

# Understanding Electric Flux

# What is Electric Flux?

- Electric flux is a measure of the electric field passing through a surface.
- It is calculated as the product of the electric field and the area of the surface.
- The formula is:  $\Phi = E \times A \times \cos(\varphi)$

# Understanding the Components

- $E$  represents the electric field strength.
- $A$  is the area of the surface.
- $\phi$  is the angle between the electric field and the normal to the surface.

# Electric Field Perpendicular to Surface

- When the electric field is perpendicular to the surface,  $\phi = 0^\circ$ .
- In this case,  $\cos(0^\circ) = 1$ , so  $\Phi = E \times A$ .
- This results in maximum electric flux.

# Electric Field at an Angle

- If the electric field is at an angle to the surface,  $\phi$  is not zero.
- The electric flux is then calculated as  $\Phi = E \times A \times \cos(\phi)$ .
- The angle  $\phi$  affects the amount of flux passing through the surface.

# Electric Field Parallel to Surface

- When the electric field is parallel to the surface,  $\phi = 90^\circ$ .
- In this case,  $\cos(90^\circ) = 0$ , resulting in zero electric flux.
- No electric field lines pass through the surface.

## Example Problem: Sphere with Charges

- Consider a sphere of radius 4 meters with a  $50\text{ }\mu\text{C}$  charge at its center.
- The electric flux through the sphere can be calculated using Gauss's Law.
- The formula is:  $\Phi = Q_{\text{enc}} / \epsilon_0$ , where  $Q_{\text{enc}}$  is the enclosed charge.

# Calculating Electric Flux for the Sphere

- For the sphere with a positive and negative charge, the total enclosed charge is zero.
- Thus, the electric flux through the sphere is also zero.
- This illustrates the concept of electric flux in closed surfaces.



# Gauss's Law Overview

- Gauss's Law states that the electric flux through a closed surface is proportional to the charge enclosed.
- Mathematically:  $\Phi = Q_{\text{enc}} / \epsilon_0$ .
- This law simplifies the calculation of electric flux in complex situations.

## Example Problem: Horizontal Disk

- Consider a horizontal disk with an electric field at an angle of  $30^\circ$ .
- The electric flux can be calculated using the formula:  $\Phi = E \times A \times \cos(\varphi)$ .
- Here,  $\varphi$  is the complementary angle to the angle of the electric field.

# Calculating Electric Flux for the Disk

- The area of the disk is  $A = \pi r^2$ , where  $r$  is the radius.
- Substitute values to find the electric flux.
- This example demonstrates the application of electric flux in real scenarios.

# Electric Flux through a Cube

- When a positive charge is placed at the center of a cube, the total electric flux can be calculated.
- Use Gauss's Law:  $\Phi = Q_{\text{enc}} / \epsilon_0$ .
- This approach simplifies the calculation without needing to analyze each face of the cube.

# Electric Flux through Cube Faces

- To find the flux through one face of the cube, divide the total flux by 6.
- Each face experiences the same amount of flux due to symmetry.
- This is a practical application of Gauss's Law.

# Electric Flux with No Charge

- If there is no charge inside a closed surface, the total electric flux is zero.
- This is consistent with Gauss's Law:  $\Phi = Q_{\text{enc}} / \epsilon_0$ , where  $Q_{\text{enc}} = 0$ .
- The flux entering equals the flux leaving the surface.

# Summary of Key Concepts

- Electric flux is a measure of the electric field through a surface.
- It depends on the electric field strength, area, and angle.
- Gauss's Law provides a powerful tool for calculating electric flux.

# Conclusion

- Understanding electric flux is crucial in electromagnetism.
- It helps in analyzing electric fields and their effects on surfaces.
- Thank you for your attention! Any questions?