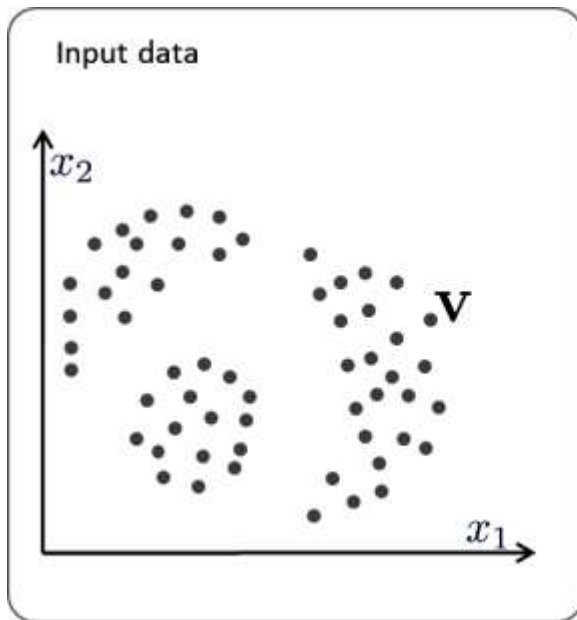


# Step 5: Leaf Prediction Model

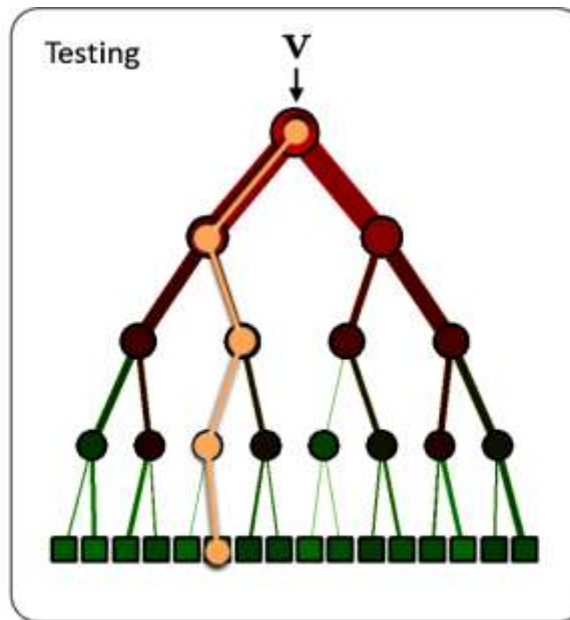




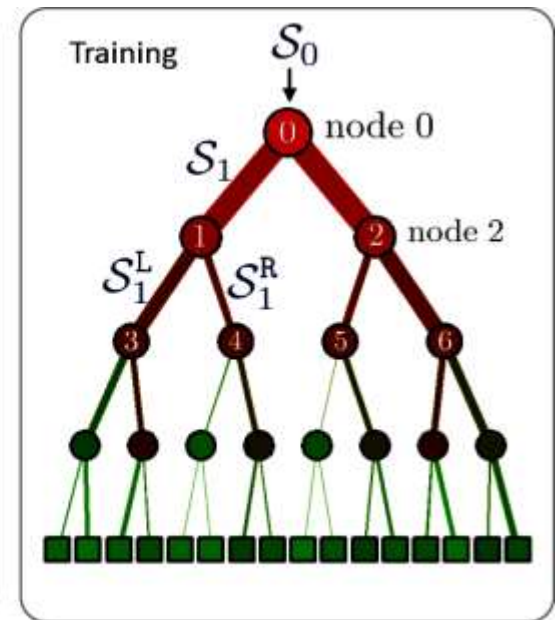
# Deploying a Decision Tree



(a)



(b)



(c)



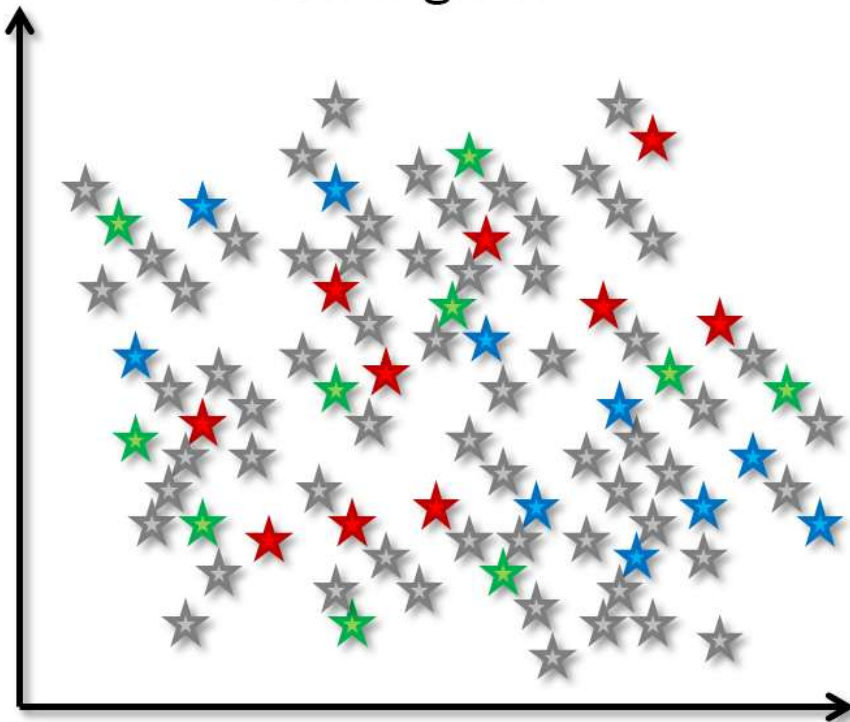
# RANDOM FOREST



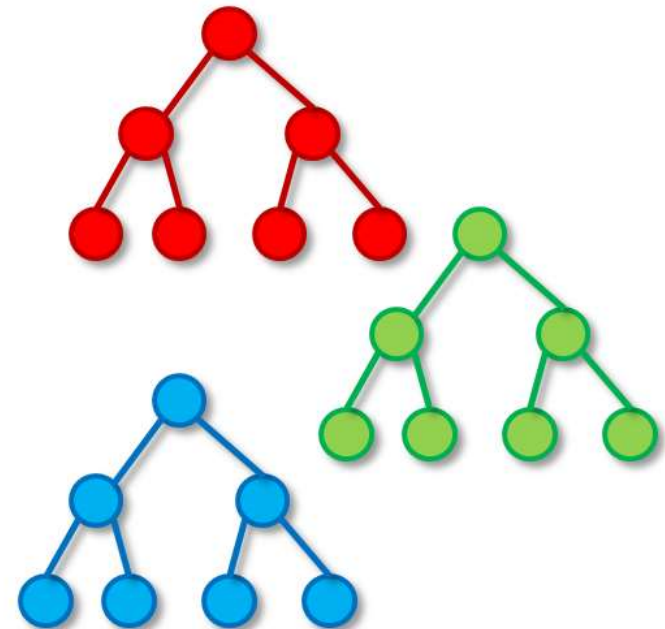


# Growing Multiple Trees in a Forest

Training set



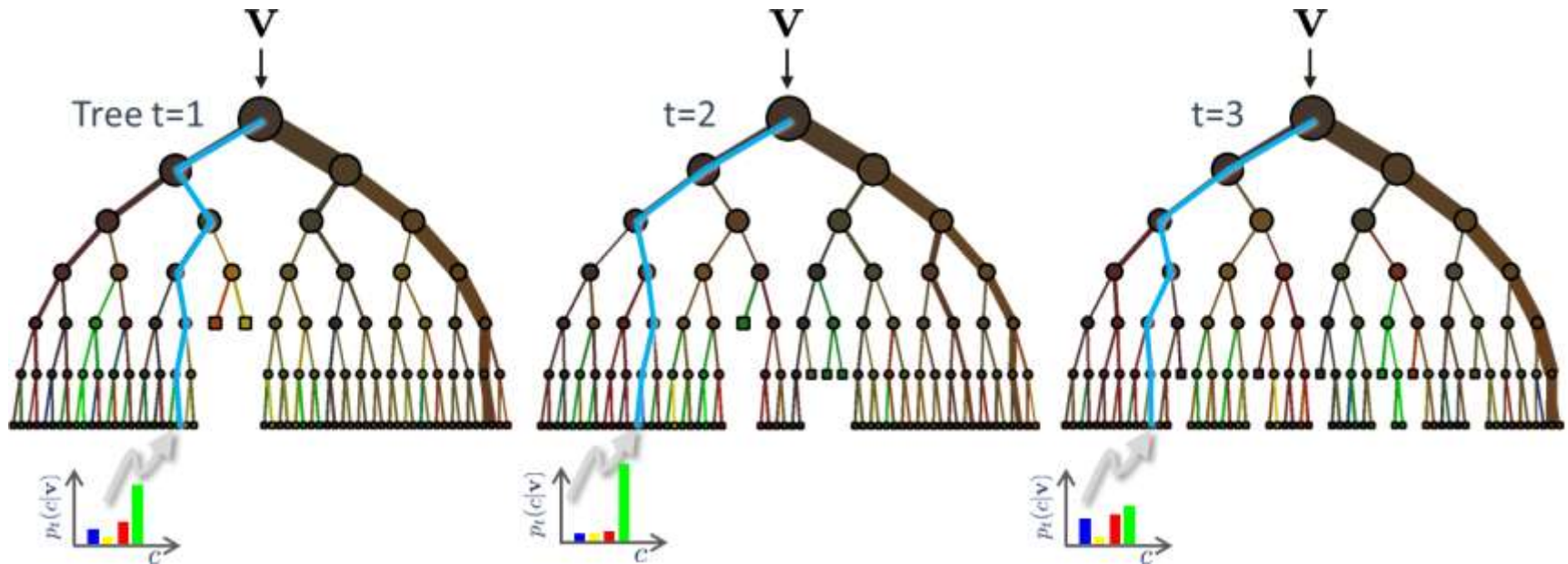
Decorrelated trees



Bagging – Bootstrapped Aggregation



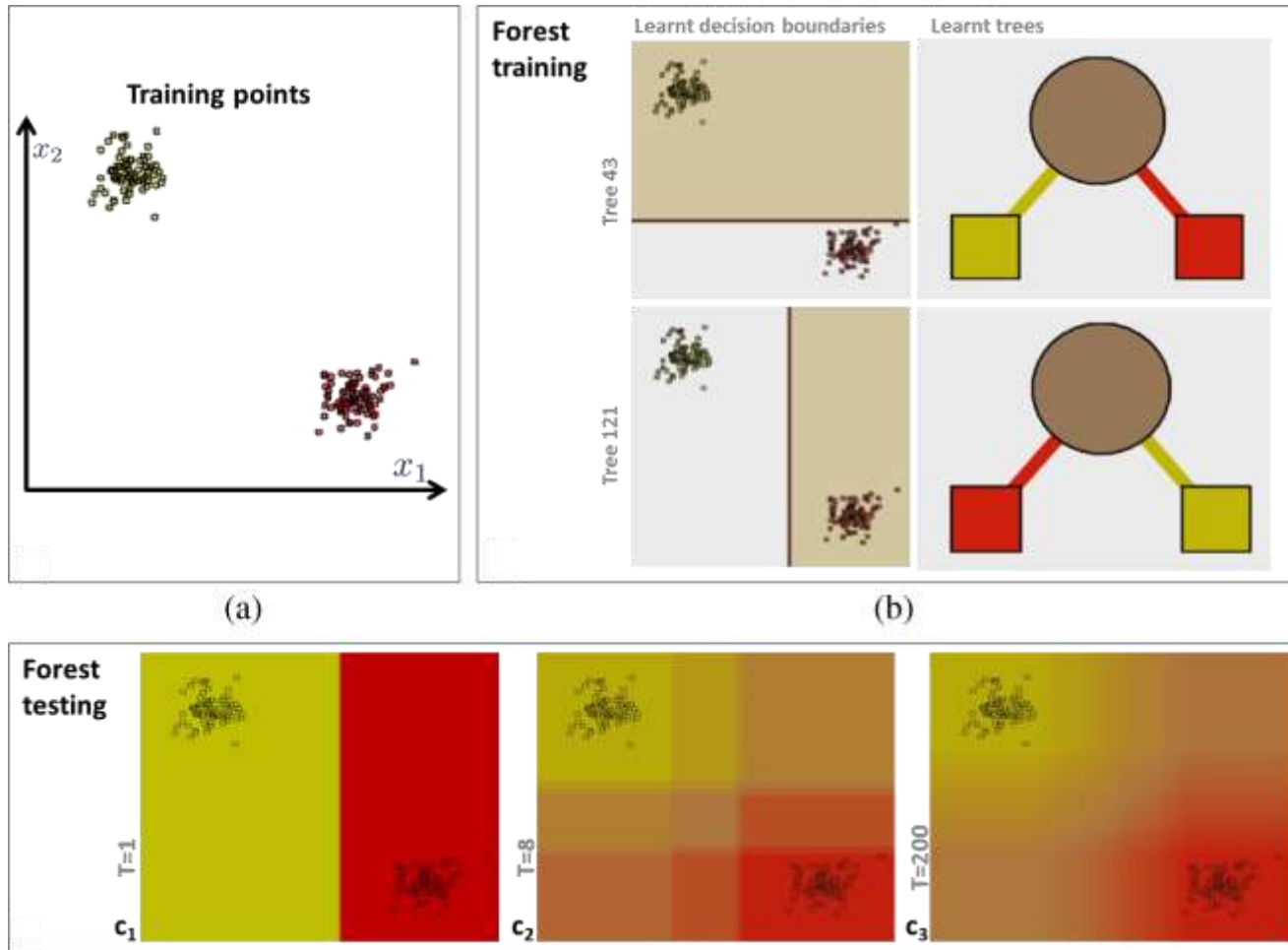
# Ensemble Prediction Model



$$p(c|\mathbf{v}) = \frac{1}{T} \sum_t^T p_t(c|\mathbf{v})$$

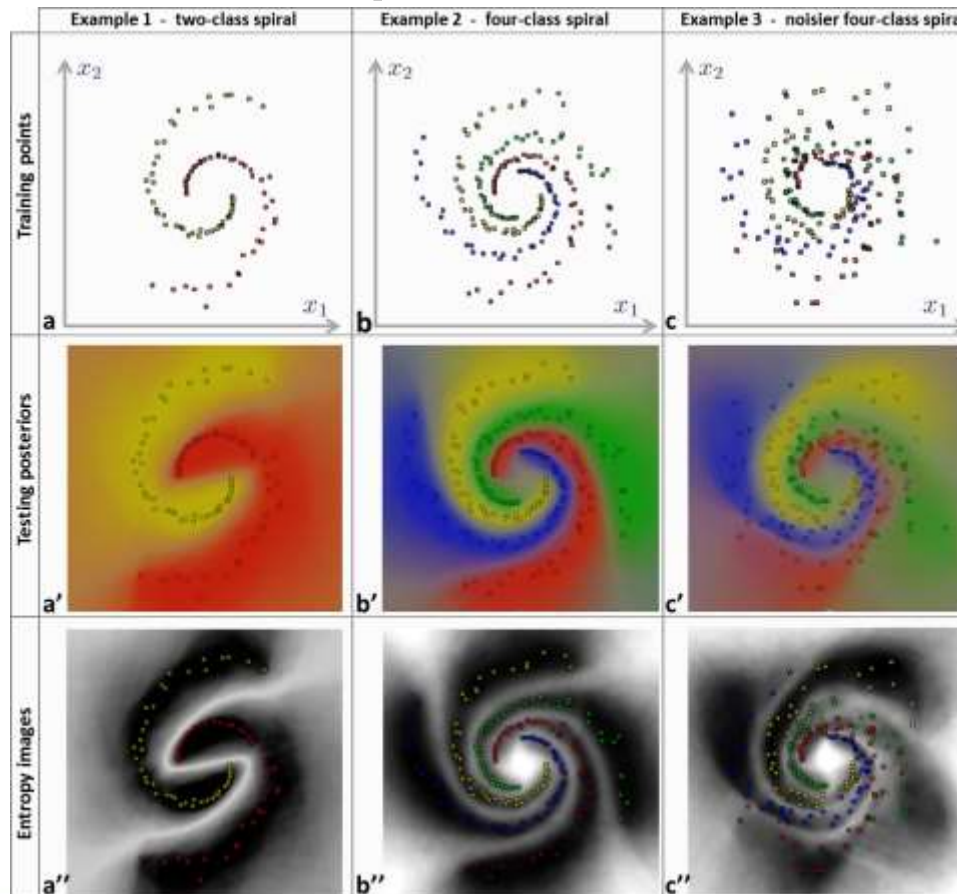


# What do we gain by using a Forest?





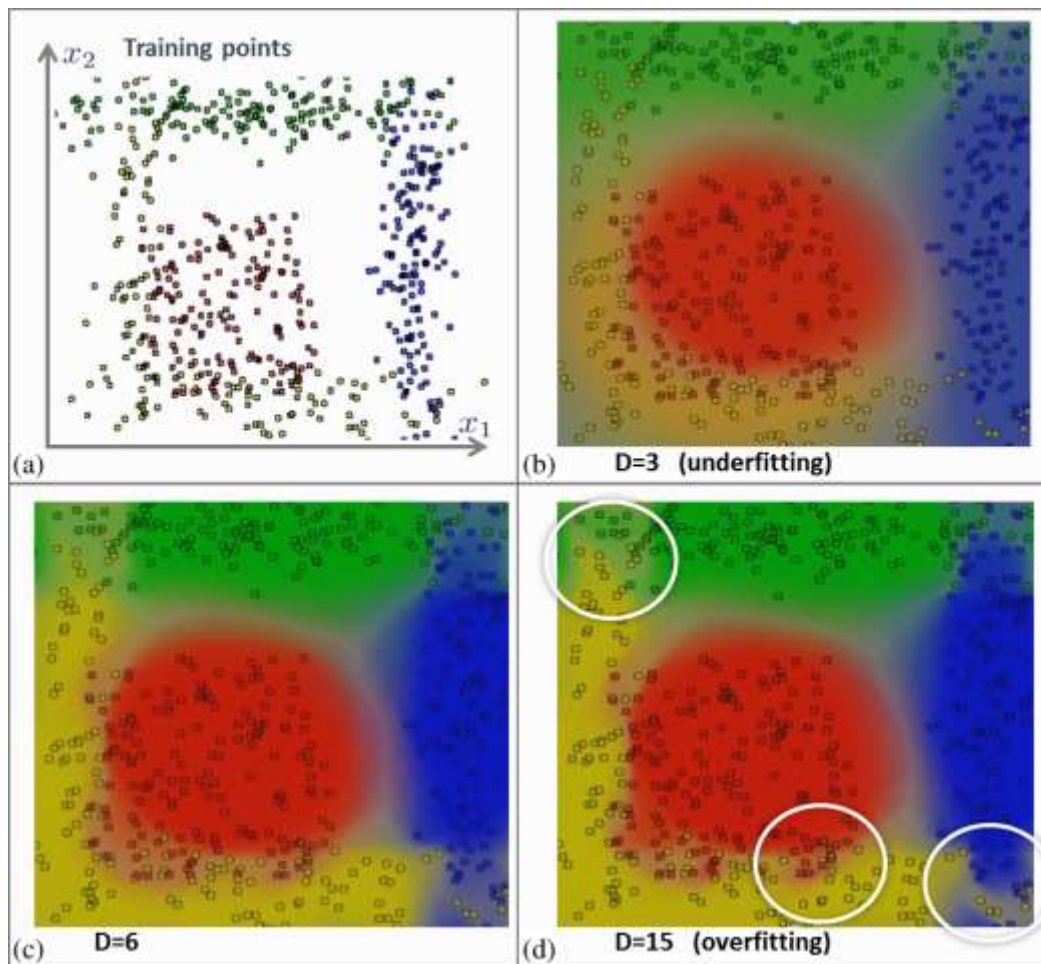
# Noise Resilience and Topology Independence







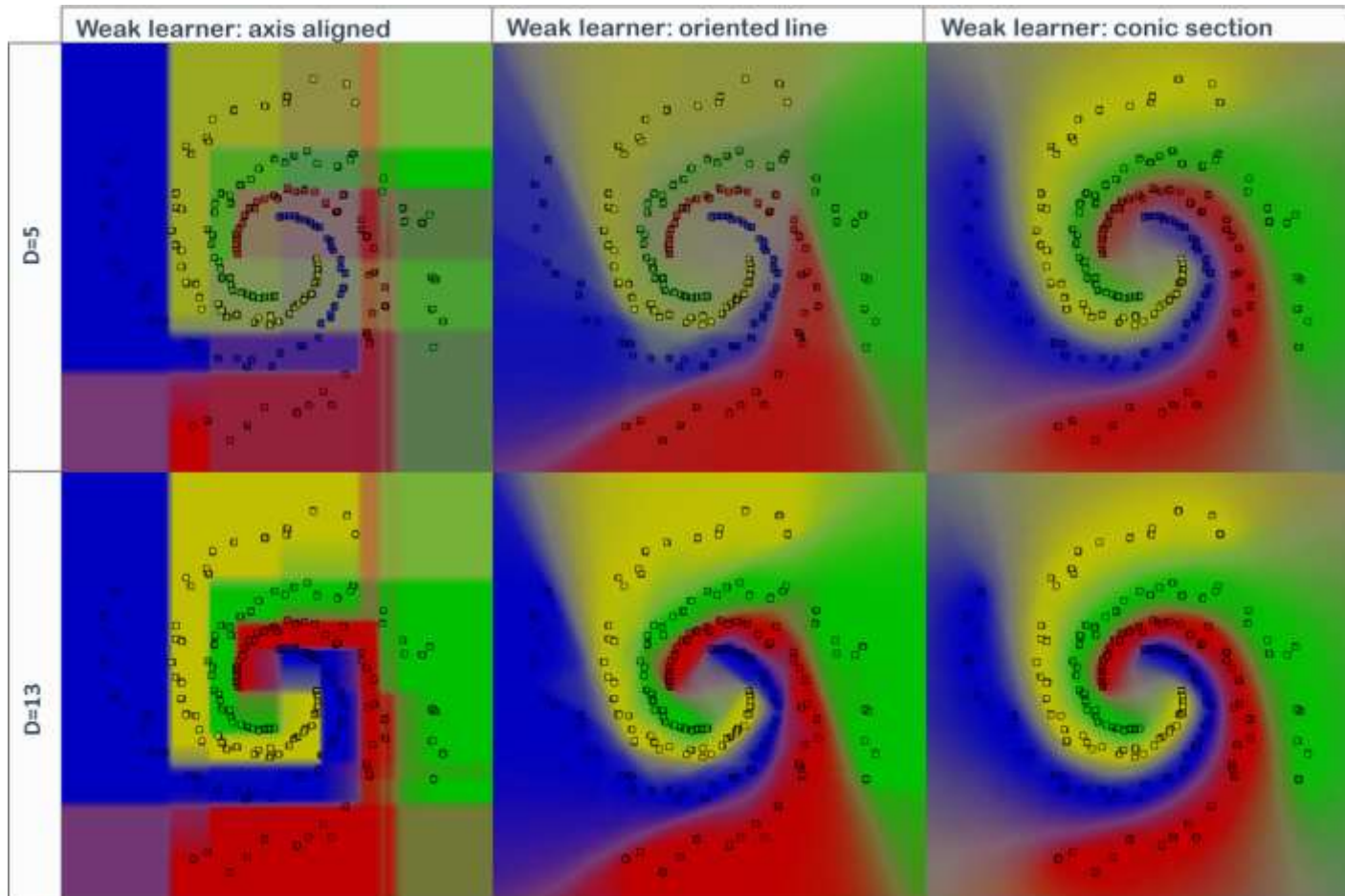
# Effect of Tree Depth





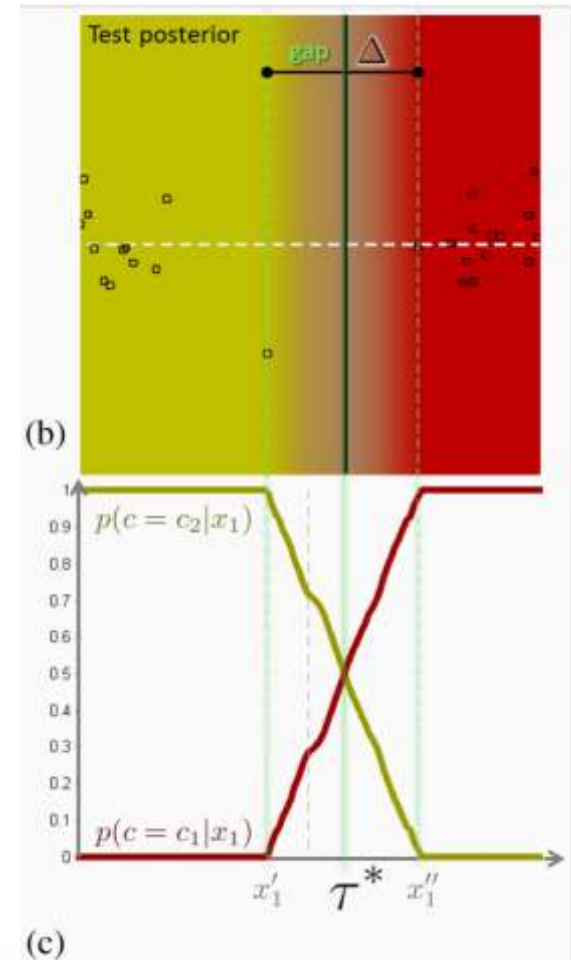
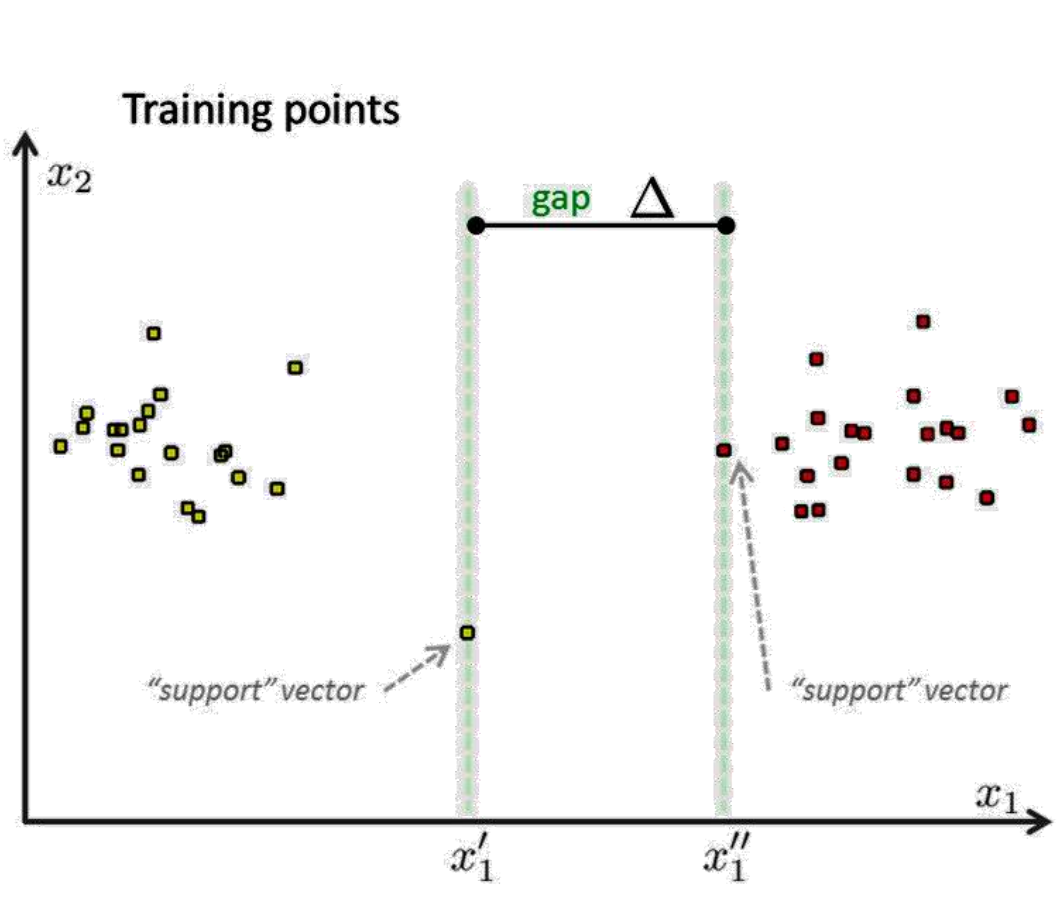


# Effect of Split Function



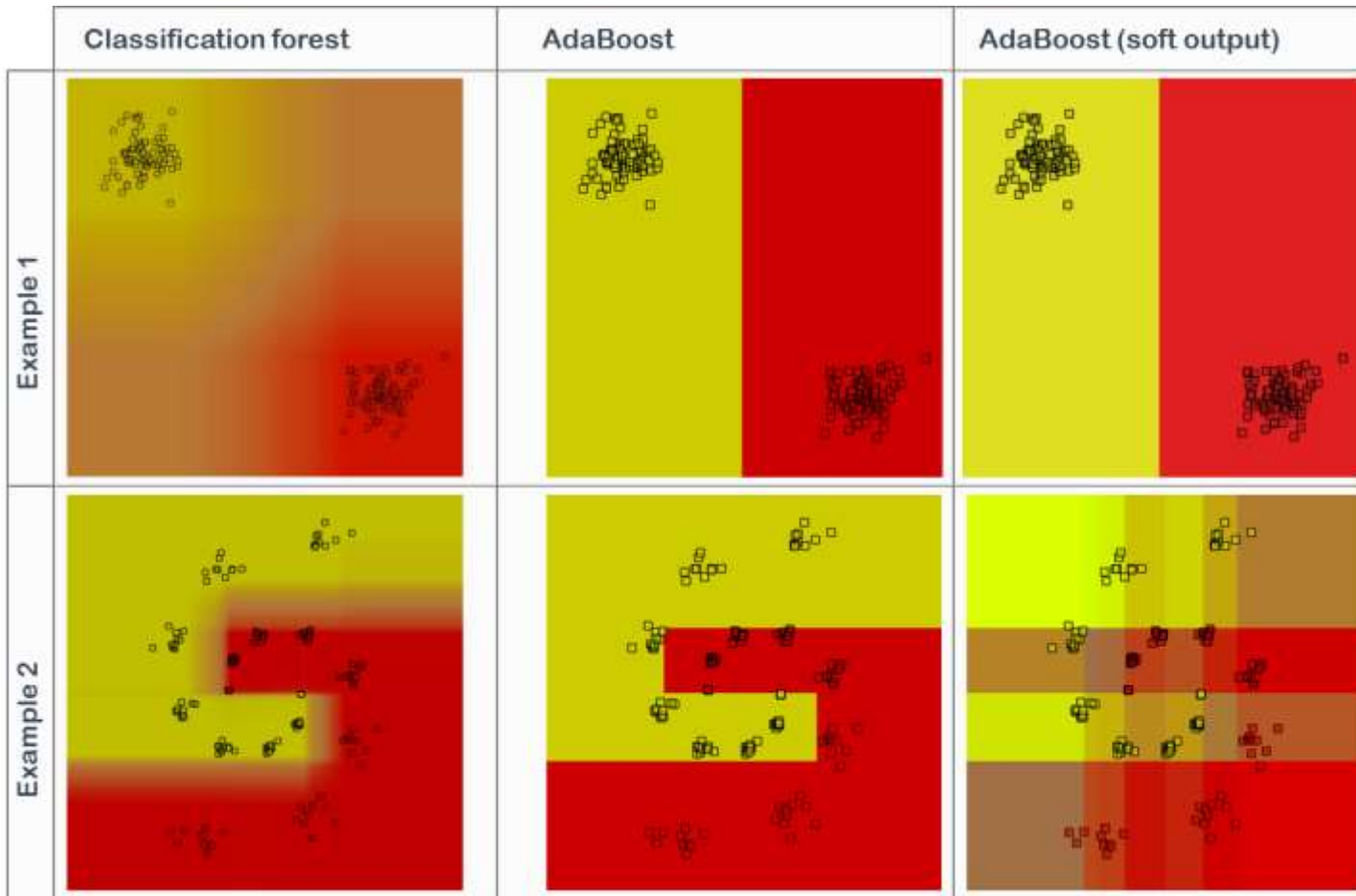


# Classification Margin



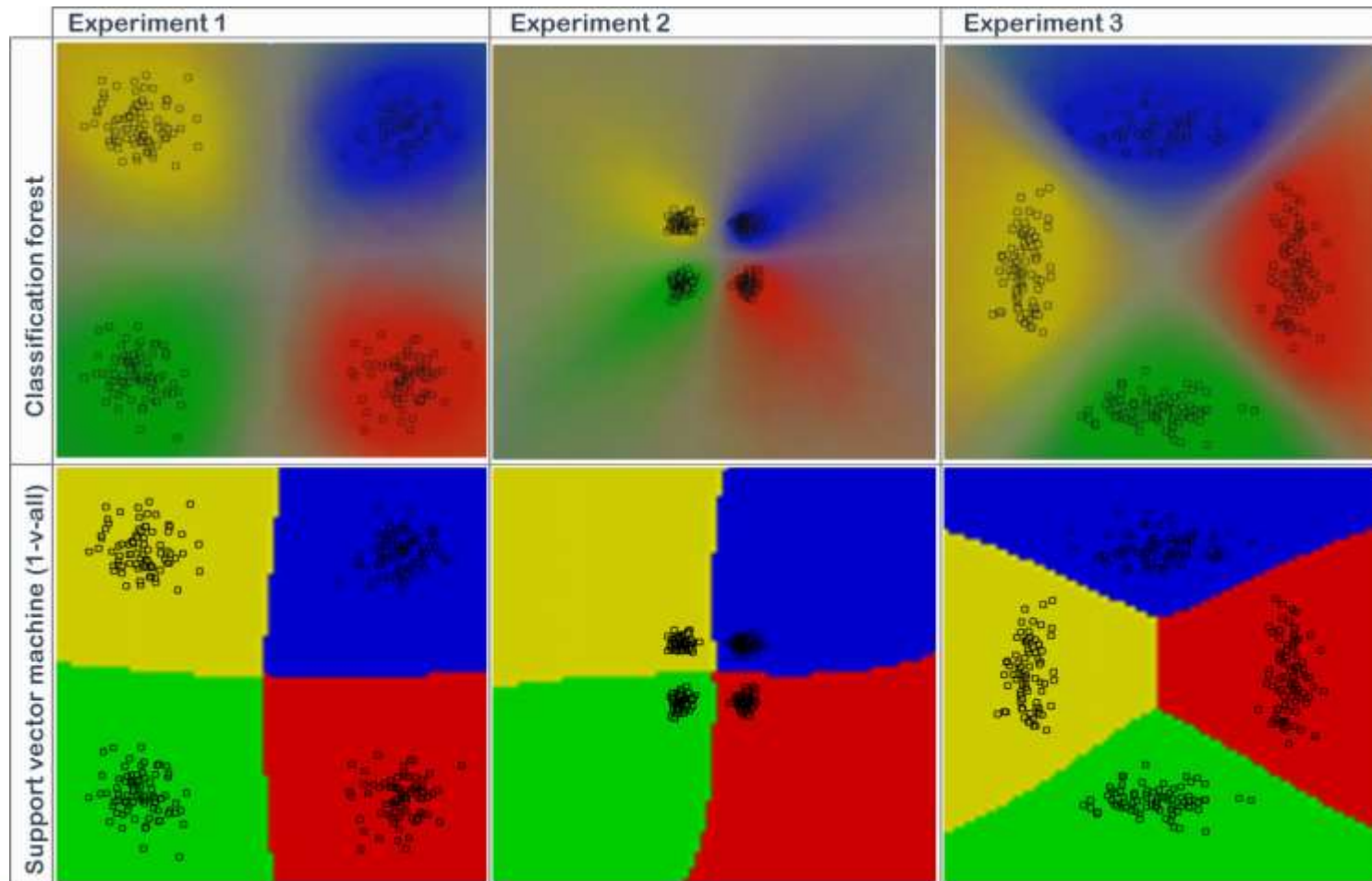


# Random Forest vs. AdaBoost



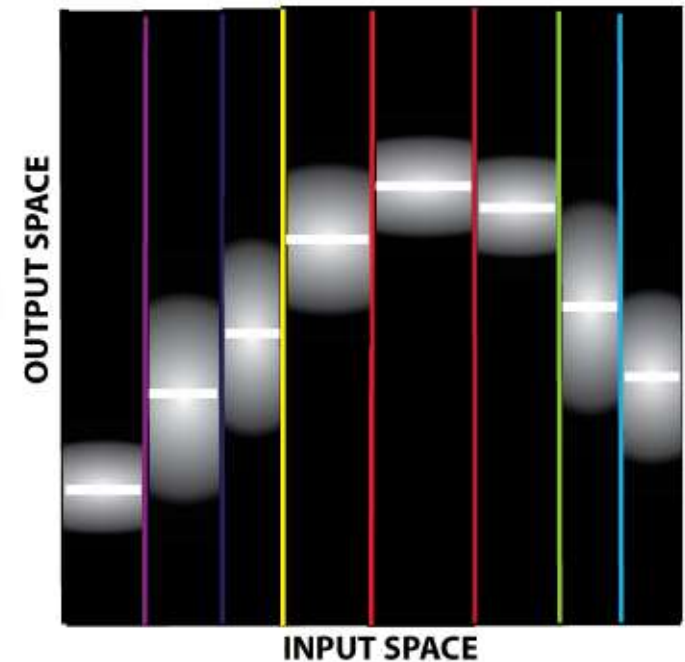
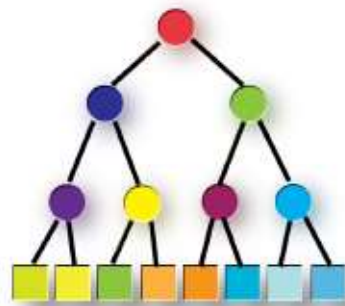
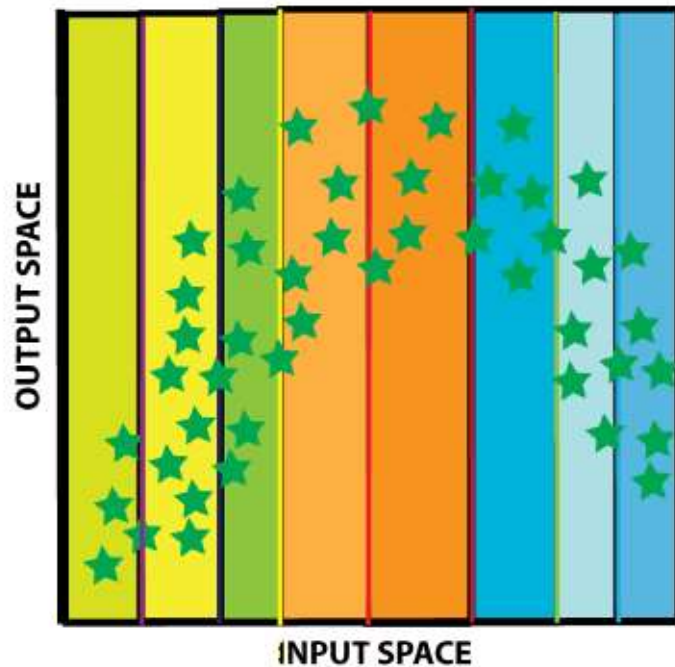


# Random Forest vs. SVM



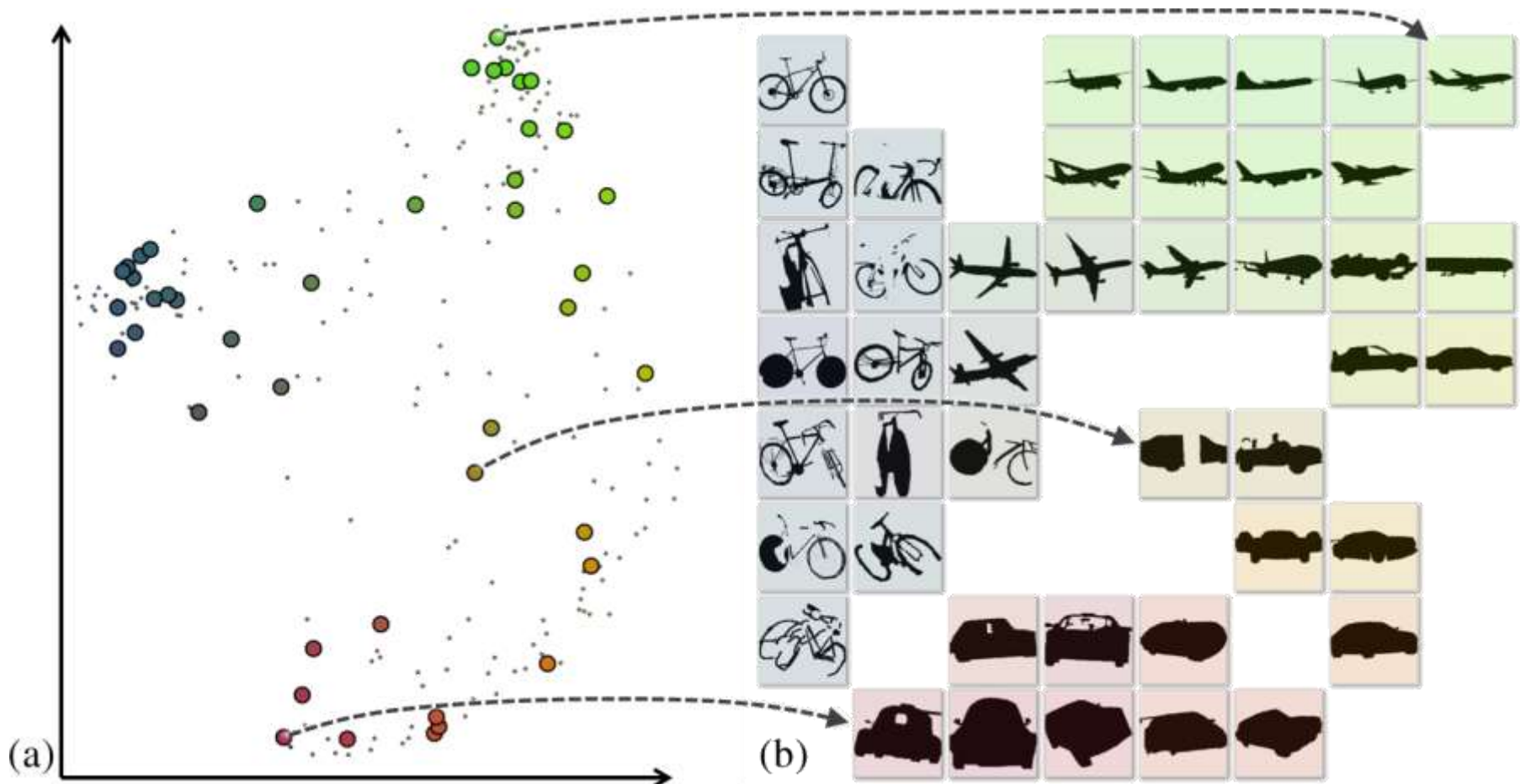


# Regression Forest





# Manifold Forest

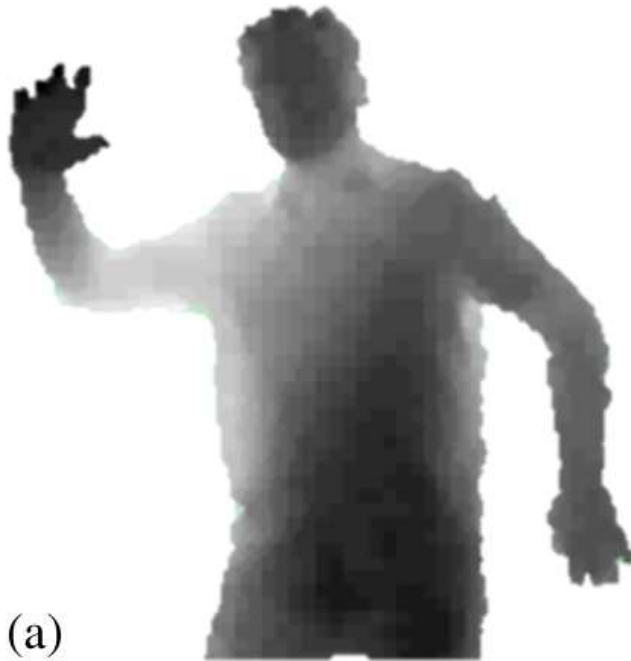




After the Brainstorming (Break)!

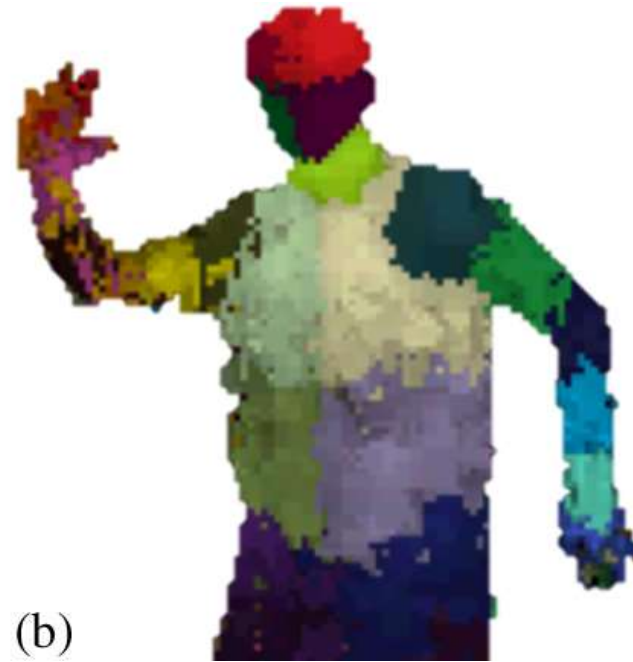
# APPLICATION SCENARIOS

# Gaming – Kinect for Xbox 360



(a)

Depth map



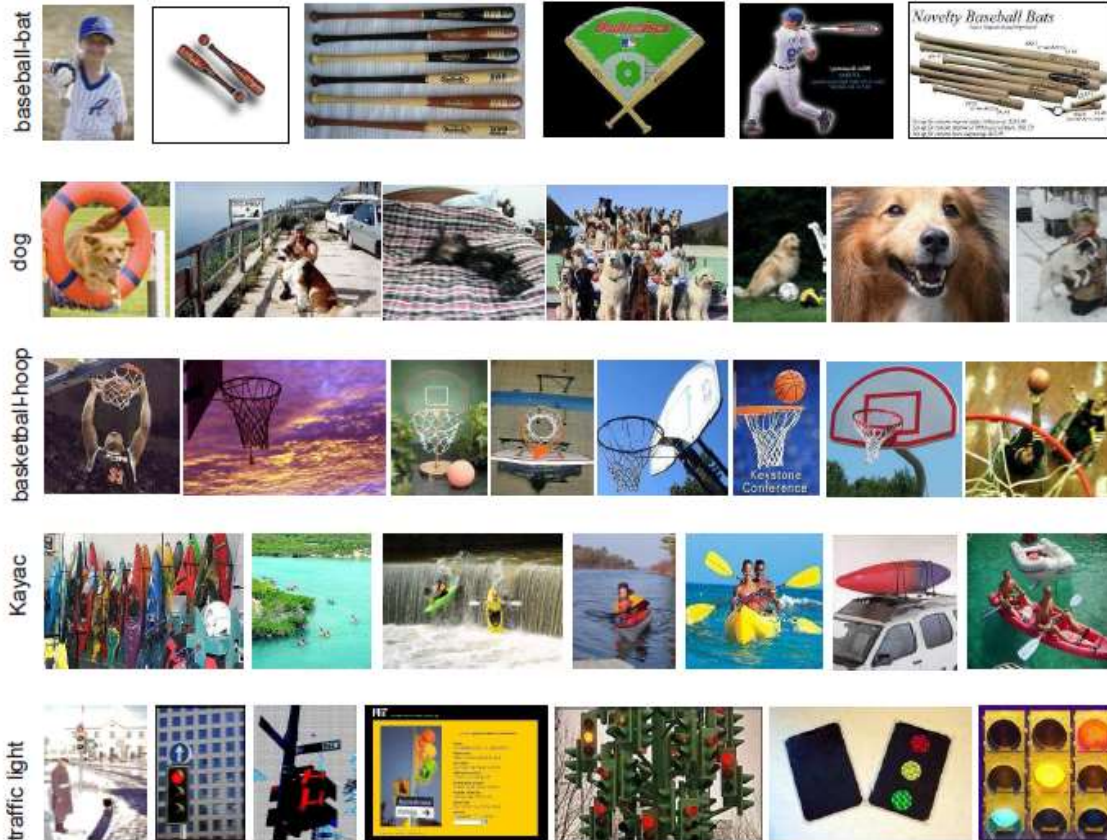
(b)

Body part classification

J. Shotton, A. Fitzgibbon, M. Cook, T. Sharp, M. Finocchio, R. Moore, A. Kipman, and A. Blake, "Real-time human pose recognition in parts from a single depth image," in *Proc. CVPR, 2011*.



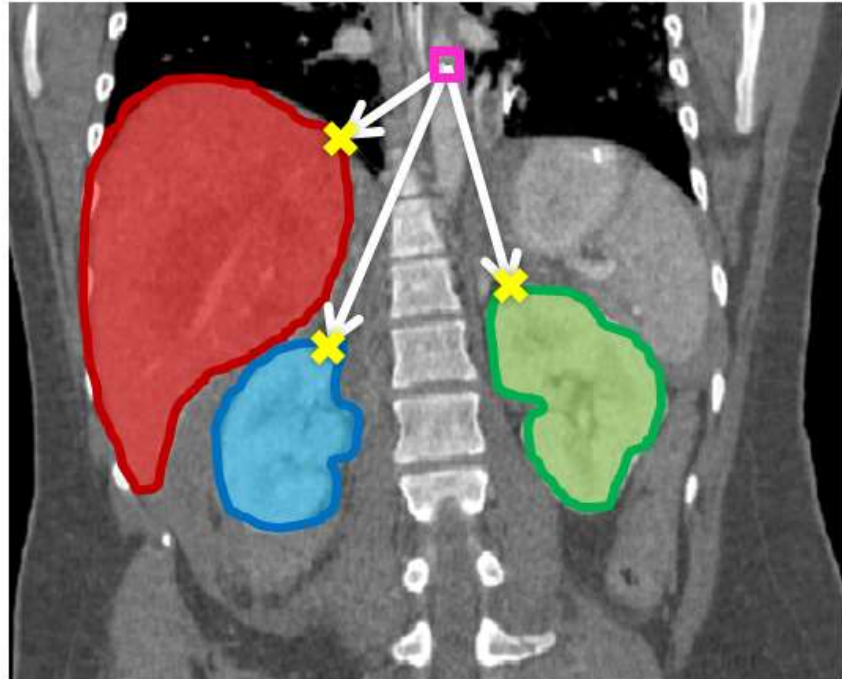
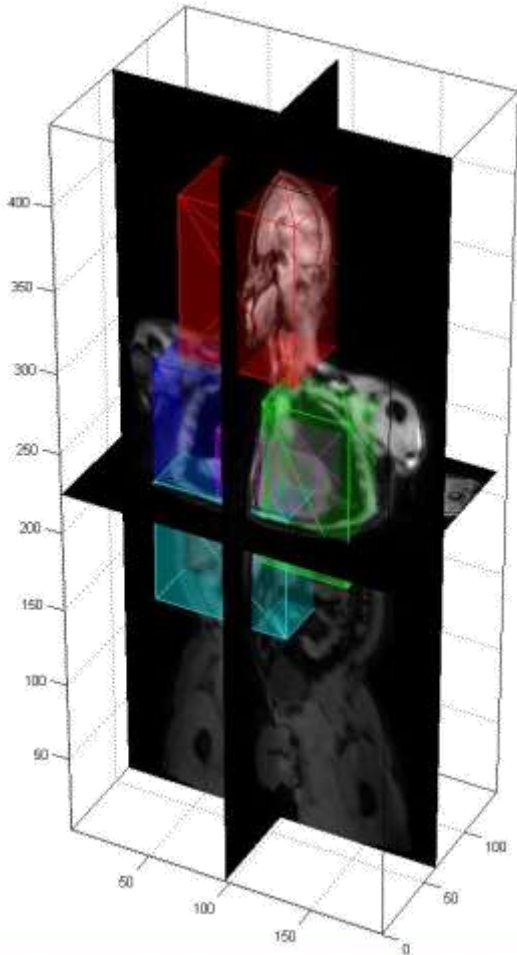
# Vision – Scene Classification



Bosch, A., Zisserman, A., & Muoz, X. "Image classification using random forests and ferns", *ICCV 2007*.



# Medical – Digital Anatomy



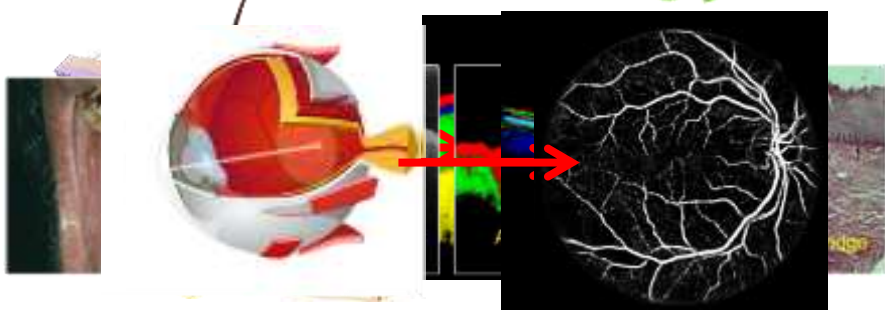
A. Criminisi, D. Robertson, E. Konukoglu, J. Shotton, S. Pathak, S. White, and K. Siddiqui, "Regression Forests for Efficient Anatomy Detection and Localization in Computed Tomography Scans", *Medical Image Analysis*, 2013





# Medical – Computational Histology

Physics  
MULTISCALE  
Tissue Photon  
MACHINE LEARNING  
DEEP LEARNING  
TISSUE ENERGY  
INTERACTION  
STATISTICS  
MODELLING



D. Sheet, et al., "Deriving histological tissue structure from optical coherence tomography and histology using deep learning", *Proc. SPIE 9183*, 91830A, 2014.  
D. Sheet, et al., "Transfer Learning of Tissue Photon Interaction in Optical Coherence Tomography towards In vivo Imaging for necrosis in the shadows of histology of the Oral Mucosa", *Proc. SPIE 9183*, 91830A, 2014.

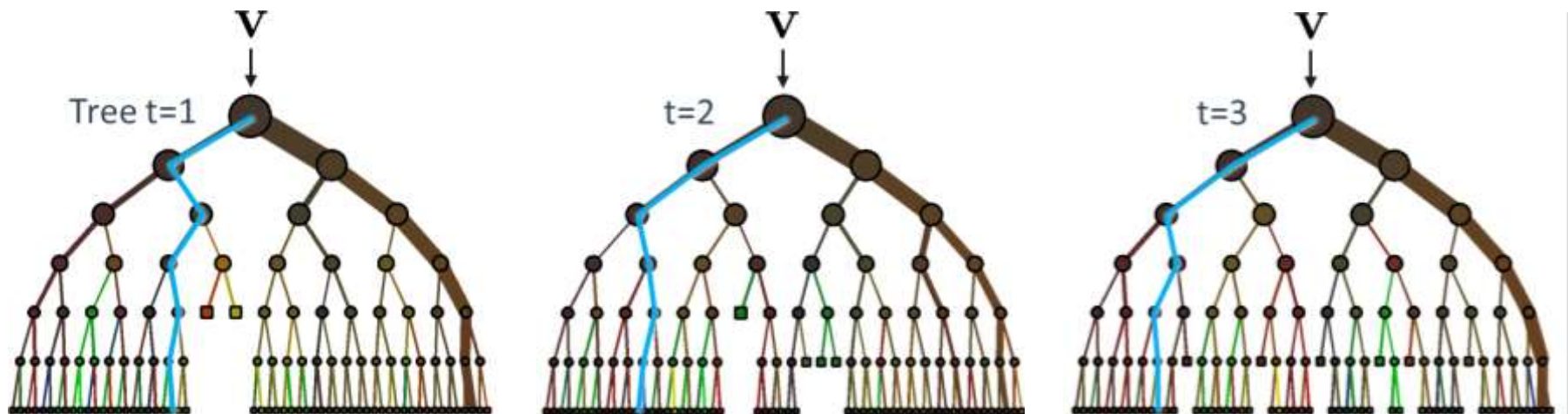
D. Sheet, et al., "Transfer Learning of Tissue Photon Interaction in Optical Coherence Tomography towards In vivo Imaging for necrosis in the shadows of histology of the Oral Mucosa", *Proc. SPIE 9183*, 91830A, 2014.  
SPK Kamri and D. Sheet, et al., "Deep Learnt Reconstruction of Histology of Retina through Transfer Learning of Tissue Photon Interaction in Optical Coherence Tomography with virtual histology", *IEEE TBME*, 59(11), 2012.



# ENGINEERING DESIGN PERSPECTIVE



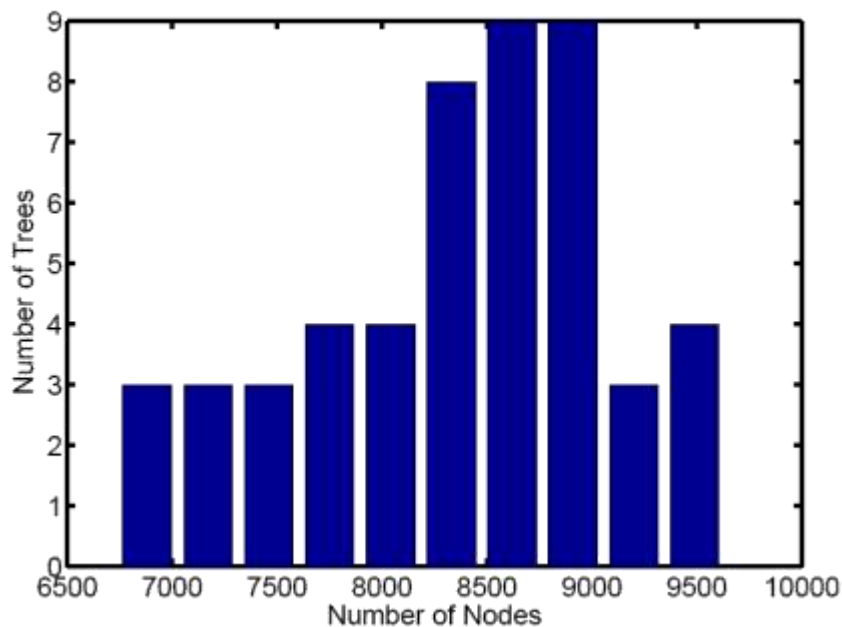
# Understanding Computations



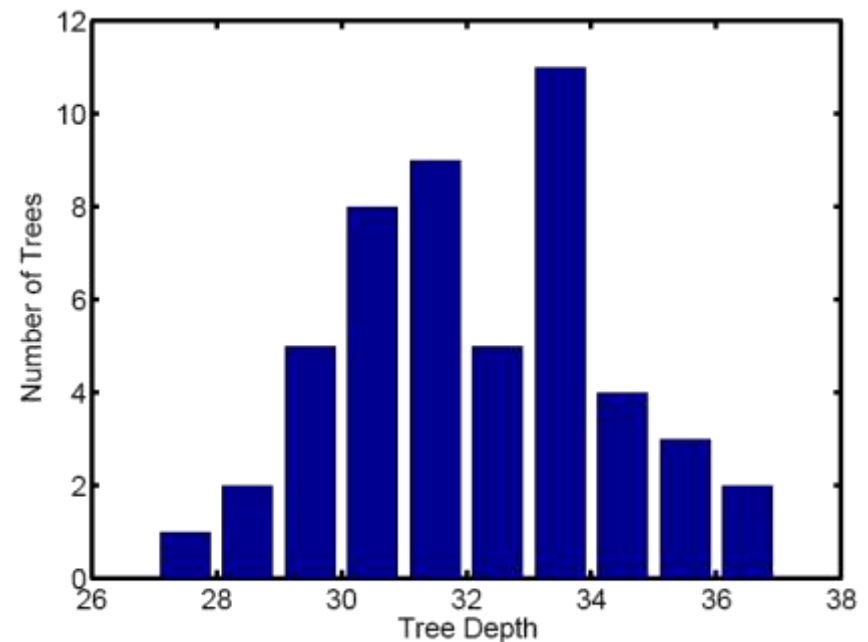


# Computational Complexity

## Training Complexity



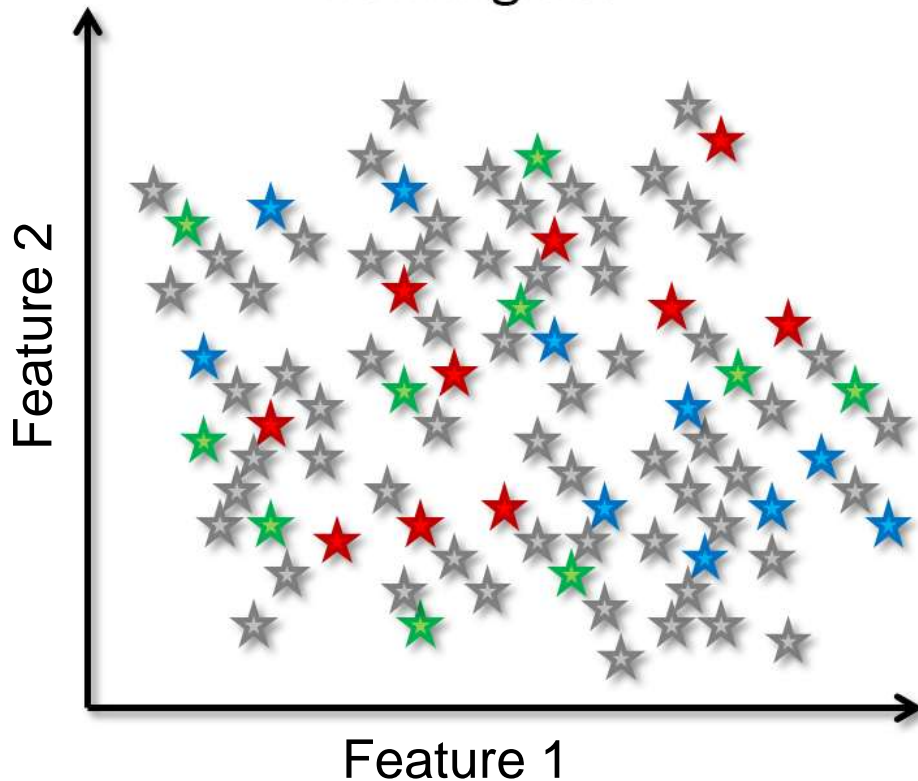
## Testing Complexity



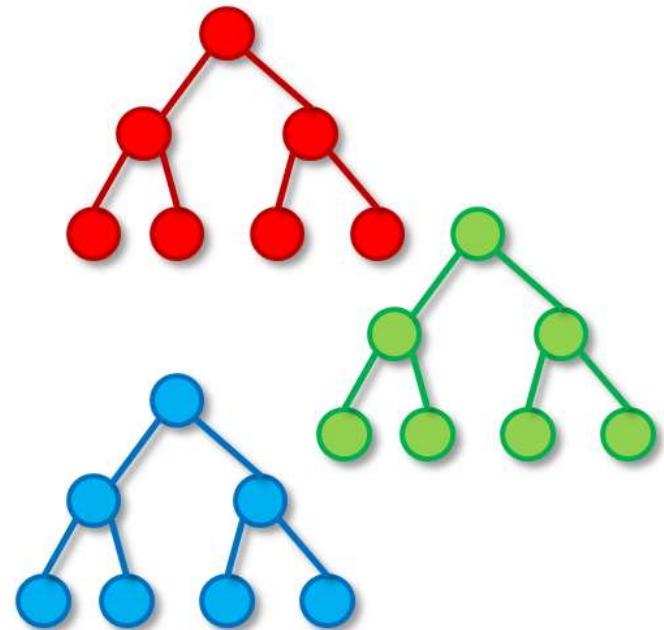


# Features and their Role

Training set



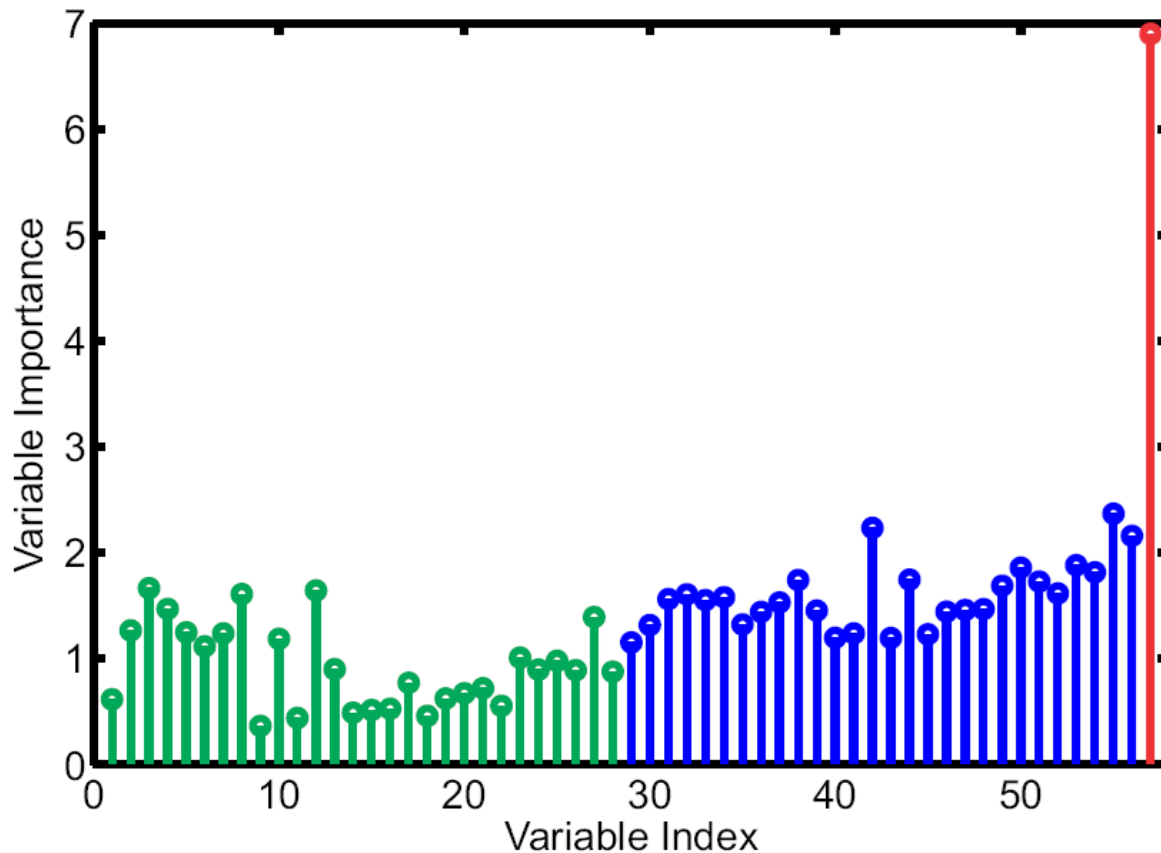
Decorrelated trees







# Variable Importance



Genuer, R., Poggi, J.-M., Tuleau-Malot, C., (2010). Variable selection using random forests. *Pat. Recogn. Letters*. **31**(14):2225-2236



# WHAT'S HOT IN RESEARCH?



# Research Challenges in 2015

- Architecture
  - Online learning
  - Incremental learning
  - Long term memory
  - Parallel - distributed architectures
  - Split functions, cost functions, stopping criteria
  - Domain adaptation
- Engineering and Application
  - Computational complexity
- Statistics and Science
  - Consistency of forests
  - VC dimension
  - De-correlated trees



# Take Home Message

- Reading
  - L. Breiman, J. Friedman, C. J. Stone, and R. A. Olshen, *Classification and Regression Trees*. Chapman and Hall/CRC, 1984.
  - L. Breiman, "Random forests," *Machine Learning*, vol. 45, no. 1, pp. 5–32, 2001.
  - A. Criminisi and J. Shotton, *Decision Forests for Computer Vision and Medical Image Analysis*, Springer, 2013.
- Toolboxes and Packages
  - randomForest in [R](#)
  - TreeBagger in [Matlab](#)
  - sklearn.ensemble.RandomForestClassifier in [Python-Scikit-learn](#)
- Conferences
  - Int. Conf. Comp. Vis. (ICCV)
  - Eur. Conf. Comp. Vis. (ECCV)
  - Asian Conf. Comp. Vis. (ACCV)
  - Comp. Vis. Patt. Recog. (CVPR)
  - Med. Image Comp., Comp. Assist. Interv. (MICCAI)